My First Compiler - Home Exam

Compiler Construction and Formal Languages, ${\bf D7050E}$

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April 14, 2021

https://github.com/Aleman778/First-Compiler



Contents

1	Syntax		
	1.1	EBNF Grammar	2
	1.2	Demo Code	
	1.3	Requirements and Contributions	
2	Semantics		
	2.1	Structural Operational Semantics	7
	2.2	Interpreting Demo Code	9
	2.3	Requirements and Contributions	
3	Type Checker		
	3.1	Typing Rules	12
	3.2	Examples	14
	3.3	Requirements and Contributions	17
4	Borrow Checker		
	4.1	Specification	18
	4.2	Examples	
	4.3	Requirements and Contributions	
5	Intermediate Representation		
	5.1	IR Instruction	21
	5.2	Example	22
6	X86 Backend		23
	6.1	Examples	23
	6.2	Register Allocation	
	6.3	Performance Improvements	
7	Lea	rning Outcomes	30

1 Syntax

1.1 EBNF Grammar

```
\langle file \rangle
                           ::= \{ \langle function \rangle \}
\langle function \rangle ::= \text{`fn'} \langle ident \rangle \text{`('} [\langle fn-arg \rangle \text{ {', '}} \langle fn-arg \rangle \text{ }] ['->' \langle type \rangle] \langle block \rangle
\langle fn\text{-}arg \rangle
                           ::= [`mut'] \langle ident \rangle `:` \langle type \rangle
\langle statement \rangle ::= \text{`let'} \langle ident \rangle \text{ `:'} \langle type \rangle \text{ [`='} \langle expr \rangle \text{] `;'}
                               \begin{array}{c|c} & \langle block \rangle \text{ ';'} \\ & \langle expr \rangle \text{ ';'} \\ & \langle expr \rangle \end{array} 
\langle block \rangle ::= '{' { \langle statement \rangle } '}'
\langle expr \rangle
                           ::= \langle atom \rangle '=' \langle expr \rangle
                                    'if' <expr> <block> ['else' \langle block \rangle]
                                    'while' \langle expr \rangle \langle block \rangle
                                     \langle block \rangle
                                    'return' \langle expr \rangle
                                     'break'
                                     'continue'
                                     \langle atom \rangle \ \{ \ \langle binop \rangle \ \langle atom \rangle \ \}
                                     \langle atom \rangle
\langle atom \rangle
                           ::= \langle literal \rangle
                                  ((\langle expr \rangle))
                              | \langle ident \rangle '(' [\langle expr \rangle { ',' \langle expr \rangle }] ')'
                                    \langle unop \rangle \langle expr \rangle
                                     \langle ref \rangle \langle expr \rangle
\langle literal \rangle
                           := regexp[0-9] +
                                     'true'
                                    'false'
```

$$\langle ident \rangle \qquad ::= \ \operatorname{regexp}[\operatorname{a-zA-Z}][\operatorname{a-zA-Z0-9}_]^*$$

$$\langle \mathit{unop} \rangle \quad ::= \, `!\, `| \, `-' \mid `*'$$

$$\langle \mathit{ref} \rangle \hspace{1cm} ::= \text{`\&' [`mut']}$$

$$\langle type \rangle \hspace{1cm} ::= \text{`i32'} \mid \text{`bool'} \mid \langle \textit{ref} \rangle \ \langle \textit{type} \rangle$$

1.2 Demo Code

```
1 fn main() -> i32 {
      let x: &mut i32 = &mut 0;
      let mut i: i32 = 0;
      while i < 10 {
           i = i + 1;
           next_prime(x);
6
           print_int(*x);
8
      return *x;
9
10 }
11
12 fn next_prime(n: &mut i32) {
      while true {
13
           *n = *n + 1;
14
           if is_prime(*n) {
15
               break;
16
           }
17
      }
18
19 }
20
  fn is_prime(n: i32) -> bool {
21
      if n < 2 {
           return false;
23
24
25
      let mut i: i32 = 2;
27
      while i < n {
           if n % i == 0 {
               return false;
           }
           i = i + 1;
31
      }
32
       true
```

where print_int is an intrinsic to print an i32 to the console.

1.3 Requirements and Contributions

The parser implements all the listed requirements and more:

- Function definitions
- Commands (let, assignment, if then (else), while)
- Expressions (includig function calls)

- Primitive types (boolean, i32) and their literals
- Explicit types everywhere
- Explicit return(s)
- Operator precedence (optional)
- Location information (optional)

The only missing optional feature is error recovery thus only a single error can be reported during the entire parsing stage. There is also an issue with the error locations when they are reported from within the parser. For example missing a semicolon the **nom** parser combinator **Tag** is reported as the error message and but somewhere in unwinding the call stack the location information is lost. For example running this results in location pointing to the first character in the function:

However, it works fine when the error is outside the parser e.g. type errors are able to correctly locate the error:

When designing the syntax for this language the Rust language was used as a guide for most of the decisions made because the goal was essentially to create a mini Rust language. Like Rust this language syntax treats most things as expressions even **if** and **while** which normally are statements (or commands) because they modify the state of the program. The only real statement in this language and like Rust is the **let** statement.

There is support for defining foreign function interfaces in the syntax but this was not actually used in the final compiler and was instead replaced by hardcoded intrinsics. That is why they were left out from the **EBNF** grammar but can still be parsed however there is no support for loading dynamic libraries so this feature is not that usefull. There are explicit return(s) in the language but like Rust implicit return(s) were also added for example:

```
1 firstc -r "fn main() -> i32 { 10 }"
2
3 Interpreter exited with code 10
```

Since if is an expression together with the fact that blocks can return values to the its parent block means that conditional ternary operator (i.e. x = true ? 10 : 20) is supported, like this:

```
1 firstc -r "fn main() -> i32 { let x: i32 = if true { 10 }
        else { 20 }; x + 5 }"
2
3 Interpreter exited with code 15
```

Another contribution that a string interner is used to avoid unnecessary copies of strings and this is used for function names, identifiers and even internal temporary names used by the compiler. This works by essentially storing each string onces in a permanent storage that only gets freed when the compiler exits. Storing references to a string is done through using symbols (i.e. integer id) and can be resolved its original string through a hash table lookup. This adds a cost for looking up names but since this only really is used for error handling it is not a big problem. It also reduces the memory footprint since string clones was previously used extensively to avoid complex borrowing situation between systems which now is replaced by cheap integer copy. This was implemented using a library called *string-interner* which provides the permanent storage and hash table lookup.

