InfoSeminar



Chapter 15 Representation Learning

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2017.01.16

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 - 11.2 Transfer Learning and Domain Adaptation
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 - 11.6 Providing Clues to Discover Underlying Causes

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- Introduction of supervised(SL) and unsupervised learning(UL)
- Representation
- Clustering
- K-means
- Gaussian Mixture Model
- EM algorithm
- Practical example

Unsupervised Pre-training(UP)

Details

- Learning without labelling
- Learning only once before joint training
- Regularizer or parameter init that reduces test error

Basic idea of UP

- Features from UP are also useful for SL by using representation
- To draw a car, you need to the number of wheels

Property of UP

- Because it is not mathematically well-defined,
 the way to benefit from UL is not well defined
- The results of whether pretraining is good or bad
- On average, pretraining is slightly detrimental
- But it can be a significant help in many tasks
- You need to understand when and why it works,
 So you can use UL properly

Background of UP

- This way of learning has been recognized for years as a way of learning about in-depth networks since 2006
- But it is rarely used later.
- The reason for this is that as of 2010
- ReLU, dropout, maxout, data augmentation and deterministic batch normalization methods are introduced
- It is possible to get better performance by SL without using UP

Pros of unsupervised pre-training(UP)

Shared representations

- To handle multiple domains
- To transfer learned knowledge to many other tasks

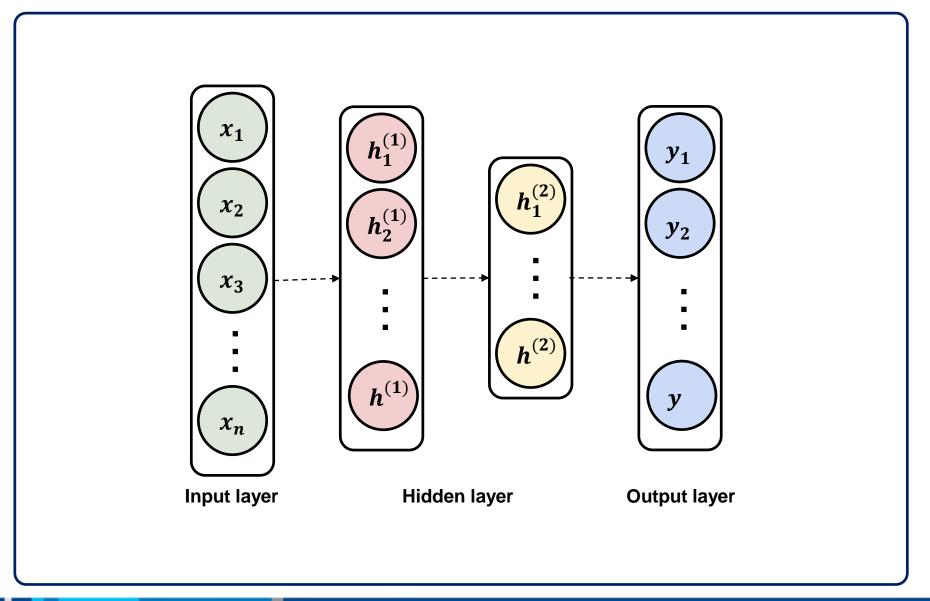
Data sets used

- In order to learn neural network, many data are needed
- However, there are many data which do not have label but little label data
- In this case, it is possible to pre-train each layer

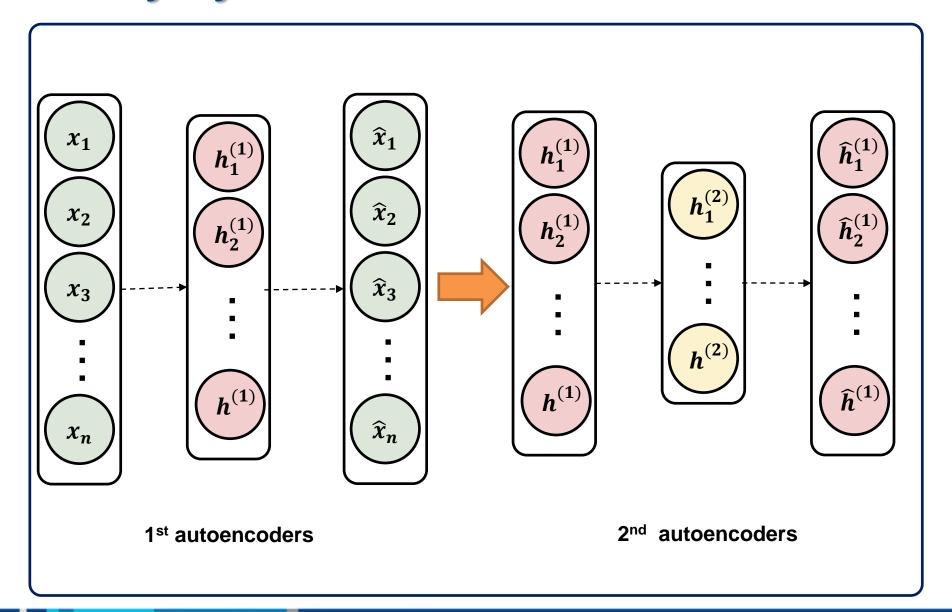
Greedy layer-wise UP in the book

- UL per a single layer basis
- Greedy
 - It progresses by layer
- Pretraining
 - It runs only once before joint training
- Regularizer or parameter init that reduces test error

Pre-training for deep neural network example



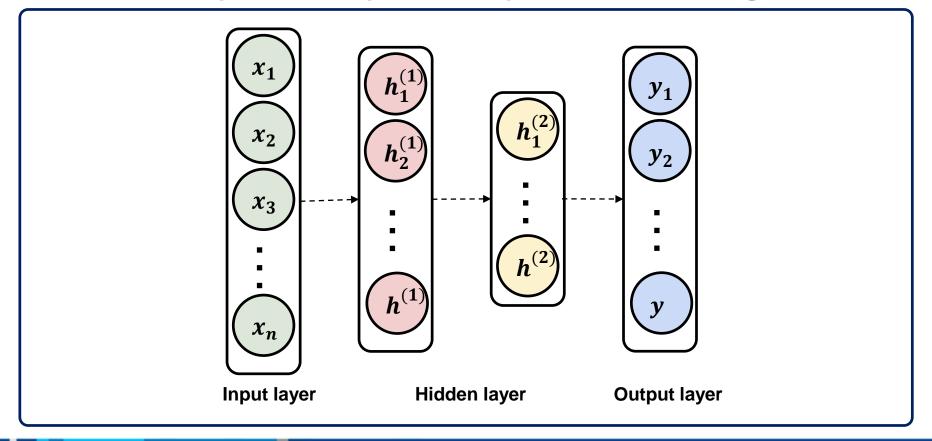
Greedy layer-wise UP



Combining layers after pre-training

After combining layers

- The parameters for each layer have been determined
- It is then possible to perform supervised fine-tuning



Introduction of SL and UL

Supervised Learning

- Classification

A classification problem is when the output variable is a category, such as "red" or "blue" or "disease" and "no disease"

- Regression

A regression problem is when the output variable is a real value, such as "dollars" or "weight"

Unsupervised Learning

- Clustering

It is where you want to discover the inherent groupings in the data, such as grouping customers by purchasing behavior

Introduction of SL and UL

Supervised Learning

- Let's say you are a real estate agent

Bedrooms	Sq. feet	Neighborhood	Sale price
3	2000	Normaltown	\$250,000
2	800	Hipsterton	\$300,000
2	850	Normaltown	\$150,000
1	550	Normaltown	\$78,000
4	2000	Skid Row	\$150,000
Bedrooms	Sq. feet	Neighborhood	Sale price
3	2000	Hipsterton	???

