

KSU / AdaCore / Altran Praxis Discussions on Enhancing Information Flow Framework of SPARK

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Goals

Make SPARK the language of choice for certified embedded information assurance systems by adding “developer support” and enhanced information flow specification verification

- Phase I:
 - IDE support for information flow browsing & querying based on existing SPARK information flow framework
 - Require no changes to underlying semantics and annotations
- Phase II:
 - High-level information flow policy language for specifying domains, allowable flows between domains
 - Requires minimal changes to underlying semantics and annotations
- Phase III:
 - Conditional information flow / conditional declassification
 - Requires moderate changes to underlying semantics and annotations
- Phase IV:
 - Precise array frame conditions and information flow
 - Requires substantial changes to underlying semantics and annotations

Phase I - Technical Background

- Two algorithms for reasoning about information flow within the existing derives framework
 - Bergeretti and Carre “matrix” approach used in Examiner
 - Conventional “program dependence graph” data-dependence / control-dependence used in KSU info flow browsing components
- Both of these compute same results and have the same correctness properties
- Neither of these directly support more precise reasoning needed for conditional flow or precise array flows

Phase I - Flow Browsing

- Intra-procedural forwards/backwards slice
- Inter-procedural forwards/backwards slice
- Developer selects
 - Program statement
 - Procedure parameter / global
 - Variable in a derives annotation
- Tool calculates
 - Incoming flows or outgoing flows (based on choice of forward/backward)

Basic Info Flow Browsing



Bakar automatically marks the lines and input vars from which information flows into Response.

```
180
181
182
183
184 procedure Add
185   ID : Value
186   Response : 
187   --# global in out Item_List, Next_List, Free_Head, Used_Head;
188   --# derives Item_List from ID, Value, Item_List, Next_List,
189   --#           Free_Head, Used_Head &
190   --#           Response, Next_List, Free_Head, Used_Head from
191   --#           ID, Item_List, Next_List, Free_Head, Used_Head;
192   is
193     Curr_Index : Link_Type;
194     Temp_Value : ArraySetDefs.Value_Type;
195     Found : Boolean;
196   begin
197     if ID /= ArraySetDefs.Null_ID then
198       if Free_Head /= Terminator then
199         Get_Value(ID, Temp_Value, Found);
200         if not Found then
201           Curr_Index := Free_Head;
202           Free_Head := Next_List(Free_Head);
203           Item_List(Curr_Index).ID := ID;
204           Item_List(Curr_Index).Value := Value;
205           Next_List(Curr_Index) := Used_Head;
206           Used_Head := Curr_Index;
207           Response := ArraySetDefs.DB_Success;
208         else
209           Response := ArraySetDefs.DB_Already_Exists;
210         end if;
211       else
212         Response := ArraySetDefs.DB_No_Room;
213       end if;
214     else
215       Response := ArraySetDefs.DB_Input_Check_Fail;
216     end if;
217   end Add;
```

Developer highlights RESPONSE and selects "Backward Flow" visualization.

Phase I - Derives Support

- Automatically calculate and insert derives clauses into code
 - Per procedure
 - Per package
 - Entire program
- Derives clause refactoring
 - Allow user to select if changes made in derives lower in the call tree propagate to derives contracts for procedures higher in call tree

ArraySet.adb X Insert annotations

```
154 procedure Get_Value
155     (ID      : in ArraySetDefs.ID_Type;
156      Value    : out ArraySetDefs.Value_Type;
157      Found    : out Boolean)
158
159     --# global in Item_List, Next_List, Used_Head;           -- generated
160     --# derives Value from Item_List, Next_List, Used_Head, ID & -- generated
161     --#          Found from Item_List, Next_List, Used_Head, ID;   -- generated
162     is
163         Curr_Index : Link_Type;
164 begin
165     Value := ArraySetDefs.Null_Value;
166     Curr_Index := Used_Head;
167     Found := False;
168     while not Found and then
169         if Item_List (Curr_Index) then
170             Value := Item_List (Curr_Index);
171             Found := True;
172         else
173             Curr_Index := Next_List (Curr_Index);
174         end if;
175     end loop;
```

Bakar automatically infers an information flow contract for a given subprogram implementation

Info Flow Contract
(Derives Clause)
Autogeneration

What should my info flow contract be for this procedure?



Phase I - Security Domain Highlighting

- Allow colors to be associated with declared security domains
- Developer can request visualization of program statements/variables that manipulate data from selected domains

MLS Flow Markup



Show me all variables and statements in my program that manipulate top secret data

Given an initial tagging of input variables according to security level, SpAda propagates and marks up source code to indicate MLS level of statement/variable

The screenshots show the Eclipse IDE with the SpAda plugin open. The code editor displays a procedure P1 with various statements and variables. Red boxes highlight parts of the code where Top Secret data is manipulated. Orange boxes highlight parts where High data is manipulated. Yellow boxes highlight parts where Low data is manipulated. Green boxes highlight parts where Public data is manipulated. The tool also shows a 'Generated Code' pane and a 'Resource' pane.

Principals Security Lattice

A1	Top Secret	
A2	High	
A3	Low	
...		
An	Public	

MLS security lattice with color mark-up tags

(not yet implemented -- target May 2009)

Phase I - Named Queries

Provide a simple information flow “scripting language” (inspired by CodeSurfer / Indus)

- Allow developers/auditors to name/save common information flow queries
- Can be used to support declaration of high-level information flow policies
 - Certain flow never overlap / intersect
 - Certain program features and contained within specified flows
- Can also be used to support partitioning of code by criticality levels (e.g., code that provides safety-critical calculations vs code that performs logging)

Info Flow Contract (Derives Clause) Autogeneration



I'd like to name and save my common queries...

Bakar provides a simple query language that be used to define common queries/policies

Can reuse the results of one query in other

The screenshot shows a software interface with two windows. The top window is titled 'mailbox-rv3.adb' and contains Ada code for 'WRITE_OUTPUT_1' and 'MACHINE_STEP' procedures. The bottom window is titled 'QueryView' and displays a table of queries with their names, values, and expressions.

```
procedure WRITE_OUTPUT_1(Data : in INTEGER) is
begin
    INTEGER_OUTPUT_1_DATA := Data;
end WRITE_OUTPUT_1;

procedure MACHINE_STEP
is
    DATA_0 : INTEGER;
    DATA_1 : INTEGER;
begin
    if INPUT_0_READY and OUTPUT_1_CONSUMED then
        DATA_0 := READ_INPUT_0;
        NOTIFY_INPUT_0_CONSUMED;
        WRITE_OUTPUT_1(DATA_0);
        NOTIFY_OUTPUT_1_READY;
    end if;
    if INPUT_1_READY and OUTPUT_0_CONSUMED then
        DATA_1 := READ_INPUT_1;
        NOTIFY_INPUT_1_CONSUMED;
        WRITE_OUTPUT_0(DATA_1);
        NOTIFY_OUTPUT_0_READY;
    end if;
end MACHINE_STEP;
```

Query Name	Value	Expression
pathA_1	38	slice FORWARD with {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_INPUT_1_DATA)}
pathB_0	38	slice FORWARD with {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_INPUT_0_DATA)}
pathA_0	68	slice BACKWARD with {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_OUTPUT_0_DATA)}
pathB_1	75	slice BACKWARD with {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_OUTPUT_1_DATA)}
pathA1_0	17	chop FULL from {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_INPUT_1_DATA)} to {body}
pathB0_1	17	chop FULL from {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_INPUT_0_DATA)} to {body}
A_B	true	assert (pathA_1 DISJOINT pathB_0)
AintersectA	18	pathA_1 INTERSECTION pathA_0
AintersectB		pathA_1 INTERSECTION pathB_0
A1_0_B0_1	true	assert (pathA1_0 DISJOINT pathB0_1)

Info Flow Contract (Derives Clause) Autogeneration



Bakar provides a simple query language that be used to define common queries/policies

The image shows a software interface with two main windows. The top window is titled "mailbox-rv3.adb" and contains Ada code for a "MAILBOX" package. The bottom window is titled "QueryView" and displays a table of queries and their values.

