

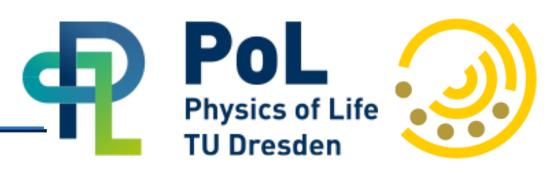


# Clustering K-means & density-based scan

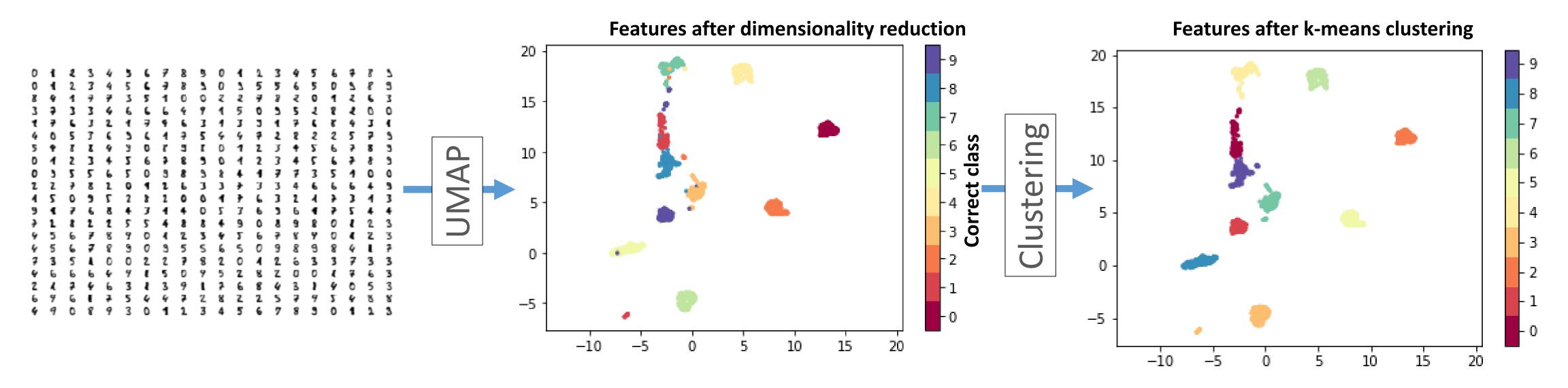
Johannes Müller







#### From digits example notebook:



In practice, this may not be possible – the true group is usually not known!

> Clustering allows to stratify data into groups without previous annotations

Source: <a href="https://archive.ics.uci.edu/ml/datasets/Optical+Recognition+of+Handwritten+Digits">https://archive.ics.uci.edu/ml/datasets/Optical+Recognition+of+Handwritten+Digits</a>

