1 Surroundings

1.1 setup

```
1 | 測機 (test on C++ and Python)
2 AC: 好好寫
3 | WA: cout << "0\n" / 結尾多印一行;
4 RE:空間越界/除0
5 TLE : while(true);
6 CE : empty code
7 OLE: 瘋狂Hello World
8 NO Output : default code
9 | 待測:stack深度、iudge速度、陣列MAX
11 1. bash.rc‡Tac
12 2. 調gedit設定
13 3. 打default_code
14 4. 測試ac
```

1.2 bashrc

```
1 oj() {
   ext=${1##*.}
                         #空格敏感
   filename=${1##*/}
                         #空格敏感
   filename=${filename%.*} #空格敏感
   case $ext in
     cpp ) g++ -o "/tmp/$filename" "$1" && "/tmp/$filename" ;;
          #空格不敏感
     py ) python3 "$1" ;;
                                          #空格不敏感
   esac
```

1.3 vimrc

```
1 set tabston=4
2 set shiftwidth=4
3 set softtabstop=4
4 set expandtab
5 set autoindent
6 set number
```

Data Structure

2.1 Sparse Table

```
1 // https://judge.yosupo.jp/problem/staticrmq 214 ms
3 template<typename T, int RANGE>
4 struct Sparse Table {
```

單點修改、區間查詢線段樹 struct Node {

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```
T val;
      Node(): val(INF) {}
      Node operator +(const Node &rhs) {
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12
         ret.val = min(val, rhs.val);
         return ret; // 視情況修改
13
14
15
    };
16
     vector<vector<Node>> arr;
17
     Sparse Table() {
18
      arr.resize(__lg(RANGE) + 1, vector<Node>(RANGE, Node()));
19
20
21
22
     void build(auto &v) {
23
       for (int i = 1; i <= n; i++) {
         arr[0][i].val = v[i];
25
26
       for (int i = 1; i <= lg(n); i++)
         for (int j = 1; j + (1 << (i - 1)) <= n; <math>j++)
           arr[i][j] = arr[i - 1][j] + arr[i - 1][j + (1 << (i - 20))]
    }
29
    Node query(int ql, int qr) {
      int \lg = \lg(qr - ql + 1);
      return arr[lg][ql] + arr[lg][qr - (1 << lg) + 1];</pre>
34
35 };
```

2.2 Fenwick Tree

```
1 / ** 普通 BIT ,為了加速打字只支援 1-based **/
  const int MAXN = ?; // 開全域加速打字
  #define lowbit(x & (-x))
  template<typename T>
  struct Fenwick Tree { // 1 based
      // 二維: 陣列開二維, 修改跟查詢就是對 (x, y) 各自 +-
           lowbit
      T arr[MAXN];
      void init(int _n = MAXN) {
          for (int i = 0; i < _n; i++)</pre>
              arr[i] = 0;
12
13
      void update(int i, T val) {
14
          for (: i < MAXN: i += lowbit(i))</pre>
              arr[i] += val;
16
17
18
      T query(int i) {
          T ret = 0;
          for (; i; i -= lowbit(i))
20
              ret += arr[i];
21
22
          return ret;
23
```

```
1 // https://judge.yosupo.jp/problem/point_add_range_sum 331 ms
2 // https://judge.yosupo.jp/problem/staticrmq 359 ms
3 template<typename T, int RANGE>
 4 struct Segment Tree {
    struct Node {
      T val;
       Node (): val(0) {} // mx: -INF, mn: INF, sum: 0, gcd: 1,
            1cm: 1
       Node operator +(const Node &rhs) {
         Node ret;
         ret.val = val + rhs.val; // 對應不同操作修改
         return ret;
       void update(int _val) {
         val += val;
    };
    vector<Node> arr:
     Segment Tree() {
       arr.resize(RANGE << 2);</pre>
     void build(vector<int> &v, int i = 1, int l = 1, int r = n)
       if (1 == r) {
         arr[i].val = v[1];
         return;
       int mid = (1 + r) \gg 1;
       build(v, i << 1, 1, mid);
       build(v, i << 1 | 1, mid + 1, r);
       arr[i] = arr[i << 1] + arr[i << 1 | 1];
     void update(int pos, int val, int i = 1, int l = 1, int r =
           n) {
       if (1 == r) {
         arr[i].update(val);
         return;
       int mid = (1 + r) >> 1;
       if (pos <= mid) update(pos, val, i << 1, 1, mid);</pre>
       else update(pos, val, i << 1 | 1, mid + 1, r);</pre>
       arr[i] = arr[i << 1] + arr[i << 1 | 1];</pre>
     Node query(int ql, int qr, int i = 1, int l = 1, int r = n)
       if (\dot{l} > qr \mid | r < ql)
        return Node();
       if (ql <= 1 && r <= qr)</pre>
        return arr[i];
       int mid = (1 + r) >> 1;
       return query(ql, qr, i << 1, l, mid) + query(ql, qr, i <</pre>
            1 \mid 1, \text{ mid } + 1, \text{ r};
58 };
```

2.4 最大區間和線段樹

```
1 /** 計算最大子區間連續和的線段樹,限定 1-based。
2 * 複雜度 O(O*log(N)) **/
3 #define ls i << 1
4 #define rs i << 1 | 1
  class MaxSumSegmentTree {
     private:
      struct node {
          11 lss, rss, ss, ans;
          void set(11 v) { lss = rss = ss = ans = v; }
11
      int n;
      vector<node> a; // 萬萬不可用普通陣列,要用 vector
      vector<11> z:
      void pull(int i) {
          a[i].ss = a[ls].ss + a[rs].ss;
          a[i].lss = max(a[ls].lss, a[ls].ss + a[rs].lss);
          a[i].rss = max(a[rs].rss, a[rs].ss + a[ls].rss):
          a[i].ans = max(max(a[ls].ans, a[rs].ans),
                         a[ls].rss + a[rs].lss);
20
      void build(int i, int 1, int r) {
21
          if (1 == r) return a[i].set(z[1]), void();
23
          int m = (1 + r) >> 1;
          build(ls, l, m), build(rs, m + 1, r), pull(i);
24
25
      void set(int i, int l, int r, int q, ll v) {
26
          if (1 == r) return a[i].set(v), void();
          int m = (1 + r) >> 1;
          if (q <= m) set(ls, l, m, q, v);</pre>
          else set(rs, m + 1, r, q, v);
          pull(i);
      node query(int i, int l, int r, int ql, int qr) {
          if (ql <= 1 && r <= qr) return a[i];</pre>
          int m = (1 + r) >> 1:
          if (qr <= m) return query(ls, l, m, ql, qr);</pre>
          if (m < ql) return query(rs, m + 1, r, ql, qr);</pre>
          node lo = query(ls, l, m, ql, qr),
               ro = query(rs, m + 1, r, ql, qr), ans;
          ans.ss = lo.ss + ro.ss;
          ans.lss = max(lo.lss, lo.ss + ro.lss):
          ans.rss = max(ro.rss, ro.ss + lo.rss);
          ans.ans = max(max(lo.ans, ro.ans), lo.rss + ro.lss);
          return ans:
     public:
      MaxSumSegmentTree(int n) : n(n) {
          a.resize(n << 2), z.resize(n << 2);
          build(1, 1, n);
50
      // 單點設值。限定 1-based 。
      inline void set(int i, ll v) { set(1, 1, n, i, v); }
      // 問必區間 [1, r] 的最大子區間連續和。限定 1-based 。
      inline 11 querv(int 1, int r) {
          return query(1, 1, n, l, r).ans;
58 };
```

2.5 懶標線段樹

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```
1 struct Node {
      int sum, tag;
      Node(): sum(0), tag(0) {}
      void update(int val, int 1, int r) {
          sum += (val) * (r - 1 + 1);
          tag += val:
      Node operator +(const Node rhs) {
          ret.sum = sum + rhs.sum:
          return ret:
      void operator *=(const Node rhs) {
          sum = rhs.sum;
17
  };
18
   template<typename T>
   struct Segment Tree {
      vector<T> arr:
      void init() {
          arr.resize(MAXN << 2, Node());</pre>
      void push(int i, int l, int r) {
          if (1 == r | | arr[i].tag == 0)
          int mid = (1 + r) / 2:
          arr[i * 2].update(arr[i].tag, 1, mid);
          arr[i * 2 + 1].update(arr[i].tag, mid + 1, r);
          arr[i].tag = 0:
      void update(int al, int ar, int val, int i = 1, int l =
           1, int r = n) {
          if (al <= 1 && r <= ar) {
              arr[i].update(val, l, r);
              return;
          if (1 > qr || r < q1)
              return;
          int mid = (1 + r) / 2;
          push(i, 1, r);
          update(q1, qr, val, i * 2, 1, mid);
          update(ql, qr, val, i * 2 + 1, mid + 1, r);
          arr[i].sum = (arr[i * 2] + arr[i * 2 + 1]).sum;
      T query(int ql, int qr, int i = 1, int l = 1, int r = n) 2.7 李超線段樹
          if (q1 <= 1 && r <= qr)
              return arr[i];
          if (1 > qr \mid | r < q1)
              return T();
          push(i, 1, r);
          int mid = (1 + r) / 2;
          auto q1 = query(q1, qr, i * 2, 1, mid);
          auto q2 = query(q1, qr, i * 2 + 1, mid + 1, r);
          return q1 + q2;
60
61 };
```

2.6 持久化線段樹

```
int a[maxn], b[maxn], root[maxn], cnt;
 2 struct node {
      int sum, L son, R son;
 4 } tree[maxn << 51:
 5 int create(int sum, int L son, int R son) {
       int idx = ++cnt;
       tree[idx].sum = sum, tree[idx].L son = L son, tree[idx
           1.R son = R son;
       return idx;
void Insert(int &root, int pre_rt, int pos, int L, int R) {
       root = create(tree[pre rt].sum+1, tree[pre rt].L son,
            tree[pre rt].R son);
       if(L==R) return:
       int M = (L+R) >> 1:
       if(pos<=M) Insert(tree[root].L_son, tree[pre_rt].L_son,</pre>
            pos, L, M);
       else Insert(tree[root].R son, tree[pre rt].R son, pos, M
            +1, R);
16 }
  int query(int L id, int R id, int L, int R, int K) {
       if(L==R) return L;
       int M = (L+R)>>1:
       int s = tree[tree[R id].L son].sum - tree[tree[L id].
20
            L son ]. sum;
       if(K<=s) return query(tree[L_id].L_son, tree[R_id].L_son,</pre>
            L, M, K);
       return query(tree[L id].R son, tree[R id].R son, M+1, R,
22
            K-s):
23
  int main() {
24
       int n.m: cin >> n >> m
25
       for(int i=1; i<=n; i++) {</pre>
           cin >> a[i]; b[i] = a[i];
27
       } sort(b+1,b+1+n); //離散化
       int b sz = unique(b+1, b+1+n) - (b+1);
29
       cnt = root[0] = 0;
31
       for(int i=1; i<=n; i++) {</pre>
           int pos = lower bound(b+1, b+1+b sz, a[i]) - b;
32
33
           Insert(root[i], root[i-1], pos, 1, b sz);
34
       while(m--) {
35
           int 1, r, k; cin \gg 1 \gg r \gg k;
36
37
           int pos = query(root[1-1],root[r],1,b sz,k);
38
           cout << b[pos] << endl;</pre>
39
       } return 0:
```

```
1 template<typename T>
2 struct LiChao SegTree {
     T arr[MAXM << 2];
      void init() {
          for (int i = 0; i < (MAXM << 2); i++) {
              arr[i] = \{m, 0\};
```

```
void insert(int i, int l, int r, T x) {
                                                                               if (!t) return:
                                                                               t->val += v, t->inc += v, t->mn += v;
           if (1 == r) {
12
                                                                   21
                                                                                                                                               // 區間 [1, r] 向右 rotate k 次, k < 0 表向左 rotate
               if (x(1) < arr[i](1)) {</pre>
13
                                                                    22
                                                                                                                                               void rotate(int 1, int r, int k) {
                                                                                                                                        87
                                                                           void push(Node* t) {
                   arr[i] = x;
14
                                                                    23
                                                                                                                                                   int len = r - 1 + 1;
                                                                                                                                        88
                                                                               if (t\rightarrow rev) rev(t\rightarrow lc), rev(t\rightarrow rc), t\rightarrow rev = 0;
15
                                                                    24
                                                                                                                                                   Node *a, *b, *c, *d, *e, *f;
                                                                                                                                        89
                                                                    25
                                                                               update(t->lc, t->inc), update(t->rc, t->inc);
                                                                                                                                                   split(root, a, b, r);
               return;
                                                                                                                                        90
17
                                                                    26
                                                                               t\rightarrow inc = 0:
                                                                                                                                                   split(a, c, d, 1 - 1);
                                                                                                                                        91
                                                                    27
18
                                                                                                                                        92
                                                                                                                                                   k = (k + len) \% len:
           if (arr[i].a > x.a) {
                                                                           void pull(Node* t) {
19
                                                                    28
                                                                                                                                        93
                                                                                                                                                   split(d, e, f, len - k);
               swap(arr[i], x);
                                                                    29
                                                                               t\rightarrow size = 1 + size(t\rightarrow lc) + size(t\rightarrow rc);
20
                                                                                                                                        94
                                                                                                                                                   root = merge(merge(c, merge(f, e)), b);
21
                                                                    30
                                                                               t \rightarrow mn = t \rightarrow val:
                                                                                                                                        95
22
                                                                    31
                                                                               if (t->1c) t->mn = min(t->mn, t->1c->mn):
                                                                                                                                               // 插入一個元素 val 使其 index = i
                                                                               if (t->rc) t->mn = min(t->mn, t->rc->mn);
23
           int mid = (1 + r) / 2;
                                                                    32
                                                                                                                                               // 注意 i <= size
                                                                                                                                        97
24
                                                                    33
                                                                                                                                               void insert(int i, ll val) {
                                                                                                                                        98
25
           if (x(mid) > arr[i](mid)) {
                                                                    34
                                                                           // 看你要不要釋放記憶體
                                                                                                                                                   if (i == size() + 1) {
                                                                                                                                        99
26
               insert(i * 2, 1, mid, x);
                                                                           void discard(Node* t) {
                                                                    35
                                                                                                                                       100
                                                                                                                                                       push back(val);
27
                                                                    36
                                                                               if (!t) return;
                                                                                                                                                       return;
                                                                                                                                       101
           else {
28
                                                                               discard(t->lc), discard(t->rc);
                                                                    37
                                                                                                                                       102
29
               swap(arr[i], x);
                                                                    38
                                                                               delete t:
                                                                                                                                                   assert(i <= size());</pre>
                                                                                                                                       103
               insert(i * 2 + 1, mid + 1, r, x);
30
                                                                    39
                                                                                                                                                   Node *a, *b;
                                                                                                                                       104
31
                                                                           void split(Node* t, Node*& a, Node*& b, int k) {
                                                                    40
                                                                                                                                                   split(root, a, b, i - 1);
                                                                                                                                       105
32
                                                                    41
                                                                               if (!t) return a = b = 0, void();
                                                                                                                                       106
                                                                                                                                                   root = merge(merge(a, new Node(val)), b);
33
                                                                               push(t);
                                                                                                                                       107
34
       int query(int i, int l, int r, int pos) {
                                                                               if (size(t->lc) < k) {
                                                                                                                                       108
                                                                                                                                               void push back(ll val) {
           if (1 == r)
35
                                                                                                                                                   root = merge(root, new Node(val));
                                                                                                                                       109
36
               return arr[i](pos);
                                                                                   split(t\rightarrow rc, a\rightarrow rc, b, k - size(t\rightarrow lc) - 1);
                                                                                                                                       110
           int mid = (1 + r) / 2;
37
                                                                    46
                                                                                   pull(a);
                                                                                                                                               void remove(int 1, int r) {
                                                                                                                                       111
38
           int res:
                                                                    47
                                                                               } else {
                                                                                                                                                   int len = r - l + 1;
                                                                                                                                       112
           if (pos <= mid) {</pre>
39
                                                                    48
                                                                                   b = t:
                                                                                                                                                   Node *a, *b, *c, *d;
                                                                                                                                       113
               res = query(i * 2, 1, mid, pos);
40
                                                                    49
                                                                                   split(t->lc, a, b->lc, k);
                                                                                                                                                   split(root, a, b, l - 1);
                                                                                                                                       114
41
                                                                    50
                                                                                   pull(b);
                                                                                                                                       115
                                                                                                                                                   split(b, c, d, len);
42
           else {
                                                                    51
                                                                               }
                                                                                                                                                   discard(c); // 看你要不要釋放記憶體
                                                                                                                                       116
               res = query(i * 2 + 1, mid + 1, r, pos);
43
                                                                    52
                                                                                                                                                   root = merge(a, d);
                                                                                                                                       117
44
                                                                           Node* merge(Node* a, Node* b) {
                                                                                                                                       118
45
           return min(res, arr[i](pos));
                                                                               if (!a | | !b) return a ? a : b:
                                                                                                                                               11 minn(int 1, int r) {
                                                                                                                                       119
46
                                                                               if (a->pri > b->pri) {
                                                                                                                                                   Node *a, *b, *c, *d;
                                                                                                                                       120
47 };
                                                                                   push(a);
                                                                                                                                                   split(root, a, b, r);
                                                                                                                                       121
                                                                    57
                                                                                   a \rightarrow rc = merge(a \rightarrow rc, b);
                                                                                                                                                   split(a, c, d, l - 1);
                                                                                                                                       122
                                                                                   pull(a);
                                                                                                                                                   int ans = d->mn:
                                                                                                                                       123
                                                                                   return a:
                                                                                                                                                   root = merge(merge(c, d), b);
                                                                                                                                       124
  2.8 Treap
                                                                    60
                                                                               } else {
                                                                                                                                       125
                                                                                                                                                   return ans;
                                                                    61
                                                                                   push(b);
                                                                                                                                       126
                                                                                   b->lc = merge(a, b->lc);
                                                                                                                                       127 };
1 // 支援區間加值、區間反轉、區間 rotate 、區間刪除、插入元素、
                                                                                   pull(b);
                                                                                   return b:
        ポ 區 間
2 /// 最小值的元素的 Treap。使用前建議 srand(time(0)); 除了 size
                                                                                                                                          2.9 Dynamic KD tree
                                                                           inline int size(Node* t) { return t ? t->size : 0: }
3 // 方法以外,所有操作都是 O(log N) 。所有 public 方法各自獨
                                                                           int size() { return size(root); }
4 // 斟酌要使用到哪些方法,有需要的才抄。
                                                                           void add(int 1, int r, 11 val) {
                                                                                                                                         1 template<typename T, size t kd>//有kd個維度
  class Treap {
                                                                                                                                         2 struct kd tree{
                                                                               Node *a, *b, *c, *d;
     private:
                                                                               split(root, a, b, r);
                                                                                                                                            struct point{
                                                                    72
       struct Node {
                                                                    73
                                                                               split(a, c, d, l - 1);
                                                                                                                                              T d[kd];
           int pri = rand(), size = 1;
                                                                                                                                               T dist(const point &x)const{
                                                                    74
                                                                               update(d, val);
           11 \text{ val, mn, inc} = 0;
                                                                                                                                                 T ret=0:
                                                                    75
                                                                               root = merge(merge(c, d), b);
           bool rev = 0;
                                                                                                                                                 for(size t i=0;i<kd;++i)ret+=abs(d[i]-x.d[i]);</pre>
                                                                    76
           Node *1c = 0. *rc = 0:
                                                                                                                                                 return ret:
                                                                           // 反轉區間 [1, r]
                                                                    77
           Node(11 v) { val = mn = v; }
12
                                                                           void reverse(int 1, int r) {
                                                                                                                                               bool operator == (const point &p){
13
                                                                                                                                        10
                                                                               Node *a, *b, *c, *d;
                                                                    79
                                                                                                                                                 for(size t i=0;i<kd;++i)</pre>
       Node* root = 0;
                                                                                                                                        11
                                                                               split(root, a, b, r):
       void rev(Node* t) {
                                                                                                                                                   if(d[i]!=p.d[i])return 0;
15
                                                                                                                                        12
                                                                               split(a, c, d, 1 - 1);
                                                                    81
```

swap(d->lc, d->rc);

root = merge(merge(c, d), b);

d->rev ^= 1:

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13

14

return 1:

return d[0]<b.d[0];</pre>

bool operator<(const point &b)const{</pre>

if (!t) return;

void update(Node* t, 11 v) {

17

18

 $swap(t->lc, t->rc), t->rev ^= 1;$

```
148 public:
                                                                         node *findmin(node*o,int k){
                                                                                                                                             kd tree(const T &INF, double a=0.75):
18
    };
   private:
                                                                    84
                                                                           if(!o)return 0;
                                                                                                                                             root(0),alpha(a),loga(log2(1.0/a)),INF(INF),maxn(1){}
19
                                                                           if(cmp.sort id==k)return o->1?findmin(o->1,(k+1)%kd):o;
                                                                                                                                             ~kd tree(){delete root;}
20
    struct node{
                                                                    85
                                                                                                                                             void clear(){delete root,root=0,maxn=1;}
       node *1,*r;
                                                                    86
                                                                           node *l=findmin(o->l,(k+1)%kd);
21
                                                                           node *r=findmin(o->r,(k+1)%kd);
                                                                                                                                             void build(int n,const point *p){
22
       point pid;
23
       int s:
                                                                    88
                                                                           if(1&&!r)return cmp(1.o)?1:o:
                                                                                                                                        154
                                                                                                                                                delete root.A.resize(maxn=n);
       node(const point &p):1(0),r(0),pid(p),s(1){}
                                                                    89
                                                                           if(!1&&r)return cmp(r,o)?r:o;
                                                                                                                                        155
                                                                                                                                                for(int i=0;i<n;++i)A[i]=new node(p[i]);</pre>
24
                                                                           if(!1&&!r)return o;
                                                                                                                                                root=build(0,0,n-1);
25
       ~node(){delete l,delete r;}
                                                                    90
                                                                                                                                        156
       void up()\{s=(1?1->s:0)+1+(r?r->s:0);\}
                                                                    91
                                                                           if(cmp(1,r))return cmp(1,0)?1:0;
                                                                                                                                        157
26
27
                                                                    92
                                                                           return cmp(r,o)?r:o;
                                                                                                                                        158
                                                                                                                                             void insert(const point &x){
     const double alpha,loga;
                                                                    93
                                                                                                                                                insert(root,0,x,__lg(size(root))/loga);
                                                                                                                                        159
                                                                    94
                                                                         bool erase(node *&u,int k,const point &x){
                                                                                                                                                if(root->s>maxn)maxn=root->s;
29
     const T INF;//記得要給INF,表示極大值
                                                                                                                                        160
                                                                    95
                                                                           if(!u)return 0:
                                                                                                                                        161
30
     int maxn;
                                                                    96
                                                                           if(u->pid==x){
                                                                                                                                        162
                                                                                                                                             bool erase(const point &p){
     struct __cmp{
                                                                    97
                                                                             if(u->r);
                                                                                                                                        163
                                                                                                                                                bool d=erase(root,0,p);
       int sort id;
32
                                                                    98
                                                                              else if(u \rightarrow 1) u \rightarrow r = u \rightarrow 1, u \rightarrow 1 = 0:
                                                                                                                                                if(root&&root->s<alpha*maxn)rebuild();</pre>
                                                                                                                                        164
       bool operator()(const node*x,const node*y)const{
33
                                                                             else return delete(u),u=0, 1;
                                                                                                                                                return d;
         return operator()(x->pid,y->pid);
                                                                    99
                                                                                                                                        165
34
                                                                   100
                                                                                                                                        166
35
                                                                             cmp.sort id=k:
                                                                                                                                             void rebuild(){
                                                                   101
                                                                                                                                        167
36
       bool operator()(const point &x,const point &y)const{
                                                                   102
                                                                             u->pid=findmin(u->r,(k+1)%kd)->pid;
                                                                                                                                        168
                                                                                                                                                if(root)rebuild(root,0);
37
         if(x.d[sort id]!=y.d[sort id])
                                                                             return erase(u->r.(k+1)%kd.u->pid):
                                                                                                                                                maxn=root->s:
           return x.d[sort id]<y.d[sort id];</pre>
                                                                   103
                                                                                                                                        169
                                                                   104
                                                                                                                                        170
         for(size t i=0;i<kd;++i)</pre>
                                                                   105
                                                                           cmp.sort id=k;
                                                                                                                                        171
                                                                                                                                             T nearest(const point &x,int k){
           if(x.d[i]!=y.d[i])return x.d[i]<y.d[i];</pre>
                                                                           if(erase(cmp(x,u->pid)?u->1:u->r,(k+1)%kd,x))
                                                                   106
                                                                                                                                        172
         return 0;
                                                                   107
                                                                             return --u->s, 1:
                                                                                                                                        173
                                                                                                                                                T mndist=INF,h[kd]={};
42
                                                                           return 0;
                                                                                                                                                nearest(root,0,x,h,mndist);
                                                                   108
                                                                                                                                        174
     }cmp;
                                                                                                                                        175
                                                                                                                                                mndist=pQ.top().first;
                                                                   109
     int size(node *o){return o?o->s:0;}
                                                                   110
                                                                         T heuristic(const T h[])const{
                                                                                                                                        176
                                                                                                                                                pQ = priority_queue<pair<T,point>>();
     vector<node*> A:
                                                                   111
                                                                                                                                                return mndist;//回傳離x第k近的點的距離
    node* build(int k,int l,int r){
                                                                                                                                        177
                                                                   112
                                                                           for(size t i=0;i<kd;++i)ret+=h[i];</pre>
       if(1>r) return 0;
                                                                                                                                        178
                                                                   113
                                                                           return ret;
       if(k==kd) k=0;
                                                                                                                                        179
                                                                                                                                             const vector<point> &range(const point&mi,const point&ma){
                                                                   114
       int mid=(1+r)/2;
                                                                                                                                                in range.clear();
                                                                                                                                        180
                                                                   115
                                                                         int qM;
       cmp.sort id = k;
                                                                                                                                                range(root,0,mi,ma);
50
                                                                                                                                        181
                                                                         priority_queue<pair<T,point>> pQ;
       nth element(A.begin()+1, A.begin()+mid, A.begin()+r+1, cmp); 116
                                                                                                                                                return in range;//回傳介於mi到ma之間的點vector
                                                                                                                                        182
                                                                         void nearest(node *u,int k,const point &x,T *h,T &mndist){
52
       node *ret=A[mid];
                                                                           if(u==0||heuristic(h)>=mndist)return;
                                                                   118
       ret->l = build(k+1,l,mid-1);
                                                                                                                                        184
                                                                                                                                             int size(){return root?root->s:0;}
                                                                           T dist=u->pid.dist(x),old=h[k];
       ret->r = build(k+1,mid+1,r);
                                                                   119
                                                                                                                                        185 };
                                                                   120
                                                                           /*mndist=std::min(mndist.dist):*/
55
       ret->up();
                                                                   121
                                                                           if(dist<mndist){</pre>
       return ret:
                                                                             pQ.push(std::make pair(dist,u->pid));
                                                                   122
57
                                                                             if((int)pQ.size()==qM+1)
                                                                   123
     bool isbad(node*o){
58
                                                                                                                                           2.10 Heavy Light
                                                                               mndist=p0.top().first,p0.pop();
       return size(o->1)>alpha*o->s||size(o->r)>alpha*o->s;
                                                                   124
59
                                                                   125
60
                                                                           if(x.d[k]<u->pid.d[k]){
     void flatten(node *u, typename vector<node*>::iterator &it){126
61
                                                                             nearest(u->1,(k+1)%kd,x,h,mndist);
                                                                                                                                         1 | #include < vector >
62
       if(!u)return;
                                                                             h[k] = abs(x.d[k]-u->pid.d[k]);
                                                                                                                                         2 #define MAXN 100005
63
       flatten(u->1,it);
                                                                   128
                                                                             nearest(u->r,(k+1)%kd,x,h,mndist);
                                                                                                                                         3 int siz[MAXN], max son[MAXN], pa[MAXN], dep[MAXN];
                                                                   129
64
       *it=u:
                                                                                                                                         4 int link_top[MAXN],link[MAXN],cnt;
65
       flatten(u->r,++it);
                                                                   130
                                                                             nearest(u->r,(k+1)%kd,x,h,mndist);
                                                                                                                                         5 vector<int> G[MAXN];
                                                                   131
66
                                                                                                                                         6 void find max son(int u){
                                                                             h[k] = abs(x.d[k]-u->pid.d[k]);
     void rebuild(node*&u,int k){
                                                                   132
67
                                                                             nearest(u->1,(k+1)%kd,x,h,mndist);
                                                                                                                                             siz[u]=\overline{1};
                                                                   133
       if((int)A.size()<u->s)A.resize(u->s);
                                                                                                                                             max son[u]=-1;
69
       auto it=A.begin();
                                                                   134
       flatten(u.it):
                                                                   135
                                                                           h[k]=old;
                                                                                                                                             for(auto v:G[u]){
70
                                                                   136
                                                                                                                                               if(v==pa[u])continue;
       u=build(k,0,u->s-1);
71
                                                                         vector<point>in_range;
                                                                                                                                                pa[v]=u;
72
                                                                         void range(node *u,int k,const point&mi,const point&ma){
                                                                                                                                                dep[v]=dep[u]+1;
     bool insert(node*&u,int k,const point &x,int dep){
73
                                                                   139
                                                                           if(!u)return:
                                                                                                                                                find max son(v);
74
       if(!u) return u=new node(x), dep<=0;</pre>
                                                                                                                                                if(max_son[u]==-1||siz[v]>siz[max_son[u]])max_son[u]=v;
75
       ++u->s:
                                                                   140
                                                                           bool is=1;
                                                                                                                                         14
                                                                           for(int i=0:i<kd:++i)</pre>
                                                                                                                                                siz[u]+=siz[v];
                                                                   141
                                                                                                                                         15
76
       cmp.sort id=k;
                                                                             if(u->pid.d[i]<mi.d[i]||ma.d[i]<u->pid.d[i])
       if(insert(cmp(x,u->pid)?u->l:u->r,(k+1)%kd,x,dep-1)){
                                                                   142
                                                                                                                                         16
         if(!isbad(u))return 1;
                                                                   143
                                                                               { is=0;break; }
                                                                                                                                         17 }
78
                                                                   144
                                                                           if(is) in range.push back(u->pid);
                                                                                                                                           void build link(int u,int top){
         rebuild(u,k);
79
                                                                           if(mi.d[k]<=u->pid.d[k])range(u->1,(k+1)%kd,mi,ma);
                                                                                                                                             link[u]=++cnt;
                                                                   145
                                                                           if(ma.d[k]>=u->pid.d[k])range(u->r,(k+1)%kd,mi,ma);
                                                                                                                                             link top[u]=top;
                                                                   146
       return 0;
```

if(max son[u]==-1)return;

```
build link(max son[u],top);
    for(auto v:G[u]){
23
      if(v==max_son[u]||v==pa[u])continue;
24
25
      build link(v,v);
26
27
   int find lca(int a,int b){
    //求LCA,可以在過程中對區間進行處理
    int ta=link_top[a],tb=link_top[b];
    while(ta!=tb){
31
      if(dep[ta]<dep[tb]){</pre>
32
33
        swap(ta,tb);
34
        swap(a,b);
35
      //這裡可以對a所在的鏈做區間處理
      //區間為(link[ta],link[a])
38
      ta=link_top[a=pa[ta]];
39
    //最後a,b會在同一條鏈,若a!=b還要在進行一次區間處理
    return dep[a]<dep[b]?a:b;</pre>
42
```

2.11 HLD By Koying

```
1 // https://cses.fi/problemset/task/1137/
   struct HLD {
       struct Info {
           int sub, mxsub, dep, fa, root, id;
       } arr[MAXN];
       int index = 0:
       void find_son(int i, int fa) {
           pii mx(0, i);
           arr[i].sub = 1;
12
           for (auto it: G[i]) if (it != fa) {
13
               arr[it].dep = arr[i].dep + 1;
14
               arr[it].fa = i;
15
               find son(it, i);
16
               cmax(mx, pii(arr[it].sub, it));
17
18
               arr[i].sub += arr[it].sub;
19
           arr[i].mxsub = mx.S;
20
21
22
       void build(int i, int root) {
23
           arr[i].root = root;
24
           arr[i].id = ++index;
26
           y[arr[i].id] = x[i];
27
           if (arr[i].mxsub != i) {
               build(arr[i].mxsub, root);
29
               y[arr[i].id] += y[arr[arr[i].mxsub].id];
32
           for (auto it: G[i]) if (it != arr[i].fa && it != arr[ 39
33
               build(it, it);
35
               y[arr[i].id] += y[arr[it].id];
36
```

```
void jump(int a, int b) \{ // \text{ from a to b } (dep(a) > dep(b)) | 46 | int access(int x) \}
39
                                                                           47
40
            while (arr[a].root != arr[b].root) {
                 if (arr[arr[a].root].dep < arr[arr[b].root].dep)</pre>
41
42
                 a = arr[arr[a].root].fa;
43
44
45
            if (arr[a].dep < arr[b].dep)</pre>
46
                 swap(a, b);
47
48
            return mx:
49
   } HLD;
```

2.12 Link Cut Tree

```
1 | struct splay_tree{
    int ch[2],pa;//子節點跟父母
    bool rev;//反轉的懶惰標記
    splay_tree():pa(0),rev(0){ch[0]=ch[1]=0;}
  vector<splay_tree> nd;
  //有的時候用vector會TLE,要注意
 8 | // 這邊以node [0] 作為null 節點
9 bool isroot(int x){//判斷是否為這棵splay tree的根
    return nd[nd[x].pa].ch[0]!=x&&nd[nd[x].pa].ch[1]!=x;
11
12
  void down(int x){//懶惰標記下推
    if(nd[x].rev){
      if(nd[x].ch[0])nd[nd[x].ch[0]].rev^=1;
14
15
      if(nd[x].ch[1])nd[nd[x].ch[1]].rev^=1;
      swap(nd[x].ch[0],nd[x].ch[1]);
16
17
      nd[x].rev=0;
18
19
  void push down(int x){//所有祖先懶惰標記下推
    if(!isroot(x))push down(nd[x].pa);
22
    down(x);
23
  void up(int x){}//將子節點的資訊向上更新
   void rotate(int x){//旋轉,會自行判斷轉的方向
    int y=nd[x].pa,z=nd[y].pa,d=(nd[y].ch[1]==x);
28
    if(!isroot(y))nd[z].ch[nd[z].ch[1]==y]=x;
    nd[y].ch[d]=nd[x].ch[d^1];
29
    nd[nd[y].ch[d]].pa=y;
30
    nd[y].pa=x,nd[x].ch[d^1]=y;
31
32
    up(y),up(x);
33
   void splay(int x){//將x伸展到splay tree的根
    push down(x);
    while(!isroot(x)){
      int y=nd[x].pa;
      if(!isroot(y)){
        int z=nd[y].pa;
        if((nd[z].ch[0]==y)^(nd[y].ch[0]==x))rotate(y);
        else rotate(x);
41
42
43
      rotate(x);
```

```
48
     while(x){
       splay(x);
49
       nd[x].ch[1]=last;
51
       up(x):
       last=x;
52
53
       x=nd[x].pa;
54
     return last;//access後splay tree的根
56
   void access(int x,bool is=0){//is=0就是一般的access
     int last=0;
     while(x){
60
       splay(x);
       if(is&&!nd[x].pa){
61
62
         //printf("%d\n", max(nd[last].ma,nd[nd[x].ch[1]].ma));
63
       nd[x].ch[1]=last;
64
65
       up(x);
66
       last=x:
67
       x=nd[x].pa;
68
69
   void query edge(int u,int v){
     access(u);
     access(v,1);
73
   void make_root(int x){
     access(x), splay(x);
     nd[x].rev^=1;
77
   void make root(int x){
     nd[access(x)].rev^=1;
     splay(x);
81
    void cut(int x,int y){
     make root(x);
     access(y);
     splay(y);
     nd[y].ch[0]=0;
     nd[x].pa=0;
    void cut parents(int x){
     access(x);
     splay(x);
     nd[nd[x].ch[0]].pa=0;
     nd[x].ch[0]=0;
    void link(int x,int y){
     make root(x);
97
     nd[x].pa=y;
    int find root(int x){
     x=access(x):
101
     while(nd[x].ch[0])x=nd[x].ch[0];
102
     splay(x);
     return x;
103
104
   int query(int u,int v){
106 //傳回uv路徑splay tree的根結點
107 // 這種寫法無法求LCA
     make root(u);
108
     return access(v);
```

int last=0;

```
A.push_back(BB(w, v, c));
                                                                                       if( a[i-1]>b[j-1] && dp[i-1][j]>dp[i-1][p] ) 41
int query_lca(int u,int v){
                                                                                                                                       42
                                                                                           p = j;
    // 假 設 求 鏈 上 點 權 的 總 和 , sum 是 子 樹 的 權 重 和 , data 是 節 點 的 權 重
                                                                                   } else {
                                                                                                                                       43
                                                                                                                                                  assert(N < MAXN);</pre>
                                                                                       dp[i][j] = dp[i-1][p]+1, pre[i][j] = p;
                                                                                                                                                  static int dp1[MAXW+1], dp2[MAXW+1];
     access(u);
                                                                                                                                       44
                                                                                                                                                  BB Ar[2][MAXN];
     int lca=access(v);
                                                                    13
                                                                                                                                       45
                                                                    14
                                                                                                                                       46
                                                                                                                                                  int ArN[2] = \{\};
115
     splay(u);
                                                                    15
                                                                           int len = 0, p = 0;
                                                                                                                                       47
                                                                                                                                                  memset(dp1, 0, sizeof(dp1[0])*(W+1));
     if(u==lca){
                                                                                                                                                  memset(dp2, 0, sizeof(dp2[0])*(W+1));
                                                                    16
                                                                           for(int j=1; j<=m; j++)</pre>
                                                                                                                                       48
       //return nd[lca].data+nd[nd[lca].ch[1]].sum
117
                                                                               if(dp[n][j]>len) len = dp[n][j], p = j;
                                                                                                                                       49
                                                                                                                                                  sort(A.begin(), A.end());
                                                                    17
118
                                                                           vector<int> ans;
                                                                                                                                       50
                                                                                                                                                  int sum[2] = {};
       //return nd[lca].data+nd[nd[lca].ch[1]].sum+nd[u].sum
                                                                    18
119
                                                                           for(int i=n; i>=1; i--) {
                                                                                                                                                  for (int i = 0; i < N; i++) {
                                                                    19
                                                                                                                                       51
120
                                                                               if(a[i-1]==b[p-1]) ans.push_back(b[p-1]);
                                                                                                                                       52
                                                                                                                                                      int ch = sum[1] < sum[0];</pre>
                                                                    20
121
                                                                    21
                                                                               p = pre[i][p];
                                                                                                                                       53
                                                                                                                                                      Ar[ch][ArN[ch]] = A[i];
    struct EDGE{
                                                                    22
                                                                                                                                       54
                                                                                                                                                      ArN[ch]++;
     int a,b,w;
                                                                    23
                                                                           reverse(ans.begin(), ans.end());
                                                                                                                                       55
                                                                                                                                                      sum[ch] = min(sum[ch] + A[i].w*A[i].c, W);
   }e[10005];
                                                                    24
                                                                           return ans;
                                                                                                                                       56
                                                                                                                                       57
                                                                                                                                                  run(Ar[0], dp1, W, ArN[0]);
   vector<pair<int,int>> G[10005];
                                                                                                                                       58
                                                                                                                                                  run(Ar[1], dp2, W, ArN[1]);
   //first表示子節點, second表示邊的編號
                                                                                                                                       59
                                                                                                                                                  int ret = 0;
   int pa[10005],edge_node[10005];
                                                                                                                                       60
                                                                                                                                                  for (int i = 0, j = W, mx = 0; i \leftarrow W; i++, j--) {
129 | //pa是父母節點,暫存用的,edge_node是每個編被存在哪個點裡面的
                                                                            Bounded Knapsack
                                                                                                                                                      mx = max(mx, dp2[i]);
                                                                                                                                       61
                                                                                                                                       62
                                                                                                                                                      ret = max(ret, dp1[j] + mx);
   void bfs(int root){
                                                                                                                                       63
    //在建構的時候把每個點都設成一個splay tree
                                                                       namespace {
                                                                                                                                       64
                                                                                                                                                  return ret;
     queue<int > q;
                                                                           static const int MAXW = 1000005;
                                                                                                                                       65
     for(int i=1;i<=n;++i)pa[i]=0;</pre>
                                                                           static const int MAXN = 1005;
                                                                                                                                       66
     q.push(root);
134
                                                                           struct BB {
                                                                                                                                       67
                                                                                                                                          int main() {
135
     while(q.size()){
                                                                               int w, v, c;
                                                                                                                                              int W, N;
136
       int u=q.front();
                                                                               BB(int w = 0, int v = 0, int c = 0): w(w), v(v), c(c) 69
                                                                                                                                              assert(scanf("%d %d", &W, &N) == 2);
137
                                                                                                                                              int C[MAXN][3];
       for(auto P:G[u]){
138
                                                                               bool operator<(const BB &x) const {</pre>
                                                                                                                                              for (int i = 0; i < N; i++)
139
         int v=P.first;
                                                                                                                                                  assert(scanf("%d %d %d", &C[i][1], &C[i][0], &C[i
                                                                                   return w * c < x.w * x.c;</pre>
                                                                                                                                       72
         if(v!=pa[u]){
140
                                                                                                                                                       ][2]) == 3);
141
           pa[v]=u;
                                                                           };
                                                                                                                                              printf("%d\n", knapsack(C, N, W));
           nd[v].pa=u;
142
                                                                           static int run(BB A[], int dp[], int W, int N) {
                                                                    11
                                                                                                                                              return 0;
           nd[v].data=e[P.second].w;
143
                                                                    12
                                                                               static int MQ[MAXW][2];
144
           edge_node[P.second]=v;
                                                                    13
                                                                               for (int i = 0, sum = 0; i < N; i++) {
           up(v);
145
                                                                                   int w = A[i].w, v = A[i].v, c = A[i].c;
           q.push(v);
146
                                                                    15
                                                                                   sum = min(sum + w*c, W);
                                                                                                                                          3.3 1D1D
147
                                                                    16
                                                                                   for (int j = 0; j < w; j++) {
148
                                                                    17
                                                                                       int 1 = 0, r = 0;
149
                                                                                       MQ[1][0] = 0, MQ[1][1] = dp[j];
150
                                                                    19
                                                                                       for (int k = 1, tw = w+j, tv = v; tw <= sum
                                                                                                                                        1 int t, n, L, p;
    void change(int x,int b){
                                                                                            && k <= c; k++, tw += w, tv += v) {
                                                                                                                                        2 char s[MAXN][35];
152
     splay(x);
                                                                    20
                                                                                            int dpv = dp[tw] - tv;
                                                                                                                                        3 | 11 sum[MAXN] = \{0\};
153
     //nd[x].data=b;
                                                                                            while (1 <= r && MQ[r][1] <= dpv) r--;
                                                                                                                                        4 long double dp[MAXN] = {0};
154
     up(x);
                                                                    ^{22}
                                                                                                                                          int prevd[MAXN] = {0};
155
                                                                                            MQ[r][0] = k, MQ[r][1] = dpv;
                                                                                                                                          long double pw(long double a, int n) {
                                                                    24
                                                                                            dp[tw] = max(dp[tw], MQ[1][1] + tv);
                                                                                                                                              if ( n == 1 ) return a;
                                                                                                                                              long double b = pw(a, n/2);
                                                                    26
                                                                                       for (int k = c+1, tw = (c+1)*w+j, tv = (c+1)*
                                                                                                                                              if ( n & 1 ) return b*b*a;
                                                                                            v; tw <= sum; k++, tw += w, tv += v) {
                                                                                                                                              else return b*b;
        DP
                                                                                            if (k - MQ[1][0] > c) 1++;
                                                                                                                                       11
                                                                                            int dpv = dp[tw] - tv;
                                                                                                                                          long double f(int i, int j) {
                                                                                            while (1 <= r \&\& MQ[r][1] <= dpv) r--;
                                                                                                                                              // cout << (sum[i] - sum[j]+i-j-1-L) << endl;</pre>
   3.1 LCIS
                                                                                                                                              return pw(abs(sum[i] - sum[j]+i-j-1-L), p) + dp[j];
                                                                                            MQ[r][0] = k, MQ[r][1] = dpv;
                                                                                                                                       15 }
                                                                                            dp[tw] = max(dp[tw], MQ[1][1] + tv);
                                                                                                                                          struct INV {
 1 vector<int> LCIS(vector<int> a, vector<int> b) {
                                                                                                                                              int L, R, pos;
       int n = a.size(), m = b.size();
       int dp[LEN][LEN] = {}, pre[LEN][LEN] = {};
                                                                    35
                                                                                                                                       19 INV stk[MAXN*10];
       for(int i=1; i<=n; i++) {</pre>
                                                                    36
                                                                                                                                       20 int top = 1, bot = 1;
                                                                           static int knapsack(int C[][3], int N, int W) { // O(WN)
                                                                                                                                          void update(int i) {
           int p = 0;
                                                                    37
           for(int j=1; j<=m; j++)</pre>
                                                                                                                                              while ( top > bot && i < stk[top].L && f(stk[top].L, i) <</pre>
                                                                    38
                                                                               vector<BB> A;
                                                                                                                                                    f(stk[top].L, stk[top].pos) ) {
                if(a[i-1]!=b[j-1]) {
                                                                    39
                                                                               for (int i = 0; i < N; i++) {
                    dp[i][j] = dp[i-1][j], pre[i][j] = j;
                                                                                   int w = C[i][0], v = C[i][1], c = C[i][2];
                                                                                                                                                  stk[top - 1].R = stk[top].R;
```

```
top--;
25
       int lo = stk[top].L, hi = stk[top].R, mid, pos = stk[top
26
       // if ( i >= lo ) lo = i + 1;
27
       while ( lo != hi ) {
29
           mid = lo + (hi - lo) / 2:
           if ( f(mid, i) < f(mid, pos) ) hi = mid;</pre>
30
31
           else lo = mid + 1;
32
33
       if ( hi < stk[top].R ) {</pre>
           stk[top + 1] = (INV) { hi, stk[top].R, i };
34
35
           stk[top++].R = hi;
36
37
38
   int main() {
       cin >> t:
39
       while ( t-- ) {
           cin >> n >> L >> p;
41
           dp[0] = sum[0] = 0;
42
43
           for ( int i = 1 ; i \le n ; i++ ) {
               cin >> s[i];
44
45
                sum[i] = sum[i-1] + strlen(s[i]);
               dp[i] = numeric_limits<long double>::max();
46
47
           stk[top] = (INV) \{1, n + 1, 0\};
           for ( int i = 1 ; i <= n ; i++ ) {
49
                if ( i >= stk[bot].R ) bot++;
50
51
               dp[i] = f(i, stk[bot].pos);
               update(i);
52
53
               // cout << (11) f(i, stk[bot].pos) << endl;</pre>
55
           if ( dp[n] > 1e18 ) {
                cout << "Too hard to arrange" << endl;</pre>
56
           } else {
                vector<PI> as:
59
               cout << (11)dp[n] << end1;</pre>
60
       } return 0;
61
```