Ada Code (mailbox-rv3.adb):

```
procedure WRITE_OUTPUT_1(Data : in INTEGER) is
begin
    INTEGER_OUTPUT_1_DATA := Data;
end WRITE_OUTPUT_1;

procedure MACHINE_STEP
is
    DATA_0 : INTEGER;
    DATA_1 : INTEGER;
begin
    if INPUT_0_READY and OUTPUT_1_CONSUMED then
        DATA_0 := READ_INPUT_0;
        NOTIFY_INPUT_0_CONSUMED;
        WRITE_OUTPUT_1(DATA_0);
        NOTIFY_OUTPUT_1_READY;
    end if;
    if INPUT_1_READY and OUTPUT_0_CONSUMED then
        DATA_1 := READ_INPUT_1;
        NOTIFY_INPUT_1_CONSUMED;
        WRITE_OUTPUT_0(DATA_1);
        NOTIFY_OUTPUT_0_READY;
    end if;
end MACHINE_STEP;
```

QueryView Data:

Query Name	Value	Expression
pathA_1	38	slice FORWARD with {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_INPUT_1_DATA)}
pathB_0	38	slice FORWARD with {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_INPUT_0_DATA)}
pathA_0	68	slice BACKWARD with {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_OUTPUT_0_DATA)}
pathB_1	75	slice BACKWARD with {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_OUTPUT_1_DATA)}
pathA1_0	17	chop FULL from {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_INPUT_1_DATA)} to {body}
pathB0_1	17	chop FULL from {body Mailbox.MACHINE_STEP(Mailbox.INTEGER_INPUT_0_DATA)} to {body}
A_B	true	assert (pathA_1 DISJOINT pathB_0)
AintersectA	18	pathA_1 INTERSECTION pathA_0
AintersectB		pathA_1 INTERSECTION pathB_0
A1_0_B0_1	true	assert (pathA1_0 DISJOINT pathB0_1)

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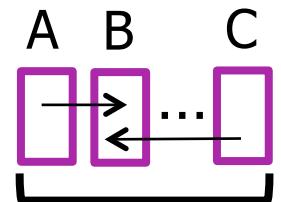
Contract Language (1)

- Domain represent either
 - an integrity level, which constructs a lattice,
or
 - a system's partition to show noninterference
between them

Contract Language (1)

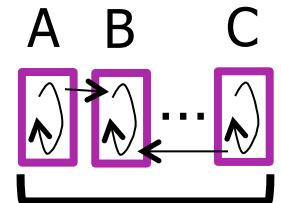
```
p ::=  
| Domain A, B, C, ...  
| Ordering A > B, B > C, ... (* can be null {}) *)  
| x ... in A, ...  
| Declassify (exp, A → C), ... (* can be null {}) *)
```

Abstract



```
p ::=  
| Derives o From i On guard  
| Derives Forall j With p(j) h[exp (j)] From i On guard
```

Refinement



It expresses information contract both within one domain and across-domain

In abstract policy, **Declassify()** constraints the mount of information that can be released through both the data flow (exp) and control flow (guard) mentioned in refinement policy.

Contract Language (1) - case 1

```
p ::=  
| Domain A, B, C, ...  
| Ordering A > B, B > C, ...  
| x ... in A, ...  
| Declassify { }
```

```
p ::=  
| Derives o From i On guard  
| Derives Forall j With p(j) h[exp (j)] From i On guard
```

Abstract

Refinement

It expresses information contract both within one domain and across-domain

Isolation: tag data with different integrity levels (for example MILS), and enforce that data with higher integrity level can never be released into lower data. However, it allows data with lower integrity level flowing into higher data, for example: $h := h + l$.

Contract Language (1) - case 2

```
p ::=  
| Domain A, B, C, ...  
| Ordering { }  
| x ... in A, ...  
| Declassify { }
```

```
p ::=  
| Derives o From i On guard  
| Derives Forall j With p(j) h[exp (j)] From i On guard
```

Abstract

Refinement

It expresses information contract both within one domain and across-domain

Isolation: divide the system into several partitions, and enforce the noninterference between these partitions

Contract Language (1) - case 3

```
p ::=  
| Domain A, B, C, ...  
| Ordering A > B, B > C, ...  
| x ... in A, ...  
| Declassify { exp: A → C }
```

```
p ::=  
| Derives o From i On guard  
| Derives Forall j With p(j) h[exp (j)] From i On guard
```

Abstract

Refinement

It expresses information contract both within one domain and across-domain

Declassify can express both (1) the information release channel from high to low and (2) explicitly specified information channel between two non-interference partitions. No restriction on domains appearing in Declassify, they can be element of a lattice or just partitions.

Contract Language (1) - case 4

```
p ::=  
| Domain A, B, C, ...  
| Ordering { }  
| x ... in A, ...  
| Declassify { exp: A → C }
```

```
p ::=  
| Derives o From i On guard  
| Derives Forall j With p(j) h[exp (j)] From i On guard
```

Abstract

Refinement

It expresses information contract both within one domain and across-domain

Declassify can express both (1) the information release channel from high to low and (2) explicitly specified information channel between two non-interference partitions. No restriction on domains appearing in Declassify, they can be element of a lattice or just partitions.

Security (1)

Two-level required contract

```
p ::=  
| Domain A, B, C, ...  
| Ordering A > B, B > C, ... (* can be null {}) *)  
| x ... in A, ...  
| Declassify (exp, A → C), ... (* can be null {}) *)
```



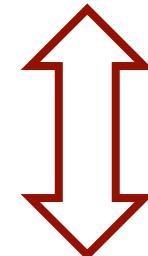
```
p ::=  
| Derives o From i On guard  
| Derives Forall j With p(j) h[exp (j)] From i On guard
```



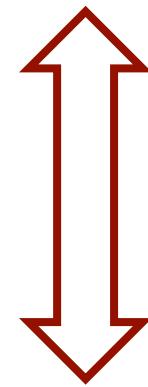
Actual contract by SIFL algorithm

```
Procedure foo( ... )  
is  
begin  
...  
end foo;
```

Abstract

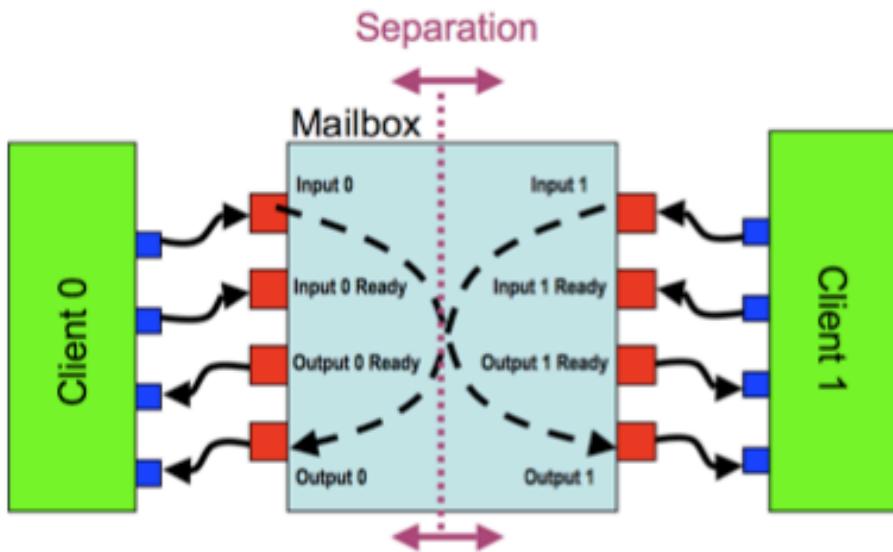


Refinement



Implementation

Contract Language (1) - Example 1



```

procedure MACHINE_STEP
— INFORMATION FLOW CONTRACT (Figure 3)
is D_0, D_1 : CHARACTER;
begin
  if IN_0.RDY and not OUT_1.RDY then
    D_0 := IN_0.DAT; IN_0.RDY := FALSE;
    OUT_1.DAT := D_0; OUT_1.RDY := TRUE;
  end if;
  if IN_1.RDY and not OUT_0.RDY then
    D_1 := IN_1.DAT; IN_1.RDY := FALSE;
    OUT_0.DAT := D_1; OUT_0.RDY := TRUE;
  end if;
end MACHINE_STEP;

