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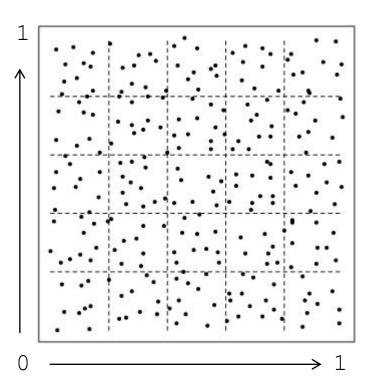




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For the purpose of setting-up an example, let's suppose that

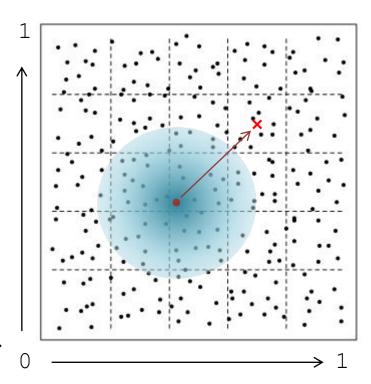
1) we have a distribution of random data points on a 2D plane which we subdivide in sub-regions using a grid.



For the purpose of setting-up an example, let's suppose that

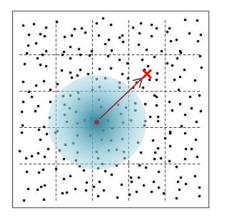
- 1) we have a distribution of random data points on a 2D plane which we subdivide in sub-regions using a grid.
- 2) for each point *p*, we want to select all the grid cells whose center is closer to *p* than a given radius *r*, and to perform some operations accordingly to our search result.

L> CLUSTE PINO



We may consider to use a nested loop like this one \rightarrow

Is there anything you would change?



```
for(p = 0; p < Np; p++)
    for(i = 0; i < Ng; i++)
      for(j = 0; j < Nq; j++)
        for(k = 0; k < Nq; k++)
            dist = sqrt(
                    pow(x[p] - (double)i/Ng - half size, 2) +
                    pow(y[p] - (double)j/Ng - half size, 2) +
                    pow(z[p] - (double)k/Ng - half size, 2));
                  if(dist < R)
                     do something;
```







Some function calls are particularly expensive. Those include, among others. sart(). ...

Try to avoid them if possible.

```
for(p = 0; p < Np; p++)
    for(i = 0; i < Ng; i++)
      for(i = 0; i < Nq; i++)
        for(k = 0; k < Ng; k++)
            dist2 = pow(x[p] - (double)i/Ng - half_size, 2) +
                    pow(y[p] - (double)j/Ng - half size, 2) +
                    pow(z[p] - (double)k/Ng - half size, 2));
                  if(dist2 < R2) HERF THE SORT
                     do something:
```







Some function calls are particularly expensive. Those include, among others, sqrt(), pow(), ...

Try to avoid them if possible.

```
for(p = 0; p < Np; p++)
    for(i = 0; i < Ng; i++)
      for(i = 0; i < Nq; i++)
        for(k = 0; k < Nq; k++)
            dx = x[p] - (double)i/Ng - half_size;
            dy = y[p] - (double)j/Ng - half size;
            dz = z[p] - (double)k/Ng - half size;
                                         -7 MOVE THE POWER
            dist2 = dx*dx + dy*dy + dz*dz; HERE
            if(dist2 < R2)
               do something;
```







Some function calls are particularly expensive. Those include, among others, sqrt(), pow(), floating point division... Try to avoid them if possible.

```
for(p = 0; p < Np; p++)
    for(i = 0; i < Ng; i++)
      for(i = 0; i < Nq; i++)
        for(k = 0; k < Ng; k++)
            dx = x[p] - (double)i * Ng inv - half size;
            dy = y[p] - (double)j * Ng inv - half size;
            dz = z[p] - (double)k * Ng inv - half size;
            dist2 = dx*dx + dy*dy + dz*dz;
            if(dist2 < R2)
               do something with sqrt(dist2);
```







(double)<i,j,k> * Ng inv + half size

was performed N³+N²+N times, always returning the same values.

