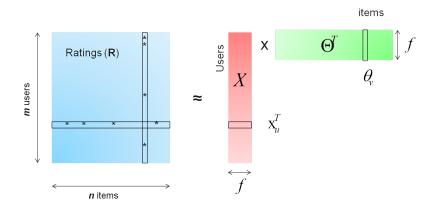
2017 Fall, Numerical Linear Algebra, Final project

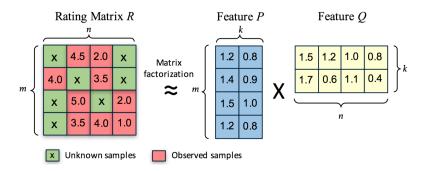
Applied Math & Electrical Engineering, NTU
R05246005 徐唯恩 B03901023 許秉鈞 B03901041 王文謙 R06246001 陳博允
January 13, 2018

1 Introduction

What is matrix factorization? Matrix factorization (MF) factors a sparse rating matrix R (m by n, with N_z non-zero elements) into a m-by-f and a f-by-n matrices, as shown below.



Matrix factorization (MF) is at the core of many popular algorithms, e.g., collaborative filtering (https://en.wikipedia.org/wiki/Collaborativefiltering), word embedding, and topic model. GPU (graphics processing units) with massive cores and high intra-chip memory bandwidth sheds light on accelerating MF much further when appropriately exploiting its architectural characteristics.



Matrix factorization has been demonstrated to be effective in recommender system, topic modeling, word embedding, and other machine learning applications. As the input data set is often large, MF solution are time-consuming. Therefore, how to solve MF problems efficiently is an important problem.

Now, we will start from paper reading and the following items are what we have done after paper reading:

- 1. Discuss the background of matrix factorization, including that why we do it and what we need to do.
- 2. Understand the algorithm of non-negative matrix factorization with projected gradient method and the theorems that support to this method.
- 3. Realize the difference between gradient method and projected gradient method.
- 4. Read the code (including cuda, cpp, matlab) from the internet and modify these code to fit our data.
- 5. Write code according to the algorithm in this paper and try to run some bigger data.
- 6. Compare the results with different parameters. Although there are some data from the internet file of the code are too big to run for our computers, but we still try to make the other data which are smaller and run them successfully.

For the **item 4 and 5**, we've implemented the **matlab**, **C++ CPU version**, **C++ GPU CUDA verion** of the Projected NMF methods based on some sketchy, fragmented piece of code available on Github, and we will provide links for those references if you're interested. Later on, you can easily see our experimental results and some comparisons with respective to a lot of different parameter settings. You can re-run our experiment based on the **README** provided in our github repo (https://github.com/AdrianHsu/cuMF-final), which is already attached in

the end of this pdf file.

Finally we've spent a lot of time dealing with the libraries called **cuMF-sgd** and **cuMF-als**, which are the cuda-based libraries that can solve huge problem like Netflix 1GB dataset, or MovieLens 10M dataset. However, the libraries are a bit intricated in that the environment set and input data preprocessing, i.e. transform the 3 columns data into COO, CSR format, or binary file in order to speed up.

2 Paper reading and comprehension

We first start from reading the paper Projected Methods for Non-negative Matrix Factorization (CJ Lin, 2005). The reason why we choose this paper is that the factorization a nonnegative matrix is needed in recommendation system. Thus we will state and show the algorithm as detail as possible. Now, we have a core problem is that given a nonnegative matrix $V_{n\times m}$ to find two nonnegative matrices $W_{n\times r}$, $H_{r\times m}$ such that

$$V = WH$$
.

However, we cannot ensure that the equility always holds. So, the problem can be convert to an optimal problem in several ways. One way is as follow.

2.1 Some existing methods for matrix factorization

Given $f: \mathbb{R}^{n \times r} \times \mathbb{R}^{r \times m} \to \mathbb{R}$ which is defined as

$$f(W, H) := \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{m} (V_{ij} - (WH)_{ij})^2,$$

where the factor $\frac{1}{2}$ is for convenience to operate the gradient differentiation. In fact, it is exact half of square of Frobenius norm of V - WH, that is

$$\sum_{i=1}^{n} \sum_{j=1}^{m} (V_{ij} - (WH)_{ij})^2 = ||V - WH||_F^2$$

So what we want to find is the to optimal

$$\min_{W,H} f(W,H) = \min_{W,H} \sum_{i=1}^{n} \sum_{j=1}^{m} (V_{ij} - (WH)_{ij})^{2}$$

which is subject to $W_{ia} \geq 0, H_{bj} \geq 0, \forall i, a, b, j$.

