Elevnente de calcul integral 03.12.2021 (I) Driwn Live sefinite the fisch it is simperval. Spenson ce tunction of advante planishine pe i dans exists a function F: I - ik, an proprietation: a) Feste alliva ma pe j Mustinea privativele franctici f ne musulte ivæglate medefinati a bri f oi el nateata prin Sfirl dx = {F: i - 1/2 | Fentle primative a brify. fact & admite primitisce pe i atume + advinte a in Limitate of primitine pe i or abicult dana primative difert inthe elephints-a canstable: Sfixled x = Fixte = Fixte = Fixte)=fix, Tablort primativeles functiveles elementate Interietasi es resultante fundamentate 10 0 functse continuré, 7: j-12, adamte pleuntine @ Back f: i - e R admitte phimitive pli a funció f are preparetated los sarforens pe i

(Daga f: i internationale pe i a funció

detivada na fi i ine da un este caratione

darbans pe i consulte mecesaria en a

pe i) ten o consulte mecesaria en a Lonette f në adwite plemitive se i'er le en towethe f no aiba PD. se i'er f un ed oute pumitive pe I. you file fig : i -ik on f p g advet phrom fine pe i. Atuna:

a) It g admit primative re i n' [H(x) + g(x) . dx = [f(x) dx + [g(x) dx (adissimilate) b) (+1 & e IR as a fordrom to phi von tise n' I(d. fixi) dx = d. ffixi dx (among em talle) cor cans-James lesse de mon integrale 4/1/2 de sons

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set. O extreette a distina es amagent fras

ne un meste aptrentse Brimair.

as is se part prose into a oringure relation (d. \$14/+ Brg(x)). Ax = d. | \$MAX + B. Gendx = 1 physietalea de lamoritage a habye de timaritate a desirata. rastade de calent a shinntivelar 19 Metoda integrani survete (prin formule, on ajutolul ta be bulum plima fine Car) 4) S(x-3 Vx + Vx). dx = 5xdx-35 x2.dx+5x3 dx $= \frac{x^{2}}{2} - \frac{3}{3} \cdot \frac{x^{2}}{\frac{3}{2}} + \frac{x^{3}}{\frac{4}{3}} + C = \frac{x^{2}}{2} - 2 \cdot x\sqrt{x} + \frac{3}{4} \cdot x\sqrt{x} + C$ - 1 (x = - 3 x 6). dx = x = + = + = = = 3, x 3 - 3, 5, x + c uneon functiile de mb ivregrati trehuse en forma din salvelor plim simediate.

c) \ \frac{dx}{Vy-qxe} = \int \frac{dx}{Vq(\frac{a}{q}-y')} = \frac{3}{3}\int \frac{dx}{V\frac{a}{3}\frac{dx}{V\frac{dx}{V\frac{a}{3}\frac{dx}{V\frac{dx}{V\frac{a}{3}\frac{dx}{V\frac{dx}{ S Vain = arenin x + c - { aresim = + c = 1. oresim 3x + c = / (Vx2-3 + 1/x2-(V3)2) dx = (n/x + Vx2-3) + # 1 . ln | x-13 | + C er 5 3+ \x 2+ 9, dx = \frac{3}{x^2+9} dx + \frac{\sqrt{x}^2+4}{x^2+9} dx = 3. - arcfg = + 1 - 3. arcfg = + ho/x4/x4n 2) Metoda integration prim parti A vastà unetoda, ca si untadelle ell'ulate de suria mo ne noi listed sa a huner ea not explica de sur in regaze se in tabelor un se regaze se un pradus phinostineles inncellate nom este un pradus Il function. rephermé Ett fig: i - it, desivatule en desivate caustinue pe i. Atames Luntiste 4.9' of 4', g advent plum time pet or are luc relatia: Stirlagicaldx = fixt. girl - Stirligery dx (714. g(x)) = 7'14. g(x) + 714. g(x) (=> [(4(x1. 9(x1)) (xx = (4/1x1. 9(x) + 4(x). 9(1x) dx 4181. g(8) = 5 7 / M. g(x) dx + 5 \$181. g/1x) dx = 1 Still. 3/14 dx = fixt. 91xt - Still. 91xt dx]

Alegetra juvetisor + n' g' dim insteglala de ealerCat re face ulwithind ca integlula dem surun en de de integrate prim fasti sa flo mai nor de calculat deest coa initiala.