Hoisting would save

 $N(N^2+N^1+1)$ mul, add and mem accesses.

You can do better pre-computing the relevant values:

```
double ijk[Ng];
for(i = 0; i < Ng; i++)
   ijk[i] = i * Ng inv + half size
```

```
for(p = 0; p < Np; p++)
    for(i = 0; i < Ng; i++)
     for(i = 0; i < Nq; i++)
        for(k = 0; k < Nq; k++)
            dx = x[p] - (double)i * Ng inv - half size;
            dy = y[p] - (double)j * Ng_inv - half_size;
            dz = z[p] - (double)k * Ng_inv - half_size;
            dist2 = dx*dx + dy*dy + dz*dz;
            if(dist2 < R2)
               do something with sqrt(dist2);
```



(2) *Hoisting* of expressions



```
(double)<i,j,k> * Ng_inv + half_size
```

was performed N³+N²+N times, always returning the same values.

Hoisting would save $N(N^2+N^1+1)$ mul, add and mem accesses.

```
for(i = 0; i < Ng; i++) {
  dx2 = x[p] - (double)i * Ng inv - half size;
   dx2 = dx2*dx2;
      for(j = 0; j < Ng; j++) {
         dv2 = v[p] - (double)j * Ng inv - half size;
         dy2 = dy2*dy2;
         dist2 xv = dx2 + dv2;
         for(k = 0; k < Nq; k++) {
            dz = z[p] - (double)k * Ng inv - half size;
            dist2 = dist2 xy + dz*dz;
            if(dist2 < Rmax2)
               do something with sqrt(dist2); } } }
```





(2) *Hoisting* of expressions



You could do even better by precomputing the relevant values:

```
double ijk[Ng];
for(i = 0; i < Ng; i++)
   ijk[i] = i * Ng inv + half size
```

```
for(i = 0; i < Ng; i++) {
   dx2 = x[p] - Ng inv[i] - half size;
   dx2 = dx2*dx2:
      for(j = 0; j < Ng; j++) {
         dy2 = y[p] - Ng_inv[j] - half_size;
         dist2 xy = dx2 + dy2*dy2;
         for(k = 0; k < Nq; k++) {
            dz = z[p] - Ng_inv[k] - half_size;
            dist2 = dist2 xy + dz*dz;
            if(dist2 < Rmax2)</pre>
               do something with sqrt(dist2); } } }
```





(3) Clarify the variables' scope



All these variables are very local, there's no need for them to have a wider scope.

That will help you in writing the code, and may help the compiler in optimizing the stack and perhaps the registers usage.

```
for(int i = 0; i < Ng; i++) {
   double dx2 = x[p] - (double)i * Ng_inv - half_size;
 \int dx2 = dx2:
      for(j = 0; j < Ng; j++) {
      >> double dy2 = y[p] - (double)j * Ng inv - half size;
      \rightarrow double dist2 xy = dx2 + dy2*dy2;
         for(k = 0; k < Ng; k++) {
            double dz = z[p] - (double)k * Ng inv - half size;
            double dist2 = dist2 xy + dz*dz;
            if(dist2 < Rmax2)</pre>
               do something with sqrt(dist2); } } }
```



(4) Suggest what is important



These variables are often calculated and reused subsequently.

Keeping a register dedicated to them may be useful.

Note: this is a suggestion, the compiler, after analyzing the code, may decide differently

```
double register Ng inv = 1.0 / Ng;
for(int i = 0; i < Ng; i++) {
   double dx2 = x[p] - (double)i * Ng inv - half size;
   dx2 *= dx2;
      for(j = 0; j < Ng; j++) {
         double dy2 = y[p] - (double)j * Ng inv - half size;
         dy2 *= dy2;
         double register dist2 xy = dx2 + dy2;
         for(k = 0; k < Nq; k++) {
            double register dz = z[p] - (double)k * Ng_inv - ...;
            double register dist2 = dist2 xy + dz*dz;
            if(dist2 < Rmax2)</pre>
               do something with sqrt(dist2); } } }
```

Note: the importance of being earnest

Paying attention to the scope of the variables and keeping local what is local has a twofold importance.