Sure, there are some other methods to convert such as an "entropy like" method, that is

$$\min_{W,H} \left(\sum_{i=1}^{n} \sum_{j=1}^{m} \left(V_{ij} \log \frac{V_{ij}}{W H_{ij}} - V_{ij} + (WH)_{ij} \right) \right).$$

Also, there are some nontrivial properties but not used in this paper, so we skip these detail in existing methods.

2.2 Explain how projective gradient method works

Now we will see the projective gradient methods for bound-constrained optimization. Consider the following standard form of bound-constrained optimization problem.

Let $f: \mathbb{R}^n \to \mathbb{R}$ is a continuous differentiable function, and \mathbf{l}, \mathbf{u} are lower and upper bound-constrains. Assume k is the index of iterations.

$$\min_{x \in \mathbb{R}^n} f(x)$$

subject to $l_i \leq x_i \leq u_i$ for i = 1, 2, ..., n. Now we are going to explain why the minimum will occurs. And in section (2.3), we will explain the how Projective Gradient Method apply to nonnegative matrix factorization and how its algorithm comes.

2.3 Proof of existence of the projective gradient method

In this paper, there is no proof of existence of the projective gradient method. First of all, we assume that we are process an optimization problem in a convex domain. In particular, \mathbb{R}^n is convex set. Now we consider the problem

$$\min_{x \in S} f(x),$$

where S is a nonempty closed convex set. We want to prove there exist a projection operator $P_S(x)$ which can calculate the minimum $\arg\min_{y\in S}\|x-y\|$. In fact, Projected Gradient Method is a simple method which modify the Gradient Method by the projection process. One can prove that the convergence and convergent rate is closed to Gradient Descent. Now we want to show the existence and uniqueness of projection matrix.

Theorem 1. If $S \subset \mathbb{R}^n$ is a nonempty closed convex set, then for any $x \in \mathbb{R}^n$,

$$\min_{y \in S} \|x - y\|$$

exists a unique solution x_S . And x_S is the optimal solution if and only if $(x - x_S)^T (y - x_s) \le 0$, $\forall y \in S$.

Pf. Let $x' \in S$, and consider a ball $B_{\|x-x'\|}(x)$. Then $S \cap B_{\|x-x'\|}(x)$ is nonempty and convex, thus it follows the existence.

For second part, if $x \in S$, naturally the optimal solution $x_S = x$. Conversely, $(x - x_S)^T (y - x_s) \le 0$ and $x \in S$ imply $||x - x_S||^2 \ne 0$ and hence the necessary and sufficiency holds. The other case if $x \notin S$, we prove the necessary first by contradiction. Suppose x_S is a projection point and the inequality doesn't hold. So there exist $y \in S$ such that $(x - x_S)^T (y - x_s) > 0$. Now consider $x_\theta = x_S + \theta(y - x_S)$, where $\theta \in [0, 1]$. And by the convexity, we get $x_\theta \in S$. Consider

$$||x - x_{\theta}||^{2} = ||x - x_{S} - \theta(y - x_{S})||^{2} = ||x - x_{S}||^{2} - 2\theta(x - x_{S})^{T}(y - x_{S}) + \theta^{2}||y - x_{S}||^{2}$$

Since θ^2 approaches to zero faster than θ as $\theta \to 0$. So

$$-2\theta(x - x_S)^T (y - x_S) + \theta^2 ||y - x_S||^2 < 0$$

whenever θ small enough. Hence get a contraction. Second, we prove the sufficiency. Suppose the inequality always holds $\forall y \in S$. To prove x_S is the optimal solution, consider for any $y \in S$, we have

$$||x - y||^{2} = ||x - x_{S} + x_{S} - y||^{2}$$

$$= ||x - x_{S}||^{2} - 2(x - x_{S})^{T}(y - x_{S}) + ||x_{S} - y||^{2}$$

$$\geq ||x - x_{S}||^{2} + ||x_{S} - y||^{2}$$

So we get that as $y \neq x_S$, $||x_S - y||^2 > 0$, and so $||x - y||^2 > ||x - x_S||^2$. And since y is arbitrary. So we proved that x_S is optimal solution.

