Bootcamp Machine Learning



Module09 Regularization

Module 09 - Regularization

Today you will fight overfitting!

You will discover the concepts of regularization and how to implement it into the algorithms you already saw until now.

Notions of the module

Regularization, overfitting. Regularized cost function, regularized gradient descent. Regularized linear regression. Regularized logistic regression.

Useful Ressources

You are strongly advise to use the following resource: Machine Learning MOOC - Stanford Here are the sections of the MOOC that are relevant for today's exercises:

Week 3:

Solving the Problem of Overfitting:

- Classification (Video + Reading)
- \bullet Hypothesis Representation (Video + Reading)
- Decision Boundary (Video + Reading)

Logistic Regression Model:

- Cost Function (Video + Reading)
- Simplified Cost Function and Gradient Descent (Video + Reading)

Multiclass Classification:

- Mutliclass Classification: One-vs-all (Video + Reading)
- Review (Reading + Quiz)

General rules

- The Python version to use is 3.7, you can check with the following command: python -V
- The norm: during this bootcamp you will follow the Pep8 standards
- The function eval is never allowed.
- The exercises are ordered from the easiest to the hardest.
- Your exercises are going to be evaluated by someone else, so make sure that your variable names and function names are appropriate and civil.
- Your manual is the internet.
- You can also ask questions in the #bootcamps channel in 42AI's Slack workspace.
- If you find any issues or mistakes in this document, please create an issue on our dedicated Github repository.

Helper

Ensure that you have the right Python version.

```
> which python
/goinfre/miniconda/bin/python
> python -V
Python 3.7.*
```

> which pip /goinfre/miniconda/bin/pip

Exercise 00 - Logistic Regression

Exercise 01 - Polynomial models

Exercise 02 - Ai Key Notions

Exercise 03 - Polynomial models II

Interlude - Fighting overfitting... enter Regularization

Interlude - Answers to the vectorization problem

Exercise 04 - L2 Regularization

Interlude - Predict II: Hypothesis

Exercise 05 - Regularized Linear Cost Function

Exercise 06 - Regularized Logistic Cost Function

Interlude - Regularized Gradient

Exercise 07 - Regularized Linear Gradient

Exercise 08 - Regularized Logistic Gradient

Interlude - Linear Regression to the next level: Ridge Regression

Exercise 09 - Ridge Regression

Exercise 10 - Practicing Ridge Regression

Interlude - Regularized Logistic Regression is still Logistic Regression

Exercise 11 - Regularized Logistic Regression

Exercise 12 - Practicing Regularized Logistic Regression

Exercise 00 - Logistic Regression

Turn-in directory: ex00/

Files to turn in : my_logistic_regression.py

Authorized modules : numpy Forbidden modules : sklearn

AI Classics:

These exercises are key assignments from the previous module. If you haven't completed them yet, you should finish them first before you continue with today's exercises.

Objective:

The time to use everything you built so far has come! Demonstrate your knowledge by implementing a logistic regression classifier using the gradient descent algorithm. You must have seen the power of numpy for vectorized operations. Well let's make something more concrete with that.

You may have to take a look at Scikit-Learn's implementation of logistic regression and noticed that the sklearn.linear_model.LogisticRegression class offers a lot of options.

The goal of this exercise is to make a simplified but nonetheless useful and powerful version, with fewer options.

Instructions:

In the my_logistic_regression.py file, write a MyLogisticRegression class as in the instructions below:

```
class MyLogisticRegression():
    """
    Description:
        My personnal logistic regression to classify things.
    """

def __init__(self, thetas, alpha=0.001, max_iter=1000):
        self.alpha = alpha
        self.max_iter = max_iter
        self.thetas = thetas
        ... Your code here ...
... other methods ...
```

You will add the following methods:

```
• predict_(self, x)
```

- cost_elem_(self, y, yhat)
- cost_(self, y, yhat)
- fit_(self, x, y)

You have already written these functions, you will just need a few adjustments so that they all work well within your MyLogisticRegression class.

```
import numpy as np
from my_logistic_regression import MyLogisticRegression as MyLR
X = np.array([[1., 1., 2., 3.], [5., 8., 13., 21.], [3., 5., 9., 14.]])
Y = np.array([[1], [0], [1]])
mylr = MyLR([2, 0.5, 7.1, -4.3, 2.09])
```

Exercise 01 - Polynomial models

Turn-in directory: ex01/

Files to turn in: polynomial_model.py

Authorized modules : numpy Forbidden modules : sklearn

AI Classics:

These exercises are key assignments from the previous module. If you haven't completed them yet, you should finish them first before you continue with today's exercises.

