

# Definition of the NPS function in python

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## Code function

This document presents a python implementation of the multivariate categorical sampling function mentioned in the “A Fast Nonparametric Sampling (NPS) Method for Time-to-Event in Individual-Level Simulation Models.” manuscript, and used in the R examples provided in the Appendix.

```
def nps_nhpp(a_probs, correction, a_categories=None):  
    """  
    Generate samples from different probability distributions using a  
    multivariate categorical distribution.  
  
    Parameters:  
    -----  
    a_probs (array): Array filled with independent and equally-length  
    probability distributions.  
    correction (str): String defining whether to a random variable between 0  
    and 1 to approximate continuous time ("uniform") or no modification at all  
    after performing the sample ("none").  
    a_categories (array): (Optional) Array defining the names of the  
    categories to sample.  
  
    Returns:  
    -----  
    numpy.array: Array filled with the sampled categories for all the
```

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probability distributions.

Example:

-----

```
import numpy as np
import scipy.stats as stats

# Number of repetitions
n_samp = 100

# define random numbers
a_unif_samp = np.random.uniform(size = n_rep*2)

# Create an array filled with categories
a_categories = np.arange(1, 101)

# Parameters of normal distribution
## First distribution
norm_mean_1, norm_var_1 = 30, 10
## second distribution
norm_mean_2, norm_var_2 = 60, 10

# Get PDF from distributions
v_disc_PDF_norm_1 = stats.norm.pdf(a_categories, loc = norm_mean_1,
    scale = norm_var_1)
v_disc_PDF_norm_2 = stats.norm.pdf(a_categories, loc = norm_mean_2,
    scale = norm_var_2)

# normalize values
## First version
v_norm_PDF_norm_1 = v_disc_PDF_norm_1/sum(v_disc_PDF_norm_1)
## Second version
v_norm_PDF_norm_2 = v_disc_PDF_norm_2/sum(v_disc_PDF_norm_2)

a_PDF_1_2 = np.array([v_norm_PDF_norm_1, v_norm_PDF_norm_2])

a_choice = np.random.choice(a = [0, 1], size = n_samp, replace = True,
    p = [0.5, 0.5])

a_probs = np.stack(arrays = a_PDF_1_2[a_choice], axis = 0)

nps_nhpp(a_probs= a_probs, correction="none")
```

```

-----
"""
valid_correction = {'none', 'uniform'}

if correction not in valid_correction:
    print("Warning: correction argument only accepts: 'none' and uniform")

    corresponding_values = None

if a_categories is None:
    # Get number of categories
    a_categories = np.arange(0, a_probs.shape[1])

# Check that all PDF's sum up to 1
if not all(np.isclose(a_probs.sum(axis = 1), 1)):
    a_probs = a_probs/a_probs.sum(axis=1, keepdims=True)

# Get number of elements to draw
a_samp_size = a_probs.shape[0]

# Obtain array filled with random numbers following a uniform distribution
a_unif_probs = np.vstack(np.random.uniform(size = a_samp_size))

# Get cumulative probabilities array from `a_probs`
# Every row is a CDF
a_cum_probs = np.cumsum(a_probs, axis = 1)

# Compare uniform probabilities against cumulative probs
comparison_result = a_cum_probs >= a_unif_probs

# Getting positions where values are greater than or equal
positions = np.argmax(comparison_result, axis = 1)

corresponding_values = a_categories[positions]

if correction == "uniform":
    corresponding_values = corresponding_values + a_unif_probs

return corresponding_values

```