Now we consider the nonnegative cone: $S := \{x | x \ge 0\}$ we only project from each dimension to nonnegative semi axis, that is $x_i \leftarrow \max\{x_i, 0\}$. Now we go back to the Projected Gradient Method. Assume we have a blackbox can easily compute $P_S(x)$, then we only need to process follows to convergent.

$$\bar{x_k} = P_S(x_k - s_k \nabla f(x_k)), s_k > 0$$

 $x_{k+1} = x_k + \alpha_k(\bar{x_k} - x_k), \alpha_k \in (0, 1],$

where $s_k > 0$ is a step size parameter. And thus the iterated algorithm as follow

$$x_{k+1} = P_S(x_k - s_k \nabla f(x_k)).$$

That is a combination of common gradient descent and projection operator $P_S(\dot{})$ in some feasible set. And the parameter α is a step size of choice of line search. We demand $\alpha_k \in (0,1]$ can make sure next x will not go out of feasible set. By the property of Gradient Descent which has a fixed step size:

$$||x_{k+1} - x*|| \le M||x_k - x*||,$$

where x* is the optimal solution and $M \in (0,1)$. So in the Projected Gradient Method. We have the same inequality as above. And we get

$$||P_S(x_{k+1} - x*)|| = ||P_S(x_{k+1}) - P_S(x*)||$$

$$\leq ||x_{k+1} - x*||$$

$$\leq M||x_k - x*||$$

Finally, we prove the contraction of the projection operator.

Theorem 2. Let $S \subset \mathbb{R}^n$ is a nonempty closed convex set, then the projection operator

$$P_S: x \mapsto \arg\min_{y \in S} ||x - y||, \forall x, y \in \mathbb{R}^n$$

Pf. Consider x, y and their projection x_S, y_S . Let H_x, H_y are hyperplanes passing through x_S, y_S and with the normal vector $x_S - y_S$. So we know the distance of two hyperplanes is $||x_S - y_S||$. By Theorem1, we know x, y are either in the hyperplane or out of the hyperplane. Thus the theorem2 follows.

By the previous conclusion, the projection operator is a contraction, so though we add a projection precess, it will not change the convergence of original Gradient Method.

2.4 Projected Gradient Method for NMF

We use the same optimization problem as (2.1) mentioned, that is

$$f(W,H) := \frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{m} (V_{ij} - (WH)_{ij})^{2},$$

Now, we calculate the gradient

$$\nabla_H f(W, H) = W^T (WH - V).$$

At each iteration, we can find a step size α by algorithm (4) in this paper. This algorithm satis equation

$$f(x^{k+1}) - f(x^k) \le \sigma \nabla f(x^k)^T (x^{k+1} - x^k).$$
 (1)

And check whether the current solution

$$\tilde{H} := P[H - \alpha \nabla f(H)]$$

satisfies above equation or not. The other hand, consider the quadratic function f(x) and any vector \mathbf{d} , we have

$$f(x + \mathbf{d}) = f(x) + \nabla f(x)^T \mathbf{d} + \frac{1}{2} \mathbf{d}^T \nabla^2 f(x) \mathbf{d}.$$

Then for two consecutive iterations \bar{x} and \tilde{x} , equation (1) can be rewritten as

$$(1-\sigma)\nabla f(\bar{x})^T(\tilde{x}-\bar{x}) + \frac{1}{2}(\tilde{x}-\bar{x})^T\nabla^2 f(\bar{x})(\tilde{x}-\bar{x}) \le 0.$$

As put H into x, we have

$$(1 - \sigma)\langle \nabla f(\bar{H}), \tilde{H} - \bar{H}\rangle + \frac{1}{2}\langle \tilde{H} - \bar{H}, W^T W(\tilde{H} - \bar{H})\rangle \le 0$$

Also, we can use the same procedure to update W.

