



SAPIENZA
UNIVERSITÀ DI ROMA

Multi-UAV path planning for target localization using AirSim virtual simulator

Facoltà di Ingegneria dell'informazione, informatica e statistica
Corso di Laurea Magistrale in Engineering in Computer Science

Candidate

Giuseppe Capaldi
ID number 1699498

Thesis Advisors

Prof. Luca Iocchi
Dr. Nome Cognome

Co-Advisor

Dr. Nome Cognome

Academic Year 2019/2020

Thesis defended on 22 January 2021
in front of a Board of Examiners composed by:

Prof. Nome Cognome (chairman)

Prof. Nome Cognome

Dr. Nome Cognome

Multi-UAV path planning for target localization using AirSim virtual simulator
Master thesis. Sapienza – University of Rome

© 2021 Giuseppe Capaldi. All rights reserved

This thesis has been typeset by L^AT_EX and the Sapthesis class.

Version: November 10, 2020

Author's email: giuseppe.capaldi96@gmail.com

*Dedicated to
my family*

Abstract

This document is an example which shows the main features of the L^AT_EX 2_& class **sapthesis.cls** developed by Francesco Biccari with the help of GuIT (Gruppo Utilizzatori Italiani di T_EX).

Acknowledgments

Ho deciso di scrivere i ringraziamenti in italiano per dimostrare la mia gratitudine verso i membri del GuIT, il Gruppo Utilizzatori Italiani di TeX, e, in particolare, verso il prof. Enrico Gregorio.

Contents

Problem space	xi
1 Style features of <code>sapthesis</code>	1
1.1 Page layout	1
1.2 Page style	2
1.3 About figures and tables	2
1.4 A section	3
1.5 Another section	5
A Special commands provided by <code>sapthesis</code>	7

Problem space

This section presents (as a first draft) the theoretical formulation of our problem, in which we have multiple UAVs sensing the simulated environment and sending data to the ground station (centralized system in this phase), making possible to train using reinforcement learning and optimize a fully cooperative task.

I considered two scenario in the contest of industrial inspection and maintenance, they've arisen from the knowledge and tools I have or I plan to acquire in this master thesis. The main framework is AirSim built on top of Unreal Editor so many possibilities are limited to the experience with them.

I started from a first scenario of target detection and localization (targets characteristics will be specified in the future) considering also a second scenario similar to a multi-agent network problem focused on coverage.

I will present a formulations for both scenarios' problems including the environment model, the vehicle dynamics model, the agent observations, environment's states and action space involved.

Scenario 1: Problem definition and motivation

In this scenario we can think of one or more targets, moving or stationary, that will be detected and classified, using standard supervised learning techniques (asynchronous calls to a specific thread), by a small number of UAVs.

Their navigation path will be determined by the results of the reinforcement learning training, in order to avoid collisions and minimize the time in which targets are detected, localized, classified.

Environment

The environment design is inspired by the free, but detailed and realistic "LandscapeMountains" Unreal project, which consists of a snowy mountain landscape with a street crossing the entire map. The street has no intersection but it is not straight and some bridges sustain it in some areas.

In this scenario the Environment E consists of a non-flat space area of $E_x \times E_y$ meters. There are N agents (where $N \leq 6$) moving at the same discrete time synchronously, sending to the ground station at each time step information about the current state of drone i at time step t .

The vehicles are assumed to be equipped with reliable communication capabilities so that they can exchange sensing information among the group without any error or delay. The objective of UAVs is to explore the environment cooperatively and to gather information till the target (or multiple targets) is detected and localized.

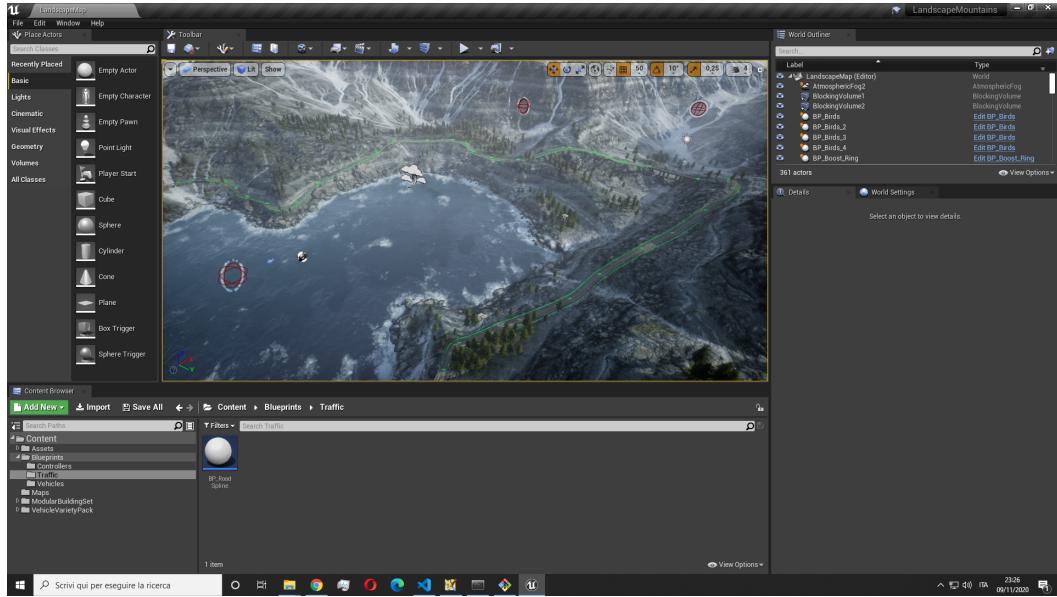


Figure 0.1. Perspective view of the LandscapeMountain project. The green border delimits the border of the street.