Supervised Learning

Let's solve the problem with solutions(labels)

Math Quiz #1 - Teacher's Answer Key

$$3) 2 2 1 = 3$$

Unsupervised Learning

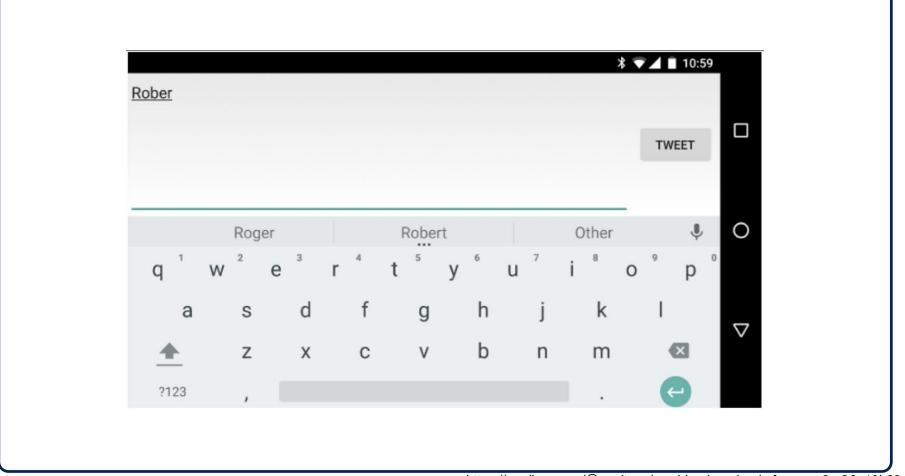
- I don't know what these numbers mean but maybe you(computer) can figure out
- Goal
 - modeling the underlying structure or distribution in the data in order to learn more about the data

Math Quiz #1 - Teacher's Answer Key

$$3) 2 2 1 =$$

Predicting the next letter in Phone keyboard

One cool use might be auto-predict for a phone keyboard



Predicting the next letter in a story

As we just start to train the RNN, after a 100 train loops

hjCTCnhoofeoxelif edElobe negnk e iohehasenoldndAmdaI ayio pe e h'e btentmuhgehi bcgdltt. gey heho grpiahe. Ddelnss.eelaishaner" cot AAfhB ht ltny ehbih a"on bhnte ectrsnae abeahngy amo k ns aeo?cdse nh a taei.rairrhelardr er deffijha

After about 1000 iterations

hing soor ither. And the caraos, and the crowebel for figttier and ale the room of me? Streat was not to him Bill-stook of the momansbed mig out ust on the bull, out here. I been soms inick stalling that aid. "Hon't me and acrained on .Hw's don't you for the roed," In's pair."

After several thousand more iterations, it looks pretty good

He went over to the gate of the café. It was like a country bed.

"Do you know it's been me."

"Damned us," Bill said.

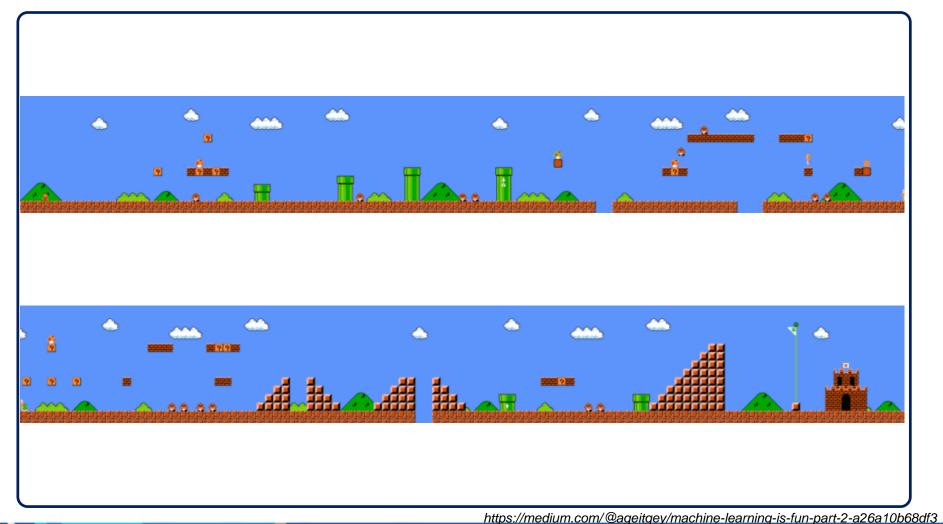
"I was dangerous," I said. "You were she did it and think I would a fine cape you,"

I said.

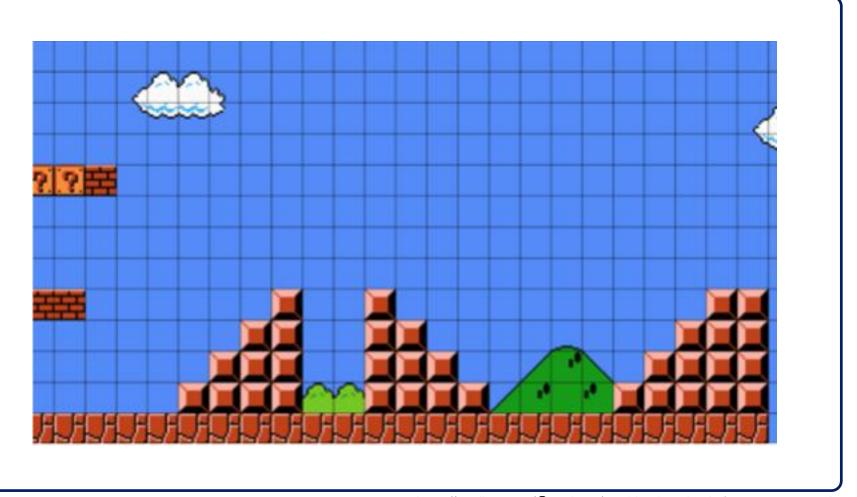
Making Mario without actually Making Mario