2 Semantics

2.1 Structural Operational Semantics

Evaluation of a statement s in the state σ yields new state σ' :

$$\langle s, \sigma \rangle \Downarrow \sigma'$$
 (1)

Whenever there is nothing to evaluate the state is left unchanged denoted by skip.

$$\overline{\langle \text{skip}, \sigma \rangle \Downarrow \sigma}$$
 (2)

For let bindings the expression e is evaluated first to n and then assigned to the actual variable x.

$$\frac{\langle e, \sigma \rangle \Downarrow n}{\langle \mathbf{let} \ x = e, \sigma \rangle \Downarrow \sigma[x = n]}$$
 (3)

After previously binding a variable x if it was annotated as mutable it is possible to assign a new value to it.

$$\frac{\langle e, \sigma[x=n_1] \rangle \Downarrow n_2}{\langle x=e, \sigma[x=n_1] \rangle \Downarrow \sigma[x=n_2]} \tag{4}$$

Blocks may contain multiple statements and they have to be evaluated in the same order that they were defined in. For two statements it is important that the first is evaluated before the other statement because it needs use the new state produced by the first statement evaluation.

$$\frac{\langle s_1, \sigma \rangle \Downarrow \sigma' \langle s_2, \sigma' \rangle \Downarrow \sigma''}{\langle s_1; s_2, \sigma \rangle \Downarrow \sigma''}$$
 (5)

Note that if-expressions are syntactically expressions but the semantics behaves more like statements because they change the state of σ . If the condition c evaluates to true then block b_1 will be evaluated and resulting in the new state σ'

$$\frac{\langle c, \sigma \rangle \Downarrow true \ \langle b_1, \sigma \rangle \Downarrow \sigma'}{\langle \mathbf{if} \ c \ \{ b_1 \ \} \ \mathbf{else} \ \{ b_2 \ \}, \sigma \rangle \Downarrow \sigma'}$$
 (6)

If the condition c evaluates to false then block b_2 will be evaluated and result in state σ'' .

$$\frac{\langle c, \sigma \rangle \Downarrow false \langle b_2, \sigma \rangle \Downarrow \sigma''}{\langle \mathbf{if} \ c \ \{ b_1 \ \} \ \mathbf{else} \ \{ b_2 \ \}, \sigma \rangle \Downarrow \sigma''}$$
 (7)

While-loops also changes the state in a similar way except repeats, for the case where the condition c evaluates to false then nothing happens to the state.

$$\frac{\langle c, \sigma \rangle \Downarrow false}{\langle \mathbf{while} \ c \ \{ \ b \ \}, \sigma \rangle \Downarrow \sigma}$$
 (8)

If the condition c evaluates to true then the semantics is recursive.

$$\frac{\langle c, \sigma \rangle \Downarrow true \ \langle b, \sigma \rangle \Downarrow \sigma' \ \langle \mathbf{while} \ c \ \{ b \ \}, \sigma' \rangle \Downarrow \sigma''}{\langle \mathbf{while} \ c \ \{ b \ \}, \sigma \rangle \Downarrow \sigma''}$$
(9)

Continue-expressions can only affect the current while-loop if the condition c is true. Using (5) it can be expressed as continue following by wildcard denoted by $_$.

$$\frac{\langle c, \sigma \rangle \Downarrow true \ \langle b', \sigma \rangle \Downarrow \sigma' \ \langle \mathbf{while} \ c \ \{ b \ \}, \sigma' \rangle \Downarrow \sigma''}{\langle \mathbf{continue}; _, \sigma \rangle \Downarrow \sigma''}$$
(10)

For break-expressions it simply terminates the loop and like continue-expressions it can be followed by a wildcard. Note that continue- and break-expressions can only appear inside of loops this is ensured by the type checker, see Section 3.1.

$$\overline{\langle \mathbf{break}; \ , \sigma \rangle \Downarrow \sigma}$$
 (11)

Return-expressions evaluates its inner expression first and then propagates the result upwards through blocks, loops, if-expressions. It will also ignore any future statements in the current block through the wildcard.

$$\frac{\langle e, \sigma \rangle \Downarrow \langle n, \sigma' \rangle}{\langle \mathbf{return} \ e ; _, \sigma \rangle \Downarrow \langle \mathbf{return} \ n, \sigma' \rangle}$$
(12)

The inner expression is optional and without it the return value will be an unit value.

$$\frac{}{\langle \mathbf{return} \; ; \; , \sigma \rangle \Downarrow \langle \mathbf{return}, \sigma \rangle} \tag{13}$$

Example of binary addition operation uses an implementation specific function called add which usually translates into an ADD instruction in most processor architectures.

$$\frac{\langle e_1, \sigma \rangle \Downarrow n_1 \langle e_2, \sigma \rangle \Downarrow n_2}{\langle e_1 + e_2, \sigma \rangle \Downarrow \operatorname{add}(n_1, n_2)}$$
(14)

Calling a function f with the parameter expressions $p_1, p_2, ..., p_n$ has to first evaluate those expressions in order, this builds a new state σ_{params} can be used to look up the parameters. After parameters are evaluated then the

function block f.b and it uses a backing storage denoted M which contains all the values stored before calling the function. After evaluating the function it will return a value r and M'.

$$\frac{\langle p_1, \sigma_0 \rangle \Downarrow \langle n_1, \sigma_1 \rangle \cdots \langle p_n, \sigma_{n-1} \rangle \Downarrow \langle n_n, \sigma_{params} \rangle \langle f.b, (\sigma_{params}, M) \rangle \Downarrow \langle r, M' \rangle}{\langle f(n_1, n_2, ..., n_n), \sigma_0 \rangle \Downarrow \langle r, M' \rangle}$$
(15)

