## Example 1 using R

Time to event from parametric hazards

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## **Code function**

This document presents the code corresponding to the first example presented in the "A Fast Nonparametric Sampling (NPS) Method for Time-to-Event in Individual-Level Simulation Models." manuscript, all of them using R.

```
# 01 Initial Setup -----
# Clean global environment
remove(list = ls())
# Free unused R memory
gc()
```

```
# 02 Define general parameters -----
#' Number of samples to draw from the life table
n_samp_life_tables <- 1e5

#' Number of samples, by sex, to draw from the life table
n_samp_by_sex <- 1e5

# Sample size for every sampling iteration</pre>
```

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```
n_samples <- 1e4
# Number of times to repeat the sampling
n_sim_reps <- 1e3</pre>
# Number of repetitions in microbenchmark
n_reps_microbench <- 100</pre>
# Seed for reproducibility in random number generation
n_{seed} < 10242022
# 03 Define required functions ---
# Calculate expected value using NPS method
calc_ev_nps <- function(n_samples, v_probs){</pre>
  # Sample times to event
  v_time_to_event_rates_cat <- sample(size = n_samples,</pre>
                                              = 0:150,
                                       prob = v_probs,
                                       replace = TRUE)
 return(mean(v_time_to_event_rates_cat))
}
# Calculate expected value using NPS approach and continous time approximation
calc_ev_nps_corr <- function(n_samples, v_probs){</pre>
  # Sample times to event
  v_time_to_event_rates_cat <- sample(size = n_samples,</pre>
                                              = 0:150,
                                       prob = v_probs,
                                       replace = TRUE)
  # Generate a random number following a unifrom distribution
  v_unif <- runif(n_samples)</pre>
  # Add random number
  v_time_to_event_rates_cat_unif <- v_time_to_event_rates_cat + v_unif
  return(mean(v_time_to_event_rates_cat_unif))
```

```
calc_stats_nps_corr <- function(n_reps = 1000,</pre>
                                  n_samples = 10000, v_time_int = 0:150,
                                  v probs, alpha level = 0.05,
                                  true_ev, true_var){
  # Draw 'n reps' samples from the NPS TTT
  m_out <- replicate(n = n_reps,</pre>
                      expr = sample_ttt_nps(n_samples = n_samples,
                                              v_time_int = v_time_int,
                                              v_probs = v_probs))
  ## Calculate summary statistics
  v_ev_est <- colMeans(m_out)</pre>
  v_var_est <- matrixStats::colVars(m_out)</pre>
  v_se_ev_est <- sqrt(v_ev_est/n_samples)</pre>
  v_se_var_est <- sqrt(v_var_est/n_samples)</pre>
  # Expected values
  mean_ev_est <- mean(v_ev_est)</pre>
  mean_var_est <- mean(v_var_est)</pre>
  # Bias
  bias_ev_est <- abs(mean(v_ev_est) - true_ev)</pre>
  bias_var_est <- abs(mean(v_var_est) - true_var)</pre>
  # Monte Carlo Standard Error (MCSE) of Bias
  mcse_bias_ev_est <- sqrt(</pre>
    (sum((v_ev_est - true_ev)^2)/(n_reps - 1))/n_reps)
  mcse_bias_var_est <- sqrt(</pre>
    (sum((v_var_est - true_var)^2)/(n_reps - 1))/n_reps)
  # Mean Square Error (MSE)
  mse_ev_est <- sum((v_ev_est - true_ev)^2)/n_reps</pre>
  mse_var_est <- sum((v_var_est - true_var)^2)/n_reps</pre>
  # Confidence interval of bias
  z\_score \leftarrow qnorm(p = 1 - alpha\_level/2)
  ci_bias_ev_est <- c(LB = bias_ev_est - z_score*mcse_bias_ev_est,</pre>
                       UB = bias_ev_est + z_score*mcse_bias_ev_est)
  ci_bias_var_est <- c(LB = bias_var_est - z_score*mcse_bias_var_est,</pre>
                        UB = bias_var_est + z_score*mcse_bias_var_est)
```