4 Graph

4.1 Dijkstra

4.2 Bellman Ford

```
1 vector<pii> G[maxn];
2 int dis[maxn];
  bool BellmanFord(int n,int s) {
       for(int i=1; i<=n; i++) dis[i] = INF;</pre>
       dis[s] = 0:
       bool relax;
       for(int r=1; r<=n; r++) { //0(VE)
           relax = false;
           for(int i=1; i<=n; i++)</pre>
               for(pii e:G[i])
                   if( dis[i] + e.second < dis[e.first] )</pre>
11
                        dis[e.first] = dis[i] + e.second, relax =
12
13
14
       return relax; //有負環
```

4.3 SPFA

```
1 | vector<pii> G[maxn]; int dis[maxn];
  void SPFA(int n,int s) { //O(kE) k~2.
       for(int i=1; i<=n; i++) dis[i] = INF;</pre>
       dis[s] = 0;
       queue<int> q; q.push(s);
      bool inque[maxn] = {};
       while(!q.empty()) {
           int u = q.front(); q.pop();
           inque[u] = false;
           for(pii e:G[u]) {
11
               int v = e.first , w = e.second;
               if( dis[u] + w < dis[v]) {
13
                   if(!inque[v]) q.push(v), inque[v] = true;
14
                   dis[v] = dis[u] + w;
15
16
          }
```

4.4 Prim

```
9 while (nvis < n && q.size()) {
    11 d = q.top().first;
    int v = q.top().second; q.pop();
    if (vis[v]) continue;
    vis[v] = 1; ret += d;
    if (++nvis == n) return ret;
    for (auto& e : edge[v])
        if (!vis[e.second]) q.push(e);
    return -1;
    }
}</pre>
```

4.5 Mahattan MST

```
1 #define REP(i,n) for(int i=0;i<n;i++)</pre>
2 typedef long long LL;
3 const int N=200100;
4 int n,m;
5 struct PT {int x,y,z,w,id;} p[N];
  inline int dis(const PT &a,const PT &b){return abs(a.xb.x)+
       abs(a.y-b.y);}
  inline bool cpx(const PT &a,const PT &b)
8 {return a.x!=b.x? a.x>b.x:a.y>b.y;}
9 inline bool cpz(const PT &a,const PT &b){return a.z<b.z;}</pre>
struct E{int a,b,c;}e[8*N];
bool operator<(const E&a,const E&b){return a.c<b.c;}</pre>
12 struct Node{ int L,R,key; } node[4*N];
13 int s[N];
14 int F(int x) {return s[x]==x ? x : s[x]=F(s[x]); }
  void U(int a, int b) {s[F(b)]=F(a);}
16 void init(int id,int L,int R) {
17
       node[id] = (Node)\{L,R,-1\};
18
       if(L==R)return;
       init(id*2,L,(L+R)/2);
19
       init(id*2+1,(L+R)/2+1,R);
20
21 }
void ins(int id,int x) {
       if(node[id].key==-1 || p[node[id].key].w>p[x].w)
23
24
           node[id].key=x;
       if(node[id].L==node[id].R) return;
25
       if(p[x].z<=(node[id].L+node[id].R)/2) ins(id*2,x);</pre>
26
27
       else ins(id*2+1.x):
28
29
  int Q(int id,int L,int R){
       if(R<node[id].L || L>node[id].R)return -1;
       if(L<=node[id].L && node[id].R<=R)return node[id].key;</pre>
       int a=Q(id*2,L,R),b=Q(id*2+1,L,R);
32
       if(b==-1 || (a!=-1 && p[a].w<p[b].w)) return a;
33
       else return b;
34
35
  void calc() {
36
37
       REP(i,n) {
38
           p[i].z = p[i].y-p[i].x;
39
           p[i].w = p[i].x+p[i].y;
       sort(p,p+n,cpz);
       int cnt = 0, j, k;
43
       for(int i=0; i<n; i=j){</pre>
44
           for(j=i+1; p[j].z==p[i].z && j<n; j++);</pre>
45
           for(k=i, cnt++; k<j; k++) p[k].z = cnt;</pre>
       init(1,1,cnt);
47
       sort(p,p+n,cpx);
       REP(i,n) {
```

```
j=Q(1,p[i].z,cnt);
                                                                                                                                          // edge 是傳 reference ,完成所有查詢前萬萬不可以改。
           if(j!=-1) e[m++] = (E){p[i].id, p[j].id, dis(p[i],p[j 25])}
                                                                                                                                          OfflineTarjan(vector<vector<int>>& edge, int root)
                                                                                                                                   90
                                                                        SsadpTarjan(vector<vector<int>>& edge, int root)
                                                                                                                                   91
                                                                                                                                              : edge(edge), root(root), n(edge.size()) {}
          ins(1,i);
                                                                            : n(edge.size()) {
                                                                 27
                                                                                                                                          // 離線查詢, query 陣列包含所有詢問 {src, dst}。呼叫一
                                                                                                                                   92
53
                                                                 28
                                                                            dep.assign(n, -1); par.resize(n);
                                                                            ca.assign(n, vector<int>(n));
54
                                                                 29
                                                                                                                                          // 論 query 量多少, 複雜度都是 O(N) 。所以應盡量只呼叫一
                                                                                                                                   93
55
   LL MST() {
                                                                 30
                                                                                                                                               次。
      LL r=0;
                                                                 31
                                                                            for (int i = 0; i < n; i++) par[i] = i;
56
                                                                                                                                          vector<int> lca(vector<pii>& query) {
                                                                                                                                   94
57
       sort(e, e+m);
                                                                 32
                                                                            dfs(root, edge, 0);
                                                                                                                                   95
                                                                                                                                              solve(query);
58
       REP(i, m) {
                                                                 33
                                                                                                                                   96
                                                                                                                                              return ans:
59
           if(F(e[i].a)==F(e[i].b)) continue;
                                                                 34
                                                                        int lca(int a, int b) { return ca[a][b]; }
                                                                                                                                   97
          U(e[i].a, e[i].b);
                                                                 35
                                                                        int dist(int a, int b) {
60
                                                                                                                                   98
                                                                                                                                          vector<int> dist(vector<pii>& query) {
          r += e[i].c;
                                                                 36
                                                                            return dep[a] + dep[b] - 2 * dep[ca[a][b]];
61
                                                                                                                                   99
                                                                                                                                              solve(query);
62
                                                                 37
                                                                                                                                  100
                                                                                                                                              for (int i = 0; i < query.size(); i++) {</pre>
63
      return r;
                                                                 38
                                                                    };
                                                                                                                                                  auto& q = query[i];
                                                                                                                                  101
64
                                                                 39
                                                                                                                                                  ans[i] = dep[q.first] + dep[q.second] -
                                                                                                                                  102
   int main() {
65
                                                                    /** 最快的 LCA O(N+O) 且最省記憶體 O(N+O) 。但必須離線。**/
                                                                                                                                                           2 * dep[ans[i]];
                                                                                                                                  103
      int ts;
66
                                                                 41 #define x first // 加速
                                                                                                                                  104
       scanf("%d", &ts);
67
                                                                    #define y second
                                                                                                                                  105
                                                                                                                                              return ans;
68
       while (ts--) {
                                                                    class OfflineTarian {
                                                                 43
                                                                                                                                  106
69
          m = 0;
                                                                       private:
                                                                                                                                  107 };
          scanf("%d",&n);
70
                                                                        vector<int> par, anc, dep, ans, rank;
                                                                                                                                  108
          REP(i,n) {scanf("%d%d",&p[i].x,&p[i].y);p[i].id=s[i]= 46
71
                                                                        vector<vector<pii>>> qry;
                                                                                                                                  109 | /** 威達的 LCA , 時間普通 O(O*log(N)) , 記憶體需求也普通
               i;}
                                                                        // 出於安全考量你可以把 & 去掉
                                                                                                                                      * O(N*log(N)) 。 支援非離線。**/
72
           calc():
                                                                        vector<vector<int>>& edge;
                                                                 48
                                                                                                                                      class SparseTableTarjan {
73
          REP(i,n)p[i].y=-p[i].y;
                                                                                                                                  111
                                                                        int root, n;
                                                                 49
           calc();
                                                                                                                                  112
                                                                                                                                        private:
74
                                                                 50
          REP(i,n)swap(p[i].x,p[i].y);
                                                                                                                                          int maxlg;
75
                                                                                                                                  113
                                                                 51
                                                                        void merge(int a, int b) {
                                                                                                                                  114
                                                                                                                                          vector<vector<int>> anc;
76
          calc();
                                                                            a = parent(a), b = parent(b);
                                                                                                                                          vector<int> dep:
                                                                                                                                  115
77
          REP(i,n)p[i].x=-p[i].x;
                                                                 53
                                                                            if (rank[a] < rank[b]) swap(a, b);</pre>
78
           calc();
                                                                                                                                  116
                                                                 54
                                                                            par[b] = a;
                                                                                                                                          void dfs(int u, vector<vector<int>>& edge, int d) {
79
          printf("%lld\n",MST()*2);
                                                                                                                                  117
                                                                 55
                                                                            if (rank[a] == rank[b]) rank[a]++:
80
                                                                                                                                  118
                                                                                                                                              dep[u] = d;
                                                                 56
                                                                                                                                              for (int i = 1; i < maxlg; i++)</pre>
                                                                                                                                  119
81
       return 0;
                                                                        void dfs(int u, int d) {
                                                                 57
                                                                                                                                                  if (anc[u][i - 1] == -1) break;
                                                                                                                                  120
82
                                                                 58
                                                                            anc[parent(u)] = u, dep[u] = d;
                                                                                                                                                  else anc[u][i] = anc[anc[u][i - 1]][i - 1];
                                                                                                                                  121
                                                                 59
                                                                            for (int a : edge[u]) {
                                                                                                                                              for (int a : edge[u]) {
                                                                                                                                  122
                                                                                if (dep[a] != -1) continue;
                                                                 60
                                                                                                                                                  if (dep[a] != -1) continue;
                                                                                                                                  123
                                                                                dfs(a, d + 1);
                                                                 61
                                                                                                                                                  anc[a][0] = u;
                                                                                                                                  124
  4.6 LCA
                                                                 62
                                                                                merge(a, u);
                                                                                                                                  125
                                                                                                                                                  dfs(a, edge, d + 1);
                                                                 63
                                                                                anc[parent(u)] = u;
                                                                                                                                  126
                                                                 64
                                                                                                                                          }
                                                                                                                                  127
                                                                 65
                                                                            for (auto q : qry[u]) {
1 /** 所有 LCA 都是 0/1-based 安全的。建構式 edge 表示 adj
                                                                                                                                  128
                                                                                if (dep[a.first] != -1)
                                                                 66
   * 邊資訊。 只支援無向樹。這三個類別各有優缺點。**/
                                                                                                                                  129
                                                                                    ans[q.second] = anc[parent(q.first)];
                                                                 67
                                                                                                                                  130
                                                                                                                                          SparseTableTarjan(vector<vector<int>>& edge, int root) {
                                                                            }
                                                                 68
                                                                                                                                              int n = edge.size():
   /** 最快的 LCA O(N+O) ,但非常吃記憶體 O(N^2)。支援非離線。
                                                                                                                                  131
                                                                 69
                                                                                                                                              maxlg = ceil(log2(n));
                                                                                                                                  132
                                                                 70
                                                                        int parent(int x) {
  class SsadpTarjan {
                                                                                                                                  133
                                                                                                                                              anc.assign(n, vector<int>(maxlg, -1));
                                                                            if (par[x] == x) return x;
                                                                 71
                                                                                                                                  134
                                                                                                                                              dep.assign(n, -1);
     private:
                                                                 72
                                                                            return par[x] = parent(par[x]);
                                                                                                                                  135
                                                                                                                                              dfs(root, edge, 0);
      int n:
                                                                 73
                                                                                                                                  136
       vector<int> par, dep; vector<vector<int>> ca;
                                                                 74
                                                                        void solve(vector<pii>& query) {
                                                                                                                                          int lca(int a, int b) {
       int dfs(int u, vector<vector<int>>& edge, int d) {
                                                                                                                                  137
                                                                 75
                                                                            dep.assign(n, -1), rank.assign(n, 0);
                                                                                                                                              if (dep[a] > dep[b]) swap(a, b);
                                                                                                                                  138
          dep[u] = d;
                                                                            par.resize(n), anc.resize(n);
                                                                 76
                                                                                                                                              for (int k = 0; dep[b] - dep[a]; k++)
                                                                                                                                  139
           for (int a = 0; a < n; a++)</pre>
                                                                 77
                                                                            for (int i = 0; i < n; i++) anc[i] = par[i] = i;
                                                                                                                                  140
                                                                                                                                                  if (((dep[b] - dep[a]) >> k) & 1) b = anc[b][k];
12
               if (dep[a] != -1)
                                                                            ans.resize(query.size());
                   ca[a][u] = ca[u][a] = parent(a);
                                                                                                                                  141
13
                                                                            qry.resize(n);
                                                                                                                                  142
                                                                                                                                              if (a == b) return a:
           for (int a : edge[u]) {
14
                                                                 80
                                                                            for (int i = 0; i < query.size(); i++) {</pre>
                                                                                                                                  143
                                                                                                                                              for (int k = maxlg - 1; k >= 0; k--)
               if (dep[a] != -1) continue;
15
                                                                                auto& q = query[i];
                                                                 81
                                                                                                                                                  if (anc[a][k] != anc[b][k])
                                                                                                                                  144
16
               dfs(a, edge, d + 1);
                                                                                qry[q.first].emplace back(q.second, i);
                                                                 82
                                                                                                                                                      a = anc[a][k], b = anc[b][k];
                                                                                                                                  145
17
               par[a] = u;
                                                                 83
                                                                                qry[q.second].emplace back(q.first, i);
                                                                                                                                  146
                                                                                                                                              return anc[a][0];
18
          }
                                                                 84
                                                                                                                                  147
19
                                                                            dfs(root, 0);
                                                                 85
                                                                                                                                          int dist(int a, int b) {
20
       int parent(int x) {
                                                                                                                                  148
                                                                 86
                                                                        }
                                                                                                                                  149
                                                                                                                                              return dep[a] + dep[b] - 2 * dep[lca(a, b)];
```

150

151 };

if (par[x] == x) return x;

return par[x] = parent(par[x]);

87

public:

21

22

4.7 Tarjan

```
1 割點
2| 點 u 為割點 if and only if 滿足 1. or 2.
3 1. u 爲樹根,且 u 有多於一個子樹。
4 2. u 不爲樹根,且滿足存在 (u,v) 爲樹枝邊 (或稱父子邊,即 u 爲
        v 在搜索樹中的父親),使得 DFN(u) <= Low(v)。
   一條無向邊 (u,v) 是橋 if and only if (u,v) 爲樹枝邊,且滿足
       DFN(u) < Low(v) °
8 // 0 base
  struct TarjanSCC{
      static const int MAXN = 1000006;
      int n, dfn[MAXN], low[MAXN], scc[MAXN], scn, count;
      vector<int> G[MAXN];
13
      stack<int> stk;
      bool ins[MAXN];
15
      void tarjan(int u) {
          dfn[u] = low[u] = ++count;
16
17
          stk.push(u);
18
          ins[u] = true;
          for(auto v:G[u]) {
19
              if(!dfn[v]) {
20
                  tarjan(v);
21
                  low[u] = min(low[u], low[v]);
22
              } else if(ins[v]) {
23
                  low[u] = min(low[u], dfn[v]);
24
25
26
27
          if(dfn[u] == low[u]) {
28
              int v;
29
              do {
              v = stk.top(); stk.pop();
30
31
              scc[v] = scn;
32
              ins[v] = false;
              } while(v != u);
33
34
              scn++:
35
36
      void getSCC(){
37
          memset(dfn,0,sizeof(dfn));
          memset(low,0,sizeof(low));
39
          memset(ins,0,sizeof(ins));
40
          memset(scc,0,sizeof(scc));
41
42
          count = scn = 0;
43
          for(int i = 0 ; i < n ; i++ )</pre>
              if(!dfn[i]) tarjan(i);
44
45
46 } SCC;
```

4.8 BCC edge

```
2 任意兩點間至少有兩條不重疊的路徑連接,找法:
3 1. 標記出所有的橋
4 2. 對全圖進行 DFS,不走橋,每一次 DFS 就是一個新的邊雙連通
5 // from BCW
6 struct BccEdge {
  static const int MXN = 100005;
```

```
struct Edge { int v,eid; };
     int n,m,step,par[MXN],dfn[MXN],low[MXN];
     vector<Edge> E[MXN];
    DisjointSet djs;
    void init(int n) {
      n = n; m = 0;
      for (int i=0; i<n; i++) E[i].clear();</pre>
      djs.init(n);
     void add_edge(int u, int v) {
      E[u].PB({v, m});
      E[v].PB({u, m});
     void DFS(int u, int f, int f eid) {
      par[u] = f;
       dfn[u] = low[u] = step++;
       for (auto it:E[u]) {
        if (it.eid == f_eid) continue;
         int v = it.v:
         if (dfn[v] == -1) {
          DFS(v, u, it.eid);
          low[u] = min(low[u], low[v]);
        } else {
          low[u] = min(low[u], dfn[v]);
      }
    void solve() {
      step = 0;
      memset(dfn, -1, sizeof(int)*n);
       for (int i=0; i<n; i++) {
       if (dfn[i] == -1) DFS(i, i, -1);
      djs.init(n);
       for (int i=0; i<n; i++) {
        if (low[i] < dfn[i]) djs.uni(i, par[i]);</pre>
47 } graph;
```

4.9 最小平均環

11

15

16

17

20

21

22

23

26

27

28

30

31

32

33

34

35

36

37

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39

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42

43

44

45

46

```
1 #include < cfloat > //for DBL_MAX
int dp[MAXN][MAXN]; // 1-base,0(NM)
3 vector<tuple<int,int,int>> edge;
4 double mmc(int n){ //allow negative weight
      const int INF = 0x3f3f3f3f;
       for(int t=0; t<n; ++t){</pre>
           memset(dp[t+1],0x3f,sizeof(dp[t+1]));
           for(const auto &e:edge) {
               int u, v, w; tie(u,v,w) = e;
               dp[t+1][v] = min(dp[t+1][v], dp[t][u]+w);
10
11
          }
12
       double res = DBL_MAX;
       for(int u=1; u<=n; ++u) {</pre>
           if(dp[n][u]==INF) continue;
16
           double val = -DBL MAX;
           for(int t=0;t<n;++t)</pre>
               val = max(val,(dp[n][u]-dp[t][u])*1.0/(n-t));
           res = min(res,val);
19
      } return res;
```

21 }

4.10 2-SAT

```
_{1} const int MAXN = 2020;
2 struct TwoSAT{
       static const int MAXv = 2*MAXN;
       vector<int> GO[MAXv], BK[MAXv], stk;
       bool vis[MAXv];
       int SC[MAXv];
       void imply(int u,int v){ // u imply v
           GO[u].push back(v);
           BK[v].push back(u);
11
       int dfs(int u,vector<int>*G,int sc){
           vis[u]=1, SC[u]=sc;
13
           for (int v:G[u])if (!vis[v])
14
               dfs(v,G,sc);
15
           if (G==GO) stk.push back(u);
16
17
       int scc(int n=MAXv){
           memset(vis,0,sizeof(vis));
18
           for (int i=0; i<n; i++)</pre>
19
               if (!vis[i]) dfs(i,G0,-1);
20
           memset(vis,0,sizeof(vis));
21
           int sc=0;
           while (!stk.empty()){
23
24
               if (!vis[stk.back()])
                   dfs(stk.back(),BK,sc++);
26
               stk.pop_back();
27
28
29
   } SAT;
  int main(){
       SAT.scc(2*n);
       bool ok = 1;
32
33
       for (int i=0; i<n; i++){</pre>
34
           if (SAT.SC[2*i]==SAT.SC[2*i+1]) ok = 0;
35
       if (ok) {
36
37
           for (int i=0; i<n; i++)</pre>
               if (SAT.SC[2*i]>SAT.SC[2*i+1])
39
                   cout << i << endl;
40
       else puts("NO");
41
42
43 void warshall(){
       bitset<2003> d[2003];
45
       for (int k=0; k<n; k++)</pre>
           for (int i=0; i<n; i++)</pre>
46
               if (d[i][k]) d[i] |= d[k];
47
```