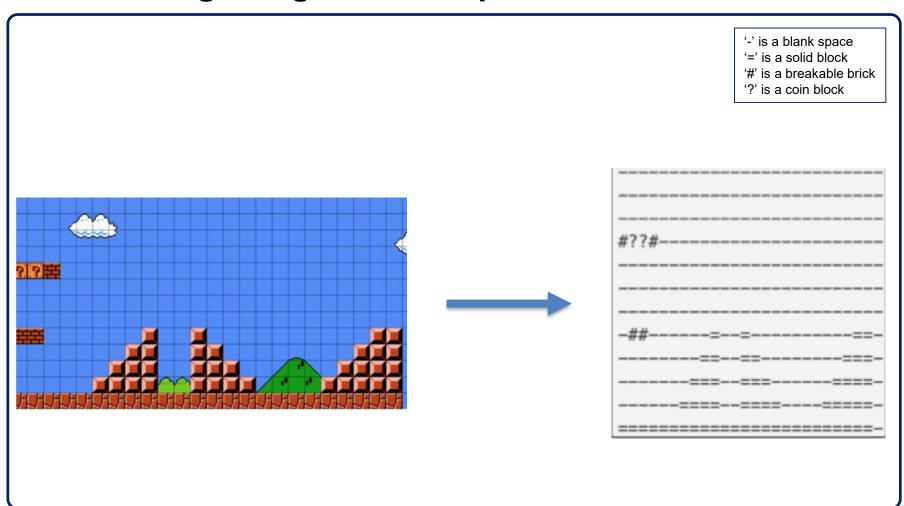
The first level from the game



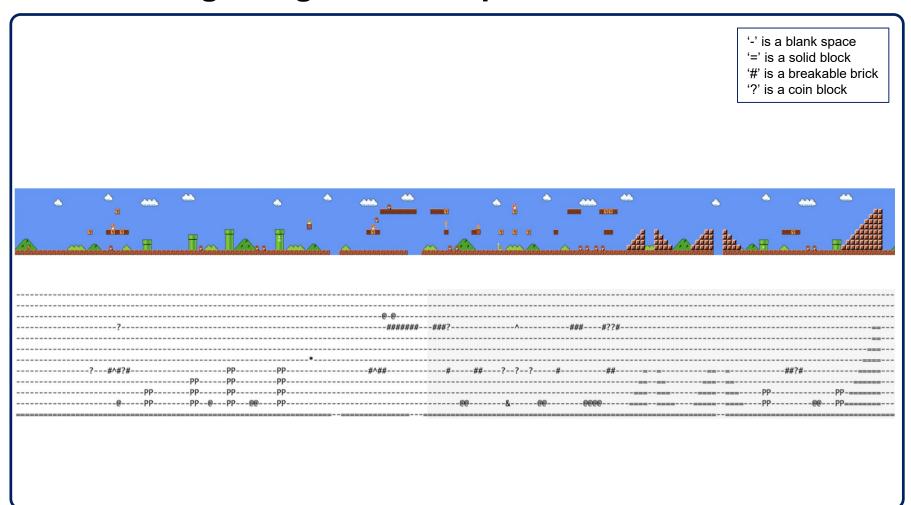
Simple grid of objects



Converting this grid as a sequence of characters

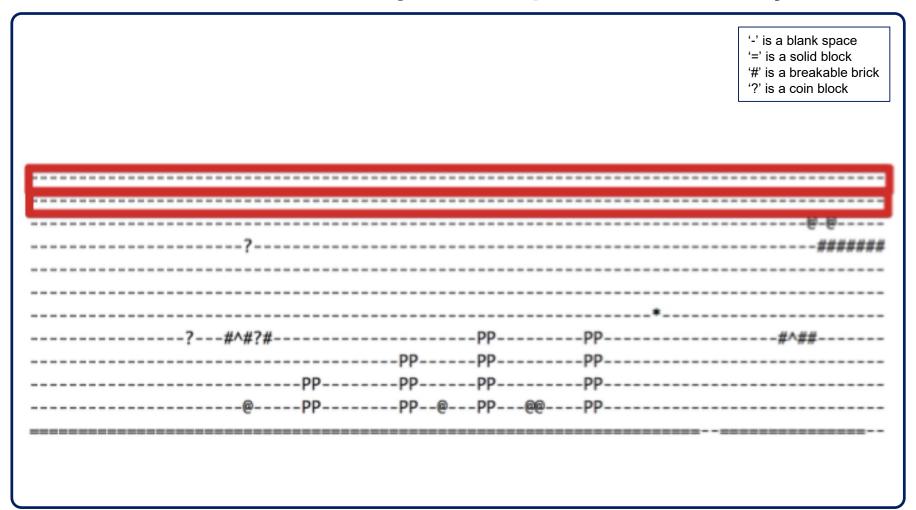


Converting this grid as a sequence of characters



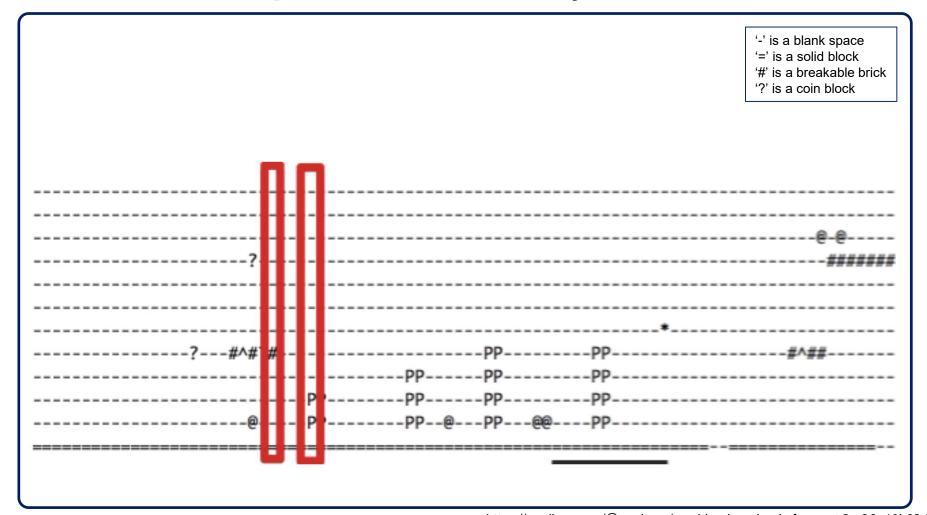
Patterns

Mario levels don't really have a pattern in row-by-row



Patterns

There's a real pattern in column-by-column



Generating mario level

After a little training, our model is generating junk

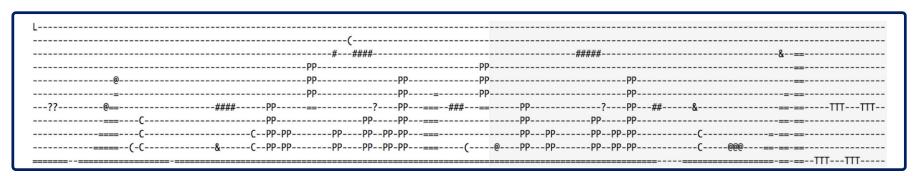
- After several thousand iterations
 - The model has almost figured out that each line should be the same length.
 - It has even started to figure out some of the logic of Mario
 - The pipes in mario are two blocks wide and at least two blocks high, so the "P"s in the data should appear in 2x2 clusters



Generating mario level

With a lot more training

- It put a Lakitu (the monster that floats on a cloud) up in the sky at the beginning of the level—just like in a real Mario level.
- It knows that pipes floating in the air should be resting on top of solid blocks and not just hanging in the air.
- It places enemies in logical places.
- It doesn't create anything that would block a player from moving forward.
- It feels like a real level from Super Mario Bros. 1



- This model is generated from very little data
- There just aren't enough levels in the Mario game
- With the thousands of user-created levels, we could make an amazing model.
- The difference between a good and a bad program
 - How much data you have to train your models

Unsupervised pre-training(UP)

Details

- Learning without labelling
- Learning only once before joint training
- Regularizer or parameter init that reduces test error