Identifier x evaluates to local variable hash table lookup.

$$\overline{\langle x, \sigma[x=n] \rangle \Downarrow n} \tag{16}$$

Unary negation operation uses an implementation specific function called neg which usually translates into an NEG or (0-n) SUB instruction in most processor architectures.

$$\frac{\langle e, \sigma \rangle \Downarrow n}{\langle -e, \sigma \rangle \Downarrow \operatorname{neg}(n)}.$$
 (17)

Borrows (&) evaluates to the memory location denoted by star symbol (*) of a particular variable x

$$\overline{\langle \&x, \sigma[x=n] \rangle \Downarrow *x} \tag{18}$$

It is also possible to borrow from a literal value v however in order to get a valid memory location it has to first be stored in memory as a temporary variable

$$\frac{}{\langle \&v, \sigma \rangle \Downarrow \langle *temp, \sigma[temp = v] \rangle}$$
 (19)

Unary dereference operation on identifier x finds the underlying value that the particular borrow points to and the operation evaluates to that value. For nested borrows this only dereferences one borrow at a time.

$$\frac{\langle y, \sigma[y = *x, x = n] \rangle \Downarrow *x}{\langle *y, \sigma[y = *x, x = n] \rangle \Downarrow n}.$$
(20)

2.2 Interpreting Demo Code

The state of the interpreter is represented by the *InterpContext* struct which holds things like the AST (or *File* struct), hash map of functions, callstack and the memory. The memory acts as a stack and gets automatically cleaned up after each function. When parsing is done the AST (or *File* struct) is produced which contains a list of functions that first has to be inserted into *InterpContext* hash map for access when calling functions. After this is done calling *interp_entry_point* will find the *main* function and start executing its block.

The first statement in main uses rules (19) and (3).

let x: &mut i32 = &mut 0;

$$\frac{\langle \& \text{mut } 0, \sigma \rangle \Downarrow \langle *temp, \sigma[temp = 0] \rangle}{\langle \textbf{let } x = \& \text{mut } 0, \sigma \rangle \Downarrow \sigma[x = *temp, temp = 0]}$$

The second statement evaluates to state $\sigma[x = *temp, temp = 0, i = 0]$, the third statement is a while loop which uses rules (8) when i >= 10 and (9) otherwise.

while i < 10 {

$$\frac{\langle i<10,\sigma[i>=10]\rangle \Downarrow false}{\langle \mathbf{while}\ c\ \{\ b\ \},\sigma\rangle \Downarrow \sigma}$$

$$\frac{\langle i<10,\sigma[i<10]\rangle \Downarrow true\ \langle b,\sigma\rangle \Downarrow \sigma'\ \langle \mathbf{while}\ c\ \{\ b\ \},\sigma'\rangle \Downarrow \sigma''}{\langle \mathbf{while}\ c\ \{\ b\ \},\sigma\rangle \Downarrow \sigma''}$$

The first statement inside the while loop increments the iterator variable i with one using semantic rules (4), (14) and (16) togheter.

Next is a function call to $next_prime$ which uses semantic rules (15) and (16). Calling the function $next_prime$ also calls is_prime which will produce the new state $\Sigma = [\sigma_{next_prime}, \sigma_{is_prime}]$. Note that this function does not return any value so it is elided from the equation.

$$\begin{split} & \texttt{next_prime(x);} \\ & \underline{\langle x, \sigma_0 \rangle \Downarrow \langle n, \sigma_{params}[x = n] \rangle} \ \langle \texttt{next_prime.b}, \sigma_{params}[x = n] \rangle \Downarrow \Sigma \\ & \underline{\langle \texttt{next_prime}(x), \sigma_0 \rangle \Downarrow \Sigma} \end{split}$$

Inside next_prime function there is an infinite loop that increments the argument by one each time. The loop only terminates if the value is a prime number, this uses semantic rule (6). The is_prime is quite self explanatory so that is skipped to keep this explanation short.

if is_prime(*n) {
$$\frac{\langle \text{is}_\text{prime}(*n), \sigma \rangle \Downarrow true \ \langle b_1, \sigma \rangle \Downarrow \sigma'}{\langle \text{if is} \ \text{prime}(*n) \ \{ \ b_1 \ \}, \sigma \rangle \Downarrow \sigma'}$$

Inside the if-expression there is a break expression that will terminate the infinte loop whenever evaluated, defined by semantic rule (11).

break;

$$\overline{\langle \mathbf{break}; _, \sigma \rangle \Downarrow \sigma'}$$

Back to main when $\sigma[i=10]$ the loop terminates and the resulting value of x is dereferenced and returned. This uses the semantics rules (13) and (20).

```
return *x;  \frac{\langle *y, \sigma[y = *temp, temp = 29] \rangle \Downarrow \langle 29, \sigma' \rangle}{\langle \mathbf{return} \ *y; \_, \sigma[y = *temp, temp = 29] \rangle \Downarrow \langle \mathbf{return} \ 29, \sigma' \rangle}
```

2.3 Requirements and Contributions

- Your interpreter should be able to correctly execute programs according to your SOS.
- Your interpreter should panic (with an appropriate error message) when encountering an evaluation error (e.g., 1 + false)

The interpreter was implemented before writing the SOS rules so the SOS rules were formed based on the code. While the interpreter by itself can report type errors it should not panic but instead report a maximum of one fatal error (usually type errors) and exit the program.

