Lecture 18 Part D:
How Texture Mapping Works

The Texture Coordinate

UV Mapping with Barycentric Coodinates

The Texture Lookup

Given UV what is the color?

Where does the color go?

Pixel is a little square?

(no, but useful for thinking about it)

Assume UV is the center of the pixel

The problems

1. U,V might not be integers
2. Target Area of the pixel
3. Target Areas next to each other

The general problem...

The world/image in continuous

The pixel grid is discrete

This is a fundamental problem in graphics

We'll come back to it

Texture Lookups: Magnification

A pixel covers less than a pixel in the image

Note: this same reasoning works for "point sampling" (the center of an area)

Basic Solution: Nearest-Neighbor

Think of colors at grid corners (points) not filling squares

Standard Solution: Bi-Linear Interpolation

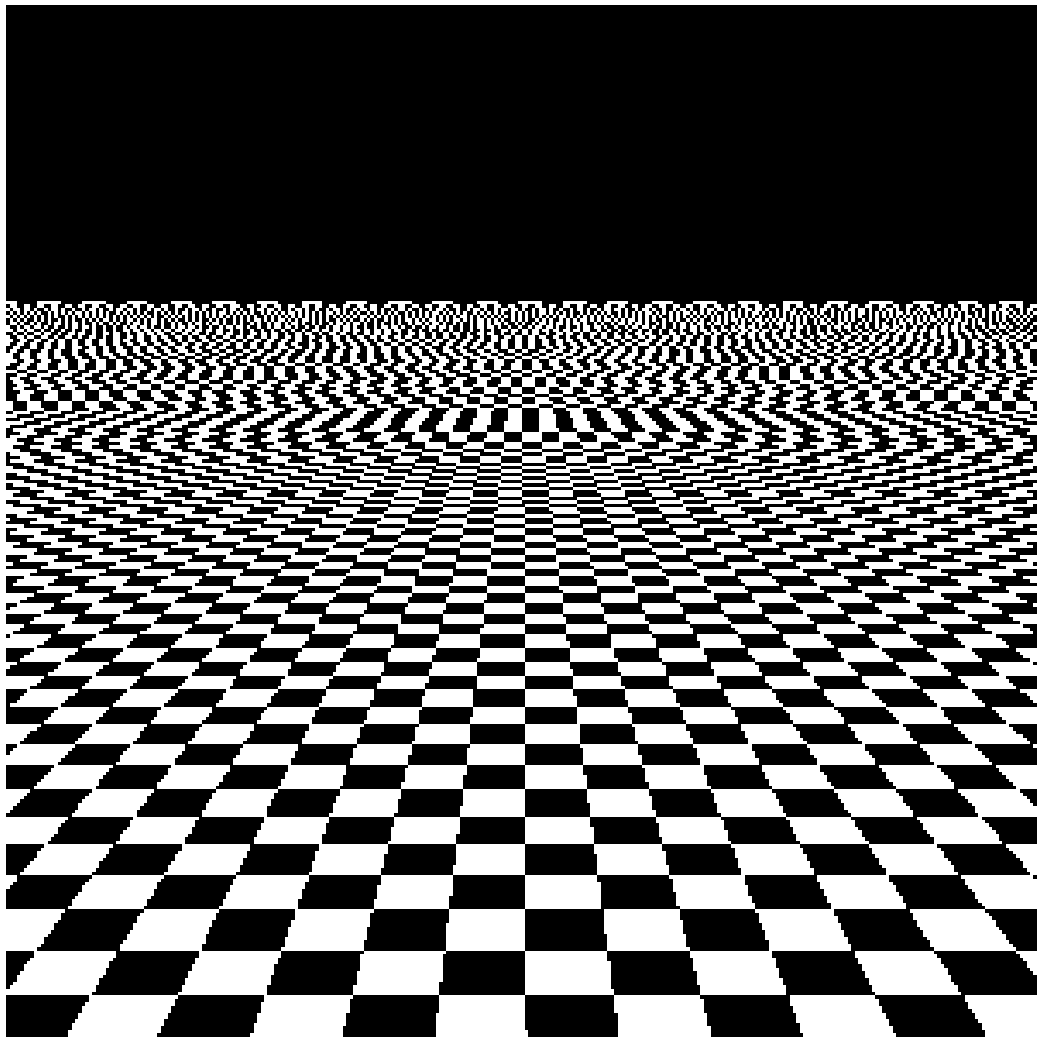
Treat the pixel as a point

Does not consider edges of pixels

Texture Lookups: Minification

One pixel covers an area of the texture

What if we just look up the color?