4.11 牛成樹數量

```
1 // D : degree-matrix
2 // A : adjacent-matrix
3 // 無向圖
   // (u,v)
```

while ($ll\ f = aug(s, 9e18, d)$) ret += f;

```
// A[u][v]++, A[v][u]++
   // D[u][u]++, D[v][v]++
                                                        46
   // G = D-A
                                                        47
   // abs(det(G去掉i-col和i-row))
                                                        48
                                                        49
   // 生成樹的數量
                                                        50
// 有向圖
                                                        51
   // A[u][v]++
                                                        52
   // D[v][v]++ (in-deg)
                                                        53
   // 以i為root的樹形圖數量
                                                        54 };
   // 所有節點都能到達root
```

5.2 Min Cost Max Flow

11 max_flow(int s, int d) {

while (mklv(s, d)) {

ve.assign(n, 0);

11 ret = 0;

return ret;

5.1 Dinic

Flow Matching

```
1 // 一般來說複雜度遠低於 O(EV^2) , 二分圖約 O(E * sqrt(v)) 。
2 // 0/1-based 都安全。
3 class Dinic {
      struct edge {
          int d, r; 11 c;
          edge(int d, ll c, int r) : d(d), c(c), r(r){};
     private:
      vector<vector<edge>> adj; vector<int> lv, ve; int n;
      bool mklv(int s, int d) {
          lv.assign(n, -1); lv[s] = 0;
12
          queue<int> q; q.push(s);
          while (!q.empty()) {
13
              int v = q.front(); q.pop();
              for (auto& e : adj[v]) {
                  if (e.c == 0 | | lv[e.d] != -1) continue;
                  lv[e.d] = lv[v] + 1, q.push(e.d);
              }
19
20
          return lv[d] > 0;
      11 aug(int v, 11 f, int d) {
          if (v == d) return f;
          for (; ve[v] < adj[v].size(); ve[v]++) {</pre>
25
              auto& e = adi[v][ve[v]];
              if (lv[e.d] != lv[v] + 1 || !e.c) continue;
              11 \text{ sent} = aug(e.d, min(f, e.c), d);
              if (sent > 0) {
                  e.c -= sent, adj[e.d][e.r].c += sent;
33
          return 0;
34
     public:
35
      // 建立空圖, n 是節點 (包含 source, sink) 數量
      Dinic(int n) : n(n + 1) { clear(); }
      // 清空整個圖,這需要重複使用 dinic 時 (如二分搜) 很方便
38
                                                               44
39
      void clear() { adj.assign(n, vector<edge>()); }
      // 加有向邊 src->dst , cap 是容量
      void add edge(int src, int dst, ll cap) {
          edge ss(dst, cap, adj[dst].size());
          edge dd(src, 0, adj[src].size());
43
44
          adj[src].push back(ss), adj[dst].push back(dd);
```

```
1 /** Min cost max flow 。 0/1-based 都安全。 **/
  class MCMF {
     private:
      struct edge { int to, r; ll rest, c; };
      int n; 11 f = 0, c = 0;
      vector<vector<edge>> g;
       vector<int> pre, prel;
      bool run(int s, int t) {
           vector<ll> dis(n, inf); vector<bool> vis(n);
10
           dis[s] = 0; queue<int> q; q.push(s);
           while (q.size()) {
               int u = q.front(); q.pop(); vis[u] = 0;
               for (int i = 0; i < g[u].size(); i++) {</pre>
13
                   int v = g[u][i].to; ll w = g[u][i].c;
                   if (g[u][i].rest <= 0 ||
                       dis[v] \leftarrow dis[u] + w
16
                       continue;
17
18
                   pre[v] = u, prel[v] = i;
                   dis[v] = dis[u] + w;
19
                   if (!vis[v]) vis[v] = 1, q.push(v);
20
21
22
          if (dis[t] == inf) return 0;
23
          11 tf = inf;
24
           for (int v = t, u, 1; v != s; v = u) {
25
               u = pre[v], 1 = prel[v];
               tf = min(tf, g[u][1].rest);
27
           for (int v = t, u, 1; v != s; v = u) {
               u = pre[v], 1 = prel[v], g[u][1].rest -= tf;
31
               g[v][g[u][1].r].rest += tf;
           c += tf * dis[t], f += tf;
33
34
          return 1;
35
36
     public:
37
      // 建立空圖, n 是節點數量 (包含 source 和 sink)
      MCMF(int n)
38
39
           : n(n + 1), g(n + 1), pre(n + 1), prel(n + 1) {}
      // 加有向邊 u->v ,cap 容量 cost 成本
40
       void add_edge(int u, int v, ll cap, ll cost) {
41
           g[u].push_back({v, (int)g[v].size(), cap, cost});
42
           g[v].push_back({u, (int)g[u].size() - 1, 0, -cost});
43
45
      pair<11, 11> query(int src, int sink) {
           while (run(src, sink));
46
          return {f, c}; //{min cost, max flow}
47
48
49 };
```

5.3 Ford Fulkerson

```
1 const int maxn = 1e5 + 10, INF = 1e9;
const long long INF64 = 1e18;
3 struct edge{ int to, cap, rev; };
 4 vector<edge> G[maxn];
 5 int n, m, s, t, a, b, c;
 6 bool vis[maxn];
 7 int dfs(int v, int t, int f) {
       cout << v << ' ' << t << ' ' << f << '\n';
       if (v == t) return f;
       vis[v] = true;
       for (edge &e: G[v]) {
           if (!vis[e.to] && e.cap > 0) {
               int d = dfs(e.to, t, min(f, e.cap));
               if (d > 0) {
                   e.cap -= d, G[e.to][e.rev].cap += d;
                   return d;
16
17
           }
18
19
20
       return 0:
21
   int ford fulkerson(int s, int t) {
23
       int flow = 0, f:
24
       for (int i = 0; i < n; i++) {</pre>
           cout << i << " : ";
25
           for (edge e: G[i])
26
               cout << '(' << e.to << ',' << e.cap << ')' << ' '
27
           cout << '\n';
28
29
      }
30
       do {
           memset(vis, false, sizeof(vis));
31
32
           f = dfs(s, t, INF);
33
           for (int i = 0; i < n; i++) {</pre>
               cout << i << " : ";
               for (edge e: G[i])
                   cout << '(' << e.to << ',' << e.cap << ')' <<
37
               cout << '\n';
38
           cout << f << '\n';
           flow += f;
       } while (f > 0);
       return flow:
43
  void init(int n) {
       for (int i = 0; i < n; i++) G[i].clear();</pre>
46 }
47 int main() {
      cin >> n >> m >> s >> t;
48
       init(n);
49
       while (m--) {
           cin >> a >> b >> c;
           G[a].push_back((edge){b, c, (int)G[b].size()});
           G[b].push_back((edge){a, 0, (int)G[a].size() - 1});
54
       cout << ford_fulkerson(s, t) << '\n';</pre>
55
       return 0;
57 }
```

5.4 KM

```
1 /** 二分圖最大權值匹配 KM 演算法,複雜度 O(n^3)*/
2 #define inf 5e18
3 class KM {
     private:
      const vector<vector<11>>& e:
      vector<11> cx, cy, wx, wy;
      vector<bool> vx, vy;
      11 z:
10
11
      bool dfs(int u) {
12
          vx[u] = 1;
          for (int v = 0; v < yy; v++) {
   if (vy[v] || e[u][v] == inf) continue;</pre>
13
14
              11 t = wx[u] + wy[v] - e[u][v];
15
              if (t == 0) {
                  vy[v] = 1;
                  if (cy[v] == -1 || dfs(cy[v])) {
                       cx[u] = v, cy[v] = u;
                       return 1;
20
21
              } else if (t > 0)
22
23
                  z = min(z, t);
24
25
          return 0;
26
27
     public:
      // 問最大匹配權重。
       11 max weight() {
          for (int i = 0; i < xx; i++)
               for (int j = 0; j < yy; j++) {
32
                   if (e[i][j] == inf) continue;
33
                  wx[i] = max(wx[i], e[i][j]);
          for (int i = 0; i < xx; i++) {
                  z = \inf, vx.assign(xx, 0), vy.assign(yy, 0);
                  if (dfs(i)) break;
                  for (int j = 0; j < xx; j++)
                       if (vx[j]) wx[j] -= z;
                   for (int j = 0; j < yy; j++)
                       if (vy[j]) wy[j] += z;
              }
          11 ans = 0:
          for (int i = 0; i < xx; i++)
              if (cx[i] != -1) ans += e[i][cx[i]];
          return ans:
       // 給他 n * m 的權重表 (n <= m),求最大完全匹配權重,權重
       // 是負數。注意 n > m 會導致無窮迴圈。
       KM(vector<vector<ll>>& e) : e(e) {
          xx = e.size(), yy = e[0].size(); // xx 要 <= yy !!
54
          cx.assign(xx, -1), cy.assign(yy, -1);
          wx.assign(xx, 0), wy.assign(yy, 0);
55
57 };
```

5.5 Hopcroft Karp

```
1 int n, m, vis[maxn], level[maxn], pr[maxn], pr2[maxn];
  vector<int> edge[maxn]; // for Left
  bool dfs(int u) {
       vis[u] = true;
       for (vector<int>::iterator it = edge[u].begin();
            it != edge[u].end(); ++it) {
           int v = pr2[*it];
           if (v == -1 ||
               (!vis[v] && level[u] < level[v] && dfs(v))) {
               pr[u] = *it, pr2[*it] = u;
               return true;
11
12
       return false;
15
   int hopcroftKarp() {
16
       memset(pr, -1, sizeof(pr));
       memset(pr2, -1, sizeof(pr2));
       for (int match = 0;;) {
           queue<int> 0;
           for (int i = 1; i <= n; ++i) {
21
               if (pr[i] == -1) {
                   level[i] = 0;
24
                   Q.push(i);
               } else
26
                   level[i] = -1;
27
           while (!O.empty()) {
28
               int u = 0.front();
29
30
31
               for (vector<int>::iterator it = edge[u].begin();
32
                    it != edge[u].end(); ++it) {
                   int v = pr2[*it]:
33
                   if (v != -1 && level[v] < 0) {</pre>
34
                       level[v] = level[u] + 1;
35
                       Q.push(v);
36
37
                   }
38
           for (int i = 1; i \le n; ++i) vis[i] = false;
           int d = 0:
41
           for (int i = 1; i <= n; ++i)
42
               if (pr[i] == -1 && dfs(i)) ++d:
43
           if (d == 0) return match;
44
45
           match += d;
46
47
```

5.6 SW-MinCut

```
11
           edge[u][v] += w; edge[v][u] += w;
12
       void search(int &s, int &t) {
13
           FZ(vst); FZ(wei);
14
15
           s = t = -1;
           while (true){
16
17
               int mx=-1. cur=0:
                for (int i=0; i<n; i++)
18
                    if (!del[i] && !vst[i] && mx<wei[i])</pre>
19
20
                        cur = i, mx = wei[i];
                if (mx == -1) break;
21
                vst[cur] = 1:
22
23
                s = t; t = cur;
                for (int i=0; i<n; i++)</pre>
24
25
                    if (!vst[i] && !del[i]) wei[i] += edge[cur][i
                         1;
26
27
       int solve() {
28
            int res = 2147483647:
30
            for (int i=0, x, y; i<n-1; i++) {
                search(x,y);
31
32
                res = min(res,wei[y]);
33
                del[y] = 1;
34
                for (int j=0; j<n; j++)</pre>
35
                    edge[x][j] = (edge[j][x] += edge[y][j]);
36
37
           return res:
38
39 } graph;
```

5.7 Stable Marriage

2 1. N位男士各自向自己最喜愛的女士求婚。

1 / / 演算法筆記

19

21

22

```
      3 | 2. N位女士各自從自己的求婚者中,挑最喜愛的那位男士訂婚,但是

      1
      往後可背約。

      4 | 沒有求婚者的女士,就只好等等。

      5 | 3. 失敗的男士們,只好各自向自己次喜愛的女士求婚。
```

6 4. N位女士各自從自己的求婚者中,挑最喜歡的那位男士訂婚,但是 往後可背約。

已訂婚卻有更喜愛的男士求婚的女士,就毀約,改為與此男士訂 婚。

灯。 8 | 沒有求婚者的女士,就只好再等等。 9 | 5. 重複3. 4.直到形成N對伴侶為止。

while (此考生未分發) {
 指標移到下一志願;
 if (已經沒有志願 or 超出志願總數) break;
 計算該考生在該科系加權後的總分;

計算該考生在該科系加權後的總分; if (不符合科系需求) continue; if (目前科系有餘額) {

if (fastpow(y, (p - 1 / 2), p) == p - 1) return -1;

if (fastpow(q, (p - 1) / 2, p) == p - 1)

if (o == fastpow(2, m, p)) break;

g = fastpow(g, fastpow(2, e - m, p), p);

x = x * fastpow(g, fastpow(2, e - m - 1), p) % p;

return ret;

int e = 0;

int q = 2;

while (1)

while (1) {

int m:

6.4 外星模運算

18

19

20

21

23

24

25

26

27

28

29

30

31

32

33

34

35 36

37

11 s = p - 1:

else a++:

8 // 把 fastpow 也抄過來,會用到。

if (__gcd(y, p) != 1) return -1;

while (!(s & 1)) s >>= 1, e++;

11 x = fastpow(y, (s + 1) / 2, p);

for (m = 0; m < e; m++) {

int o = order(p, b);

if (o == -1) return -1;

11 b = fastpow(y, s, p);

if (m == 0) return x;

b = b * g % p;

11 g = fastpow(q, s, p);

```
依加權後分數高低順序將考生id加入科系錄取名單中;
25
           break;
26
        if (目前科系已額滿) {
27
                                                9 // 問 (x^2 = y) mod p 的解。回傳 -1 表示 x 無解。
           if ( 此考生成績比最低分數還高 ) {
                                                10 ll dsqrt(ll y, ll p) {
              依加權後分數高低順序將考生id加入科系錄取名單; 11
             Q.push(被踢出的考生);
                                                13
                                                14
32
                                                15
33
                                                16
                                                17
```

Math

快速羃

```
1 | const int P = 1e9 + 7;
2 #define 11 long long
3 11 fpow(int a, int b) {
     ll ret = 1;
     while (b) {
         if (b & 1)
             ret = ret * a % P;
         a = a * a % P;
      return ret;
```

模逆元

```
1 // 解 (ax == 1) mod p 。p 必須是質數,a 是正整數。
2 11 modinv(ll a, ll p) {
      if (p == 1) return 0;
      11 pp = p, y = 0, x = 1;
      while (a > 1) {
         11 q = a / p, t = p;
          p = a \% p, a = t, t = y, y = x - q * y, x = t;
      if (x < 0) x += pp;
      return x;
12 // 解 (ax == b) mod p 。p 必須是質數, a 和 b 是正整數。
13 ll modiny(ll a, ll b, ll p) {
      11 ret = modinv(a, p);
14
      return ret * b % p;
15
```

離散根號

```
int order(ll b, ll p) {
     if (__gcd(b, p) != 1) return -1;
     int ret = 2;
      while (++ret)
         if (fastpow(b, ret, p) == 1) break;
```

if (b == 1) return x; e = m:

```
1 //a[0]^(a[1]^a[2]^...)
2 #define maxn 1000000
3 int euler[maxn+5];
4 bool is prime[maxn+5];
  void init_euler(){
    is prime[1] = 1: //一不是質數
     for(int i=1; i<=maxn; i++) euler[i]=i;</pre>
     for(int i=2: i<=maxn: i++) {</pre>
      if(!is_prime[i]) { //是質數
        euler[i]--;
         for(int j=i<<1; j<=maxn; j+=i) {</pre>
          is prime[j]=1;
13
           euler[j] = euler[j]/i*(i-1);
15
16
17
  LL pow(LL a, LL b, LL mod) { //a^b%mod
   LL ans=1;
    for(; b; a=a*a%mod, b>>=1)
    if(b&1) ans = ans*a%mod;
   return ans;
24 bool isless(LL *a, int n, int k) {
    if(*a==1)return k>1;
    if(--n==0)return *a<k;</pre>
```

```
int next=0:
    for(LL b=1;b<k;++next)</pre>
     b *= *a;
    return isless(a+1, n, next);
31
  LL high pow(LL *a, int n, LL mod){
    if(*a==1||--n==0)return *a%mod;
    int k = 0, r = euler[mod];
    for(LL tma=1;tma!=pow(*a,k+r,mod);++k)
     tma = tma*(*a)%mod;
    if(isless(a+1,n,k))return pow(*a,high_pow(a+1,n,k),mod);
    int tmd = high pow(a+1,n,r), t = (tmd-k+r)%r;
    return pow(*a,k+t,mod);
41 LL a[1000005]; int t, mod;
42 int main(){
    init euler():
    scanf("%d", &t);
    #define n 4
45
    while(t--){
     for(int i=0;i<n;++i)scanf("%lld", &a[i]);</pre>
47
      scanf("%d", &mod);
49
     printf("%11d\n", high pow(a,n,mod));
50
51
    return 0;
```

6.5 SG

```
1 | Anti Nim (取走最後一個石子者敗):
2 先手必勝 if and only if
3 1. 「所有」堆的石子數都為 1 目遊戲的 SG 值為 0。
4 2. 「有些」堆的石子數大於 1 且遊戲的 SG 值不為 0。
5 -----
6 | Anti-SG (決策集合為空的遊戲者贏):
7 定義 SG 值為 0 時,遊戲結束,
s 則先手必勝 if and only if
9 1. 遊戲中沒有單一遊戲的 SG 函數大於 1 且遊戲的 SG 函數為 0。
10 2. 遊戲中某個單一遊戲的 SG 函數大於 1 且遊戲的 SG 函數不為 0
12 Sprague-Grundy:
13 1. 雙人、回合制
14 2. 資訊完全公開
15 3. 無隨機因素
16 4. 可在有限步內結束
17 5. 沒有和局
18 6. 雙方可採取的行動相同
20 SG(S) 的值為 0:後手(P)必勝
21 不為 0: 先手(N)必勝
22 int mex(set S) {
// find the min number >= 0 that not in the S
24 // e.g. S = {0, 1, 3, 4} mex(S) = 2
25 }
26 state = []
27 int SG(A) {
if (A not in state) {
   S = sub states(A)
     if( len(S) > 1 ) state[A] = reduce(operator.xor, [SG(B)
        for B in S])
```

```
else state[A] = mex(set(SG(B) for B in next states(A)))
                                                                                    m[i].swap(m[j]); sign = !sign;
32
    } return state[A]
                                                                 57
                                                                                for (int j = 0; j < r; ++j) {
                                                                 58
                                                                 59
                                                                                    if (i == j) continue;
                                                                                    lazy[j] = lazy[j] * m[i][i];
                                                                 60
                                                                 61
                                                                                    11 mx = m[j][i];
  6.6 Matrix
                                                                 62
                                                                                    for (int k = 0; k < c; ++k)
                                                                 63
                                                                                        m[j][k] =
                                                                 64
                                                                                            m[j][k] * m[i][i] - m[i][k] * mx;
                                                                 65
1 struct Matrix {
                                                                 66
      int r, c;
                                                                            11 det = sign ? -1 : 1;
                                                                 67
       vector<vector<ll>> m;
                                                                            for (int i = 0; i < r; ++i) {
      Matrix(int r, int c): r(r), c(c), m(r, vector<ll>(c)) {}
                                                                                det = det * m[i][i] / lazy[i];
      vector<ll> &operator[](int i) { return m[i]; }
                                                                 70
                                                                                for (auto &j : m[i]) j /= lazy[i];
      Matrix operator +(const Matrix &a) {
                                                                 71
          Matrix rev(r, c);
                                                                 72
                                                                            return det;
           for (int i = 0; i < r; ++i)
                                                                 73
               for (int j = 0; j < c; ++j)
                                                                 74 };
                  rev[i][j] = m[i][j] + a.m[i][j];
13
      Matrix operator -(const Matrix &a) {
                                                                    6.7 Karatsuba
14
           Matrix rev(r, c);
           for (int i = 0; i < r; ++i)
               for (int j = 0; j < c; ++j)</pre>
                                                                  1 // N is power of 2
                  rev[i][j] = m[i][j] - a.m[i][j];
                                                                    template<typename Iter>
18
          return rev:
                                                                    void DC(int N, Iter tmp, Iter A, Iter B, Iter res){
19
                                                                        fill(res,res+2*N,0);
20
       Matrix operator *(const Matrix &a) {
                                                                        if (N<=32){
           Matrix rev(r, a.c);
21
                                                                            for (int i=0; i<N; i++)</pre>
22
           Matrix tmp(a.c, a.r);
                                                                                for (int j=0; j<N; j++)</pre>
23
           for (int i = 0; i < a.r; ++i)</pre>
                                                                                    res[i+j] += A[i]*B[j];
24
               for (int j = 0; j < a.c; ++j)
                                                                            return:
                  tmp[j][i] = a.m[i][j];
           for (int i = 0; i < r; ++i)</pre>
                                                                 10
                                                                        int n = N/2;
                                                                 11
               for (int j = 0; j < a.c; ++j)
                                                                        auto a = A+n, b = A;
                                                                 12
                   for (int k = 0; k < c; ++k)
                                                                        auto c = B+n, d = B;
                                                                 13
                       rev.m[i][j] += m[i][k] * tmp[j][k];
                                                                        DC(n,tmp+N,a,c,res+2*N);
                                                                 14
          return rev;
30
                                                                        for (int i=0; i<N; i++){
                                                                 15
31
                                                                            res[i+N] += res[2*N+i];
                                                                 16
      // 回傳反矩陣。注意這是 const 方法所以原矩陣不受影響。
                                                                            res[i+n] -= res[2*N+i];
                                                                 17
      Matrix inverse() const {
                                                                 18
34
           Matrix t(r, r + c);
                                                                        DC(n,tmp+N,b,d,res+2*N);
                                                                 19
           for (int y = 0; y < r; y++) {
                                                                        for (int i=0; i<N; i++){</pre>
                                                                 20
               t.m[y][c + y] = 1;
                                                                            res[i] += res[2*N+i];
               for (int x = 0; x < c; x++) t.m[y][x] = m[y][x];
                                                                            res[i+n] -= res[2*N+i];
          if (!t.gauss()) return Matrix(0, 0);
                                                                 24
                                                                        auto x = tmp;
          Matrix ret(c, r);
                                                                        auto y = tmp+n;
           for (int y = 0; y < r; y++)
                                                                        for (int i=0; i<n; i++) x[i] = a[i]+b[i];</pre>
               for (int x = 0; x < c; x++)
                                                                        for (int i=0; i<n; i++) y[i] = c[i]+d[i];</pre>
                  ret[y][x] = t.m[y][c + x] / t.m[y][y];
                                                                        DC(n,tmp+N,x,y,res+2*N);
44
          return ret:
                                                                        for (int i=0; i<N; i++)</pre>
45
                                                                            res[i+n] += res[2*N+i];
       // 做高斯消去 (最高次係數應置於最左,常數應置於最右) 並回
46
                                                                 32 // DC(1<<16,tmp.begin(),A.begin(),B.begin(),res.begin());</pre>
       // 行列式值。複雜度 O(n^3)。如果不是方陣,回傳值無意義
       11 gauss() {
          vector<ll> lazy(r, 1);
                                                                    6.8 Euler Function
50
          bool sign = false;
           for (int i = 0; i < r; ++i) {
51
               if (m[i][i] == 0) {
                                                                  1 // 查詢 phi(x) 亦即比 x 小且與 x 互質的數的數量。
53
                   int j = i + 1;
                   while (j < r \&\& !m[j][i]) j++;
                                                                    int phi(int x) {
54
```

int r = x;

if (j == r) continue;

```
for (int p = 2; p * p <= x; p++) {
           if (x % p == 0) {
               while (x \% p == 0) x /= p;
               r -= r / p;
      if (x > 1) r -= r / x;
11
      return r;
12 }
13 | // 查詢所有 phi(x) ,且 x in [0, n) 。注意右開區間,回傳陣
14 | vector<int> phi in(int n) {
      vector<bool> p(n, 1); vector<int> r(n);
15
      p[0] = p[1] = 0;
       for (int i = 0; i < n; i++) r[i] = i;
      for (int i = 2; i < n; i++) {
           if (!p[i]) continue;
19
20
          r[i]--;
           for (int j = i * 2; j < n; j += i)</pre>
21
              p[j] = 0, r[j] = r[j] / i * (i - 1);
22
23
24
      r[1] = 0;
25
      return r;
```