2.5 Stopping Condition

Finally, the last main idea is in the section 5 this paper, the left section 6 and 7 are some numerical experiments. In this section, we make the algorithm stop when the numbers of iteration achieve to the given limit or the difference between recent iterations small enough. For the second item, a common condition to check if a point x^k is close to a stationary point for bound-constraint optimization is

$$\|\nabla^p f(x^k)\| \le \epsilon \|\nabla f(x^1)\|,\tag{2}$$

where $\nabla^p f(x^k)$ is the projected gradient defined as

$$\nabla^p f(x^k)_i := \begin{cases} \nabla f(x)_i & \text{if } l_i < x_i < u_i)\\ \min \{0, \nabla f(x)_i\}, & \text{if } x_i = l_i\\ \max \{0, \nabla f(x)_i\}, & \text{if } x_i = u_i \end{cases}$$

which follows from an equivalent form of the KKT condition for bounded problem and

$$\|\mathbf{\nabla}^p f(x)\| = 0$$

The other hand, for NMF, equation (2) becomes

$$\|\boldsymbol{\nabla}^p f(W^k, H^k)\|_F \le \epsilon \|\boldsymbol{\nabla} f(W^1, H^!)\|_F$$

Notice that the tolerance of the sub-problem should not be the same as the global one but relatively, i.e. The return matrices W^{k+1} and H^{k+1} from the sub-problem should respective satisfy

$$\|\nabla^p f(W^{k+1}, H^k)\|_F \leq \bar{\epsilon}_W$$
$$\|\nabla^p f(W^{k+1}, H^{k+1})\|_F \leq \bar{\epsilon}_H,$$

where we set

$$\bar{\epsilon}_H = \bar{\epsilon}_W = \max\{10^{-3}, \epsilon\} \cdot \|\nabla f(W^1, H^1)\|_F$$

with given ϵ in the beginning. If, unfortunately, the projected gradient method complete without any iterations, we decrease the stopping tolerance by

$$\bar{\epsilon}_W \leftarrow \frac{\bar{\epsilon}_W}{10}$$

and $\bar{\epsilon}_H$ is reduced in a similar way for the sub-problem.

3 Experiments

3.1 how dimension R affects the convergence

This experiment describes about how the dimension R in M*R*N affects the convergence. We use the MovieLens 100K datasets which is (943, 1682), and the nnz = 100000. As the table shows, we can discover that as R goes larger, the will affect the projection norm in the final round, and if the tolerance is larger, the norm will be larger in the final round. However, even if the norm changes drastically, we can still discover that the Frobenious norm still remains, around 1000.00

R = 5					
	10^-3	10^-4	10^-5	10^-6	
iteration	2	4	7	12	
time(sec)	0.015	0.018	0.043	0.0781	
final projNorm	5849.85	1682.09	181.665	17.511	
II W*H - V II_F	1111.5	989.34	913.97	910.39	
R = 10					
	10^-3	10^-4	10^-5	10^-6	
iteration	2	4	6	11	
time(sec)	0.0182	0.0218	0.0784	0.1799	
final projNorm	44185.8	5348.21	532.22	54.241	
II W*H - V II_F	1115	1108.8	25.44	885.93	
R = 15					
11.2.10	10^-3	10^-4	10^-5	10^-6	
iteration	2	4	6	11	
time(sec)	0.0223	0.0326	0.08714	0.2138	
final projNorm	82814	9865.41	928.583	100.798	
II W*H - V II_F	1122.5	1107.4	924.24	864.91	
R = 20					
	10^-3	10^-4	10^-5	10^-6	
iteration	2	4	6	8	
time(sec)	0.0206	0.0317	0.0864	0.1321	
final projNorm	145575	13052.5	1362.88	145.89	
II W*H - V II_F	1139.5	1108.6	987.36	869.75	

3.2 how dimension M,N affects the convergence

For this experiment, we want to discuss about the correlation between the dimension M, N will affect the number of iterations, and the total time... etc. As the table shows, we find that when M and N is around 100, and then we fix the tolerance, we can see that the Final projForm and Frobenius norm, the value are heavily depend on the M nad M; however, the number of iterations remain almost the same even though the matrix is very large.

