#### CS 106B

Lecture 10: Recursive

Backtracking 2:

Common Problem Types

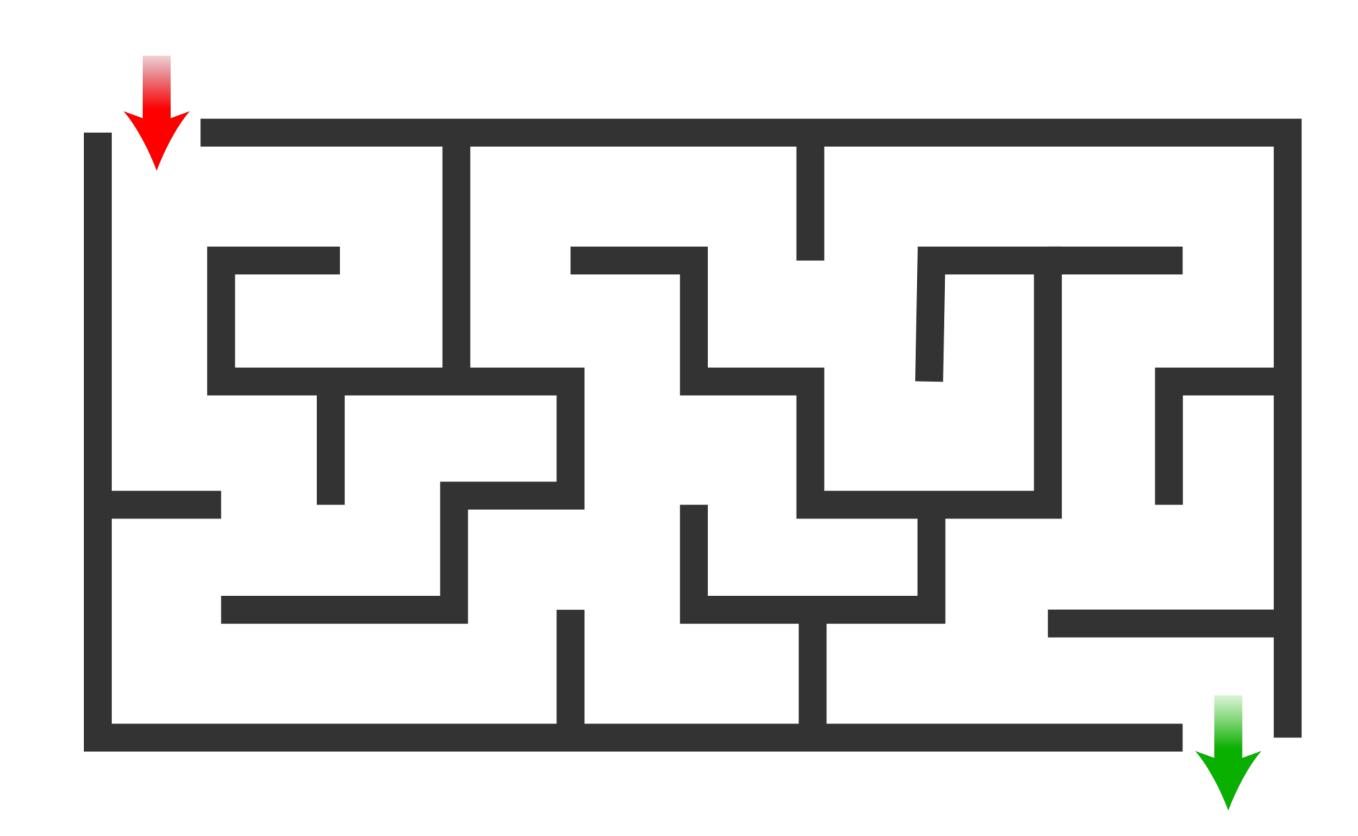
Monday, April 23, 2018

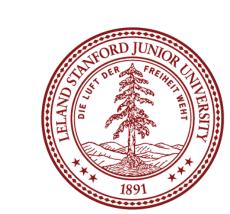
Programming Abstractions
Spring 2018
Stanford University
Computer Science Department

Lecturer: Chris Gregg

reading:

Programming Abstractions in C++, Chapter 8.2-8.3





# Today's Topics

- Logistics:
  - Due date for Assignment 3 (Recursion): Thursday, Noon
  - Practice midterm materials will be out by mid-week
  - Midterm will be on laptops! You must let me and Nick know now if you don't have a workable laptop or need other accommodations.
  - Today's handout: <a href="http://web.stanford.edu/class/cs106b/lectures/10-RecursiveBacktracking2/code/handout.pdf">http://web.stanford.edu/class/cs106b/lectures/10-RecursiveBacktracking2/code/handout.pdf</a>
- Common Problem Types for Recursive Backtracking
  - Partitionable (determine whether a solution exists)
  - Knapsack Problem (find the best solution)
  - Maze Solving (find a solution)
  - Clumsy Thumbsy (find all solutions)

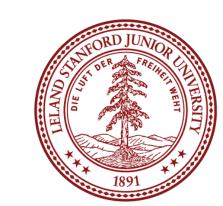


# Recursive Backtracking: Templates /



There are basically five different problems you might see that will require recursive backtracking:

- Determine whether a solution exists
- Find a solution
- Find the best solution
- Count the number of solutions
- Print/find all the solutions



Write a function named **partionable** that takes a vector of **ints** and returns **true** if it is possible to divide the **ints** into two groups such that each group has the same sum. For example, the **Vector** {1,1,2,3,5} can be split into {1,5} and {1,2,3}. However, the **vector** {1,4,5,6} can't be split into two.

bool partitionable(Vector<int>& nums) { ...



bool partitionable(Vector<int>& nums) { ...

This is our first example of recursive backtracking where we **make a change** and must restore some data before we can move on; otherwise, the solution degrades.

#### Basic idea:

- Keep track of the two sums! Must use helper function.
- Keep removing values from the Vector until we have no more values left (base case)
- Search each possible path

bool partitionable(Vector<int>& rest, int sum1, int sum2);

```
bool partitionable(Vector<int>& nums) {
    return partitionable(nums, 0, 0); // no sums yet
bool partitionable(Vector<int>& rest, int sum1, int sum2) {
```



CodeStepByStep

```
bool partitionable(Vector<int>& nums) {
    return partitionable(nums, 0, 0); // no sums yet
bool partitionable(Vector<int>& rest, int sum1, int sum2) {
    if (rest.isEmpty()) {
                                     base case: note the return value
        return sum1 == sum2;
    } else {
        int n = rest[0];
                              — adjust rest (must restore!!!)
        rest.remove(0);
        bool answer = partitionable(rest, sum1 + n, sum2)
                    or partitionable(rest, sum1, sum2 + n);
        rest.insert(0, n); —— here is the restoration
        return answer;
```

#### The Knapsack Problem: Find the best solution

One famous problem in theoretical computer science is the so-called knapsack problem. Given a target weight and a set of objects in which each object has a value and a weight, determine a subset of objects such that the sum of their weights is less than or equal to the target weight and the sum of their values is maximized.

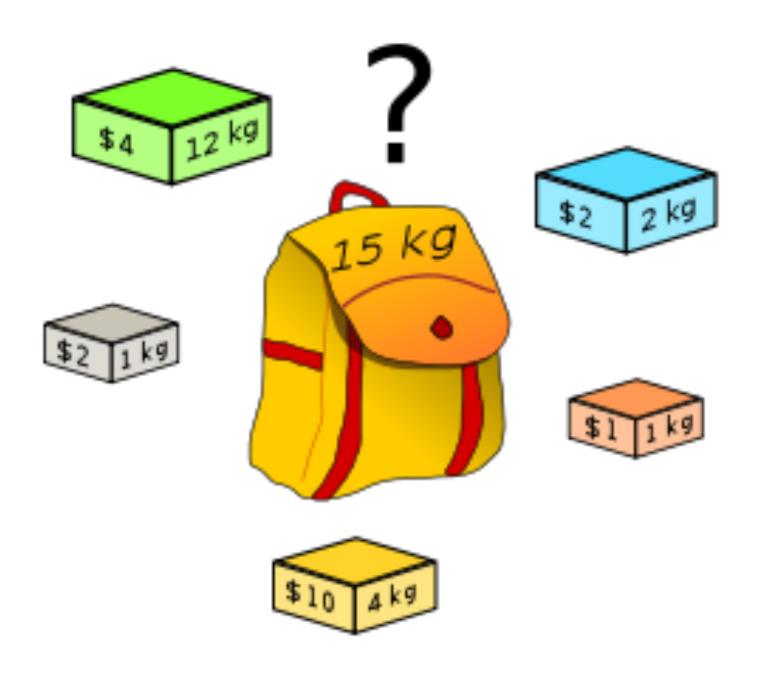


image courtesy of wikipedia.org



#### The Knapsack Problem: Find the best solution

For this problem we will represent an object with the following struct:

```
struct objectT {
    int weight; //You may assume this is greater than or equal to 0
    int value; //You may assume this is greater than or equal to 0
};
```

Let's write the function:

```
int fillKnapsack(Vector<objectT> &objects, int targetWeight)
```

that considers all possible combinations of **objectT** from objects (such that the sum of their weights is less than or equal to targetWeight) and returns the maximum possible sum of object values.

## The Knapsack Problem: Find the best solution

int fillKnapsack(Vector<objectT> &objects, int targetWeight)

#### Basic idea:

- Keep track of the weight and keep track of the best total value ("score").
- Loop over all items, adding value to the knapsack, and subtracting the weight of items from the total weight allowed.
- If the weight goes below zero, we have too many items.
- Must have a helper function!

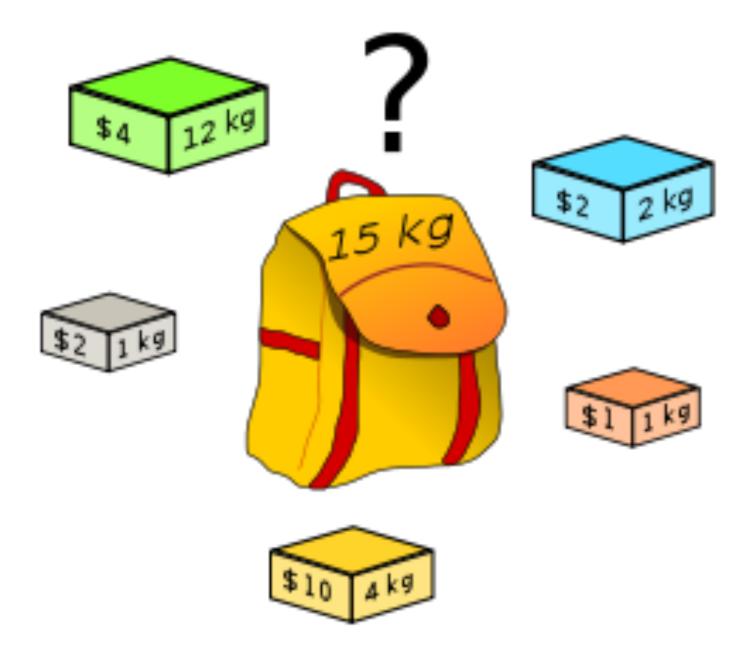


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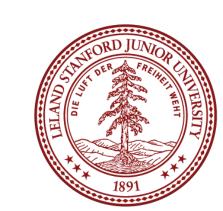
int fillKnapsack(Vector<objectT> &objects, int weight, int bestScore);