Objective:

Broaden the comprehension of the notion of hypothesis. Create a function that takes a vector x of dimension m and an integer n as input, and returns a matrix of dimension $m \times n$.

Each column of the matrix contains x raised to the power of j, for j = 1, 2, ..., n:

$$x \mid x^2 \mid x^3 \mid \dots \mid x^n$$

Instructions:

In the polynomial_model.py file, write the following function as per the instructions given below:

Exercise 02 - AI Key Notions:

These questions are about key notions from the previous modules. Making sure you can formulate a clear answer to each of them is necessary before you keep going. Discuss them with a fellow student if you can.

Are you able to clearly and simply explain:

- 1 What is overfitting?
- 2 What do you think underfitting might be?
- 3 Why is it important to split the data set in a training and a test set?
- 4 If a model overfits, what will happen when you compare its performance on the training set vs. its performance on the test set?
- 5 If a model underfits, what do you think will happen when you compare its performance on the training set vs. its performance on the test set?

Exercise 03 - Polynomial models II

Turn-in directory: ex03/

Files to turn in: polynomial_model_extended.py

Authorized modules : numpy Forbidden modules : sklearn

Objective:

Create a function that takes a matrix X of dimensions $m \times n$ and an integer p as input, and returns a matrix of dimensions $m \times (np)$.

For each column x_i of the matrix X, the new matrix contains x_i raised to the power of k, for k = 1, 2, ..., p:

$$x_1 \mid \ldots \mid x_n \mid x_1^2 \mid \ldots \mid x_n^2 \mid \ldots \mid x_n^p \mid \ldots \mid x_n^p$$

Instructions:

In the polynomial_model_extended.py file, write the following function as per the instructions given below:

```
import numpy as np
x = np.arange(1,11).reshape(5, 2)

# Example 1:
add_polynomial_features(x, 3)

# Output:
array([[ 1,  2,  1,   4,  1,  8],
        [  3,  4,  9,  16,  27,  64],
        [  5,  6,  25,  36,  125,  216],
        [  7,  8,  49,  64,  343,  512],
        [  9,  10,  81,  100,  729,  1000]])

# Example 2:
add_polynomial_features(x, 4)

# Output:
array([[ 1,  2,  1,  4,  1,  8,  1,  16],
        [  3,  4,  9,  16,  27,  64,  81,  256],
        [  5,  6,  25,  36,  125,  216,  625,  1296],
```

```
64,
100,
8,
10,
            49,
81,
                                 343, 512, 2401, 4096],
729, 1000, 6561, 10000]])
```

Interlude - Fighting Overfitting... With Regularization

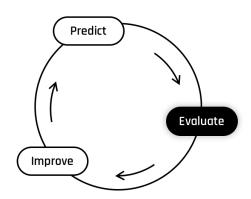


Figure 1: The Learning Cycle - Evaluate

In the **module07**, we talked about the problem of **overfitting** and the necessity of splitting the dataset into a **training set** and a **test set** in order to spot it.

However, being able to detect overfitting does not mean being able to avoid it.

To address this important issue, it is time to introduce you to a new technique: regularization.

If you remember well, overfitting happens because the model takes advantage of irrelevant signals in the training data. The basic idea behind regularization is to **penalize the model for putting too much weight on certain** (usually heavy polynomial) **features**. We do this by adding an extra term in the cost function:

regularized cost function = cost function +
$$\frac{\lambda}{2m} \sum_{j=1}^{n} \theta_j^2$$

By doing so, we are encouraging the model to keep its θ values as small as possible. Indeed, the values of θ themselves are now taken into account when calculating the cost.

 λ (called lambda) is the parameter through which you can modulate how reglarization should impact the model's construction.

- If $\lambda = 0$, there is no regularization (as we did until now),
- If λ is very large, it will drive all the θ parameters to 0.

Please notice: in the regularization term, the sum starts at j = 1 because we do NOT want to penalize the value of θ_0 (the y-intercept, which doesn't depend on a feature).

Be carefull!

Machine Learning was essentially developed by computer scientists (not mathematicians). This can cause problems when we try to represent things mathematically.

For example: using the θ_0 notation to represent the y-intercept makes things easy when we apply the linear algebra trick, **but** it completly messes up the overall matrix notation!