# K-means clustering

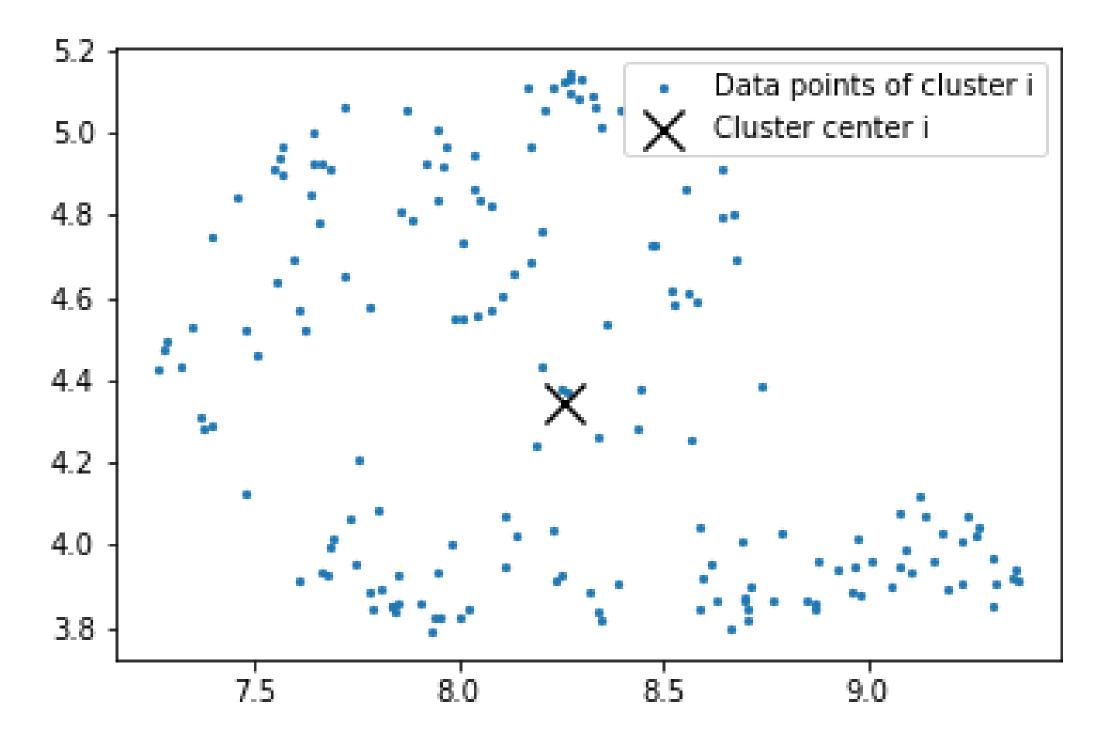


**Strategy:** Group data points into n groups so that variance within group is minimal

 $\sum_{i=1}^{k} \sum_{x_j \in S_i} ||x_j - \mu_i||^2$   $\mu_i$ : Center of cluster i

S<sub>i</sub>: Cluster i

 $x_i$ : Datapoint j

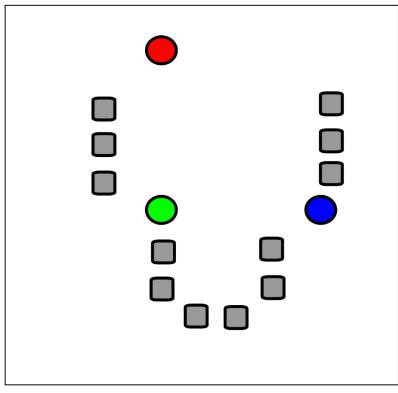


## K-means clustering

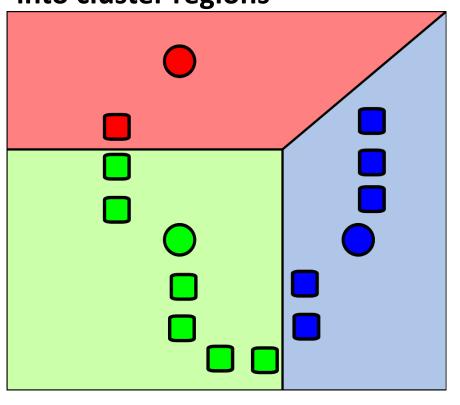


# **Strategy:** Group data points into n groups so that variance within group is minimal

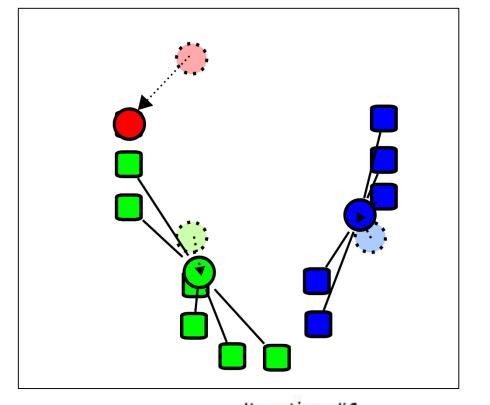
Step1: Random initialization of cluster centers



**Step2: Tessellation of space into cluster regions** 



Step3: Replace cluster center with centrois



In Python:

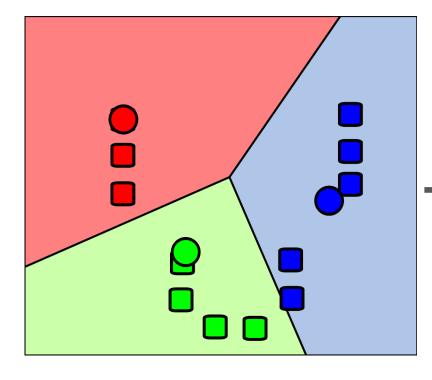
Import from sklearn import cluster

Create

clusterer = cluster.KMeans(n\_clusters=3)
clusterer.fit(X)

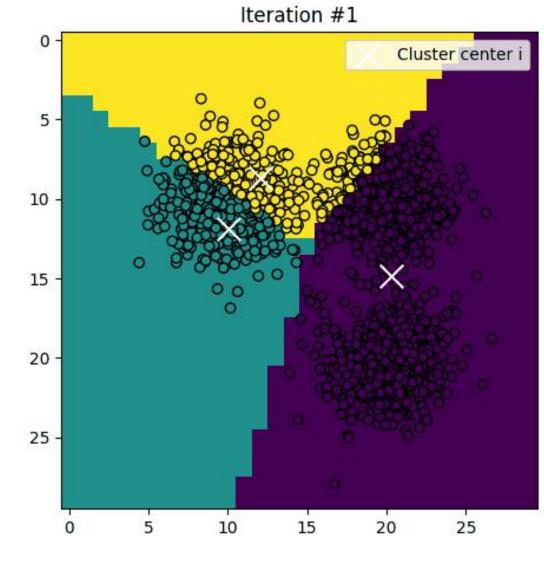
Predict

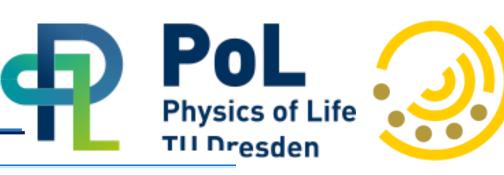
predicted\_class = clusterer.predict(X)