Setup struct and call to recursive function:

```
struct objectT {
    int weight; //You may assume this is greater than or equal to 0
    int value; //You may assume this is greater than or equal to 0
};

int fillKnapsack(Vector<objectT> &objects, int targetWeight) {
    return fillKnapsack(objects, targetWeight, 0);
}
```



```
int fillKnapsack(Vector<objectT> &objects, int weight, int bestScore) {
   if (weight < 0) return 0; // we tried too much weight!
        base case</pre>
```





```
int fillKnapsack(Vector<objectT> &objects, int weight, int bestScore) {
   if (weight < 0) return 0; // we tried too much weight!
   int localBestScore = bestScore;
   int obSize = objects.size();
   for (int i = 0; i < obSize; i++) {
      objectT originalObject = objects[i];
   int currValue = bestScore + originalObject.value;
   int currWeight = weight - originalObject.weight;</pre>
```



```
int filknapsack(Vector<objectT> &objects, int weight, int bestScore) {
   if (weight < 0) return 0; // we tried too much weight!
   int localBestScore = bestScore;
   int obSize = objects.size();
   for (int i = 0; i < obSize; i++) {
      objectT originalObject = objects[i];
      int currValue = bestScore + originalObject.value;
      int currWeight = weight - originalObject.weight;
      // remove object for recursion
      objects.remove(i);</pre>
```

remove the object we are looking at so we can recurse.



```
int fillKnapsack(Vector<objectT> &objects, int weight, int bestScore) {
    if (weight < 0) return 0; // we tried too much weight!</pre>
    int localBestScore = bestScore;
    int obSize = objects.size();
    for (int i = 0; i < obSize; i++) {</pre>
        objectT originalObject = objects[i];
        int currValue = bestScore + originalObject.value;
        int currWeight = weight - originalObject.weight;
        // remove object for recursion
        objects.remove(i);
                                                     remove the object we
                                                      are looking at so we
        // replace
                                                       can recurse. Must
        objects.insert(i,originalObject);
                                                    remember to replace it!
```

```
int fillKnapsack(Vector<objectT> &objects, int weight, int bestScore) {
    if (weight < 0) return 0; // we tried too much weight!</pre>
    int localBestScore = bestScore;
    int obSize = objects.size();
    for (int i = 0; i < obSize; i++) {</pre>
        objectT originalObject = objects[i];
        int currValue = bestScore + originalObject.value;
        int currWeight = weight - originalObject.weight;
        // remove object for recursion
        objects.remove(i);
        currValue = fillKnapsack(objects,currWeight,currValue);
        if (localBestScore < currValue) {</pre>
                                                     remove the object we
            localBestScore = currValue;
                                                are looking at so we
        // replace
                                                      can recurse. Must
        objects.insert(i,originalObject);
                                                    remember to replace it!
```

```
int fillKnapsack(Vector<objectT> &objects, int weight, int bestScore) {
    if (weight < 0) return 0; // we tried too much weight!</pre>
    int localBestScore = bestScore;
    int obSize = objects.size();
    for (int i = 0; i < obSize; i++) {</pre>
        objectT originalObject = objects[i];
        int currValue = bestScore + originalObject.value;
        int currWeight = weight - originalObject.weight;
        // remove object for recursion
        objects.remove(i);
        currValue = fillKnapsack(objects,currWeight,currValue);
        if (localBestScore < currValue) {</pre>
            localBestScore = currValue;
        // replace
        objects.insert(i,originalObject);
    return localBestScore; we return the local best score
```



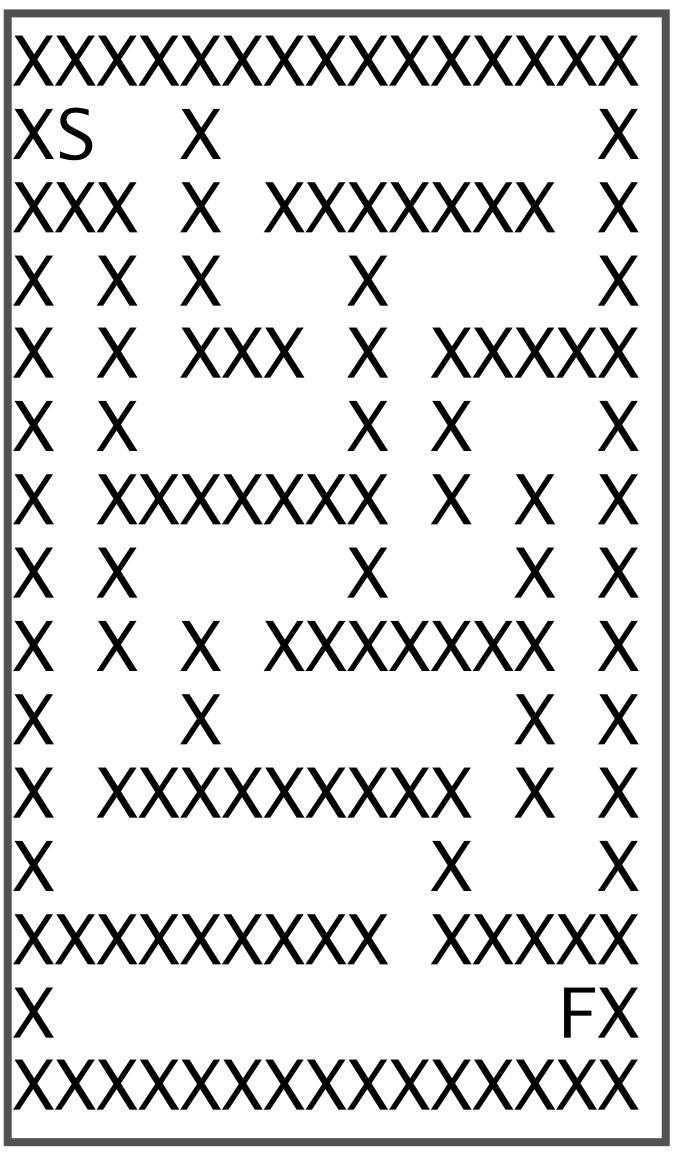
### Maze Solving: Find a Solution

- A classic example of backtracking is solving a maze: if you go down one path and it isn't the correct path, then you backtrack to your last decision point to try an alternate path.
- If you are using an object passed by reference you need to either *undo* (or "un-choose") paths that fail, or somehow mark them in your object.
- For a maze, you don't want to try and traverse the same path twice, so you need to mark whether you have been down that path before.



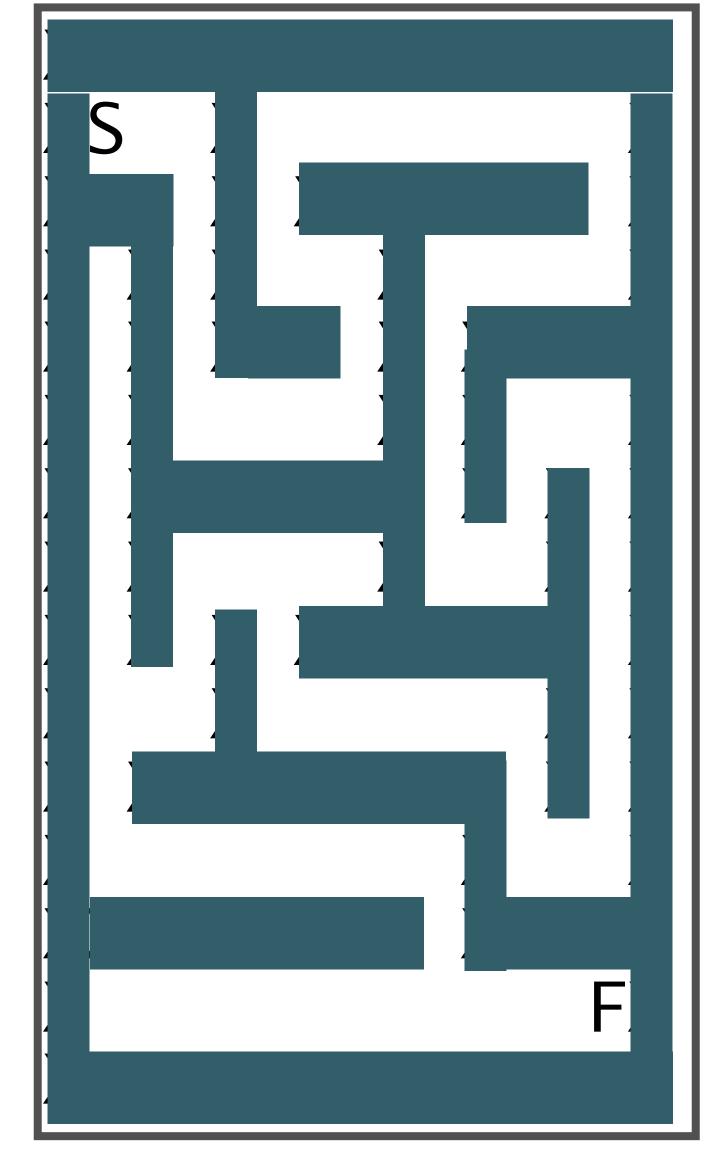


- The code for today's class includes a text-based recursive maze creator and solver.
- The mazes look like the one to the right
  - There is a Start (marked with an "S") and a Finish (marked with an "F").
  - The Xs represent walls, and the spaces represent paths to walk through the maze.



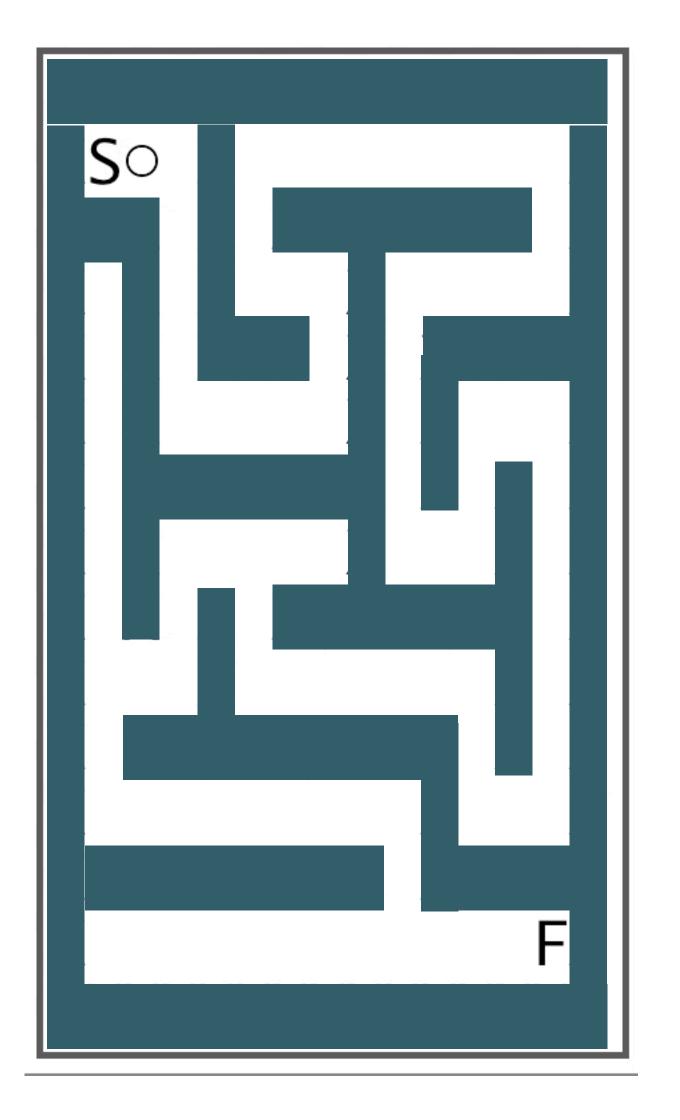


Let's make it a bit easier to see on the screen:

