

Team notebook

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1 data-structures

1.1 fenwick

```
template <class T>
class fenwick {
    vector<T> a;
    int n;

public:
    fenwick() {}

    fenwick(int n_) : n(n_) {
        // check initial value
        a.assign(n + 5, static_cast<T>(0));
    }
};
```

```

}

T query(int r) {
    T q = 0; // check default value of query
    for (; r > 0; r -= (r & -r)) {
        q += a[r]; // check query modification
    }
    return q;
}

void update(int r, T del) {
    for (; r <= n; r += (r & -r)) {
        a[r] += del; //check update rule
    }
}
};

```

1.2 fenwick2d

```

// from online git I don't remember, all credits go to them
template<
    typename T // need to support +, -
> struct Fenwick2D {
    // 1-indexed
    int n1, n2;
    vector<vector<T>> f;

    Fenwick2D(int _n1, int _n2) : n1(_n1 + 1), n2(_n2 + 1), f(1+n1,
        vector<T> (1+n2, T(0))) {}
    Fenwick2D() {}
    // a[x][y] += val
    void update(ll x, ll y, T val) {
        assert(0 <= x && x < n1);
        assert(0 <= y && y < n2);
        ++x; ++y;
        for (int u = x; u <= n1; u += u & -u) {
            for (int v = y; v <= n2; v += v & -v) {
                f[u][v] += val;
            }
        }
    }

    T get(ll x1, ll y1, ll x2, ll y2) const { // [x1,y1] -> [x2,y2]

```

```

        return _get(x1, y1, x2 + 1, y2 + 1);
    }
    T get(ll x, ll y) const { // [0,0] -> [x,y]
        return _get(x + 1, y + 1);
    }

private:
    // return rect sum of [0, 0] -> [x-1, y-1]
    T _get(ll x, ll y) const {
        assert(0 <= x && x <= n1);
        assert(0 <= y && y <= n2);
        T res(0);
        for (int u = x; u > 0; u -= u & -u) {
            for (int v = y; v > 0; v -= v & -v) {
                res += f[u][v];
            }
        }
        return res;
    }

    // returns rect sum of [x1, y1] -> [x2-1, y2-1]
    T _get(ll x1, ll y1, ll x2, ll y2) {
        if (x1 == x2 || y1 == y2) return T(0);
        return get(x2, y2) - get(x1, y2) - get(x2, y1) + get(x1, y1);
    }
};

```

1.3 lazysegtree

```

// lazy propagation with one-based indexing
//
// build:
//     lazySegtree<int> seg(n); // vector<int> a(n + 1)
//     seg.build(a); // vector 'a' must be one-indexed
//
// update:
//     seg.update(l, r, inc); //increase a[l -> r] += inc
//     //you may want to set this
// query:
//     seg.query(l, r)

template <class T>
struct lazySegTree {

```

```

vector<T> st, lazy;
int n;
lazySegTree(int _n) : n(_n) {
    T default_value = 0;
    st.assign(4 * n + 5, default_value);
    lazy.assign(4 * n + 5, default_value);
}
void build(const vector<T> &a) {
    build(a, 1, 1, n);
}
void build(const vector<T> &a, int id, int l, int r) {
    lazy[id] = 0;
    if(l == r) {
        if(l < a.size()) {
            st[id] = a[l];
        }
        return;
    }
    int mid = (l + r) >> 1;
    build(a, id * 2, l, mid);
    build(a, id * 2 | 1, mid + 1, r);
    st[id] = max(st[id * 2], st[id * 2 | 1]);
}
void down(int id) {
    if(lazy[id] == 0)
        return;
    st[id * 2] += lazy[id];
    st[id * 2 | 1] += lazy[id];
    lazy[id * 2] += lazy[id];
    lazy[id * 2 | 1] += lazy[id];
    lazy[id] = 0;
}
void update(int u, int v, T val) {
    update(u, v, val, 1, 1, n);
}
void update(int u, int v, T val, int id, int l, int r) {
    if(v < l || r < u) return;
    if(u <= l && r <= v) {
        lazy[id] += val;
        st[id] += val;
        return;
    }
    down(id);
    int mid = (l + r) >> 1;
    update(u, v, val, id * 2, l, mid);

```

```

    update(u, v, val, id * 2 | 1, mid + 1, r);
    st[id] = max(st[id * 2], st[id * 2 | 1]);
}
T query(int u, int v) {
    return query(u, v, 1, 1, n);
}
T query(int u, int v, int id, int l, int r) {
    if(v < l || r < u) {
        return -INF;
    }
    if(u <= l && r <= v) {
        return st[id];
    }
    int mid = (l + r) >> 1;
    down(id);
    return max(query(u, v, id * 2, l, mid), query(u, v, id * 2 | 1, mid + 1, r));
}
};

```

1.4 make-pbds

```

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

/**
 * Description: Policy-based data structures that supports normal set
 *              operation and
 * * find_by_order(k) returns iterator to kth element starting from 0;
 * * order_of_key(k) returns count of elements strictly [smaller] than
 *   k;
 * Caution:
 * * do not define int long long before below declaration
 */

template <class T, class cmp = std::less<T>>
using ordered_set = tree<T, null_type, cmp,
    rb_tree_tag, tree_order_statistics_node_update>;

template <class key, class value, class cmp = std::less<key>>
using ordered_map = tree<key, value, cmp, rb_tree_tag,
    tree_order_statistics_node_update>;

```

1.5 rmq

min/max[i...j] --> O(1)

Build: O(nlogn)

```
template<class T>
struct RMQ {
    T st[LG + 1][N];
    int n;
    void build(const vector<T> &a) {
        n = a.size() - 1;
        for (int i = 1; i <= n; ++i) st[0][i] = a[i];
        for (int j = 1; j <= LG; ++j)
            for (int i = 1; i + (1 << j) - 1 <= n; ++i)
                st[j][i] = min(st[j - 1][i], st[j - 1][i + (1 << (j - 1))]);
    }
    T query(int l, int r) {
        int k = __lg(r - l + 1);
        return min(st[k][l], st[k][r - (1 << k) + 1]);
    }
};
```

vector a = {1,2,31,15,19,22}

RMQ<int> rmq;

rmq.build(a);

-----> rmq.query(i,j)

1.6 segment-tree

```
// segtree with one-based indexing
//
// build:
//   segtree<int> seg(n); // vector<int> a(n + 1);
//   seg.build(a); // vector 'a' must be one-indexed
//
// update:
//   seg.update(pos, inc); //increase a[pos] to a[pos] + inc
//   //you may want to set this
// query:
//   seg.query(l, r)   tính tổng từ a[l..r]
```

```
template<class T>
struct segTree {
    vector<T> st;
    int n;
    segTree(int _n) : n(_n) {
        T default_value = 0;
        st.assign(4 * n + 5, default_value);
    }
    void build(const vector<T> &a) {
        build(a, 1, 1, n);
    }
};
```