	+	1	+		
(M, R, N)					
(37, 5, 140)					
	10^-3	10^-4	10^-5	10^-6	
iteration	2	5	7	31	
time (second)	0.015	0.01	0.005	0.016	
Frobenius Norm	131.62	118.98	117.0	115.58	
Final ProjNorm	257.14	24.01	2.861	0.285	
(100, 10, 250)					
	10^-3	10^-4	10^-5	10^-6	
iteration	2	4	8	53	
time (second)	0.015	0.0128	0.0181	0.0705	
Frobenius Norm	2440.85	245.80	21.818	2.266	
Final ProjNorm	284.08	267.90	259.81	255.69	
(1000, 50, 800)					
	10^-3	10^-4	10^-5	10^-6	
iteration	2	4	6	17	
time (second)	0.067	0.1147	0.3568	0.99	
Frobenius Norm	329620	27557	3235	291.95	
Final ProjNorm	1704.7	1613.5	1552.9	1510.4	
(5000, 5, 8000)					
	10^-3	10^-4	10^-5	10^-6	
iteration	2	5	7	18	
time (second)	0.736	2.4498	3.774	10.5727	
Frobenius Norm	213021	21012	2250.48	202.748	
Final ProjNorm	11572	11398	11393	11387s	

3.3 GPU v.s. CPU w.r.t memory and time

For this subsection, we will consider the dataset named **Movie Lens 100K** that contains 100000 nnz and the M = 943, N = 2625, which is not so large but still have some interesting properties that we can investigate. If you want to re-implement this experiment, you can download the code on Github and then fetch the data from here: **konect.uni-koblenz.de/networks/movielens-100k_rating**. This dataset is also provided in the README file, so you can get the link in my repo.

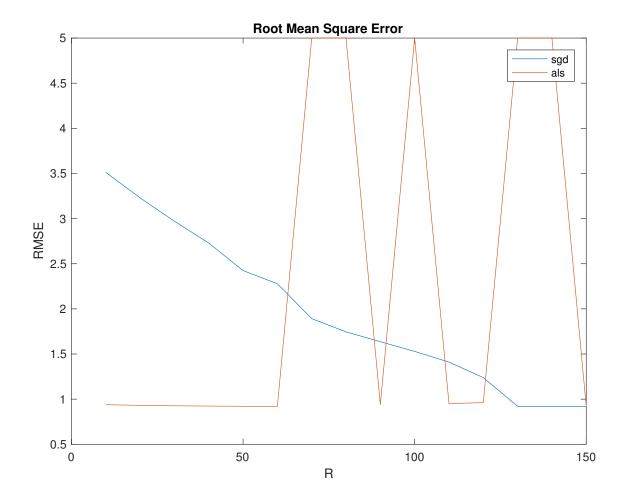
^{1 ~/}nla/pgrad-2\$./NMF ml100k.txt

² GPU Device 0: Tesla K80 with compute capability 3.7

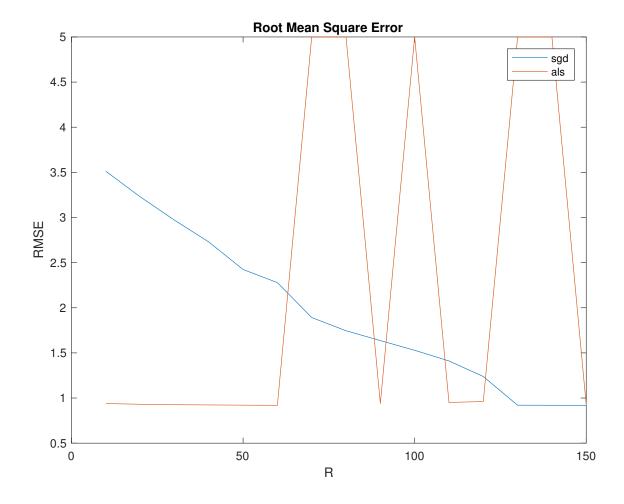
```
3 Init gradient norm 7348422.314490
_4 tol*initgrad = 7.348422
5 Iter = 1 Final proj-grad norm 8008612.469400
6 Iter = 2 Final proj-grad norm 112.232496
7 Iter = 3 Final proj-grad norm 472.571561
8 Iter = 4 Final proj-grad norm 1.020186
9 values in W*H (column major) are:
_{10} The ||W*H-V||_F is: 1066.802909
11 total elapsed time:
          0m24.912s
12 user
13 S Y S
          0m8.120s
_{14} === CPU version (tol = 1e-7) ===
15 /tmp3/4dr14nh5u/nla/cpu$ ./setup.sh ml100k.txt
16 Init gradient norm 64382280.742422
17 tol*initgrad = 6.438228
18 Iter = 1 Final proj-grad norm 64382280.742422
19 Iter = 2 Final proj-grad norm 0.650105
20 Iter = 3 Final proj-grad norm 0.650105
21 The result W*H is
_{22} The ||W*H-V|| is: 1076.549118
23 total elapsed time:
          0m1.620s
24 user
          0m0.020s
25 S V S
_{26} === CPU version (tol = 1e-9) ===
27 /tmp3/4dr14nh5u/nla/cpu$ ./setup.sh ml100k.txt
28 Init gradient norm 64382280.742422
_{29} tol*initgrad = 0.064382
30 Iter = 1 Final proj-grad norm 64382280.742422
31 Iter = 2 Final proj-grad norm 0.650105
32 Iter = 3 Final proj-grad norm 1.516980
33 Iter = 4 Final proj-grad norm 3.809543
_{34} Iter = 5 Final proj-grad norm 685.653741
35 Iter = 6 Final proj-grad norm 182.464007
```