```

```

Procedure MACHINE_STEP
--# Domain P0In, P0Out, P1In, P1Out;
--# Ordering {} ;
--# IN_0.DAT, IN_0.RDY in P0In ; OUT_0.DAT, OUT_0.RDY in P0Out ;
--# IN_1.DAT, IN_1.RDY in P1In ; OUT_1.DAT, OUT_1.RDY in P1Out ;
--# Declassify (IN_0.DAT, IN_0.RDY: P0In → P1Out), (IN_1.DAT, IN_1.RDY: P1In → P0Out) ;
--# Derives OUT_1.DAT from IN_0.DAT On (IN_0.RDY && ¬ OUT_1.RDY)
--#
--# * On ¬(IN_0.RDY && ¬ OUT_1.RDY)
--# (IN_0.RDY) & (OUT_1.RDY)
--# Derives OUT_0.DAT from IN_1.DAT On (IN_1.RDY && ¬ OUT_0.RDY)
--#
--# * On ¬(IN_1.RDY && ¬ OUT_0.RDY)
--# (IN_1.RDY) & (OUT_0.RDY)

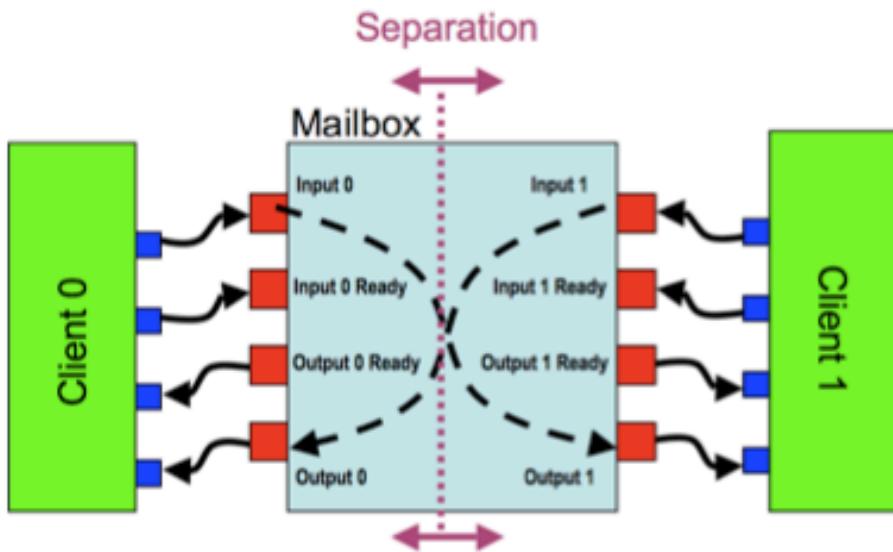
```

Abstract

Refinement

Both declassification policy and
Conventional information
contract

Contract Language (1) - Example 1



```

procedure MACHINE_STEP
— INFORMATION FLOW CONTRACT (Figure 3)
is D_0, D_1 : CHARACTER;
begin
  if IN_0.RDY and not OUT_1.RDY then
    D_0 := IN_0.DAT; IN_0.RDY := FALSE;
    OUT_1.DAT := D_0; OUT_1.RDY := TRUE;
  end if;
  if IN_1.RDY and not OUT_0.RDY then
    D_1 := IN_1.DAT; IN_1.RDY := FALSE;
    OUT_0.DAT := D_1; OUT_0.RDY := TRUE;
  end if;
end MACHINE_STEP;

```

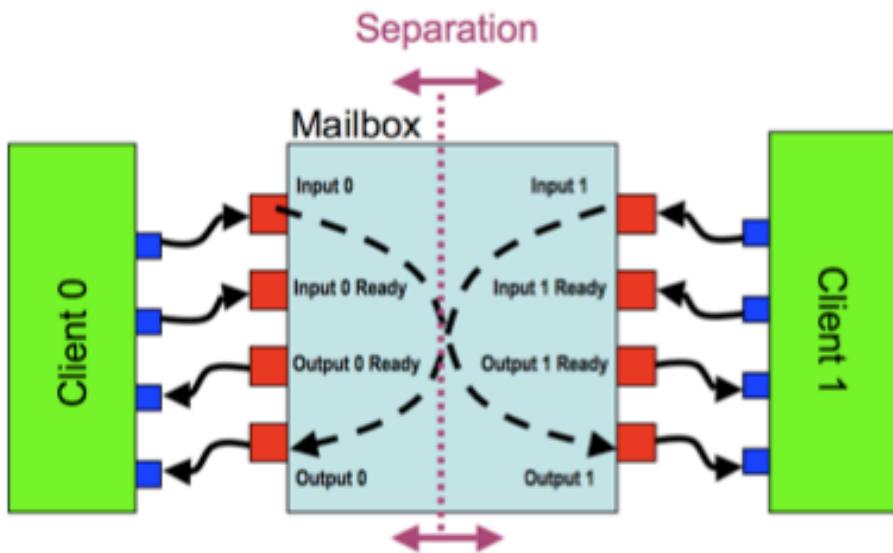
```

Procedure MACHINE_STEP
--# Domain Channel1, Channel2;
--# Ordering {};
--# IN_0_DAT, IN_0_RDY, OUT_1_DAT, OUT_1_RDY in Channel1;
--# IN_1_DAT, IN_1_RDY, OUT_0_DAT, OUT_0_RDY in Channel2;
--# Declassify {};
--# Derives OUT_1_DAT from IN_0_DAT On (IN_0_RDY && ~ OUT_1_RDY)
--# * On ~(IN_0_RDY && ~ OUT_1_RDY)
--# (IN_0_RDY && ~ OUT_1_RDY)
--# Derives OUT_0_DAT from IN_1_DAT On (IN_1_RDY && ~ OUT_0_RDY)
--# * On ~(IN_1_RDY && ~ OUT_0_RDY)
--# (IN_1_RDY && ~ OUT_0_RDY)

```

Partitions' Isolation

Contract Language (1) - Example 1



```

procedure MACHINE_STEP
— INFORMATION FLOW CONTRACT (Figure 3)
is D_0, D_1 : CHARACTER;
begin
  if IN_0_RDY and not OUT_1_RDY then
    D_0 := IN_0_DAT; IN_0_RDY := FALSE;
    OUT_1_DAT := D_0; OUT_1_RDY := TRUE;
  end if;
  if IN_1_RDY and not OUT_0_RDY then
    D_1 := IN_1_DAT; IN_1_RDY := FALSE;
    OUT_0_DAT := D_1; OUT_0_RDY := TRUE;
  end if;
end MACHINE_STEP;