One hand:

all your local variables will reside in the stack.

However also the stack, which can be wide, is better to be clearly organized: where each "variable" should be put? Where is the best location for it to be "hot" at the right moment at the right place? Should it stay "together" (i.e. close in memory and hence probably close in cache) with other local variables that will be used at the same time?

for instance, in the previous example: i,j,k,dx2,dy2,dz,dist2 xy,Rmax2 are all used packed together. What if they were all defined at the begin of a long procedure and used for different purposes all around? What would have been the most optimal place to stack all them? (help the poor compiler in taking the best decision..)

Note: the compiler cares for it all?

Paying attention to the scope of the variables and keeping local what is local has a twofold importance.

One the other hand:

Keep your mind clear and sharp. Think carefully to what you need and where, and make it clear.

That will help you a lot in the next future when you'll have to maintain/debug - or just understand - your code.

That will help you in *not* inserting dependence chains by mistake (for instance, with a variable with a general label "temp" used all around may carry some garbage when it was not intended to).

Being a good programmer is all about thinking clearly and sharply.

Note: the importance of being earnest

Your compiler is able to take care of most of the aspect we have seen above (but for one, obvisouly: the usage of expensive functions calls, like pow and sqrt).

We'll see that better when talking about loops and branches.

However, that is not a good reason not to write a decent code from the beginning.





Do not suppose that your compiler is *always* able to re-arrange calculations – like avoiding expensive calls or using mathematically-equivalent more convenient expressions – all the time. It may be able to do that for **integer** calculations but it will not do it for **floating-point** calculations.

The reason is simple, and it is related to the fact that on a digital system the math is *not* always as it is on the blackboard.

> Integer math (+ and ×) in 2's complement is commutative and associative.

Floating point math $(+ \text{ and } \times)$ is commutative between 2 operands is never associative.



In fact, if you study, as you should, the "what every computer scientist should know about floating-point" paper (find it in the sco/materials/ folder on github), you discover that if **a**, **b**, and **c** are FP numbers,

$$(a + b) + c \neq a + (b + c)$$

due to the very nature of floating-point representation in a digital system (with a finite number of digits).

The issue is related to the limited number of digits available to represent the number which, in turn, limits the precision.



Let's suppose that we have 3 digits of precision for the mantissa. For the sake of simplicity, we consider a base 10 (so every single digit ranges in [0..9]).

Then the following hold:

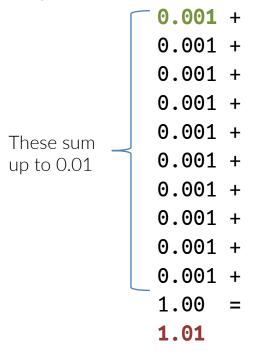
$$1.00 + 0.01 = 1.01$$

$$1.00 + 0.001 = 1.00$$

The last is true because, although we can represent 0.001 (it is 1.00 with a -3 exponent) the summation of 1.00 and 0.001 is beyond our precision: 1.001 would require 4 digits. As a consequence, we are not able to distinguish it from 1.00.



Then again:



```
1.00 +
0.001 +
0.001 +
0.001 +
0.001 +
0.001 +
0.001 +
0.001 +
0.001 +
0.001 +
0.001 =
1.00
```

Fach of

these ops

results in

1.00

So, the compiler is **NOT** free to reshuffle the order of floating-point operations,

..even if a mathematicallyequivalent formulation, different than the one you coded, would be more performant.

see the materials in the github folder ./AOB/kahan summation

Associative math



Every compiler allows the users to relax the rules for IEEE FP arithmetics.

Many of these rules ensure the correct treatment of under-normal numbers, 0+ and 0-, Inf and NaN. As such, relaxing the checks and the branches that deal with those cases, may incur in some un-correct result.

Explore two resources to have a better comprehension of this

https://simonbyrne.github.io/notes/fastmath/

https://kristerw.github.io/2021/10/19/fast-math/

Appreciate that also explicit tests as **isinf(x)** or **isnan(x)** will be disabled. As such, to be confident in deactivating those switches, you must be sure that your code is not incurring in those cases. However, by definition, the tests performed without those flags are not definitive because once the operations are re-shuffled, which is due exactly to those flags, the results may be different.