We can easily discover that the CPU version is performing better than the GPU version, which is abnormal. As what we've discovered, the reason is that for CUDA, we have to use cudaMalloc(), cudaFree() and a lot of memory operation for GPU version, however in CPU version you can perform the linear algebra operation directly on stack Memory. Nevertheless, we have confidence that if we can try on larger dataset, (given that we solved the memory not-enough problem, please see the chapter talked about what problem we have encountered)for example, Netflix 1G dataset, and utilizing the BLOCK and THREAD in cuda programming, we can found that the GPU verion perform better if data grows larger.

4 Comparison of cuMF Libraries



In the first plot, we compare the execution time with different R between cumf_als and cumf_sgd methods. It is reasonable that the execution time increase as R become greater because of the data to be processed increase, but surprisingly the execution time seems to have nothing to do with R increase in the SGD method. On the other hand, the execution time by the cumf_sgd method is overall less than that of the cumf_als method.



In the second plot, we compare the RMSE(Root Mean Square Error) between the two methods. There are some aspects that can be observed in this plot. First of all, the RMSE in cumf_als method will diverge in some R (The RMSE result in the program outputs NaN, and we set these result as 5 for the sake of betterlook in this plot) although the diversity hasn't been mentioned in the paper.

The reason of this property, we guess, is that when we calculate the Ax = b, the singularity of A could approach 0(ill-conditioned). This may result in the components in A^{-1} becomes large when we take inverse of A. Second, the RMSEs for cumf_sgd method are larger than that of cumf_als in small R, but it gradually decreases while R increase and approach the RMSEs of cumf_als, if it doesn't diverge, of course.

5 Difficulties and Challenges

During our implementation process and the environment setting such as installing CBLAS, CUBLAS, CMAKE...etc, We've encountered a lot of difficulties. Ine problem is that the data type "double" in C/C++ cannot handle such large number, and therefore we slightly modified the data so that it is more adaptable toward our model.

The other problem we've encountered is that we don't have to transform our initial matrix from dense to the sparse one, because we have to admit that we've spent too much time dealing with the environment setting and getting familiar with the c memory allocation, and cuda memory allocation. Therefore if the matrix is too large, such as M = 1E6, and also N = 1E6, and then our matrix cannot contain these data, since that our 2-D array is too small to being performing and multiplication or dot product on them.

6 References

- 1. Xiaolong Xie, Wei Tan, Liana Fong, Yun Liang, CuMFSGD: Parallelized Stochastic Gradient Descent for Matrix Factorization on GPUs.
- 2. Faster and Cheaper: Parallelizing Large-Scale Matrix Factorization on GPUs. Wei Tan, Liangliang Cao, Liana Fong.
- 3. NMF.cu: This code solves NMF by alternative non-negative least squares using projected gradients. It's an implementation of **Projected gradient methods for non-negative matrix factorization** by CJ Lin. You may read the paper for more details.

Non-negative Matrix Factorization (CUDA)

README.md

This is the README.md of our final project in the course Numerical Linear Algebra, 2017 Fall in NTU.

