```
T(i): \mathbb{R} \to \mathbb{Z}
     return (|0x100000000 \cdot | sin(i) ||)
F(i, x, y, z) \colon \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z} \to \mathbb{Z}
     if i < 16 then
          return ((x \wedge y) \vee (\neg x \wedge z))
     else if i < 32 then
           return ((x \land z) \lor (y \land \neg z))
     else if i < 48 then
          return (x \oplus y \oplus z)
     else if i < 64 then
          return (y \oplus (x \vee \neg z))
     end if
      "Circular shift of a number"
rol(val, s): \mathbb{Z}, \mathbb{Z} \to \mathbb{Z}
     r \in \mathbb{Z}
     r^{[0]} \leftarrow val
     r^{[i]} \leftarrow (r^{[i-1]} \ll 1) + ((r^{[i-1]} \land 0x80000000) \gg 31)
     return (r^{[s]})
P(a, b, c, d, k, s, i, W, X): \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, \mathbb{Z}, ([0, 4] \Rightarrow \mathbb{Z}), ([0, 4] \times
[0,16] \Rightarrow \mathbb{Z}) \rightarrow ([0,4] \times [0,16] \times [0,4] \Rightarrow \mathbb{Z})
     r \in \mathbb{Z}
     tmp \leftarrow W_a + X_k + T(i+1) + F(i, W_b, W_c, W_d)
```

return (W)

<sup>&</sup>quot;Transform a byte array with 64 elements into a 4 byte array with 16 elements"

$$transform(a): ([0,64] \Rightarrow \mathbb{Z}) \rightarrow ([0,64] \times [0,16] \Rightarrow \mathbb{Z})$$

$$r \in ([0,16] \Rightarrow \mathbb{Z})$$

$$r_{i} \mid \forall i \leftarrow a_{4 \cdot i}$$

$$r_{i} \mid \forall i \leftarrow r_{i} + (a_{4 \cdot i+1} \ll 8)$$

$$r_{i} \mid \forall i \leftarrow r_{i} + (a_{4 \cdot i+2} \ll 16)$$

$$r_{i} \mid \forall i \leftarrow r_{i} + (a_{4 \cdot i+3} \ll 24)$$

$$\mathbf{return} (r)$$

$$transform\_back(a) \colon ([0,4] \Rightarrow \mathbb{Z}) \to ([0,4] \times [0,16] \Rightarrow \mathbb{Z})$$

$$r \in ([0,16] \Rightarrow \mathbb{Z})$$

$$r_{i} | \forall i \leftarrow \begin{cases} (a_{\lfloor \frac{i}{4} \rfloor} \land 0 \times FF000000) \gg 24 & i:i \mod 4 = 3 \\ (a_{\lfloor \frac{i}{4} \rfloor} \land 0 \times 00FF0000) \gg 16 & i:i \mod 4 = 2 \\ (a_{\lfloor \frac{i}{4} \rfloor} \land 0 \times 0000FF000) \gg 8 & i:i \mod 4 = 1 \\ (a_{\lfloor \frac{i}{4} \rfloor} \land 0 \times 000000FF0) & \textbf{otherwise} \end{cases}$$