Step4: Repeat 2&3 until convergence

→ Fast convergence

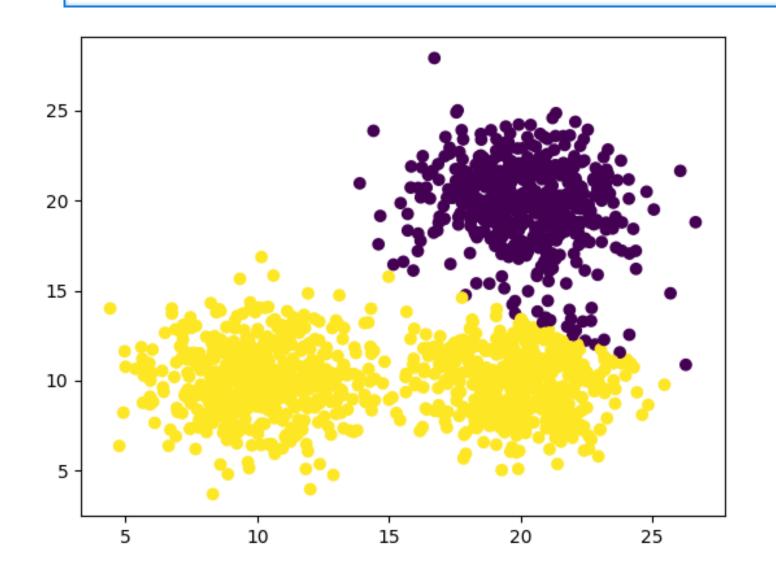


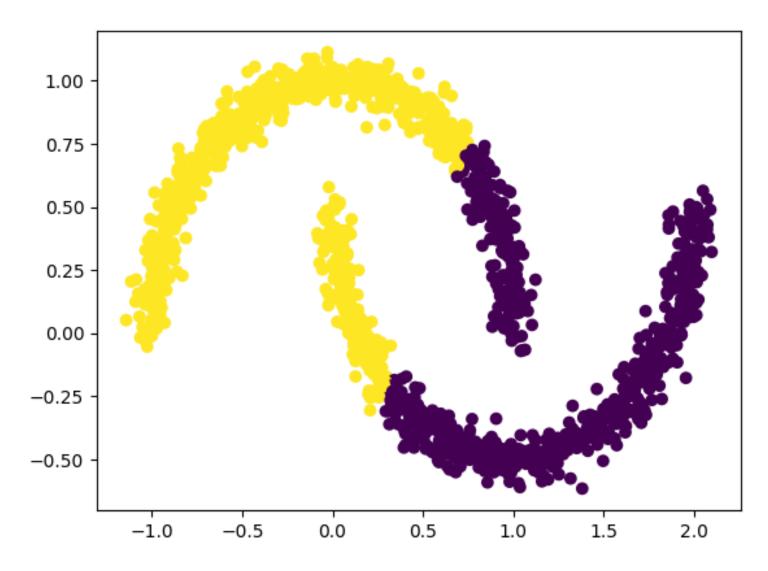


#### Strength and weaknesses

- Number of clusters needs to be known
- Clusters can not capture more complex topologies
- Very fast
- Based on Euclidian metrics → every new point can be assigned to a cluster

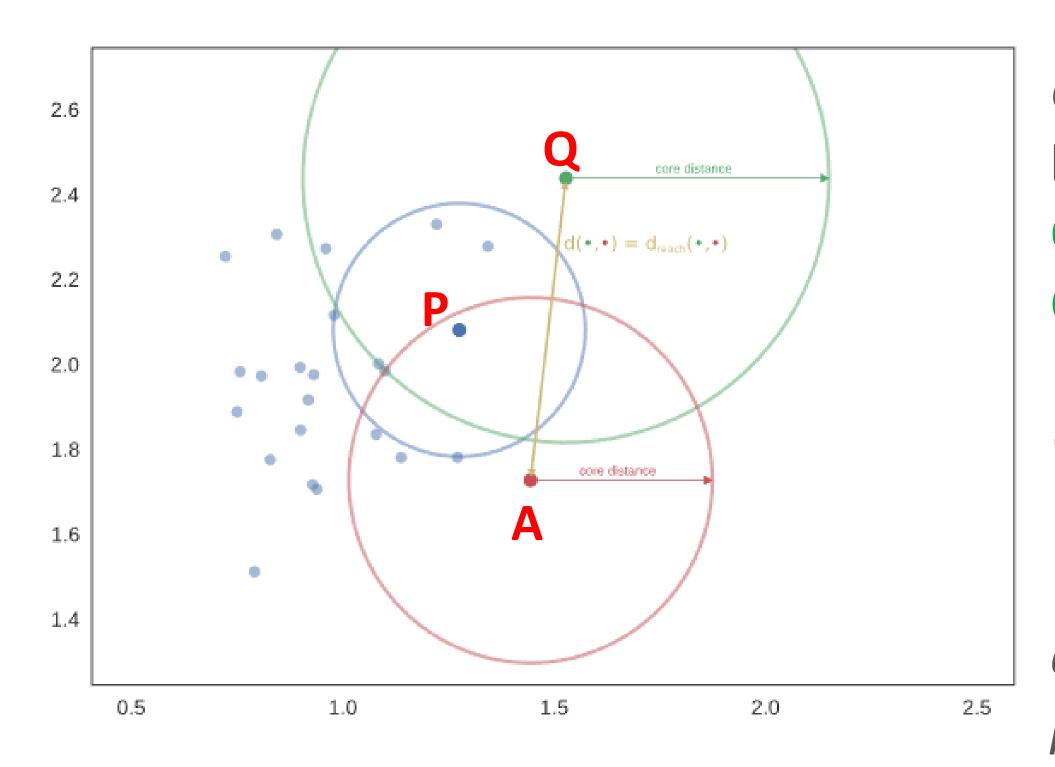
clusterer = cluster.KMeans(n\_clusters=2)
clusterer.fit(X)







Hierarchical Density-Based Spatial Clustering of Applications with Noise **Strategy:** Build neighborhood graph and identify strongly connected groups