According to that notation, the X' matrix has the following properties:

- its rows, $x'^{(i)}$, follow the mathematical indexing: starting at 1.
- its columns, x'_i , follow the computer science indexing: starting at 0.

$$X' = \underbrace{\begin{bmatrix} 1 & x_1^{(1)} & \dots & x_n^{(1)} \\ \vdots & \vdots & \ddots & \vdots \\ 1 & x_1^{(m)} & \dots & x_n^{(m)} \end{bmatrix}}_{j = 0, \dots, n} = \begin{bmatrix} x_0^{(1)} & x_1^{(1)} & \dots & x_n^{(1)} \\ \vdots & \vdots & \ddots & \vdots \\ x_0^{(m)} & x_1^{(m)} & \dots & x_n^{(m)} \end{bmatrix}}_{j = 1, \dots, m}$$

It's precisely for this reason that you keep seeing that X' is of dimensions $m \times (n+1)$

Terminology:

The regularization technique we are introducing here is named L_2 regularization, because it adds the squared L_2 norm of the θ vector to the cost function.

The L_2 norm of a given vector x, written

$$L_2(x) = ||x||_2 = \sqrt{\sum_i x_i^2} L_2(x)^2 = ||x||_2^2 = \sum_i x_i^2$$

is its euclidean norm (i.e. the sum of the components squared).

There is an infinite variety of norms that could be used as regularization terms, depending on the desired regularization effect. Here, we will only use L_2 , the most common one.

Note:

the notation
$$\sum_{i}$$
 means: "the sum for all i "

There is no need to give explicitly the start and the end of the summation index if we want to sum over all the values of i.

However, it is better to do it anyway because it forces us to be sure of what we are doing. And in our case, we do not want to sum over θ_0 ...

Our old friend vectorization ...

It is not a surprise, we can use vectorization to calculate $\sum_{j=1}^{n} \theta_{j}^{2}$ more efficiently. It could be a good exercise for you to try to figure it out by yourself. We suggest you give it a try and then check the answer on the next page.

Interlude - Answers to the Vectorization Problem

So, how do you vectorize the following?

$$\sum_{i=j}^{n} \theta_j^2$$

It's very similar to a **dot product** of θ with itself. The only problem here is to find a way to not take θ_0 into account.

Let's construct a vector θ' with the following rules :

$$\theta'_0 = 0
\theta'_j = \theta_j \text{ for } j = 1, \dots, n$$

In other words:

$$\theta' = \begin{bmatrix} 0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix}$$

This way, we can perform the dot product without having θ_0 interfering in our calculations:

$$\theta' \cdot \theta' = \begin{bmatrix} 0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix} \cdot \begin{bmatrix} 0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix}$$

$$= 0 \cdot 0 + \theta_1 \cdot \theta_1 + \dots + \theta_n \cdot \theta_n$$

$$= \sum_{j=1}^n \theta_j^2$$

Exercise 04 - L2 Regularization

Turn-in directory: ex04/
Files to turn in: l2_reg.py
Authorized modules: Numpy
Forbidden modules: sklearn

Objective:

You must implement the following formulas as functions:

Iterative:

$$L_2(\theta)^2 = \sum_{j=1}^n \theta_j^2$$

Where θ is a vector of dimension n.

Vectorized:

$$L_2(\theta)^2 = \theta' \cdot \theta'$$

Where θ' is a vector of dimension n, constructed using the following rules:

$$\theta'_0 = 0
\theta'_j = \theta_j \text{ for } j = 1, \dots, n$$

Instructions:

In the 12_reg.py file, write the following function as per the instructions given below:

```
def iterative_12(theta):
    """Computes the L2 regularization of a non-empty numpy.ndarray, with a for-loop.
    Args:
        theta: has to be a numpy.ndarray, a vector of shape n * 1.
    Returns:
        The L2 regularization as a float.
        None if theta in an empty numpy.ndarray.
    Raises:
        This function should not raise any Exception.
    """
        ... Your code ...

def 12(theta):
    """Computes the L2 regularization of a non-empty numpy.ndarray, without any for-loop.
    Args:
        theta: has to be a numpy.ndarray, a vector of shape n * 1.
    Returns:
        The L2 regularization as a float.
        None if theta in an empty numpy.ndarray.
    Raises:
        This function should not raise any Exception.
    """
        ... Your code ...
```

```
x = np.array([2, 14, -13, 5, 12, 4, -19])

# Example 1:
iterative_12(x)
# Output:
911.0

# Example 2:
12(x)
# Output:
911.0

y = np.array([3,0.5,-6])
# Example 3:
iterative_12(y)
# Output:
36.25

# Example 4:
12(y)
# Output:
36.25
```