```
# Confidence intervals pf estimates
 chi_score_lb <- qchisq(p = alpha_level/2, df = (n_samples - 1))</pre>
  chi_score_ub <- qchisq(p = 1 - alpha_level/2, df = (n_samples - 1))</pre>
 m ci ev est <- cbind(LB = v ev est - z score*v se ev est,
                       UB = v_ev_est + z_score*v_se_ev_est)
 # DescTools::MeanCI(v time to event rates cat unif, conf.level = 0.95)
  # confint(lm(v_time_to_event_rates_cat_unif ~ 1))
 m_ci_var_est <- cbind(LB = ((n_samples - 1)*v_var_est)/chi_score_ub,</pre>
                         UB = ((n_samples - 1)*v_var_est)/chi_score_lb)
 # DescTools::VarCI(v_time_to_event_rates_cat_unif, conf.level = 0.95)
 # Coverage
  coverage_ev_est <- mean(true_ev >= m_ci_ev_est[, 1] &
                              true_ev <= m_ci_ev_est[, 2])
  coverage_var_est <- mean(true_var >= m_ci_var_est[, 1] &
                              true_var <= m_ci_var_est[, 2])</pre>
 # Output
 return(c(mean_ev_est = mean_ev_est,
           mean var est = mean var est,
           bias_ev_est = bias_ev_est,
           bias_var_est = bias_var_est,
           coverage_ev_est = coverage_ev_est,
           coverage_var_est = coverage_var_est
 ))
sample_ttt_nps <- function(n_samples,</pre>
                            v_{time_int} = 0:150,
                            v_probs){
 v_time_to_event_rates_cat <- sample(size = n_samples, x = v_time_int,</pre>
                                       prob = v_probs,
                                       replace = T)
 v_unif <- runif(n_samples)</pre>
 v_time_to_event_rates_cat_unif <- v_time_to_event_rates_cat + v_unif</pre>
 return(v_time_to_event_rates_cat_unif)
# 04 Calculate expected values from distributions --
## Exponential distribution ----
```

```
# Define distribution parameters
par_exp_rate
              <- 0.1
# Analytical values
                 <- 1/par_exp_rate # Analytical expected value
ev_exp
                 <- ev exp^2
                                # Analytical variance
var_exp
# Get instantaneous probability of occurrence
v_prob_exp_rates <- pexp(q = 1:151, rate = par_exp_rate) -</pre>
  pexp(q = 0:150, rate = par_exp_rate)
# Simulations using the nps method multiple times
ev_exp_uncorr <- mean(</pre>
  replicate(n_sim_reps,
            expr = calc_ev_nps(n_samples = n_samples,
                               v_probs = v_prob_exp_rates)))
# Simulations using the nps method, adding continuous time approximation
ev_exp_corr <- mean(</pre>
  replicate(n_sim_reps,
            expr = calc_ev_nps_corr(n_samples = n_samples,
                                    v_probs = v_prob_exp_rates)))
# Round values
ev exp corr <- round(ev exp corr, 2)
ev_exp_uncorr <- round(ev_exp_uncorr, 2)</pre>
# Measure mean execution time
## Without continuous time correction
l_mbench_exp_uncorr <- microbenchmark::microbenchmark(</pre>
  calc_ev_nps(n_samples = n_samples, v_probs = v_prob_exp_rates),
 times = n_reps_microbench,
  unit = "ms")
#* The default output of microbenchmark is in nanoseconds (1/1e-9).
#* The results are converted into miliseconds
t_m_exp_u <- format(round(mean(l_mbench_exp_uncorr$time/1e6), 2),</pre>
                      nsmall = 2)
t_CI_exp_u <- format(round(quantile(x = l_mbench_exp_uncorr$time/1e6,
                                     probs = c(0.025, 0.975)), 2),
                      nsmall = 2
```

```
## With continuous time correction
l_mbench_exp_corr <- microbenchmark::microbenchmark(</pre>
  calc_ev_nps_corr(n_samples = n_samples, v_probs = v_prob_exp_rates),
  times = n_reps_microbench,
  unit = "ms")
#* The default output of microbenchmark is in nanoseconds (1/1e-9).
#* The results are converted into miliseconds
t_m_exp_c <- format(round(mean(l_mbench_exp_corr$time/1e6), 2),</pre>
                     nsmall = 2
t_CI_exp_c <- format(round(quantile(l_mbench_exp_corr$time/1e6,
                                     probs = c(0.025, 0.975)), 2),
                     nsmall = 2
# Using general function
v_sim_nps_out_exp <- calc_stats_nps_corr(n_reps = n_sim_reps,</pre>
                                          n_samples = n_samples,
                                          v_{time_int} = 0:150,
                                          v_probs = v_prob_exp_rates,
                                          alpha_level = 0.05,
                                          true_ev = ev_exp,
                                          true_var = var_exp)
## Gamma distribution ----
# Define distribution parameters
par_gamma_shape <- 4</pre>
par_gamma_rate <- 0.1</pre>
# Analytical values
ev_gamma <- par_gamma_shape/par_gamma_rate  # Analytical expected value
var_gamma <- par_gamma_shape/(par_gamma_rate^2) # Analytical variance</pre>
# Get instantaneous probability of ocurrence
v_prob_gamma_rates <-</pre>
  pgamma(q = 1:151, shape = par_gamma_shape, rate = par_gamma_rate) -
  pgamma(q = 0:150, shape = par_gamma_shape, rate = par_gamma_rate)
# Simulations using the nps method multiple times
ev_gamma_uncorr <- mean(</pre>
```