6.9 Miller Rabin

```
1 typedef long long LL;
2 inline LL mul(LL a, LL b, LL m){//a*b%m
       return (a%m)*(b%m)%m;
   template<typename T> bool isprime(T n, int num=3) { //num =
       3,7
       int sprp[3] = {2,7,61}; //int範圍可解
       //int llsprp[7] =
            {2,325,9375,28178,450775,9780504,1795265022}; //至少
            unsigned long long範圍
       if(n==2) return true;
       if(n<2 || n%2==0) return false;</pre>
10
       //n-1 = u * 2^t
11
       int t = 0; T u = n-1;
       while(u%2==0) u >>= 1, t++;
       for(int i=0; i<num; i++) {</pre>
           T a = sprp[i]%n;
           if(a==0 || a==1 || a==n-1) continue;
16
17
           T x = fpow(a,u,n);
18
           if(x==1 || x==n-1) continue;
           for(int j=1; j<t; j++) {</pre>
19
               x = mul(x,x,n);
20
               if(x==1) return false;
21
               if(x==n-1) break;
22
23
^{24}
           if(x!=n-1) return false;
25
       } return true;
```

6.10 質因數分解

```
1 typedef int128 11;
  vector<11>vv;
   /* fastoi here */
   ll abs(ll x){
       return (x>0?x:-x):
   11 func(ll t,ll c,ll x) {
    return (t*t+c)%x;
11
   11 Pollard Rho(11 x) {
         11 t = 0;
13
14
         11 c = rand() % (x - 1) + 1:
         for (int i = 1; i < 1145; ++i) t = func(t, c, x);
15
16
         11 s = t;
         int step = 0, goal = 1;
17
         ll val = 1;
18
         for (goal = 1;; goal <<= 1, s = t, val = 1) {</pre>
19
               for (step = 1; step <= goal; ++step) {</pre>
20
                     t = func(t, c, x);
21
                     val = val * abs(t - s) % x:
22
23
                     if (!val) return x;
                     if (step % 127 == 0)
24
25
                           11 d = \_gcd(val, x);
                           if (d > 1) return d;
26
27
28
               11 d = \_gcd(val, x);
29
30
               if (d > 1) return d;
31
32
   void prefactor(ll &n, vector<ll> &v) {
       ll prime[12] = {2,3,5,7,11,13,17,19,23,29,31,37};
     for(int i=0;i<12;++i) {</pre>
35
       while(n%prime[i]==0) {
36
         v.push_back(prime[i]);
37
38
         n/=prime[i];
39
40
    }
41
   void comfactor(const 11 &n, vector<11> &v) {
    if(isPrime(n,15)) { // MillerRabin
       v.push back(n);
44
45
       return;
46
    11 d = Pollard Rho(n);
47
48
    comfactor(d,v);
     comfactor(n/d,v);
50
   void Factor(const 11 &x, vector<11> &v) {
    11 n = x;
    if(n==1) { puts("Factor 1"); return; }
    prefactor(n,v);
    if(n==1) return;
    comfactor(n,v);
    sort(v.begin(),v.end());
   void AllFactor(const 11 &n,vector<11> &v) {
    vector<ll> tmp:
    Factor(n,tmp);
    v.clear();
    v.push back(1);
    ll len;
    ll now=1;
    11 lentmp = tmp.size();
```

```
for(int i=0;i<lentmp;++i) {</pre>
       if(i==0 || tmp[i]!=tmp[i-1]) {
69
         len = v.size();
70
         now = 1;
71
72
       now*=tmp[i];
73
       for(int i=0:i<len:++i)</pre>
74
         v.push_back(v[j]*now);
75
76
77
   void prime factorization(){
         srand(time(NULL));
78
         11 n = read();
79
80
         AllFactor(n.vv):
81
          sort(vv.begin(), vv.end());
82
         for(auto i:vv){
83
              print(i); putchar(' ');
84
```

6.11 質數

```
1 | 12721
              13331
                          14341
                                       75577
  123457
              222557
                           556679
                                       880301
  999983
              1e6+99
                          1e9+9
                                       2e9+99
  1e12+39
              1e15+37
                          1e9+7
                                       1e7+19
  1097774749
              1076767633 100102021
  999997771
              1001010013
                          1000512343
  987654361
              999991231
                          999888733
  98789101
              987777733
                          999991921
  1010101333 1010102101
10 2305843009213693951
                           4611686018427387847
11 9223372036854775783
                          18446744073709551557
```

6.12 實根

```
1 // an*x^n + ... + a1x + a0 = 0;
  int sign(double x){
   return x < -eps ? -1 : x > eps;
  double get(const vector<double>&coef, double x){
    double e = 1, s = 0;
    for(auto i : coef) s += i*e, e *= x;
    return s;
  double find(const vector<double>&coef, int n, double lo,
       double hi){
     double sign_lo, sign_hi;
    if( !(sign lo = sign(get(coef,lo))) ) return lo;
    if( !(sign_hi = sign(get(coef,hi))) ) return hi;
    if(sign lo * sign hi > 0) return INF;
     for(int stp = 0; stp < 100 && hi - lo > eps; ++stp){
      double m = (lo+hi)/2.0;
       int sign mid = sign(get(coef,m));
      if(!sign mid) return m;
19
      if(sign lo*sign mid < 0) hi = m;</pre>
      else lo = m;
^{21}
    return (lo+hi)/2.0;
22
```

```
24 | vector<double> cal(vector<double>coef, int n){
     vector<double>res;
26
     if(n == 1){
       if(sign(coef[1])) res.pb(-coef[0]/coef[1]);
      return res;
28
29
30
     vector<double>dcoef(n);
     for(int i = 0; i < n; ++i) dcoef[i] = coef[i+1]*(i+1);</pre>
     vector<double>droot = cal(dcoef, n-1);
     droot.insert(droot.begin(), -INF);
34
     droot.pb(INF);
     for(int i = 0: i+1 < droot.size(): ++i){</pre>
35
       double tmp = find(coef, n, droot[i], droot[i+1]);
36
37
      if(tmp < INF) res.pb(tmp);</pre>
38
39
    return res;
40
  int main () {
41
42
    vector<double>ve;
    vector<double>ans = cal(ve, n);
    // 視情況把答案 +eps, 避免 -0
45 }
```

6.13 FFT

```
1 template<typename T, typename VT=vector<complex<T> > >
   struct FFT{
       const T pi;
       FFT(const T pi=acos((T)-1)):pi(pi){}
       unsigned bit reverse(unsigned a,int len){
           a=((a\&0x55555555U)<<1)|((a\&0xAAAAAAAAU)>>1);
           a=((a\&0x33333333U)<<2)|((a\&0xCCCCCCCU)>>2);
           a=((a&0x0F0F0F0FU)<<4)|((a&0xF0F0F0F0U)>>4);
           a=((a\&0x00FF00FFU)<<8)|((a\&0xFF00FF00U)>>8);
           a=((a&0x0000FFFFU)<<16)|((a&0xFFFF0000U)>>16);
11
           return a>>(32-len):
12
13
       void fft(bool is inv,VT &in,VT &out,int N){
           int bitlen=__lg(N),num=is_inv?-1:1;
14
           for(int i=0;i<N;++i) out[bit reverse(i,bitlen)]=in[i</pre>
15
                1;
            for(int step=2; step<=N; step<<=1){</pre>
16
                const int mh = step>>1;
17
                for(int i=0: i<mh: ++i){</pre>
18
19
                    complex<T> wi = exp(complex<T>(0,i*num*pi/mh)
                         );
20
                    for(int j=i; j<N; j+=step){</pre>
                        int k = j+mh;
21
22
                        complex<T> u = out[j], t = wi*out[k];
23
                        out[j] = u+t;
                        out[k] = u-t;
24
25
                    }
26
               }
27
28
           if(is inv) for(int i=0;i<N;++i) out[i]/=N;</pre>
29
30 };
```

6.14 NTT

20

21

22

23

24

25

26

27

28

29

30

31

32

33

34

35

36

37

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55

57

58

59

```
1 template<typename T, typename VT=std::vector<T> >
   struct NTT{
     const T P,G;
     NTT(T p=(1<<23)*7*17+1,T g=3):P(p),G(g){}
     inline unsigned int bit_reverse(unsigned int a,int len){
       a=((a&0x55555555U)<<1)|((a&0xAAAAAAAAU)>>1);
       a=((a&0x33333333U)<<2)|((a&0xCCCCCCCU)>>2);
       a = ((a\&0x0F0F0F0FU) <<4) | ((a\&0xF0F0F0F0U) >>4);
       a = ((a\&0x00FF00FFU) < < 8) | ((a\&0xFF00FF00U) >> 8);
       a=((a&0x0000FFFFU)<<16)|((a&0xFFFF0000U)>>16);
11
       return a>>(32-len);
12
     inline T pow_mod(T n,T k,T m){
13
14
       T ans=1:
15
       for (n=(n)=m?n\%m:n); k; k>>=1){
16
         if(k&1)ans=ans*n%m;
         n=n*n%m:
17
       } return ans;
18
19
     inline void ntt(bool is inv,VT &in,VT &out,int N){
20
21
       int bitlen=std:: lg(N);
       for(int i=0;i<N;++i)out[bit reverse(i,bitlen)]=in[i];</pre>
22
23
       for(int step=2,id=1;step<=N;step<<=1,++id){</pre>
         T wn=pow_mod(G,(P-1)>>id,P),wi=1,u,t;
24
         const int mh=step>>1;
25
         for(int i=0:i<mh:++i){</pre>
26
           for(int j=i;j<N;j+=step){</pre>
27
             u = out[j], t = wi*out[j+mh]%P;
28
29
             out[j] = u+t;
30
             out[j+mh] = u-t;
             if(out[j]>=P)out[j]-=P;
31
             if(out[j+mh]<0)out[j+mh]+=P;</pre>
32
33
34
           wi = wi*wn%P;
35
36
       if(is inv){
37
         for(int i=1;i<N/2;++i)std::swap(out[i],out[N-i]);</pre>
39
         T invn=pow mod(N,P-2,P);
         for(int i=0;i<N;++i)out[i]=out[i]*invn%P;</pre>
40
41
42
43 };
44 #endif
```

6.15 Simplex

```
1 /*target:
    max \sum {j=1}^n A {0,j}*x j
    \sum_{j=1}^n A_{i,j}*x_j <= A_{i,0} | i=1\sim m
    x \neq 0 \neq 1
6 VDB = vector<double>*/
7 template<class VDB>
  VDB simplex(int m,int n,vector<VDB> a){
    vector<int> left(m+1), up(n+1);
    iota(left.begin(), left.end(), n);
    iota(up.begin(), up.end(), 0);
    auto pivot = [&](int x, int y){
      swap(left[x], up[y]);
      auto k = a[x][y]; a[x][y] = 1;
      vector<int> pos;
15
      for(int j = 0; j <= n; ++j){
```

```
17
         a[x][j] /= k;
         if(a[x][i] != 0) pos.push back(i);
18
19
20
       for(int i = 0; i <= m; ++i){
         if(a[i][v]==0 || i == x) continue;
21
         k = a[i][y], a[i][y] = 0;
22
23
         for(int j : pos) a[i][j] -= k*a[x][j];
24
25
     };
26
     for(int x,y;;){
27
       for(int i=x=1; i <= m; ++i)</pre>
28
         if(a[i][0] < a[x][0]) x = i;
       if(a[x][0]>=0) break;
29
       for(int j=y=1; j <= n; ++j)</pre>
31
         if(a[x][j]<a[x][y]) y = j;</pre>
32
       if(a[x][y]>=0) return VDB();//infeasible
33
       pivot(x, y);
34
35
     for(int x,y;;){
       for(int j=y=1; j <= n; ++j)</pre>
37
         if(a[0][j] > a[0][y]) y = j;
       if(a[0][y]<=0) break;</pre>
38
39
       x = -1:
40
       for(int i=1; i<=m; ++i) if(a[i][y] > 0)
         if(x == -1 || a[i][0]/a[i][y]
41
            < a[x][0]/a[x][y]) x = i;
42
       if(x == -1) return VDB();//unbounded
43
       pivot(x, y);
44
45
46
     VDB ans(n + 1);
47
     for(int i = 1; i <= m; ++i)</pre>
48
      if(left[i] <= n) ans[left[i]] = a[i][0];</pre>
49
     ans[0] = -a[0][0];
     return ans;
50
```

6.16 Expression

1 /**

```
* 支援處理四則運算的工具。給四則運算的字串,檢查格式並計算其 61
  *格式不合法,會丟出錯誤。複雜度 O(字串長度)。支援的符號有
  * 和求餘數,先乘除後加減。可以使用括號、或前置正負號。數字開
      頭可以為
  * 零或禁止為零。可以兼容或禁止多重前置號(例如 --1 視為 1
  * 視為 -1) 。空字串視為不合法。運算範圍限於 long long 。如果
  * 以零或對零求餘也會丟出錯誤。
  */
  void req(bool b) { if (!b) throw ""; }
  const int B = 2; // 可以調整成 B 進位
  class Expr {
11
12
    private:
14
     Expr(const string& s) : src(s.begin(), s.end()) {}
     inline char top() {
        return src.empty() ? '\0' : src.front();
16
17
     inline char pop() {
```

```
char c = src.front(); src.pop front(); return c;
ll n() {
    11 ret = pop() - '0';
    // 若要禁止數字以 0 開頭,加上這行
    // req(ret || !isdigit(top()));
    while (isdigit(top())) ret = B * ret + pop() - '0';
    return ret:
11 fac() {
    if (isdigit(top())) return n();
    if (top() == '-') { pop(); return -fac(); }
    if (top() == '(') {
        pop();
        11 \text{ ret} = \exp(1);
        req(pop() == ')');
        return ret;
    // 若要允許前置正號,加上這行
    // if(top() == '+') { pop(); return fac(); }
    throw "";
 11 term() {
    11 ret = fac(); char c = top();
    while (c == '*' || c == '/' || c == '%') {
        pop();
        if (c == '*') ret *= fac();
        else {
            11 t = fac(); req(t);
            if (c == '/') ret /= t; else ret %= t;
        c = top();
    } return ret;
11 expr(bool k) {
    11 ret = term();
    while (top() == '+' || top() == '-')
        if (pop() == '+') ret += term();
        else ret -= term();
    req(top() == (k ? ')' : '\0'));
    return ret;
public:
// 給定數學運算的字串,求其值。若格式不合法,丟出錯誤。
static ll eval(const string& s) {
    // 若要禁止多重前置號,加上這四行
    // req(s.find("--") == -1); // 禁止多重負號
    // reg(s.find("-+") == -1);
    // req(s.find("+-") == -1);
    // req(s.find("++") == -1);
    return Expr(s).expr(0);
```

6.17 Pick's Theorem

```
1 /* i:number of integer points interior to the polygon
2 b:the number of integer points on its boundary (including both vertices and points along the sides).
3 Then the area A of this polygon is: A = i + b/2 - 1 */
```

```
5 | pair<11, 11> operator-(const pair<11, 11>& a, const pair<11,
       11>& b) {
     return {a.first - b.first, a.second - b.second};
   int n;
10 pair<ll, ll> p[100010];
   11 Pick() {
    cin >> n;
    for(int i = 0; i < n; ++i)</pre>
      cin >> p[i].first >> p[i].second;
    p[n] = p[0];
17
    11 \text{ area} = 0:
    for(int i = 0; i < n; ++i)</pre>
       area += p[i].first * p[i + 1].second - p[i].second * p[i
            + 11.first:
    area = abs(area);
20
    11 b = 0:
21
22
     for(int i = 0; i < n; ++i) {
       pair < 11, 11 > v = p[i + 1] - p[i];
23
       b += abs(__gcd(v.first, v.second));
24
25
26
    11 a = (area + 2 - b) / 2;
27
    return a;
```

6.18 攜展歐幾里德

```
1  // 給 a,b , 解 ax+by=gcd(a,b)
2  typedef pair<ll, ll> pii;
3  pii extgcd(ll a, ll b) {
4    if (b == 0) return {1, 0};
5    ll k = a / b;
6    pii p = extgcd(b, a - k * b);
7    return {p.second, p.first - k * p.second};
8 }
```

6.19 線性篩

```
      1 int prime[MAXN];

      2 vector(int) p;

      3 void sieve(int n){

      4 fill(prime+2,prime+n+1,1);

      5 for(int i=2;i<=n;++i){</td>

      6 if(prime[i]==1) p.push_back(i);

      7 for(int j:p){

      8 if(i*j>n) break;

      9 prime[i*j]=j; //順便紀錄最小的質因數是誰

      10 if(i%j==0) break; //表示後面的質數都大於最小質因數

      11 }

      12 }

      13 }
```

7 String

7.1 Rolling Hash

```
1 // 問 pat 在 str 第一次出現的開頭 index 。-1 表示找不到。
  int rollhash(string& str, string& pat) {
      const ll x = 1e6 + 99; // 隨意大質數,建議 1e6
      const ll m = 1e9 + 9; // 隨意大質數,建議 1e9
      assert(pat.size());
                             // pat 不能是空字串
      11 xx = 1, sh = 0;
      for (char c : pat)
          sh = (sh * x + c) % m, xx = xx * x % m;
      deque<11> hash = {0};
      int ret = 0;
      for (char c : str) {
          hash.push back((hash.back() * x + c) % m);
          if (hash.size() <= pat.size()) continue;</pre>
14
          11 h = hash.back() - hash.front() * xx;
15
          h = (h \% m + m) \% m;
16
          if (h == sh) return ret;
17
          hash.pop_front();
          ret++;
18
      } return -1;
19
```

7.2 Trie

```
1 class Trie {
   private:
       struct Node {
           int cnt = 0, sum = 0;
           Node *tr[128] = {};
           ~Node() {
                for (int i = 0; i < 128; i++)
                   if (tr[i]) delete tr[i];
      };
11
      Node *root:
   public:
^{12}
       void insert(char *s) {
           Node *ptr = root;
14
15
           for (; *s; s++) {
               if (!ptr->tr[*s]) ptr->tr[*s] = new Node();
17
               ptr = ptr->tr[*s];
18
               ptr->sum++;
19
20
           ptr->cnt++;
21
22
       inline int count(char *s) {
           Node *ptr = find(s);
23
24
           return ptr ? ptr->cnt : 0;
       Node *find(char *s) {
           Node *ptr = root;
           for (; *s; s++) {
29
               if (!ptr->tr[*s]) return 0;
30
               ptr = ptr->tr[*s];
31
           } return ptr;
32
```

bool erase(char *s) {

```
Node *ptr = find(s);
35
           if (!ptr) return false;
           int num = ptr->cnt;
36
37
           if (!num) return false;
           ptr = root;
38
           for (; *s; s++) {
39
40
               Node *tmp = ptr:
                ptr = ptr->tr[*s];
41
42
                ptr->sum -= num;
                if (!ptr->sum) {
43
44
                    delete ptr;
                    tmp - > tr[*s] = 0;
45
                    return true;
46
47
48
49
       Trie() { root = new Node(); }
50
       ~Trie() { delete root; }
51
```