Exercise 05 - Regularized Linear Cost Function

Turn-in directory: ex05/

Files to turn in: linear_cost_reg.py

Authorized modules : numpy Forbidden modules : sklearn

Objective:

You must implement the following formula as a function:

$$J(\theta) = \frac{1}{2m} [(\hat{y} - y) \cdot (\hat{y} - y) + \lambda(\theta' \cdot \theta')]$$

Where:

- y is a vector of dimension m, the expected values,
- \hat{y} is a vector of dimension m, the predicted values,
- λ is a constant, the regularization hyperparameter,
- θ' is a vector of dimension n, constructed using the following rules:

$$\begin{array}{ll} \theta_0' &= 0 \\ \theta_j' &= \theta_j & \text{for } j = 1, \dots, n \end{array}$$

Instructions:

In the linear_cost_reg.py file, write the following function as per the instructions given below:

Hint: such situation is a good use case of decorators...

```
y = np.array([2, 14, -13, 5, 12, 4, -19])
y_hat = np.array([3, 13, -11.5, 5, 11, 5, -20])
```

```
theta = np.array([1, 2.5, 1.5, -0.9])

# Example :
reg_cost_(y, y_hat, theta, .5)
# Output:
0.8503571428571429

# Example :
reg_cost_(y, y_hat, theta, .05)
# Output:
0.5511071428571429

# Example :
reg_cost_(y, y_hat, theta, .9)
# Output:
1.116357142857143
```

Exercise 06 - Regularized Logistic Cost Function

Turn-in directory: ex06/

Files to turn in: logistic_cost_reg.py

Authorized modules: numpy Forbidden modules: sklearn

Objective:

You must implement the following formula as a function:

$$J(\theta) = -\frac{1}{m} [y \cdot \log(\hat{y}) + (\vec{1} - y) \cdot \log(\vec{1} - \hat{y})] + \frac{\lambda}{2m} (\theta' \cdot \theta')$$

Where:

- \hat{y} is a vector of dimension m, the vector of predicted values,
- y is a vector of dimension m, the vector of expected values,
- $\vec{1}$ is a vector of dimension m, a vector full of ones,
- λ is a constant, the regularization hyperparameter,
- θ' is a vector of dimension n, constructed using the following rules:

$$\theta'_0 = 0
\theta'_j = \theta_j \text{ for } j = 1, \dots, n$$

Instructions:

In the logistic_cost_reg.py file, write the following function as per the instructions given below:

Hint: such situation is a good use case for decorators...

```
y = np.array([1, 1, 0, 0, 1, 1, 0])
y_hat = np.array([.9, .79, .12, .04, .89, .93, .01])
theta = np.array([1, 2.5, 1.5, -0.9])

# Example :
reg_log_cost_(y, y_hat, theta, .5)
# Output:
0.43377043716475955

# Example :
reg_log_cost_(y, y_hat, theta, .05)
# Output:
0.13452043716475953

# Example :
reg_log_cost_(y, y_hat, theta, .9)
# Output:
0.6997704371647596
```

Interlude - Regularized Gradient

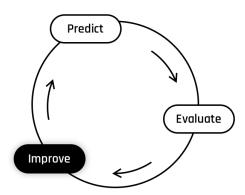


Figure 2: The Learning Cycle - Improve

To derive the gradient of the regularized cost function, $\nabla(J)$ you have to change a bit the formula of the unregularized gradient.

Given the fact that we are not penalizing θ_0 , the formula will remain the same as before for this parameter. For the other parameters $(\theta_1, \dots, \theta_n)$, we must add the partial derivative of the regularization term: $\lambda \theta_i$.