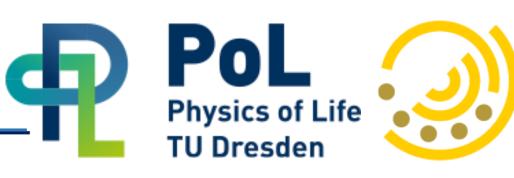
Core distance: Distance to n-th nearest neighbor

Distance metric: Mutual reachability

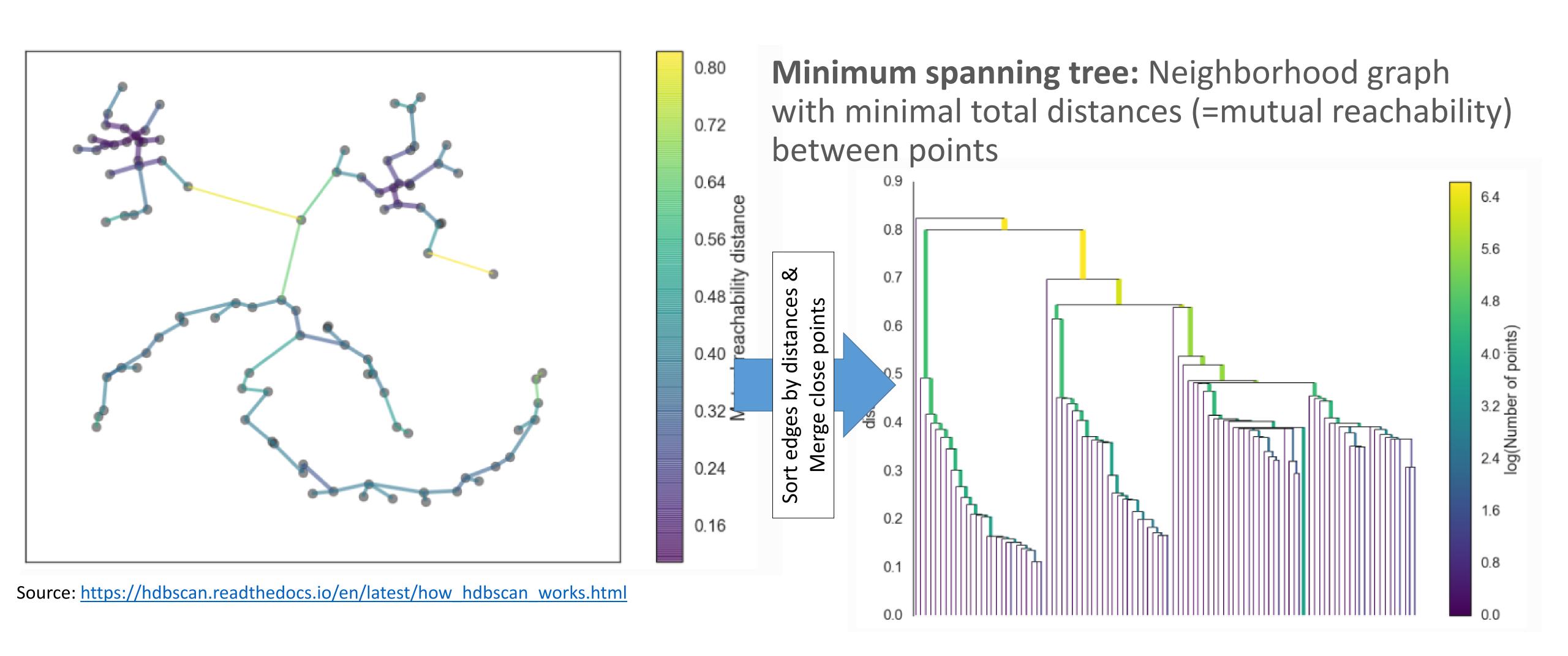
Core distance of  $Q > d(P, Q) \rightarrow d_{new}(P,Q) = core distance$ Core distance of  $Q < d(A, Q) \rightarrow d_{new}(A,Q) = d(A,Q)$ 

> Isolated points are pushed further away from clusters

"To find clusters we want to find the islands of higher density amid a sea of sparser noise [...] For practical purposes that means making 'sea' points more distant from each other and from the 'land'."