Cho 1 mảng. và q câu hỏi

$n \leq 1e5, q \leq 1e5$

Yêu cầu: với câu hỏi thì chúng ta

1. Tang vị trí $a[i]$ lên x đơn vị

2. Cho 2 số l,r. Tính tổng từ l..r

2 4 5 1 2 3

10

1 1 3 $a[i] += x$

2 1 4 for l --> r sum += $a[i]$

1 2 4 // O(n)

1 3 5

1 6 2

2 2 6

---> O(q.n)

```
}
void build(const vector<T> &a, int id, int l, int r) {
    if(l == r) {
        st[id] = a[l];
        return;
    }
    int mid = (l + r) >> 1;
    build(a, id * 2, l, mid);
    build(a, id * 2 | 1, mid + 1, r);
    st[id] = st[id * 2] + st[id * 2 | 1];
}
void update(int pos, T inc) {
    update(pos, inc, 1, 1, n);
}
void update(int pos, T inc, int id, int l, int r) {
    if(pos < l || r < pos) {
        return;
    }
    if(l == r) {
        st[id] += inc;
        return;
    }
    int mid = (l + r) >> 1;
    update(pos, inc, id * 2, l, mid);
    update(pos, inc, id * 2 | 1, mid + 1, r);
    st[id] = st[id * 2] + st[id * 2 | 1];
}
T query(int u, int v) {
    return query(u, v, 1, 1, n);
}
T query(int u, int v, int id, int l, int r) {
    if(v < l || r < u) {
        return 0;
    }
    if(u <= l && r <= v) {
        return st[id];
    }
    int mid = (l + r) >> 1;
    return query(u, v, id * 2, l, mid) + query(u, v, id * 2 | 1, mid + 1, r);
}
};
```

1.7 treap-pbds

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

/// *** Needs C++11 or C++14 ***/

/// Treap supporting duplicating values in set
/// Maximum value of treap * ADD must fit in long long

struct Treap { /// hash = 96814
    int len;
    const int ADD = 1000010;
    const int MAXVAL = 1000000010;
    unordered_map <long long, int> mp; /// Change to int if only int in
        treap
    tree<long long, null_type, less<long long>, rb_tree_tag,
        tree_order_statistics_node_update> T;

    Treap(){
        len = 0;
        T.clear(), mp.clear();
    }

    inline void clear(){
        len = 0;
        T.clear(), mp.clear();
    }

    inline void insert(long long x){
        len++, x += MAXVAL;
        int c = mp[x]++;
        T.insert((x * ADD) + c);
    }

    inline void erase(long long x){
        x += MAXVAL;
        int c = mp[x];
        if (c){
            c--, mp[x]--, len--;
            T.erase((x * ADD) + c);
        }
    }
}
```

```
/// 1-based index, returns the K'th element in the treap, -1 if none
    exists
inline long long kth(int k){
    if (k < 1 || k > len) return -1;
    auto it = T.find_by_order(--k);
    return ((*it) / ADD) - MAXVAL;
}

/// Count of value < x in treap
inline int count(long long x){
    x += MAXVAL;
    int c = mp[--x];
    return (T.order_of_key((x * ADD) + c));
}

/// Number of elements in treap
inline int size(){
    return len;
}
};
```

1.8 treap

```
//replace sum with many other function, just like cnt
struct item {
    long long prior, value, cnt, sum;
    bool rev;
    item *l, *r;
    item(long long value): prior(rand()), value(value), cnt(1),
        rev(false), sum(value), l(0), r(0) {}
};

long long cnt (item* it) {
    return it ? it->cnt : 0;
}

long long sum (item* it) {
    return it ? it->sum : 0;
}

void upd_cnt (item* it) {
    if (it)
        it->cnt = cnt(it->l) + cnt(it->r) + 1;
```

```

}

void upd_sum(item* it) {
    if (it)
        it->sum = sum(it->l) + sum(it->r) + it->value;
}

void push (item* it) {
    if (it && it->rev) {
        it->rev = false;
        swap(it->l, it->r);
        if (it->l) it->l->rev ^= true;
        if (it->r) it->r->rev ^= true;
    }
}

void merge (item* & t, item* l, item* r) {
    push (l);
    push (r);
    if (!l || !r)
        t = l ? l : r;
    else if (l->prior > r->prior)
        merge (l->r, l->r, r), t = l;
    else
        merge (r->l, l, r->l), t = r;
    upd_cnt(t);
    upd_sum(t);
}

// split so that the number of the node in the left is "num"
void split (item* t, item* & l, item* & r, long long num, long long add =
0) {
    if (!t)
        return void( l = r = 0 );
    push (t);
    int cur_num = add + cnt(t->l);
    if (num <= cur_num)
        split (t->l, l, t->l, num, add), r = t;
    else
        split (t->r, t->r, r, num, add + 1 + cnt(t->l)), l = t;

    upd_cnt(t);
    upd_sum(t);
}

```

```

// l, r are 1-indexed
void reverse (item* t, int l, int r) {
    item *t1, *t2, *t3;
    split (t, t1, t2, l-1);
    split (t2, t2, t3, r-l+1);
    t2->rev ^= true;
    merge (t, t1, t2);
    merge (t, t, t3);
}

void traverse (item* t) {
    if (!t) return;
    push (t);
    traverse (t->l);
    // do stuff with current value
    cout << t->value << " ";
    traverse (t->r);
}

```

1.9 z-function

```

vector<int> z_function(const string& s) {
    int n = (int) s.size();
    vector<int> z(n);
    for (int i = 1, l = 0, r = 0; i < n; ++i) {
        if (i <= r)
            z[i] = min (r - i + 1, z[i - l]);
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])
            ++z[i];
        if (i + z[i] - 1 > r)
            l = i, r = i + z[i] - 1;
    }
    return z;
}

```

2 gen

```

/**
 * Usage:
 * 1. Compile and run "your_code.cpp" and "brute.cpp" on example

```

```

* 2. Only modify gen_test() function
* 3. Run gen.cpp
* Note: Use gen_test() if only want to generate testcases, use check()
      if need stress testing
* Default OS: Linux
* In Windows: change "diff" to "fc", remove "./"
*/

```

```

#include <bits/stdc++.h>
using namespace std;
using ll = long long;

```

```

mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());

```

```

const string NAME = "test";
const int NTEST = 5;

```

```

ll randint(ll l, ll r) {
    return uniform_int_distribution<ll> (l,r) (rng);
}

```