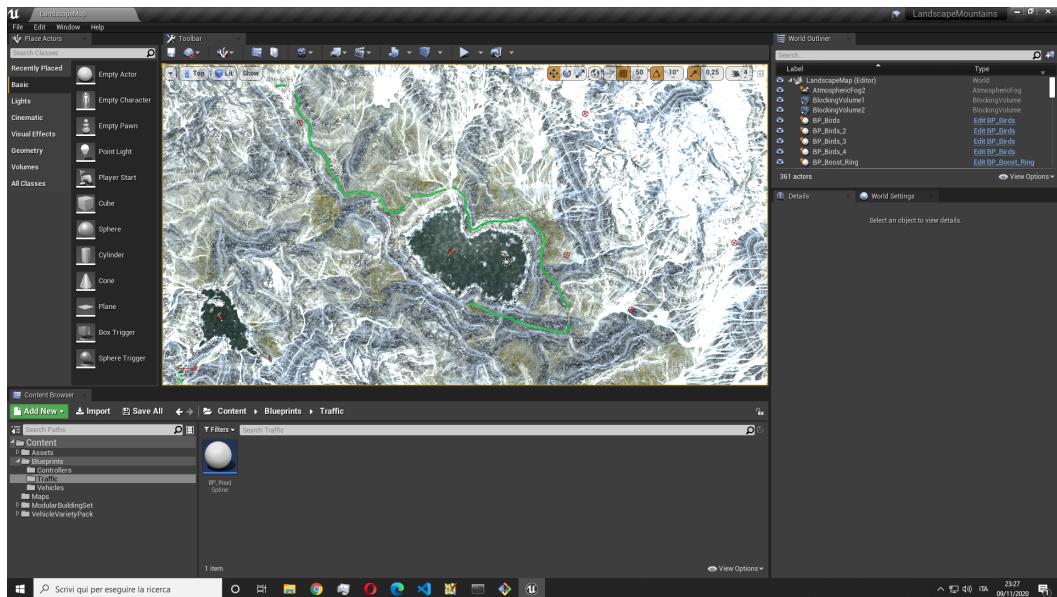


Figure 0.2. Top view of the LandscapeMountain project. The green line represents the street.

Action space for simplified Aerial Vehicle

At initial timestep $t = 0$ each UAV is laying on the ground, positioned inside the respective takeoff zone. Each UAV has associated a takeoff zone which is a rectangular area, not bordering with the others, used to delimit the random initial position for each single UAV inside of it. At the next time steps each drone moves to the nearest point belonging to the line representing the street to be patrolled. When a UAV is positioned over the street it start flying above it, so at each time step it moves and take pictures of the street. In this phase drones can move in 8 directions in order to follow the path of the street in both direction of travel. So the action space will be:

$$A = \{1 (\text{up}), 2 (\text{up-right}), 3 (\text{right}), 4 (\text{down-right}), 5 (\text{down}), 6 (\text{down-left}), 7 (\text{left}), 8 (\text{up-left})\}$$

Each $a \in A$ has specific velocity and angles of motion designed to respect maneuverability constraints.

States and observations

The state $s_i(t) \in S$ for vehicle i at time step t can be defined as so:

$$s_i(t) = (\bar{g}_i(t), F_{i,t}, C_{i,t})$$

where:

- $\bar{g}_i(t) = (x_{i,t}, y_{i,t}, z_{i,t})$, $\bar{g}_i(t)$ are the GPS simulated coordinates at time t for drone i , $x_{i,t}$ is the latitude coordinate, $y_{i,t}$ is the longitude coordinate, $z_{i,t}$ is the height

- $(F_{i,t})_{n \times m} = \begin{bmatrix} p_{0,0} & \dots & p_{0,m-1} \\ \dots & \dots & \dots \\ p_{n-1,0} & \dots & p_{n-1,m-1} \end{bmatrix}$, $F_{i,t}$ is a matrix of $n \times m$ pixels (p) taken by drone i at time t

$$\bullet (C_{i,t})_{N \times N} = \begin{bmatrix} c_{0,0} & \dots & c_{0,N-1} \\ \dots & \dots & \dots \\ c_{N-1,0} & \dots & c_{N-1,N-1} \end{bmatrix},$$

$C_{i,t}$ is the communication matrix associated to instant t for drone i .

$$(c_{u,v})_{u,v=0,\dots,N-1} = \begin{cases} 0 (\text{false}), & \text{if } drone_{u,v} \text{ is outside coverage area of drone } i \\ 1 (\text{true}), & \text{otherwise} \end{cases}$$

. This information, in particular the first and last component ($\bar{g}_i(t)$ and $C_{i,t}$) are used to guide the search to certain areas of the environment and can be consistently updated using sensor information about the environment. The communication matrix $C_{i,t}$ is used to prevent eventual collision and improve cooperation avoiding multiple exploration of the same places in a limited range of time.

Scenario 2: Problem definition and motivation

This scenario keeps the multi agent nature of the problem so as before we have a small number of UAVs that cooperate, now to scan a real world network of streets (or pipelines or transmission lines).

Using GPS and Open data about the locations involved, we will use AirSim simulator to train on a map that will be generated from real data with 3D buildings and streets in the correct positions. GPS coordinates will be used to define paths over the streets (whose location is perfectly known) while 3D generated buildings will be useful to make realistic simulations of eventual collisions and visual obstructions in highly populated urban areas, exploiting the simulated cameras on the UAV.