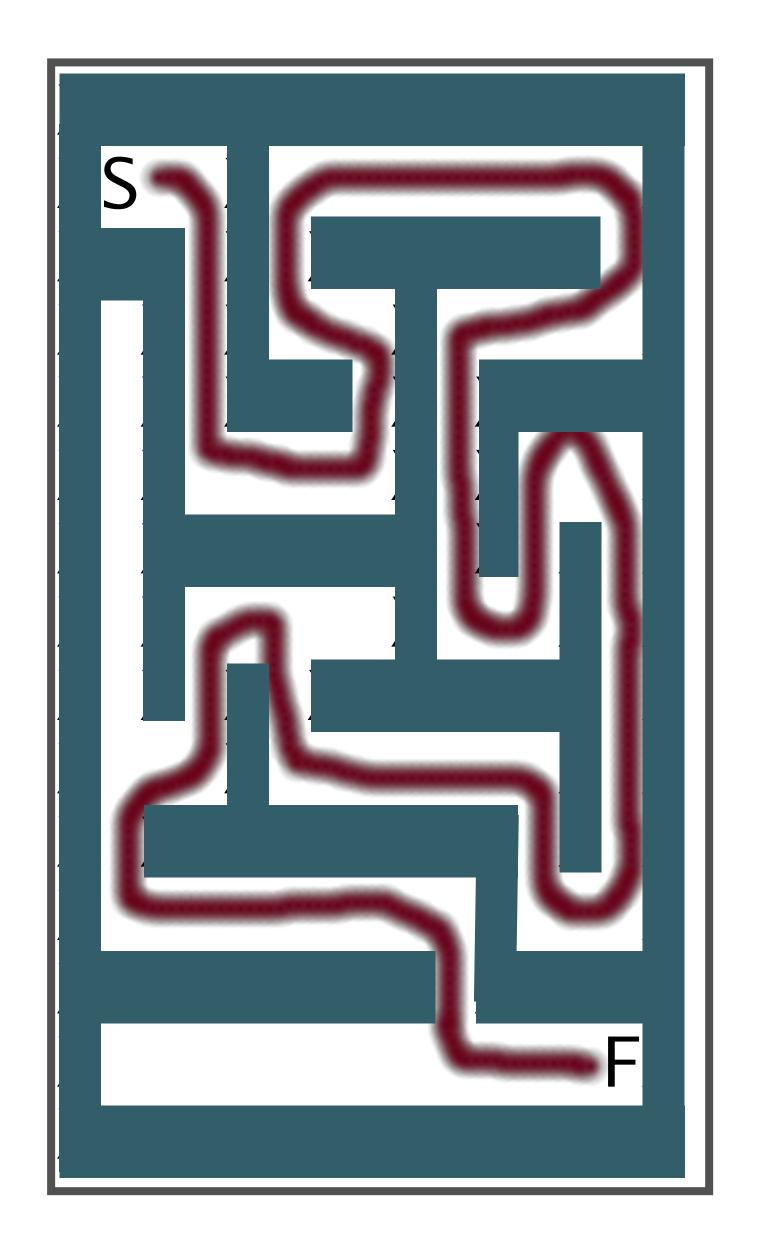




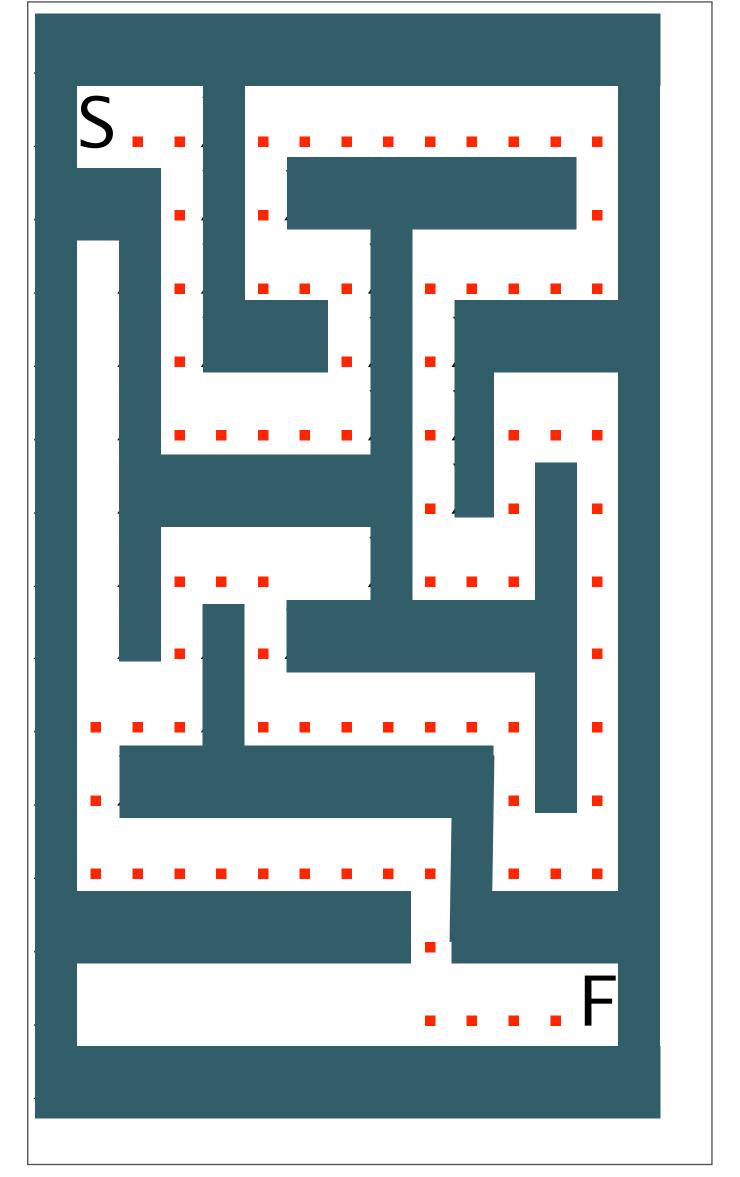
• The solution to the maze is shown here (video):



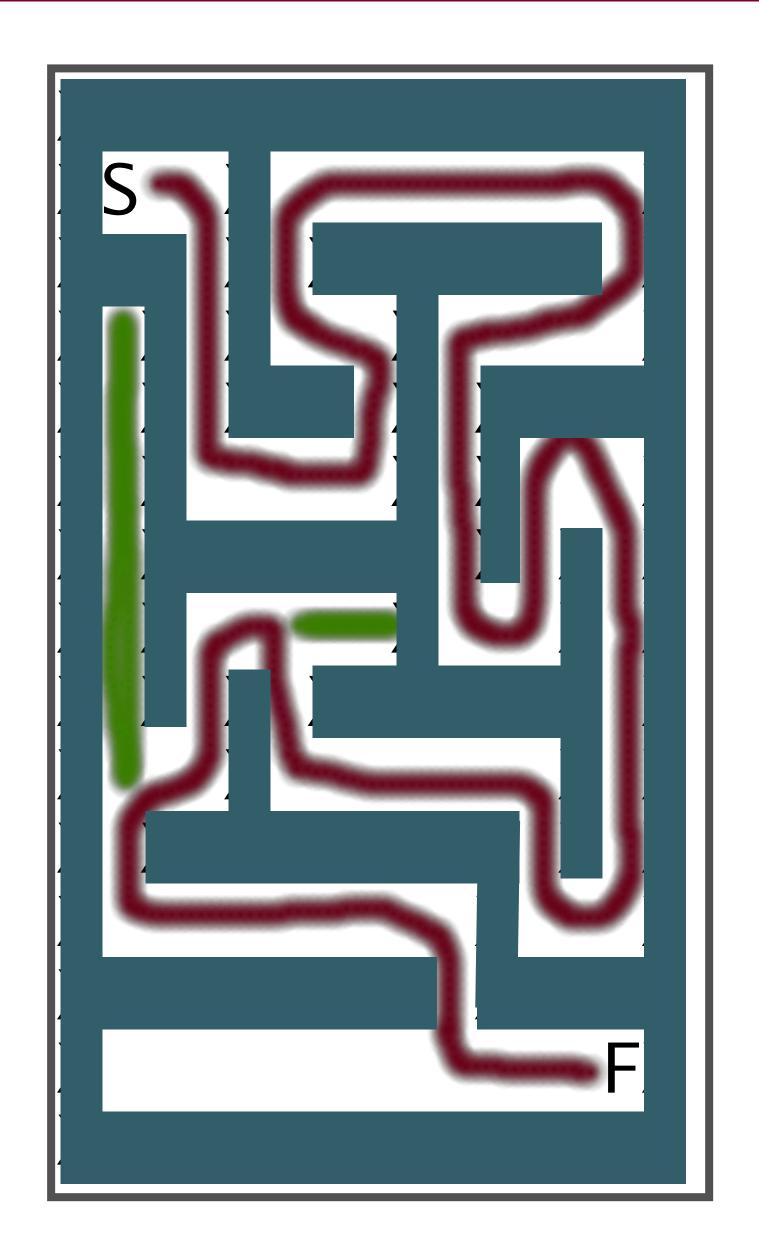




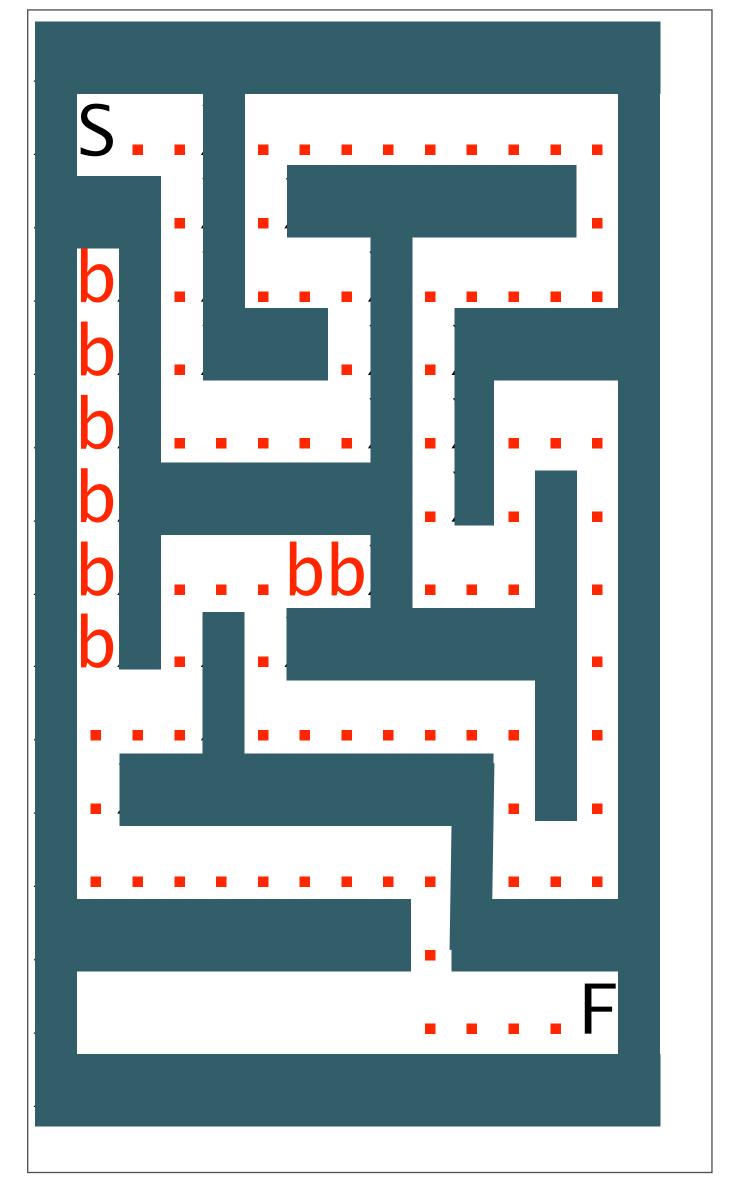
 The program will put dots in the correct positions.





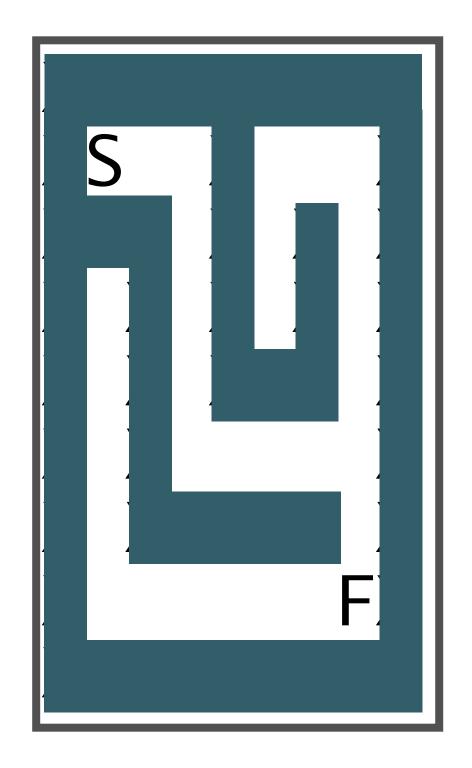


- The program will put dots in the correct positions.
- But, it will also put lowercase b's when it goes in the wrong direction and has to backtrack.



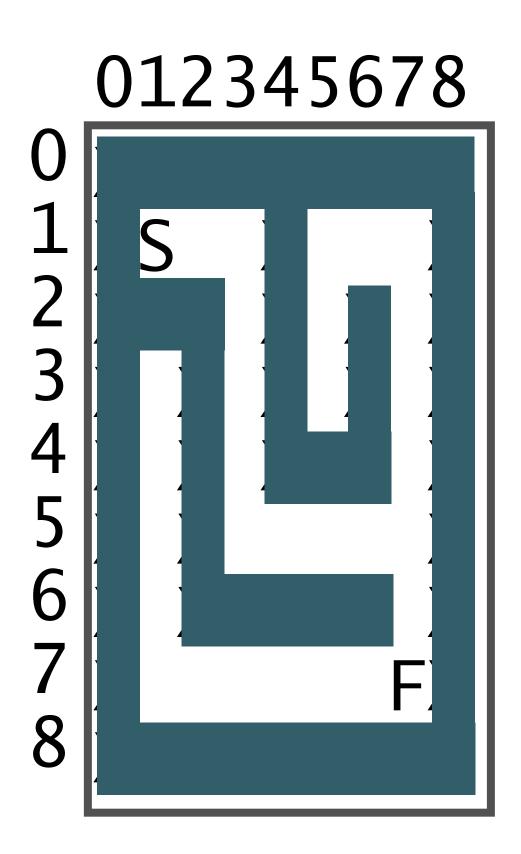


- What are some actual methods for solving a maze?
  - "Hand on a wall" -- put one hand on a wall at the start and keep following. Eventually you will reach the finish (circular paths may disrupt this method).
  - Break through walls (best for Corn Mazes)
  - Backtracking! Keep track of where you've been, and systematically test all solutions. Pick compass directions in order (e.g., N/E/S/W), returning to check other paths when you hit dead ends and have tried all combinations.
- Let's use the backtracking method to solve the maze to the right
   -- we will go N/E/S/W, from the Start.



