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 $T(i): \mathbb{R} \rightarrow \mathbb{Z}$ 
  return ( $\lfloor 0x100000000 \cdot \sin(i) \rfloor$ )

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 $F(i, x, y, z): \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z} \rightarrow \mathbb{Z}$ 
  if  $i < 16$  then
    return  $((x \wedge y) \vee (\neg x \wedge z))$ 
  else if  $i < 32$  then
    return  $((x \wedge z) \vee (y \wedge \neg z))$ 
  else if  $i < 48$  then
    return  $(x \oplus y \oplus z)$ 
  else if  $i < 64$  then
    return  $(y \oplus (x \vee \neg z))$ 
  end if

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*"Circular shift of a number"*

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 $rol(val, s): \mathbb{Z}, \mathbb{Z} \rightarrow \mathbb{Z}$ 
   $r \in \mathbb{Z}$ 
   $r^{[0]} \leftarrow val$ 
   $r^{[i]} \leftarrow (r^{[i-1]} \ll 1) + ((r^{[i-1]} \wedge 0x80000000) \gg 31)$ 
  return  $(r^{[s]})$ 

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 $P(a, b, c, d, k, s, i, W, X): \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}_4^1, \mathbb{Z}_{16}^1 \rightarrow \mathbb{Z}_4^1$ 
   $r \in \mathbb{Z}$ 
   $tmp \leftarrow W_a + X_k + T(i + 1) + F(i, W_b, W_c, W_d)$ 
   $W_a \leftarrow (W_b + rol(tmp, s)) \wedge 0xFFFFFFFF$ 
  return  $(W)$ 

```

*"Transform a byte array with 64 elements into a 4 byte array with 16 elements"*

$transform(a): \mathbb{Z}_{64}^1 \rightarrow \mathbb{Z}_{16}^1$   
 $r \in \mathbb{Z}_{16}^1$   
 $r_i \mid \forall i \leftarrow a_{4 \cdot i}$   
 $r_i \mid \forall i \leftarrow r_i + (a_{4 \cdot i + 1} \ll 8)$   
 $r_i \mid \forall i \leftarrow r_i + (a_{4 \cdot i + 2} \ll 16)$   
 $r_i \mid \forall i \leftarrow r_i + (a_{4 \cdot i + 3} \ll 24)$   
**return** ( $r$ )

$transform\_back(a): \mathbb{Z}_4^1 \rightarrow \mathbb{Z}_{16}^1$   
 $r \in \mathbb{Z}_{16}^1$   
 $r_i \mid \forall i \leftarrow \begin{cases} (a_{\lfloor \frac{i}{4} \rfloor} \wedge 0xFF000000) \gg 24 & i : i \bmod 4 = 3 \\ (a_{\lfloor \frac{i}{4} \rfloor} \wedge 0x00FF0000) \gg 16 & i : i \bmod 4 = 2 \\ (a_{\lfloor \frac{i}{4} \rfloor} \wedge 0x0000FF00) \gg 8 & i : i \bmod 4 = 1 \\ (a_{\lfloor \frac{i}{4} \rfloor} \wedge 0x000000FF) & \textbf{otherwise} \end{cases}$   
**return** ( $r$ )

$process(A): \mathbb{Z}_{64}^1 \rightarrow \mathbb{Z}_{16}^1$

$$W \leftarrow \begin{pmatrix} 0x67452301 \\ 0xEFCDAB89 \\ 0x98BADCFE \\ 0x10325476 \end{pmatrix}$$

$Q \leftarrow list(W)$

$X \leftarrow transform(A)$

$W \leftarrow P(0, 1, 2, 3, 0, 7, 0, W, X); \quad W \leftarrow P(3, 0, 1, 2, 1, 12, 1, W, X)$

$W \leftarrow P(2, 3, 0, 1, 2, 17, 2, W, X); \quad W \leftarrow P(1, 2, 3, 0, 3, 22, 3, W, X)$

$W \leftarrow P(0, 1, 2, 3, 4, 7, 4, W, X); \quad W \leftarrow P(3, 0, 1, 2, 5, 12, 5, W, X)$

$W \leftarrow P(2, 3, 0, 1, 6, 17, 6, W, X); \quad W \leftarrow P(1, 2, 3, 0, 7, 22, 7, W, X)$

$W \leftarrow P(0, 1, 2, 3, 8, 7, 8, W, X); \quad W \leftarrow P(3, 0, 1, 2, 9, 12, 9, W, X)$

$W \leftarrow P(2, 3, 0, 1, 10, 17, 10, W, X); \quad W \leftarrow P(1, 2, 3, 0, 11, 22, 11, W, X)$

$W \leftarrow P(0, 1, 2, 3, 12, 7, 12, W, X); \quad W \leftarrow P(3, 0, 1, 2, 13, 12, 13, W, X)$