```

$$\{ (IN_0_RDY \wedge \neg OUT_1_RDY) \Rightarrow IN_0_DAT\#, \\ \neg (IN_0_RDY \wedge \neg OUT_1_RDY) \Rightarrow OUT_1_DAT\#, \\ (IN_0_RDY \wedge \neg OUT_1_RDY)\# \}$$

$$\{ (IN_1_RDY \wedge \neg OUT_0_RDY) \Rightarrow IN_1_DAT\#, \\ \neg (IN_1_RDY \wedge \neg OUT_0_RDY) \Rightarrow OUT_0_DAT\#, \\ (IN_1_RDY \wedge \neg OUT_0_RDY)\# \}$$

Mailbox

$\{ OUT_1_DAT \# \}$

Mailbox

$\{ OUT_0_DAT \# \}$

Contract Language (1) - Example 1

Actual information flow

```
{ (IN_0_RDY ∧ ¬OUT_1_RDY) ⇒ IN_0_DAT#,  
¬(IN_0_RDY ∧ ¬OUT_1_RDY) ⇒ OUT_1_DAT#,  
(IN_0_RDY ∧ ¬OUT_1_RDY)#}
```



{ **OUT_1_DAT#** }

Step 1: Generate data dependence between variables in input and output channels

Contract Language (1) - Example 1

```
--# Derives OUT_1_DAT from IN_0_DAT  On (IN_0_RDY && ~OUT_1_RDY)  &
--#                                     OUT_1_DAT  On ~(IN_0_RDY && ~OUT_1_RDY)  &
--#                                     (IN_0_RDY)                                &
--#                                     (OUT_1_RDY);
```



```
--# Derives OUT_0_DAT from IN_1_DAT  On (IN_1_RDY && ~OUT_0_RDY)  &
--#                                     OUT_0_DAT  On ~(IN_1_RDY && ~OUT_0_RDY)  &
--#                                     (IN_1_RDY)                                &
--#                                     (OUT_0_RDY);
```

Step 2: Transfer from user-supplied contract to 2-assertions

Required information flow



{ (IN_0_RDY / \ -OUT_1_RDY) => IN_0_DAT#,
-(IN_0_RDY / \ -OUT_1_RDY) => OUT_1_DAT#,
IN_0_RDY#, OUT_1_RDY#}



{ OUT_1_DAT# }

Actual information flow

{ (IN_0_RDY / \ -OUT_1_RDY) => IN_0_DAT#,
-(IN_0_RDY / \ -OUT_1_RDY) => OUT_1_DAT#,
(IN_0_RDY / \ -OUT_1_RDY)#}



{ OUT_1_DAT# }

Step 1: Generate data dependence between variables in input and output channels

Contract Language (1) - Example 1

```
--# Derives OUT_1_DAT from IN_0_DAT  On (IN_0_RDY && ~OUT_1_RDY)  &
--#                                     OUT_1_DAT  On ~(IN_0_RDY && ~OUT_1_RDY)  &
--#                                     (IN_0_RDY)                                &
--#                                     (OUT_1_RDY);
```



```
--# Derives OUT_0_DAT from IN_1_DAT  On (IN_1_RDY && ~OUT_0_RDY)  &
--#                                     OUT_0_DAT  On ~(IN_1_RDY && ~OUT_0_RDY)  &
--#                                     (IN_1_RDY)                                &
--#                                     (OUT_0_RDY);
```

Step 2: Transfer from user-supplied contract to 2-assertions

Required information flow



```
{ (IN_0_RDY / \ -OUT_1_RDY) => IN_0_DAT#,  
  -(IN_0_RDY / \ -OUT_1_RDY) => OUT_1_DAT#,  
  IN_0_RDY#, OUT_1_RDY#}
```

```
{ OUT_1_DAT# }
```

Step 3: 2-assertions inference



Actual information flow

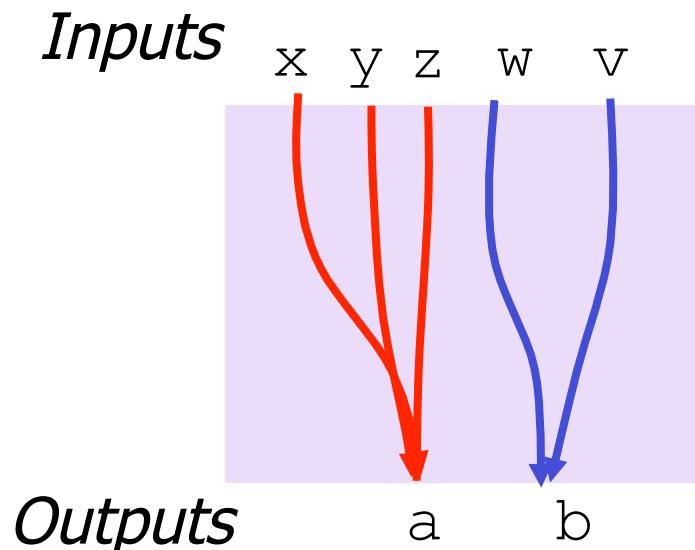
```
{ (IN_0_RDY / \ -OUT_1_RDY) => IN_0_DAT#,  
  -(IN_0_RDY / \ -OUT_1_RDY) => OUT_1_DAT#,  
  (IN_0_RDY / \ -OUT_1_RDY)#}
```

```
{ OUT_1_DAT# }
```

Step 1: Generate data dependence between variables in input and output channels

Non-interference

The classical notion of *non-interference* (Goguen & Meseguer) provides semantic foundation for describing the required separation...



Proving "nothing interferes with red channel" (i.e., a only depends on x, y and z)...

$$\begin{aligned}s_1(x) &= s_2(x) \\s_1(y) &= s_2(y) \\s_1(z) &= s_2(z)\end{aligned}$$

implies

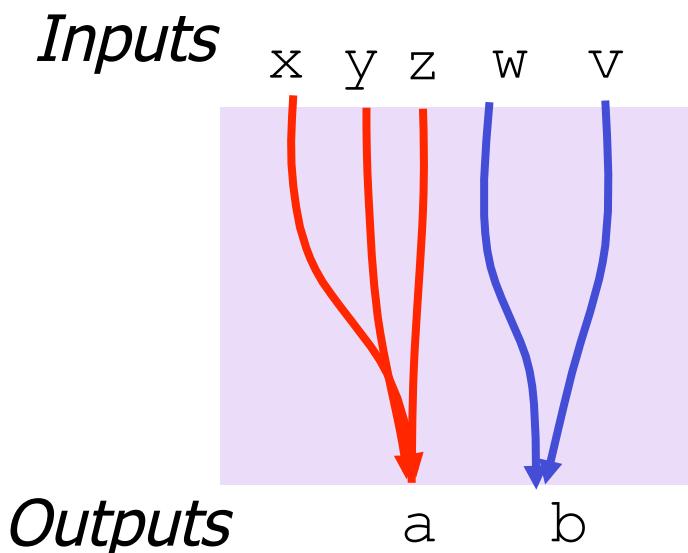
$$s'_1(a) = s'_2(a)$$
$$s'_1 \quad \quad \quad s'_2$$

Non-interference theorem:

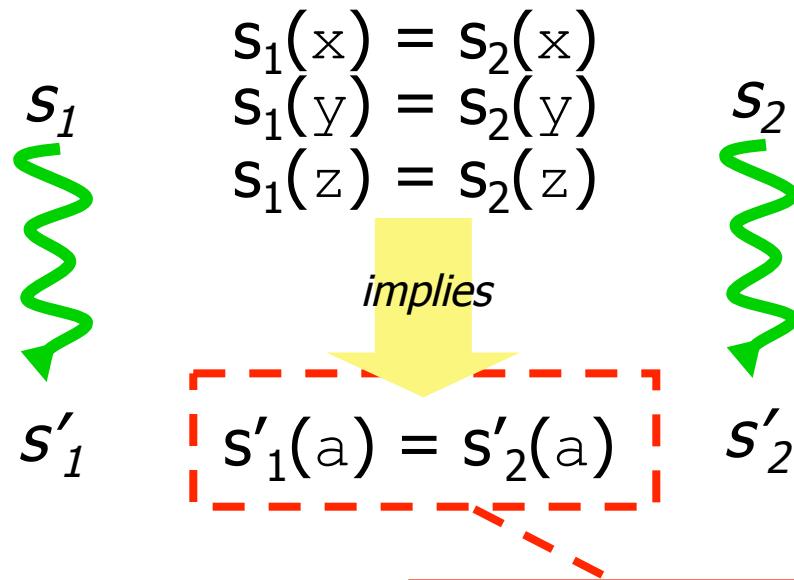
For any two executions with initial states s_1, s_2 ,
if s_1 and s_2 both **agree** on the values of x, y and z ,
then final states s'_1 and s'_2 **agree** on the value of a

Non-interference

How can we lift reasoning about non-interference to code-level annotations?