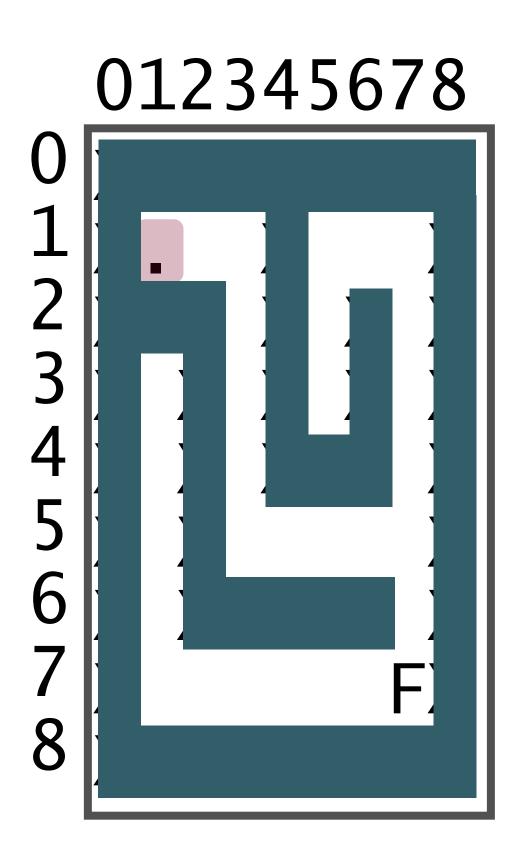


 We will mark positions we have seen with a period ('.'), and mark backtracking with 'b'.



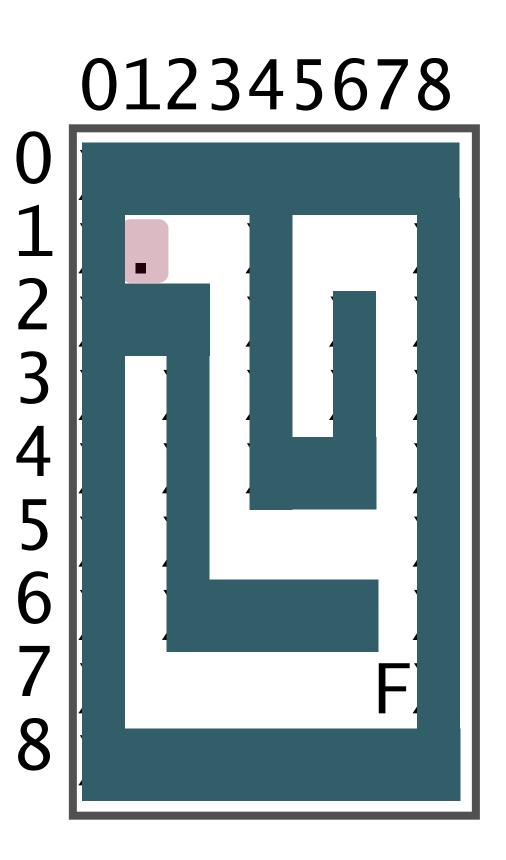


- We will mark positions we have seen with a period ('.'), and mark backtracking with 'b'.
- Start: row=1 and col=1, Marking with period (.)



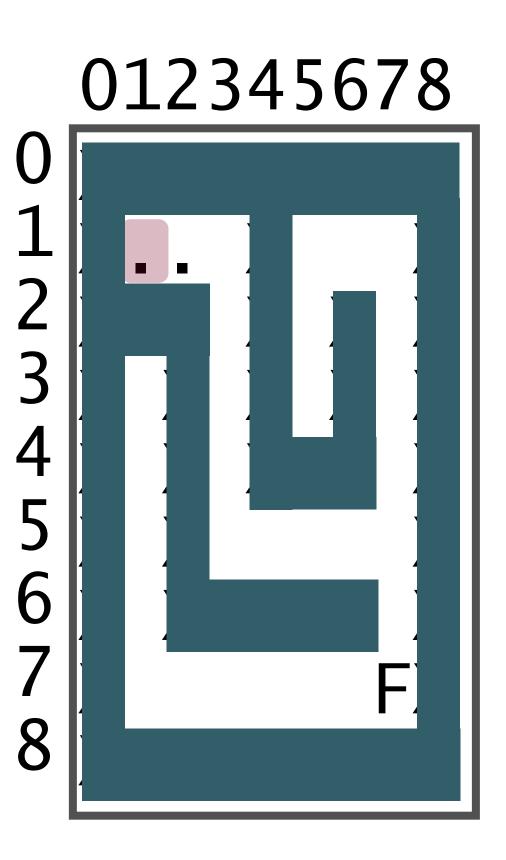


- We will mark positions we have seen with a period ('.'), and mark backtracking with 'b'.
- Start: row=1 and col=1, Marking with period (.)
- We have to try all paths, N/E/S/W, and if we hit a wall ('X'), we can't go that direction.
- Trying north, row=0 and col=1, Hit wall! Back at row=1 and col=1,
- Trying east, row=1 and col=2, Marking with period (.)



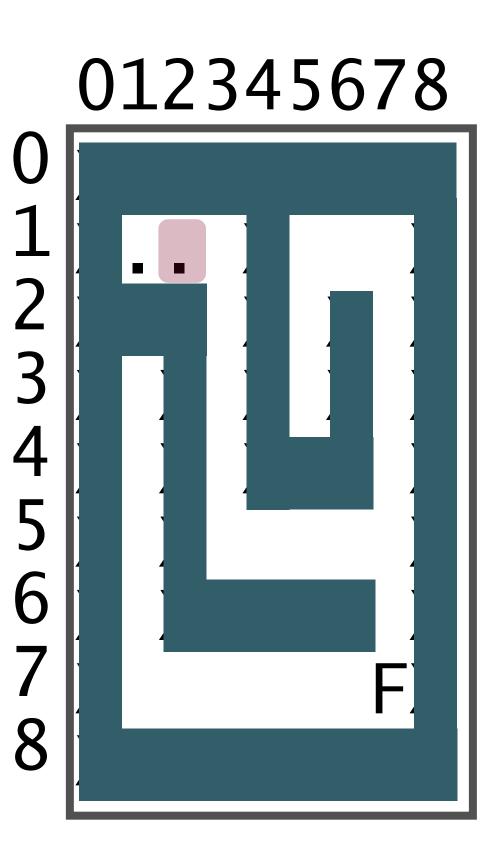


- We will mark positions we have seen with a period ('.'), and mark backtracking with 'b'.
- Start: row=1 and col=1, Marking with period (.)
- We have to try all paths, N/E/S/W, and if we hit a wall ('X'), we can't go that direction.
- Trying north, row=0 and col=1, Hit wall! Back at row=1 and col=1,
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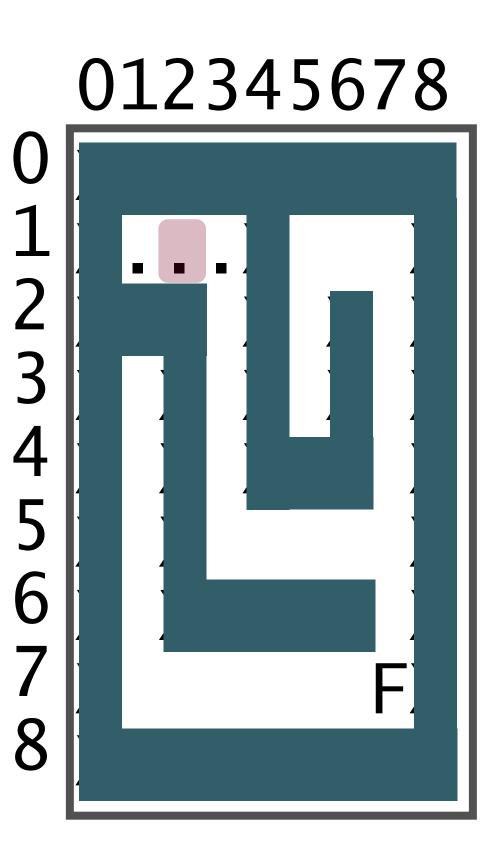


- We will mark positions we have seen with a period ('.'), and mark backtracking with 'b'.
- Start: row=1 and col=1, Marking with period (.)
- We have to try all paths, N/E/S/W, and if we hit a wall ('X'), we can't go that direction.
- Trying north, row=0 and col=1, Hit wall! Back at row=1 and col=1,
- Trying east, row=1 and col=2, Marking with period (.)
- Trying north, row=0 and col=2, Hit wall! Back at row=1 and col=2,
- Trying east, row=1 and col=3, Marking with period (.)



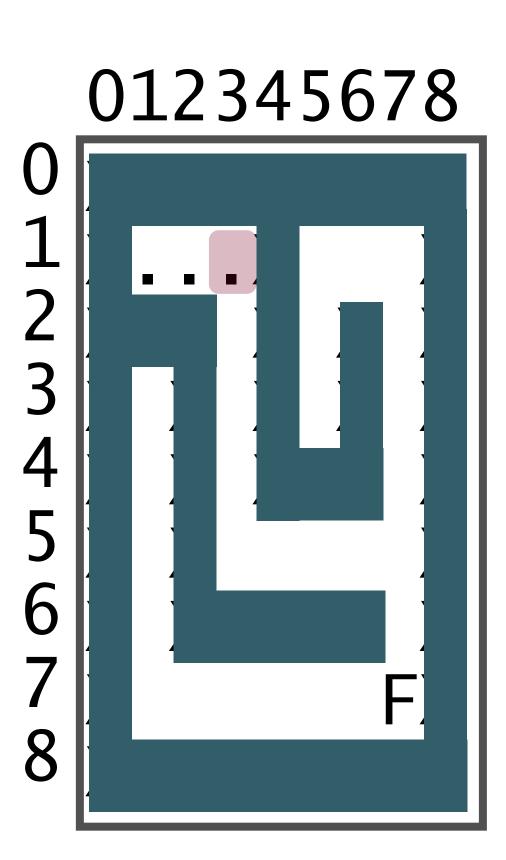


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- Start: row=1 and col=1, Marking with period (.)
- We have to try all paths, N/E/S/W, and if we hit a wall ('X'), we can't go that direction.
- Trying north, row=0 and col=1, Hit wall! Back at row=1 and col=1,
- Trying east, row=1 and col=2, Marking with period (.)
- Trying north, row=0 and col=2, Hit wall! Back at row=1 and col=2,
- Trying east, row=1 and col=3, Marking with period (.)