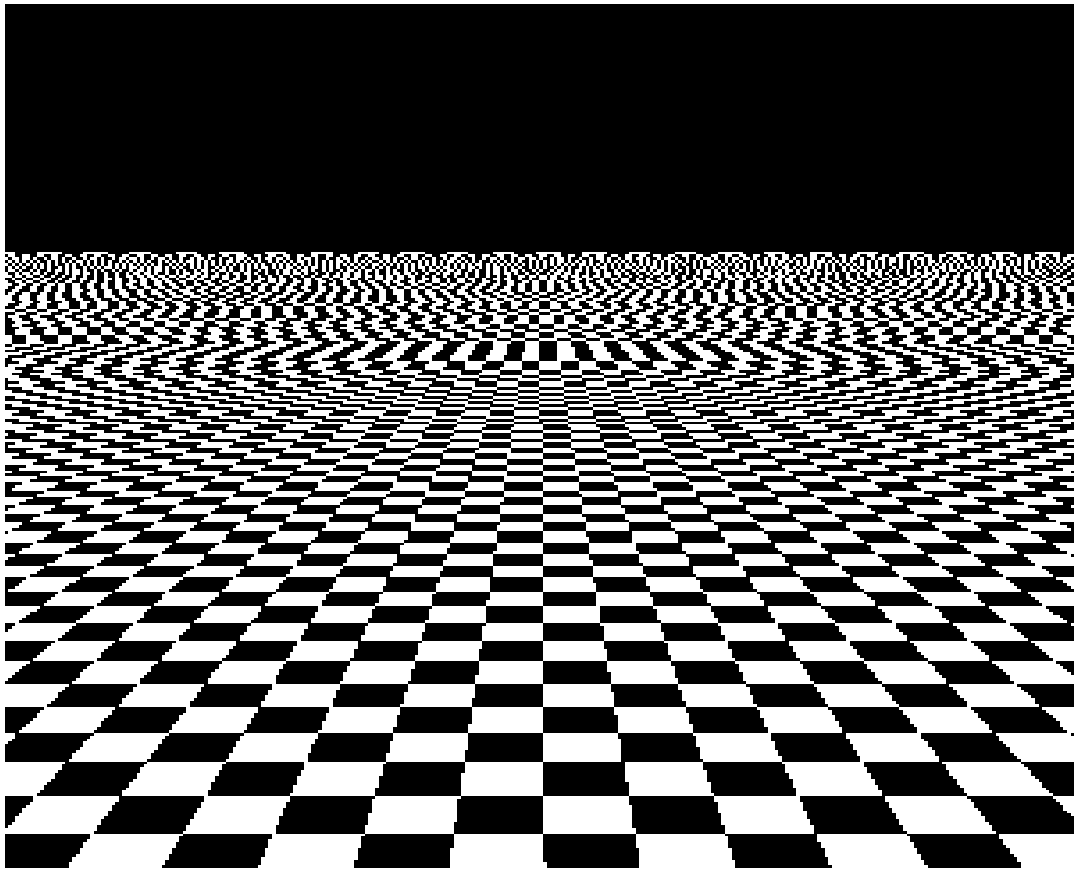


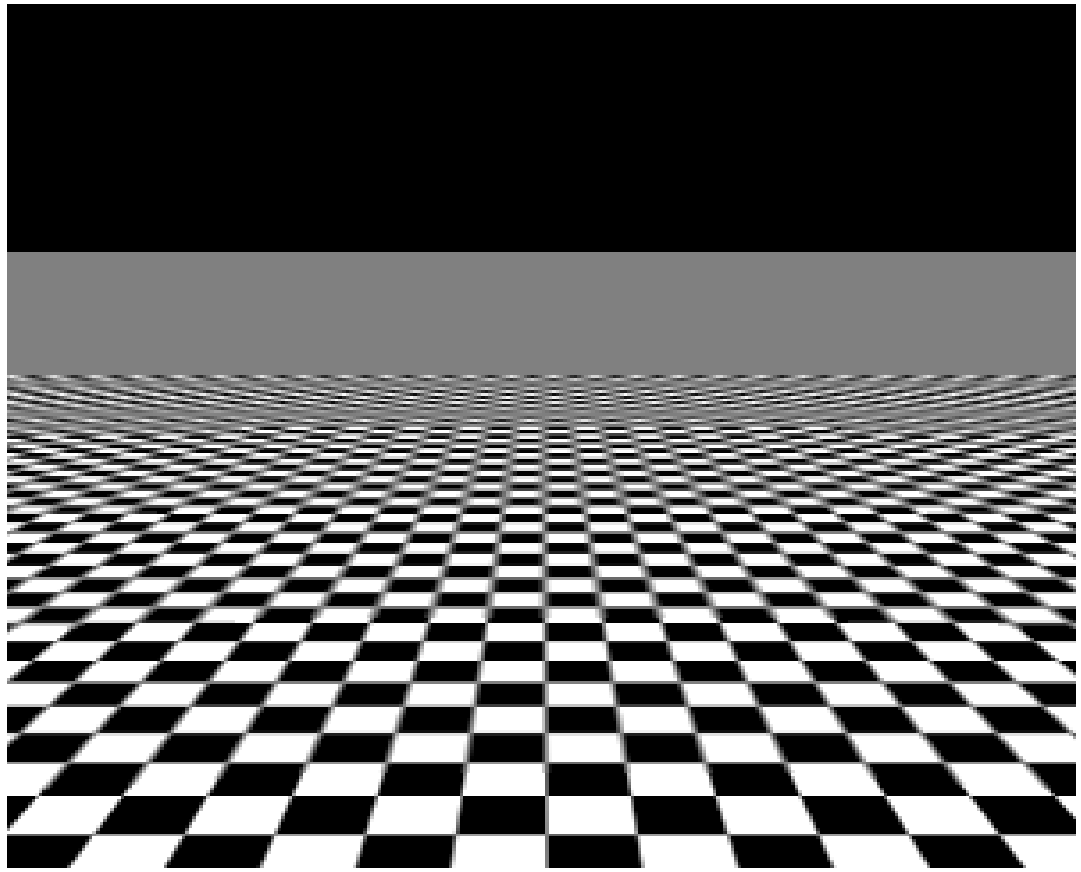
Filtering: The Basic Idea

We need to average together all the texture pixels (texels) the pixel covers

Lots of theory on how to do this correctly...

Simple Filtering





Filtering: The practical problem

We need to average together a lot of texels

What to average?

How to average it **fast**?

The Secrets of performance...

1. Pre-computation
2. Amortization
3. Approximation

We'll see all of these...