Basic idea of UP

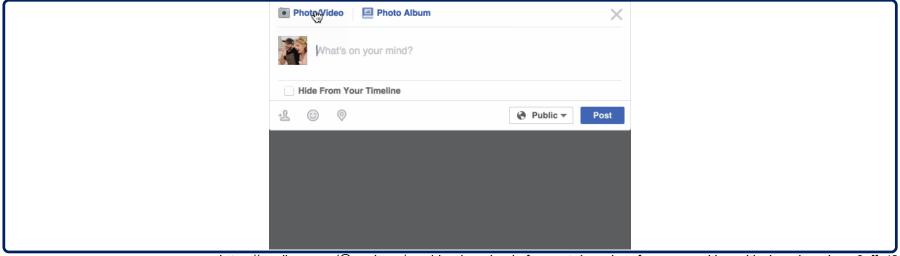
- Features from UP are also useful for SL by using representation
- To draw a car, you need to the number of wheels

Representation

- Information processing becomes easy or difficult
 - Depending on how information is represented
- Numbers are easy to divide
 - But difficult if they are romanized
- Good representation makes it easy to follow up
- Neural network learns how to represent
- The previous steps learn how to express
 - To the last softmax classifier
- Many representation learning faces a tradeoff
 - Between preserving information and obtaining good attributes

Face recognition

- Taging everyone for you like magic by Facebook
- Recognizing your friends' faces
 after they have been tagged only a few times.
- 98% accuracy which is much as good as humans can do!
- Pushing this tech to the limit to solve a challenging problem
 - Will Ferrell apart from Chad Smith



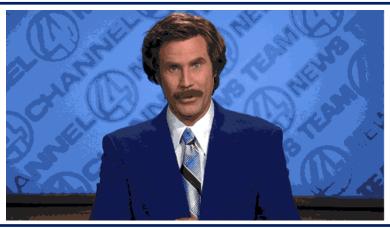
Face recognition

They are different people!



https://medium.com/@ageitgey/machine-learning-is-fun-part-4-modern-face-recognition-with-deep-learning-c3cffc121d78

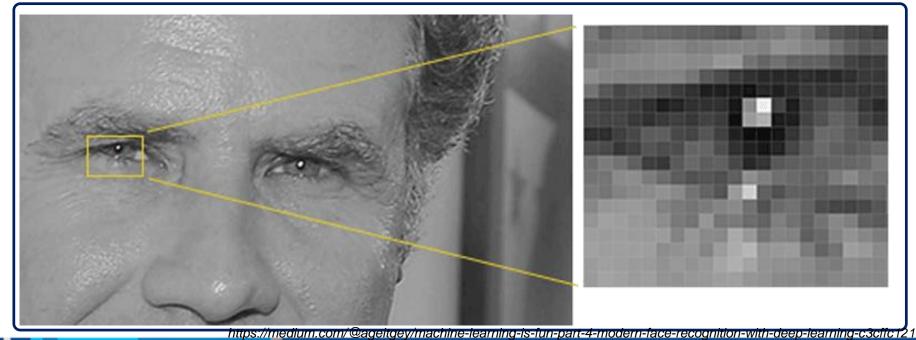
- 1: Look at a picture and find all the faces in it
- 2: Focus on each face and be able to understand that
 - Even if a face is turned in a weird direction or in bad lighting, it is still the same person.
- 3: Pick out unique features of the face
 - You can use to tell it apart from other people
- 4: Compare the unique features of that face to all the people



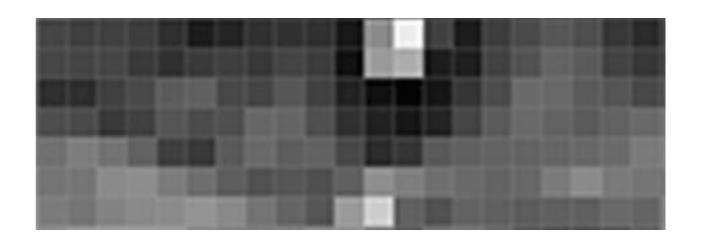
- To find faces in an image
 - we'll start by making our image black and white because we don't need color data to find faces



- For every single pixel, look at the pixels that surrounding it
- Our goal
 - Figuring out how dark the current pixel
 - Then we want to draw an arrow showing in which direction the image is getting darker



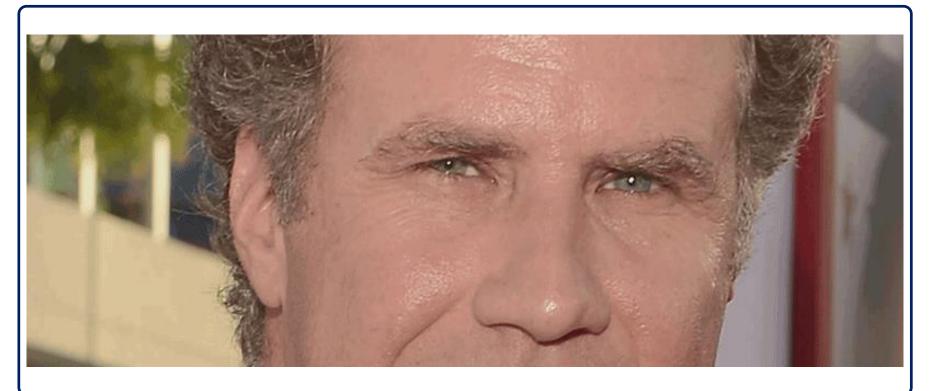
- Every pixel is replaced by an arrow
- These arrows are called gradients
- They show the flow from light to dark



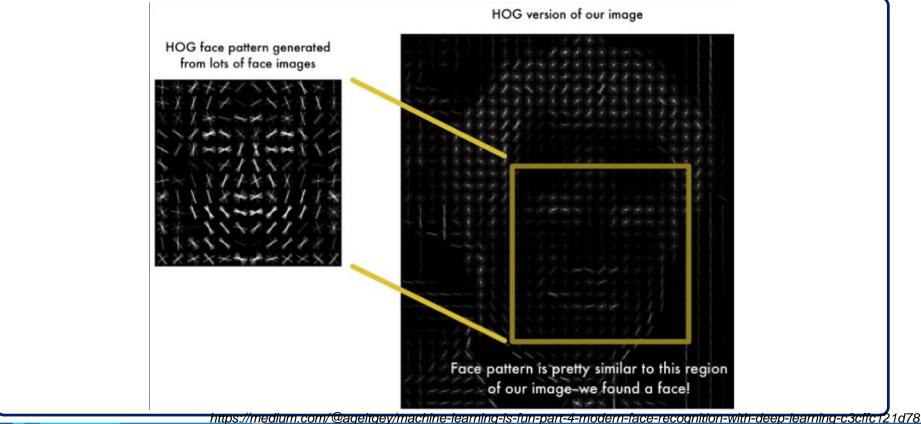
- There's a reason for replacing the pixels with gradients
 - If we analyze pixels directly, dark images and light images of the same person will have different pixel values
- But saving the gradient for every single pixel
 - Too much detail
 - Missing the forest for the trees



- Breaking up the image into squares of 16x16 pixels each
- The end result is we turn the original image
 - Into a very simple representation

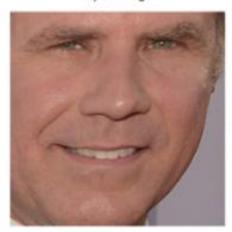


- To find faces in this HOG image
 - Find the part of our image that looks the most similar to a known HOG pattern that was extracted from other faces