$W \leftarrow P(2, 3, 0, 1, 14, 17, 14, W, X); \quad W \leftarrow P(1, 2, 3, 0, 15, 22, 15, W, X)$

$W \leftarrow P(0, 1, 2, 3, 1, 5, 16, W, X); \quad W \leftarrow P(3, 0, 1, 2, 6, 9, 17, W, X)$

$W \leftarrow P(2, 3, 0, 1, 11, 14, 18, W, X); \quad W \leftarrow P(1, 2, 3, 0, 0, 20, 19, W, X)$

$W \leftarrow P(0, 1, 2, 3, 5, 5, 20, W, X); \quad W \leftarrow P(3, 0, 1, 2, 10, 9, 21, W, X)$

$W \leftarrow P(2, 3, 0, 1, 15, 14, 22, W, X); \quad W \leftarrow P(1, 2, 3, 0, 4, 20, 23, W, X)$

$W \leftarrow P(0, 1, 2, 3, 9, 5, 24, W, X); \quad W \leftarrow P(3, 0, 1, 2, 14, 9, 25, W, X)$

$W \leftarrow P(2, 3, 0, 1, 3, 14, 26, W, X); \quad W \leftarrow P(1, 2, 3, 0, 8, 20, 27, W, X)$

$W \leftarrow P(0, 1, 2, 3, 13, 5, 28, W, X); \quad W \leftarrow P(3, 0, 1, 2, 2, 9, 29, W, X)$

$W \leftarrow P(2, 3, 0, 1, 7, 14, 30, W, X); \quad W \leftarrow P(1, 2, 3, 0, 12, 20, 31, W, X)$

$W \leftarrow P(0, 1, 2, 3, 5, 4, 32, W, X); \quad W \leftarrow P(3, 0, 1, 2, 8, 11, 33, W, X)$

$W \leftarrow P(2, 3, 0, 1, 11, 16, 34, W, X); \quad W \leftarrow P(1, 2, 3, 0, 14, 23, 35, W, X)$

$W \leftarrow P(0, 1, 2, 3, 1, 4, 36, W, X); \quad W \leftarrow P(3, 0, 1, 2, 4, 11, 37, W, X)$

$W \leftarrow P(2, 3, 0, 1, 7, 16, 38, W, X); \quad W \leftarrow P(1, 2, 3, 0, 10, 23, 39, W, X)$

$W \leftarrow P(0, 1, 2, 3, 13, 4, 40, W, X); \quad W \leftarrow P(3, 0, 1, 2, 0, 11, 41, W, X)$

$W \leftarrow P(2, 3, 0, 1, 3, 16, 42, W, X); \quad W \leftarrow P(1, 2, 3, 0, 6, 23, 43, W, X)$

$W \leftarrow P(0, 1, 2, 3, 9, 4, 44, W, X); \quad W \leftarrow P(3, 0, 1, 2, 12, 11, 45, W, X)$

$W \leftarrow P(2, 3, 0, 1, 15, 16, 46, W, X); \quad W \leftarrow P(1, 2, 3, 0, 2, 23, 47, W, X)$

$W \leftarrow P(0, 1, 2, 3, 0, 6, 48, W, X); \quad W \leftarrow P(3, 0, 1, 2, 7, 10, 49, W, X)$

$W \leftarrow P(2, 3, 0, 1, 14, 15, 50, W, X); \quad W \leftarrow P(1, 2, 3, 0, 5, 21, 51, W, X)$

$W \leftarrow P(0, 1, 2, 3, 12, 6, 52, W, X); \quad W \leftarrow P(3, 0, 1, 2, 3, 10, 53, W, X)$

$W \leftarrow P(2, 3, 0, 1, 10, 15, 54, W, X); \quad W \leftarrow P(1, 2, 3, 0, 1, 21, 55, W, X)$

$W \leftarrow P(0, 1, 2, 3, 8, 6, 56, W, X); \quad W \leftarrow P(3, 0, 1, 2, 15, 10, 57, W, X)$

$W \leftarrow P(2, 3, 0, 1, 6, 15, 58, W, X); \quad W \leftarrow P(1, 2, 3, 0, 13, 21, 59, W, X)$

$W \leftarrow P(0, 1, 2, 3, 4, 6, 60, W, X); \quad W \leftarrow P(3, 0, 1, 2, 11, 10, 61, W, X)$

$W \leftarrow P(2, 3, 0, 1, 2, 15, 62, W, X); \quad W \leftarrow \frac{1}{3} P(1, 2, 3, 0, 9, 21, 63, W, X)$

$W \leftarrow W + Q$

**return** ( $transform\_back(W)$ )

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divide(w):  $\mathbb{Z}^1 \rightarrow \mathbb{Z}_{64}^1$ 
  ret  $\in \mathbb{Z}_{64}^1$ 
   $ret_i | \forall i \leftarrow \begin{cases} w_i & i : i < len(w) \\ 0x80 & i : i = len(w) \\ 8 \cdot len(w) & i : i = 56 \\ 0 & \text{otherwise} \end{cases}$ 
  return (ret)

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 $\mu( ) : \rightarrow \mathbb{Z}_{16}^1$ 
  "An input string stored as a vector, where symbols are ASCII numbers"
   $w \leftarrow \begin{pmatrix} 97 \\ 98 \\ 99 \\ 100 \\ 101 \\ 101 \\ 100 \\ 99 \\ 98 \\ 97 \end{pmatrix}$ 
  a  $\leftarrow divide(w)$ 
  return (process(a))

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