3 Type Checker

3.1 Typing Rules

Let bindings requires that the type specified is the same as the resulting type of the expression e. It is also possible to define let binding without an expression e that instead only requires the type to be specified.

$$\frac{\Gamma \vdash e : \tau}{\Gamma \vdash \mathbf{let} \ x : \tau = e} \tag{21}$$

$$\frac{\Gamma \vdash \mathbf{let} \ x : \tau}{\Gamma} \tag{22}$$

Break and continue are not allowed outside of loops and will generate an error message if such case is detected. These evaulates to the type **unit** referred to as () in error messages which essentially means that it has no type similar to void in C.

$$\frac{\Gamma \vdash \mathbf{while} \ \{ \ b \ \} : \mathbf{unit}}{\Gamma \vdash \mathbf{break} \in b : \mathbf{unit}}$$
 (23)

$$\frac{\Gamma \vdash \mathbf{while} \ \{ \ b \ \} : \mathbf{unit}}{\Gamma \vdash \mathbf{continue} \in b : \mathbf{unit}}$$
 (24)

Assignment has two rules either assign directly through mutable variable x or first dereference it *x (this is recursive and can handle any number of deferences). Note that for assigning to *x then x has to be a mutable reference to the same type as the expression e. If x is something other than an identifier or deference (recursively) to identifier it will generate an invalid expression error. Note that $\tau(\text{mut})$ means that the actual underlying let binding is mutable.

$$\frac{\Gamma \vdash x : \tau(\text{mut}) \ \Gamma \vdash e : \tau}{\Gamma \vdash x = e : \mathbf{unit}}$$
 (25)

$$\frac{\Gamma \vdash x : \& mut \ \tau(\text{mut}) \ \Gamma \vdash e : \tau}{\Gamma \vdash *x = e : \mathbf{unit}}$$
 (26)

Binary expression can be divided into four groups arithmetic (e.g. +, - etc.), logical (&&, ||), equality (==, !=) and comparator (e.g. <, >= etc.). Here are the typing rules for each respective group

$$\frac{\Gamma \vdash e_1 : \mathbf{int} \ \Gamma \vdash e_2 : \mathbf{int}}{\Gamma \vdash e_1 + e_2 : \mathbf{int}}$$
 (27)

$$\frac{\Gamma \vdash e_1 : \mathbf{bool} \ \Gamma \vdash e_2 : \mathbf{bool}}{\Gamma \vdash e_1 \& \& e_2 : \mathbf{bool}}$$
 (28)

$$\frac{\Gamma \vdash e_1 : \tau \; \Gamma \vdash e_2 : \tau}{\Gamma \vdash e_1 == e_2 : \tau} \tag{29}$$

$$\frac{\Gamma \vdash e_1 : \mathbf{int} \ \Gamma \vdash e_2 : \mathbf{int}}{\Gamma \vdash e_1 < e_2 : \mathbf{bool}}$$
(30)

Calling a function requires that all the paramters passed have the same type that are defined in the function declaration.

$$\frac{\Gamma \vdash f(\tau_1, \tau_2, ..., \tau_n) : \tau \ \Gamma \vdash e_1 : \tau_1 \ \Gamma \vdash e_2 : \tau_2 \ \cdots \ \Gamma \vdash e_n : \tau_n}{\Gamma \vdash f(e_1, e_2, ..., e_n) : \tau}$$
(31)

Identifiers are stored in a type table and in order to use an identifier there is one check to see if the value has been initialized since let bindings doesn't require an initialization immediately.

If expressions requires that both blocks b_1 and b_2 has the same type and the condition is c is a boolean then the result will be τ .

$$\frac{\Gamma \vdash c : bool \ \Gamma \vdash b_1 : \tau \ \Gamma \vdash b_2 : \tau}{\Gamma \vdash \mathbf{if} \ c \ \{ b_1 \ \} \ \mathbf{else} \ \{ b_2 \ \} : \tau}$$
(32)

Taking a reference either mutable or immutable only requires that the referenced expression actually has a type.

$$\frac{\Gamma \vdash e_1 : \&\tau \; \Gamma \vdash e_2 : \tau}{\Gamma \vdash e_1 = \&e_2 : \&\tau}$$
(33)

Explicit and implicit return has to have the same type as the return type in the function declaration.

$$\frac{\Gamma \vdash f : \tau}{\Gamma \vdash \mathbf{return} \ e \in f : \tau} \tag{34}$$

$$\frac{\Gamma \vdash f(...)b : \tau}{\Gamma \vdash b.last : \tau} \tag{35}$$

Unary expressions have very straightforward typing rules.

$$\frac{\Gamma \vdash e : \mathbf{int}}{\Gamma \vdash -e : \mathbf{int}} \tag{36}$$

$$\frac{\Gamma \vdash e : \mathbf{bool}}{\Gamma \vdash !e : \mathbf{bool}} \tag{37}$$

$$\frac{\Gamma \vdash e : \&\tau \text{ or } \&mut \ \tau}{\Gamma \vdash *e : \tau} \tag{38}$$

While expressions only requires that the condition c is a boolean. While is an expression but does not evaluate to any type.

$$\frac{\Gamma \vdash c : bool \ \Gamma \vdash b : \mathbf{unit}}{\Gamma \vdash \mathbf{while} \ c \ \{ \ b \ \} : \mathbf{unit}}$$
(39)

3.2 Examples

```
Rule 21:
```

```
firstc -r "fn main() { let x: i32 = false; }"
2 <run>:1:26: error: expected 'i32', found 'bool'
4 1 | fn main() { let x: i32 = false; }
5
    Rule 22:
1 firstc -r "fn main() { let x: i32; }" [OK]
firstc -r "fn main() { break; }"
2 <run>:1:13: error: cannot break outside loop
4 1 | fn main() { break; }
                  \mbox{\tt ```````} help: remove this or move it inside a
 loop
    Rule 24:
firstc -r "fn main() { continue; }"
2 <run>:1:13: error: cannot continue outside loop
4 1 | fn main() { continue; }
                  ^~~~~~ help: remove this or move it inside
 a loop
    Rule 25:
1 firstc -r "let mut x: i32 = 10; x = 20; print_int(x);" [OK]
g firstc -r "let mut x: i32 = 10; x = false; print_int(x);"
4 <run>:1:22: error: expected 'i32', found 'bool'
6 1 | let mut x: i32 = 10; x = false; print_int(x);
8 firstc -r "let x: i32 = 10; x = 20; print_int(x);"
9 <run>:1:18: error: cannot assign twice to immutable variable
    ʻxʻ
10
11 1 | let x: i32 = 10; x = 20; print_int(x);
                       cannot assign twice to immutable
      variable
13 1 | let x: i32 = 10; x = 20; print_int(x);
14 | ^ help: make variable mutable 'mut x'
```