$$\mathbf{return} \ (r)$$

```
process(A): ([0,64] \Rightarrow \mathbb{Z}) \rightarrow ([0,64] \times [0,16] \Rightarrow \mathbb{Z})
             0x67452301
0xEFCDAB89
0x98BADCFE
    Q \leftarrow list(W)
    X \leftarrow transform(A)
    W \leftarrow P(0, 1, 2, 3, 0, 7, 0, W, X); \quad W \leftarrow P(3, 0, 1, 2, 1, 12, 1, W, X)
    W \leftarrow P(2,3,0,1,2,17,2,W,X); \quad W \leftarrow P(1,2,3,0,3,22,3,W,X)
    W \leftarrow P(0, 1, 2, 3, 4, 7, 4, W, X); \quad W \leftarrow P(3, 0, 1, 2, 5, 12, 5, W, X)
    W \leftarrow P(2,3,0,1,6,17,6,W,X); \quad W \leftarrow P(1,2,3,0,7,22,7,W,X)
    W \leftarrow P(0, 1, 2, 3, 8, 7, 8, W, X); \quad W \leftarrow P(3, 0, 1, 2, 9, 12, 9, W, X)
    W \leftarrow P(2,3,0,1,10,17,10,W,X); \quad W \leftarrow P(1,2,3,0,11,22,11,W,X)
    W \leftarrow P(0, 1, 2, 3, 12, 7, 12, W, X); \quad W \leftarrow P(3, 0, 1, 2, 13, 12, 13, W, X)
    W \leftarrow P(2,3,0,1,14,17,14,W,X); \quad W \leftarrow P(1,2,3,0,15,22,15,W,X)
    W \leftarrow P(0, 1, 2, 3, 1, 5, 16, W, X); \quad W \leftarrow P(3, 0, 1, 2, 6, 9, 17, W, X)
    W \leftarrow P(2,3,0,1,11,14,18,W,X); \quad W \leftarrow P(1,2,3,0,0,20,19,W,X)
    W \leftarrow P(0, 1, 2, 3, 5, 5, 20, W, X); \quad W \leftarrow P(3, 0, 1, 2, 10, 9, 21, W, X)
    W \leftarrow P(2, 3, 0, 1, 15, 14, 22, W, X); \quad W \leftarrow P(1, 2, 3, 0, 4, 20, 23, W, X)
    W \leftarrow P(0, 1, 2, 3, 9, 5, 24, W, X); \quad W \leftarrow P(3, 0, 1, 2, 14, 9, 25, W, X)
    W \leftarrow P(2,3,0,1,3,14,26,W,X); \quad W \leftarrow P(1,2,3,0,8,20,27,W,X)
    W \leftarrow P(0, 1, 2, 3, 13, 5, 28, W, X); \quad W \leftarrow P(3, 0, 1, 2, 2, 9, 29, W, X)
    W \leftarrow P(2, 3, 0, 1, 7, 14, 30, W, X);
                                                 W \leftarrow P(1, 2, 3, 0, 12, 20, 31, W, X)
    W \leftarrow P(0, 1, 2, 3, 5, 4, 32, W, X); \quad W \leftarrow P(3, 0, 1, 2, 8, 11, 33, W, X)
    W \leftarrow P(2,3,0,1,11,16,34,W,X); \quad W \leftarrow P(1,2,3,0,14,23,35,W,X)
    W \leftarrow P(0, 1, 2, 3, 1, 4, 36, W, X); \quad W \leftarrow P(3, 0, 1, 2, 4, 11, 37, W, X)
    W \leftarrow P(2,3,0,1,7,16,38,W,X); \quad W \leftarrow P(1,2,3,0,10,23,39,W,X)
    W \leftarrow P(0, 1, 2, 3, 13, 4, 40, W, X);
                                                 W \leftarrow P(3, 0, 1, 2, 0, 11, 41, W, X)
    W \leftarrow P(2, 3, 0, 1, 3, 16, 42, W, X);
                                                  W \leftarrow P(1, 2, 3, 0, 6, 23, 43, W, X)
    W \leftarrow P(0, 1, 2, 3, 9, 4, 44, W, X); \quad W \leftarrow P(3, 0, 1, 2, 12, 11, 45, W, X)
    W \leftarrow P(2,3,0,1,15,16,46,W,X); \quad W \leftarrow P(1,2,3,0,2,23,47,W,X)
    W \leftarrow P(0, 1, 2, 3, 0, 6, 48, W, X);
                                               W \leftarrow P(3, 0, 1, 2, 7, 10, 49, W, X)
    W \leftarrow P(2,3,0,1,14,15,50,W,X); \quad W \leftarrow P(1,2,3,0,5,21,51,W,X)
    W \leftarrow P(0, 1, 2, 3, 12, 6, 52, W, X); \quad W \leftarrow P(3, 0, 1, 2, 3, 10, 53, W, X)
    W \leftarrow P(2,3,0,1,10,15,54,W,X); \quad W \leftarrow P(1,2,3,0,1,21,55,W,X)
    W \leftarrow P(0, 1, 2, 3, 8, 6, 56, W, X);
                                               W \leftarrow P(3, 0, 1, 2, 15, 10, 57, W, X)
    W \leftarrow P(2,3,0,1,6,15,58,W,X); \quad W \leftarrow P(1,2,3,0,13,21,59,W,X)
    W \leftarrow P(0, 1, 2, 3, 4, 6, 60, W, X);
                                               W \leftarrow P(3, 0, 1, 2, 11, 10, 61, W, X)
                                                   W \leftarrow_{3} P(1, 2, 3, 0, 9, 21, 63, W, X)
    W \leftarrow P(2, 3, 0, 1, 2, 15, 62, W, X);
    W \leftarrow W + Q
    return (transform\_back(W))
```

$$\begin{aligned} \operatorname{divide}(w) &: ([0, \ldots] \Rightarrow \mathbb{Z}) \to ([0, \ldots] \times [0, 64] \Rightarrow \mathbb{Z}) \\ \operatorname{ret} &\in ([0, 64] \Rightarrow \mathbb{Z}) \\ \operatorname{ret}_{i} | \forall i \leftarrow \begin{cases} w_{i} & i : i < \operatorname{len}(w) \\ 0 \times 80 & i : i = \operatorname{len}(w) \\ 8 \cdot \operatorname{len}(w) & i : i = 56 \\ 0 & \text{otherwise} \end{cases} \\ \mathbf{return} \ (\operatorname{ret}) \end{aligned}$$

$$\mu(): \rightarrow ([0,16] \Rightarrow \mathbb{Z})$$

"An input string stored as a vector, where symbols are ASCII numbers"

$$w \leftarrow \begin{pmatrix} 97 \\ 98 \\ 99 \\ 100 \\ 101 \\ 101 \\ 100 \\ 99 \\ 98 \\ 97 \end{pmatrix}$$

 $a \leftarrow divide(w)$ 

return (process(a))