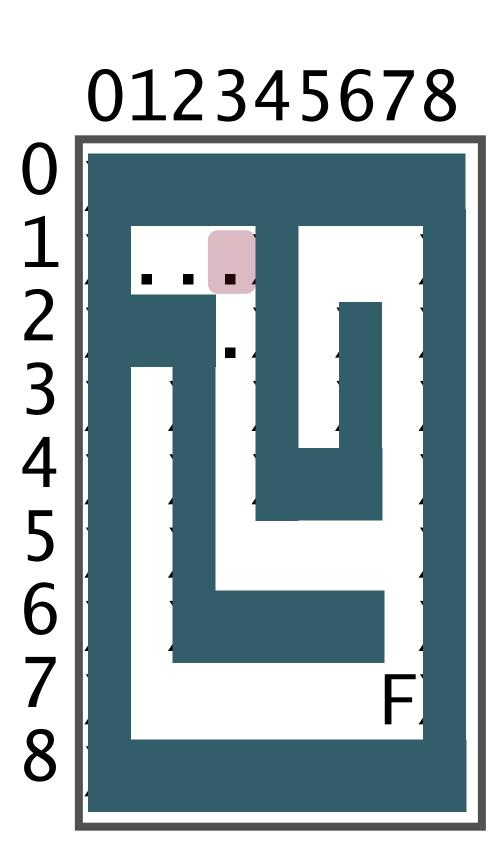


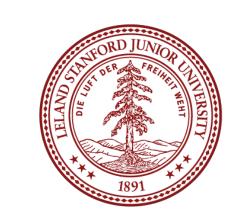
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- Start: row=1 and col=1, Marking with period (.)
- We have to try all paths, N/E/S/W, and if we hit a wall ('X'), we can't go that direction.
- Trying north, row=0 and col=1, Hit wall! Back at row=1 and col=1,
- Trying east, row=1 and col=2, Marking with period (.)
- Trying north, row=0 and col=2, Hit wall! Back at row=1 and col=2,
- Trying east, row=1 and col=3, Marking with period (.)
- Trying north, row=0 and col=3, Hit wall! Back at row=1 and col=3,
- Trying east, row=1 and col=4, Hit wall! Back at row=1 and col=3,
- Trying south, row=2 and col=3, Marking with period (.)



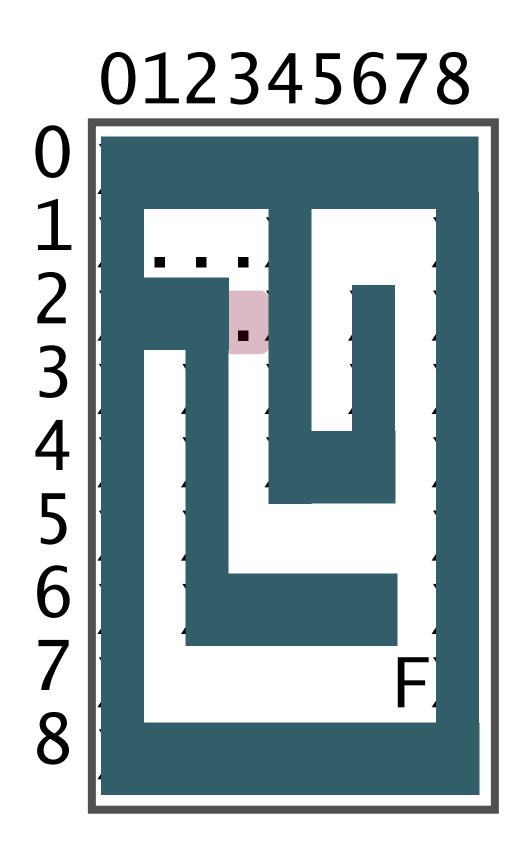


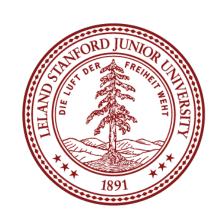
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- Trying east, row=1 and col=2, Marking with period (.)
- Trying north, row=0 and col=2, Hit wall! Back at row=1 and col=2,
- Trying east, row=1 and col=3, Marking with period (.)
- Trying north, row=0 and col=3, Hit wall! Back at row=1 and col=3,
- Trying east, row=1 and col=4, Hit wall! Back at row=1 and col=3,
- Trying south, row=2 and col=3, Marking with period (.)



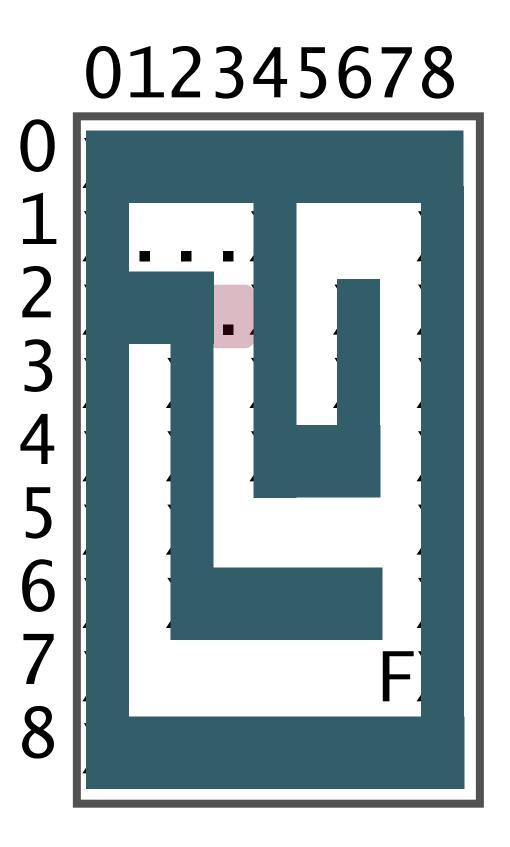


• Trying north, row=1 and col=3, We came from here! Back at row=2 and col=3,



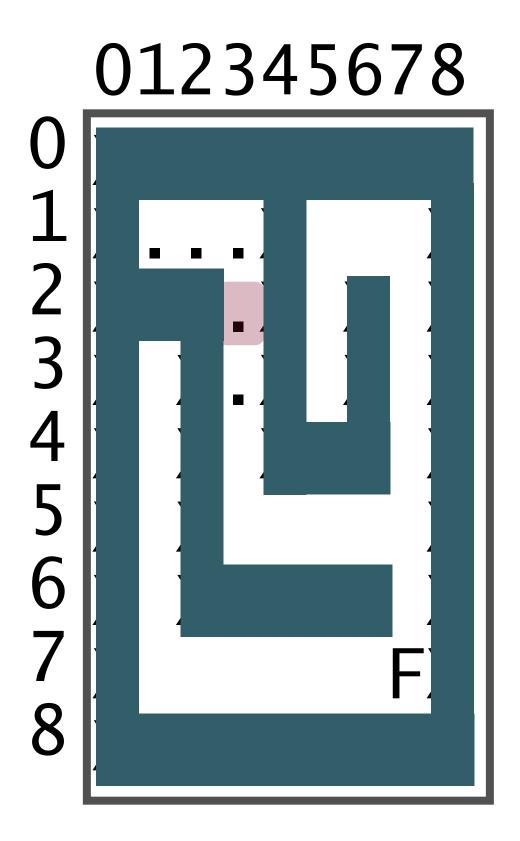


- Trying north, row=1 and col=3, We came from here! Back at row=2 and col=3,
- Trying east, row=2 and col=4, Hit wall! Back at row=2 and col=3,
- Trying south, row=3 and col=3, Marking with period (.)



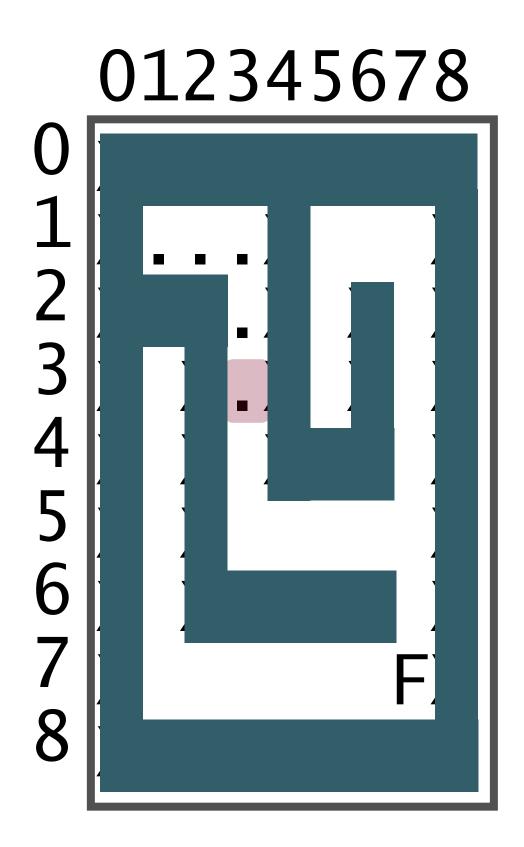


- Trying north, row=1 and col=3, We came from here! Back at row=2 and col=3,
- Trying east, row=2 and col=4, Hit wall! Back at row=2 and col=3,
- Trying south, row=3 and col=3, Marking with period (.)





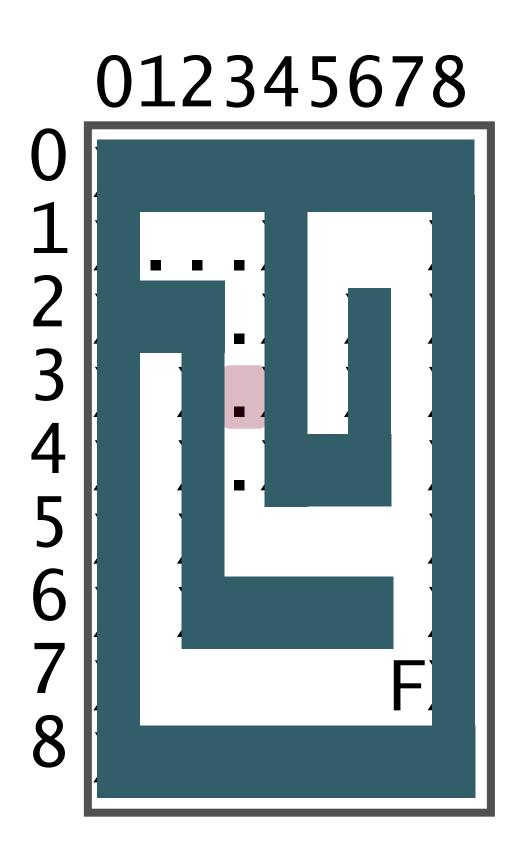
- Trying north, row=1 and col=3, We came from here! Back at row=2 and col=3,
- Trying east, row=2 and col=4, Hit wall! Back at row=2 and col=3,
- Trying south, row=3 and col=3, Marking with period (.)
- Trying north, row=2 and col=3, We came from here! Back at row=3 and col=3,
- Trying east, row=3 and col=4, Hit wall! Back at row=3 and col=3,
- Trying south, row=4 and col=3, Marking with period (.)





- Trying north, row=1 and col=3, We came from here! Back at row=2 and col=3,
- Trying east, row=2 and col=4, Hit wall! Back at row=2 and col=3,
- Trying south, row=3 and col=3, Marking with period (.)
- Trying north, row=2 and col=3, We came from here! Back at row=3 and col=3,
- Trying east, row=3 and col=4, Hit wall! Back at row=3 and col=3,
- Trying south, row=4 and col=3, Marking with period (.)

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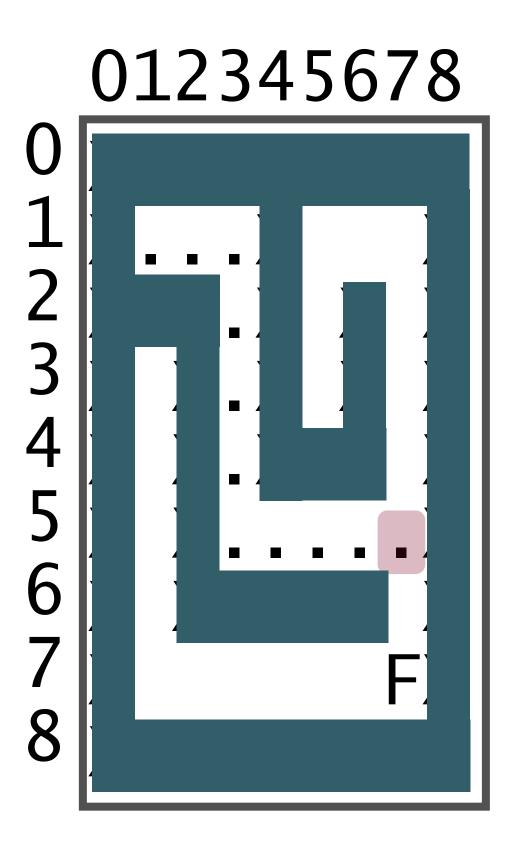




- Trying north, row=1 and col=3, We came from here! Back at row=2 and col=3,
- Trying east, row=2 and col=4, Hit wall! Back at row=2 and col=3,
- Trying south, row=3 and col=3, Marking with period (.)
- Trying north, row=2 and col=3, We came from here! Back at row=3 and col=3,
- Trying east, row=3 and col=4, Hit wall! Back at row=3 and col=3,
- Trying south, row=4 and col=3, Marking with period (.)

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What happens here?