Rule 26:

Rule 27, 28, 29 and 30:

```
1 firstc -r "let x: i32 = 10 + 20;" [OK]
2 firstc -r "let x: i32 = 10 + false;"
3 <run>:1:1: error: cannot add 'i32' to 'bool'
4
5 1 | let x: bool = 10 + false;
                    ~~~~~~~~ no implementation for 'i32 +
     bool '
7 firstc -r "let x: bool = true && false;" [OK]
8 firstc -r "let x: bool = true && 20;"
9 <run>:1:1: error: cannot logical and 'bool' to 'i32'
11 1 | let x: bool = true && 20;
                    ~~~~~~~~ no implementation for 'bool &&
    i32'
13 firstc -r "let x: bool = 10 == 10;" [OK]
14 firstc -r "let x: bool = true == true;" [OK]
15 firstc -r "let x: bool = true == 20;"
16 <run>:1:1: error: cannot compare equal 'bool' to 'i32'
17
18 1 | let x: bool = true == 20;
                    ~~~~~~~ no implementation for 'bool ==
     i32'
20 firstc -r "let x: bool = 10 < 20;" [OK]
21 firstc -r "let x: bool = 10 < false;"</pre>
22 <run>:1:15: error: cannot compare less than 'i32' to 'bool'
24 1 | let x: bool = 10 < false;</pre>
                    ~~~~~~~ no implementation for 'i32 <
25
 bool'
```

Rule 31:

Rule 32:

Rule 33:

Rule 34 and 35:

```
9 <run>:1:20: error: expected 'i32', found 'bool'
10  |
11  | fn main() -> i32 { false }
12  |
```

Rule 36, 37 and 38:

```
1 firstc -r "let x: i32 = -10;" [OK]
2 firstc -r "let x: i32 = -false;"
3 <run>:1:14: error: type 'bool' cannot be negated
5 1 | let x: i32 = -false;
                   ~~~~~ no implementation for '-bool'
7 firstc -r "let x: bool = !false;" [OK]
8 firstc -r "let x: bool = !10;"
9 <run>:1:15: error: type 'i32' cannot be logical inverted
10
11 1 | let x: bool = !10;
                   ~~~ no implementation for '!i32'
12
13 firstc -r "let x: i32 = *&10;" [OK]
14 firstc -r "let x: i32 = *10;"
15 <run>:1:14: error: type 'i32' cannot be dereferenced
17 1 | let x: i32 = *10;
        ~~~ no implementation for '*i32'
```

Rule 39 (infinite loops are not detected by the compiler):

3.3 Requirements and Contributions

The type checker is complete since it is able to correctly identify type errors for the previously specified type rules. Note that the type checker was written before the type rules were specified. The type checker was designed by using mostly common sense and previous programming experience. The strict static typing and the error messages was directly inspired by the Rust compiler. The only thing the type checker is not able to do is type inference.

4 Borrow Checker

4.1 Specification

The borrow checker has a few responsibilies to ensure memory safety. Since this compiler only has primitive types that are always copied it means that move semantics is not needed. On most processesors registers hold these values and are moved between registers and stack using a single instruction which means copys (or moves) are very cheap. The borrow checker is only concerned with borrowed values through references. Here is the specification that defines the rules the borrow checker follows:

- Lifetime is defined to be an unsigned 32-bit integer.
- Lifetimes are only based on lexical scoping, there is no support for non-lexical lifetimes.
- Block scopes are assigned a lifetime from an incremental counter. This has a useful property when iterating over each scope in order where smaller lifetime values will always live longer than higher lifetime values. This is true because inner scopes are always entered last therefore will have a higher lifetime value and an inner scope cannot live longer than its outer scopes.
- Lifetimes of variables are assigned to have the same lifetime as the block it resides in.
- Whenever a value is borrowed the lifetime property is used to compare the values to ensure that the borrowed value lives long enough.
- Each let expression has its own reference counter which is used to ensure memory safety when dealing with multiple references. Every time a new borrow occurs the reference counter for the owned value has to first count the new reference and check that the following conditions are met:
 - Multiple immutable references, no mutable references
 - One mutable reference, no immutable references
- There is no concept of move semantics in this borrow checker since all types are primitives and they get copied instead of moved.

4.2 Examples

```
1 fn inc(x: &mut i32) {
      *x = *x + 1;
3 }
5 fn test_references_1() {
      let mut a: i32 = 10;
      let b: \&i32 = \&a;
      let c: \&i32 = (\&a);
      inc(&mut a);
9
10 }
11
12 fn test_references_2() {
      let mut a: i32 = 10;
      inc(&mut a);
15
      let b: \&i32 = \&a;
16 }
17
18 fn test_references_3() {
      let mut a: i32 = 10;
      let b: &mut i32 = &mut a;
      let c: &mut i32 = (&mut a);
21
22 }
24 fn test_returning_reference() -> &i32 {
      let a: i32 = 10;
      &a
27 }
19 fn test_reference_out_of_scope() {
      let mut a: \&i32 = \&0;
      {
31
           let b: i32 = 5;
32
           a = \&b;
      print_int(*a);
35
36 }
37
38 fn test_mutate_while_borrow() {
      let mut a: i32 = 5;
      let b: \&i32 = \&a;
      a = a + 5;
      print_int(*b);
42
```

Running this code shows all the borrowing errors that the compiler is capable of catching. This program is designed so only one error is reported per function.

```
firstc borrowing.sq
2 borrowing.sq:9:9: error: cannot borrow 'a' as mutable because
      it is also borrowed as immutable
4 9 I
          inc(&mut a);
              ```` immutable borrow occurs here
 borrowing.sq:15:19: error: cannot borrow 'a' as immutable
 because it is also borrowed as mutable
 let b: &i32 = &a;
9 15 |
 ^~ immutable borrow occurs here
10
11
12 borrowing.sq:21:24: error: cannot borrow 'a' as mutable more
 than once
13
 let c: &mut i32 = (&mut a);
14 21 I
                               ```` immutable borrow occurs
     here
16
17 borrowing.sq:26:6: error: cannot return value borrowed from
     this function
19 26 |
           &a
              borrowed value will outlive owned value
20
22 borrowing.sq:33:13: error: 'b' does not live long enough
24 33 I
               a = \&b;
                   ^~ borrowed value does not live long enough
27 borrowing.sq:41:5: error: cannot assign to 'a' because it is
     borrowed
29 41 |
           a = a + 5;
                      assignment to borrowed 'a' occurs here
```

4.3 Requirements and Contributions

The borrow checker is able to detect and reject ill-formed borrows using only lexical scoping. For the borrow checker a first draft of the specification was actually first written before the implementation and still remains in the source code. The specification was refined after finishing the project. The only thing not implemented was non-lexical scoping and move semantics.