7.3 AC 自動機

```
1 template < char L='a', char R='z'>
2 class ac_automaton{
    struct joe{
      int next[R-L+1], fail, efl, ed, cnt_dp, vis;
       joe():ed(0),cnt_dp(0),vis(0){
         for(int i=0; i<=R-L; i++) next[i]=0;</pre>
    };
   public:
    std::vector<joe> S;
    std::vector<int> q;
     int qs,qe,vt;
     ac_automaton():S(1),qs(0),qe(0),vt(0){}
     void clear(){
15
      q.clear();
      S.resize(1);
       for(int i=0; i<=R-L; i++) S[0].next[i] = 0;</pre>
18
      S[0].cnt_dp = S[0].vis = qs = qe = vt = 0;
19
20
     void insert(const char *s){
21
      int o = 0;
       for(int i=0,id; s[i]; i++){
         id = s[i]-L;
         if(!S[o].next[id]){
25
           S.push back(joe());
26
           S[o].next[id] = S.size()-1;
27
28
         o = S[o].next[id];
29
       ++S[o].ed;
31
     void build fail(){
      S[0].fail = S[0].efl = -1;
       q.clear();
       q.push back(0);
       ++qe;
       while(qs!=qe){
         int pa = q[qs++], id, t;
         for(int i=0;i<=R-L;i++){</pre>
           t = S[pa].next[i];
           if(!t)continue;
```

```
ans += S[t].ed;/*因為都走efl邊所以保證匹配成功*/
          id = S[pa].fail;
                                                                                                                                       if (z[i] + i > z[bst] + bst) bst = i;
43
          while(~id && !S[id].next[i]) id = S[id].fail;
                                                             100
          S[t].fail = ~id ? S[id].next[i] : 0;
                                                             101
                                                                    }
          S[t].efl = S[S[t].fail].ed ? S[t].fail : S[S[t].fail 102]
                                                                    return ans;
                                                                                                                            10 // Queries how many times s appears in t
                                                                                                                            int z_match(string &s, string &t) {
              1.efl;
                                                             103
          q.push_back(t);
                                                                   /*把AC自動機變成真的自動機*/
                                                                                                                                  int ans = 0;
          ++qe;
                                                                                                                            13
                                                                                                                                   int lens = s.length(), lent = t.length();
47
                                                                   void evolution(){
                                                             105
                                                                                                                                   int z[lens + lent + 5];
48
                                                                                                                            14
                                                                    for(qs=1; qs!=qe;){
                                                             106
49
                                                                                                                                   string st = s + "$" + t;
                                                             107
                                                                      int p = q[qs++];
                                                                                                                                   z_build(st, z);
50
                                                                      for(int i=0; i<=R-L; i++)</pre>
                                                             108
                                                                                                                                   for (int i = lens + 1; i <= lens + lent; i++)</pre>
    /*DP出每個前綴在字串s出現的次數並傳回所有字串被s匹配成功的
                                                                        if(S[p].next[i]==0) S[p].next[i] = S[S[p].fail].next[ 17
                                                                                                                                       if (z[i] == lens) ans++;
         次數O(N+M)*/
                                                                                                                                   return ans;
    int match_0(const char *s){
                                                             110
      int ans = 0, id, p = 0, i;
                                                             111
                                                                 }
                                                             112 };
      for(i=0; s[i]; i++){
        id = s[i]-L;
55
        while(!S[p].next[id] && p) p = S[p].fail;
        if(!S[p].next[id])continue;
                                                                                                                               7.6 BWT
                                                                 7.4 KMP
        p = S[p].next[id];
        ++S[p].cnt_dp; /* 匹配成功則它所有後綴都可以被匹配(DP計算
                                                                                                                                                          // 字串長度
                                                                                                                             1 const int N = 8;
                                                               1 // KMP fail function.
                                                                                                                             2 int s[N+N+1] = "suffixes"; // 字串, 後面預留一倍空間。
                                                                 int* kmp_fail(string& s) {
61
      for(i=qe-1; i>=0; --i){
                                                                                                                                                         // 後綴陣列
                                                                                                                             3 int sa[N];
                                                                    int* f = new int[s.size()]; int p = f[0] = -1;
62
        ans += S[q[i]].cnt_dp * S[q[i]].ed;
                                                                                                                             4 int pivot;
                                                                    for (int i = 1; s[i]; i++) {
        if(~S[q[i]].fail) S[S[q[i]].fail].cnt_dp += S[q[i]].
                                                                                                                             5 int cmp(const void* i, const void* j) {
                                                                        while (p != -1 \&\& s[p + 1] != s[i]) p = f[p];
                                                                                                                                  return strncmp(s+*(int*)i, s+*(int*)j, N);
                                                                        if (s[p + 1] == s[i]) p++;
65
      return ans;
                                                                        f[i] = p;
                                                                                                                             8 // 此處便宜行事,採用 O(N2logN) 的後綴陣列演算法。
                                                                                                                             9 void BWT() {
    /*多串匹配走efl邊並傳回所有字串被s匹配成功的次數O(N*M^1.5)
                                                                    return f;
                                                                                                                                   strncpy(s + N, s, N);
                                                                 // 問 sub 在 str 中出現幾次。
                                                                                                                                   for (int i=0; i<N; ++i) sa[i] = i;
    int match 1(const char *s)const{
                                                                                                                                   qsort(sa, N, sizeof(int), cmp);
      int ans = 0, id, p = 0, t;
                                                                 int kmp_count(string& str, string& sub) {
                                                                                                                                   // 當輸入字串的所有字元都相同,必須當作特例處理。
                                                                    int* fail = kmp_fail(sub); int p = -1, ret = 0;
      for(int i=0; s[i]; i++){
                                                                                                                                   // 或者改用stable sort。
        id = s[i]-L;
                                                                     for (int i = 0; i < str.size(); i++) {</pre>
72
        while(!S[p].next[id] && p) p = S[p].fail;
                                                                        while (p != -1 \&\& sub[p + 1] != str[i]) p = fail[p];
                                                                                                                                   for (int i=0; i<N; ++i)</pre>
        if(!S[p].next[id])continue;
                                                                        if (sub[p + 1] == str[i]) p++;
                                                                                                                                       cout << s[(sa[i] + N-1) % N];
        p = S[p].next[id];
                                                              17
                                                                        if (p == sub.size() - 1) p = fail[p], ret++;
                                                                                                                            17
                                                                                                                                   for (int i=0; i<N; ++i)</pre>
        if(S[p].ed) ans += S[p].ed;
                                                                                                                                       if (sa[i] == 0) {
        for(t=S[p].efl; ~t; t=S[t].efl){
                                                              19
                                                                    delete[] fail; return ret;
                                                                                                                                          pivot = i;
          ans += S[t].ed;/*因為都走efl邊所以保證匹配成功*/
                                                              20 }
                                                                                                                            20
                                                                                                                                          break;
                                                                                                                            21
                                                              21 // 問 sub 在 str 第一次出現的開頭 index 。-1 表示找不到。
                                                              22
                                                                 int kmp(string& str, string& sub) {
                                                                                                                            22
79
                                                                    int* fail = kmp_fail(sub);
                                                                                                                            23 // Inverse BWT
                                                              23
80
      return ans;
                                                                                                                                                          // 字串長度
                                                                    int i, j = 0;
                                                                                                                            24 const int N = 8;
                                                                    while (i < str.size() && j < sub.size()) {</pre>
    /*枚舉(s的子字串@A)的所有相異字串各恰一次並傳回次數O(N*M
                                                                                                                            25 char t[N+1] = "xuffessi"; // 字串
                                                                        if (sub[j] == str[i]) i++, j++;
         ^(1/3))*/
                                                                                                                              int pivot;
                                                                        else if (j == 0) i++;
    int match 2(const char *s){
                                                              27
                                                                                                                            27 int next[N];
                                                                        else j = fail[j - 1] + 1;
      int ans=0, id, p=0, t;
                                                              28
                                                                                                                            28 void IBWT() {
84
                                                                                                                                  vector<int> index[256];
85
                                                                    delete[] fail;
      /*把戳記vt+=1,只要vt沒溢位,所有S[p].vis==vt就會變成
                                                                                                                                   for (int i=0; i<N; ++i)</pre>
                                                              31
                                                                    return j == sub.size() ? (i - j) : -1;
                                                                                                                                      index[t[i]].push_back(i);
                                                                                                                            31
                                                                                                                            32
                                                                                                                                   for (int i=0, n=0; i<256; ++i)
       這種利用vt的方法可以0(1)歸零vis陣列*/
                                                                                                                            33
                                                                                                                                       for (int j=0; j<index[i].size(); ++j)</pre>
      for(int i=0; s[i]; i++){
                                                                                                                            34
                                                                                                                                          next[n++] = index[i][j];
        id = s[i]-L;
                                                                                                                            35
                                                                                                                                   int p = pivot;
        while(!S[p].next[id]&&p)p = S[p].fail;
                                                                 7.5 Z
                                                                                                                            36
                                                                                                                                   for (int i=0; i<N; ++i)</pre>
        if(!S[p].next[id])continue;
                                                                                                                                       cout << t[p = next[p]];</pre>
                                                                                                                            37
        p = S[p].next[id];
        if(S[p].ed && S[p].vis!=vt){
                                                               1 void z build(string &s, int *z) {
          S[p].vis = vt;
                                                                    int bst = z[0] = 0;
          ans += S[p].ed;
                                                                    for (int i = 1; s[i]; i++) {
                                                                        if (z[bst] + bst < i) z[i] = 0;
        for(t=S[p].efl; ~t && S[t].vis!=vt; t=S[t].efl){
                                                                                                                               7.7 Suffix Array LCP
```

else z[i] = min(z[bst] + bst - i, z[i - bst]);

while (s[z[i]] == s[i + z[i]]) z[i]++;

S[t].vis = vt;

```
1 #define radix sort(x,y){
                                                                                                                                   point operator-(const point &b)const{
                                                                              z[i] = extend(i, i);
    for(i=0;i<A;++i) c[i] = 0;
                                                               25
                                                                             L = i;
                                                                                                                                     return point(x-b.x,y-b.y); }
                                                                                                                                   point operator*(const T &b)const{
    for(i=0;i<n;++i) c[x[y[i]]]++;</pre>
                                                                              R = i + z[i] - 1;
                                                               26
                                                                          } else if (z[ii] == n) {
                                                                                                                                     return point(x*b,y*b); }
    for(i=1;i<A;++i) c[i] += c[i-1];</pre>
                                                               27
    for(i=n-1;~i;--i) sa[--c[x[y[i]]]] = y[i];
                                                                              z[i] = n + extend(i-n, i+n);
                                                                                                                                   point operator/(const T &b)const{
                                                               28
                                                                                                                                     return point(x/b,y/b); }
                                                                             L = i;
  #define AC(r,a,b) r[a]!=r[b]||a+k>=n||r[a+k]!=r[b+k]
                                                               30
                                                                             R = i + z[i] - 1:
                                                                                                                                   bool operator == (const point &b)const{
   void suffix array(const char *s,int n,int *sa,int *rank,int
                                                                         } else z[i] = min(z[ii], n);
                                                                                                                                     return x==b.x&&y==b.y; }
                                                             * 31
                                                                                                                                   T dot(const point &b)const{
       tmp,int *c){
    int A='z'+1,i,k,id=0;
                                                                                                                                     return x*b.x+y*b.y; }
                                                                      // 尋找最長迴文子字串的長度。
                                                               33
    for(i=0; i<n; ++i)rank[tmp[i]=i]=s[i];</pre>
                                                                                                                               20
                                                                                                                                   T cross(const point &b)const{
                                                               34
                                                                      int n = 0, p = 0;
    radix sort(rank.tmp);
                                                                                                                                     return x*b.y-y*b.x; }
11
                                                               35
                                                                      for (int i=0; i<N; ++i)</pre>
    for(k=1; id<n-1; k<<=1){</pre>
12
                                                               36
                                                                          if (z[i] > n) n = z[p = i];
                                                                                                                                   point normal()const{//求法向量
      for(id=0,i=n-k; i<n; ++i) tmp[id++]=i;</pre>
13
                                                                                                                                     return point(-y,x); }
                                                                      // 記得去掉特殊字元。
                                                               37
14
      for(i=0; i<n; ++i)</pre>
                                                                                                                                   T abs2()const{//向量長度的平方
                                                                      cout << "最長迴文子字串的長度是" << (n-1) / 2;
15
       if(sa[i]>=k) tmp[id++]=sa[i]-k;
                                                                                                                                     return dot(*this); }
                                                                      // 印出最長迴文子字串,記得別印特殊字元。
                                                               39
      radix sort(rank,tmp);
16
                                                                                                                                   T rad(const point &b)const{//兩向量的弧度
                                                                      for (int i=p-z[p]+1; i<=p+z[p]-1; ++i)</pre>
                                                               40
      swap(rank,tmp);
17
                                                                                                                                  return fabs(atan2(fabs(cross(b)),dot(b))); }
                                                                          if (i & 1) cout << s[i];</pre>
                                                               41
      for(rank[sa[0]]=id=0,i=1; i<n; ++i)</pre>
18
                                                               42 }
                                                                                                                                   T getA()const{//對x軸的弧度
        rank[sa[i]] = id+=AC(tmp,sa[i-1],sa[i]);
19
                                                                                                                                     T A=atan2(y,x);//超過180度會變負的
20
      A = id+1;
                                                                                                                                     if(A<=-PI/2)A+=PI*2;
21
                                                                                                                               31
                                                                                                                                     return A:
22
                                                                  7.9 Edit Distance
                                                                                                                               32
23 //h: 高度數組 sa:後綴數組 rank: 排名
                                                                                                                               33
                                                                                                                                 };
   void suffix_array_lcp(const char *s,int len,int *h,int *sa,
                                                                                                                                 template<typename T>
       int *rank){
                                                                                                                                 struct line{
                                                                1 // 問從 src 到 dst 的最小 edit distance
    for(int i=0; i<len; ++i)rank[sa[i]]=i;</pre>
                                                                                                                                   line(){}
    for(int i=0,k=0; i<len; ++i){</pre>
                                                                2 // ins 插入一個字元的成本
                                                                                                                                   point<T> p1,p2;
      if(rank[i]==0)continue;
                                                                3 // del 刪除一個字元的成本
                                                                                                                                   T a,b,c;//ax+by+c=0
      if(k)--k;
                                                                  // sst 替换一個字元的成本
                                                                                                                                   line(const point<T>&x,const point<T>&y):p1(x),p2(y){}
      while(s[i+k]==s[sa[rank[i]-1]+k])++k;
29
                                                                  11 edd(string& src, string& dst, ll ins, ll del, ll sst) {
                                                                                                                                   void pton(){//轉成一般式
      h[rank[i]]=k;
                                                                      ll dp[src.size() + 1][dst.size() + 1]; // 不用初始化
                                                                                                                               41
                                                                                                                                     a=p1.y-p2.y;
31
                                                                      for (int i = 0; i <= src.size(); i++) {</pre>
                                                                                                                                     b=p2.x-p1.x;
                                                                                                                               42
32
    h[0]=0;// h[k]=lcp(sa[k],sa[k-1]);
                                                                          for (int j = 0; j <= dst.size(); j++) {</pre>
                                                                                                                                     c=-a*p1.x-b*p1.y;
                                                                                                                               43
                                                                              if (i == 0) dp[i][j] = ins * j;
                                                                                                                               44
                                                                              else if (j == 0) dp[i][j] = del * i;
                                                                                                                                   T ori(const point<T> &p)const{//點和有向直線的關係, >0左
                                                                                                                               45
                                                               11
                                                                              else if (src[i - 1] == dst[j - 1])
                                                                                                                                        邊、=0在線上<0右邊
                                                               12
                                                                                  dp[i][j] = dp[i - 1][j - 1];
                                                                                                                                     return (p2-p1).cross(p-p1);
                                                                                                                               46
  7.8 LPS
                                                               13
                                                                                                                               47
                                                               14
                                                                                  dp[i][j] = min(dp[i][j - 1] + ins,
                                                                                                                                   T btw(const point<T> &p)const{//點投影落在線段上<=0
                                                                                             min(dp[i - 1][j] + del,
                                                               15
                                                                                                                               49
                                                                                                                                     return (p1-p).dot(p2-p);
                                                               16
                                                                                              dp[i - 1][j - 1] + sst));
                         // 原字串
1 char t[1001];
                                                                                                                               50
                                                               17
                                                                         }
2 char s[1001 * 2];
                         // 穿插特殊字元之後的t
                                                                                                                               51
                                                                                                                                   bool point on segment(const point<T>&p)const{//點是否在線段
                                                               18
                                                                      }
3 int z[1001 * 2], L, R; // 源自Gusfield's Algorithm
                                                               19
                                                                      return dp[src.size()][dst.size()];
4 // 由a往左、由b往右,對稱地作字元比對。
                                                                                                                                     return ori(p)==0&&btw(p)<=0;</pre>
                                                                                                                               52
5 int extend(int a, int b) {
                                                                                                                               53
      int i = 0:
                                                                                                                                   T dis2(const point<T> &p,bool is_segment=0)const{//點跟直線
      while (a-i)=0 \&\& b+i < N \&\& s[a-i] == s[b+i]) i++;
                                                                                                                                        /線段的距離平方
                                                                                                                                     point<T> v=p2-p1,v1=p-p1;
                                                                                                                               55
                                                                       Geometry
                                                                                                                                     if(is segment){
                                                                                                                               56
  void longest_palindromic_substring() {
                                                                                                                               57
                                                                                                                                       point<T> v2=p-p2;
      int N = strlen(t);
                                                                                                                                       if(v.dot(v1)<=0)return v1.abs2();</pre>
                                                                                                                               58
      // t穿插特殊字元,存放到s。
12
                                                                  8.1 Geometry
                                                                                                                               59
                                                                                                                                       if(v.dot(v2)>=0)return v2.abs2();
      // (實際上不會這麼做,都是細算索引值。)
13
                                                                                                                               60
      memset(s, '.', N*2+1);
14
                                                                                                                               61
                                                                                                                                     T tmp=v.cross(v1):
15
      for (int i=0; i<N; ++i) s[i*2+1] = t[i];
                                                                                                                               62
                                                                                                                                     return tmp*tmp/v.abs2();
                                                                1 //Copy from Jinkela
16
      N = N*2+1;
                                                                                                                               63
                                                                  const double PI=atan2(0.0,-1.0);
      // s[N] = '\0'; // 可做可不做
17
                                                                  template<typename T>
                                                                                                                               64
                                                                                                                                   T seg dis2(const line<T> &1)const{//兩線段距離平方
18
      // Manacher's Algorithm
                                                                  struct point{
                                                                                                                                     return min({dis2(1.p1,1),dis2(1.p2,1),1.dis2(p1,1),1.dis2
      z[0] = 1; L = R = 0;
19
                                                                   T \times v;
                                                                                                                                          (p2,1));
      for (int i=1; i<N; ++i) {</pre>
20
                                                                    point(){}
                                                                                                                               66
          int ii = L - (i - L); // i的映射位置
21
                                                                    point(const T&x, const T&y):x(x),y(y){}
                                                                                                                               67
                                                                                                                                   point<T> projection(const point<T> &p)const{//點對直線的投
```

point operator+(const point &b)const{

return point(x+b.x,y+b.y); }

影

int n = R + 1 - i;

