

$$0 = (0, 0, 0) \quad \text{or } f_0 = 0$$

$$t = (0, 1, 0) \quad f_1 = 3$$

$$t^2 = (1, 0, 0) \quad f_2 = 9$$

$$t^3 = (0, 1, 2) \quad f_3 = ?$$

$$GF(\mathbb{3})$$

$$f(t) = t^3 + 2t + 1 = 0$$

$$t^3 = -2t - 1$$

$$t^3 = 1 \cdot t + 2$$

$$|-2| \bmod(3) = 1$$

$$|-1| \bmod(3) = 2$$

$$1 \cdot t + 2 = (0, 1, 2) \Rightarrow 1 \cdot \mathbb{3} + 2 = 5$$

$$GF(3^3) \mid 3^3 = 27$$

$$y_1 = a_1 x_1 + b_1, a_1 \neq 0$$

$$a_{i+2} = a_{i+1} + a_i; i=1,2,3$$

$$b_{i+2} = b_{i+1} \cdot b_i; i=1,2,3$$

de adunare + mod(3)

$$a_1 = (0, 2, 1) = t^{16}$$

$$a_2 = (1, 1, 1) = t^6$$

$$b_1 = (0, 0, 2) = t^{13}$$

$$b_2 = (1, 1, 0) = t^{10}$$

$$(13 + 10) \bmod(26) = 23$$

valoarea din camp GALOIS

Cifrare litere

(a)	S
i(b)	19 (index literă alfabet)
x(c)	(2,0,1)
x(d)	25
a(e)	(1,0,2) (indexul din tabelă pag 2 a_{19})
a(f)	12 (t-ul pentru a(e) tot pag 2)
b(g)	(0,1,1) (ne ia puterea din tabelul Galois t pentru a(f))
b	9 (din tabel, valoarea lui b(g))
(h)	26
(i)	Z (index literă)

În câmpul Galois, $19 = t^{25}$
 $= (2,0,1)$

$$\begin{aligned}
t^0 &= (0, 0, 0) & f_0 &= 0 \\
t^1 &= (0, 1, 0) & f_1 &= 3 \\
t^2 &= (1, 0, 0) & f_2 &= 9 \\
t^3 &= (0, 1, 2) & f_3 &= 5 \\
t^4 &= (1, 2, 0) & f_4 &= 15 \\
t^5 &= (2, 1, 2) & f_5 &= 23 \\
t^6 &= (1, 1, 1) & f_6 &= 13 \\
t^7 &= (1, 2, 2) & f_7 &= 17 \\
t^8 &= (2, 0, 2) & f_8 &= 20 \\
t^9 &= (0, 1, 1) & f_9 &= 4 \\
t^{10} &= (1, 1, 0) & f_{10} &= 12 \\
t^{11} &= (1, 1, 2) & f_{11} &= 14 \\
t^{12} &= (1, 0, 2) & f_{12} &= 11 \\
t^{13} &= (0, 0, 2) & f_{13} &= 2 \\
t^{14} &= (0, 2, 0) & f_{14} &= 6
\end{aligned}$$

$$\begin{aligned}
t^{15} &= (2, 0, 0) & f_{15} &= 18 \\
t^{16} &= (0, 2, 1) & f_{16} &= 7 \\
t^{17} &= (2, 1, 0) & f_{17} &= 21 \\
t^{18} &= (1, 2, 1) & f_{18} &= 16 \\
t^{19} &= (2, 2, 2) & f_{19} &= 26 \\
t^{20} &= (2, 1, 1) & f_{20} &= 22 \\
t^{21} &= (1, 0, 1) & f_{21} &= 10 \\
t^{22} &= (0, 2, 2) & f_{22} &= 8 \\
t^{23} &= (2, 2, 0) & f_{23} &= 24 \\
t^{24} &= (2, 2, 1) & f_{24} &= 25 \\
t^{25} &= (2, 0, 1) & f_{25} &= 19 \\
t^{26} &= (0, 0, 1) & f_{26} &= 1
\end{aligned}$$

Q_i a_1 0 1 1 a_2 1 2 1 a_3 1 0 2 a_4 2 2 0 a_5 0 2 2 a_6 2 1 2 a_7 2 0 1 a_8 1 1 0 a_9 0 1 1 a_{10} 1 2 1 a_{11} 1 0 2 a_{12} 2 2 0 a_{13} 0 2 2 a_{14} 2 1 2 a_{15} 2 0 1 a_{16} 1 1 0 a_{17} 0 1 1 a_{18} 1 2 1 a_{19} 1 0 2 a_{20} 2 2 0 a_{21} 0 2 2 a_{22} 2 1 2 a_{23} 2 0 1 a_{24} 1 1 0 a_{25} 0 1 1 a_{26} 1 2 1

b_i				
b_1	0	0	2	13
b_2	1	1	0	10
b_3	2	2	0	23
b_4	1	2	2	7
b_5	1	2	0	4
b_6	1	1	2	11
b_7	2	0	0	15
b_8	0	0	1	26
b_9	2	0	0	15
b_{10}	2	0	0	15
b_{11}	1	2	0	4
b_{12}	2	2	2	19
b_{13}	2	2	0	23
b_{14}	0	2	1	16

b_{15}	0	0	2	13
b_{16}	0	1	2	3
b_{17}	0	2	1	16
b_{18}	2	2	2	19
b_{19}	0	1	1	9
b_{20}	1	0	0	2
b_{21}	1	1	2	11
b_{22}	0	0	2	13
b_{23}	2	2	1	24
b_{24}	1	1	2	11
b_{25}	0	1	1	9
b_{26}	2	1	1	20

	D	A
x	4	1
x-pol	(0, 1, 1)	(0, 0, 1)
x-exp	3	26
a-pol	(2, 2, 0)	(0, 1, 1)
a-exp	23	9
b-pol	(1, 2, 2)	(0, 0, 2)
b-exp	7	13
h	18	3
i	R	C

$$y_4 = t^{23} \cdot t^9 + (1, 2, 2)$$

$$= t^6 + (1, 2, 2) =$$

$$= (1, 1, 1) + (1, 2, 2) = (2, 0, 0) = 18$$

$$y_1 = t^9 \cdot t^{26} + (0, 0, 2)$$

$$= t^9 + (0, 0, 2)$$

$$= (0, 1, 1) + (0, 0, 2) = (0, 1, 0)$$

$$= 3$$