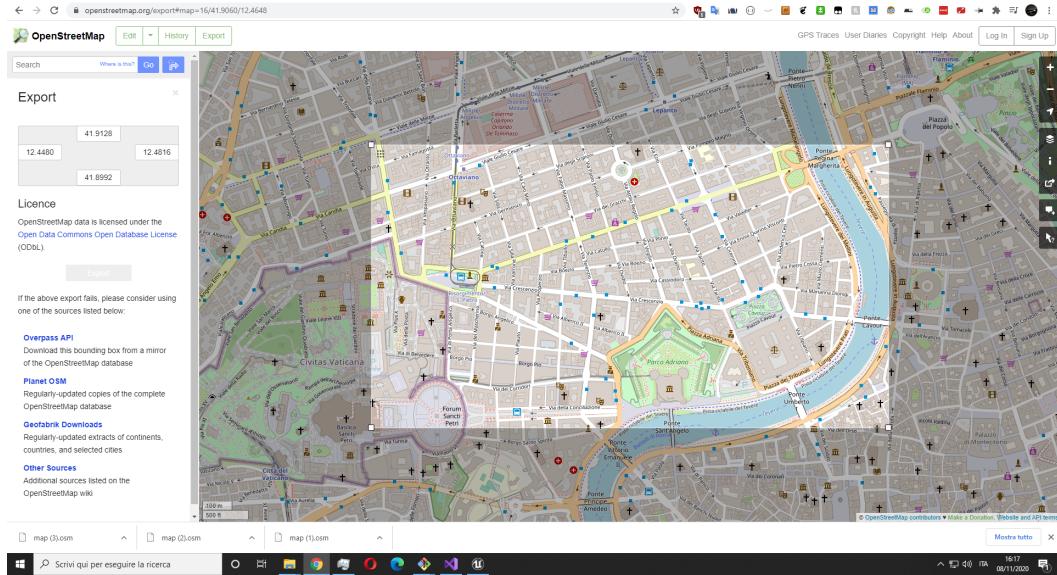


Figure 0.3. OpenStreetMap website, it allows to download the .osm file to be later used as input to build 3D buildings assets.

In this scenario the task could be to cover all the streets in the minimum possible time, considering other possible factors such as different importance assigned to some streets or battery consumption in drones, radio signal coverage ecc...

Environment

We have an environment E , considered as a flat space of dimension $E_x \times E_y$, with the presence of streets considerable as segment connecting GPS positions. 3D buildings are present as obstacles at the margin of the street.

For this scenario too we can think of different initial positions for UAVs, this time they can be extracted from a pool of possible initial positions constrained to be fairly distant one from the others.

Action space

We can keep the formulation of discrete simplified actions for the motion of UAVs. At initial timestep $t = 0$, each UAV is laying on the ground, positioned inside the

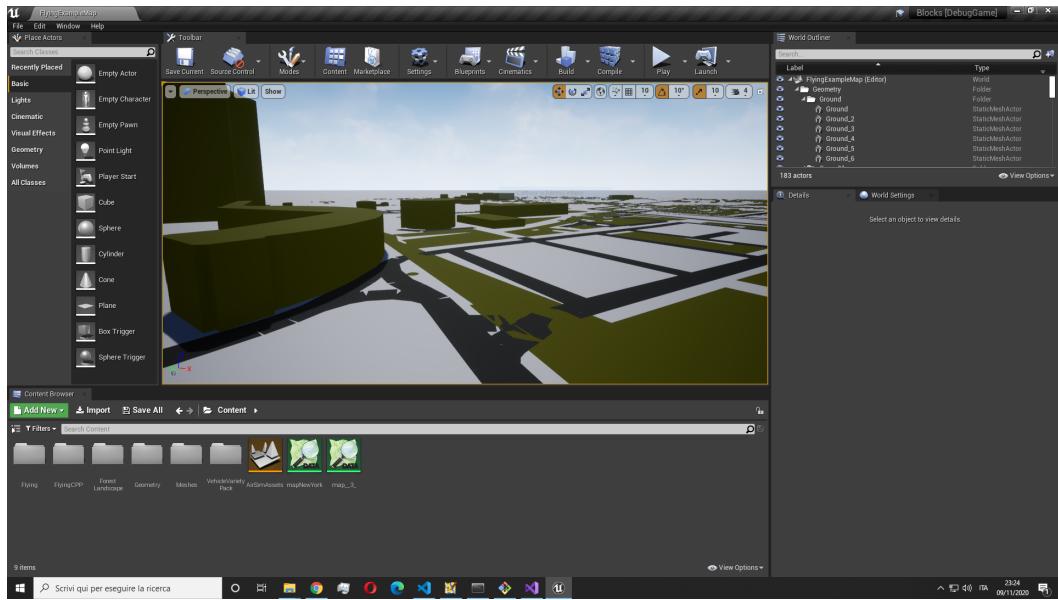


Figure 0.4. Perspective view of the imported 3D assets map.

respective random initial position. At the next time step $t = 1$, each drone moves toward one direction or the other (at random) following the path of the street on which it is. When a UAV is positioned over the street it start flying above it, so at each time step it moves and take pictures of the street. In this phase drones can move in 8 directions in order to follow the path of the street in both direction of travel. So the action space will be:

$$A = \{1 \text{ (up)}, 2 \text{ (up-right)}, 3 \text{ (right)}, 4 \text{ (down-right)}, 5 \text{ (down)}, 6 \text{ (down-left)}, 7 \text{ (left)}, 8 \text{ (up-left)}\}$$

Each $a \in A$ has specific velocity and angles of motion designed to respect maneuverability constraints.

States and observations

For this scenario states can be the GPS positions of all drones timestep t :

$$s(t) = (\bar{g}_0(t), \bar{g}_1(t), \dots, g_{N-1}(t))$$

where $\bar{g}_i(t) = (x_{i,t}, y_{i,t}, z_{i,t})$ for drone i , $x_{i,t}$ is the latitude coordinate, $y_{i,t}$ is the longitude coordinate, $z_{i,t}$ is the height

Chapter 1

Style features of **sapthesis**

In this chapter I will discuss my stylistic choices of **sapthesis**. I will show the page layout geometry and I will describe the page style.