Moreoni metoda se a prica mecania, de viai multe ari. multe als. as $\int x^2, e^{x}. dx = f \cdot g - \int f' \cdot g dx =$ JIN = ex => g(x)= fexdx = ex = x'ex-f2x.exdx j=x2ex-2/xexdx. =]= / x'ex = x'. ex - 2 (xex-ex) 4 e = xex-2xex+2xex+C Ti y. lux - t. fx3 lnx, dx =1 fe x lax-ff. x dx J= [x3. ln x dx 4 1 = x . lux - x . lnx + xy + c @ j= fe, min bx dr; j= fedr. ch bx.dx iz sex. maskdx

\$141 = e = 1/1/2 diex ging nim by = gray = Sain by dx = - CABX =9 = - ex. cossx - fd. ex. (-cusy). dx I = - ex. 08/34 + 2. 10xx dx 1 - x, j = - ex couls / (10) the j= / ex. obj x. dx f(x/= edx = 5 f'(x) = d. edx gire MAY; girl= scon Axdx = 1. min Bx J'= e' min Ax - d fet. win / k, dx 2 j + j = ex, nim / 20 1 - d.j = - ex. on/3x 17 c | di +j' = ex nim/sk Apliente - metoda relationer de receeve seuten ealeulul shimm Firelar La re statuelle de réculente plotter integrale: In = flnx, dx In = Iln'x todx fixe lunx = fixe n. (lux) . & - 7 7 = [1.dx = x 21x101

$$\int_{n} = x \cdot \ln^{n} x - \int_{n} \cdot \frac{1}{x} \cdot \ln^{n} \frac{1}{x} \cdot x = 1x$$

$$\int_{n} = x \cdot \ln^{n} x - n \cdot \int_{n} \ln^{n} \frac{1}{x} \cdot dx$$

$$\int_{n} = x \cdot \ln^{n} x - n \cdot \int_{n-1} \int_{n-1} \int_{n-1} \int_{n-1} \int_{n} \frac{1}{x} \cdot \ln^{n} x \cdot dx$$

$$\int_{n} = x \cdot \ln^{n} x - n \cdot \int_{n-1} \int_{n-1} \int_{n} \frac{1}{x} \cdot \ln^{n} x \cdot dx$$

$$\int_{n} = x \cdot \ln^{n} x - n \cdot \int_{n} \int_{n} \frac{1}{x} \cdot dx$$

$$\int_{n} = x \cdot \ln^{n} x - n \cdot \int_{n} \int_{n} \int_{n} \frac{1}{x} \cdot dx$$

$$\int_{n} = x \cdot \ln^{n} x - n \cdot \int_{n} \int_{n}$$

In (1+ n-2) = - calx + (n-2). In-2 /: n-1 In= - 1 mmx + n-2 In-2 Exp To = I min's odx O In = S xh dx ; jn = S x dx ; Kn = S Vac-ye dx In = S x dx = Sxny. X dx

Y(x) = x n-1 = 4/(x) = (n-1) x n-2 In = x " · V x t+ at - SIn-1) · x " V x t+ at dx In = x " Vx exa = - (n-1) / x " (x +a?) dx In(1+n-1) = x / x exa2 - (n-1) · a2 · In-2 /: 2 (In = - x, Vx+ai - n, a: In-2) Ex In Kn;

