

**In-tutorial exercise sheet 4**  
**supporting the lecture Mathematical Statistics**  
(Discussion in the tutorial on 25. November 2015)

**Exercise 1.**

Let  $X \sim \text{Bin}(n, p)$  having density

$$f(k, p) = \binom{n}{k} p^k (1-p)^{n-k}, \quad k = 0, 1, \dots, n.$$

with respect to the counting measure on  $\mathbb{N}_0$ . Determine the maximum-likelihood estimator for  $p \in [0, 1]$ .

- a) Argue why instead of maximizing  $f(X, p)$  one can instead maximize  $\log(f(X, p))$  over  $p$ .
- b) Determine the maximum of  $\log(f(X, p))$ .
- c) Define an estimator for  $p$  using the method of moments.

**Exercise 2.**

Let  $X_1, \dots, X_n$  i.i.d  $\sim f$  with Lebesgue density  $f$ . Determine the density of

$$Z := \max\{X_1, \dots, X_n\}.$$

*Hint:* Start with calculating the distribution function of  $Z$  and then use it to identify the density.