Therefore, we get:

$$\nabla(J)_0 = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

$$\nabla(J)_j = \frac{1}{m} \left(\sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \lambda \theta_j \right) \text{ for } j = 1, ..., n$$

Where:

- $\nabla(J)_i$ is the j^{th} component of the gradient vector $\nabla(J)$,
- m is the number of training examples used,
- $h_{\theta}(x^{(i)})$ is the model's prediction for the i^{th} training example,
- $x^{(i)}$ is the feature vector of the i^{th} training example,
- $y^{(i)}$ is the expected target value for the i^{th} example,
- λ is a constant, the regularization hyperparameter
- θ_j is the j^{th} parameter of the θ vector,

Which can be vectorized as:

$$\nabla(J) = \frac{1}{m} [X'^T (h_{\theta}(X) - y) + \lambda \theta']$$

Where:

- $\nabla(J)$ is a vector of dimension (n+1), the gradient vector,
- *m* is the number of training examples used,
- X is a matrix of dimensions $m \times n$, the design matrix,

- X' is a matrix of dimensions $m \times (n+1)$, the design matrix onto which a column of ones is added as a first column,
- y is a vector of dimension m, the vector of expected values,
- $h_{\theta}(X)$ is a vector of dimension m, the vector of predicted values,
- λ is a constant,
- θ is a vector of dimension (n+1), the parameter vector,
- θ' is a vector of dimension (n+1), constructed using the following rules:

$$\theta'_0 = 0
\theta'_j = \theta_j \text{ for } j = 1, \dots, n$$

Linear Gradient vs Logistic Gradient

As before, we draw your attention on the only difference between linear regression and logistic regression's gradient equations: the hypothesis function $h_{\theta}(X)$.

- In the linear regression: $h_{\theta}(X) = X'\theta$
- In the logistic regression: $h_{\theta}(X) = \operatorname{sigmoid}(X'\theta)$

Exercise 07 - Regularized Linear Gradient

Turn-in directory: ex07/

Files to turn in: reg_linear_grad.py

Authorized modules : numpy Forbidden modules : sklearn

Objective:

You must implement the following formulas as a functions for the linear regression hypothesis:

Iterative:

$$\nabla(J)_0 = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$
$$\nabla(J)_j = \frac{1}{m} \left(\sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \lambda \theta_j \right) \text{ for } j = 1, ..., n$$

Where:

- $\nabla(J)_j$ is the j^{th} component of $\nabla(J)$,
- $\nabla(J)$ is a vector of dimension (n+1), the gradient vector,
- \bullet m is a constant, the number of training examples used,
- $h_{\theta}(x^{(i)})$ is the model's prediction for the i^{th} training example,
- $x^{(i)}$ is the feature vector (of dimension n) of the i^{th} training example, found in the i^{th} row of the X matrix,
- X is a matrix of dimensions $m \times n$, the design matrix,
- $y^{(i)}$ is the i^{th} component of the y vector,
- y is a vector of dimension m, the vector of expected values,
- λ is a constant, the regularization hyperparameter,
- θ_j is the j^{th} parameter of the θ vector,
- θ is a vector of dimension (n+1), the parameter vector,

Vectorized:

$$\nabla(J) = \frac{1}{m} [X'^{T}(h_{\theta}(X) - y) + \lambda \theta']$$

Where:

- $\nabla(J)$ is a vector of dimension (n+1), the gradient vector,
- m is a constant, the number of training examples used,
- X is a matrix of dimension $m \times n$, the design matrix,
- X' is a matrix of dimensions $m \times (n+1)$, the design matrix onto which a column of ones is added as a first column,
- $X^{\prime T}$ is the transpose of the matrix, with dimensions $(n+1)\times m$,
- $h_{\theta}(X)$ is a vector of dimension m, the vector of predicted values,

- y is a vector of dimension m, the vector of expected values,
- λ is a constant, the regularization hyperparameter,
- θ is a vector of dimension (n+1), the parameter vector,
- θ' is a vector of dimension n, constructed using the following rules:

$$\begin{array}{ll} \theta_0' &= 0 \\ \theta_j' &= \theta_j & \text{for } j = 1, \dots, n \end{array}$$

Instructions:

In the reg_linear_grad.py file, write the following functions as per the instructions given below:

```
def reg_linear_grad(y, x, theta, lambda_):
    ... Your code ...
def vec_reg_linear_grad(y, x, theta, lambda_):
    ... Your code ...
```