1.1 Page layout

The page is fixed at the dimensions of an A4 paper, therefore you have to print your thesis on A4 paper to obtain the best results. The font dimension is fixed at 11 pt. The text column and the margins are chosen to fill to the best an A4 paper while keeping a reasonable line length (396 pt) for a good readability. The text height and the text width are in golden ratio (~ 1.6180) as well as the outer and inner margins in a two-side document after binding margin removal. Also the top margin (excluding the header) and bottom margin are in the golden ratio. In Fig. 1.1 a sketch of the **sapthesis** page layout is shown.

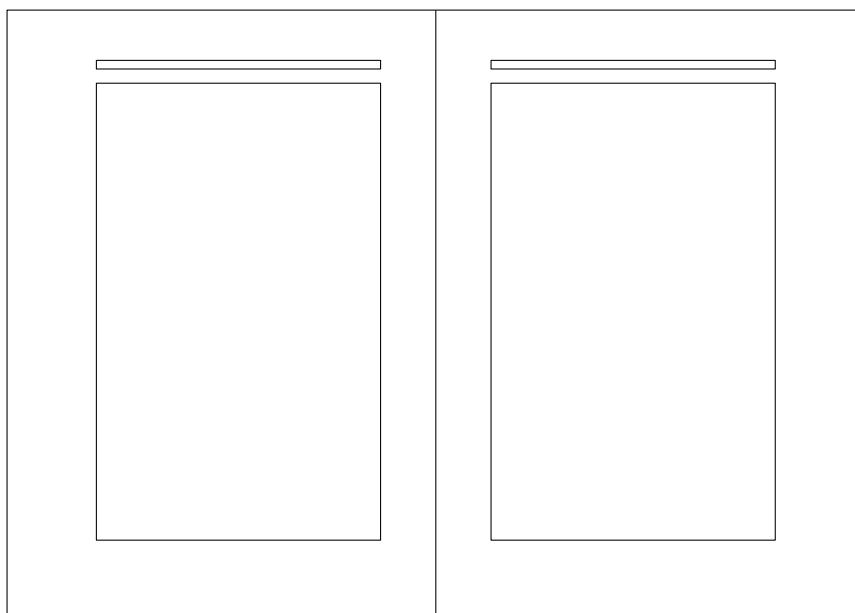


Figure 1.1. Page layout scheme of **sapthesis** class using a zero binding margin.



Figure 1.2. Logo of the Sapienza – University of Rome.

1.2 Page style

The captions have a smaller font respect to the text and the label is in boldface. The appearance of the margin notes has been improved. They have the same font dimension of the footnotes and are typed in italics. Moreover I defined a new command to typeset margin note aligned to the left on the right page and vice versa on the left page. Notice that if a binding margin greater than 1.5 cm is used, the dimensions of the margin notes become too small and very ugly. Do not use them in this case.

The mathematical objects, figures and tables are numbered within the chapters (e.g. 1.1, 1.2,... for the first chapter, 2.1, 2.2 for the second one and so on...). See for example the number of this simple equation

$$x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad (1.1)$$

The title page is automatically composed when the `\maketitle` command is given. The parameters needed for the title page, author, title, etc..., are supplied by dedicated commands explained in the next section. Two copies of the university logo in `pdf` format, one for color printing and the other one for black and white printing, are supplied in the `sapthesis` package. They are shown in Fig. 1.2.

1.3 About figures and tables

As regards the image formats, please use vector images as much as possible! Use `jpg` images only for photographs! `pdflatex` supports the `pdf`, `jpg` and `png` formats.

A very simple table is show in Tab. 1.1. Remember to typeset always the table caption above the table. Do not use vertical lines.

Table 1.1. This is a simple table.

Letter	Test	Test
A	C	E
B	D	F

1.4 A section

In this manual you can skip the gray text because it is just dummy text.

Lorem ipsum dolor sit amet, consectetuer adipiscing elit. Ut purus elit, vestibulum ut, placerat ac, adipiscing vitae, felis. Curabitur dictum gravida mauris. Nam arcu libero, nonummy eget, consectetuer id, vulputate a, magna. Donec vehicula augue eu neque. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Mauris ut leo. Cras viverra metus rhoncus sem. Nulla et lectus vestibulum urna fringilla ultrices. Phasellus eu tellus sit amet tortor gravida placerat. Integer sapien est, iaculis in, pretium quis, viverra ac, nunc. Praesent eget sem vel leo ultrices bibendum. Aenean faucibus. Morbi dolor nulla, malesuada eu, pulvinar at, mollis ac, nulla. Curabitur auctor semper nulla. Donec varius orci eget risus. Duis nibh mi, congue eu, accumsan eleifend, sagittis quis, diam. Duis eget orci sit amet orci dignissim rutrum.

Nam dui ligula, fringilla a, euismod sodales, sollicitudin vel, wisi. Morbi auctor lorem non justo. Nam lacus libero, pretium at, lobortis vitae, ultricies et, tellus. Donec aliquet, tortor sed accumsan bibendum, erat ligula aliquet magna, vitae ornare odio metus a mi. Morbi ac orci et nisl hendrerit mollis. Suspendisse ut massa. Cras nec ante. Pellentesque a nulla. Cum sociis natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Aliquam tincidunt urna. Nulla ullamcorper vestibulum turpis. Pellentesque cursus luctus mauris.

Nulla malesuada porttitor diam. Donec felis erat, congue non, volutpat at, tincidunt tristique, libero. Vivamus viverra fermentum felis. Donec nonummy pellentesque ante. Phasellus adipiscing semper elit. Proin fermentum massa ac quam. Sed diam turpis, molestie vitae, placerat a, molestie nec, leo. Maecenas lacinia. Nam ipsum ligula, eleifend at, accumsan nec, suscipit a, ipsum. Morbi blandit ligula feugiat magna. Nunc eleifend consequat lorem. Sed lacinia nulla vitae enim. Pellentesque tincidunt purus vel magna. Integer non enim. Praesent euismod nunc eu purus. Donec bibendum quam in tellus. Nullam cursus pulvinar lectus. Donec et mi. Nam vulputate metus eu enim. Vestibulum pellentesque felis eu massa.