Proving "nothing interferes with red channel" (i.e., a only depends on x, y and z)...



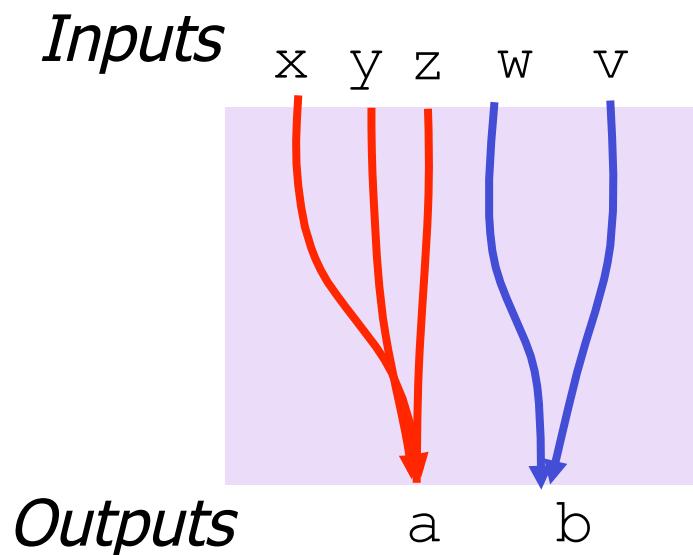
Non-interference theorem:

For any two executions with initial states s_1, s_2 , if s_1 and s_2 both **agree** on the values of x, y and z , then final states s'_1 and s'_2 **agree** on the value of a

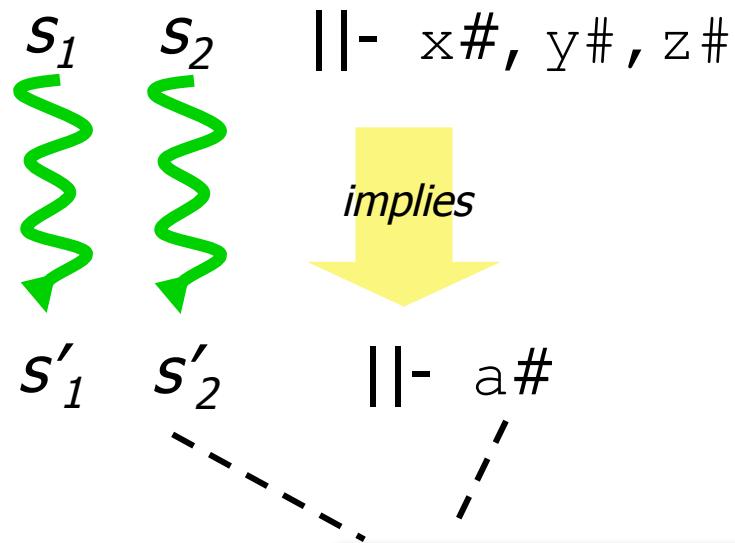
Let's have an abbreviation for the concept of "agreement"

Non-interference

The classical notion of *non-interference* provides semantic foundation for describing the required separation...



Proving "nothing interferes with red channel" (i.e., a only depends on x, y and z)...



Agreement Assertion:

$$s_1, s_2 \Vdash x\# \text{ iff } s_1(x) = s_2(x)$$

*Novel form of assertion has semantics based on **pair of states** instead of just a single state.*

Conditional Agreement Assertions

We'll use a more general form of the logic described by Amtoft and Banerjee in [FMSE 07]...

 $s_1, s_2 \Vdash x\#$

iff $\llbracket x \rrbracket s_1 = \llbracket x \rrbracket s_2$

generalize

 $s_1, s_2 \Vdash P \Rightarrow E\#$

iff whenever $\llbracket P \rrbracket s_1$ and $\llbracket P \rrbracket s_2$ hold
then $\llbracket E \rrbracket s_1 = \llbracket E \rrbracket s_2$