Meto La 1 de neilevo Care de variatinto se neilliseasa cama explésia de ente integrala este un pradus de 2 functió, de a jalori speciala. con proprietation: as u este desiratula pe s' bl + ad mute phi von tine pe f, Fle Fo phi mistra a na pe j (F'(t) = f(t), (x) t = j')
Atunci: a) Functia (foll). M' ad mite primitive
ye j; B) \ f(x(x)). u'(x). dx = F(u(x)) + C Function u eve sunte care seithment variabile. fahrer de calcellat phi un Lina u orle Luntili de fahrer: f(u(x)). u'(x): Algorithm de aplicale. Of the interpretation, and integrate, Luntiile u'ul of tirand seama de fastul ca u'este un factor in accasta explété. @ se jace restambater de namatique U(x)= £ ni de calenteate onferentiala acentei relatio ucriet as duixi = dt as wixidx = dt in unhalula t, sutfel: 1+ = 1 7(+). dt = +(+) +C (4°) Se renine en natialnée installé, re: 1 41 u(x1). u'(x) dx = F (u(x)) +c [F(USFI)] = F'(USF). U'IK = f(USK), U'IK), 2.e.d.

selvel a peratical; Ix= Sfluirilalistalx ucriet = Sfithest = F(+1+c => F(ura)+c Asbientie : i - 1P @ S (1+x2) (alety x + 3) 4'(x1= 1+ x= 1 4(x) = arctgx +3; \$111= == u'M.dx=dt U(1x) = (arefgx+3) = 1+42 i 415/= t (= s one/gx + 3 = t =) 1+42 dx = dt 1+= 1+ of = lut + e = Ix = In(arcAgx +3) +C 4 f (1+ ln x/3; x? 1; U'141= + 1 M(x) = 1+ lnx ; f(t) = +3 U(x)= + (2) (1+ lnx) = + = 1 U'(x) dx = + dx = dt 1 = 1 dt = 1 = 1 = - 1 + c =)]x = - = (1+ enx)2. + c @ 1/2 x3. V1+x2 dx = /x2. V1+x2. x. dx UIXIE XCHIET => UIXINDX= 2x. dx=dt 1+ = + 1x2. Vx2+1.2xdx = 1 x2= t-1 It = 1 S(t-1. Vt. dt = 2 S(t Vt - Vt) dt = 2 st - + 2 st = 1 (t2 - t2) = f. tVt- 3 + TE + C =1/2x= = (x2+11): \x2+1 - = (x2+1). \x2+1 + C

A dana unitoda de relibratare de narialnio countabation on phima fahrwei de settinatique de nation Ente im accst eat amon de calculat a phimative de fahra:],: [fuly]dx [laipse de factohne will and integralay on prepredation: some discourse se i ia in verte na, ni: j-ri ense desirable no over derivota cantimo re ji b) f: J-R ente constenura put Atomer: as fork adownte prosumtive the i b) dad F: i-it ender plaim time a Luncter f(t). (U-1(t)) Pe i, a Lunci /fuckldx = Fruck/+C Practice & se face netternbarer de variable UIXI=t : M:Ì-J; M:J-Ì: Le dodnor x= M'(+); M:J-Ì: 3 se calenteato dx = (ū'(t))'. dt (4) Le calculate le = f(t). ü'(t) et = f(t) O se reruine la variable surffate: Sfinix)dx = F(N(x)) +c aplicated accasté mostades ne alitén den femetir lationale in mariationa t. de regula, persun Line a) 1 - 1 - ex . dx Exemple

ex= t => x = ent] => dx = (ent). Lt (unx=t c=) x = u'(t)) / dx = f. dt. It = 5 t dt = 5 dt = areget + c (2) \\ \frac{\frac{1}{x}}{\frac{1}{x}} \cdot \dx \\ \frac{1}{x} \\ = 6 \ \frac{t}{t-1} dt = 6 \ \frac{t^6-1+1}{t-1} dt = 6 \ \ \frac{t^6-1}{t-1} dt + \ \frac{dt}{t-1} \ \] tb-1 = (t-1)(t5+t4+t3+t2+t+1) = 6(t6+ t5+ t4+ t3+ t2+t)+66n/4-1/+ C Le inlarmente t en Vx =4 1x. 3 1x= 1 x -1 = t => x-1= t; x= t+1 dx=388t => == == == 5 (+4+) d+ = 3(f + t) + c; Se inflevoiente t en Tx1 (9) Ix = I minix, cayix, dx = Iminix, conix, nimx dx

casx = t => (- minx), dx = dt 1't = - [(-t'). t'. dt = [(t'-t').c+= t'-t'] + e = 1 1 x = cos x - cos x + c