Hint: this is a great occasion to use decorators...

```
[ 9, -11, 8]])
y = np.array([[2], [14], [-13], [5], [12], [4], [-19]])
theta = np.array([[7.01], [3], [10.5], [-6]])
reg_linear_grad(y, x, theta, 1)
array([[ -60.99
       [-195.64714286],
       [ 863.46571429],
       [-644.52142857]])
vec_reg_linear_grad(y, x, theta, 1)
array([[ -60.99
                    ],
       [-195.64714286],
       [-644.52142857]])
reg_linear_grad(y, x, theta, 0.5)
array([[ -60.99
       [-195.86142857],
       [-644.09285714]])
vec_reg_linear_grad(y, x, theta, 0.5)
array([[ -60.99
       [-195.86142857],
       [ 862.71571429],
[-644.09285714]])
reg_linear_grad(y, x, theta, 0.0)
array([[ -60.99
       [-643.66428571]])
vec_reg_linear_grad(y, x, theta, 0.0)
array([[ -60.99
       [-196.07571429],
       [ 861.96571429],
[-643.66428571]])
```

Exercise 08 - Regularized Logistic Gradient

Turn-in directory: ex08/

Files to turn in : reg_logistic_grad.py

Authorized modules : Numpy Forbidden modules : sklearn

Objective:

You must implement the following formulas as a functions for the logistic regression hypothesis:

Iterative:

$$\nabla(J)_0 = \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$
$$\nabla(J)_j = \frac{1}{m} \left(\sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_j^{(i)} + \lambda \theta_j \right) \text{ for } j = 1, ..., n$$

Where:

- $\nabla(J)_j$ is the j^{th} component of $\nabla(J)$,
- $\nabla(J)$ is a vector of dimension (n+1), the gradient vector,
- m is a constant, the number of training examples used,
- $h_{\theta}(x^{(i)})$ is the model's prediction for the i^{th} training example,
- $x^{(i)}$ is the feature vector (of dimension n) of the i^{th} training example, found in the i^{th} row of the X matrix,
- X is a matrix of dimensions $m \times n$, the design matrix,
- $y^{(i)}$ is the i^{th} component of the y vector,
- y is a vector of dimension m, the vector of expected values,
- λ is a constant, the regularization hyperparameter,
- θ_j is the j^{th} parameter of the θ vector,
- θ is a vector of dimension (n+1), the parameter vector,

Vectorized:

$$\nabla(J) = \frac{1}{m} [X'^{T}(h_{\theta}(X) - y) + \lambda \theta']$$

Where:

- $\nabla(J)$ is a vector of dimension (n+1), the gradient vector,
- m is a constant, the number of training examples used,
- X is a matrix of dimensions $m \times n$, the design matrix,
- X' is a matrix of dimensions $m \times (n+1)$, the design matrix onto which a column of ones is added as a first column,
- $X^{\prime T}$ is the transpose of the matrix, with dimensions $(n+1)\times m$,
- $h_{\theta}(X)$ is a vector of dimension m, the vector of predicted values,

- y is a vector of dimension m, the vector of expected values,
- λ is a constant, the regularization hyperparameter,
- θ is a vector of dimension (n+1), the parameter vector,
- θ' is a vector of dimension n, constructed using the following rules:

$$\begin{array}{ll} \theta_0' &= 0 \\ \theta_j' &= \theta_j & \text{for } j = 1, \dots, n \end{array}$$

Instructions:

In the reg_logistic_grad.py file, create the following function as per the instructions given below:

```
def reg_logistic_grad(y, x, theta, lambda_):
    ... Your code ...
def vec_reg_logistic_grad(y, x, theta, lambda_):
    ... Your code ...
```

Hint: this is a great occasion to use decorators...

```
reg_logistic_grad(y, x, theta, 1)
array([[-0.55711039],
        [-1.40334809],
[-1.91756886],
[-2.56737958],
        [-3.03924017]])
vec_reg_logistic_grad(y, x, theta, 1)
array([[-0.55711039],
        [-1.40334809],
[-1.91756886],
        [-2.56737958],
        [-3.03924017]])
reg_logistic_grad(y, x, theta, 0.5)
array([[-0.55711039],
        [-2.33404624],
        [-3.15590684]])
vec_reg_logistic_grad(y, x, theta, 0.5)
array([[-0.55711039],
        [-1.15334809],
        [-1.96756886],
        [-2.33404624],
[-3.15590684]])
reg_logistic_grad(y, x, theta, 0.0)
array([[-0.55711039],
        [-0.90334809],
        [-3.27257351]])
vec_reg_logistic_grad(y, x, theta, 0.0)
array([[-0.55711039],
        [-0.90334809],
[-2.01756886],
        [-3.27257351]])
```

Interlude - Linear Regression to the Next Level: Ridge Regression

Until now we only talked about L2 regularization and its implication on the calculation of the cost function and gradient for both linear and logistic regression.