Agreement on
expression E
under condition P

Note: $x\#$ abbreviates $\text{true} \Rightarrow x\#$

Automating the Analysis

```

{ $\Theta$ }  $\Leftarrow$  skip { $\Theta'$ } iff  $\Theta = \Theta'$ 
{ $\Theta$ }  $\Leftarrow$  assert( $\phi_0$ ) { $\Theta'$ }
  iff  $\Theta = \{\phi \wedge \phi_0 \Rightarrow E \times \mid \phi \Rightarrow E \times \in \Theta'\}$ 
{ $\Theta$ }  $\Leftarrow$   $x = A \{ \Theta' \}$  iff  $\Theta = \Theta'[A/x]$ 
{ $\Theta$ }  $\Leftarrow$   $h[A_0] := A \{ \Theta' \}$  iff  $\Theta = \Theta'[h[A_0 := A]/h]$ 
{ $\Theta$ }  $\Leftarrow$   $h := \text{new } \{\Theta'\}$  iff  $\Theta = \Theta'[Z/h]$ 
{ $\Theta$ }  $\Leftarrow$   $S_1 ; S_2 \{ \Theta' \}$ 
  iff  $\{\Theta''\} \Leftarrow S_2 \{ \Theta' \}$  and  $\{\Theta\} \Leftarrow S_1 \{ \Theta'' \}$ 
{ $\Theta$ }  $\Leftarrow$  if  $B$  then  $S_1$  else  $S_2 \{ \Theta' \}$ 
  iff  $\Theta = \bigcup_{\theta \in \Theta'} \text{Pre}_{\text{if}}(\theta)$  where
     $\text{Pre}_{\text{if}}(\phi \Rightarrow E \times) =$ 
      let  $\{\Theta_1\} \Leftarrow S_1 \{ \phi \Rightarrow E \times \}$ 
      let  $\{\Theta_2\} \Leftarrow S_2 \{ \phi \Rightarrow E \times \}$ 
      in if Preserves( $S_1, E'$ ) and Preserves( $S_2, E$ )
        then  $(\phi_1 \wedge B \vee \phi_2 \wedge \neg B \Rightarrow E \times \mid$ 
           $\phi_i \Rightarrow \neg x \in \Theta_i (i=1,2))$ 
        else  $\{\phi_1 \wedge B \Rightarrow E_1 \times \mid \phi_1 \Rightarrow E_1 \times \in \Theta_1\} \cup$ 
           $\{\phi_2 \wedge \neg B \Rightarrow E_2 \times \mid \phi_2 \Rightarrow E_2 \times \in \Theta_2\} \cup$ 
           $\{\phi_1 \wedge B \vee \phi_2 \wedge \neg B \Rightarrow B \times \mid$ 
           $\phi_i \Rightarrow \neg x \in \Theta_i (i=1,2)\}$ 
{ $\Theta$ }  $\Leftarrow$  call  $p \{ \Theta' \}$  iff  $\Theta = \bigcup_{\theta \in T} \text{Pre}_{\text{call}}(\theta) \cup R$ 
  where  $(R, T) = \text{PreProc}(\Theta')$  and
   $\text{Pre}_{\text{call}}(\phi' \Rightarrow E \times) =$ 
    let  $\phi = \text{NPC}(p, \phi')$ 
    in case  $E$  of
       $w \Rightarrow \{\phi \wedge \phi_w \Rightarrow E_w \times \mid \phi_w \Rightarrow E_w \times \in \text{2PC}_w^p\}$ 
       $h[A] \Rightarrow \{\phi \wedge \phi_h[A/u] \Rightarrow E_h[A/u] \times \mid$ 
         $\phi_h \Rightarrow E_h \times \in \Theta_h\}$ 
        where  $\text{2PC}_h[\cdot] = \forall u. \Theta_h$ 
{ $\Theta$ }  $\Leftarrow$  for  $q \leftarrow 1$  to  $y$  do  $S_0 (= S) \{ \Theta' \}$ 
  iff  $\Theta = \Theta_f \cup \Theta_a \cup \Theta_w[1/q] \cup R$ 
  and  $(R, T) = \text{PreProc}(\Theta')$  where
     $\Theta'_a = \{\theta \in T \mid \exists h, A : \text{con}(\theta) = h[A]\}$ 
     $\Theta'_f = \{\theta \in \Theta'_a \mid \text{Pre}_{\text{for}}(S_0, q, y, \theta) \text{ succeeds}\}$ 
     $\Theta'_w = \Theta'_a \setminus \Theta'_f$ 
     $\Theta_f = \bigcup_{\theta \in \Theta'_f} \text{Pre}_{\text{for}}(S_0, q, y, \theta)$ 
     $\Theta_a = \{\text{NPC}(S, \phi) \Rightarrow A \times \mid \phi \Rightarrow h[A] \times \in \Theta'_w\}$ 
     $\Theta'_h = \{\phi \Rightarrow h \times \mid \phi \Rightarrow h[A] \times \in \Theta'_w\}$ 
     $\Theta_w = \text{Pre}_{\text{while}}((S_0 ; q = q + 1), q \leq y, \Theta'_h \cup (T \setminus \Theta'_a))$ 
{ $\Theta$ }  $\Leftarrow$  while  $B$  do  $S_0$  od( $= S$ ) { $\Theta' \}$ 
  iff  $\Theta = \Theta_w \cup \Theta_a \cup R$  and  $(R, T) = \text{PreProc}(\Theta')$  where
     $\Theta_a = \{\text{NPC}(S, \phi) \Rightarrow A \times \mid \phi \Rightarrow h[A] \times \in T\}$ 
     $\Theta'_h = \{\phi \Rightarrow h \times \mid \phi \Rightarrow h[A] \times \in T\}$ 
     $\Theta'_w = \{\theta \in T \mid \text{con}(\theta) \text{ is a variable}\}$ 
     $\Theta_w = \text{Pre}_{\text{while}}(S_0, B, \Theta'_h \cup \Theta'_w)$ 

```

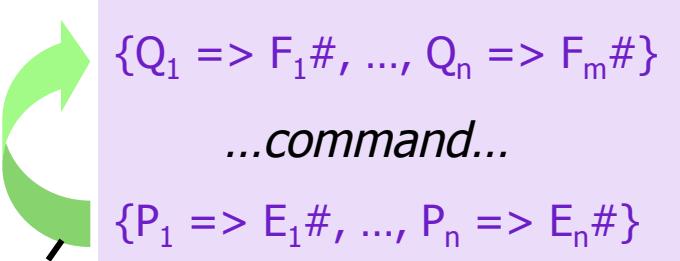
Helper functions:

- $\text{Pre}_{\text{for}}(S, q, y, \phi \Rightarrow h[u] \times) =$
let A_j be all expressions such that S_j is a subcommand of S
and S_j is of the form $h[A_j] := -$ with $j \in J$
and $J = \{1, 2, \dots, \#\text{ArrUpd}(S)\}$
in
let $\forall j \in J . \{\Theta_j\} \Leftarrow S \{ h[A_j] \}$
in
if $(\forall S_i . S_i \text{ occurs in } S \wedge (S_i = \text{call } p) \Rightarrow \text{Preserves}(S_i, h))$
 $\wedge (\forall j \in J . \exists A'_j . (\text{fv}(A'_j) \subseteq \{u\} \cup \text{fv}(A_j) \setminus \{q\} \wedge$
 $\forall s . [u = A_j]_s = [q = A'_j]_s)$
 $\wedge (\forall j \in J . \exists \phi_j . (\text{fv}(\phi_j) \subseteq \{u\} \cup \text{fv}(A_j) \setminus \{q\} \wedge$
 $(\forall s, n . [s \mid u \mapsto n] \models \phi_j \Leftrightarrow$
 $n \in ([A_j]_{[s|q \mapsto i]} \mid 1 \leq i \leq s(y)))$
 $\wedge w \in \text{fv}(\Theta_j) \wedge \neg \text{Preserves}(S, w) \Rightarrow w = h)$
 $\wedge \forall j \in J . h[A] . h[A] \text{ is a subexpression of } \Theta_j \Rightarrow$
 $(\forall s . \text{Store}, i, i' \in \{1, \dots, s(y)\} .$
 $[A]_{[s|q \mapsto i]} = [A_j]_{[s|q \mapsto i]} \Rightarrow i' \leq i)$
then $\{\phi_j \Rightarrow \Theta_j[A'_j/q] \times \mid j \in J\}$
 $\cup \{\wedge_{j \in J} \neg \phi_j \Rightarrow h[u] \times\}$
 $\cup \{x \times \mid \exists j \in J : x \in \text{fv}(A_j) \setminus \{q\}\}$
 $\cup \{y \times\}$
(succeeds)
else
()

$\text{PreProc}(\Theta') =$
 $P := \text{Purify}(\Theta')$
 $R := \emptyset$
 $T := \emptyset$
while $P \neq \emptyset$
remove $(\phi \Rightarrow E \times)$ from P and do
if $\text{Preserves}(p, E)$
then $R := R \cup \{\text{NPC}(S, \phi) \Rightarrow E \times\}$
else case E of
 $E_1 \text{ op } E_2 \text{ or } E_1 \text{ bop } E_2$
 $\Rightarrow P := P \cup \{\phi \Rightarrow E_1 \times, \phi \Rightarrow E_2 \times\}$
 $w \Rightarrow T := T \cup \{\phi \Rightarrow w \times\}$
 $h[A] \Rightarrow$
if $\text{Preserves}(p, h) \wedge \neg \text{Preserves}(p, A)$
then $R := R \cup \{\text{NPC}(p, \phi) \Rightarrow h \times\}$
else if $\neg \text{Preserves}(p, h) \wedge \text{Preserves}(p, A)$
then $T := T \cup \{\phi \Rightarrow h[A] \times\}$
else if $\neg \text{Preserves}(p, h) \wedge \neg \text{Preserves}(p, A)$
then $T := T \cup \{\phi \Rightarrow h \times\}$
return (R, T)

$\text{Pre}_{\text{while}}(S, B, \Theta') = \Theta^j$ such that
for each $w \in X$ (with $X = \text{fv}(S) \cup \text{fv}(B) \cup U$), where U is the set of all variables involved in procedure calls occurring in S , we inductively in i define
 $\phi_w^i, \Theta^i, \Psi^i, \psi_w^i$ by
 $\phi_w^0 = \bigvee \{\phi \mid \exists E : (\phi \Rightarrow E \times) \subset \Theta' \wedge \phi \in \text{fv}(E)\}$
 $\Theta^i = \{\phi_w^i \Rightarrow w \times \mid w \in X\}, \{$
 $\Psi^i = \bigcup_{w \in X} \psi_w^i$
 $\psi_w^i = \bigvee \{\phi \mid \exists (\phi \Rightarrow E \times) \in \Theta^i \wedge w \in \text{fv}(E)\}$
 $\text{and } \exists z \in X . \neg \text{Preserves}(S, z \Rightarrow \phi_w^i) \Rightarrow \psi_w^{i+1} = \psi_w^i \wedge \phi_w^i$
 $\text{and } j \text{ is the least } i \text{ such that } \Theta^i = \Theta^{i+1}$

- Can check contracts
- Can (in many cases) automatically infer contracts



our precondition algorithm
automatically generates pre-
conditions from post-conditions

Example Derivation

```
if INP_0_RDY and  
    not OUT_1_RDY then  
  
    DATA_0 := INP_0_DAT;  
  
    INP_0_RDY := false;  
  
    OUT_1_DAT := DATA_0;  
  
    OUT_1_RDY := true;  
fi  
  
OUT_1_DAT# ----- .
```

What do we need agreement on in the pre-state to obtain agreement on OUT_1_DAT in the post-state?