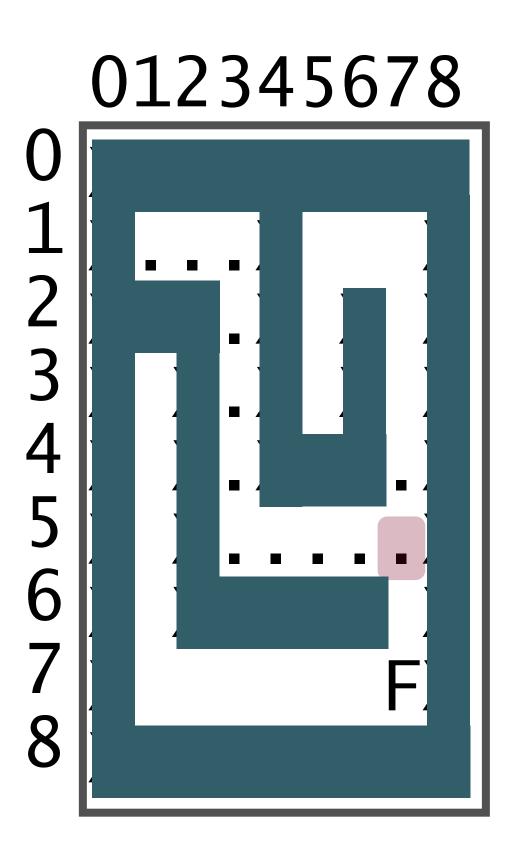


- Trying north, row=1 and col=3, We came from here! Back at row=2 and col=3,
- Trying east, row=2 and col=4, Hit wall! Back at row=2 and col=3,
- Trying south, row=3 and col=3, Marking with period (.)
- Trying north, row=2 and col=3, We came from here! Back at row=3 and col=3,
- Trying east, row=3 and col=4, Hit wall! Back at row=3 and col=3,
- Trying south, row=4 and col=3, Marking with period (.)

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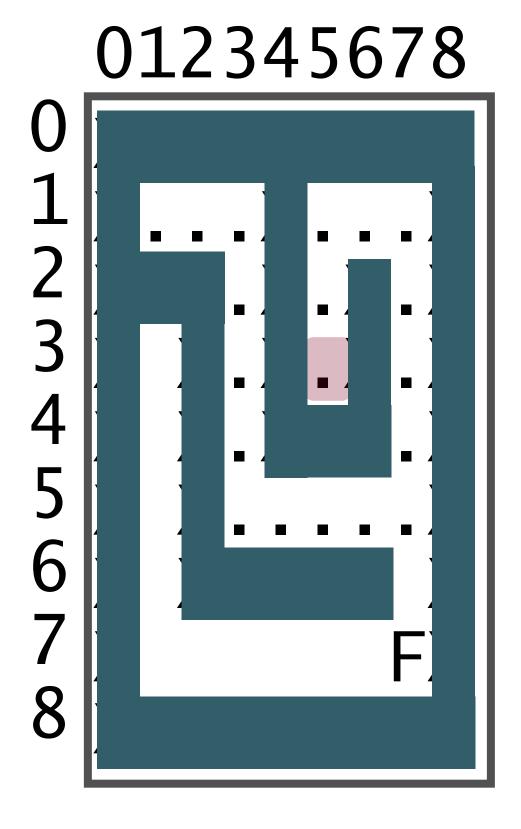
What happens here?

Bummer. We check North first, so we start going up.



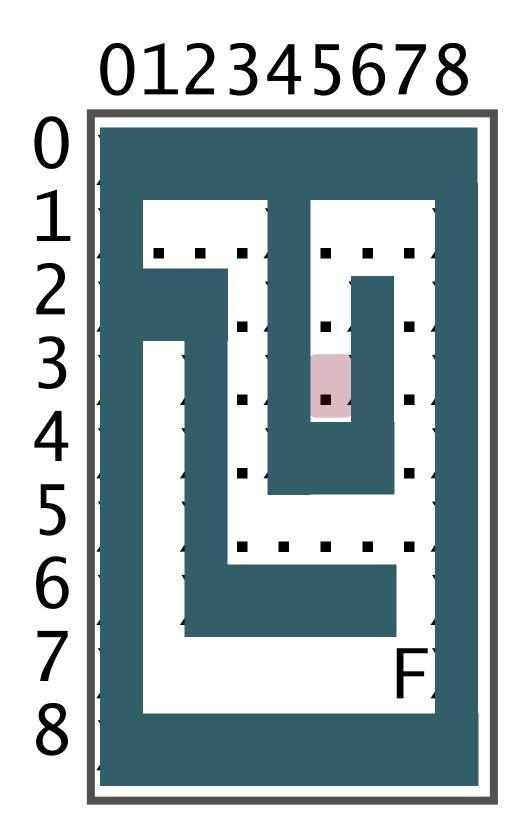


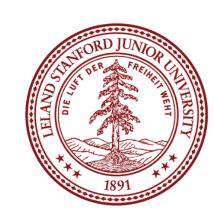
Now what?





- Trying north, row=2 and col=5, We came from here! Back at row=3 and col=5,
- Trying east, row=3 and col=6, Hit wall! Back at row=3 and col=5,
- Trying south, row=4 and col=5, Hit wall! Back at row=3 and col=5,
- Trying west, row=3 and col=4, Hit wall! Back at row=3 and col=5,
- Failed. Marking bad path with b. Back at row=2 and col=5,

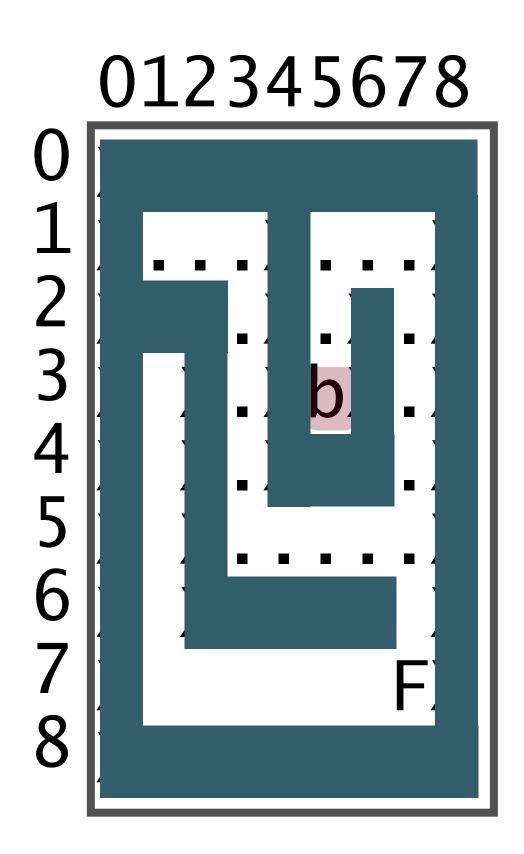




- Trying north, row=2 and col=5, We came from here! Back at row=3 and col=5,
- Trying east, row=3 and col=6, Hit wall! Back at row=3 and col=5,
- Trying south, row=4 and col=5, Hit wall! Back at row=3 and col=5,
- Trying west, row=3 and col=4, Hit wall! Back at row=3 and col=5,
- Failed. Marking bad path with b. Back at row=2 and col=5,

What is next?

How did we get here? From the North, meaning we checked South to get here. So, we now check West (remember, we are checking N/E/S/W)



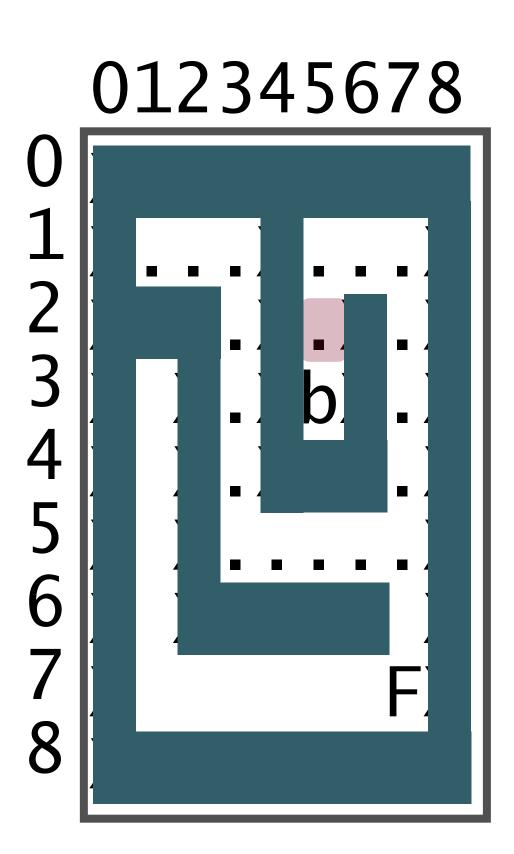


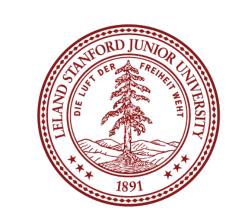
- Trying north, row=2 and col=5, We came from here! Back at row=3 and col=5,
- Trying east, row=3 and col=6, Hit wall! Back at row=3 and col=5,
- Trying south, row=4 and col=5, Hit wall! Back at row=3 and col=5,
- Trying west, row=3 and col=4, Hit wall! Back at row=3 and col=5,
- Failed. Marking bad path with b. Back at row=2 and col=5,

What is next?

How did we get here? From the North, meaning we checked South to get here. So, we now check West (remember, we are checking N/E/S/W)

Trying west, row=2 and col=4, Hit wall! Back at row=2 and col=5, Failed. Marking bad path with b. Back at row=1 and col=5,



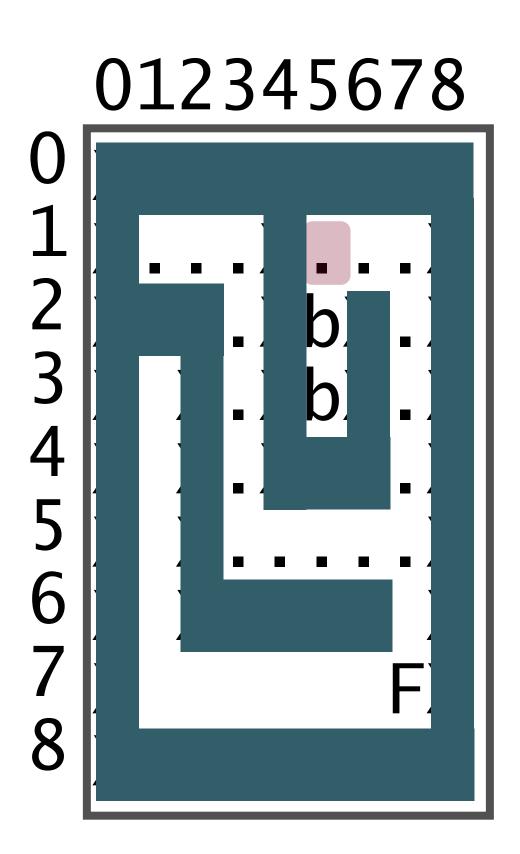


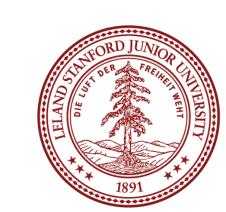
- Trying north, row=2 and col=5, We came from here! Back at row=3 and col=5,
- Trying east, row=3 and col=6, Hit wall! Back at row=3 and col=5,
- Trying south, row=4 and col=5, Hit wall! Back at row=3 and col=5,
- Trying west, row=3 and col=4, Hit wall! Back at row=3 and col=5,
- Failed. Marking bad path with b. Back at row=2 and col=5,

What is next?