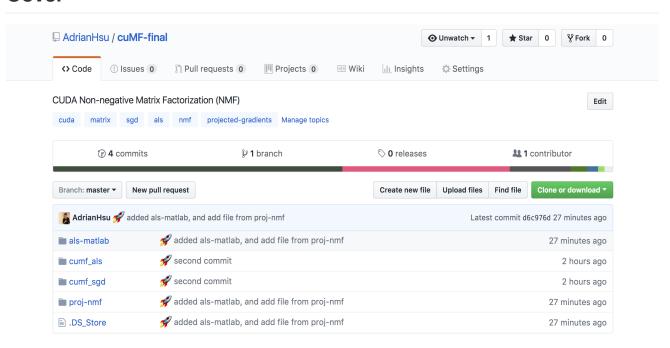
Instructor

王偉仲 教授(WEICHUNG WANG)

Members

R05246005 徐唯恩 B03901023 許秉鈞 B03901041 王文謙 R06246001 陳博允

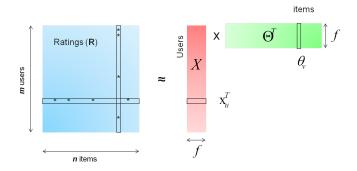
Cover



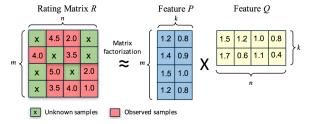
For this final project, you can access all of our code (CUDA, C++, matlab) directly on Github. Please check the link below: https://github.com/AdrianHsu/cuMF-final

What is matrix factorization?

Matrix factorization (MF) factors a sparse rating matrix R (m by n, with N_z non-zero elements) into a m-by-f and a f-by-n matrices, as shown below.



Matrix factorization (MF) is at the core of many popular algorithms, e.g., collaborative filtering, word embedding, and topic model. GPU (graphics processing units) with massive cores and high intra-chip memory bandwidth sheds light on accelerating MF much further when appropriately exploiting its architectural characteristics.



Matrix factorization has been demonstrated to be effective in recommender system, topic modeling, word embedding, and other machine learning applications. As the input data set is often large, MF solution are time-consuming. Therefore, how to solve MF problems efficiently is an important problem.

Input data format

The input rating for all sub-topics are organized as follows:

user_id item_id rating

user_id and item_id are 4-byte integers and rating is 4-byte floating point.

1. Projected gradient methods for NMF

It's an implementation of Projected gradient methods for non-negative matrix factorization. You may read the paper for more details

PART 1. PROJGRAD NMF (GPU Tesla K80)

NMF(Non-negative Matrix Factorization) based on cuda, with sparse matrix as input.

NMF_pgd.cu This code solves NMF by alternative non-negative least squares using projected gradients. It's an implementation of Projected gradient methods for non-negative matrix factorization. You may read the paper for more details.

Requirements

The code is base on cuda, cuBlas and cuSparse precisely. Please get cuda from Nvidia's website, https://developer.nvidia.com/cuda-downloads.

Usage

Results will be saved in two files, W.txt and H.txt in dense format. You should use nvcc to compile the code, so make sure cuda is installed and environment is correctly setted.

- \$ make
- \$./NMF_pgd

The default data input file is Movie Lens 100K dataset, you can download it from https://github.com/AdrianHsu/cuMF-final/blob/master/proj-nmf/gpu/ml100k

Contribution

The original work is done by <code>zhangzibin: cu-nmf</code>; however this is a very scratchy version that it ignores some cases, and therefore we fixed some bugs, modified the input format for adapting the other datasets, you could access the original work from https://github.com/zhangzibin/cu-nmf

PART 2. PROJGRAD NMF (CPU)

NMF(Non-negative Matrix Factorization) based on CBLAS, with dense matrix as input.

NMF.c This code solves NMF by alternative non-negative least squares using projected gradients.

How-to

As the first time to use BLAS and CBLAS, you may need to configure like this on Linux: Download blas.tgz and cblas.tgz on http://www.netlib.org/blas/

- 1. Install BLAS, generate blas_LINUX.a
- 2. Modify the BLLIB in CBLAS/Makefile.in which link to blas_LINUX.a, and make all in CBLAS
- 3. Put the src/cblas.h to /usr/lib/ or somewhere your compiler can find it, then enjoy it!

