```
T(i) \colon \mathbb{R} \to \mathbb{Z} return (\lfloor 0x100000000 \cdot \mid sin(i) \mid \rfloor)
```

```
\begin{split} F(i,x,y,z) \colon \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z} &\to \mathbb{Z} \\ \text{if } i < 16 \text{ then} \\ \text{return } ((x \land y) \lor (\neg x \land z)) \\ \text{else if } i < 32 \text{ then} \\ \text{return } ((x \land z) \lor (y \land \neg z)) \\ \text{else if } i < 48 \text{ then} \\ \text{return } (x \oplus y \oplus z) \\ \text{else if } i < 64 \text{ then} \\ \text{return } (y \oplus (x \lor \neg z)) \\ \text{end if} \end{split}
```

"Circular shift of a number"
$$rol(val, s) \colon \mathbb{Z}, \mathbb{Z} \to \mathbb{Z}$$

$$r \in \mathbb{Z}$$

$$r^{[0]} \leftarrow val$$

$$r^{[\mathbf{i}]} \leftarrow (r^{[\mathbf{i}-1]} \ll 1) + ((r^{[\mathbf{i}-1]} \land 0 \times 80000000) \gg 31)$$

$$\mathbf{return} \ (r^{[s]})$$

$$P(a, b, c, d, k, s, i, W, X) \colon \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}^{1}, \mathbb{Z}^{1}_{16} \to \mathbb{Z}^{1}_{4}$$

$$r \in \mathbb{Z}$$

$$tmp \leftarrow W_{a} + X_{k} + T(i+1) + F(i, W_{b}, W_{c}, W_{d})$$

$$W_{a} \leftarrow (W_{b} + rol(tmp, s)) \land 0xFFFFFFFF$$

$$\mathbf{return} \ (W)$$

[&]quot;Transform a byte array of 64 element into a 4 byte array of 16 element"