Solution 1: Summed Area Table

This is a historical solution - not really used in practice

1. Estimate Shape as a rectangle
2. Pre-compute Summed Area Table
3. Fast lookups (4 values)

Summed Area Table

Key Idea: Amortization and Pre-Computation

We save time per-pixel by pre-computing the summed area table

Solution 2: Mip-Maps

De-Facto Standard in Graphics

Modern hardware can do fancier stuff

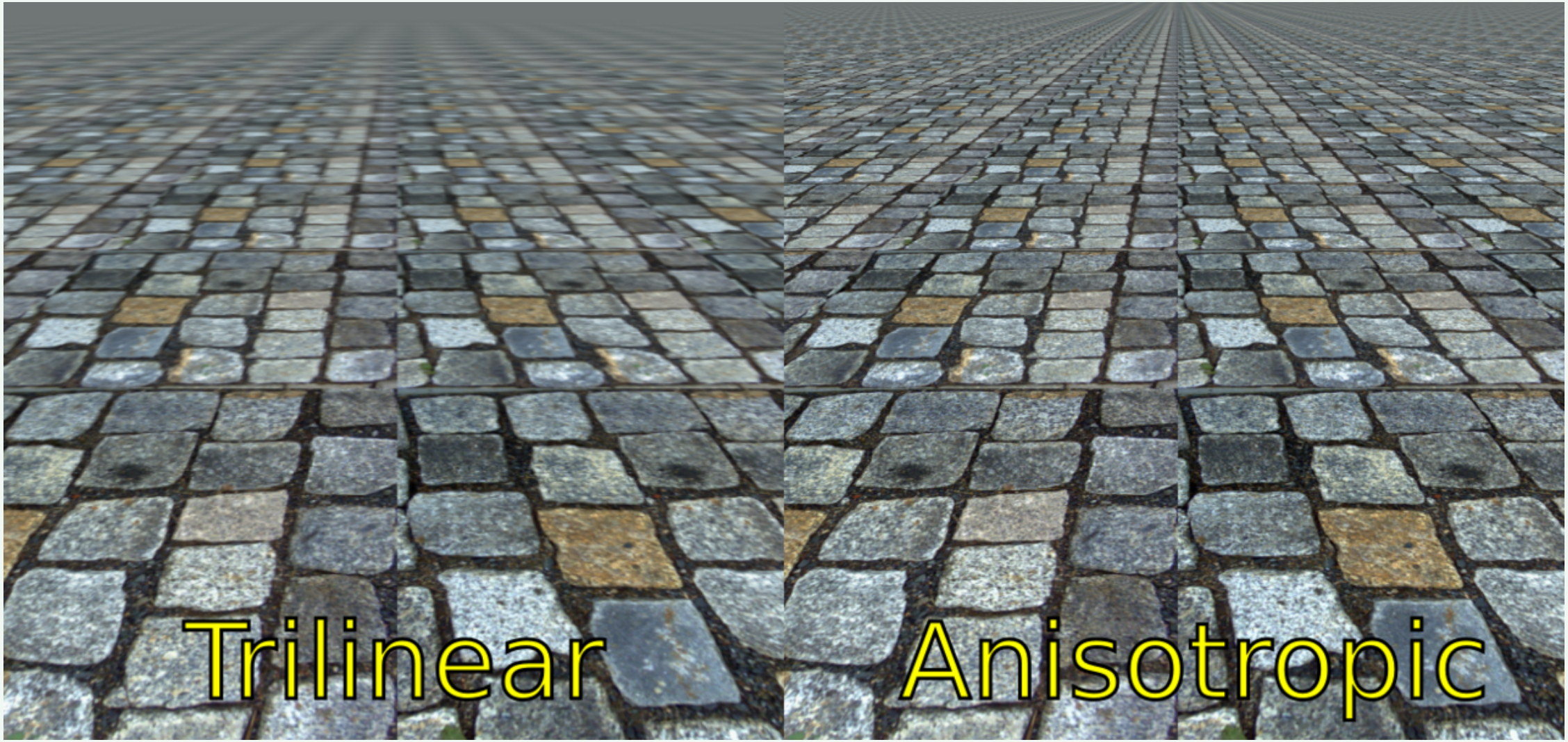
1. Approximate Filter as a Square
2. Pre-Compute Multiple Sizes of Map
3. Look up in correct sized maps