```

ll randdouble(double l, double r) {
    return uniform_real_distribution<double> (l,r) (rng);
}

```

```

void gen_test() {
    ofstream gen("test.inp");
    // gen code ( inp << . . . << . . . )
    int n = randint(1,10);
    gen << n << endl;
    for (int i = 1; i <= n; i++)    gen << randint(-1,10) << " ";
    gen.close();
}

```

```

void check() {
    for (int iTest = 1; iTest <= NTEST; iTest++) {
        gen_test();

        system(("./" + NAME + ".exe < test.inp > test.out").c_str());
        system("./brute.exe < test.inp > test.ans");

        if (system("diff test.out test.ans"))
        { // fc : Windows < > diff : Linux
            cout << "Test " << iTest << ": WRONG!\n";
            return;
        }
    }
}

```

```

    }
    cout << "Test " << iTest << ": CORRECT!\n";
}

signed main()
{
    srand(time(NULL));
    return 0;
}

```

3 graphs

3.1 DFSMatching

```

/**
 * Description: Simple bipartite matching algorithm. Graph $g$ should be
 * a list
 * of neighbors of the left partition, and $btoa$ should be a vector full
 * of
 * -1's of the same size as the right partition. Returns the size of
 * the matching. $btoa[i]$ will be the match for vertex $i$ on the right
 * side,
 * or $-1$ if it's not matched.
 * Time: O(VE)
 * Usage: vi btoa(m, -1); dfsMatching(g, btoa);
 * Status: works
 */

bool find(int j, vector<vi>& g, vi& btoa, vi& vis) {
    if (btoa[j] == -1) return 1;
    vis[j] = 1; int di = btoa[j];
    for (int e : g[di])
        if (!vis[e] && find(e, g, btoa, vis)) {
            btoa[e] = di;
            return 1;
        }
    return 0;
}

int dfsMatching(vector<vi>& g, vi& btoa) {
    vi vis;
    rep(i,0,sz(g)) {

```

```

        vis.assign(sz(btoa), 0);
        for (int j : g[i])
            if (find(j, g, btoa, vis)) {
                btoa[j] = i;
                break;
            }
    }
    return sz(btoa) - (int)count(all(btoa), -1);
}

```

3.2 EdmondKarp_{new}

// Maximum flow from s to t in a flow network. $O(E^2 \cdot V)$
 // Tested: <https://oj.vnoi.info/problem/nkflow>
 // Tested: <https://oj.vnoi.info/problem/nknet>

```

const int N = 1e3 + 5;
const int INF = numeric_limits<int>::max() / 2;
int c[N][N], par[N], f[N][N], d[N];
int n, m, s, t;

int bfs(int s, int t) {
    queue<int> q;
    fill(par, par + N, -1);
    fill(d, d + N, 0);
    q.push(s); d[s] = INF;
    while (!q.empty()) {
        int u = q.front(); q.pop();
        for (int i = 1; i <= n; i++) {
            if (c[u][i] - f[u][i] > 0 && par[i] == -1) {
                d[i] = min(d[u], c[u][i] - f[u][i]);
                par[i] = u; q.push(i);
                if (i == t) return d[t];
            }
        }
    }
    return 0;
}

int max_flow(int s, int t) {
    int cur = 0, ans = 0;
    while ((cur = bfs(s, t)) > 0) {
        ans += cur;
    }
}

```

```

    int v = t;
    while (v != s) {
        f[par[v]][v] += cur;
        f[v][par[v]] -= cur;
        v = par[v];
    }
}
return ans;
}

int vis[N];
void dfs_min_cut(int u) { // Find all edges in Min-Cut, edges u-v in
    // Min-Cut has vis[u] = 1 and vis[v] = 0
    vis[u] = 1;
    for (int v = 1; v <= n; v++) {
        if (abs(f[u][v]) < c[u][v] && !vis[v]) dfs_min_cut(v);
    }
}

vector<pair<int, int>> min_cut() { // Can optimized using edge list
    dfs_min_cut(s);
    vector<pair<int, int>> ans;
    for (int i = 1; i <= n; i++)
        for (int j = 1; j <= n; j++)
            if (f[i][j] && vis[i] && !vis[j])
                ans.push_back({i, j});
    return ans;
}

signed main() {
    cin >> n >> m >> s >> t;
    for (int i = 1; i <= m; i++) {
        int u, v, C;
        cin >> u >> v >> C;
        c[u][v] += C;
    }
    cout << max_flow(s, t) << '\n';
    auto v = min_cut();
    for (auto ii : v) cout << ii.first << " " << ii.second << '\n';
    return 0;
}

```

3.3 HopcroftKarp

```

/**
 * Description: Fast bipartite matching algorithm. Graph $g$ should be a
 * list
 * of neighbors of the left partition, and $btoa$ should be a vector full
 * of
 * -1's of the SAME SIZE as the right partition. Returns the size of
 * the matching. btoa[i] will be the match for vertex i on the right side,
 * or -1 if it's not matched.
 * Usage: vector<int> btoa(m, -1); hopcroftKarp(g, btoa);
 * Time: O(sqrt(V)*E)
 * Tested: https://oj.vnoi.info/problem/match1
 * Tested: https://oj.vnoi.info/problem/fmatch
 */

bool dfs(int a, int L, vector<vector<int>>& g, vector<int>& btoa,
vector<int>& A, vector<int>& B) {
    if (A[a] != L) return 0;
    A[a] = -1;
    for (int b : g[a]) if (B[b] == L + 1) {
        B[b] = 0;
        if (btoa[b] == -1 || dfs(btoa[b], L + 1, g, btoa, A, B))
            return btoa[b] = a, 1;
    }
    return 0;
}

```

```

int hopcroftKarp(vector<vector<int>>& g, vector<int>& btoa) {
    int res = 0;
    vector<int> A(g.size()), B(btoa.size()), cur, next;
    for (;;) {
        fill(A.begin(), A.end(), 0);
        fill(B.begin(), B.end(), 0);
        /// Find the starting nodes for BFS (i.e. layer 0).
        cur.clear();
        for (int a : btoa) if (a != -1) A[a] = -1;
        for (int a = 0; a < g.size(); a++) if (A[a] == 0)
            cur.push_back(a);
        /// Find all layers using bfs.
        for (int lay = 1; lay++ <= g.size()) {
            bool islast = 0;
            next.clear();
            for (int a : cur) for (int b : g[a]) {
                if (btoa[b] == -1) {
                    B[b] = lay;

```