Now it's time to use proper terminology:

When we apply L2 regularization on a linear regression model, the new model is called a **Ridge Regression** model.

Besides that brand-new name, Ridge regression is nothing more than linear regression regularized with L2.

We suggest you to watch this nice explanation very nice explanation of Ridge Regularization.

By the way, this Youtube channel, **StatQuest**, is very good to help you understand the gist of a lot of machine learning concepts.

You will not waste your time watching its statistics and machine learning playlists!

Exercise 09 - Ridge Regression

Turn-in directory: ex09/ Files to turn in: ridge.py Authorized modules: numpy Forbidden modules: sklearn

Objective:

Now it's time to implement your MyRidge class, similar to the class of the same name in sklearn.linear_model.

Instructions:

In the ridge.py file, create the following class as per the instructions given below:

Your MyRidge class will have several methods:

- __init__ , special method, identical to the one you wrote in MyLinearRegression (module06),
- get_params_, which get the parameters of the estimator,
- set_params_ , which set the parameters of the estimator,
- cost_, which return the cost between 2 vectors (numpy arrays),
- cost_elem_, which return a vector correspondind to the squared difference between 2 vectors (numpy arrays),
- predict_, which generate predictions using a linear model,
- fit_, which fit Ridge regression model to a training dataset.

Except for fit_, the methods are identical to the ones in your MyLinearRegression class.

You should consider inheritance

The difference between MyRidge's fit_ method and the fit_ method you implemented for your MyLinearRegression class is the use of a regularization term.

Hint: again, this is a great occasion for you to try to use decorators...

Exercise 10 - Practicing Ridge Regression

Turn-in directory: ex10/

Files to turn in : space_avocado.py, benchmark_train.py,

models.[csv/yml/pickle]

Authorized modules : numpy Forbidden modules : sklearn

Objective:

It's training time!

Let's practice our brand new Ridge Regression with a polynomial model.

Introduction:

You have already used the dataset space_avocado.csv. The dataset is constituted of 5 columns:

- index: not relevant,
- weight: the avocado weight order (in ton),
- **prod_distance**: distance from where the avocado ordered is produced (in Mkm),
- time_delivery: time between the order and the receipt (in days),
- target: price of the order (in trantorian unit).

It contains the data of all the avocado purchase made by Trantor administration. ## Instructions: You have to explore different models and select the best one. To do this, your program are expected to: 1. Split the dataset into a training, cross validation and test sets. 2. Explore several linear models with polynomial features (maximum degree of 4). 3. For each hypothesis, consider a regularized factor ranging from 0 to 1 with step of 0.2. 4. Evaluate your models on the cross-validation set. 5. Evaluate the score of the best model on the test set. According to your model evaluations, what is the best hypothesis you get? 6. Plot the evaluation curve which help you to select the best model (evaluation metric vs models + λ factor). 7. Plot the true price and the predicted price obtain via your best model with the different λ values (meaning the dataset + the 5 predicted curves).

The training of all your models can take a long time. Thus you need to train only the best one during the correction. But you should return in benchmark_train.py the program which perform the training of all the models and save the parameters of the different models into a file(models.[csv/yml/pickle]). In models.[csv/yml/pickle] one must find the parameters of all the models you have explored and trained. space_avocado.py program trains the model based on the best hypothesis you find and load the other models from models.[csv/yml/pickle]. Then evaluate the best model on the right set and plot the different graphics as asked before.

Interlude - Regularized Logistic Regression is still Logistic Regression

As opposed to linear regression, regularized logistic regression is still called logistic regression.

Working without regularization parameters can be considered simply as a special case where $\lambda = 0$.

if
$$\lambda = 0$$
:

$$\nabla(J) = \frac{1}{m} [X'^T (h_{\theta}(X) - y) + \lambda \theta']$$

$$= \frac{1}{m} [X'^T (h_{\theta}(X) - y) + 0 \cdot \theta']$$

$$= \frac{1}{m} [X'^T (h_{\theta}(X) - y)]$$

Exercise 11 - Regularized Logistic Regression

Turn-in directory: ex11/

Files to turn in: my_logistic_regression.py

Authorized modules : Numpy Forbidden modules : sklearn

Objective:

In the last exercice, you implemented of a regularized version of the linear regression algorithm, called Ridge regression. Now it's time to update your logistic regression classifier as well! In the scikit-learn library, the logistic regression implementation offers a few regularization techniques, which can be selected using the parameter penalty (L2 is default). The goal of this exercice is to update your old MyLogisticRegression class to take that into account.

