

SAMPLING DISTRIBUTIONS

A. *Sampling Distributions Appropriate for \bar{x}*

Case I

- (a) Sampling from a normal population
- (b) μ is known, σ is known
- (c) any sample size, n

$$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}}$$

Case II

- (a) Sampling is done from a population whose distribution is unknown or non-normal
- (b) μ is known, σ is known or unknown
- (c) sample size is large ($n \geq 30$)

$$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}} \quad \text{if } \sigma \text{ is known}$$

$$z = \frac{\bar{x} - \mu}{\frac{S}{\sqrt{n}}} \quad \text{if } \sigma \text{ is unknown}$$

Case III

- (a) Sampling from normal population
- (b) μ is known, σ is unknown
- (c) sample size is small ($n < 30$)

$$t = \frac{\bar{x} - \mu}{\frac{S}{\sqrt{n}}} \quad \text{with } v = n - 1 \text{ (degrees of freedom)}$$

B. Sampling Distributions Appropriate for $\bar{x}_1 - \bar{x}_2$

Case I

- (a) Sampling from normal population
- (b) σ_1 and σ_2 are known
- (c) any sample size, n_1 and n_2

$$z = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$$

Case II

- (a) Distribution of sampling population is unknown, may be normal or non-normal
- (b) σ_1 and σ_2 are known or unknown
- (c) n_1 and n_2 are ≥ 30

$$z = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} \quad \text{if } \sigma_1 \text{ and } \sigma_2 \text{ are known}$$

$$z = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}} \quad \text{if } \sigma_1 \text{ and } \sigma_2 \text{ are unknown}$$

Case III

- (a) Sampling from normal population
- (b) σ_1 and σ_2 are unknown but $\sigma_1^2 = \sigma_2^2$
- (c) n_1 and n_2 are < 30

$$t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}} \quad \text{with } v = n_1 + n_2 - 2 \quad (\text{degrees of freedom})$$

$$S_p^2 = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2} \quad (\text{pooled variance})$$

Case IV

- (a) Sampling population are normal
- (b) σ_1 and σ_2 are unknown but $\sigma_1^2 \neq \sigma_2^2$
- (c) n_1 and n_2 are < 30

$$t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}}$$

$$v = \frac{\left[\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2} \right]^2}{\frac{\left(\frac{S_1^2}{n_1} \right)^2}{n_1 - 1} + \frac{\left(\frac{S_2^2}{n_2} \right)^2}{n_2 - 1}} \quad \text{rounded to the nearest integer}$$

C. *Sampling Distribution Appropriate for S^2*

Case I

- (a) $n < 30$
- (b) sampling population is normal

$$X^2 = \frac{(n-1)S^2}{\sigma^2} \quad v = n - 1$$

Case II

- (a) $n \geq 30$
- (b) any sampling population

$$z = \frac{S - \sigma}{\frac{\sigma}{\sqrt{2n}}}$$

D. Sampling Distribution for the Ratio of Two Variances S_1^2 / S_2^2

$$F = \frac{\sigma_2^2}{\sigma_1^2} \left(\frac{S_1^2}{S_2^2} \right) \quad v_1 = n_1 - 1 \text{ and } v_2 = n_2 - 1$$

$$F_{1-\alpha(v_1, v_2)} = \frac{1}{F_{\alpha(v_2, v_1)}}$$

E. Sampling Distribution Appropriate for \hat{p}

Case I

- (a) Any sampling population
- (b) $n < 30$

Use binomial distribution

Case II

- (a) Any sampling population
- (b) $n \geq 30$

$$z = \frac{\hat{p} - p}{\sqrt{\frac{pq}{n}}}$$

F. Sampling Distribution Appropriate for $\hat{p}_1 - \hat{p}_2$

$$z = \frac{(\hat{p}_1 - \hat{p}_2) - (p_1 - p_2)}{\sqrt{\frac{p_1 q_1}{n_1} + \frac{p_2 q_2}{n_2}}} \quad \text{if } p_1 \text{ and } p_2 \text{ are known}$$

$$z = \frac{(\hat{p}_1 - \hat{p}_2) - (p_1 - p_2)}{\sqrt{\hat{p}\hat{q}\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}} \quad \text{if } p_1 \text{ and } p_2 \text{ are unknown}$$

$$\hat{p} = \frac{x_1 + x_2}{n_1 + n_2} \quad (\text{pooled estimate of proportion})$$

MEASURES OF AVERAGE AND VARIABILITY

	<u>Ungrouped Data</u>	<u>Grouped Data</u>
Mean	$\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$	$\bar{x} = \frac{\sum_{i=1}^k f_i x_i}{n}$
Median	use the rules you have learned in finding for the median in ungrouped data	$X_m = L + \left[\frac{\frac{n}{2} - F_{(m-1)}}{f_m} \right] W$
Standard Deviation	$S = \sqrt{\frac{n \sum x_i^2 - (\sum x_i)^2}{n(n-1)}}$	$S = \sqrt{\frac{n \sum f_i x_i^2 - (\sum f_i x_i)^2}{n(n-1)}}$

GOODNESS OF FIT TEST

$$\chi^2 = \frac{(o_i - e_i)^2}{e_i} \quad v = k - 1 - m$$

LINEAR REGRESSION AND CORRELATION

$$\hat{y} = a + bx$$

$$a = \frac{\sum_{i=1}^n y_i - b \sum_{i=1}^n x_i}{n}$$

$$b = \frac{n \sum_{i=1}^n x_i y_i - \left(\sum_{i=1}^n x_i \right) \left(\sum_{i=1}^n y_i \right)}{n \sum_{i=1}^n x_i^2 - \left(\sum_{i=1}^n x_i \right)^2}$$

$$r = b \sqrt{\frac{S_{xx}}{S_{yy}}} = \frac{S_{xy}}{\sqrt{S_{xx} S_{yy}}}$$

ANALYSIS OF VARIANCE

Source of Variation	Sum of Squares	Degrees of Freedom	Mean Square	Computed F
Regression	SSR	1	SSR	$F = SSR/S^2$
Error	SSE	n-2	$S^2 = SSE/(n-2)$	
Total	SST	n-1		

$$S_{xx} = \sum_{i=1}^n x_i^2 - \frac{\left(\sum_{i=1}^n x_i \right)^2}{n}$$

$$S_{yy} = \sum_{i=1}^n y_i^2 - \frac{\left(\sum_{i=1}^n y_i \right)^2}{n}$$

$$S_{xy} = \sum_{i=1}^n x_i y_i - \frac{\left(\sum_{i=1}^n x_i \right) \left(\sum_{i=1}^n y_i \right)}{n}$$

$$SST = S_{yy}$$

$$SSR = b S_{xy}$$

$$SSE = SST - SSR$$