```

                    islast = 1;
                }
                else if (btoa[b] != a && !B[b]) {
                    B[b] = lay;
                    next.push_back(btoa[b]);
                }
            }
            if (islast) break;
            if (next.empty()) return res;
            for (int a : next) A[a] = lay;
            cur.swap(next);
        }
        /// Use DFS to scan for augmenting paths.
        for (int a = 0; a < g.size(); a++)
            res += dfs(a, 0, g, btoa, A, B);
    }
}

```

3.4 Tarjan

```

int n,m;
vector<int> g[N];

bool onStack[N];
stack<int> st;
int tin[N], low[N];
int dfsTime=0;

int SCCCount=0;

void dfs(int u) {
    onStack[u]=true; st.push(u);
    low[u]=tin[u]=++dfsTime;

    for(int v : g[u]){
        /// cout<<u<<" -> "<<v<<endl;
        if (!tin[v]) dfs(v);
        if (onStack[v]) low[u]=min(low[u],low[v]); // low[v] not tin[v]
    }

    if (low[u]==tin[u]){ // new SCC found
        while (!st.empty()){
            int a = st.top();

```

```

        onStack[a]=false;st.pop();
        printf("%d ",a);
        if (a == u){
            printf("\n");
            break;
        }
    }
    SCCCount++;
}
}

```

3.5 bridge-articulation

```

/*
Usage: Find bridges and articulations
Tested: https://cses.fi/problemset/task/2076,
https://cses.fi/problemset/task/2077
*/

const int N = 1e5 + 5;
int n,m,dfsTime,numBridge;
vector<int> adj[N];
vector<pair<int,int>> bridges; // All edges that are bridges
int num[N], low[N], tail[N], joint[N]; // joint[i] = 1 <=> i is
articulation

void dfs(int u, int par = -1) {
    int numChild = 0;
    num[u] = low[u] = ++dfsTime;
    for (int v : adj[u]) {
        if (v == par) continue;
        if (!num[v]) {
            dfs(v,u);
            low[u] = min(low[u], low[v]);
            if (low[v] == num[v]) {
                bridges.push_back({u,v});
                numBridge++;
            }
            numChild++;
            if (par == -1 && numChild > 1) joint[u] = 1;
            if (par != -1 && low[v] >= num[u]) joint[u] = 1;
        }
        else low[u] = min(low[u], num[v]);
    }
}

```

```

    }
    tail[u] = dfsTime;
}

```

3.6 dijkstra

```

struct dijkstra {
    int n;
    vector<vector<pair<int, long long>> > g;
    int s;
    vector<long long> dist;

    dijkstra(int n): n(n) {
        g.assign(n + 1, vector<pair<int, long long> >());
        dist.assign(n + 1, 1e18);
    }

    void add_edge(int u, int v, ll c) {
        // change this whether directed or not
        g[u].push_back(make_pair(v,c));
        g[v].push_back(make_pair(u,c));
    }

    void build() {
        set<pair<long long, int> > st;

        st.insert(make_pair(0, s)); dist[s] = 0;

        while (st.size()) {
            long long du = st.begin()->fi; int u =
                st.begin()->se;
            st.erase(st.begin());
            if (du != dist[u]) continue;

            for (auto &[v, c] : g[u]) {
                if (dist[v] > dist[u] + c) {
                    dist[v] = dist[u] + c;
                    st.insert(make_pair(dist[v], v));
                }
            }
        }
    }
};

```

3.7 dsu

```
class dsu {
    vector<int> parent, size;

public:
    dsu() {}

    dsu(int n) {
        parent.resize(n);
        size.assign(n, 1);
        iota(all(parent), 0);
    }

    int find(int v) {
        if (v == parent[v]) return v;
        return parent[v] = find(parent[v]);
    }

    bool unite(int a, int b) {
        a = find(a);
        b = find(b);
        if (a != b) {
            if (size[a] < size[b]) swap(a, b);
            parent[b] = a;
            size[a] += size[b];
            return true;
        } else {
            return false;
        }
    }
};
```

3.8 hld-3

```
/**
 * Given a rooted tree of nodes, where each node is uniquely numbered in
 * between [1..N]. The node 1 is the root of the tree. Each node has an
 * integer value which is initially 0.
 * You need to perform the following two kinds of queries on the tree:
 *   * add t value: Add value to all nodes in subtree rooted at t
 *   * max a b: Report maximum value on the path from a to b
 * Tested: https://vjudge.net/problem/HackerRank-subtrees-and-paths
```

```
*/

#include<bits/stdc++.h>

using namespace std;

#define int long long
#define pb push_back

const int INF = 1e9 + 7;
const int N = 2e5 + 5;

vector<int> adj[N];
int id[N], head[N], sz[N], in[N], out[N], h[N], pos[N];
int p[20][N];
int nhanh = 1, cnt;

int seg[4 * N], lazy[4 * N];

void down(int id) {
    int t = lazy[id];
    int lhs = id * 2, rhs = id * 2 + 1;
    seg[lhs] += t; seg[rhs] += t;
    lazy[lhs] += t; lazy[rhs] += t;
    lazy[id] = 0;
}

void update(int id, int l, int r, int u, int v, int val) {
    if (l > v || r < u) return;
    if (l >= u && r <= v) {
        seg[id] += val;
        lazy[id] += val;
        return;
    }
    down(id);
    int mid = (l + r) / 2;
    update(id * 2, l, mid, u, v, val);
    update(id * 2 + 1, mid + 1, r, u, v, val);
    seg[id] = max(seg[id * 2], seg[id * 2 + 1]);
}

int get(int id, int l, int r, int u, int v) {
    if (l > v || r < u) return -INF;
    if (l >= u && r <= v) return seg[id];
    down(id);
```

```

    int mid = (l + r) / 2;
    return max(get(id * 2, l, mid, u, v), get(id * 2 + 1, mid + 1, r, u,
        v));
}

void dfs(int u, int par = 1) {
    sz[u] = 1;
    p[0][u] = par;
    for (int i = 1; i < 20; i++)    p[i][u] = p[i - 1][p[i-1][u]];
    for (int v : adj[u]) if (v != par) {
        h[v] = h[u] + 1;
        dfs(v,u);
        sz[u] += sz[v];
    }
}

void hld(int u, int par = -1) {
    if (head[nhanh] == 0)    {
        head[nhanh] = u;
    }
    ++cnt;
    in[u] = cnt;
    id[u] = nhanh;
    pos[u] = cnt;

    int target = -1;
    for (int v : adj[u]) if (v != par) {
        if (target == -1 || sz[target] < sz[v])
            target = v;
    }

    if (target != -1) hld(target,u);

    for (int v : adj[u]) if (v != par) {
        if (v != target) {
            ++nhanh;
            hld(v,u);
        }
    }
    out[u] = cnt;
}