Instructions:

In the my logistic regression.py file, update your MyLogisticRegression class according to the following:

• add a penalty parameter wich can take the following values: {'12', 'none'}, default = '12'.

```
class MyLogisticRegression():
    """
    Description:
        My personnal logistic regression to classify things.
    """

def __init__(self, theta, alpha=0.001, max_iter=1000, penalty='12'):
        self.alpha = alpha
        self.max_iter = max_iter
        self.theta = theta
        self.penalty=penalty
        ... Your code ...
... other methods ...
```

- update the fit_(self, x, y) method:
 - if penalty == '12':
 use a regularized version of the gradient descent.
 - if penalty = 'none':
 use the unregularized version of the gradient descent from module08.

Hint: this is also a great use case for decorators...

Exercise 12 - Practicing Regularized Logistic Regression

Turn-in directory: ex12/

Files to turn in : solar_system_census.py, benchmark_train.py,

models.[csv/yml/pickle]

Authorized modules : numpy Forbidden modules : sklearn

Objective:

It's training time!

Let's practice our updated Logistic Regression with polynomial models.

Introduction:

You have already used the dataset solar_system_census.csv and solar_system_census_planets.csv.

- The dataset is divided in two files which can be found in the resources folder: solar_system_census.csv and solar_system_census_planets.csv.
- The first file contains biometric information such as the height, weight, and bone density of several Solar System citizens.
- The second file contains the homeland of each citizen, indicated by its Space Zipcode representation (i.e. one number for each planet...:)).

As you should know, Solar citizens come from four registered areas (zipcodes):

- The flying cities of Venus (0),
- United Nations of Earth (1),
- Mars Republic (2),
- The Asteroids' Belt colonies (3).

Instructions:

What you have to do is very similar to what you have done in the exercise 10.

You have to explore different models and select the best one. To do this, you will create 2 programs: benchmark_train.py and solar_system_censu.py.

Benchmark and train:

benchmark_train.py is expected to: 1. Split the dataset into a training, cross-validation and test sets. 2. Explore several regularized logistic models with polynomial hypotheses (maximum degree of 3). The models will be trained with different λ values, ranging from 0 to 1. 3. Evaluate your models with the **f1-score** on the cross-validation set. 4. Print the evaluation score which help you to select the best model (evaluation metric vs models + λ factor). 5. Save the different models into models. [csv/yml/pickle] file.

solar system census program:

benchmark_train.py is expected to: 1. Split the dataset into a training, cross-validation and test sets. 2. Load the differents models from models.[csv/yml/pickle] and train from scratch the best model you find during your benchmark. 4. Print and plot the performance of the different models (different hypotheses and different values for λ factor) measured with the f1-score on the cross-validation set and also the score of your best model on the test set. 5. Plot the target values and the predicted values of your best model on the same scatter plot. Make some effort to have a readable figure.

One Last Word - It's Just a Beginning...

Congratulation!!

You have finished this bootcamp and you can be proud of yourself! We hope you liked it and that the material were understandable.

We tried our best to make it as accessible as possible to anyone, even for someone with little mathematical background. It was quite a challenge, and we hope we succeed to that difficult mission.

Equiped with your brand-new knowledge you are now able to tackle more challenging algorithm like **ensemble** methods (random forest, gradient boosting), support vector machine or even artificial neural networks!!

An because we know that a lot of you have neural networks in mind when you started this journey into machine learning, let's talk a bit more about why you are now able to deep dive into it... fearlessly!

Neural networks are based on the same blocks you should now be familiar with. Essentially:

- matrix and vector operations,
- gradient descent,
- regularization,
- sigmoid (as activation functions, even if it is a bit outdated now)

Let's see what you can do now.

To go further

To keep learning Machine Learning, here are several options you should consider:

- To complete the entire Stanford's Machine Learning MOOC. It is a great ressource, a classic for those who want to study machine learning. This bootcamp followed thighly the architecture of its first three weeks. This course still worth your time even if it is old now! Also, someone did a great work to convert all the Octave assignments into Python notebooks. For the neural network part, it would be better to follow the Deep Learning specialization on coursera. There are much more formation about AI also on coursera made by Deeplearning.ai.
- To take fast.ai Deep Learning MOOC. It's a great way to learn Deep Learning following a top-down approach.