Quisque ullamcorper placerat ipsum. Cras nibh. Morbi vel justo vitae lacus tincidunt ultrices. Lorem ipsum dolor sit amet, consectetuer adipiscing elit. In hac habitasse platea dictumst. Integer tempus convallis augue. Etiam facilisis. Nunc elementum fermentum wisi. Aenean placerat. Ut imperdiet, enim sed gravida sollicitudin, felis odio placerat quam, ac pulvinar elit purus eget enim. Nunc vitae tortor. Proin tempus nibh sit amet nisl. Vivamus quis tortor vitae risus porta vehicula.

Fusce mauris. Vestibulum luctus nibh at lectus. Sed bibendum, nulla a faucibus semper, leo velit ultricies tellus, ac venenatis arcu wisi vel nisl. Vestibulum diam. Aliquam pellentesque, augue quis sagittis posuere, turpis lacus congue quam, in hen-

drerit risus eros eget felis. Maecenas eget erat in sapien mattis porttitor. Vestibulum porttitor. Nulla facilisi. Sed a turpis eu lacus commodo facilisis. Morbi fringilla, wisi in dignissim interdum, justo lectus sagittis dui, et vehicula libero dui cursus dui. Mauris tempor ligula sed lacus. Duis cursus enim ut augue. Cras ac magna. Cras nulla. Nulla egestas. Curabitur a leo. Quisque egestas wisi eget nunc. Nam feugiat lacus vel est. Curabitur consectetur.

Suspendisse vel felis. Ut lorem lorem, interdum eu, tincidunt sit amet, laoreet vitae, arcu. Aenean faucibus pede eu ante. Praesent enim elit, rutrum at, molestie non, nonummy vel, nisl. Ut lectus eros, malesuada sit amet, fermentum eu, sodales cursus, magna. Donec eu purus. Quisque vehicula, urna sed ultricies auctor, pede lorem egestas dui, et convallis elit erat sed nulla. Donec luctus. Curabitur et nunc. Aliquam dolor odio, commodo pretium, ultricies non, pharetra in, velit. Integer arcu est, nonummy in, fermentum faucibus, egestas vel, odio.

Sed commodo posuere pede. Mauris ut est. Ut quis purus. Sed ac odio. Sed vehicula hendrerit sem. Duis non odio. Morbi ut dui. Sed accumsan risus eget odio. In hac habitasse platea dictumst. Pellentesque non elit. Fusce sed justo eu urna porta tincidunt. Mauris felis odio, sollicitudin sed, volutpat a, ornare ac, erat. Morbi quis dolor. Donec pellentesque, erat ac sagittis semper, nunc dui lobortis purus, quis congue purus metus ultricies tellus. Proin et quam. Class aptent taciti sociosqu ad litora torquent per conubia nostra, per inceptos hymenaeos. Praesent sapien turpis, fermentum vel, eleifend faucibus, vehicula eu, lacus.

Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Donec odio elit, dictum in, hendrerit sit amet, egestas sed, leo. Praesent feugiat sapien aliquet odio. Integer vitae justo. Aliquam vestibulum fringilla lorem. Sed neque lectus, consectetur at, consectetur sed, eleifend ac, lectus. Nulla facilisi. Pellentesque eget lectus. Proin eu metus. Sed porttitor. In hac habitasse platea dictumst. Suspendisse eu lectus. Ut mi mi, lacinia sit amet, placerat et, mollis vitae, dui. Sed ante tellus, tristique ut, iaculis eu, malesuada ac, dui. Mauris nibh leo, facilisis non, adipiscing quis, ultrices a, dui.

Morbi luctus, wisi viverra faucibus pretium, nibh est placerat odio, nec commodo wisi enim eget quam. Quisque libero justo, consectetur a, feugiat vitae, porttitor eu, libero. Suspendisse sed mauris vitae elit sollicitudin malesuada. Maecenas ultricies eros sit amet ante. Ut venenatis velit. Maecenas sed mi eget dui varius euismod. Phasellus aliquet volutpat odio. Vestibulum ante ipsum primis in faucibus orci luctus et ultrices posuere cubilia Curae; Pellentesque sit amet pede ac sem eleifend consectetur. Nullam elementum, urna vel imperdiet sodales, elit ipsum pharetra ligula, ac pretium ante justo a nulla. Curabitur tristique arcu eu metus. Vestibulum lectus. Proin mauris. Proin eu nunc eu urna hendrerit faucibus. Aliquam auctor, pede consequat laoreet varius, eros tellus scelerisque quam, pellentesque hendrerit ipsum dolor sed augue. Nulla nec lacus.

Suspendisse vitae elit. Aliquam arcu neque, ornare in, ullamcorper quis, commodo eu, libero. Fusce sagittis erat at erat tristique mollis. Maecenas sapien libero, molestie et, lobortis in, sodales eget, dui. Morbi ultrices rutrum lorem. Nam elementum ullamcorper leo. Morbi dui. Aliquam sagittis. Nunc placerat. Pellentesque tristique sodales est. Maecenas imperdiet lacinia velit. Cras non urna. Morbi eros pede, suscipit ac, varius vel, egestas non, eros. Praesent malesuada, diam id pretium elementum, eros sem dictum tortor, vel consectetur odio sem sed wisi.

1.5 Another section

In this manual you can skip the gray text because it is just dummy text.