int query(int u, int v) {
    int ans = -INF;
    while (id[u] != id[v]) {

```

```

        if (h[head[id[u]]] > h[head[id[v]]])    swap(v,u);
        int v2 = head[id[v]];
        ans = max(ans, get(1,1,cnt,pos[v2], pos[v]));
        v = p[0][v2];
    }
    if (pos[u] > pos[v])    swap(u,v);
    ans = max(ans, get(1,1,cnt,pos[u], pos[v]));
    return ans;
}

void solve() {
    int n; cin >> n;
    for (int i = 1; i < n; i++) {
        int u,v;    cin >> u >> v;
        adj[u].pb(v);
        adj[v].pb(u);
    }

    dfs(1);
    hld(1);

    int q; cin >> q;
    while (q--) {
        string typ;    cin >> typ;
        if (typ == "add") {
            int u,val;    cin >> u >> val;
            update(1,1,cnt,in[u], out[u], val);
        }
        else {
            int u,v;    cin >> u >> v;
            cout << query(u,v) << '\n';
        }
    }
}

int32_t main() {
    ios_base :: sync_with_stdio(0); cin.tie(nullptr); cout.tie(nullptr);
    solve();
    return 0;
}

/*
5
1 2
2 3

```

```

2 4
5 1
6
add 4 30
add 5 20
max 4 5
add 2 -20
max 4 5
max 3 4
*/

```

3.9 hld

```

/**
 * You are given a tree
 * We will ask you to perform some instructions of the following form:
 * CHANGE i ti : change the cost of the i-th edge to ti
 * or
 * QUERY a b : ask for the maximum edge cost on the path from node a to
 *             node b
 * Status: Tested: https://vjudge.net/problem/SPOJ-QTREE
 */

#include<bits/stdc++.h>
using namespace std;

#define int long long
#define pb push_back
const int N = 1e5 + 5;

int sz[N];
int n, dfsTime;
int nhanh, cnt;
int id[N]; // <=> thu tu cua chain chua dinh i = id[i]
int head[N]; // <=> gia tri dau tien cua chain thu i = head[i]
int pos[N]; // <=> thu tu cua dinh u sau khi duoc trai phang = pos[i]
int in[N], out[N], h[N], a[N], p[N][20];
vector<int> adj[N];

struct seg2D { // 0-index
    int n;
    vector<int> seg;
    seg2D() = default;

```

```

    seg2D(int _n) : seg(2 * _n, INT_MIN), n(_n) {}
    void update(int u, int val) {
        for (seg[u += n] = val; u > 1; u /= 2) {
            seg[u >> 1] = max(seg[u], seg[u ^ 1]);
        }
    }
    int get(int u, int v) {
        int ans = INT_MIN;
        for (u += n, v += n; u <= v; u/=2, v /= 2) {
            if (u & 1)    ans = max(ans, seg[u++]);
            if (~v & 1)   ans = max(ans, seg[v--]);
        }
        return ans;
    }
}seg;

void reset() {
    nhanh = 1;
    dfsTime = 0;
    cnt = 0;
    for (int i = 1; i <= n; i++){
        adj[i].clear();
        h[i] = 0;
        in[i] = 0;
        out[i] = 0;
        pos[i] = 0;
        head[i] = 0;
        id[i] = 0;
        a[i] = 0;
        sz[i] = 1;
    }
    memset(p, 0, sizeof p);
}

void dfs(int u, int par = -1) {
    p[u][0] = par;
    for (int i = 1; i < 20; i++)    p[u][i] = p[p[u][i-1]][i-1];
    ++dfsTime;
    in[u] = dfsTime;
    sz[u] = 1;
    for (int v : adj[u]) if (v != par) {
        h[v] = h[u] + 1;
        dfs(v, u);
    }
}

```

```

        sz[u] += sz[v];
    }
    out[u] = dfsTime;
}

bool cha(int u, int v) {
    return (in[u] <= in[v] && out[u] >= out[v]);
}

void build_hld(int u, int par = -1) {
    if (head[nhanh] == 0) {
        head[nhanh] = u;
    }
    ++cnt;
    pos[u] = cnt;
    id[u] = nhanh;

    int tmp = -1;
    for (int v : adj[u]) if (v != par) {
        if (tmp == -1 || sz[tmp] < sz[v]) tmp = v;
    } // Tim dinh v co sz lon nhat

    // heavy edge
    if (tmp != -1) build_hld(tmp, u);

    for (int v : adj[u]) if (v != par && v != tmp) {
        /// light edge
        nhanh++;
        build_hld(v, u);
    }
}

int ans_hld(int u, int v) { // the maximum edge cost on the path from
    node u to node v
    int ans = INT_MIN;
    while (id[u] != id[v]) {
        if (h[head[id[u]]] > h[head[id[v]]]) swap(u, v);
        int v2 = head[id[v]];
        ans = max(ans, seg.get(pos[v2] - 1, pos[v] - 1));
        v = p[v2][0];
    }
    /// id[u] == id[v]
    if (pos[u] > pos[v]) swap(u, v);
    ans = max(ans, seg.get(pos[u], pos[v] - 1)); /// Khi u va v o cung
    nhanh, ta chi nhay tu v len dinh gan u nhat vi u o day la lca (ta

```

```

        phai bo a[lca] di do qua trinh chuyen duong di)
    return ans;
}

int lca(int u, int v) { // Bin lift
    if (h[u] < h[v]) swap(u, v);
    int k = h[u] - h[v];
    for (int j = 0; j < 20; j++) if (k >> j & 1) u = p[u][j];
    if (u == v) return u;
    for (int i = 19; i >= 0; i--) {
        if (p[u][i] != p[v][i]) u = p[u][i], v = p[v][i];
    }
    return p[u][0];
}

void precalc() {
    dfs(1, 1);
    build_hld(1);
}

void solve() {
    cin >> n;
    reset();
    vector<array<int, 3>> ed(n + 1);
    for (int i = 1; i < n; i++) {
        int u, v, w; cin >> u >> v >> w;
        ed[i] = {u, v, w};
        adj[u].pb(v);
        adj[v].pb(u);
    }
    precalc();
    seg = seg2D(cnt);
    for (int i = 1; i < n; i++) {
        int u = ed[i][0], v = ed[i][1], w = ed[i][2];
        if (!cha(u, v)) swap(u, v);
        a[v] = w;
        seg.update(pos[v] - 1, w);
    }
    while (1) {
        string typ;
        cin >> typ;
        if (typ == "DONE") return;
        if (typ == "QUERY") {
            int u, v; cin >> u >> v;
            int LCA = lca(u, v);

```