Mip Maps 1: Approximate as square

Mip Maps 1: Approximate as square

Problem: Anisotropy

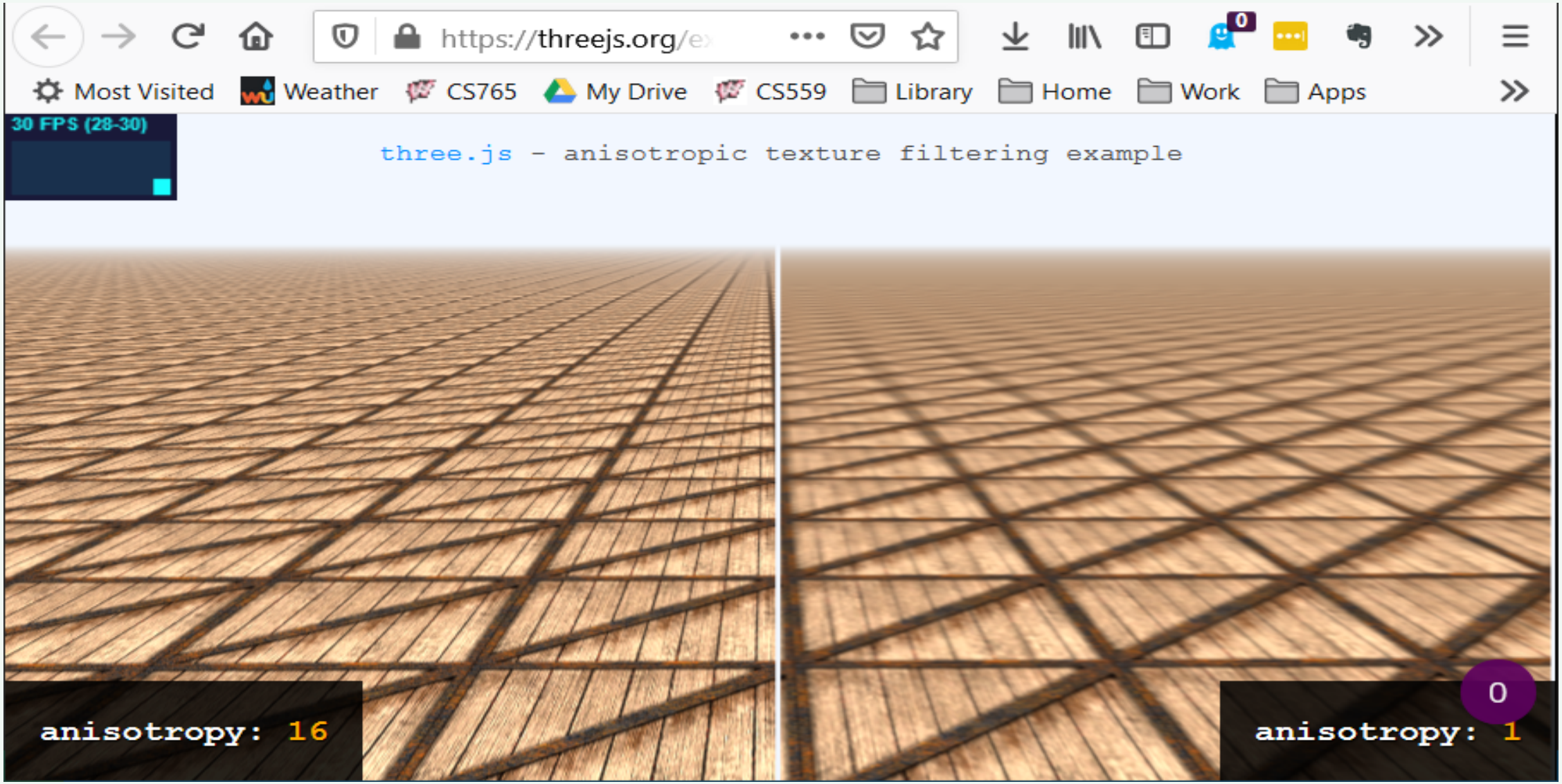
The areas are not square!


Trilinear
Anisotropic

Anisotropic Filtering

Hack version:

Use multiple squares (three supports this)


https://threejs.org/e
Most Visited
Weather
CS765
My Drive
CS559
Library
Home
Work
Apps
30 FPS (28-30)
three.js - anisotropic texture filtering example
anisotropy: 16
anisotropy: 1

Mip Maps 2: Lookup in smaller image

Mip Maps 3: Lookup in smallest image

Bi-Linear Interpolation

Mip Maps 4: Lookup in-between images

Tri-Linear Interpolation

requires 8 values (4 per layer)

Mip Maps 5: A Historic Storage Trick

Why is it called "MIP"?

We don't actually do this any more...

Mip Maps Summary

1. Pre-Compute MIP-Map (images of various sizes)
2. Aproximate area with square (center is easy, size is harder)
3. Figure out which image to sample from
4. Tri-Linear Interpolate between levels

In Practice...

#1 must be done at texture loading (THREE does it for us by default)

#2-#4 is done by hardware - per pixel

THREE Options

Minification

THREE.NearestFilter

THREE.NearestMipMapNearestFilter

THREE.NearestMipMapLinearFilter

THREE.LinearFilter

THREE.LinearMipMapNearestFilter

THREE.LinearMipMapLinearFilter

Magnification

THREE.NearestFilter

THREE.LinearFilter

Texture Mapping Summary

1. Define UVs for Triangles
2. Lookup values in an image
3. Use images for coloring materials

And inside...

1. Use Barycentric interpolation for UVs
2. Use image sampling to lookup values
3. Use MIP Maps to filter efficiently

Next time...

Facier uses of texture maps!