How did we get here? From the North, meaning we checked South to get here. So, we now check West (remember, we are checking N/E/S/W)

Trying west, row=2 and col=4, Hit wall! Back at row=2 and col=5, Failed. Marking bad path with b. Back at row=1 and col=5,





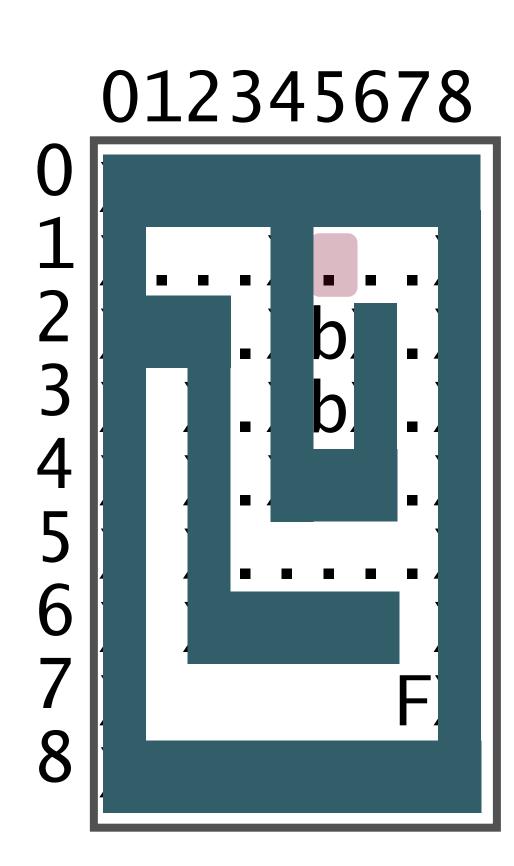
- Trying north, row=2 and col=5, We came from here! Back at row=3 and col=5,
- Trying east, row=3 and col=6, Hit wall! Back at row=3 and col=5,
- Trying south, row=4 and col=5, Hit wall! Back at row=3 and col=5,
- Trying west, row=3 and col=4, Hit wall! Back at row=3 and col=5,
- Failed. Marking bad path with b. Back at row=2 and col=5,

What is next?

How did we get here? From the North, meaning we checked South to get here. So, we now check West (remember, we are checking N/E/S/W)

Trying west, row=2 and col=4, Hit wall! Back at row=2 and col=5, Failed. Marking bad path with b. Back at row=1 and col=5,

Now, we are "remembering" where we have been because we've been keeping track of our positions and what we last checked at a given position -- we will use recursion to do this!





- Trying north, row=2 and col=5, We came from here! Back at row=3 and col=5,
- Trying east, row=3 and col=6, Hit wall! Back at row=3 and col=5,
- Trying south, row=4 and col=5, Hit wall! Back at row=3 and col=5,
- Trying west, row=3 and col=4, Hit wall! Back at row=3 and col=5,
- Failed. Marking bad path with b. Back at row=2 and col=5,

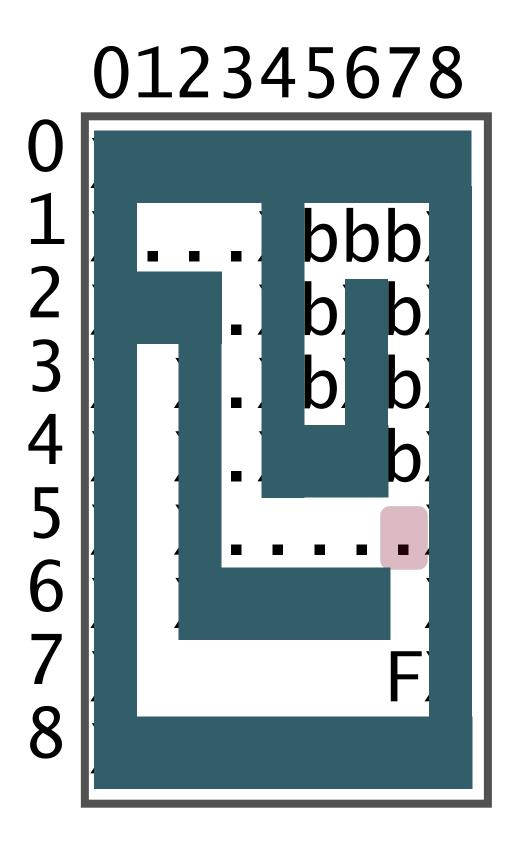
What is next?

How did we get here? From the North, meaning we checked South to get here. So, we now check West (remember, we are checking N/E/S/W)

Trying west, row=2 and col=4, Hit wall! Back at row=2 and col=5, Failed. Marking bad path with b. Back at row=1 and col=5,

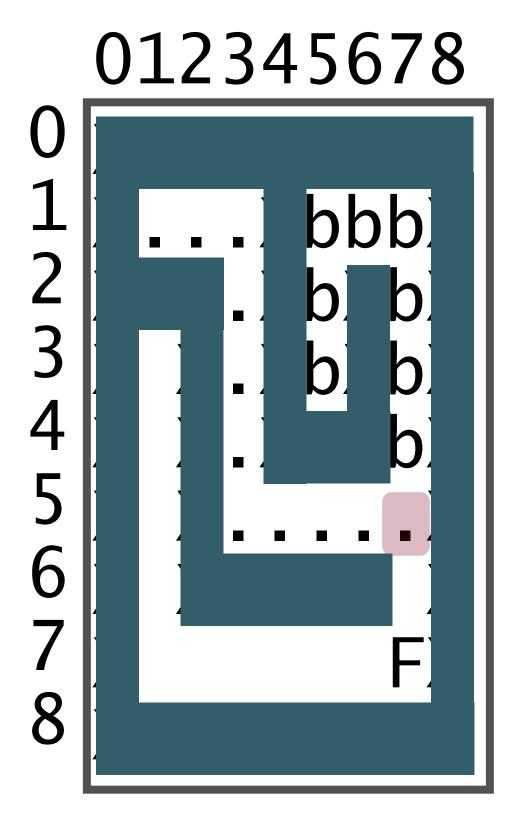
Now, we are "remembering" where we have been because we've been keeping track of our positions and what we last checked at a given position -- we will use recursion to do this!

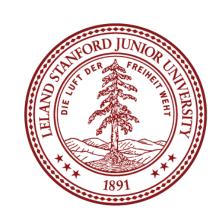
We will arrive back at row=5, col=7 quickly.



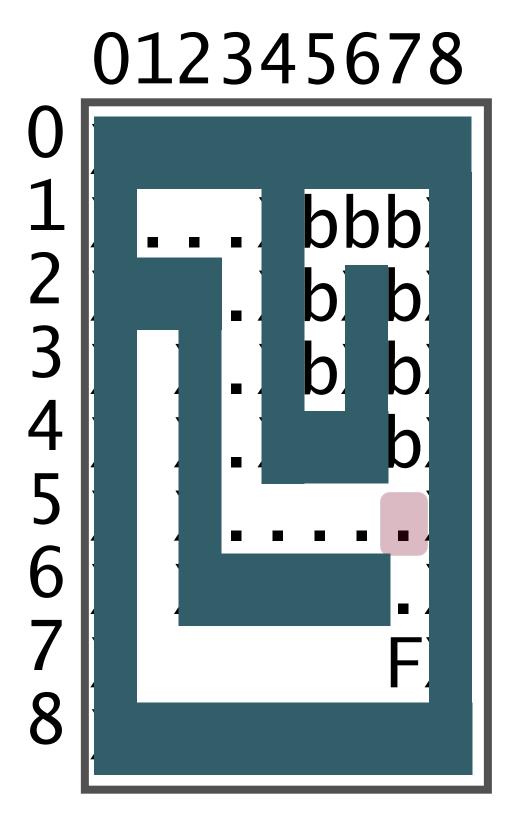


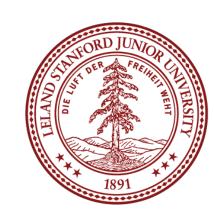
- Trying east, row=5 and col=8, Hit wall! Back at row=5 and col=7,
- Trying south, row=6 and col=7, Marking with period (.)



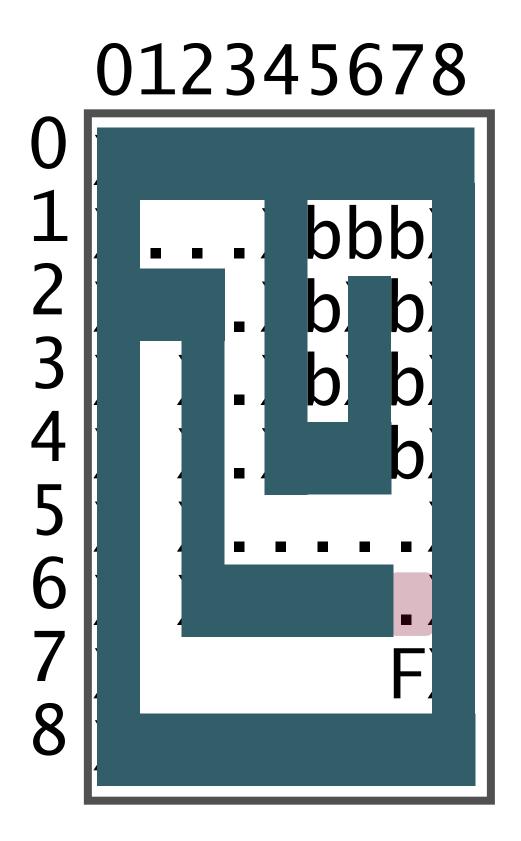


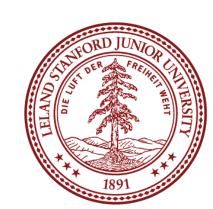
- Trying east, row=5 and col=8, Hit wall! Back at row=5 and col=7,
- Trying south, row=6 and col=7, Marking with period (.)



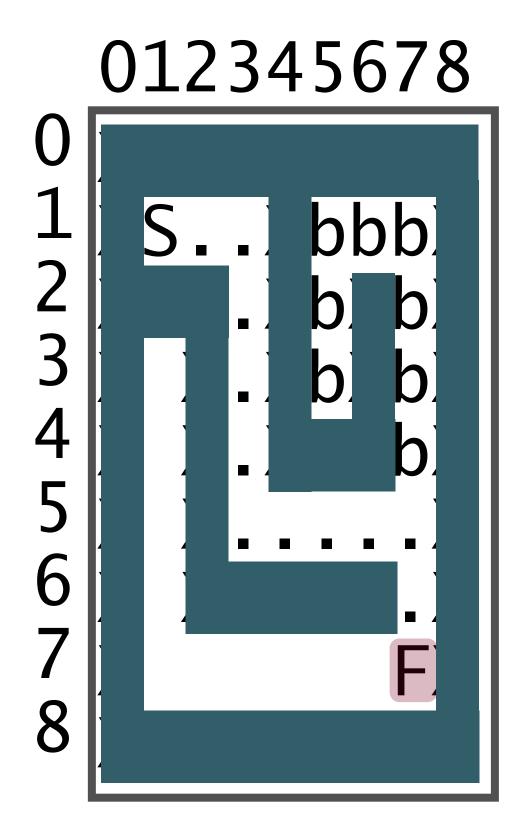


- Trying east, row=5 and col=8, Hit wall! Back at row=5 and col=7,
- Trying south, row=6 and col=7, Marking with period (.)
- Trying north, row=5 and col=7, We came from here! Back at row=6 and col=7,
- Trying east, row=6 and col=8, Hit wall! Back at row=6 and col=7,
- Trying south, row=7 and col=7, Found the Finish!





- Trying east, row=5 and col=8, Hit wall! Back at row=5 and col=7,
- Trying south, row=6 and col=7, Marking with period (.)
- Trying north, row=5 and col=7, We came from here! Back at row=6 and col=7,
- Trying east, row=6 and col=8, Hit wall! Back at row=6 and col=7,
- Trying south, row=7 and col=7, Found the Finish!



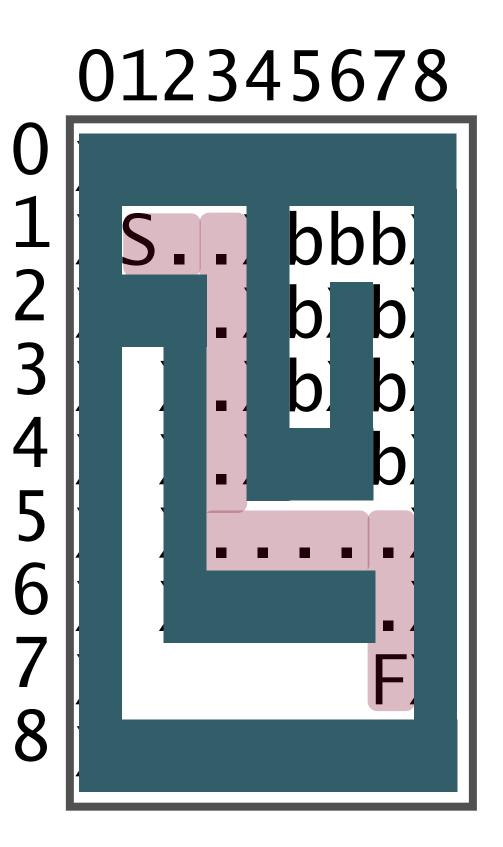


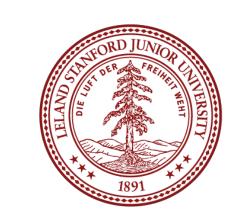
- Trying east, row=5 and col=8, Hit wall! Back at row=5 and col=7,
- Trying south, row=6 and col=7, Marking with period (.)
- Trying north, row=5 and col=7, We came from here! Back at row=6 and col=7,
- Trying east, row=6 and col=8, Hit wall! Back at row=6 and col=7,
- Trying south, row=7 and col=7, Found the Finish!