```

        cout << max(ans_hld(u,LCA), ans_hld(v,LCA)) << '\n';
    }
    else {
        int id;    cin >> id;
        int nval;  cin >> nval;
        int u = ed[id][0], v = ed[id][1], w = ed[id][2];
        if (!cha(u,v))    swap(u,v);    // v la con u
        a[v] = nval;
        ed[id][2] = nval;
        seg.update(pos[v] - 1, nval);
    }
}

int32_t main() {
    ios_base :: sync_with_stdio(0); cin.tie(nullptr); cout.tie(nullptr);
    int test; cin >> test;
    while (test--) {
        solve();
        cout << '\n';
    }
    return 0;
}

/*
1
3
1 2 1
2 3 2
QUERY 1 2
CHANGE 1 3
QUERY 1 2
DONE
*/

```

3.10 lca-binarylift

```

/**
 * Description: Finding LCA and Kth Ancestor using Binary Lifting
 * Caution:
 *     * adj must be one-indexed
 *     * root must be 1 (can be modified if required)
 * Source : https://oj.vnoi.info/submission/4618381

```

```

* Verification : https://oj.vnoi.info/problem/hbtlca
*
* usage LCA lca(n + 1, root) // default root is 1
*/

```

```

struct LCA {
    vector<vector<int>>> par;
    vector<int> dep;
    int LG;
    void dfs(int u, int p = 0) {
        par[u][0] = p;
        for (int i = 1; i < LG; i++)
            par[u][i] = par[par[u][i - 1]][i - 1];
        for (int v : adj[u]) {
            if (v == p) continue;
            dep[v] = dep[u] + 1;
            dfs(v, u);
        }
    }
}

```

```

int ancestor(int u, int k) {
    for (int i = 0; i < LG; i++)
        if (k & (1 << i))
            u = par[u][i];
    return u;
}

```

```

int lca(int u, int v) {
    if (dep[u] < dep[v]) swap(u, v);
    u = ancestor(u, dep[u] - dep[v]);
    if (u == v) return u;
    for (int i = LG - 1; i >= 0; i--)
        if (par[u][i] != par[v][i])
            u = par[u][i], v = par[v][i];
    return par[u][0];
}

```

```

LCA (int _n, int root = 1) {
    int n = _n;
    LG = 64 - __builtin_clzll(n);
    par.assign(n, vector<int>(LG, 0));
    dep.assign(n, 0);
    dfs(root);
}
};

```

3.11 minimum-path-cover-in-DAG

```
#include <bits/stdc++.h>

#define MAX 505
#define clr(ar) memset(ar, 0, sizeof(ar))
#define read() freopen("lol.txt", "r", stdin)
#define dbg(x) cout << #x << " = " << x << endl
#define ran(a, b) (((rand() << 15) ^ rand()) % ((b) - (a) + 1)) + (a))

using namespace std;
/// Minimum path cover/Maximum independent set in DAG
namespace dag{
    /// For transitive closure and minimum path cover with not
    /// necessarily disjoint vertex
    bool ar[MAX][MAX];

    vector<int> adj[MAX];
    bool visited[MAX], first_set[MAX], second_set[MAX];
    int n, L[MAX], R[MAX], D[MAX], Q[MAX], dis[MAX], parent[MAX];

    inline void init(int nodes){ /// Number of vertices in DAG
        n = nodes;
        for (int i = 0; i < MAX; i++) adj[i].clear();
    }

    inline void add_edge(int u, int v){ /// 0 based index, directed edge
        /// of DAG
        adj[u].push_back(v);
    }

    bool dfs(int i){
        int len = adj[i].size();
        for (int j = 0; j < len; j++){
            int x = adj[i][j];
            if (L[x] == -1 || (parent[L[x]] == i)){
                if (L[x] == -1 || dfs(L[x])){
                    L[x] = i, R[i] = x;
                    return true;
                }
            }
        }
        return false;
    }
}
```

```
bool bfs(){
    clr(visited);
    int i, j, x, d, f = 0, l = 0;

    for (i = 0; i < n; i++){
        if (R[i] == -1){
            visited[i] = true;
            Q[l++] = i, dis[i] = 0;
        }
    }

    while (f < l){
        i = Q[f++];
        int len = adj[i].size();
        for (j = 0; j < len; j++){
            x = adj[i][j], d = L[x];
            if (d == -1) return true;

            else if (!visited[d]){
                Q[l++] = d;
                parent[d] = i, visited[d] = true, dis[d] = dis[i] + 1;
            }
        }
    }
    return false;
}

void get_path(int i){
    first_set[i] = true;
    int j, x, len = adj[i].size();

    for (j = 0; j < len; j++){
        x = adj[i][j];
        if (!second_set[x] && L[x] != -1){
            second_set[x] = true;
            get_path(L[x]);
        }
    }
}

void transitive_closure(){ /// Transitive closure in O(n * m)
    clr(ar);
    int i, j, k, l;
    for (i = 0; i < n; i++){
        l = adj[i].size();
```



```

    for (j = 0; j < l; j++){
        ar[i][adj[i][j]] = true;
    }
    adj[i].clear();
}

for (k = 0; k < n; k++){
    for (i = 0; i < n; i++){
        if (ar[i][k]){
            for (j = 0; j < n; j++){
                if (ar[k][j]) ar[i][j] = true;
            }
        }
    }
}

for (i = 0; i < n; i++){
    for (j = 0; j < n; j++){
        if (i != j && ar[i][j]){
            adj[i].push_back(j);
        }
    }
}

}

/// Minimum vertex disjoint path cover in DAG. Handle isolated
/// vertices appropriately
int minimum_disjoint_path_cover() {
    int i, res = 0;
    memset(L, -1, sizeof(L));
    memset(R, -1, sizeof(R));

    while (bfs()){
        for (i = 0; i < n; i++){
            if (R[i] == -1 && dfs(i)) res++;
        }
    }

    return n - res;
}

int minimum_path_cover(){ /// Minimum path cover in DAG. Handle
    isolated vertices appropriately
    transitive_closure();
    return minimum_disjoint_path_cover();
}

```

```

/// Minimum vertex cover of DAG, equal to maximum bipartite matching
vector <int> minimum_vertex_cover(){
    int i, res = 0;
    memset(L, -1, sizeof(L));
    memset(R, -1, sizeof(R));

    while (bfs()){
        for (i = 0; i < n; i++){
            if (R[i] == -1 && dfs(i)) res++;
        }
    }

    vector <int> v;
    clr(first_set), clr(second_set);
    for (i = 0; i < n; i++){
        if (R[i] == -1) get_path(i);
    }

    for (i = 0; i < n; i++){
        if (!first_set[i] || second_set[i]) v.push_back(i);
    }

    return v;
}

/// Maximum independent set of DAG, all vertices not in minimum
/// vertex cover
vector <int> maximum_independent_set() {
    vector <int> v = minimum_vertex_cover();
    clr(visited);
    int i, len = v.size();
    for (i = 0; i < len; i++) visited[v[i]] = true;

    vector <int> res;
    for (i = 0; i < n; i++){
        if (!visited[i]) res.push_back(i);
    }

    return res;
}
}

```

3.12 minimum-vertex-cover

```
/**
```

```

* Description: Finds a minimum vertex cover in a bipartite graph.
* The size is the same as the size of a maximum matching, and
* the complement is a maximum independent set.
* Status: stress-tested
*/

```