$$transform(a): \mathbb{Z}_{64}^{1} \to \mathbb{Z}_{16}^{1}$$

$$r \in \mathbb{Z}_{16}^{1}$$

$$r_{i} \mid \forall i \leftarrow a_{4 \cdot i}$$

$$r_{i} \mid \forall i \leftarrow r_{i} + (a_{4 \cdot i+1} \ll 8)$$

$$r_{i} \mid \forall i \leftarrow r_{i} + (a_{4 \cdot i+2} \ll 16)$$

$$r_{i} \mid \forall i \leftarrow r_{i} + (a_{4 \cdot i+3} \ll 24)$$

$$\mathbf{return} (r)$$

$$\begin{aligned} transform_back(a) \colon \mathbb{Z}_4^1 \to \mathbb{Z}_{16}^1 \\ r \in \mathbb{Z}_{16}^1 \\ r_i | \forall i \leftarrow \begin{cases} (a_{\lfloor \frac{i}{4} \rfloor} \land 0 \text{xFF000000}) \gg 24 & i:i \mod 4 = 3 \\ (a_{\lfloor \frac{i}{4} \rfloor} \land 0 \text{x000FF0000}) \gg 16 & i:i \mod 4 = 2 \\ (a_{\lfloor \frac{i}{4} \rfloor} \land 0 \text{x000000FF00}) \gg 8 & i:i \mod 4 = 1 \\ (a_{\lfloor \frac{i}{4} \rfloor} \land 0 \text{x00000000FF}) & \textbf{otherwise} \end{cases} \\ \mathbf{return} \ (r) \end{aligned}$$

```
process(A): \mathbb{Z}^1_{64} \to \mathbb{Z}^1_{16}

\begin{pmatrix}
0x67452301 \\
0xEFCDAB89 \\
0x98BADCFE \\
0x10225476
\end{pmatrix}

     Q \leftarrow list(W)
     X \leftarrow transform(A)
     W \leftarrow P(0, 1, 2, 3, 0, 7, 0, W, X); \quad W \leftarrow P(3, 0, 1, 2, 1, 12, 1, W, X)
     W \leftarrow P(2,3,0,1,2,17,2,W,X); \quad W \leftarrow P(1,2,3,0,3,22,3,W,X)
     W \leftarrow P(0, 1, 2, 3, 4, 7, 4, W, X); \quad W \leftarrow P(3, 0, 1, 2, 5, 12, 5, W, X)
     W \leftarrow P(2,3,0,1,6,17,6,W,X); \quad W \leftarrow P(1,2,3,0,7,22,7,W,X)
     W \leftarrow P(0, 1, 2, 3, 8, 7, 8, W, X); \quad W \leftarrow P(3, 0, 1, 2, 9, 12, 9, W, X)
     W \leftarrow P(2,3,0,1,10,17,10,W,X); \quad W \leftarrow P(1,2,3,0,11,22,11,W,X)
     W \leftarrow P(0, 1, 2, 3, 12, 7, 12, W, X); \quad W \leftarrow P(3, 0, 1, 2, 13, 12, 13, W, X)
     W \leftarrow P(2,3,0,1,14,17,14,W,X); \quad W \leftarrow P(1,2,3,0,15,22,15,W,X)
     W \leftarrow P(0, 1, 2, 3, 1, 5, 16, W, X); \quad W \leftarrow P(3, 0, 1, 2, 6, 9, 17, W, X)
     W \leftarrow P(2,3,0,1,11,14,18,W,X); \quad W \leftarrow P(1,2,3,0,0,20,19,W,X)
     W \leftarrow P(0, 1, 2, 3, 5, 5, 20, W, X); \quad W \leftarrow P(3, 0, 1, 2, 10, 9, 21, W, X)
     W \leftarrow P(2,3,0,1,15,14,22,W,X); \quad W \leftarrow P(1,2,3,0,4,20,23,W,X)
     W \leftarrow P(0, 1, 2, 3, 9, 5, 24, W, X); \quad W \leftarrow P(3, 0, 1, 2, 14, 9, 25, W, X)
     W \leftarrow P(2,3,0,1,3,14,26,W,X); \quad W \leftarrow P(1,2,3,0,8,20,27,W,X)
     W \leftarrow P(0, 1, 2, 3, 13, 5, 28, W, X); \quad W \leftarrow P(3, 0, 1, 2, 2, 9, 29, W, X)
     W \leftarrow P(2, 3, 0, 1, 7, 14, 30, W, X);
                                                 W \leftarrow P(1, 2, 3, 0, 12, 20, 31, W, X)
     W \leftarrow P(0, 1, 2, 3, 5, 4, 32, W, X); \quad W \leftarrow P(3, 0, 1, 2, 8, 11, 33, W, X)
     W \leftarrow P(2,3,0,1,11,16,34,W,X); \quad W \leftarrow P(1,2,3,0,14,23,35,W,X)
     W \leftarrow P(0, 1, 2, 3, 1, 4, 36, W, X); \quad W \leftarrow P(3, 0, 1, 2, 4, 11, 37, W, X)
                                                  W \leftarrow P(1, 2, 3, 0, 10, 23, 39, W, X)
     W \leftarrow P(2, 3, 0, 1, 7, 16, 38, W, X);
                                                  W \leftarrow P(3, 0, 1, 2, 0, 11, 41, W, X)
     W \leftarrow P(0, 1, 2, 3, 13, 4, 40, W, X);
     W \leftarrow P(2, 3, 0, 1, 3, 16, 42, W, X);
                                                   W \leftarrow P(1, 2, 3, 0, 6, 23, 43, W, X)
     W \leftarrow P(0, 1, 2, 3, 9, 4, 44, W, X); \quad W \leftarrow P(3, 0, 1, 2, 12, 11, 45, W, X)
     W \leftarrow P(2,3,0,1,15,16,46,W,X); \quad W \leftarrow P(1,2,3,0,2,23,47,W,X)
                                                 W \leftarrow P(3, 0, 1, 2, 7, 10, 49, W, X)
     W \leftarrow P(0, 1, 2, 3, 0, 6, 48, W, X);
                                                   W \leftarrow P(1, 2, 3, 0, 5, 21, 51, W, X)
     W \leftarrow P(2, 3, 0, 1, 14, 15, 50, W, X);
     W \leftarrow P(0, 1, 2, 3, 12, 6, 52, W, X);
                                                   W \leftarrow P(3, 0, 1, 2, 3, 10, 53, W, X)
     W \leftarrow P(2,3,0,1,10,15,54,W,X); \quad W \leftarrow P(1,2,3,0,1,21,55,W,X)
     W \leftarrow P(0, 1, 2, 3, 8, 6, 56, W, X);
                                                W \leftarrow P(3, 0, 1, 2, 15, 10, 57, W, X)
     W \leftarrow P(2,3,0,1,6,15,58,W,X); \quad W \leftarrow P(1,2,3,0,13,21,59,W,X)
                                                W \leftarrow P(3, 0, 1, 2, 11, 10, 61, W, X)
     W \leftarrow P(0, 1, 2, 3, 4, 6, 60, W, X);
                                                    W \leftarrow_{3} P(1, 2, 3, 0, 9, 21, 63, W, X)
     W \leftarrow P(2, 3, 0, 1, 2, 15, 62, W, X);
     W \leftarrow W + Q
     return (transform\_back(W))
```

$$\begin{aligned} divide(w) \colon \mathbb{Z}^1 &\to \mathbb{Z}^1_{64} \\ ret &\in \mathbb{Z}^1_{64} \\ \\ ret_i | \forall i \leftarrow \begin{cases} w_i & i: i < len(w) \\ 0 \mathbf{x} 80 & i: i = len(w) \\ 8 \cdot len(w) & i: i = 56 \\ 0 & \mathbf{otherwise} \end{cases} \\ \mathbf{return} \ (ret) \end{aligned}$$

$$\mu(): \to \mathbb{Z}^1_{16}$$

"An input string stored as a vector, where symbols are ASCII numbers"

$$w \leftarrow \begin{pmatrix} 97 \\ 98 \\ 99 \\ 100 \\ 101 \\ 101 \\ 100 \\ 99 \\ 98 \\ 97 \end{pmatrix}$$

 $a \leftarrow divide(w)$

return (process(a))