#### The total number of steps: 71!

That seems like a lot of steps to solve such a small maze, but remember, we are going through a methodical process that must check all paths.

(see extra slides for all steps for this maze)

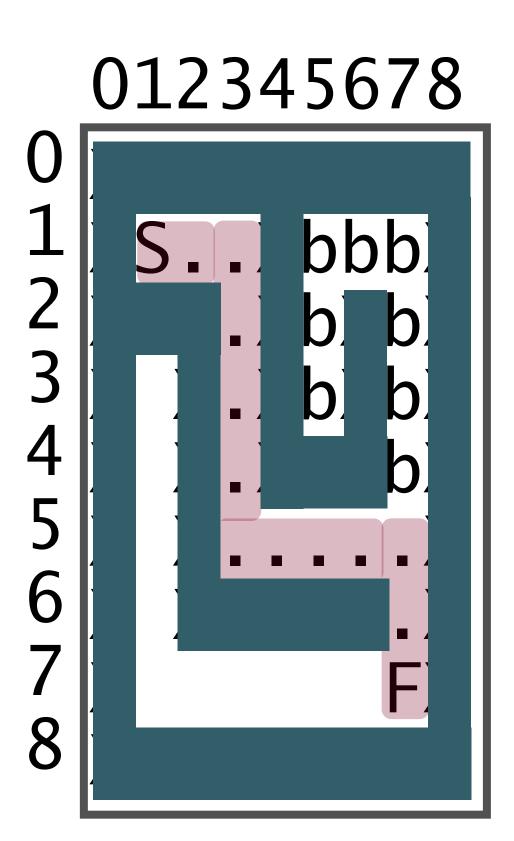




- Our recursive backtracking method for solving mazes must follow the same rules for all recursion:
- (1) have a case for all valid inputs,
- (2) must have base cases,
- (3) make forward progress towards the base case.

#### Let's start with the base cases. How many are there?

- (1) If we go out of the bounds of the maze (the grid bounds).
  - This actually won't happen for our mazes, because we have surrounded all paths with walls.
- (2) If we hit a backtracked position ('b')
  - •Also won't happen, because once we mark as backtracked, we'll never get there again.
- (3) If we hit a wall ('X')
- (4) If we hit a position we have seen before ('.')
- (5) If we find the finish ('F')

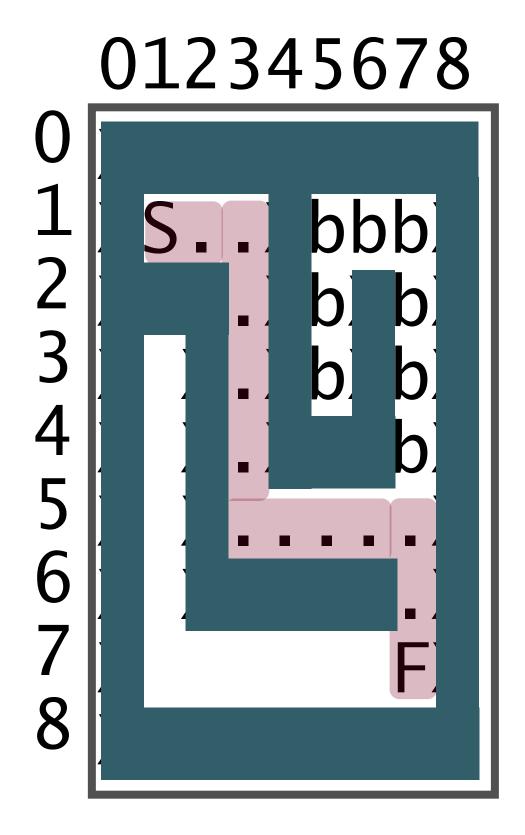




#### Base cases:

Returning **true** means we have solved the maze!
Returning **false** means that this path does not solve the maze.

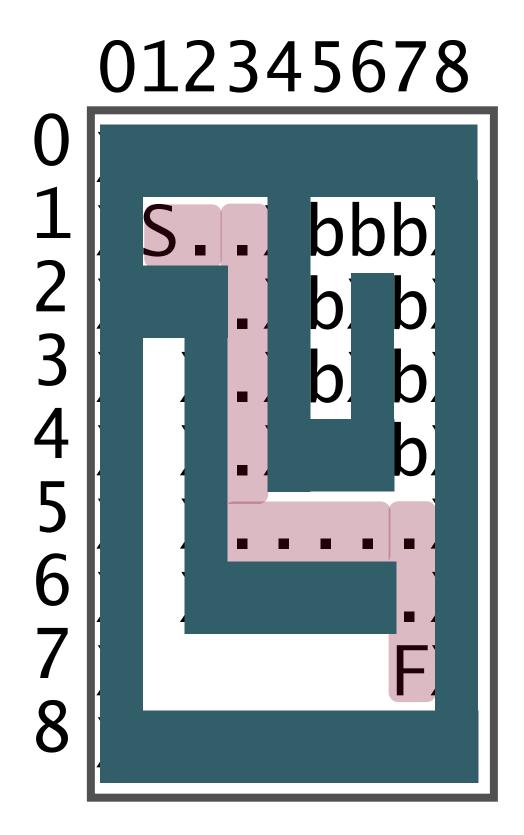
```
bool solveMazeRecursive(int row, int col, Grid<int> &maze) {
    if (maze[row][col] == 'X') {
        return false;
    if (maze[row][col] == '.') {
        return false;
       (maze[row][col] == 'F') {
        return true;
```





Once we take care of our base cases, we'd better mark the position we are at!

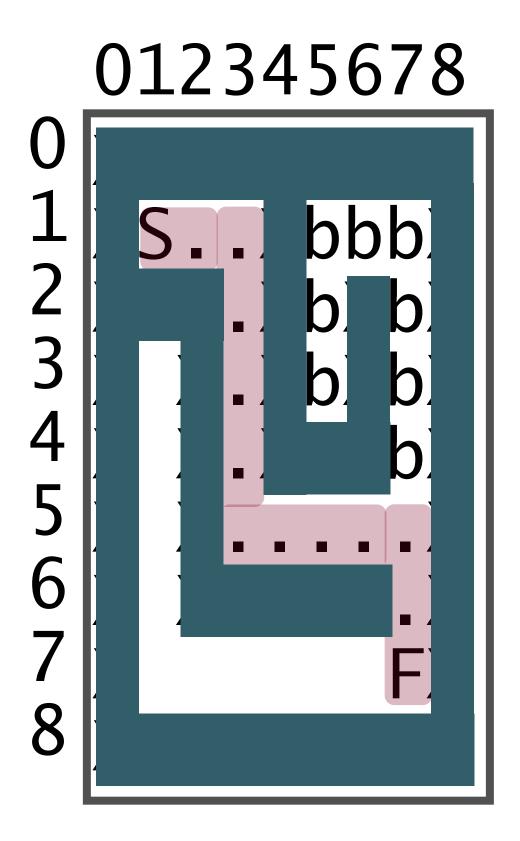
```
bool solveMazeRecursive(int row, int col, Grid<int> &maze) {
    if (maze[row][col] == 'X') {
        return false;
    if (maze[row][col] == '.') {
        return false;
       (maze[row][col] == 'F') {
        return true;
    maze[row][col] = '.';
```

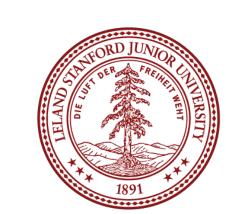




Now we can recurse -- we have to check all directions!

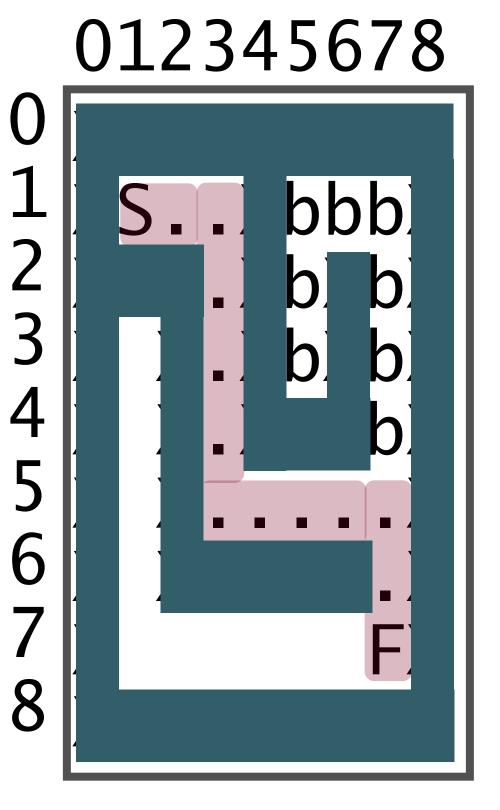
```
bool solveMazeRecursive(int row, int col, Grid<int> &maze) {
    maze[row][col] = '.';
    // Recursively call solveMazeRecursivePrint(row,col)
    // for north, east, south, and west
    // If one of the positions returns true, then return true
    // north
    if (solveMazeRecursivePrint(row-1,col,maze)) {
        return true;
```





All four recursions. If all four return, we have to backtrack!

```
bool solveMazeRecursive(int row, int col, Grid<int> &maze) {
   // north
    if (solveMazeRecursive(row-1,col,maze)) {
        return true;
    // east
    if (solveMazeRecursive(row,col+1,maze)) {
        return true;
    // south
    if (solveMazeRecursive(row+1,col,maze)) {
        return true;
    // west
       (solveMazeRecursive(row,col-1,maze)) {
        return true;
    maze[row][col] = 'b';
    return false;
```





You want to write a program that will autocorrect words.

Given a string that represents a single (potentially misspelled) word, a lexicon of English words, a map that maps from a character to a string of the characters near it on a keyboard, and an admissible number of errors, find the Set of all potential intended words.

(Problem courtesy of Jerry Cain)



Prototype (note the whitespace -- no need to have this be a giant line!)

First, we have to think of how we will solve this...



Prototype (note the whitespace -- no need to have this be a giant line!)

Definition: "maxTypos": how many letters we can have incorrect

#### Idea:

- Build up new potential words one character at a time until we have a word (or not).
- Replace all letters with their near-letters.
- Can also choose not to replace a letter!
- Base cases: if we have exhausted our max typos, or if the prefix of the word is not in the dictionary, or if we have built up to a word and it is in the dictionary

Prototype (note the whitespace -- no need to have this be a giant line!)

We are going to need a helper function to keep track of the remaining letters, the built-up string, the other reference parameters, and the maxTypos.



## Clumsy Thumbsy: Base Cases

```
Set<string> result;
if (allowableTypos < 0 || !dictionary.containsPrefix(builtUp)) {</pre>
    // too many typos, or no potential to build word
    return result; //empty set
} else if (remaining == "") {
    if (dictionary.contains(builtUp)) {
        // if word, add it to set
        result.add(builtUp);
    return result;
```





## Clumsy Thumbsy: Recursive Cases

```
char curr = remaining[0];
string rest = remaining.substr(1);
for (int i = 0; i < (int)nearLetters[curr].length(); i++) {</pre>
    result += autocorrect(rest, nearLetters, dictionary,
                          allowableTypos - 1, builtUp + nearLetters[curr][i]);
//can also choose not to change character
result += autocorrect(rest, nearLetters, dictionary,
                      allowableTypos, builtUp + curr);
return result;
```





#### References and Advanced Reading

#### References:

- Understanding permutations: <a href="http://stackoverflow.com/questions/7537791/">http://stackoverflow.com/questions/7537791/</a>
   understanding-recursion-to-generate-permutations
- Maze algorithms: <a href="https://en.wikipedia.org/wiki/Maze\_solving\_algorithm">https://en.wikipedia.org/wiki/Maze\_solving\_algorithm</a>

#### •Advanced Reading:

- Exhaustive recursive backtracking: <a href="https://see.stanford.edu/materials/icspacs106b/">https://see.stanford.edu/materials/icspacs106b/</a>
   h19-recbacktrackexamples.pdf
- Backtracking: <a href="https://en.wikipedia.org/wiki/Backtracking">https://en.wikipedia.org/wiki/Backtracking</a>



## Extra Slides