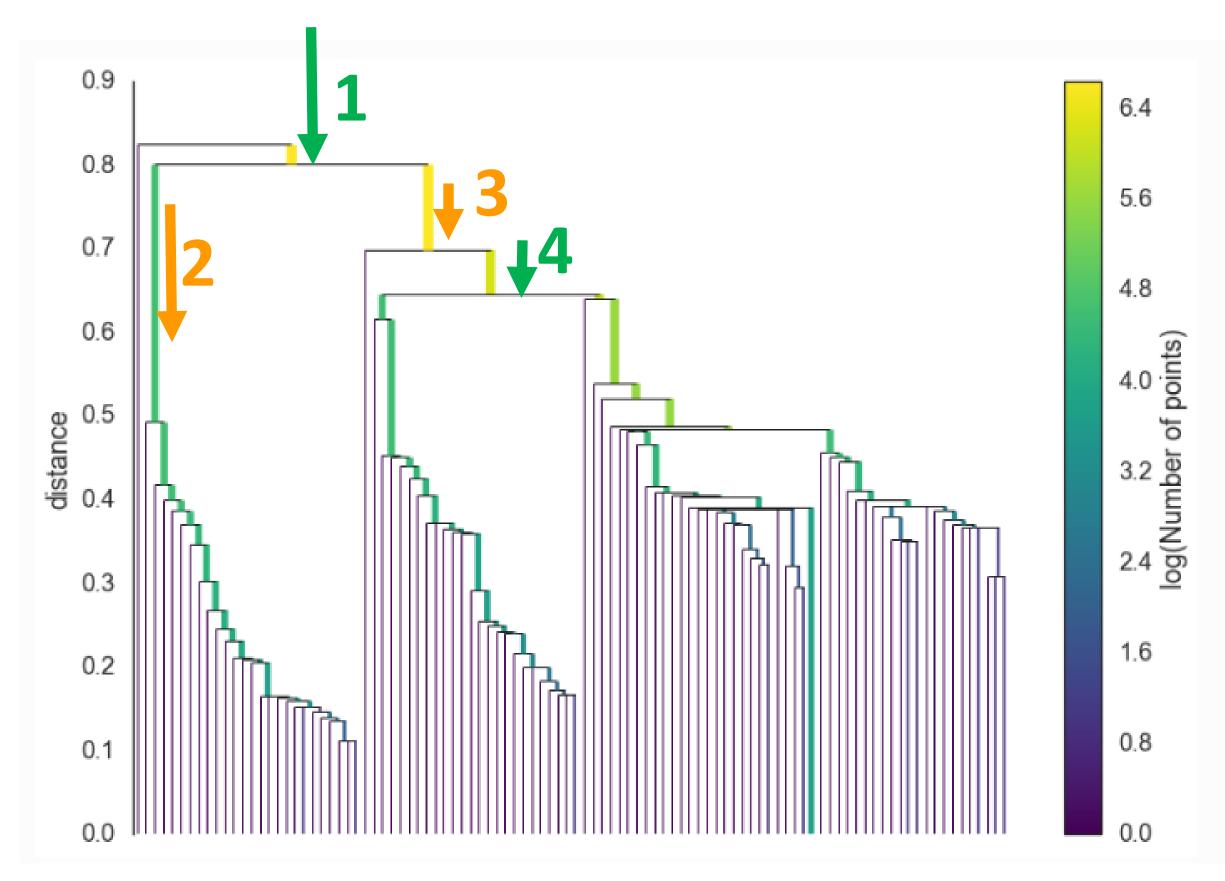


## Strategy: Build neighborhood graph and identify strongly connected groups





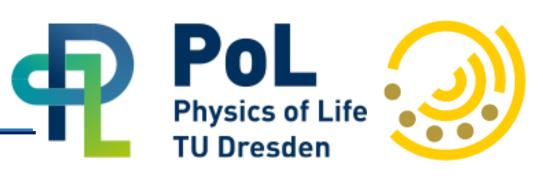
#### Strategy: Build neighborhood graph and identify strongly connected groups