 Lorem ipsum dolor sit amet, consectetuer adipiscing elit. Ut purus elit, vestibulum ut, placerat ac, adipiscing vitae, felis. Curabitur dictum gravida mauris. Nam arcu libero, nonummy eget, consectetuer id, vulputate a, magna. Donec vehicula augue eu neque. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Mauris ut leo. Cras viverra metus rhoncus sem. Nulla et lectus vestibulum urna fringilla ultrices. Phasellus eu tellus sit amet tortor gravida placerat. Integer sapien est, iaculis in, pretium quis, viverra ac, nunc. Praesent eget sem vel leo ultrices bibendum. Aenean faucibus. Morbi dolor nulla, malesuada eu, pulvinar at, mollis ac, nulla. Curabitur auctor semper nulla. Donec varius orci eget risus. Duis nibh mi, congue eu, accumsan eleifend, sagittis quis, diam. Duis eget orci sit amet orci dignissim rutrum.

 Nam dui ligula, fringilla a, euismod sodales, sollicitudin vel, wisi. Morbi auctor lorem non justo. Nam lacus libero, pretium at, lobortis vitae, ultricies et, tellus. Donec aliquet, tortor sed accumsan bibendum, erat ligula aliquet magna, vitae ornare odio metus a mi. Morbi ac orci et nisl hendrerit mollis. Suspendisse ut massa. Cras nec ante. Pellentesque a nulla. Cum sociis natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Aliquam tincidunt urna. Nulla ullamcorper vestibulum turpis. Pellentesque cursus luctus mauris.

 Nulla malesuada porttitor diam. Donec felis erat, congue non, volutpat at, tincidunt tristique, libero. Vivamus viverra fermentum felis. Donec nonummy pellentesque ante. Phasellus adipiscing semper elit. Proin fermentum massa ac quam. Sed diam turpis, molestie vitae, placerat a, molestie nec, leo. Maecenas lacinia. Nam ipsum ligula, eleifend at, accumsan nec, suscipit a, ipsum. Morbi blandit ligula feugiat magna. Nunc eleifend consequat lorem. Sed lacinia nulla vitae enim. Pellentesque tincidunt purus vel magna. Integer non enim. Praesent euismod nunc eu purus. Donec bibendum quam in tellus. Nullam cursus pulvinar lectus. Donec et mi. Nam vulputate metus eu enim. Vestibulum pellentesque felis eu massa.

 Quisque ullamcorper placerat ipsum. Cras nibh. Morbi vel justo vitae lacus tincidunt ultrices. Lorem ipsum dolor sit amet, consectetuer adipiscing elit. In hac habitasse platea dictumst. Integer tempus convallis augue. Etiam facilisis. Nunc elementum fermentum wisi. Aenean placerat. Ut imperdiet, enim sed gravida sollicitudin, felis odio placerat quam, ac pulvinar elit purus eget enim. Nunc vitae tortor. Proin tempus nibh sit amet nisl. Vivamus quis tortor vitae risus porta vehicula.

 Fusce mauris. Vestibulum luctus nibh at lectus. Sed bibendum, nulla a faucibus semper, leo velit ultricies tellus, ac venenatis arcu wisi vel nisl. Vestibulum diam. Aliquam pellentesque, augue quis sagittis posuere, turpis lacus congue quam, in hendrerit risus eros eget felis. Maecenas eget erat in sapien mattis porttitor. Vestibulum porttitor. Nulla facilisi. Sed a turpis eu lacus commodo facilisis. Morbi fringilla, wisi in dignissim interdum, justo lectus sagittis dui, et vehicula libero dui cursus dui. Mauris tempor ligula sed lacus. Duis cursus enim ut augue. Cras ac magna. Cras nulla. Nulla egestas. Curabitur a leo. Quisque egestas wisi eget nunc. Nam feugiat lacus vel est. Curabitur consectetur.

 Suspendisse vel felis. Ut lorem lorem, interdum eu, tincidunt sit amet, laoreet

vitae, arcu. Aenean faucibus pede eu ante. Praesent enim elit, rutrum at, molestie non, nonummy vel, nisl. Ut lectus eros, malesuada sit amet, fermentum eu, sodales cursus, magna. Donec eu purus. Quisque vehicula, urna sed ultricies auctor, pede lorem egestas dui, et convallis elit erat sed nulla. Donec luctus. Curabitur et nunc. Aliquam dolor odio, commodo pretium, ultricies non, pharetra in, velit. Integer arcu est, nonummy in, fermentum faucibus, egestas vel, odio.

Sed commodo posuere pede. Mauris ut est. Ut quis purus. Sed ac odio. Sed vehicula hendrerit sem. Duis non odio. Morbi ut dui. Sed accumsan risus eget odio. In hac habitasse platea dictumst. Pellentesque non elit. Fusce sed justo eu urna porta tincidunt. Mauris felis odio, sollicitudin sed, volutpat a, ornare ac, erat. Morbi quis dolor. Donec pellentesque, erat ac sagittis semper, nunc dui lobortis purus, quis congue purus metus ultricies tellus. Proin et quam. Class aptent taciti sociosqu ad litora torquent per conubia nostra, per inceptos hymenaeos. Praesent sapien turpis, fermentum vel, eleifend faucibus, vehicula eu, lacus.

Appendix A

Special commands provided by sapthesis

Sapthesis provides some special commands, particularly useful for scientific works. You can use for example the roman shape, instead of the italic, for the imaginary unit (`\iu`) and Napier's number (`\eu`):

$$e^{i\pi} + 1 = 0 \quad (\text{A.1})$$

There are also two commands to speed up the writing of derivatives. In the following example we have used the commands `\der` and `\pder`):

$$\frac{\partial f}{\partial x} \quad \frac{\partial^2 f}{\partial y^2} \quad (\text{A.2})$$

Sapthesis provides also 4 commands to improve the writing of subscripts, `\rb` and `\tb`, and superscripts, `\rp` and `\tp`. Two of these commands, `\rb` and `\rp`, can be used both in text and in math mode and compose their argument in roman. The other two, `\tb` and `\tp`, can be used only in text mode and compose their argument as are. Here it is an usage example of `\rb` and `\rp`:

$$a_b \neq a_{\mathbf{b}} \quad a^b \neq a^{\mathbf{b}}$$

And here it is an usage example of `\tb`: *Cu_{It}* indicates copper bought in Italy. And a usage example of `\ts`: *Cher G^{le} Napoléon*.

