

Calculus

H0 Parate kennis

Goniometrische functies

$$A^2 - B^2 = (A + B)(A - B)$$

Exponentiële regels

$$a^x \cdot a^y = a^{x+y}$$

$$\frac{a^x}{a^y} = a^{x-y}$$

$$\left(\frac{a^y}{a^x}\right)^y = a^{xy}$$

$$\frac{1}{a^x} = a^{-x}$$

$$\sqrt[n]{a^x} = a^{\frac{x}{n}}$$

Logaritmische regels

$$y = \log_a x \Leftrightarrow x = a^y$$

$$\log_a x + \log_a y = \log_a xy$$

$$\log_a x - \log_a y = \log_a \frac{x}{y}$$

$$n \log_a x = \log_a x^n$$

$$\log_a x = \frac{\log_b x}{\log_b a}$$

H1 Getallenverzameling

Complexe getallen

$$i^2 = -1$$

Poolcoördinaten

$$r = \sqrt{(x^2 + y^2)}$$

$$\theta = \arctan\left(\frac{y}{x}\right)$$

$$z = r \operatorname{cis} \alpha = r(\cos \alpha + i \sin \alpha)$$

$$(r \operatorname{cis} \alpha)^n = r^n \operatorname{cis}(n\alpha)$$

$$z_k = \sqrt[n]{r} \operatorname{cis}\left(\frac{\alpha + 2k\pi}{n}\right)$$

H2 Limieten

Cyclometrische functies

$$y = \operatorname{Bgsin} x \Leftrightarrow x = \sin y$$

$$y = \operatorname{Bgcos} x \Leftrightarrow x = \cos y$$

$$y = \operatorname{Bgtan} x \Leftrightarrow x = \tan y$$

$$y = \operatorname{Bgcot} x \Leftrightarrow x = \cot y$$

Exponentiële functies

$$\lim_{x \rightarrow \infty} \left(1 + \frac{1}{x}\right)^x = e$$

$$\lim_{x \rightarrow \infty} \left(1 + \frac{k}{x}\right)^x = e^k$$

$$\lim_{x \rightarrow \infty} \left(1 + \frac{f(x)}{g(x)}\right)^{h(x)} = e^{\lim_{x \rightarrow \infty} \frac{f(x) \cdot h(x)}{g(x)}} \quad \text{where } \lim_{x \rightarrow a} g(x) = 0$$

Bijzondere goniometrische limieten

$$\lim_{x \rightarrow 0} \frac{\sin(x)}{x} = 1$$

$$\lim_{x \rightarrow 0} \frac{\tan(x)}{x} = 1$$

H3 Afgeleiden

Basics

$$D(x^n) = nx^{n-1} dx$$

$$D(f(x) + g(x)) = D(f(x)) + D(g(x))$$

$$D(\lambda f(x)) = \lambda D(f(x))$$

$$d(f \cdot g)(x) = f(x)g'(x) + f'(x)g(x)$$

$$d\left(\frac{f(x)}{g(x)}\right) = \frac{g(x)f'(x) - g'(x)f(x)}{(g(x))^2}$$

Goniometrische functies

$$D(\sin x) = \cos x$$

$$D(\cos x) = -\sin x$$

$$D(\tan x) = \frac{1}{\cos^2 x}$$

$$D(\cot x) = \frac{-1}{\sin^2 x}$$

$$D(\sec x) = \frac{\cos^2 x}{\sin^2 x}$$

$$D(\csc x) = \frac{-\cos x}{\sin^2 x}$$

Cyclometrische functies

$$D(\operatorname{Bgsin} x) = \frac{1}{\sqrt{1-x^2}}$$

$$D(\operatorname{Bgcos} x) = \frac{-1}{\sqrt{1-x^2}}$$

$$D(\operatorname{Bgtan} x) = \frac{1}{1+x^2}$$

$$D(\operatorname{Bgcot} x) = \frac{-1}{1+x^2}$$

Hyperbolische functies

$$D(\sinh x) = \cosh x$$

$$D(\cosh x) = \sinh x$$

$$D(\tanh x) = \frac{1}{\cosh^2 x}$$

$$D(\coth x) = \frac{-1}{\sinh^2 x}$$

Exponentiële functies

$$D(a^x) = a^x \ln a$$

$$D(e^x) = e^x$$

$$D(\ln x) = \frac{1}{x}$$

$$D(\log_a x) = \frac{1}{x \ln a}$$

Kettingregel

$$D(f(g(x))) = f'(g(x))g'(x)$$

Machtsregel

$$D(f(x)^{g(x)}) = g(x)f(x)^{g(x)-1}f'(x) + f(x)^{g(x)}g'(x) \ln f(x)$$

H4 Integralen

Basics

$$\int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\int f(x) + g(x) dx = \int f(x) dx + \int g(x) dx$$

$$\int \lambda f(x) dx = \lambda \int f(x) dx$$

$$\int f(x)g'(x) dx = f(x)g(x) - \int f'(x)g(x) dx$$

$$\int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

Goniometrische functies

$$\int \sin x dx = -\cos x + C$$

$$\int \cos x dx = \sin x + C$$

$$\int \frac{1}{\cos^2 x} dx = \tan x + C$$

$$\int \frac{-1}{\sin^2 x} dx = \cot x + C$$

Cyclometrische functies

$$\int \frac{1}{\sqrt{1-x^2}} dx = \operatorname{Bgsin} x + C$$

$$\int \frac{1}{\sqrt{a^2-x^2}} dx = \operatorname{Bgsin} \frac{x}{a} + C$$

$$\int \frac{1}{x^2+1} dx = \operatorname{Bgtan} x + C$$

$$\int \frac{1}{\sqrt{x^2+a}} dx = \ln |x + \sqrt{x^2+a}| + C$$

Hyperbolische functies

$$\int \cosh x dx = \sinh x + C$$

$$\int \sinh x dx = \cosh x + C$$

$$\int \frac{1}{\cosh^2 x} dx = \tanh x + C$$

$$\int \frac{1}{\sinh^2 x} dx = -\coth x + C$$

Exponentiële functies

$$\int a^x dx = \frac{a^x}{\ln a} + C$$

$$\int e^x dx = e^x + C$$

$$\int \frac{1}{x} dx = \ln |x| + C$$

H5 Bepaalde integralen

Oppervlakte

Cartesisch	$S = \int_a^b \ f(x)\ dx$
Parameter	$S = \int_a^b \ g(t)\ f'(t) dt$
Pool	$S = \int_\alpha^\beta (r(\theta))^2 d\theta$

Omwentelingsvolume

Cartesisch	$V = \pi \int_a^b (f(x))^2 dx$
Parameter	$V = \pi \int_a^b (g(t))^2 f'(t) dt$
Pool	

Booglengte

Cartesisch	$L = \int_a^b \sqrt{1 + (f'(x))^2} dx$
Parameter	$L = \int_a^b \sqrt{(f'(t))^2 + (g'(t))^2} dt$
Pool	$L = \int_\alpha^\beta \sqrt{(r(\theta))^2 + (r'(\theta))^2} d\theta$

Complanatie

Cartesisch	$C = 2\pi \int_a^b \ f(x)\ \sqrt{1 + (f'(x))^2} dx$
Parameter	$C = 2\pi \int_a^b \ g(t)\ \sqrt{(f'(t))^2 + (g'(t))^2} dt$
Pool	