Source: <a href="https://hdbscan.readthedocs.io/en/latest/how-hdbscan-works.html">https://hdbscan.readthedocs.io/en/latest/how-hdbscan-works.html</a>

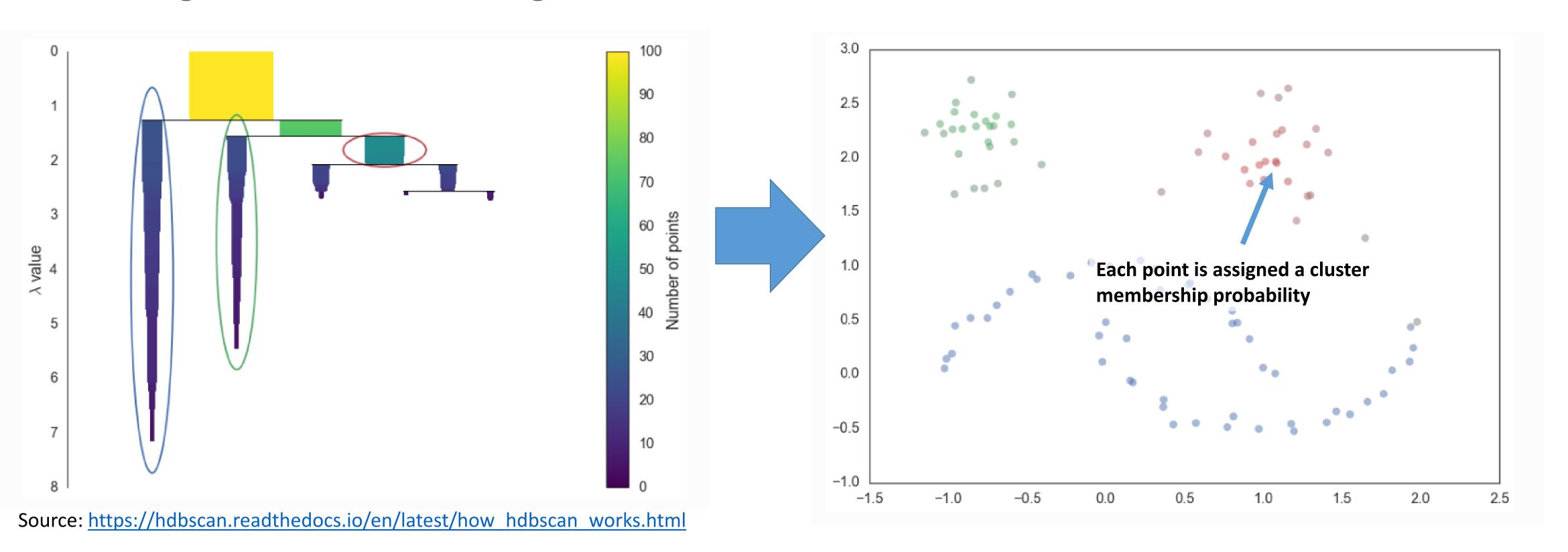
Condense the tree: Traverse graph from top to bottom and decide whether a new cluster is formed at every crossroads

- 1. If points are split into clusters here are both clusters larger than min\_size? Yes
- 2. No this part of the tree remains a single cluster
- 3. No this part of the tree remains a single cluster
- 4. Yes remaining points are split into new clusters here