5 Intermediate Representation

This intermediate representation is based of LLVM IR but does not completely follow the SSA form because there are no phi-nodes nor any control-flow graph. The intermediate representation was created to make the backend codegen easier therefore it is closer to an actual assembler level language. The conversion from AST to the IR uses a pre-order walk through each node in the AST and converts each of them separately.

5.1 IR Instruction

Instructions are stored as three-address code so each instruction has up to three operands and one opcode. Also the type of the first operand in each instruction is included to help the backend to figure out how many bytes to use. This is because booleans are represented as signed byte and integers are 4-bytes. Operands can either be an identifier or a literal.

These are the supported opcodes in the IR:

```
pub enum IrOpcode {
      Nop,
      Alloca, // op1 = alloca ty
3
      AllocParams, // allocates all defined parameters
      Copy, // op1 = op2
      CopyFromDeref, // op1 = *op2
6
      CopyFromRef , // op1 = &op2 (always mutable)
      CopyToDeref, //*op1 = op2
      Clear, // op1 = 0
      Add, // op1 = op2 + op3
10
      Sub,
      Mul,
13
      Div,
      Pow,
14
      Mod,
      And,
16
      Or,
17
      Xor,
18
      Lt, // op1 = op2 < op3 (op1 always boolean)
19
20
      Gt,
21
      Ge,
22
      Eq,
23
24
      Ne.
25
      IfLt, // jump op3 (if op1 binop op2 equals true)
      IfGt,
26
      IfLe,
27
      IfGe,
```

```
IfEq,
      IfNe,
30
                 // jump op1
31
      Jump,
                 // label op1
      Label,
32
                 // param op1 (ordered left-to-right)
      Param,
33
                 // op1 := op2(...) (#parameter stored in op3)
      Call,
34
                 // return op1 (where op1 is optional)
      Return,
35
      Prologue, // marks beginning of function
36
      Epilogue, // marks end of function
37
38 }
```

5.2 Example

Here is a very simple example showing let bindings with simple binary add expression.

```
firstc -r "let x: i32 = 20 + 10;" --backend=x86 --print=ir

main:
    prologue
    alloc_params
    %x = alloca i32
    %0 = add i32 20, 10
    %x = copy i32 %0
main1:
    epilogue
```

The -r command automatically creates a main function if there is not one already specified. The first line is a label defining where main starts similarly to the second label main1 which marks the end of the function. All functions starts with a prologue and ends with epilogue which is for backend specific use, mostly they serve as stack initialization and cleanup respectively. Next $alloc_params$ allocates parameters, however main does not take any parameters so this does nothing. Then alloca~i32 reserves 4 bytes on the stack, then the add instruction performes the addition 20+10 and stores it in variable %0 which is a temporary register. Note all the names starting with % are local variables and if it has no name like %0 it is temporary, also each name has an extra number (e.g. main1) this is to prevent aliasing internally since everything is stored in hash tables. Finally the copy commands just copies the data of %0 like a regular assignment into %x. This should be enough to give an idea of how the IR works in this language so next let's look at the actual x86 machine code generated.

6 X86 Backend

The x86 backend translates each IR instruction to machine code one by one starting always with the main function. Note that this backend can print the assembly code but it does not actually generate any valid assembly code, the main issue is that only 64-bit register types are printed. This backend is focuses on generating valid machine code so there is no need for an external assembler. There is no guarantee that this will run on every processor it has only been tested on one x86 64-bit processor but might also work on 32-bit versions too, but it has not been tested. This part of the compiler essentially boils down to encoding instructions described in Intels manual, but also it has to generate multiple instructions since the IR instructions are not one-toone with x86 instructions. For example there is no prologue opcode on x86 so it generates potentially multiple x86 instructions. The result of compiliation is a list of unsigned bytes which are copied to a new memory page marked with read and execution flags so it can be executed just-in-time. There is no support for generating actual executables but just-in-time was implemented by using the operating system APIs. The only problem with generating executables is that intrinsics needs to be linked in which seems to be more hassle than it is worth. This is not an optimizating backend there are some small optimizations tricks in some places but the focus of writing this backend was to learn of how x86 backends can be implemented.

6.1 Examples

Of course the *examples/demo.sq* program works as expected but it generates a lot of assembly code, so it is impractical to use for studying how this backend works. Lets start by using the very simple example used in the previous section.

```
firstc -r "let x: i32 = 20 + 10;" --backend=x86 --print=asm

main:
    push    rbp
    mov    rbp, rsp
    mov    rax, 20
    add    rax, 10
    mov    dword ptr [rbp - 4], rax

main1:
    pop    rbp
    ret
```

The prologue always does the first two instruction to first make sure that the

base pointer is stored and the new base pointer is set the the stack pointer. The rest looks very similar to the IR except that the add instruction cannot take two immediates (or literals) at once. Thus the add instruction has to first move the left-hand side to a temporary register and then the perform addition with the temporary register. The register allocation is aware of which registers are general purpose and how many there are (64-bit mode introduces a few more and this backend can use those). It is also necessary for the register allocator to know whenever a register is no longer in use so it can be automatically freed. This is done by checking the live intervals of variables which is provided by the IR. The alloca was moved after the addition and stores it in stack offset 4-bytes as expected. The epilogue performs stack cleanup which resets the stack pointer. It is worth mentioning this now this did not allocate any stack space which was intentional as this is called a "leaf" function since it doesn't call any other functions, thus it does not need any allocated stack space.