if (i > R) {

22

```
point<T> n=(p2-p1).normal();
                                                                   130
                                                                            T a=p[i].cross(p[j]);
                                                                                                                                              return (a.x<b.x)||(a.x==b.x&&a.y<b.y);</pre>
                                                                                                                                      184
69
       return p-n*(p-p1).dot(n)/n.abs2();
                                                                   131
                                                                             cx+=(p[i].x+p[j].x)*a;
                                                                                                                                      185
70
                                                                   132
                                                                             cy+=(p[i].y+p[j].y)*a;
                                                                                                                                      186
                                                                                                                                            void graham(vector<point<T> > &s){//凸包
71
     point<T> mirror(const point<T> &p)const{
                                                                   133
                                                                            w+=a;
                                                                                                                                      187
                                                                                                                                              sort(s.begin(),s.end(),graham_cmp);
72
       //點對直線的鏡射,要先呼叫pton轉成一般式
                                                                   134
                                                                                                                                      188
                                                                                                                                              p.resize(s.size()+1);
                                                                   135
                                                                          return point<T>(cx/3/w,cy/3/w);
73
       point<T> R;
                                                                                                                                      189
                                                                                                                                              int m=0;
                                                                   136
       T d=a*a+b*b;
                                                                                                                                              for(size_t i=0;i<s.size();++i){</pre>
                                                                                                                                      190
                                                                         char ahas(const point<T>& t)const{//點是否在簡單多邊形內
75
       R.x=(b*b*p.x-a*a*p.x-2*a*b*p.y-2*a*c)/d;
                                                                                                                                                while(m \ge 2\&\&(p[m-1]-p[m-2]).cross(s[i]-p[m-2]) <= 0)--m;
                                                                   137
76
       R.y=(a*a*p.y-b*b*p.y-2*a*b*p.x-2*b*c)/d;
                                                                              是的話回傳1、在邊上回傳-1、否則回傳0
                                                                                                                                      192
                                                                                                                                                p[m++]=s[i];
77
       return R;
                                                                           bool c=0:
                                                                                                                                      193
                                                                   138
78
                                                                           for(int i=0,j=p.size()-1;i<p.size();j=i++)</pre>
                                                                                                                                      194
                                                                                                                                              for(int i=s.size()-2,t=m+1;i>=0;--i){
                                                                   139
                                                                             if(line<T>(p[i],p[j]).point_on_segment(t))return -1;
                                                                                                                                                while(m \ge t \& (p[m-1] - p[m-2]) \cdot cross(s[i] - p[m-2]) <= 0) --m;
79
     bool equal(const line &1)const{//直線相等
                                                                   140
       return ori(1.p1)==0&&ori(1.p2)==0;
                                                                             else if((p[i].y>t.y)!=(p[j].y>t.y)&&
                                                                                                                                      196
                                                                                                                                                p[m++]=s[i];
80
                                                                  141
                                                                                                                                     x197
81
                                                                            t.x<(p[j].x-p[i].x)*(t.y-p[i].y)/(p[j].y-p[i].y)+p[i]
                                                                  142
                                                                                                                                              if(s.size()>1)--m;
     bool parallel(const line &1)const{
82
                                                                                                                                              p.resize(m);
83
       return (p1-p2).cross(1.p1-l.p2)==0;
                                                                   143
                                                                               c=!c;
84
                                                                           return c;
                                                                                                                                      200
                                                                   144
     bool cross seg(const line &1)const{
                                                                   145
                                                                                                                                      201
                                                                                                                                           T diam(){//直徑
       return (p2-p1).cross(1.p1-p1)*(p2-p1).cross(1.p2-p1)<=0;</pre>
                                                                         char point_in_convex(const point<T>&x)const{
                                                                                                                                              int n=p.size(),t=1;
                                                                  146
                                                                                                                                      202
                                                                                                                                              T ans=0;p.push_back(p[0]);
            //直線是否交線段
                                                                          int l=1,r=(int)p.size()-2;
                                                                                                                                      203
                                                                                                                                              for(int i=0;i<n;i++){</pre>
                                                                           while(l<=r){//點是否在凸多邊形內,是的話回傳1、在邊上回
                                                                                                                                    傳 204
87
                                                                   148
                                                                                                                                                point<T> now=p[i+1]-p[i];
                                                                               -1、否則回傳0
     int line_intersect(const line &1)const{//直線相交情況,-1無
                                                                                                                                                while(now.cross(p[t+1]-p[i])>now.cross(p[t]-p[i]))t=(t
                                                                             int mid=(1+r)/2;
                                                                                                                                      206
          限多點、1交於一點、0不相交
                                                                   149
                                                                            T a1=(p[mid]-p[0]).cross(x-p[0]);
       return parallel(1)?(ori(1.p1)==0?-1:0):1;
                                                                   150
                                                                                                                                      207
                                                                                                                                                ans=max(ans,(p[i]-p[t]).abs2());
                                                                             T a2=(p[mid+1]-p[0]).cross(x-p[0]);
                                                                   151
90
                                                                                                                                      208
                                                                             if(a1>=0&&a2<=0){
     int seg_intersect(const line &1)const{
                                                                   152
91
                                                                                                                                      209
                                                                                                                                              return p.pop_back(),ans;
                                                                              T res=(p[mid+1]-p[mid]).cross(x-p[mid]);
92
       T c1=ori(l.p1), c2=ori(l.p2);
                                                                   153
                                                                                                                                      210
                                                                   154
                                                                               return res>0?1:(res>=0?-1:0);
93
       T c3=1.ori(p1), c4=1.ori(p2);
                                                                                                                                      211
                                                                                                                                           T min_cover_rectangle(){//最小覆蓋矩形
                                                                            }else if(a1<0)r=mid-1;</pre>
       if(c1==0&&c2==0){//共線
94
                                                                                                                                      212
                                                                                                                                              int n=p.size(),t=1,r=1,l;
                                                                             else l=mid+1;
         bool b1=btw(1.p1)>=0,b2=btw(1.p2)>=0;
95
                                                                   157
                                                                                                                                              if(n<3)return 0;//也可以做最小周長矩形
         T a3=1.btw(p1),a4=1.btw(p2);
                                                                   158
                                                                                                                                              T ans=1e99; p. push_back(p[0]);
                                                                          return 0;
97
         if(b1&&b2&&a3==0&&a4>=0) return 2;
                                                                   159
                                                                                                                                      215
                                                                                                                                              for(int i=0;i<n;i++){</pre>
         if(b1&&b2&&a3>=0&&a4==0) return 3;
98
                                                                                                                                                point<T> now=p[i+1]-p[i];
                                                                         vector<T> getA()const{//凸包邊對x軸的夾角
         if(b1&&b2&&a3>=0&&a4>=0) return 0;
                                                                   160
99
                                                                                                                                                while(now.cross(p[t+1]-p[i])>now.cross(p[t]-p[i]))t=(t
                                                                           vector<T>res://一定是號增的
                                                                   161
         return -1; // 無限交點
                                                                           for(size_t i=0;i<p.size();++i)</pre>
                                                                   162
101
       }else if(c1*c2<=0&&c3*c4<=0)return 1;</pre>
                                                                                                                                                while(now.dot(p[r+1]-p[i])>now.dot(p[r]-p[i]))r=(r+1)%n
                                                                   163
                                                                            res.push_back((p[(i+1)%p.size()]-p[i]).getA());
       return 0;//不相交
102
                                                                   164
                                                                           return res;
103
104
     point<T> line intersection(const line &1)const{/*直線交點
                                                                                                                                                while(now.dot(p[1+1]-p[i])<=now.dot(p[1]-p[i]))1=(1+1)%
                                                                                                                                      220
                                                                         bool line_intersect(const vector<T>&A,const line<T> &1)
105
       point<T> a=p2-p1,b=l.p2-l.p1,s=l.p1-p1;
                                                                             const(//0(logN)
106
       //if(a.cross(b)==0)return INF;
                                                                           \verb|int f1=upper_bound(A.begin(),A.end(),(1.p1-1.p2).getA())-|^{221}
                                                                                                                                                T d=now.abs2();
                                                                   167
       return p1+a*(s.cross(b)/a.cross(b));
107
                                                                                                                                                T tmp=now.cross(p[t]-p[i])*(now.dot(p[r]-p[i])-now.dot(
                                                                               A.begin();
108
                                                                                                                                                     p[l]-p[i]))/d;
                                                                           int f2=upper_bound(A.begin(),A.end(),(1.p2-1.p1).getA())-
     point<T> seg_intersection(const line &1)const{//線段交點
109
                                                                                                                                                ans=min(ans,tmp);
                                                                               A.begin();
110
       int res=seg_intersect(1);
                                                                                                                                      224
                                                                   169
                                                                          return 1.cross_seg(line<T>(p[f1],p[f2]));
       if(res<=0) assert(0);</pre>
111
                                                                                                                                      225
                                                                                                                                              return p.pop_back(),ans;
                                                                  170
       if(res==2) return p1;
                                                                                                                                    直 226
112
                                                                         polygon cut(const line<T> &1)const{//凸包對直線切割,得到
                                                                   171
       if(res==3) return p2;
113
                                                                                                                                            T dis2(polygon &pl){//凸包最近距離平方
                                                                              線1左側的凸包
       return line_intersection(1);
114
                                                                                                                                              vector<point<T> > &P=p,&Q=pl.p;
                                                                           polygon ans;
                                                                   172
115
                                                                                                                                              int n=P.size(),m=Q.size(),l=0,r=0;
                                                                   173
                                                                           for(int n=p.size(),i=n-1,j=0;j<n;i=j++){</pre>
116
                                                                                                                                            for(int i=0;i<n;++i)if(P[i].y<P[1].y)l=i;</pre>
                                                                            if(1.ori(p[i])>=0){
                                                                   174
    template<typename T>
                                                                                                                                            for(int i=0;i<m;++i)if(Q[i].y<Q[r].y)r=i;</pre>
                                                                               ans.p.push_back(p[i]);
                                                                   175
    struct polygon{
                                                                                                                                              P.push_back(P[0]),Q.push_back(Q[0]);
                                                                               if(1.ori(p[j])<0)</pre>
                                                                   176
                                                                                 ans.p.push_back(1.line_intersection(line<T>(p[i],p[233
                                                                                                                                              T ans=1e99;
                                                                   177
120
     vector<point<T> > p;//逆時針順序
                                                                                                                                              for(int i=0;i<n;++i){</pre>
                                                                                      j])));
121
     T area()const{//面積
                                                                                                                                                while ((P[1]-P[1+1]) \cdot cross(Q[r+1]-Q[r]) < 0)r = (r+1) m;
                                                                   178
                                                                             }else if(l.ori(p[j])>0)
                                                                                                                                                ans=min(ans,line<T>(P[1],P[1+1]).seg_dis2(line<T>(Q[r],
122
                                                                   179
                                                                               ans.p.push_back(1.line_intersection(line<T>(p[i],p[j
123
       for(int i=p.size()-1,j=0;j<(int)p.size();i=j++)</pre>
                                                                                                                                                     0[r+1])));
         ans+=p[i].cross(p[j]);
                                                                                                                                                l=(1+1)%n;
124
                                                                                                                                      237
                                                                   180
125
       return ans/2;
                                                                                                                                      238
                                                                   181
                                                                          return ans;
                                                                                                                                              return P.pop_back(),Q.pop_back(),ans;
126
                                                                                                                                      239
                                                                   182
                                                                        \verb|static| bool| graham_cmp(const| point<T>& a,const| point<T>& b)|^{240}
     point<T> center_of_mass()const{//重心
127
                                                                   183
                                                                                                                                            static char sign(const point<T>&t){
128
       T cx=0, cy=0, w=0;
                                                                              {//凸包排序函數
                                                                                                                                              return (t.y==0?t.x:t.y)<0;</pre>
       for(int i=p.size()-1,j=0;j<(int)p.size();i=j++){</pre>
129
```

```
point3D(const T&x,const T&y,const T&z):x(x),y(y),z(z){}
                                                                                                                                           point3D<T> projection(const point3D<T> &p)const{
243
     static bool angle cmp(const line<T>& A,const line<T>& B){
244
                                                                         point3D operator+(const point3D &b)const{
                                                                                                                                      363
                                                                                                                                             return p-n*(p-p0).dot(n)/n.abs2();
       point<T> a=A.p2-A.p1,b=B.p2-B.p1;
                                                                          return point3D(x+b.x,y+b.y,z+b.z);}
245
                                                                                                                                      364
246
       return sign(a)<sign(b)||(sign(a)==sign(b)&&a.cross(b)>0);307
                                                                         point3D operator-(const point3D &b)const{
                                                                                                                                      365
                                                                                                                                           point3D<T> line intersection(const line3D<T> &1)const{
                                                                          return point3D(x-b.x,y-b.y,z-b.z);}
247
                                                                                                                                      366
                                                                                                                                             T tmp=n.dot(1.p2-1.p1);//等於0表示平行或重合該平面
                                                                         point3D operator*(const T &b)const{
     int halfplane_intersection(vector<line<T> > &s){//半平面交 309
                                                                                                                                              return 1.p1+(1.p2-1.p1)*(n.dot(p0-1.p1)/tmp);
                                                                                                                                      367
248
                                                                          return point3D(x*b,v*b,z*b);}
       sort(s.begin(),s.end(),angle_cmp);//線段左側為該線段半平
                                                                                                                                      368
249
                                                                         point3D operator/(const T &b)const{
                                                                                                                                           line3D<T> plane intersection(const plane &pl)const{
                                                                                                                                      369
                                                                  312
                                                                          return point3D(x/b,y/b,z/b);}
                                                                                                                                      370
                                                                                                                                              point3D<T> e=n.cross(pl.n),v=n.cross(e);
250
       int L,R,n=s.size();
                                                                         bool operator==(const point3D &b)const{
                                                                  313
251
       vector<point<T> > px(n);
                                                                                                                                      371
                                                                                                                                              T tmp=pl.n.dot(v):// 等於0表示平行或重合該平面
                                                                  314
                                                                          return x==b.x&&y==b.y&&z==b.z;}
       vector<line<T> > q(n);
                                                                                                                                              point3D<T> q=p0+(v*(pl.n.dot(pl.p0-p0))/tmp);
252
                                                                                                                                      372
                                                                        T dot(const point3D &b)const{
                                                                  315
                                                                                                                                              return line3D<T>(q,q+e);
253
       q[L=R=0]=s[0];
                                                                                                                                      373
                                                                          return x*b.x+y*b.y+z*b.z;}
                                                                  316
       for(int i=1;i<n;++i){</pre>
254
                                                                                                                                      374
                                                                  317
                                                                         point3D cross(const point3D &b)const{
         while(L<R&&s[i].ori(px[R-1])<=0)--R;</pre>
255
                                                                                                                                      375
                                                                  318
                                                                          return point3D(y*b.z-z*b.y,z*b.x-x*b.z,x*b.y-y*b.x);}
         while(L<R&&s[i].ori(px[L])<=0)++L;</pre>
                                                                                                                                         template<typename T>
256
                                                                                                                                      376
                                                                        T abs2()const{//向量長度的平方
                                                                  319
         q[++R]=s[i];
                                                                                                                                         struct triangle3D{
257
                                                                                                                                      377
                                                                          return dot(*this);}
                                                                  320
                                                                                                                                           point3D<T> a,b,c;
258
          if(q[R].parallel(q[R-1])){
                                                                  321
                                                                        T area2(const point3D &b)const{//和b、原點圍成面積的平方
                                                                                                                                           triangle3D(){}
259
           --R:
                                                                                                                                      379
           if(q[R].ori(s[i].p1)>0)q[R]=s[i];
                                                                          return cross(b).abs2()/4;}
                                                                                                                                           triangle3D(const point3D<T> &a,const point3D<T> &b,const
260
                                                                  322
                                                                                                                                      380
                                                                  323
                                                                                                                                                point3D<T> &c):a(a),b(b),c(c){}
261
262
         if(L<R)px[R-1]=q[R-1].line_intersection(q[R]);</pre>
                                                                  324
                                                                       template<typename T>
                                                                                                                                           bool point in(const point3D<T> &p)const{//點在該平面上的投
                                                                                                                                      381
                                                                       struct line3D{
263
                                                                   325
                                                                                                                                                 影在三角形中
       while (L < R \& q[L].ori(px[R-1]) <= 0) -- R;
                                                                  326
                                                                        point3D<T> p1,p2;
264
                                                                                                                                              return line3D<T>(b,c).same side(p,a)&&line3D<T>(a,c).
                                                                                                                                      382
       p.clear();
                                                                  327
                                                                        line3D(){}
265
                                                                                                                                                  same_side(p,b)&&line3D<T>(a,b).same_side(p,c);
                                                                        line3D(const point3D<T> &p1,const point3D<T> &p2):p1(p1),p2383
266
       if(R-L<=1)return 0;</pre>
                                                                  328
267
       px[R]=q[R].line intersection(q[L]);
                                                                              (p2){}
       for(int i=L;i<=R;++i)p.push_back(px[i]);</pre>
268
                                                                        T dis2(const point3D<T> &p,bool is_segment=0)const{//點跟直385
                                                                  329
                                                                                                                                         template<typename T>
       return R-L+1;
269
                                                                              線/線段的距離平方
                                                                                                                                          struct tetrahedron{//四面體
270
                                                                   330
                                                                           point3D<T> v=p2-p1,v1=p-p1;
                                                                                                                                           point3D<T> a,b,c,d;
271
    };
                                                                           if(is segment){
                                                                  331
                                                                                                                                           tetrahedron(){}
                                                                                                                                      388
    template<typename T>
^{272}
                                                                  332
                                                                             point3D<T> v2=p-p2;
                                                                                                                                           tetrahedron(const point3D<T> &a,const point3D<T> &b,const
273
    struct triangle{
                                                                             if(v.dot(v1)<=0)return v1.abs2();</pre>
                                                                   333
                                                                                                                                                point3D<T> &c,const point3D<T> &d):a(a),b(b),c(c),d(d)
274
     point<T> a,b,c;
                                                                   334
                                                                             if(v.dot(v2)>=0)return v2.abs2();
                                                                                                                                                {}
275
     triangle(){}
                                                                   335
                                                                                                                                           T volume6()const{//體積的六倍
                                                                                                                                      390
     triangle(const point<T> &a,const point<T> &b,const point<T>336
276
                                                                          point3D<T> tmp=v.cross(v1);
                                                                                                                                              return (d-a).dot((b-a).cross(c-a));
                                                                                                                                      391
           &c):a(a),b(b),c(c){}
                                                                           return tmp.abs2()/v.abs2();
                                                                                                                                      392
277
     T area()const{
                                                                   338
                                                                                                                                      393
                                                                                                                                           point3D<T> centroid()const{
       T t=(b-a).cross(c-a)/2;
278
                                                                   339
                                                                         pair<point3D<T>,point3D<T> > closest_pair(const line3D<T>
                                                                                                                                     &<sub>394</sub>
                                                                                                                                             return (a+b+c+d)/4;
279
       return t>0?t:-t;
                                                                             1)const{
                                                                                                                                      395
280
                                                                   340
                                                                           point3D<T> v1=(p1-p2), v2=(1.p1-1.p2);
                                                                                                                                      396
                                                                                                                                           bool point in(const point3D<T> &p)const{
     point<T> barycenter()const{//重心
281
                                                                           point3D<T> N=v1.cross(v2),ab(p1-l.p1);
                                                                  341
                                                                                                                                              return triangle3D<T>(a,b,c).point_in(p)&&triangle3D<T>(c,
                                                                                                                                      397
       return (a+b+c)/3;
282
                                                                  342
                                                                           //if(N.abs2()==0)return NULL;平行或重合
                                                                                                                                                  d,a).point in(p);
283
                                                                           T tmp=N.dot(ab),ans=tmp*tmp/N.abs2();//最近點對距離
                                                                  343
                                                                                                                                      398
     point<T> circumcenter()const{//外心
284
                                                                           point3D<T> d1=p2-p1,d2=l.p2-l.p1,D=d1.cross(d2),G=l.p1-p1<sub>399</sub>
                                                                  344
285
       static line<T> u,v;
                                                                                                                                         template<tvpename T>
       u.p1=(a+b)/2;
286
                                                                          T t1=(G.cross(d2)).dot(D)/D.abs2();
                                                                                                                                         struct convexhull3D{
                                                                  345
       u.p2=point<T>(u.p1.x-a.y+b.y,u.p1.y+a.x-b.x);
287
                                                                  346
                                                                          T t2=(G.cross(d1)).dot(D)/D.abs2():
                                                                                                                                      402
                                                                                                                                           static const int MAXN=1005:
288
       v.p1=(a+c)/2;
                                                                  347
                                                                           return make pair(p1+d1*t1,l.p1+d2*t2);
                                                                                                                                      403
                                                                                                                                           struct face{
289
       v.p2=point<T>(v.p1.x-a.y+c.y,v.p1.y+a.x-c.x);
                                                                  348
                                                                                                                                             int a,b,c;
                                                                                                                                      404
290
       return u.line intersection(v);
                                                                         bool same side(const point3D<T> &a,const point3D<T> &b)
                                                                                                                                             face(int a,int b,int c):a(a),b(b),c(c){}
                                                                  349
                                                                                                                                      405
291
                                                                                                                                      406
                                                                                                                                           };
     point<T> incenter()const{//內心
292
                                                                           return (p2-p1).cross(a-p1).dot((p2-p1).cross(b-p1))>0;
                                                                                                                                           vector<point3D<T>> pt;
                                                                                                                                      407
       T A=sqrt((b-c).abs2()), B=sqrt((a-c).abs2()), C=sqrt((a-b)._{351}
293
                                                                                                                                      408
                                                                                                                                           vector<face> ans:
                                                                                                                                      409
                                                                                                                                           int fid[MAXN][MAXN];
                                                                      };
294
       return pointT>(A*a.x+B*b.x+C*c.x,A*a.y+B*b.y+C*c.y)/(A+B<sub>353</sub>
                                                                                                                                           void build(){
                                                                       template<typename T>
                                                                                                                                      410
            +C);
                                                                       struct plane{
                                                                                                                                      411
                                                                                                                                             int n=pt.size():
295
                                                                                                                                              ans.clear();
                                                                        point3D<T> p0,n;//平面上的點和法向量
                                                                                                                                      412
296
     point<T> perpencenter()const{//垂心
                                                                                                                                      413
                                                                                                                                              memset(fid,0,sizeof(fid));
       return barycenter()*3-circumcenter()*2;
297
                                                                  357
                                                                         plane(const point3D<T> &p0,const point3D<T> &n):p0(p0),n(n)_{414}
                                                                                                                                              ans.emplace back(0,1,2);//注意不能共線
298
                                                                             {}
                                                                                                                                              ans.emplace back(2,1,0);
299
   };
                                                                                                                                      416
                                                                                                                                              int ftop = 0;
                                                                  358
                                                                        T dis2(const point3D<T> &p)const{//點到平面距離的平方
300
    template<typename T>
                                                                                                                                              for(int i=3, ftop=1; i<n; ++i,++ftop){</pre>
                                                                                                                                      417
                                                                          T tmp=(p-p0).dot(n);
                                                                  359
   struct point3D{
                                                                                                                                      418
                                                                                                                                                vector<face> next:
                                                                  360
                                                                           return tmp*tmp/n.abs2();
     T x,y,z;
                                                                                                                                                for(auto &f:ans){
                                                                                                                                      419
                                                                  361
     point3D(){}
```

```
T d=(pt[i]-pt[f.a]).dot((pt[f.b]-pt[f.a]).cross(pt[f. 29))
                                                                                                                                                // 這裡可以知道是哪兩點是最小點對
                                                                       for (int i = n - 2, t = ret.size() + 1; i >= 0; i--) {
                cl-pt[f.a]));
                                                                                                                                 24
                                                                                                                                               d = min(d, dd(t[i], t[i + j]));
                                                                           while (ret.size() >= t && jud) ret.pop back();
           if(d<=0) next.push back(f);</pre>
                                                                                                                                 25
421
                                                                 31
                                                                                                                                        return d;
                                                                           ret.push back(pp[i]);
422
           int ff=0:
                                                                 32
                                                                                                                                 26
           if(d>0) ff=ftop;
                                                                 33
423
                                                                                                                                 27 // 給一堆點,求最近點對的距離「的平方」。
           else if(d<0) ff=-ftop;</pre>
                                                                       if (n >= 2) ret.pop back();
424
                                                                 34
                                                                                                                                    11 closest_pair(vector<pii>& pp) {
425
           fid[f.a][f.b]=fid[f.b][f.c]=fid[f.c][f.a]=ff;
                                                                       return ret:
                                                                                                                                 29
                                                                                                                                        sort(pp.begin(), pp.end());
                                                                 36
426
                                                                                                                                 30
                                                                                                                                        return dac(pp, 0, pp.size() - 1);
427
         for(auto &f:ans){
                                                                    // (shoelace formula)
                                                                                                                                 31 }
           if(fid[f.a][f.b]>0 && fid[f.a][f.b]!=fid[f.b][f.a])
428
                                                                      給凸包,問其面積「的兩倍」。若凸包少於三個點,回傳零。
             next.emplace back(f.a,f.b,i);
429
                                                                   11 area(vector<pii>& poly) {
           if(fid[f.b][f.c]>0 && fid[f.b][f.c]!=fid[f.c][f.b])
430
                                                                       int n = poly.size();
             next.emplace_back(f.b,f.c,i);
431
                                                                       11 \text{ ret} = 0;
                                                                                                                                    8.4 最小覆蓋圓
432
           if(fid[f.c][f.a]>0 && fid[f.c][f.a]!=fid[f.a][f.c])
                                                                       for (int i = 0; i < n; i++)
433
             next.emplace back(f.c,f.a,i);
                                                                           ret += (poly[i].x * poly[ii].y);
434
                                                                        for (int i = 0; i < n; i++)
                                                                                                                                  1 using PT = point<T>;
435
         ans=next:
                                                                           ret -= (poly[i].y * poly[ii].x);
                                                                 45
                                                                                                                                  using CPT = const PT;
436
                                                                       return ret;
                                                                                                                                  3 PT circumcenter(CPT &a, CPT &b, CPT &c) {
437
                                                                 47 }
                                                                                                                                     PT u = b-a, v = c-a;
     point3D<T> centroid()const{
438
                                                                 48 // 給凸包,問其兩點最遠距離「的平方」。若要問平面上任意個點的
                                                                                                                                     T c1 = u.abs2()/2, c2 = v.abs2()/2;
439
       point3D<T> res(0,0,0);
                                                                                                                                      T d = u.cross(v):
       T vol=0:
440
                                                                   // 距離,請先轉成凸包。若凸包少於兩個點,回傳零。
                                                                                                                                      return PT(a.x+(v.y*c1-u.y*c2)/d, a.y+(u.x*c2-v.x*c1)/d);
       for(auto &f:ans){
441
                                                                   #define kk (k + 1) % n
         T tmp=pt[f.a].dot(pt[f.b].cross(pt[f.c]));
442
                                                                   11 maxdist(vector<pii>& poly) {
                                                                                                                                    void solve(PT p[], int n, PT &c, T &r2){
         res=res+(pt[f.a]+pt[f.b]+pt[f.c])*tmp;
443
                                                                                                                                     random_shuffle(p,p+n);
                                                                       int k = 1, n = poly.size();
         vol+=tmp:
444
                                                                       if (n < 2) return 0;</pre>
                                                                                                                                      c = p[0]; r2 = 0; // c, r2 = 圓心, 半徑平方
445
                                                                       if (n == 2) return dd(poly[0], poly[1]);
                                                                                                                                      for(int i=1; i<n; i++)</pre>
       return res/(vol*4);
446
                                                                       11 \text{ ret} = 0;
                                                                                                                                        if((p[i]-c).abs2() > r2) {
447
                                                                       for (int i = 0; i < n; i++) {
                                                                                                                                          c=p[i]; r2=0;
                                                                                                                                 14
448 };
                                                                           while (abs(crzf(poly[kk], poly[i], poly[ii])) >=
                                                                                                                                          for(int j=0; j<i; j++)</pre>
                                                                                  abs(crzf(poly[k], poly[i], poly[ii])))
                                                                                                                                            if((p[j]-c).abs2() > r2) {
                                                                                                                                              c.x = (p[i].x+p[j].x)/2;
                                                                                                                                 17
                                                                           ret = max(ret, max(dd(poly[i], poly[k]),
                                                                                                                                              c.y = (p[i].y+p[j].y)/2;
          旋轉卡尺
                                                                                              dd(poly[ii], poly[k])));
                                                                                                                                              r2 = (p[j]-c).abs2();
                                                                 62
                                                                                                                                 20
                                                                                                                                              for(int k=0; k<j; k++)</pre>
                                                                       return ret;
                                                                                                                                 21
                                                                                                                                               if((p[k]-c).abs2() > r2) {
 1 typedef pair<11, 11> pii:
                                                                                                                                                 c = circumcenter(p[i], p[j], p[k]);
 2 #define x first
                                                                                                                                                  r2 = (p[i]-c).abs2();
 3 #define y second
                                                                                                                                 24
 4 #define ii (i + 1) % n // 打字加速!
                                                                                                                                 25
                                                                         最近點對
 5 inline pii operator-(const pii& a, const pii& b) {
                                                                                                                                 26
       return {a.x - b.x, a.y - b.y};
                                                                                                                                 27 }
 7|} // const 不可省略
```

```
1 typedef pair<11, 11> pii;
  #define x first
  #define y second
  11 dd(const pii& a, const pii& b) {
      11 dx = a.x - b.x, dy = a.y - b.y;
      return dx * dx + dy * dy;
  const 11 inf = 1e18;
  11 dac(vector<pii>& p, int 1, int r) {
      if (1 >= r) return inf;
      int^m = (1 + r) / 2;
      11 d = min(dac(p, 1, m), dac(p, m + 1, r));
      vector<pii> t;
      for (int i = m; i >= 1 && p[m].x - p[i].x < d; i--)
          t.push_back(p[i]);
       for (int i = m + 1; i \le r \&\& p[i].x - p[m].x < d; i++)
          t.push back(p[i]);
       sort(t.begin(), t.end(),
           [](pii& a, pii& b) { return a.y < b.y; });
20
       int n = t.size();
       for (int i = 0; i < n - 1; i++)
           for (int j = 1; j < 4 && i + j < n; j++)
```