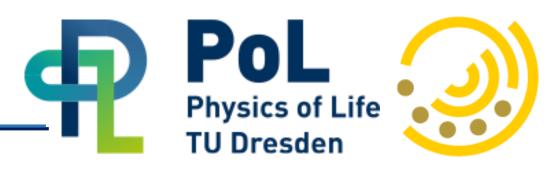


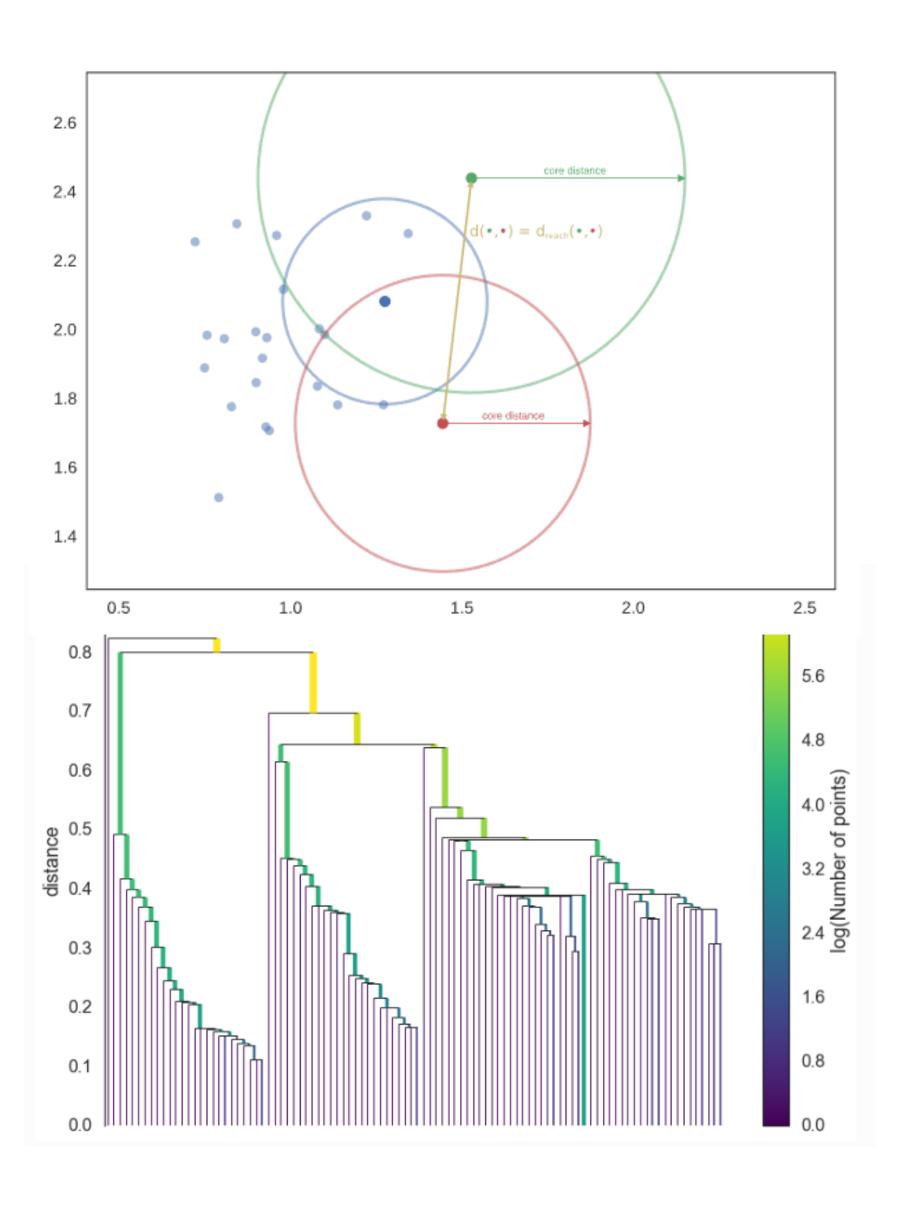
#### Strategy: Build neighborhood graph and identify strongly connected groups

Extracting the clusters with 'largest total ink area' leads to the final selection of clusters



# Variants of linkage-clustering





There are multiple ways to reconstruct the neighborhood graph and the clusters in the hierarchy schematic:

- Setting a maximum distance between two points to be considered neighbors -> DBSCAN https://scikit-learn.org/stable/modules/generated/sklearn.cluster.DBSCAN.html
- Aggregate points into clusters bottom-up -> Agglomerative clustering

https://scikit-

October 2022

learn.org/stable/modules/generated/sklearn.cluster.AgglomerativeClustering.html