

* 0-1 sorting:

ip: [↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓
1, 0, 1, 1, 0, 0, 0, 1]
0 1 2 3 4 5 6 7

Op: [0, 0, 0, 0, 1, 1, 1, 1]
 0 1 2 3 4 5 6 7

#1: insertion, bubble, selection - $O(N^2)$

~~#2~~: `arr.sort(compare)` - $O(N \log N)$

#3 : Counting / Count Sort Technique

- $$\begin{aligned} \text{cnt0} &= 0 \vee \neg \beta_4 \\ \text{cnt1} &= \phi \wedge \neg \beta_4 \end{aligned}$$

2. fill cat0 no. of zeros
fill cat1 no. of ones

```
int idx = 0
```

```
while (cnt > 0) {
```

$$\text{ans}[\text{idx}] = \text{id}$$

```
while (cnt1 > 0) {
```

```
arr[0] = 1  
idx++  
at1--;
```

Expanding Count sort 1, 2, 3, 4, 5, 6 sorting * This can be used only if elements are in range $0 \rightarrow 10^5$

\downarrow								
0	1	2	3	4	5	6	7	8

5	4	5	2	3	1	4	6	2
---	---	---	---	---	---	---	---	---

for ($0 \rightarrow n$) {

 num = arr[i];

 cnt[num]++;

}

for ($num=0 \rightarrow 6$) {

 while ($cnt[num] > 0$) {

 arr[idx] = num;

 idx++;

 cnt[num]--;

}

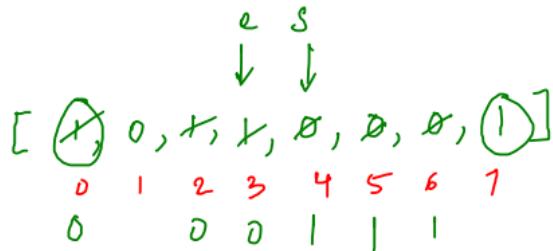
idx = 0, arr = []

cnt[0]	cnt[1]	cnt[2]	cnt[3]	cnt[4]	cnt[5]	cnt[6]
0	9	0	0	0	0	0
X	X	X	X	X	X	X
0	2	0	2	4	0	0
X	X	X	X	X	X	X
0	0	0	0	0	0	0

0	1	2	3	4	5	6	7	8
5	4	5	2	3	1	A	6	7

1	2	2	3	4	4	5	5	6
---	---	---	---	---	---	---	---	---

#4: two-pointer Technique



while ($s < e$) {

if ($\text{arr}[s] == 1 \text{ and } \text{arr}[e] == 0$) {

 swap($\text{arr}[s]$, $\text{arr}[e]$);

 s++; e--;

}

else if ($\text{arr}[s] == 0$) s++;

else if ($\text{arr}[e] == 1$) e--;

}

$$a(s) = 1$$

\Rightarrow not correct

$$a(s) = 0$$

\Rightarrow correct (start++)

$$a(e) = 1$$

\Rightarrow correct (end --)

$$a(e) = 0$$

\Rightarrow not correct

* Both are not correct

$$a(s) == 1 \text{ and } a(e) == 0$$

swap($\text{arr}[s]$, $\text{arr}[e]$)

s++, e--;

smallest greater element :

ip: [0, 1, 2, 3, 4, 5]
 ↑ ↓
 2
 4

op: [3, 2, 5, 4, -∞, 6]

* find minimum in $\{ \text{ele} > \text{arr}[i] \}$

curr_num = 2

smallest_greater = ∞ ≠ 3

4 > 2 9 > 2 6 > 2 5 > 2
4 < ∞ 9 < 4 6 < 3 5 < 5

curr_num = 1

smallest_greater = ∞ ≠ 2

8 > 1 4 > 1 3 > 1 6 > 1 5 > 1
8 < ∞ 4 < 2 × 3 < 2 × 6 < 2 × 5 < 2

curr_num = 4

smallest_greater = ∞ ≠ 5

6 > 4 5 > 4
6 < ∞ 5 < 6

* AS sorting 5 : $(1 \rightarrow 10^5)$ (+ve)

ip: $\begin{bmatrix} 5, & 6, & 2, & 7, & 4 \end{bmatrix}$
0 1 2 3 4

When will get max diff?
(a, b)

op: w, x, y, z

$$\Rightarrow w * x - y * z$$

\Rightarrow maxProd

$$w = 7 \quad y = 4$$

$$x = 6 \quad z = 2$$

$$7 * 6 - 4 * 2$$

$$\Rightarrow 42 - 8$$

$$\Rightarrow 34$$

$$\text{op} \Rightarrow (1^{\text{st} \max} + 2^{\text{nd} \max}) \\ - (1^{\text{st} \min} + 2^{\text{nd} \min})$$

$$a - b = \text{max diff}$$

$$a \uparrow - b \downarrow$$

$$\text{maxEle} - \text{minEle} = \text{maxdiff}$$

$$(w * x) - (y * z)$$

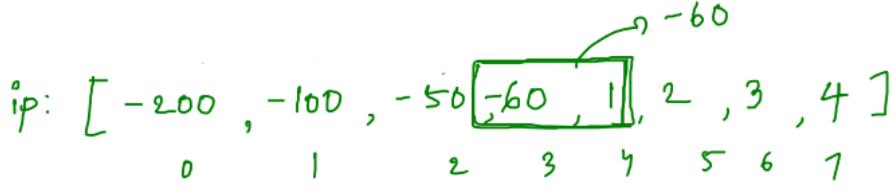
$a \uparrow \quad b \downarrow$

$$\text{maxProd} - \text{minProd} = \text{maxProddiff}$$

$$w \uparrow * x \uparrow = \text{maxProd}$$

$$y \downarrow * z \downarrow = \text{minProd}$$

what if the range of ele $(-10^5 \rightarrow 10^5)$:



OP:

$$(-200 + -100) - (-50 * 0)$$

$$20,000 - 0$$

$$\Rightarrow 20,000$$

1st min -ve + 2nd min -ve

$$\begin{aligned} & \text{--ve + --ve} \rightarrow \text{+ve} \\ & \text{and}(0) * \text{and}(1) \quad \left. \right\} \text{max prod} \\ & \text{and}(n-1) * \text{and}(n-2) \\ & \text{+ve + +ve} \rightarrow \text{+ve} \end{aligned}$$

1st max +ve + 2nd max +ve

max prod - min prod

$$\text{and}(n-1) * \text{and}(n-2) - \underline{\text{and}(0) * \text{and}(1)}$$

$$3 * 4 - (-200 * -100)$$

$$3 * 4 - (20,000)$$

$$\Rightarrow 12 - 20000$$

$$\Rightarrow -19988$$

~~Failed~~

(negative)

max Negative + min Positive \rightarrow -ve

1st min positive + 2nd min positive \rightarrow +ve

(no negative)

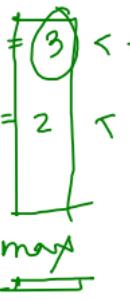
* As Sorting 4:

① ip: $[\begin{smallmatrix} 0 & 1 & 2 & 3 \\ 2 & 1 & 3 & 4 \end{smallmatrix}]$ $L = 3$

a, b, c \rightarrow maxEle - minEle $\leq L$

$$\begin{array}{lcl} (1, 2, 4) & \Rightarrow & 4 - 1 = 3 \leq L \\ (1, 2, 3) & \Rightarrow & 3 - 1 = 2 \leq L \end{array} \quad \left. \begin{array}{l} \text{max possible} \\ = 3 \end{array} \right\}$$

op: 3



② if $L = 2$,

$$\begin{array}{lcl} (1, 2, 3) & \Rightarrow & 3 - 1 = 2 \leq L \\ (1, 2, 4) & \Rightarrow & 4 - 1 = 3 \not\leq L \end{array}$$

op: 2

#2: Sorting

$O(n \log n)$

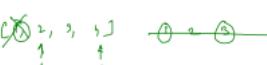
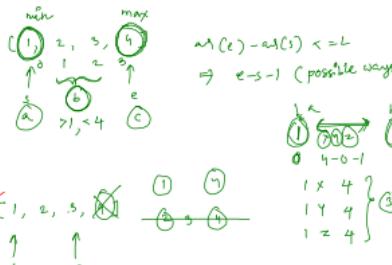
$\begin{bmatrix} 0 & 1 & 2 & 3 \\ 2 & 1 & 3 & 4 \end{bmatrix}, L = 3$

- X Count sort Technique
- X String Processing Technique
- ① Sliding window Technique
- (e.g. Two pointer Technique (when arr is sorted))

$\rightarrow [1, 2, 3, 4], L = 3$



$$\text{count } t = (e - s - 1) \\ = 2 - 0 - 1 \\ = 2$$



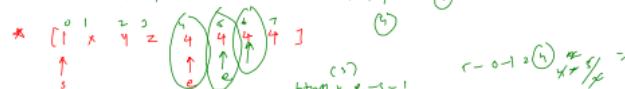
* $\begin{bmatrix} 0 & 1 & 2 & 3 \\ 1 & 2 & 3 & 4 \end{bmatrix}$

$s \quad e$

$3 - 1 \leq L$
 $2 \leq 2$

$4 - 1 \leq L$
 $3 \leq 3$

$$\text{count } t = (e - s - 1) \\ = 1 \\ = 1 + (2 - 0 - 1) \\ = 1 + 2 - 3 \\ = 3 + (3 - 1 - 1) \\ = 3 + 1 + 4$$



$$\text{count } t = (b[0] \times (b[0] + 1)) / 2 \\ = (4 + 2 + 1)$$



$$1 \times 4 \quad 2 \times 4 \quad 3 \times 4 \\ 1 \quad 4 \quad 2 \quad 3 \\ 1 \quad 2 \quad 4 \quad 3$$



$4 - 2 \leq L$
 $2 \leq 2$

$5 - 2 \leq L$
 $3 \leq 3$

$6 - 3 \leq L$
 $4 \leq 4$

$$1 \times 4 \quad 2 \times 4 \quad 3 \times 4 \\ 1 \quad 4 \quad 2 \quad 3 \\ 1 \quad 2 \quad 4 \quad 3$$

$$1 \times 4 \quad 2 \times 4 \quad 3 \times 4 \\ 1 \quad 4 \quad 2 \quad 3 \\ 1 \quad 2 \quad 4 \quad 3$$