```
replicate(n_sim_reps,
            expr = calc_ev_nps(n_samples = n_samples,
                               v_probs = v_prob_gamma_rates)))
# Simulations using the nps method, adding continuous time approximation
ev_gamma_corr <- mean(
  replicate(n_sim_reps,
            expr = calc_ev_nps_corr(n_samples = n_samples,
                                     v_probs = v_prob_gamma_rates)))
# Round values
ev_gamma_corr <- round(ev_gamma_corr, 2)</pre>
ev_gamma_uncorr <- round(ev_gamma_uncorr, 2)</pre>
# Measure mean execution time
## Without continuous time correction
l_mbench_gamma_uncorr <- microbenchmark::microbenchmark(</pre>
  calc_ev_nps(n_samples = n_samples, v_probs = v_prob_gamma_rates),
  times = n_reps_microbench,
  unit = "ms")
#* The default output of microbenchmark is in nanoseconds (1/1e-9).
#* The results are converted into miliseconds
t_m_gamma_u <- format(round(mean(l_mbench_gamma_uncorr$time/1e6), 2),
                       nsmall = 2
t CI gamma u <- format(round(quantile(1 mbench gamma uncorr$time/1e6,
                                      probs = c(0.025, 0.975)), 2),
                       nsmall = 2)
## With continuous time correction
l_mbench_gamma_corr <- microbenchmark::microbenchmark(</pre>
  calc_ev_nps_corr(n_samples = n_samples, v_probs = v_prob_gamma_rates),
  times = n_reps_microbench,
  unit = "ms")
#* The default output of microbenchmark is in nanoseconds (1/1e-9).
#* The results are converted into miliseconds
t_m_gamma_c <- format(round(mean(l_mbench_gamma_corr$time/1e6), 2),</pre>
                       nsmall = 2
t_CI_gamma_c <- format(round(quantile(1 mbench gamma_corr$time/1e6,
```

```
probs = c(0.025, 0.975)), 2),
                        nsmall = 2)
# Using general function
v_sim_nps_out_gamma <- calc_stats_nps_corr(n_reps = n_sim_reps,</pre>
                                             n_samples = n_samples,
                                             v_{time_int} = 0:150,
                                             v_probs = v_prob_gamma_rates,
                                             alpha_level = 0.05,
                                             true_ev = ev_gamma,
                                             true_var = var_gamma)
## Log-normal distribution ----
# Define distribution parameters
par_lnorm_meanlog <- 3.5</pre>
par_lnorm_sdlog <- 0.15</pre>
# Analytical values
## Analytical expected value
ev_lnorm <- exp(par_lnorm_meanlog + ((par_lnorm_sdlog^2)/2))</pre>
## Analytical variance
var_lnorm <- exp(2*par_lnorm_meanlog + (par_lnorm_sdlog^2))*(</pre>
  exp(par_lnorm_sdlog^2) - 1)
# Round values
ev_lnorm <- round(ev_lnorm, 2)</pre>
# Get instantaneous probability of ocurrence
v_prob_lnorm_rates <-</pre>
  plnorm(q = 1:151, meanlog = par_lnorm_meanlog, sdlog = par_lnorm_sdlog) -
  plnorm(q = 0:150, meanlog = par_lnorm_meanlog, sdlog = par_lnorm_sdlog)
# Simulations using the nps method multiple times
ev_lnorm_uncorr <- mean(</pre>
  replicate(n_sim_reps,
            expr = calc_ev_nps(n_samples = n_samples,
                                v_probs = v_prob_lnorm_rates)))
# Simulations using the nps method, adding continuous time approximation
```

```
ev_lnorm_corr <- mean(</pre>
  replicate(n_sim_reps,
            expr = calc_ev_nps_corr(n_samples = n_samples,
                                     v_probs = v_prob_lnorm_rates)))
# Round values
ev_lnorm_corr <- round(ev_lnorm_corr, 2)</pre>
ev_lnorm_uncorr <- round(ev_lnorm_uncorr, 2)</pre>
# Measure mean execution time
## Without continuous time correction
l_mbench_lnorm_uncorr <- microbenchmark::microbenchmark(</pre>
  calc_ev_nps(n_samples = n_samples, v_probs = v_prob_lnorm_rates),
 times = n_reps_microbench,
 unit = "ms")
#* The default output of microbenchmark is in nanoseconds (1/1e-9).
#* The results are converted into miliseconds
t_m_lnorm_u <- format(round(mean(l_mbench_lnorm_uncorr$time/1e6), 2),</pre>
                       nsmall = 2
t_CI_lnorm_u <- format(round(quantile(l_mbench_lnorm_uncorr$time/1e6,
                                       probs = c(0.025, 0.975)), 2),
                       nsmall = 2
## With continuous time correction
l_mbench_lnorm_corr <- microbenchmark::microbenchmark(</pre>
  calc_ev_nps_corr(n_samples = n_samples, v_probs = v_prob_lnorm_rates),
 times = n_reps_microbench,
 unit = "ms")
#* The default output of microbenchmark is in nanoseconds (1/1e-9).
#* The results are converted into miliseconds
t_m_lnorm_c <- format(round(mean(l_mbench_lnorm_corr$time/1e6), 2),</pre>
                       nsmall = 2)
t_CI_lnorm_c <- format(round(quantile(l_mbench_lnorm_corr$time/1e6,
                                      probs = c(0.025, 0.975)), 2),
                       nsmall = 2)
### Using general function
```