Lets look at a slightly more complicated program with a slow version of the *fibonacci* program listed below.

```
fn main() -> i32 {
    return fib(33);
}

fn fib(x: i32) -> i32 {
    if x < 2 {
        return x;
    }
    return fib(x - 1) + fib(x - 2);
}</pre>
```

```
firstc examples/fib.sq --backend=x86 --print=asm
3
4 main:
      push
            rbp
      mov
            rbp, rsp
6
            rsp, 0
      sub
            rcx, 33
      mov
      call
            fib
            main1
10
      jmp
main1:
      add
            rsp, 0
             rbp
13
      pop
      ret
14
15 fib:
      push
            rbp
  mov
            rbp, rsp
```

```
18
       sub
              rsp, 16
       mov
              dword ptr [rbp - 4], rcx
19
              dword ptr [rbp - 4],
       cmp
20
21
       jge
              rax, dword ptr [rbp - 4]
22
       mov
              fib1
23
       jmp
  .if_exit:
24
              rax, dword ptr [rbp - 4]
25
       mov
              rax, 1
       sub
26
              rcx, rax
27
       mov
28
       call
              fib
       mov
              rbx, dword ptr [rbp - 4]
29
       sub
              rbx, 2
30
              dword ptr [rbp - 8], rax
       mov
31
       mov
              rcx, rbx
32
33
       call
              rcx, dword ptr [rbp - 8]
       mov
34
              rcx, rax
       add
35
36
       mov
              rax, rcx
       jmp
              fib1
37
38 fib1:
39
       add
              rsp, 16
40
       pop
               rbp
       ret
```

The first difference is that now the stack pointer is subtracted except in main the value 0 was subtracted which might be considered a bug or oversight. There is another oversight on line 10 where there is a jump to the label on line 11. These do not actually affect the results of executing the program but wastes some spaces and CPU clock cycles. In main there is a call to fib and the argument is stored in RCX which is based of the Microsoft x64 calling convention, there is also support for sysv64 use to call intrinsics on Linux or Mac based operating systems. In both calling conventions RAX is used to store the return value. Next the fib function has an if-expression which is converted to a conditional relative jump. The condition is always inverted because when the jump should go over the first block to the second block or exit the if-expression. Since the order of the blocks are not changed it is more efficient to invert the condition otherwise more jumps would need to be added.

There is one major challange when setting jump distances which is that whenever one relative offset needes jump longer than -127 or 128 bytes. For longer relative jump distances more bytes have to be added both for the opcode and to promote to 4-byte offset. This can obviously mess up any other previously calculated relative jumps that tries to jump over this one. The code for resolving entangled relative jumps is very complicated, possibly

buggy and very messy. It works similar to a plane sweep alogrithm except it starts at the bottom of the program and sweeps upwards (discretely). When the sweep line enters an event point processing is done An event point is defined for each relative jump and is the maximum between the byte position for the jump instruction and the byte position that the jump is targeted for. At every event point it adds the jump to a list of active jumps and iterates over all the current active jumps to see if any jump needs to be removed from the list. The invariant holds that whenever a jump is removed from the list it will never need to be recalculated because adding bytes before the jump won't affect relative distances. Bytes are never added before any of the active jumps and whenever bytes are added all the active jumps needs to check if they have to also jump over those bytes or not. As previously mentioned the backend is not concerned with generating valid assembly code but instead focused on generating actual machine code which looks like this:

```
firstc examples/fib.sq --backend=x86 --print=machinecode

ff f5 48 8b ec 48 81 ec 00 00 00 c7 c1 21 00

00 00 e8 0c 00 00 eb 00 48 81 c4 00 00 00 00

8f c5 c3 ff f5 48 8b ec 48 81 ec 10 00 00 00 89

4d fc 81 7d fc 02 00 00 00 7d 05 8b 45 fc eb 2c

8b 45 fc 81 e8 01 00 00 00 8b c8 e8 d3 ff ff ff

8b 5d fc 81 eb 02 00 00 00 89 45 f8 8b cb e8 c0

ff ff ff 8b 4d f8 03 c8 8b c1 eb 00 48 81 c4 10

10 00 00 00 8f c5 c3
```

6.2 Register Allocation

The implemented register allocator is very basic and is not designed to be optimal or improve the performance of generated code. The purpose of this register allocator is to essentially map an infinite number of fake registers to a small set of hardware regsiters. Let's start looking at the IR's "register allocator" which essentially generates a unique variables for each new temporary variable. Variables in the IR are stored as a symbol (or identifier) and an index (i.e. together it's two u32 variables) which ensures uniqueness for variables with the same symbol. Temporary variables can be easily identified because they use the symbol empty string which cannot be defined by the user, the index is also used to distinguish between temporary variables. Each variable is also assigned a live interval which defines an where in the IR the variable is active and still needs to hold its hardware register. The purpose

of live interval is to ensure that the fake registers don't keep its hardware registers for longer than needed.

Now given the IR information i.e. list of IR instructions and hash map of live intervals the register allocation is very simple in theory but slightly harder in practice. This is because some inconveniences in the design of my system and also that x86 have stricter rules than my IR which further complicates this solution. For now on the term register is always referring to hardware register. The basic idea is to track both free and allocated registers at all times, so in order to spill a register to stack the register allocator has to know what variable a particular register is bound to. There is also another storage for all active local variables which maps variables to the corresponding operand it can be read from i.e. stack, register or literal. This storage needs to be notified whenever variables are spilled which makes it also slightly more tricky and buggy because of the data redundancy, if the structures become out of sync then the backend may generate incorrect code.