...on what does OUT_1_DAT depend?

Example Derivation

```
if INP_0_RDY and  
    not OUT_1_RDY then  
  
    DATA_0 := INP_0_DAT;  
  
    INP_0_RDY := false;  
  
    OUT_1_DAT := DATA_0;  
    OUT_1_DAT# -----  
    OUT_1_RDY := true;  
fi  
OUT_1_DAT#
```

*Irrelevant to OUT_1_DAT's value,
so OUT_1_DAT# still required*

Rule: NotModE

Example Derivation

```
if INP_0_RDY and
    not OUT_1_RDY then

    DATA_0 := INP_0_DAT;

    INP_0_RDY := false;
    DATA_0#;
    OUT_1_DAT := DATA_0;
    OUT_1_DAT#;
    OUT_1_RDY := true;
fi
OUT_1_DAT#
```

*OUT_1_DAT gets its value from
DATA_0 and so DATA_0# is required*

Rule: AssignE

Example Derivation

```
if INP_0_RDY and
    not OUT_1_RDY then

    DATA_0 := INP_0_DAT;
    DATA_0#
    INP_0_RDY := false; ----->
    DATA_0#
    OUT_1_DAT := DATA_0;
    OUT_1_DAT#
    OUT_1_RDY := true;
fi
OUT_1_DAT#
```

DATA_0 not modified...

Rule: NotModE

Example Derivation

```
if INP_0_RDY and
    not OUT_1_RDY then
    INP_0_DAT#
    DATA_0 := INP_0_DAT;-->
    DATA_0#
    INP_0_RDY := false;
    DATA_0#
    OUT_1_DAT := DATA_0;
    OUT_1_DAT#
    OUT_1_RDY := true;
fi
OUT_1_DAT#
```

*DATA_0 gets its value from INP_0_DAT
and so INP_0_DAT# is required*

Rule: NotModE

Example Derivation

$(\text{true} \&\& (\text{INP_0_RDY} \&\& !\text{OUT_1_RDY})) \Rightarrow \text{INP_0_DAT\#}$

```
if INP_0_RDY and  
not OUT_1_RDY then  
    true => INP_0_DAT#  
        DATA_0 := INP_0_DAT;  
        DATA_0#  
        INP_0_RDY := false;  
        DATA_0#  
        OUT_1_DAT := DATA_0;  
        OUT_1_DAT#  
        OUT_1_RDY := true;  
    fi  
    OUT_1_DAT#
```

We need agreement on INP_0_DAT\# if we enter the true branch

...and we also satisfy any conditions already associated with INP_0_DAT\# (none in this case)

Rule: CondE

Example Derivation

(true && (INP_0_RDY && !OUT_1_RDY)) => INP_0_DAT#

(true && !(INP_0_RDY && !OUT_1_RDY)) => OUT_1_DAT#

```
if INP_0_RDY and  
not OUT_1_RDY then  
    INP_0_DAT#  
    DATA_0 := INP_0_DAT;  
    DATA_0#  
    INP_0_RDY := false;  
    DATA_0#  
    OUT_1_DAT := DATA_0;  
    OUT_1_DAT#  
    OUT_1_RDY := true;  
fi  
OUT_1_DAT#
```

If we don't enter the true branch, then OUT_1_DAT is not modified, and so we need agreement on it in the pre-state

Rule: CondE

Example Derivation

$(\text{true} \&\& (\text{INP_0_RDY} \&\& \neg \text{OUT_1_RDY})) \Rightarrow \text{INP_0_DAT\#}$

$(\text{true} \&\& \neg(\text{INP_0_RDY} \&\& \neg \text{OUT_1_RDY})) \Rightarrow \text{OUT_1_DAT\#}$

$(\text{true} \&\& (\text{INP_0_RDY} \&\& \neg \text{OUT_1_RDY}) \mid\mid$

$\text{true} \&\& \neg(\text{INP_0_RDY} \&\& \neg \text{OUT_1_RDY})) \Rightarrow (\text{INP_0_RDY} \&\& \neg \text{OUT_1_RDY})\#$

```
if INP_0_RDY and
    not OUT_1_RDY then
    INP_0_DAT#
    DATA_0 := INP_0_DAT;
    DATA_0#
    INP_0_RDY := false;
    DATA_0#
    OUT_1_DAT := DATA_0;
    OUT_1_DAT#
    OUT_1_RDY := true;
fi
OUT_1_DAT#
```

If either of the guarding expressions above can be satisfied, we need agreement on the test expression to ensure agreement on which branch is taken (control dependence)

Rule: CondE

Example Derivation

(true && (INP_0_RDY && !OUT_1_RDY)) => INP_0_DAT#

(true && !(INP_0_RDY && !OUT_1_RDY)) => OUT_1_DAT#

(true && (INP_0_RDY && !OUT_1_RDY) ||
true && !(INP_0_RDY && !OUT_1_RDY)) => (INP_0_RDY && !OUT_1_RDY)#

```
if INP_0_RDY_and  
not OUT_1_RDY_then  
    INP_0_DAT#  
    DATA_0 := INP_0_DAT;  
    DATA_0#  
    INP_0_RDY := false;  
    DATA_0#  
    OUT_1_DAT := DATA_0;  
    OUT_1_DAT#  
    OUT_1_RDY := true;  
fi  
OUT_1_DAT#
```

Optimizations are detected, and a decision procedure is called to check if the optimizations are sound.

Performing simplification steps to optimize the size of expressions is a common action in the algorithm

Rules: DecisionImpl, ContraVar

Example Derivation

INP_0_RDY && !OUT_1_RDY => INP_0_DAT#

INP_0_RDY && !OUT_1_RDY => OUT_1_DAT#

INP_0_RDY#

!OUT_1_RDY#

```
if INP_0_RDY and
    not OUT_1_RDY then
    INP_0_DAT#
    DATA_0 := INP_0_DAT;
    DATA_0#
    INP_0_RDY := false;
    DATA_0#
    OUT_1_DAT := DATA_0;
    OUT_1_DAT#
    OUT_1_RDY := true;
fi
```

OUT_1_DAT#

Enhanced SPARK Contracts

```
INP_0_RDY && !OUT_1_RDY => INP_0_DAT#
```

```
INP_0_RDY && !OUT_1_RDY => OUT_1_DAT#
```

```
INP_0_RDY#
!OUT_1_RDY#
```