Do you expect any great performance from this code?

If not, why?

```
char * find char in string( char *string, char c )
                            int i = 0;
                            while ( i < strlen(string) )</pre>
                                               if(string[i] == c)

SEARCHIN FOR C
                                               else JUST USE WORCT CASE, C IS IN LAST ELEMENT
                                                                                                                                                                                                                                HOVE IF TO LAST POSITION
                           if( i < strlen(string) ) TO USELESS CONTROL

SOLUTE STRING STRING IN THE INTERIOR I
                                                 return &string[i];
                                                                                                                                                                                                                                            THE CYCLE
                             else
                                                                                                                                                                                                                                            WHEN YOU EXIT THE
                                                                                                                                                                                                                                            CYCLE RETURN IVUIL
                                                 return NULL;
```





There are several details that dump the performance, i.e. the CPE, of this loop.

The one I want to draw your attention to is the repeated call to the strlen() function.

Do you expect the string to change while you are scanning it? I guess no, but the compiler does not know it and has no way to understand that by code analysis. Moreover, the memory pointed by string could be modified somewhere else between two iterations.

```
char * find char in string( char *string, char c )
    int i = 0; _ _ _ _ _
    while ( i <istrlen(string) )
       if(string[i] == c)
         break;
       else
         i++:
    if( i < strlen(string) )</pre>
       return &string[i];
    else
       return NULL;
```





This very simple change will save you a lot of CPE

```
char * find char in string( char *string, char c )
    int i = 0;
    int len = strlen(string);
    while ( i < len )
       if( string[i] == c )
         break;
       else
         i++;
    if( i < strlen(string) )</pre>
       return &string[i];
    else
       return NULL;
```





For a number of reasons. this version is even more efficient than the previous one.

Can you tell why?

```
char * find char in string( char *string, char c )
   char *pos = string; > USE POWTER TO GO THROUGH
   while( ( *pos != '\0' ) && ( *pos != c ) )
                       LIEND CHARACTER OF STRINGS
       pos++;
    return ( *pos == '\0' ? NULL : pos );
```



(6) Avoid unnecessary memory references



This simple loop for a reduction of an array accumulates the partial results de-referencing the pointer sum at each iteration.

```
void reduce vector( int n, double *array, double *sum )
    for ( int i = 0; i < n; i++ )
         *sum += array[i];
rn;
/// CAN USG POINTER
/// INSTEAD
    return;
```



(6) Avoid unnecessary memory references



This simple loop for a reduction of an array accumulates the partial results de-referencing the pointer sum multiple times.

(asm obtained with -O1)

```
void reduce_vector( int n, double *array, double
*sum )
    for ( int i = 0; i < n; i++ )
          *sum += array[i];
    return:
```

```
.L3:
 movsd xmm0, QWORD PTR [rdx]
 addsd xmm0, QWORD PTR [rax]
 movsd QWORD PTR [rdx], xmm0
 add
        rax, 8
        гах, гсх
 CMD
 ine
        .L3
```

```
movsd xmm0, value of *sum
addsd xmm0, value of *array
movsd address of sum, xmm0
add
      rax, 8
                    ( array++ )
      rax, n
CMD
```



(6) Avoid unnecessary memory references



Introducing a separated, local accumulator will save memory accesses

(asm obtained with -O1)

```
void reduce vector( int n, double *array, double *sum )
                             WHY IS THIS FASTER?
   double temp = 0;
   for (int i = 0; i < n; i++) BECAUSE, TEMP IS LOCALLY
     temp += array[i];
                                AND CAN BE SUMED MUCH
   *sum = temp;
                                EASYER/INSTEAD OF A
   return;
                                POINTEN VALUE
```

```
.L11:
 addsd xmm0, QWORD PTR [rax]
 add
        rax, 8
        rax, rdx
 CMD
 ine
        .L11
```

```
addsd
       xmm0, value of *array
add
       rax, 8 (array++)
       rax, rdx (array with end-of-array)
CMD
```