

$$E_i(\mathbf{S}) = \alpha_{i,0} + \sum_{j=1}^{N_s} \alpha_{i,j} \frac{[S_j]}{[S_j] + K_{i,j}} + \sum_{j=1}^{N_s-1} \sum_{j'=j+1}^{N_s} \alpha_{i,j,j'} \frac{[S_j][S_{j'}]}{([S_j] + K_{Q_{i,j,j'}})([S_{j'}] + K_{Q_{i,j',j}})} \quad (2)$$

Diagram illustrating the components of the gene expression model:

- Basal (constitutive) expression:** $\alpha_{i,0}$ (green box)
- First order contribution of each signal j , where j is 3-oxo-C₁₂-HSL, C₄-HSL ($N_s = 2$):** $\sum_{j=1}^{N_s} \alpha_{i,j} \frac{[S_j]}{[S_j] + K_{i,j}}$ (yellow box)
- Second order interaction effect:** $\sum_{j=1}^{N_s-1} \sum_{j'=j+1}^{N_s} \alpha_{i,j,j'} \frac{[S_j][S_{j'}]}{([S_j] + K_{Q_{i,j,j'}})([S_{j'}] + K_{Q_{i,j',j}})}$ (purple box)

Expression level for gene i , where i is *lasI*, *rhII*, and *lasB*, as a function of all signal concentrations \mathbf{S}