Run

```
compile: gcc NMF.c -o NMF.o -c -03 -DADD_ -std=c99
    gfortran -o NMF_ex NMF.o /home/lid/Downloads/CBLAS/lib/cblas_LINUX.a /home/lid/Downloads/BLAS/blas_LIN
execute: ./NMF_ex
```

Contribution

In order to compare the GPU version algorithm with the normal one, we directly fork the CPU version provided by Professor Chih-Jen Lin's Website, https://www.csie.ntu.edu.tw/~cjlin/nmf/, and the original implementation was done by **Dong Li**, you could download the piece of code from https://www.csie.ntu.edu.tw/~cjlin/nmf/others/NMF.c

PART 3. PROJGRAD NMF (python, matlab)

Since that these two implementations are not our main concern (we use them to compare and debug the C++ version), so if you have time to review it, you're welcomed to run our code here: https://github.com/AdrianHsu/cuMF-final/tree/master/proj-nmf

2. Alternating Least Squares (matlab)

Our work: just for an alternative

We implemented the Alternating Least Squares algorithm in order to understand how **cuMF Libraries** works. you could find our code in https://github.com/AdrianHsu/cuMF-final/tree/master/als-matlab

Description

There are 4 files in the folder: ALStest.m, CGmethod.m, getAB.m, randsparse.m You can run it on matlab directly.

3. cuMF Libraries

What is cuMF?

CuMF is a CUDA-based matrix factorization library that optimizes alternate least square (ALS) method to solve very large-scale MF. CuMF uses a set of techniques to maximize the performance on single and multiple GPUs. These techniques include smart access of sparse data leveraging GPU memory hierarchy, using data parallelism in conjunction with model parallelism, minimizing the communication overhead among GPUs, and a novel topology-aware parallel reduction scheme.

Our work

This work is done by **Wei Tan**, and we use his API for experimenting.

PART 1. Alternating Least Squares

CUDA Matrix Factorization Library with Alternating Least Square (ALS) https://github.com/cuMF/cumf_als

How-to Build

Type:

make clean build

To see debug message, such as the run-time of each step, type:

make clean debug

Input Data

CuMF need training and testing rating matrices in binary format, and in CSR, CSC and COO formats. In ./data/netflix and ./data/ml10M we have already prepared (i)python scripts to download Netflix and Movielens 10M data, and preprocess them, respectively.

For Netflix data, type:

```
cd ./data/netflix/
python ./prepare_netflix_data.py
```

For Movielens:

```
cd ./data/ml10M/
ipython prepare_ml10M_data.py
```

Note: you will encounter a NaN test RMSE. Please refer to the "Known Issues" Section.

Run

Type ./main you will see the following instructions:

Usage: give M, N, F, NNZ, NNZ_TEST, lambda, X_BATCH, THETA_BATCH and DATA_DIR.

E.g., for netflix data set, use:

```
./main 17770 480189 100 99072112 1408395 0.048 1 3 ./data/netflix/
```

E.g., for movielens 10M data set, use:

./main 71567 65133 100 9000048 1000006 0.05 1 1 ./data/ml10M/

Prepare the data as instructed in the previous section, before you run. Note: rank value F has to be a multiple of 10, e.g., 10, 50, 100, 200.

PART 2. Stochastic Gradient Descent

CuMF_SGD is a CUDA-based SGD solution for large-scale matrix factorization(MF) problems. https://github.com/cuMF/cumf_sgd

Run

usage:

./singleGPU/cumf_sgd [options] train_file [model_file]

We have a run script for Netflix data set:

./data/netflix/run.sh

In this script, we set u, v, x, and y as 1 as the data set is enough to fit into one GPU.

References

More Details can be found at:

Xiaolong Xie, Wei Tan, Liana Fong, Yun Liang, CuMF_SGD: Parallelized Stochastic Gradient Descent for Matrix Factorization on GPUs, (arxiv link).

ALS-based MF solution can be found here:

Faster and Cheaper: Parallelizing Large-Scale Matrix Factorization on GPUs. Wei Tan, Liangliang Cao, Liana Fong. [HPDC 2016], Kyoto, Japan. (arXiv) (github)