- There's actually a huge problem with that approach
 - That would take way too long
 - They need to be able to recognize faces in milliseconds, not hours
- What we need is a way to extract a few measurements from each face
 - The size of each ear, the space between the eyes, etc.
- After repeating this step millions of times for millions of images of thousands of different people
 - The neural network learns to reliably generate 128 measurements for each person
 - Machine learning people call the 128 measurements of each face an embedding

Input Image

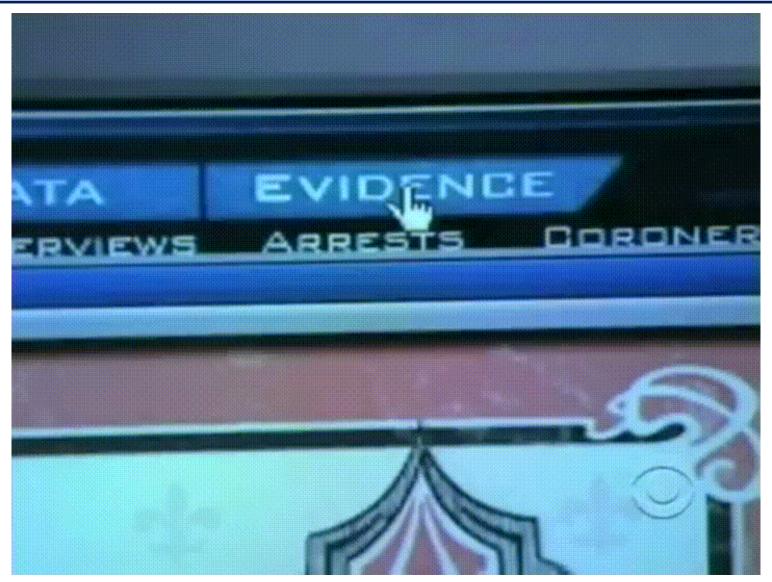


0.097496084868908 0.12529824674129 0.030809439718723 0.036050599068403 -0.097486883401871 -0.0066401711665094 -0.14131525158882 -0.048540540039539 -0.12567175924778 -0.061418771743774 0.046741496771574 -0.12113650143147 0.061606746166945 0.061989940702915 0.10904195904732 -0.019414527341723 0.15245945751667 -0.12216668576002 0.083934605121613 0.087945111095905 -0.021407851949334 -0.018298890441656 -0.011014151386917 0.0093679334968328 0.058139257133007 -0.024210374802351 -0.057223934680223 0.023535015061498 -0.0098039731383324 0.020220354199409 0.0040337680839002 0.051597066223621

128 Measurements Generated from Image

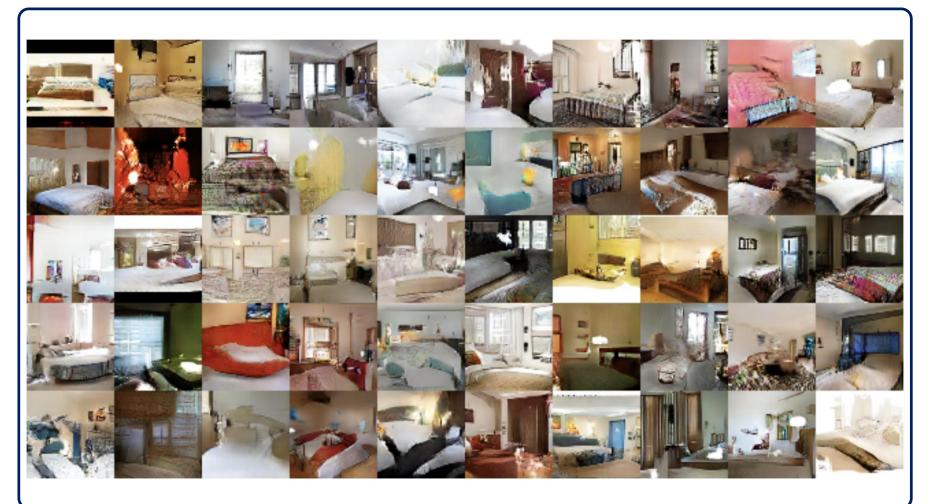
0.045223236083984 0.060309179127216 -0.01981477253139 0.065554238855839 0.1226262897253 0.036750309169292 0.14114324748516 -0.061901587992907 -0.10568545013666 -0.074287034571171 0.0061761881224811 -0.21055991947651 0.11345765739679 0.19372203946114 0.084853030741215 0.0064811296761036 -0.16582328081131 -0.0072777755558491 -0.059730969369411 0.11478432267904 0.14841195940971 0.049525424838066 -0.051016297191381 -0.062812767922878 0.0048638740554452 -0.11443792283535 0.014683869667351 -0.081752359867096 0.037022035568953 0.12788131833076 -0.094398014247417 -0.10034311562777

-0.1281466782093 0.17521631717682 0.10801389068365 0.0731306001544 -0.029626874253154 -0.15958009660244 -0.031351584941149 -0.15042643249035 -0.12728653848171 -0.065365232527256 0.14746543765068 0.0041091227903962 0.021352224051952 -0.086726233363152 0.09463594853878 0.21180312335491 -0.035577941685915 -0.036901291459799 -0.070026844739914 -0.089621491730213 0.078333757817745 0.13227833807468 -0.14132921397686 -0.13407498598099 -0.039491076022387 0.071997955441475 0.05228154733777 -0.031709920614958 0.11009479314089 0.18632389605045 -0.11768248677254 -0.040977258235216 0.032084941864014 0.020976085215807 -0.00052163278451189 -0.1318951100111 -0.0059557510539889 0.043374512344599 -0.053343612700701 0.078198105096817 -0.076289616525173 0.12369467318058 0.056418422609568 0.089727647602558 -0.0085843298584223 -0.022388197481632 0.020696049556136 -0.050584398210049 -0.072376452386379 -0.034365277737379 -0.045013956725597 -0.013955107890069 -0.17898085713387 -0.072600327432156 0.0050511928275228 -0.014829395338893 -0.043765489012003 -0.012062266469002 0.012774495407939 0.069833360612392 0.11638788878918 -0.015336792916059 0.10281457751989 -0.082041338086128

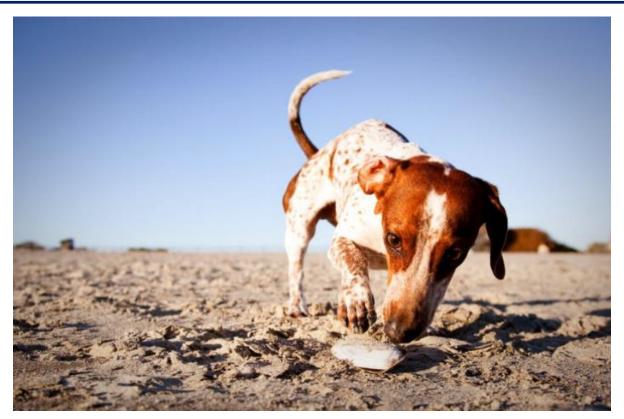


https://medium.com/@ageitgey/machine-learning-is-fun-part-4-modern-face-recognition-with-deep-learning-c3cffc121d78.