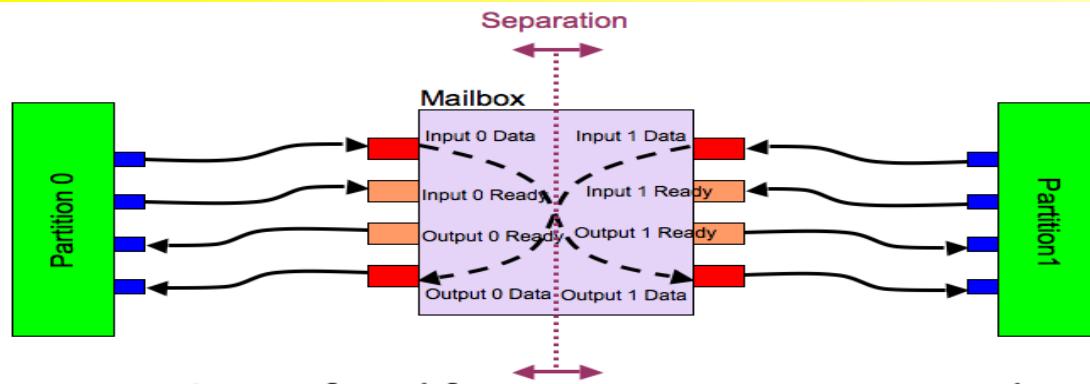
```
if INP_0_RDY and
    not OUT_1_RDY then
    INP_0_DAT#
    DATA_0 := INP_0_DAT;
    DATA_0#
    INP_0_RDY := false;
    DATA_0#
    OUT_1_DAT := DATA_0;
    OUT_1_DAT#
    OUT_1_RDY := true;
fi
OUT_1_DAT#
```

*New enhanced
SPARK contract
language hides
details of
underlying logic*

```
--# derives
--#     OUT_1_DAT from
--#         INP_0_DAT
--#             when (INP_0_RDY and
--#                     not OUT_1_RDY),
--#                 OUT_1_DAT,
--#                     when (not INP_0_RDY or
--#                             OUT_1_RDY),
--#                         INP_0_RDY,
--#                         OUT_1_RDY
```

Enhanced SPARK Contracts

Enhanced SPARK contract language can now capture the appropriate policy for the mailbox example...



*flows exist
only under
certain
conditions*

Original SPARK

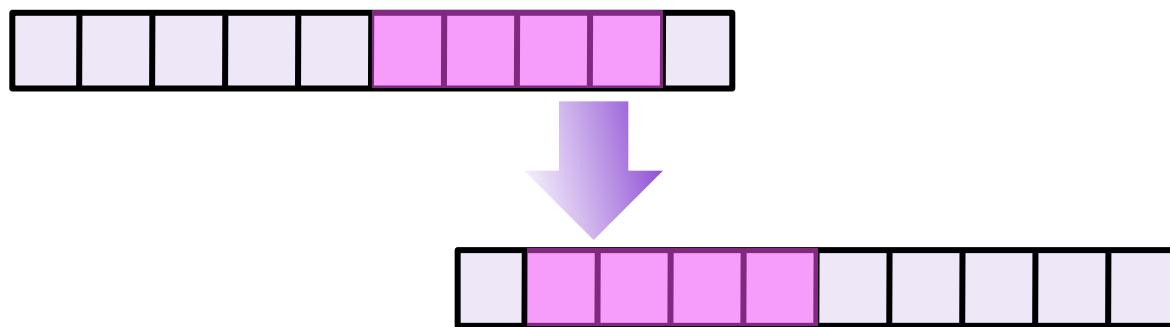
```
--# derives
--#   Output_1_Data from
--#     Input_0_Data,
--#   Output_1_Data,
--#   Input_0_Ready,
--#   Output_1_Ready
```

New conditional SPARK

```
--# derives
--#   Output_1_Data from
--#     Input_0_Data
--#   when (Input_0_Ready and
--#         not Output_1_Ready),
--#   Output_1_Data,
--#   when (not Input_0_Ready or
--#         Output_1_Ready),
--#   Input_0_Ready,
--#   Output_1_Ready
```

SPARK Contract Limitations

Many applications focus on processing of array-based message buffers that involves copying portions of buffers, moving message chunks, etc.



- We now show a collection of micro-examples that capture common idioms...
 - illustrate the short-comings of existing SPARK annotations
 - show more precise contracts that are enabled by our *secure information flow logic*.
- See previous papers for illustration of larger examples – including a MILS message router

Precise Array Information Flow

Conditional agreement assertions can be used to state precise conditions on indexing expressions...

Precondition generation rule for array assignment...

Pre: $x = y \Rightarrow w \times, x \neq y \Rightarrow A[y] \times, (x = y) \times$
 $A[x] := w$

Post: $A[y] \times$

Precise Array Information Flow

Original SPARK

```
procedure SinglePositionAssign
  (Flag : in Int;
   Value : in Types.Flagvalue)
  --# global in out Flags;
  --# derives Flags
  --#      from Flags,
  --#           Flag, Value;
is
begin
  Flags(Flag) := Value;
end SinglePositionAssign;
```

*Contract describes a flow to **all** index positions*

Enhanced SPARK

Precise frame condition -- only a specific position is affected

```
--# global out Flags(Flag);
--# derives Flags(Flag)
--#      from Value;
```

Contract describes a flow to a specific index position

Idiom: updating a single position within an array

Precise Array Information Flow

Original SPARK

```
procedure Scrub
  (B : in out Buffer)
  --# derives B
  --# , from B;
  is /
begin
  for I in Buffer_Range loop
    / B(I) := 0;
  end loop;
end Scrub;
```

Contract states that final value of B depends on its initial value; cannot capture the fact that all buffer contents are overwritten with 0;

Enhanced SPARK

Enhanced contracts allow universal quantification over array ranges...

```
--# derives forall I in
--#           Buffer_Range
--#     B(I) from {};
```

Contract states that each element in the final value of the buffer gets its value from some unspecified constant (all old information is scrubbed)

Idiom: scrubbing a buffer

Precise Array Information Flow

Original SPARK

```
procedure CopySegment
(B1 : in Buffer;
 B2 : in out Buffer)
--# derives B2
--# , from B1, B2;
is
begin
  for I in RangeToCopy loop
    B2(I) := B1(I+2);
  end loop;
end CopySegment;
```

Contract imprecision means that flow description is mangled; cannot capture the fact a specific segment of B2 comes from a specific section of B1, and the rest depends its initial value

Enhanced SPARK

Contract is able to specify a fine-grained flow policy...

```
--# derives forall I in
--#           RangeToCopy
--#     B2(I) from B1(I+2)
--# and forall I notin
--#           RangeToCopy
--#     B2(I) from B2(I)
```

Contract states that each B2 element in the RangeToCopy gets its value from a specific destination of B1, and otherwise depends on its initial value.

Idiom: copy one part of a buffer to another

Precise Array Information Flow

Flipping the halves of an array...

```
procedure flipHalves
  —# global in out h;
  —# derives for all I in h.Range =>
  —#   (h(I) from h(I+h.Range'Last/2)
  —#     when I >= 1 && I <= h.Range'Last/2 ,
  —#     h(I-h.Range'Last/2)
  —#     when I > h.Range'Last/2 && I <= h.Range ,
  —#     * when I < 1 || I > h.Range);
  is
    t : h.content;
    m : h.Range;
  begin
    m := h.Range'Last/2;
    for q in range h.Range'First .. m loop
      t := h(q);
      h(q) := h(q+m);
      h(q+m) := t;
    end loop;
  end flipHalves;
```

Assessment

When dealing with loops...

- **while** loops
 - In many cases, can infer an appropriate loop invariant
 - A loop invariant can always be inferred by dropping all conditions on assertions, but that can lead to imprecision
- **for** loops
 - Treated in clever way
 - Detects loops that are parallelizable, introduces a “schematic” variable for loop index, need only make one pass over the loop, and then generalize with universal quantification
 - Many **for** loops in information assurance applications are parallelizable and thus can be treated precisely
 - Those that aren’t are treated as **while** loops