```

/**
 * DAG
 * Maximum Independent Set == Minimum Path Cover
 * Minimum Path Cover = n - Maximum Bipartite Matching
 * Minimum vertex cover of DAG == Maximum Bipartite Matching
 */

```

```

#include "DFSMatching.cpp"

```

```

vi cover(vector<vi>& g, int n, int m) {
    vi match(m, -1);
    int res = dfsMatching(g, match);
    vector<bool> lfound(n, true), seen(m);
    for (int it : match) if (it != -1) lfound[it] = false;
    vi q, cover;
    rep(i,0,n) if (lfound[i]) q.push_back(i);
    while (!q.empty()) {
        int i = q.back(); q.pop_back();
        lfound[i] = 1;
        for (int e : g[i]) if (!seen[e] && match[e] != -1) {
            seen[e] = true;
            q.push_back(match[e]);
        }
    }
    rep(i,0,n) if (!lfound[i]) cover.push_back(i);
    rep(i,0,m) if (seen[i]) cover.push_back(n+i);
    assert(sz(cover) == res);
    return cover;
}

```

4 mathematics

4.1 DP-SOS

```

/**
 * Usage:

```

```

* subset[x]: number of element which is submask of x
* superset[x]: number of element which is superset of x
* Common heuristic:
* Number of element y such that x | y = x => y is subset of x
* Number of element y such that x & y = x => y is superset of x
* Number of element y such that x & y != 0 => n - subset[((1 << N) - 1)
    & ~x]
* a_i >= 10^6 => Change N
* Tested: https://cses.fi/problemset/task/1654
*/

```

```

const int N = 21;
int subset[1 << N], superset[1 << N];

```

```

void sum_over_subset() {
    for (int i = 0; i < N; i++) {
        for (int msk = 0; msk < (1 << N); msk++) {
            if (msk >> i & 1) subset[msk] += subset[msk ^ (1 << i)];
        }
    }
}

```

```

void sum_over_superset() {
    for (int i = 0; i < N; i++) {
        for (int msk = 0; msk < (1 << N); msk++) {
            if (msk >> i & 1) superset[msk ^ (1 << i)] += superset[msk];
        }
    }
}

```

4.2 MI

```

const ll MOD = 1e9 + 7;
ll mul(ll a, ll b){return (a%MOD)*(b%MOD)%MOD;}
ll add(ll a, ll b){return ((a+MOD)%MOD + (b+MOD)%MOD)%MOD;}
ll fpow(ll a, ll b){
    ll res=1;
    while (b){
        if (b & 1) res=mul(res,a);
        b>>=1;
        a=mul(a,a);
    }
}

```

```

    return res;
}
ll inv(ll a) {return fpow(a,MOD-2);}

// Euler's totient function. Source: cp-algorithms.com
vector<ll> phi_1_to_n(int n) {
    vector<ll> phi(n + 1);
    for (int i = 0; i <= n; i++)
        phi[i] = i;

    for (int i = 2; i <= n; i++) {
        if (phi[i] == i) {
            for (int j = i; j <= n; j += i)
                phi[j] -= phi[j] / i;
        }
    }
    return phi;
}

void factorial(vector<ll>& fact, int n) {
    fact.assign(n + 1, 0);
    fact[0] = 1;
    for (ll i = 1; i <= n; i++) fact[i] = mul(fact[i - 1], i);
}

void inv_factorial(vector<ll>& invfact, int n) {
    invfact.assign(n + 1, 0);
    invfact[0] = 1;
    for (ll i = 1; i <= n; i++) invfact[i] = mul(invfact[i - 1],
        inv(i));
}

```

4.3 combinatorics-power

```

vector<Mint> fact(1, 1);
vector<Mint> inv_fact(1, 1);

Mint power(const Mint a, const int b) {
    assert(b >= 0);
    Mint x = a, res = 1;
    U p = b;
    while (p > 0) {
        if (p & 1) res *= x;
        x *= x;

```

```

        p >>= 1;
    }
    return res;
}

Mint C(int n, int k) {
    if (k < 0 || k > n) {
        return 0;
    }
    k = min(k, n - k);
    while ((int) fact.size() < n + 1) {
        fact.push_back(fact.back() * (int) fact.size());
        inv_fact.push_back(1 / fact.back());
    }
    return fact[n] * inv_fact[k] * inv_fact[n - k];
}

```

4.4 convex-hull

```

struct Point {
    long long x, y;
};

bool operator < (const Point & a, const Point & b) {
    return ii(a.x, a.y) < ii(b.x, b.y);
}

ostream & operator << (ostream & out, const Point& a) {
    out << "(" << a.x << ", " << a.y << ")";
    return out;
}

istream & operator >> (istream & is, Point& a) {
    is >> a.x >> a.y;
    return is;
}

// A -> B -> C form counterclockwise direction
bool ccw(const Point &A, const Point &B, const Point &C) {
    return (B.x - A.x) * (C.y - A.y) - 1LL * (C.x - A.x) * (B.y - A.y) >
        0;
}

```

```

// CONVEX HULL (CLOCKWISE)
// Source: from VNOI Wiki with small modification
// for speed might change to vector<Point>& p
vector<Point> convexHull(vector<Point> p) {
    int n = p.size();

    if (n < 3) {
        // cannot form convex hull
        return vector<Point>();
    }

    // SORT POINTS
    sort(p.begin(), p.end(), [](const Point &A, const Point &B) {
        if (A.x != B.x) return A.x < B.x;
        return A.y < B.y;
    });

    vector<Point> hull;
    hull.push_back(p[0]);

    // UPPER HULL
    for (int i = 1; i < n; ++i) {
        while (hull.size() >= 2 && ccw(hull[hull.size() - 2], hull.back(),
            p[i])) {
            hull.pop_back();
        }
        hull.push_back(p[i]);
    }

    // LOWER HULL
    for (int i = n - 2; i >= 0; --i) {
        while (hull.size() >= 2 && ccw(hull[hull.size() - 2], hull.back(),
            p[i])) {
            hull.pop_back();
        }
        hull.push_back(p[i]);
    }