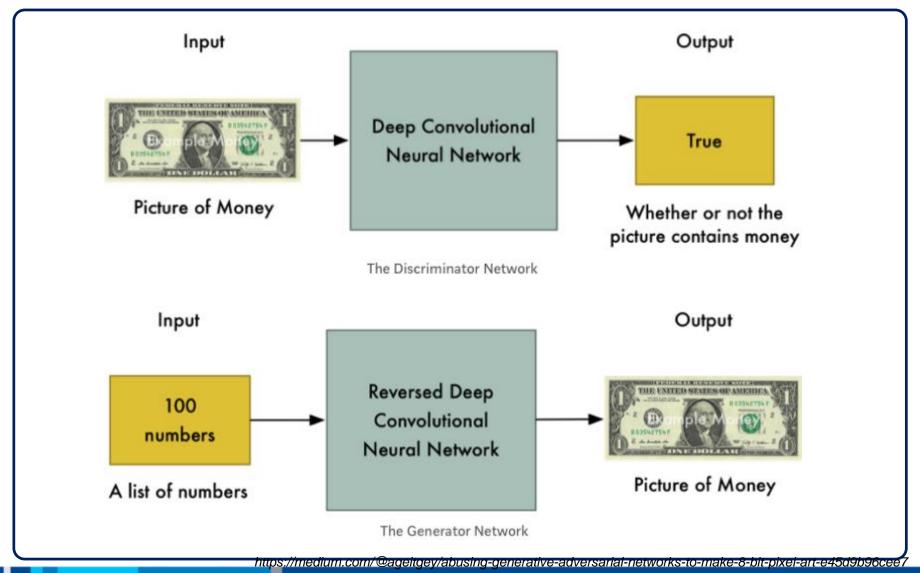
These pictures of bedrooms were dreamt up by a DCGAN



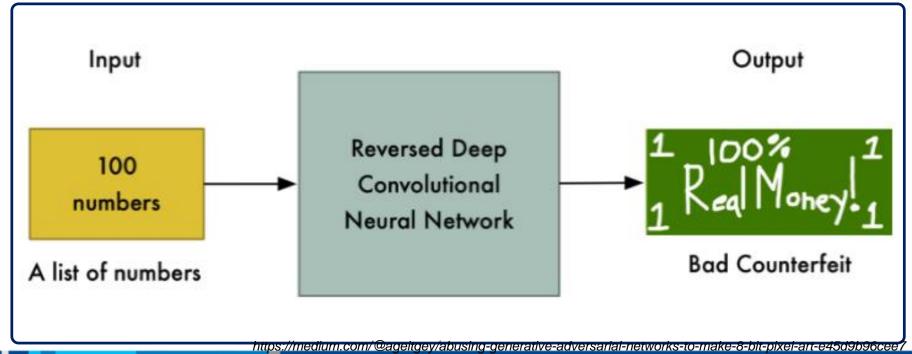
- If the computer was able to do this and the pictures
 - It produced had the right number of legs, tails, and ears
 - Computer knows what parts go into making up a "dog"



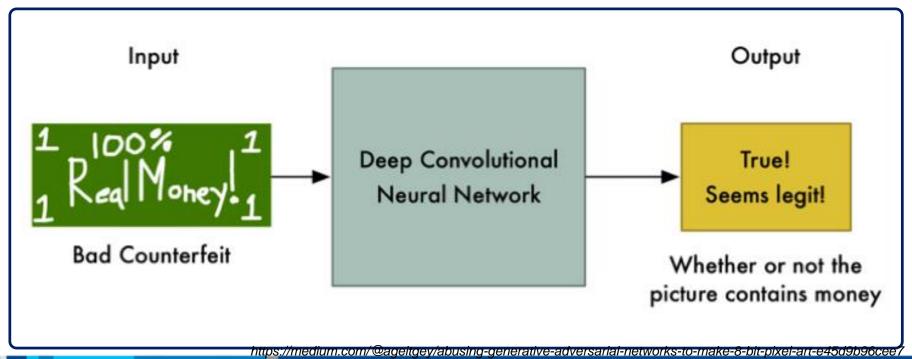
- To build a DCGAN, we create two deep neural networks
- Then we make them fight against each other
- In the process, they both become stronger
- This first neural network is called the Discriminator
- This second neural network is called the Generator



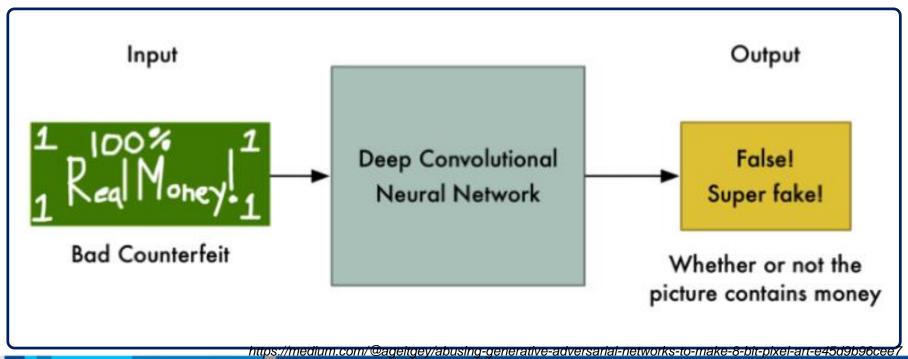
- Let's make them battle!
- In the first round
 - The Generator makes the first (terrible) fake dollar



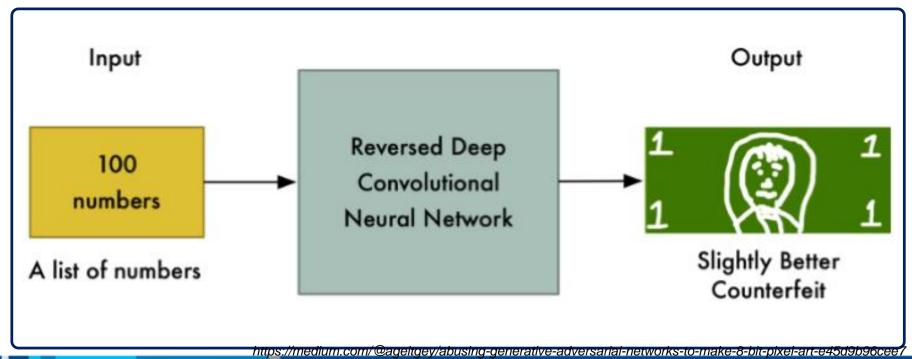
The Discriminator is equally terrible at it's job, so it won't know the difference



- The Discriminator levels up!
- It now can spot very bad fake dollars.