8 inline 11 operator*(const pii& a, const pii& b) {

inline 11 crzf(const pii& o, const pii& a, const pii& b) {

18 // 給平面上任意個點,求其凸包。返回順序為逆時針。此方法會移除

crzf(ret[ret.size() - 2], ret.back(), pp[i]) <= 0</pre>

pp.erase(unique(pp.begin(), pp.end()), pp.end());

while (ret.size() >= 2 && jud) ret.pop_back();

return a.x * b.y - a.y * b.x;

inline ll dd(const pii& a, const pii& b) {

11 dx = a.x - b.x, dy = a.y - b.y;

vector<pii> makepoly(vector<pii>& pp) {

sort(pp.begin(), pp.end());

for (int i = 0; i < n; i++) {

ret.push back(pp[i]);

return (a - o) * (b - o)

return dx * dx + dy * dy;

重複點。

int n = pp.size();

vector<pii> ret;

#define jud \

12

13

27

8.5 Rectangle Union Area

```
1 \mid const int maxn = 1e5 + 10;
2 struct rec{
    int t, b, l, r;
4 } r[maxn];
5 int n, cnt[maxn << 2];</pre>
6 long long st[maxn \langle\langle 2], ans = 0;
7 vector<int> x, y;
8 vector<pair<int, int>, pair<int, int>>> v;
9 void modify(int t, int l, int r, int ql, int qr, int v) {
      if (q1 <= 1 && r <= qr) cnt[t] += v;</pre>
      else {
           int m = (1 + r) >> 1;
           if (qr <= m) modify(t << 1, 1, m, ql, qr, v);</pre>
           else if (ql >= m) modify(t << 1 | 1, m, r, ql, qr, v)
           else modify(t \langle\langle 1, 1, m, ql, m, v\rangle\rangle, modify(t \langle\langle 1 |
                1, m, r, m, qr, v);
```

```
while(ch>='0'&&ch<='9')x=(x<<3)+(x<<1)+(ch^48),ch=getchar 3|//unsigned long ffsl
       if (cnt[t]) st[t] = y[r] - y[1];
17
                                                                            ();
                                                                                                                                   4 //unsigned long long ffsll
       else if (r - 1 == 1) st[t] = 0;
                                                                        return f?-x:x;
                                                                                                                                   5 unsigned int x; scanf("%u",&x)
18
19
       else st[t] = st[t << 1] + st[t << 1 | 1];
                                                                 9
                                                                                                                                   6 printf("右起第一個1:的位置");
20
                                                                 10
                                                                                                                                  7 printf("%d\n",__builtin_ffs(x));
21
   int main() {
                                                                 11
                                                                    inline void print(ll x,bool bk = false) {
                                                                                                                                   8 printf("左起第一個1之前0的個數:");
22
       cin >> n:
                                                                 12
                                                                       if(x<0){
                                                                                                                                  9 printf("%d\n",__builtin_clz(x));
       for (int i = 0; i < n; i++) {
                                                                 13
                                                                            putchar('-');
23
                                                                                                                                  10 printf("右起第一個1之後0的個數:");
24
          cin >> r[i].l >> r[i].r >> r[i].b >> r[i].t;
                                                                 14
                                                                            x = -x;
                                                                                                                                  printf("%d\n",__builtin_ctz(x));
          if (r[i].l > r[i].r) swap(r[i].l, r[i].r);
                                                                 15
25
                                                                                                                                  12 printf("1的個數:");
          if (r[i].b > r[i].t) swap(r[i].b, r[i].t);
26
                                                                 16
                                                                        if(x==0)
                                                                                                                                  printf("%d\n",__builtin_popcount(x));
          x.push back(r[i].1);
                                                                            if(!bk)putchar('0');
27
                                                                 17
                                                                                                                                  14 | printf("1的個數的奇偶性:");
          x.push_back(r[i].r);
28
                                                                 18
                                                                           return:
                                                                                                                                  printf("%d\n",__builtin_parity(x));
29
          y.push back(r[i].b);
                                                                 19
30
          y.push back(r[i].t);
                                                                 20
                                                                        print(x/10,true);
                                                                 21
                                                                        putchar((x-10*(x/10))^'0');
31
32
       sort(x.begin(), x.end());
                                                                                                                                    9.4 莫隊算法-區間眾數
       sort(y.begin(), y.end());
33
      x.erase(unique(x.begin(), x.end()), x.end());
34
      y.erase(unique(y.begin(), y.end()), y.end());
35
       for (int i = 0; i < n; i++) {
                                                                    9.2 pbds
                                                                                                                                   1 using namespace std;
36
          r[i].1 = lower_bound(x.begin(), x.end(), r[i].1) - x.
                                                                                                                                   2 const int maxn = 1e6 + 10;
37
               begin();
                                                                                                                                   3 struct query { int id, bk, 1, r; };
                                                                                                                                   4 int arr[maxn], cnt[maxn], d[maxn], n, m, bk, mx;
          r[i].r = lower_bound(x.begin(), x.end(), r[i].r) - x. 1 #include <bits/extc++.h>
38
                                                                                                                                   5 pair<int,int> ans[maxn];
               begin();
                                                                   using namespace __gnu_pbds;
          r[i].b = lower_bound(y.begin(), y.end(), r[i].b) - y.
                                                                                                                                   6 vector<query> q;
                                                                                                                                   7 bool cmp(query x,query y) {
                                                                    // hash table:用法和map差不多 //均攤O(1)
          r[i].t = lower_bound(y.begin(), y.end(), r[i].t) - y.
                                                                                                                                        return (x.bk < y.bk \mid | (x.bk == y.bk) && x.r < y.r);
                                                                   gp hash table <string,int> mp;
                                                                   mp.find(); mp[]=;
          v.emplace_back(make_pair(r[i].1, 1), make_pair(r[i].b
                                                                                                                                  10 void add(int pos) {
                                                                   mp.insert(make pair())
               , r[i].t));
                                                                                                                                  11
                                                                                                                                        d[cnt[arr[pos]]]--;
          v.emplace_back(make_pair(r[i].r, -1), make_pair(r[i].
                                                                                                                                  12
                                                                                                                                         cnt[arr[pos]]++;
42
                                                                   // heaps
               b, r[i].t));
                                                                                                                                  13
                                                                                                                                         d[cnt[arr[pos]]]++;
                                                                 10 priority queue<int, greater<int>, TAG> Q;
                                                                                                                                         if(d[mx + 1] > 0) mx++;
                                                                                                                                  14
43
      sort(v.begin(), v.end(), [](pair<pair<int, int>, pair<int 12 Tag
                                                                                                                                  15 }
44
                                                                                                         join
                                                                                                                  modify
           16 void del(int pos) {
                                                                                         0(1)
                                                                                                 0(lgN) \mid 0(1)
                                                                                                                 O(1gN)
          if (a.first.first != b.first.first) return a.first.
                                                                                                                                  17
                                                                                                                                         d[cnt[arr[pos]]]--;
45
                                                                 14 thin_heap_tag
                                                                                         O(1gN) | O(1gN) | 慢
                                                                                                                  爥
                                                                                                                                         cnt[arr[pos]]--;
               first < b.first.first;</pre>
                                                                                                                                  18
                                                                                         0(1)
                                                                 15 binomial_heap_tag
                                                                                                 O(\lg N) \mid O(\lg N) \mid O(\lg N)
          return a.first.second > b.first.second:
                                                                                                                                  19
                                                                                                                                         d[cnt[arr[pos]]]++;
                                                                 16 rc binomial heap tag 0(1)
                                                                                                 O(\lg N) \mid O(\lg N) \mid O(\lg N)
                                                                                                                                  20
                                                                                                                                         if(d[mx] == 0) mx --;
47
                                                                 17 binary_heap_tag
                                                                                        | O(1) | O(1gN)| 慢
                                                                                                               0(1gN)
       for (int i = 0; i < v.size(); i++) {</pre>
                                                                                                                                  21
48
          if (i) ans += (x[v[i].first.first] - x[v[i - 1].first 18
                                                                   */ //可以用迭代器遍歷
                                                                                                                                  22
                                                                                                                                    void mo(int n, int m) {
49
                                                                 19 Q.push(x); Q.pop(); Q.top();
                .first]) * st[1];
                                                                                                                                  23
                                                                                                                                         sort(q.begin(), q.end(), cmp);
          modify(1, \ 0, \ y.size(), \ v[i].second.first, \ v[i].second \ ^{20} \ | \ Q.join(b); \ //merge \ two \ heap
                                                                                                                                  24
                                                                                                                                         for(int i = 0, cl = 1, cr = 0; i < m; i++) {
50
                                                                   Q.empty(); Q.size();
                                                                                                                                  25
                                                                                                                                             while(cr < q[i].r) add(++cr);</pre>
               .second, v[i].first.second);
                                                                 22 Q.modify(it, 6); Q.erase(it);
                                                                                                                                  26
                                                                                                                                             while(cl > q[i].l) add(--cl);
       cout << ans << '\n';
                                                                                                                                  27
                                                                                                                                             while(cr > q[i].r) del(cr--);
52
                                                                    // k-th
                                                                 24
                                                                                                                                  28
                                                                                                                                             while(cl < q[i].1) del(cl++);
53
       return 0;
                                                                    typedef tree<int, null type, less<int>, rb tree tag,
                                                                                                                                  29
                                                                                                                                             ans[q[i].id] = make_pair(mx, d[mx]);
                                                                            tree_order_statistics_node_update> set_t;
                                                                                                                                  30
                                                                   set t s; s.insert(12); s.insert(505);
                                                                                                                                  31
                                                                 assert(*s.find by order(0) == 12);
                                                                                                                                  32
                                                                                                                                    int main(){
                                                                 29 assert(*s.find by order(3) == 505);
                                                                                                                                  33
                                                                                                                                         cin >> n >> m;
       Other
                                                                 30 assert(s.order_of_key(12) == 0);
                                                                                                                                  34
                                                                                                                                         bk = (int) sqrt(n + 0.5);
                                                                 31 | assert(s.order_of_key(505) == 1);
                                                                                                                                  35
                                                                                                                                         for(int i = 1; i <= n; i++) cin >> arr[i];
                                                                 32 s.erase(12);
                                                                                                                                  36
                                                                                                                                         q.resize(m);
                                                                 33 assert(*s.find by order(0) == 505);
                                                                                                                                  37
                                                                                                                                         for(int i = 0; i < m; i++) {
  9.1 Fastio
                                                                 34 assert(s.order of key(505) == 0);
                                                                                                                                             cin >> q[i].l >> q[i].r;
                                                                                                                                  38
                                                                                                                                             q[i].id = i,q[i].bk = (q[i].l - 1) / bk;
                                                                                                                                  39
                                                                                                                                  40
                                                                                                                                         mo(n, m);
1 inline 11 read(){
                                                                                                                                  41
                                                                   9.3 BuiltIn
      11 x=0, f=0;
                                                                                                                                  42
                                                                                                                                         for(int i = 0; i < m; i++)</pre>
       char ch = getchar();
                                                                                                                                  43
                                                                                                                                             cout << ans[i].first << ' ' << ans[i].second << '\n';</pre>
       if(ch==EOF)
                                                                                                                                  44
                                                                                                                                         return 0;
                                                                                                                                  45 }
                                                                 1 //gcc專用
```

2 //unsigned int ffs

while(ch<'0'||ch>'9')f|=ch=='-',ch=getchar();

9.5 CNF for(auto c:cnf) 60 if(~c.y)relax(1,r,c,dp[1][k][c.x]+dp[k+1][r][c.y]+c 53 .cost); 61 bellman(l,r,tok.size()); 1 #define MAXN 55 62 2 struct CNF{ 63 int $s,x,y;//s->xy \mid s->x$, if y==-1int cost; CNF(){} CNF(int s,int x,int y,int c):s(s),x(x),y(y),cost(c){} 提醒事項 s int state; //規則數量 map<char,int> rule;//每個字元對應到的規則,小寫字母為終端字符 vector<CNF> cnf; 1 Debug List: void init(){ 2 1. Long Long !! state=0; 3 2. python3 整數除法 "//" rule.clear(); 4 3. connected / unconnected cnf.clear(); 14 5 4. 範圍看清楚 15 6 5. eps 夠小嗎!! void add_to_cnf(char s,const string &p,int cost){ //加入一個s -> 的文法,代價為cost 7 6. 可多生 case 測 if(rule.find(s)==rule.end())rule[s]=state++; 8 7. 找不用胖資結的其他作法 e.g. multiset -> 單調對列 for(auto c:p)if(rule.find(c)==rule.end())rule[c]=state++; 9 8. 離散化 **if**(p.size()==1){ 10 9. 鴿籠原理 cnf.push_back(CNF(rule[s],rule[p[0]],-1,cost)); 21 11 10. TLE 後找人多想 22 }else{ 23 int left=rule[s]; 24 int sz=p.size(); for(int i=0;i<sz-2;++i){</pre> 25 For non-negative integer n,m and prime P, cnf.push_back(CNF(left,rule[p[i]],state,0)); $C(m,n) \mod P = C(m/M,n/M) * C(m%M,n%M) \mod P$ 27 left=state++: = mult_i (C(m_i,n_i)) where m_i is the i-th digit of m in base P. 29 cnf.push_back(CNF(left,rule[p[sz-2]],rule[p[sz-1]],cost)) Kirchhoff's theorem 30 $A_{ii} = deg(i), A_{ij} = (i,j) \in ? -1 : 0$ 31 Deleting any one row, one column, and cal the det(A) vector<long long> dp[MAXN][MAXN]; vector<bool> neg INF[MAXN][MAXN];//如果花費是負的可能會有無限 Nth Catalan recursive function: $C_0 = 1$, $C_{n+1} = C_n * 2(2n + 1)/(n+2)$ void relax(int l,int r,const CNF &c,long long cost,bool neg_c $_{26}$ 27 Mobius Formula $if(!neg_INF[1][r][c.s]&&(neg_INF[1][r][c.x]||cost<dp[1][r][_{28}|u(n) = 1]$, if n = 1 (-1)^m , 若 n 無平方數因數,且 n = p1*p2*p3*...*pk if(neg_c||neg_INF[l][r][c.x]){ 0 ,若 n 有大於 1 的平方數因數 dp[1][r][c.s]=0; - Property neg_INF[1][r][c.s]=true; 32 1. (積性函數) u(a)u(b) = u(ab) 39 }else dp[1][r][c.s]=cost; 33 2. $\Sigma_{d|n} u(d) = [n == 1]$ 40 Mobius Inversion Formula void bellman(int l,int r,int n){ if $f(n) = \sum_{d \mid n} g(d)$ for(int k=1;k<=state;++k)</pre> 37 then $g(n) = \sum_{i=1}^{n} \{d \mid n\} u(n/d)f(d)$ for(auto c:cnf) $= \sum_{d|n} u(d)f(n/d)$ if(c.y==-1)relax(1,r,c,dp[1][r][c.x]+c.cost,k==n); 46 the number/power of gcd(i, j) = kvoid cyk(const vector<int> &tok){ 41 - Trick for(int i=0;i<(int)tok.size();++i){</pre> 分塊, O(sqrt(n)) for(int j=0;j<(int)tok.size();++j){</pre> dp[i][j]=vector<long long>(state+1,INT_MAX); 51 neg_INF[i][j]=vector<bool>(state+1,false); 44 Chinese Remainder Theorem (m_i 兩兩互質) $x = a 1 \pmod{m}$ dp[i][i][tok[i]]=0; $x = a 2 \pmod{m 2}$ bellman(i,i,tok.size()); 54 $x = a i \pmod{m}$ for(int r=1;r<(int)tok.size();++r){</pre> 49 construct a solution: Let M = m_1 * m_2 * m_3 * ... * m_n for(int l=r-1;l>=0;--1){ for(int k=1;k<r;++k)</pre> Let M i = M / m i

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t_i = 1 / M_i
t_i * M_i = 1 (mod m_i)
solution x = a_1 * t_1 * M_1 + a_2 * t_2 * M_2 + ... + a_n
* t_n * M_n + k * M
= k*M + Σ a_i * t_i * M_i, k is positive integer.
under mod M, there is one solution x = Σ a_i * t_i * M_i
solution x = a_i * t_i * M_i, k is positive integer.
under mod M, there is one solution x = Σ a_i * t_i * M_i
solution x = Δ a_i * t_i * M_i
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9.7 霍夫曼樹



	NTHU-			3.3	1D1D	6		6.11 質數	14 14
	ELEPHANTGANG		4	Gra 4.1	ph Dijkstra	7 7		6.13 FFT	14
	Соревоок			4.3 4.4 4.5	SPFA	7 7 7		6.15 Simplex	1; 1; 1; 1;
C	Contents			4.6 4.7 4.8	LCATarjanBCC_edge最小平均環	8 9 9	7	6.19 線性篩	16
1	Surroundings 1.1 setup	1 1		4.11	2-SAT	9 9		7.1 Rolling Hash	10 10 10 1'
	1.2 bashrc	1	5	5.1	w_Matching Dinic	10 10		7.5 Z	1' 1'
2	Data_Structure2.1 Sparse Table2.2 Fenwick Tree	1 1 1			Min Cost Max Flow	10 10 11 11		7.7 Suffix_Array_LCP	17 18 18
	2.3 單點修改、區間查詢線段樹	1 2 2			SW-MinCut	11 11	8	Geometry 8.1 Geometry	18 18 2
	2.6 持久化線段樹	2 2 3	6	Mat 6.1 6.2	快速羃	12 12 12		8.3 最近點對	2: 2: 2:
	2.9 Dynamic_KD_tree	3 4 5		6.3 6.4 6.5	離散根號	12 12 12	9	Other 9.1 Fastio	22 23
3	2.12 Link Cut Tree	5 6		6.6 6.7 6.8	Matrix	13 13 13		9.2 pbds	25 25 25
	3.1 LCIS	6 6		$6.9 \\ 6.10$	Miller Rabin	13 13		9.5 CNF	2; 2;