The allocate register function in src/x86.rs first checks if there are any available registers. If it's true then a register is just dequeud from queue of free registers and added to the queue of allocated registers together with its bound identifier. If it's false then a registers is dequeued from the allocated registers and looks it its operand it is stored at to then move it to a new location on the stack, the register freed is then used to allocate the new variable with. The register allocator is designed to never fail because of the assumption that union of the free registers and allocated register should equal the total set of general purpose registers, so if the available register is empty then there is always possible to spill something. If this assumption is broken then the register allocator essentially does the wrong thing and will result in an incorrect program. This is where most bugs have occured because something was not uppdated correctly in the datastructure so a register might be ignored which can easily break the program, this is then a compiler bug and not an actual user level error. There is also a free_register function which simply reverses the process removes the allocated register and adds it to the free registers. After every translated IR instruction the allocated registers are iterated and any variable that is outside its live interval will be automatically freed. Besides allocating fake registers from the IR it is also possible for the backend to allocate registers for example IDIV instruction requires specific registers to be used. The IDIV instruction in particular is complicated because the system was not designed to allocate specific registers only allocate a random available or spilled register. It is also possible for the IR to generate $\%0 = add \ i32 \ 1$, 1 which is not valid on x86 so the right-hand side is moved to temporary allocated register and is freed afterwards.

In order to make this clear let's look at a very simple example that also

illustrates both allocation and spilling to stack. Since the backend is very keen on not using registers for longer intervals this example is executed with only using two registers RAX and RCX. The code for the this example looks like this:

```
1 fn main() -> i32 {
2    let x: i32 = 10;
3    return (1 + 10) - (x + x);
4 }
```

And the IR looks like this:

```
main:
prologue
alloc_params

%x = alloca i32
%x = copy i32 10
%1 = add i32 1, 10
%2 = add i32 %x, %x
%0 = sub i32 %1, %2
return i32 %0
main1:
epilogue
```

The first register allocation occurs on the assignment of variable %1. Actually there are two allocations happening here the first is when temporarily storing 1 to RAX before performing the addition (adding two immediates is invalid in x86). This gets freed immediately after the add instruction and the result %1 will just allocate RAX again however this time the live interval is specified by the IR and will live longer.

```
main:
    push rbp
mov rbp, rsp
mov dword ptr [rbp - 4], 10
mov rax, 1
add rax, 10

...
```

The third register allocation occurs on the assignment of variable %1. Again there is a temporary allocation of RCX because adding two memory addresses is invalid in x86. Then afterwards RCX will be allocated to %2.

```
mov rbx, dword ptr [rbp - 4]
add rbx, dword ptr [rbp - 4]
```

Now both RAX and RCX are allocated and both are still live because in the next instruction they are subtracted %1-%2 and the result should be stored in %0. Since there are no available register to allocate for %0 it has spill RAX to stack and allocate it to %0 instead, then %1 will be now stored

on stack location RBP-8. Now the assumption here is that the allocated register could come from anywhere so assume it can have any random value, thus the left-hand side %1 has to be loaded again to RAX in which we know is stored at stack location RBP-8 (stored in local variable table).

```
mov dword ptr [rbp - 8], rax
mov rax, dword ptr [rbp - 8]
sub rax, rbx
jmp main1
main1:
pop rbp
ret
```

Note that it would still be valid code if the allocation of %0 was skipped because the result of %1 is not used anywhere else, however this register allocator is not smart enough to recognize this.

6.3 Performance Improvements

Just for fun lets see how much faster this backend is compared to the interpreter. Let's run the *examples/fib.sq* code which is of course not an efficient way to implement *fibonacci* sequence.

```
firstc examples/fib.sq --backend=interp --profile

Interpreter exited with code 3524578
Interpreter execution time: 7.173111 seconds

firstc examples/fib.sq --backend=x86 --profile

Program exited with code 3524578
Program execution time: 0.0255269 seconds
```

The speed up from running actual machine code is quite large compared to the interpreter. This does not count the time to construct the machine code but even that would still be way faster.

7 Learning Outcomes

Lexical analysis, syntax analysis, and translation into abstract syntax. I have learnt about lexical analysis which converts source code into a stream of tokens. Tokens combines one or multiple characters and gives them a label e.g. "10" has two characters and is an integer literal token. I have implemented my own lexer for another compiler project.

I have also learnt about syntax analysis which uses the stream of tokens and the grammar for a language to construct an abstract syntax tree. This is not something I have practically implemented or used myself in my projects.

Regular expressions and grammars, context-free languages and grammars, lexer and parser generators. I have learnt a little bit about how grammars and context-free grammars work but this is something I haven't applied in my implementation. The EBNF grammar was specified as part of the assignment but was not used in writing the actual parser.

In this course I have implemented a parser for a mini Rust language using the parser generator library *nom*. I have also implemented my own parser using a lexer for another compiler project. While I have not used parser generators and grammars in practical implementations, I've found that parsing is a relatively simple problem if it is broken down into first lexing and then building the abstract syntax tree.

Identifier handling and symbol table organization. Type-checking, logical inference systems. As mentioned in Section 1.3 identifiers are converted into symbols which are cheap to copy and can easily be used to check if two symbols are equal by their id. Symbols are also easy to store in hash tables which is used by most compiler stages to keep track of variables.

I have learnt about type-checking which is the process of ensuring correctness of types and their usage according to the specified type rules. However as mentioned in Section 3.3 I didn't use the type rules directly when writing the type-checker but instead used Rust as a guide and common sense.

In the course we also looked at structural operational semantics for defining the rules for how the code should be interpreted and also for defining rules that the type checker should follow. However these were not used in the actual process of implementing both the interpreter and type checker.

Intermediate representations and transformations for different languages. I have looked at intermediate representations for LLVM and implemented a similar style however not fully committing to the SSA form. I do find however that LLVM is a very interesting way to bring more languages to compiled form, e.g. this is for example being done for web with webassembly.

Code optimization and register allocation. Machine code generation for common architectures. I didn't look much at code optimizations but some work was put into doing proper register allocation, however my version of the register allocator is still not very efficient. One notable optimization that I mistakingly choose to implement was the relative jumps with single byte offsets whenever possible.

I also didn't use LLVM for my project, instead I decided to build my own x86 backend because I wanted to understand how something like LLVM could work. For this I had to learn about how instructions are encoded in x86 and about how to run code just-in-time. Trying to understand LLVM by looking at their source code is probably not a good way to learn it and just using it will probably not give much insight into the inner workings either.