- The Generator makes a slightly better counterfeit dollar
- This back-and-forth game between them
 - Continuing thousands of times until both networks are experts



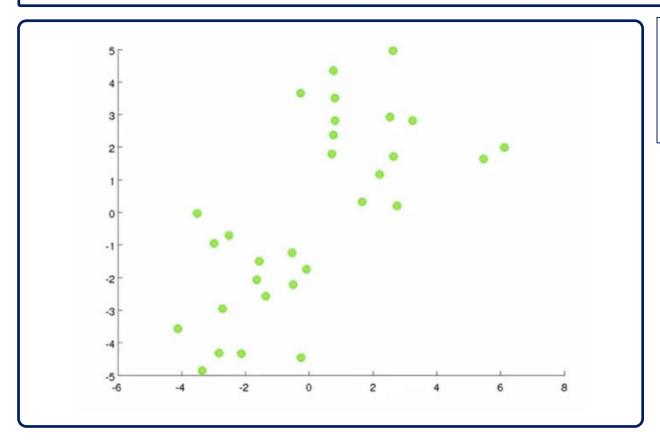
Clustering

Details

- Clustering is a kind of Unsupervised Learning,
 finding a cluster that best describes given data without label
- Classification requires data and labels for each data
- In practice, there are many cases where data exists but it does not know what label or category it is
- Sometimes it is necessary to explain the data through a method other than classfication
- K-means
- Gaussian Mixture Model(GMM)

Find the K clusters that best describes the data

$$\min_{b,w} \sum_{i}^{n} \sum_{j}^{k} w_{ij} \|x_{i} - b_{j}\|_{2}^{2} \text{ s.t. } \sum_{j} w_{ij} = 1, \forall j$$



n: # of data
k: # of clusters
I: index of data

j: index of cluster

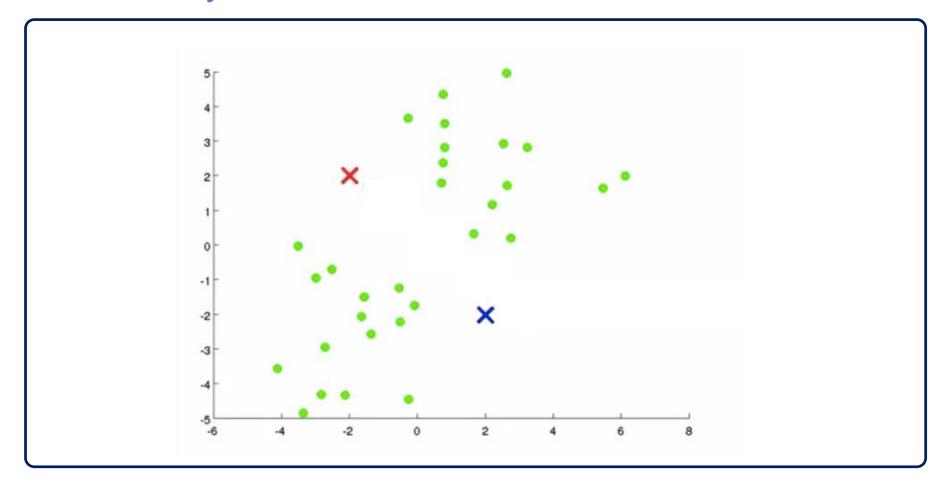
 b_i : center of j-th cluster

 w_{ij} : if i-th data is in j-th cluster, it is 1

else, it is 0

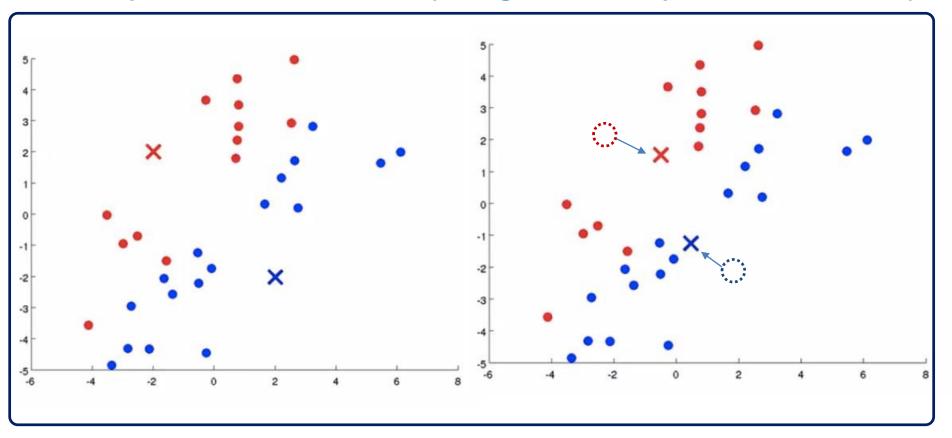
^{*} Slides from Andrew Ng(Stanford Univ.), "Machine Learning"

- Number of cluster k = 2,
 - Randomly initialize "centroids"



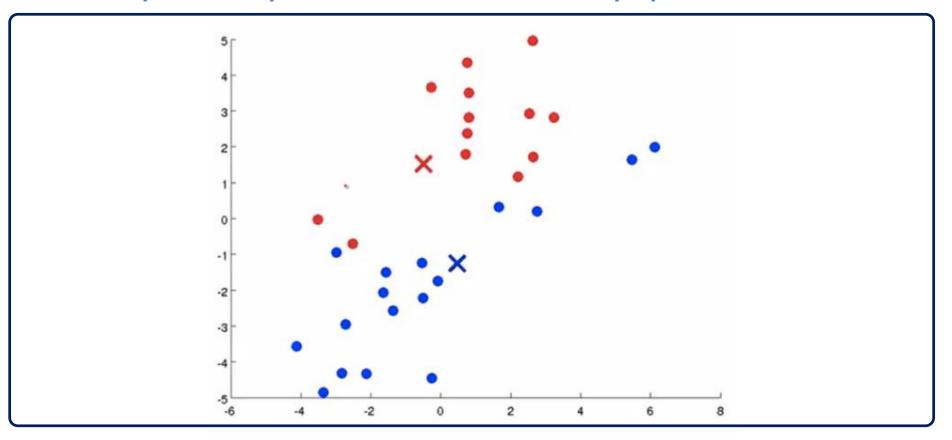
* Slides from Andrew Ng(Stanford Univ.), "Machine Learning"

- Number of cluster k = 2,
 - Assign cluster membership
 - Update the cluster centroid (average of the data points in each cluster)



* Slides from Andrew Ng(Stanford Univ.), "Machine Learning"

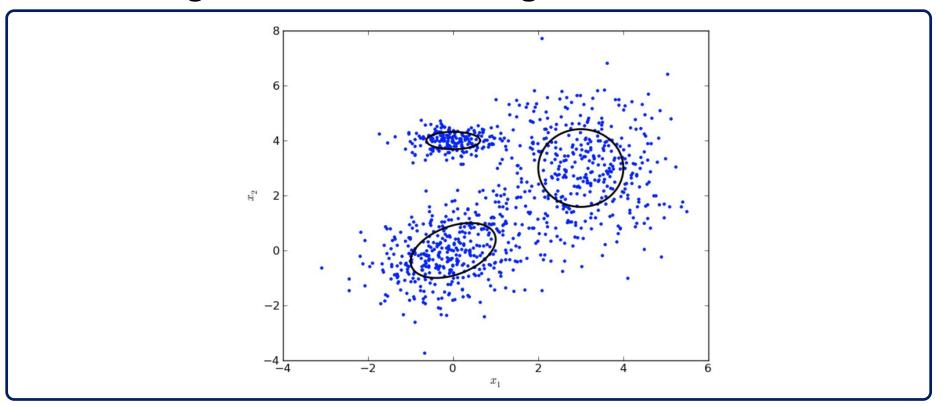
- Number of cluster k = 2,
 - Update cluster membership
 - Repeat those procedure until no membership update



^{*} Slides from Andrew Ng(Stanford Univ.), "Machine Learning"