Then several commands for the correct typesetting of unit of measurements are provided. For example the command `\un` typesets its argument in roman and leaves a thin space between the number and the unit: 25 m, 3.5 m/s. Other commands are: (`\g`) 45°, (`\c`) 30 °C, (`\a`) 12 Å, (`\micro`) 40 µm, (`\ohm`) 27 Ω.

We have also `\x` as abbreviation of `\times`: \$7 \x 10^5\$ gives 7×10^5 . Then `\di` is the differential symbol which automatically insert the correct spacing.

$$\int x \, dx$$

Finally we have defined the color `sapred` which is the official color of Sapienza – University of Rome. It is defined as RGB(130,36,51). This text is written with the color `sapred`.

In the following dummy text you can observe the usage of `\mnote` command which typesets fancy margin notes.

 Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut purus elit, vestibulum ut, placerat ac, adipiscing vitae, felis. Curabitur dictum gravida mauris. Nam arcu libero, nonummy eget, consectetur id, vulputate a, magna. Donec vehicula augue eu neque. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Mauris ut leo. Cras viverra metus rhoncus sem. Nulla et lectus vestibulum urna fringilla ultrices. Phasellus eu tellus sit amet tortor gravida placerat. Integer sapien est, iaculis in, pretium quis, viverra ac, nunc. Praesent eget sem vel leo ultrices bibendum. Aenean faucibus. Morbi dolor nulla, malesuada eu, pulvinar at, mollis ac, nulla. Curabitur auctor semper nulla. Donec varius orci eget risus. Duis nibh mi, congue eu, accumsan eleifend, sagittis quis, diam. Duis eget orci sit amet orci dignissim rutrum.

 Nam dui ligula, fringilla a, euismod sodales, sollicitudin vel, wisi. Morbi auctor lorem non justo. Nam lacus libero, pretium at, lobortis vitae, ultricies et, tellus. Donec aliquet, tortor sed accumsan bibendum, erat ligula aliquet magna, vitae ornare odio metus a mi. Morbi ac orci et nisl hendrerit mollis. Suspendisse ut massa. Cras nec ante. Pellentesque a nulla. Cum sociis natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Aliquam tincidunt urna. Nulla ullamcorper vestibulum turpis. Pellentesque cursus luctus mauris.

 Nulla malesuada porttitor diam. Donec felis erat, congue non, volutpat at, tincidunt tristique, libero. Vivamus viverra fermentum felis. Donec nonummy pellentesque ante. Phasellus adipiscing semper elit. Proin fermentum massa ac quam. Sed diam turpis, molestie vitae, placerat a, molestie nec, leo. Maecenas lacinia. Nam ipsum ligula, eleifend at, accumsan nec, suscipit a, ipsum. Morbi blandit ligula feugiat magna. Nunc eleifend consequat lorem. Sed lacinia nulla vitae enim. Pellentesque tincidunt purus vel magna. Integer non enim. Praesent euismod nunc eu purus. Donec bibendum quam in tellus. Nullam cursus pulvinar lectus. Donec et mi. Nam vulputate metus eu enim. Vestibulum pellentesque felis eu massa.

 Quisque ullamcorper placerat ipsum. Cras nibh. Morbi vel justo vitae lacus tincidunt ultrices. Lorem ipsum dolor sit amet, consectetur adipiscing elit. In hac habitasse platea dictumst. Integer tempus convallis augue. Etiam facilisis. Nunc elementum fermentum wisi. Aenean placerat. Ut imperdiet, enim sed gravida sollicitudin, felis odio placerat quam, ac pulvinar elit purus eget enim. Nunc vitae tortor. Proin tempus nibh sit amet nisl. Vivamus quis tortor vitae risus porta vehicula.

 Fusce mauris. Vestibulum luctus nibh at lectus. Sed bibendum, nulla a faucibus semper, leo velit ultricies tellus, ac venenatis arcu wisi vel nisl. Vestibulum diam. Aliquam pellentesque, augue quis sagittis posuere, turpis lacus congue quam, in hendrerit risus eros eget felis. Maecenas eget erat in sapien mattis porttitor. Vestibulum porttitor. Nulla facilisi. Sed a turpis eu lacus commodo facilisis. Morbi fringilla, wisi in dignissim interdum, justo lectus sagittis dui, et vehicula libero dui cursus dui. Mauris tempor ligula sed lacus. Duis cursus enim ut augue. Cras ac magna. Cras nulla. Nulla egestas. Curabitur a leo. Quisque egestas wisi eget nunc. Nam feugiat lacus vel est. Curabitur consectetur.

 Suspendisse vel felis. Ut lorem lorem, interdum eu, tincidunt sit amet, laoreet vitae, arcu. Aenean faucibus pede eu ante. Praesent enim elit, rutrum at, molestie

non, nonummy vel, nisl. Ut lectus eros, malesuada sit amet, fermentum eu, sodales cursus, magna. Donec eu purus. Quisque vehicula, urna sed ultricies auctor, pede lorem egestas dui, et convallis elit erat sed nulla. Donec luctus. Curabitur et nunc. Aliquam dolor odio, commodo pretium, ultricies non, pharetra in, velit. Integer arcu est, nonummy in, fermentum faucibus, egestas vel, odio.