    // REMOVE 1 OVERLAPPING
    if (n > 1) hull.pop_back();

    return hull;
}

```

4.5 geometry

```

#define pt pair<long long, long long>
#define x first
#define y second

struct Line {
    pt a, ab;
    Line(pt _a, pt _ab): a(_a), ab(_ab) {}
};

pt operator - (const pt& a, const pt& b) {return make_pair(a.x - b.x, a.y
    - b.y);}
ll operator * (const pt& a, const pt& b) {return a.x*b.x + a.y*b.y;}
ll operator ^ (const pt& a, const pt& b) {return a.x*b.y - a.y*b.x;}

pt refine(pt a) { // only for pt = pair<ll, ll>
    ll g = gcd(a.x, a.y);
    if (!g) return a;
    if (g < 0) g = -g;
    a.x /= g, a.y /= g;
    return a;
}

int dir(pt a, pt b, pt c) { // a -> b -> c
    ll x = (b - a) ^ (c - a);
    if (x == 0) return 0; // colinear
    else if (x > 0) return 1; // counterclockwise
    else return -1; // clockwise
}

```

4.6 matrix-mod

```

//Template from VNOI:
https://wiki.vnoi.info/algorithm/trick/matrix-multiplication with some
modification
// ofc this is 0-indexed
template<typename T>
struct matrix_mod {
    T add(T a, T b) {
        return ((a+MOD)%MOD + (b+MOD)%MOD)%MOD;
    }
    T mul(T a, T b) {

```

```

    a *= b;
    if (a > MOD) a %= MOD;
    return a;
}

vector <vector <T> > data;

int row() const { return data.size(); }
int col() const { return data[0].size(); }

auto & operator [] (int i) { return data[i]; }
const auto & operator [] (int i) const { return data[i]; }

matrix_mod() = default;
matrix_mod(int r, int c): data(r, vector <T> (c)) { }
matrix_mod(const vector <vector <T> > &d): data(d) {
    assert(d.size());
    int size = d[0].size();
    assert(size);
    for (auto x : d) assert(x.size() == size);
}

friend ostream & operator << (ostream &out, const matrix_mod &d) {
    for (auto x : d.data) {
        for (auto y : x) out << y << ' ';
        out << '\n';
    }
    return out;
}

static matrix_mod identity(long long n) {
    matrix_mod a = matrix_mod(n, n);
    while (n--) a[n][n] = 1;
    return a;
}

matrix_mod operator * (const matrix_mod &b) {
    matrix_mod a = *this;
    assert(a.col() == b.row());
    matrix_mod c(a.row(), b.col());
    for (int i = 0; i < a.row(); ++i)
        for (int j = 0; j < b.col(); ++j)
            for (int k = 0; k < a.col(); ++k)
                c[i][j] = add(c[i][j], mul(a[i][k], b[k][j]));
    return c;
}

```

```

matrix_mod pow(long long exp) {
    assert(row() == col());
    matrix_mod base = *this, ans = identity(row());
    for (; exp > 0; exp >>= 1, base = base * base)
        if (exp & 1) ans = ans * base;
    return ans;
}
};

```

4.7 modint

```

/*
 * Caution:
 * * need to cast into int before printing
 * source: Benq
*/
struct Mint {
    int v;
    explicit operator int() const { return v; }
    Mint() { v = 0; }
    Mint(long long _v) : v(_v % MOD) { v += (v < 0) * MOD; }
};

Mint &operator+=(Mint &a, Mint b) {
    if ((a.v += b.v) >= MOD) a.v -= MOD;
    return a;
}

Mint &operator-=(Mint &a, Mint b) {
    if ((a.v -= b.v) < 0) a.v += MOD;
    return a;
}

Mint operator+(Mint a, Mint b) { return a += b; }
Mint operator-(Mint a, Mint b) { return a -= b; }
Mint operator*(Mint a, Mint b) { return Mint((long long)a.v * b.v); }
Mint &operator*=(Mint &a, Mint b) { return a = a * b; }

Mint pow(Mint a, long long p) {
    assert(p >= 0);
    return p == 0 ? 1 : pow(a * a, p / 2) * (p & 1 ? a : 1);
}

Mint inv(Mint a) {
    assert(a.v != 0);
    return pow(a, MOD - 2);
}

```

```
Mint operator/(Mint a, Mint b) { return a * inv(b); }
```

5 rng

```
mt19937_64
    rng(chrono::high_resolution_clock::now().time_since_epoch().count());

inline long long rnd(long long l, long long r) {
    uniform_int_distribution<long long> dis(l, r);
    return dis(rng);
}
```

6 string

6.1 prefix-function

```
vector<int> prefix_function (const string& s) {
    int n = (int) s.length();
    vector<int> prefix(n, 0);
    for (int i = 1; i < n; i++) {
        int j = prefix[i - 1];
        while (j > 0 && s[i] != s[j]) j = prefix[j - 1];
        if (s[i] == s[j]) j++;
        prefix[i] = j;
    }
    return prefix;
}
```

6.2 rolling-hash

```
// rolling hash with one-based indexing
//
// usage Hash(s, BASE)
//
// query
//  hash.fwd(l, r) //get forward hash
//  hash.bwd(l, r) //get backward hash
```

```
struct Hash {
    int hash[N], hashR[N], pow[N];
    Hash(string &s, int BASE) {
        int n = s.size() - 1;
        hash[0] = 0;
        hashR[0] = 0;
        pow[0] = 1;
        for(int i = 1; i <= n; i++) {
            pow[i] = (pow[i - 1] * BASE) % MOD;
        }
        for(int i = 1; i <= n; i++) {
            hash[i] = (hash[i - 1] * BASE + s[i] - 'a' + 1) % MOD;
        }
        for(int i = n; i >= 1; i--) {
            hashR[i] = (hashR[i + 1] * BASE + s[i] - 'a' + 1) % MOD;
        }
    }
    int fwd(int i, int j) {
        return (hash[j] - hash[i - 1] * pow[j - i + 1] + MOD * MOD) % MOD;
    }
    int bwd(int i, int j) {
        return (hashR[i] - hashR[j + 1] * pow[j - i + 1] + MOD * MOD) % MOD;
    }
};
```

6.3 str-trie

```
struct str_trie {
    struct node {
        vector<int> nxt;
        int end;

        node(int n) {
            end = 0;
            nxt.assign(n, -1);
        }
    };

    int sz;
    vector<node> b;

    str_trie(int maxb = 0) {
        b.assign(maxb + 5, node(26));
    }
};
```

```
    sz = 0;
}

void add(string s) {
    int u = 0;
    for (char c : s) {
        if (b[u].nxt[c - 'a'] == -1) b[u].nxt[c - 'a'] = ++sz;
```

```
        u = b[u].nxt[c - 'a'];
    }
    b[u].end++;
}
};
```