Sed commodo posuere pede. Mauris ut est. Ut quis purus. Sed ac odio. Sed vehicula hendrerit sem. Duis non odio. Morbi ut dui. Sed accumsan risus eget odio. In hac habitasse platea dictumst. Pellentesque non elit. Fusce sed justo eu urna porta tincidunt. Mauris felis odio, sollicitudin sed, volutpat a, ornare ac, erat. Morbi quis dolor. Donec pellentesque, erat ac sagittis semper, nunc dui lobortis purus, quis congue purus metus ultricies tellus. Proin et quam. Class aptent taciti sociosqu ad litora torquent per comubia nostra, per inceptos hymenaeos. Praesent sapien turpis, fermentum vel, eleifend faucibus, vehicula eu, lacus.

This is a fancy margin note!

Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut purus elit, vestibulum ut, placerat ac, adipiscing vitae, felis. Curabitur dictum gravida mauris. Nam arcu libero, nonummy eget, consectetur id, vulputate a, magna. Donec vehicula augue eu neque. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Mauris ut leo. Cras viverra metus rhoncus sem. Nulla et lectus vestibulum urna fringilla ultrices. Phasellus eu tellus sit amet tortor gravida placerat. Integer sapien est, iaculis in, pretium quis, viverra ac, nunc. Praesent eget sem vel leo ultrices bibendum. Aenean faucibus. Morbi dolor nulla, malesuada eu, pulvinar at, mollis ac, nulla. Curabitur auctor semper nulla. Donec varius orci eget risus. Duis nibh mi, congue eu, accumsan eleifend, sagittis quis, diam. Duis eget orci sit amet orci dignissim rutrum.

Nam dui ligula, fringilla a, euismod sodales, sollicitudin vel, wisi. Morbi auctor lorem non justo. Nam lacus libero, pretium at, lobortis vitae, ultricies et, tellus. Donec aliquet, tortor sed accumsan bibendum, erat ligula aliquet magna, vitae ornare odio metus a mi. Morbi ac orci et nisl hendrerit mollis. Suspendisse ut massa. Cras nec ante. Pellentesque a nulla. Cum sociis natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Aliquam tincidunt urna. Nulla ullamcorper vestibulum turpis. Pellentesque cursus luctus mauris.

Nulla malesuada porttitor diam. Donec felis erat, congue non, volutpat at, tincidunt tristique, libero. Vivamus viverra fermentum felis. Donec nonummy pellentesque ante. Phasellus adipiscing semper elit. Proin fermentum massa ac quam. Sed diam turpis, molestie vitae, placerat a, molestie nec, leo. Maecenas lacinia. Nam ipsum ligula, eleifend at, accumsan nec, suscipit a, ipsum. Morbi blandit ligula feugiat magna. Nunc eleifend consequat lorem. Sed lacinia nulla vitae enim. Pellentesque tincidunt purus vel magna. Integer non enim. Praesent euismod nunc eu purus. Donec bibendum quam in tellus. Nullam cursus pulvinar lectus. Donec et mi. Nam vulputate metus eu enim. Vestibulum pellentesque felis eu massa.

Quisque ullamcorper placerat ipsum. Cras nibh. Morbi vel justo vitae lacus tincidunt ultrices. Lorem ipsum dolor sit amet, consectetur adipiscing elit. In hac habitasse platea dictumst. Integer tempus convallis augue. Etiam facilisis. Nunc elementum fermentum wisi. Aenean placerat. Ut imperdiet, enim sed gravida sollicitudin, felis odio placerat quam, ac pulvinar elit purus eget enim. Nunc vitae tortor. Proin tempus nibh sit amet nisl. Vivamus quis tortor vitae risus porta vehicula.

Fusce mauris. Vestibulum luctus nibh at lectus. Sed bibendum, nulla a faucibus semper, leo velit ultricies tellus, ac venenatis arcu wisi vel nisl. Vestibulum diam. Aliquam pellentesque, augue quis sagittis posuere, turpis lacus congue quam, in hendrerit risus eros eget felis. Maecenas eget erat in sapien mattis porttitor. Vestibulum porttitor. Nulla facilisi. Sed a turpis eu lacus commodo facilisis. Morbi fringilla, wisi in dignissim interdum, justo lectus sagittis dui, et vehicula libero dui cursus dui. Mauris tempor ligula sed lacus. Duis cursus enim ut augue. Cras ac magna. Cras nulla. Nulla egestas. Curabitur a leo. Quisque egestas wisi eget nunc. Nam feugiat lacus vel est. Curabitur consectetur.

Suspendisse vel felis. Ut lorem lorem, interdum eu, tincidunt sit amet, laoreet vitae, arcu. Aenean faucibus pede eu ante. Praesent enim elit, rutrum at, molestie non, nonummy vel, nisl. Ut lectus eros, malesuada sit amet, fermentum eu, sodales cursus, magna. Donec eu purus. Quisque vehicula, urna sed ultricies auctor, pede lorem egestas dui, et convallis elit erat sed nulla. Donec luctus. Curabitur et nunc. Aliquam dolor odio, commodo pretium, ultricies non, pharetra in, velit. Integer arcu est, nonummy in, fermentum faucibus, egestas vel, odio.

Sed commodo posuere pede. Mauris ut est. Ut quis purus. Sed ac odio. Sed vehicula hendrerit sem. Duis non odio. Morbi ut dui. Sed accumsan risus eget odio. In hac habitasse platea dictumst. Pellentesque non elit. Fusce sed justo eu urna porta tincidunt. Mauris felis odio, sollicitudin sed, volutpat a, ornare ac, erat. Morbi quis dolor. Donec pellentesque, erat ac sagittis semper, nunc dui lobortis purus, quis congue purus metus ultricies tellus. Proin et quam. Class aptent taciti sociosqu ad litora torquent per conubia nostra, per inceptos hymenaeos. Praesent sapien turpis, fermentum vel, eleifend faucibus, vehicula eu, lacus.