Gaussian Mixture Model

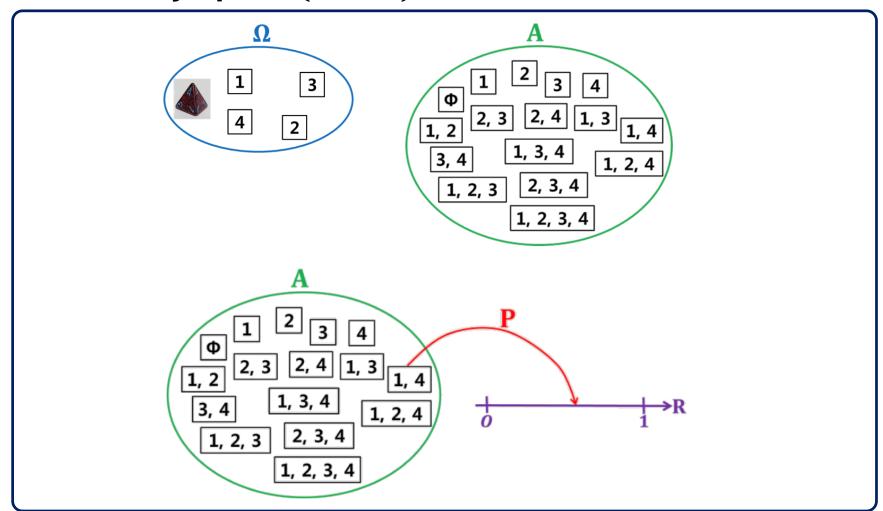
- The data is composed of 'Mixture' of 'Gaussian'
- The figure below is the result of finding the gaussian distributions assuming that it consists of three gaussian.



Probability space

- (Ω, A, P)
- Ω : a sample space
- A: a set of events
- P: the assignment of probability to the events

• Probability space (Ω, A, P)



Joint distribution

X: Observed data tensor

Z: Hidden data tensor

p(): Probability distribution

 θ : Parameter

$$p(\mathbf{X}, \mathbf{Z}|\theta)$$

Marginal probability distribution

$$p(\mathbf{X}|\theta) = \sum_{\mathbf{Z}} p(\mathbf{X}, \mathbf{Z}|\theta)$$

Marginal probability distribution

X: Observed data tensor

Z: Hidden data tensor

p(): Probability distribution

 θ : Parameter

$$p(\mathbf{X}|\theta) = \sum_{\mathbf{Z}} p(\mathbf{X}, \mathbf{Z}|\theta)$$

Maximum likelyhood estimation

$$\max_{\theta} p(\mathbf{X}|\theta) = \sum_{\mathbf{Z}} p(\mathbf{X}, Z|\theta)$$

Maximum likelyhood estimation

X: Observed data tensor

Z: Hidden data tensor

p(): Probability distribution

q(): Probability distribution of Z

 θ : Parameter

$$\max_{\theta} p(\mathbf{X}|\theta) = \sum_{\mathbf{Z}} p(\mathbf{X}, Z|\theta)$$

Maximum log likelyhood estimation

$$\ln p(\mathbf{X}|\theta) = L(q,\theta) + KL(q||p)$$

$$L(q, \theta) = \sum_{\mathbf{Z}} q(\mathbf{Z}) \ln \left\{ \frac{p(\mathbf{X}, \mathbf{Z} | \theta)}{q(\mathbf{Z})} \right\}$$

$$KL(q||p) = -\sum_{\mathbf{Z}} q(\mathbf{Z}) \ln \left\{ \frac{p(\mathbf{Z}|\mathbf{X}, \theta)}{q(\mathbf{Z})} \right\}$$

Maximum likelyhood estimation

X: Observed data tensor

Z: Hidden data tensor

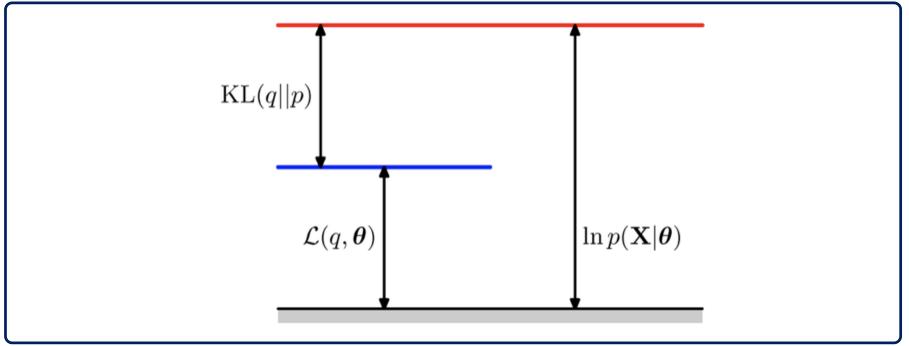
 $p(\cdot)$: Probability distribution

q(): Probability distribution of Z

 θ : Parameter

$$\ln p(\mathbf{X}|\theta) = L(q,\theta) + KL(q||p)$$

Current status



http://norman3.github.io/prml/docs/chapter09/4

http://sanghyukchun.github.io/70/

Maximum likelyhood estimation

X: Observed data tensor

Z: Hidden data tensor

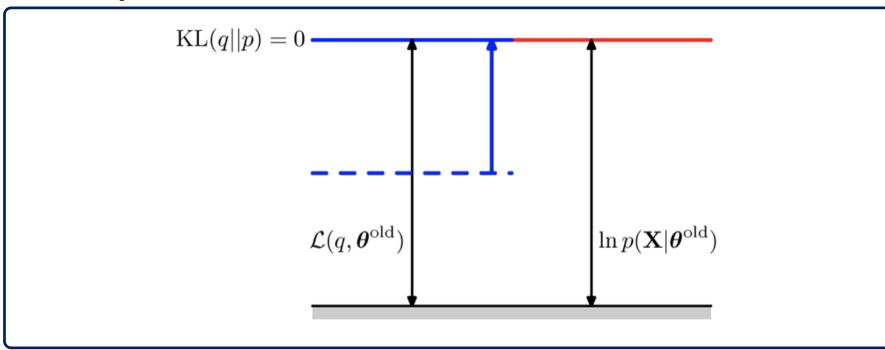
p(): Probability distribution

q(): Probability distribution of Z

 θ : Parameter

$$\ln p(\mathbf{X}|\theta) = L(q,\theta) + KL(q||p)$$

E-step



Maximum likelyhood estimation

X: Observed data tensor

Z: Hidden data tensor

p(): Probability distribution

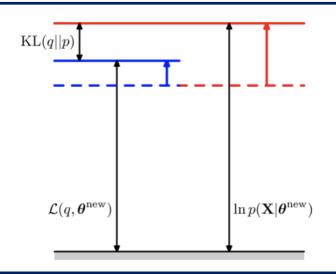
q(): Probability distribution of Z

 θ : Parameter

$$\ln p(\mathbf{X}|\theta) = L(q,\theta) + KL(q||p)$$

$$L(q, \theta) = \sum_{\mathbf{Z}} p(\mathbf{Z}|\mathbf{X}, \theta^{old}) \ln p(\mathbf{X}, \mathbf{Z}|\theta) - \sum_{\mathbf{Z}} p(\mathbf{Z}|\mathbf{X}, \theta^{old}) \ln p(\mathbf{Z}|\mathbf{X}, \theta^{old}) = Q(\theta, \theta^{old}) + const$$

M-step



http://norman3.github.io/prml/docs/chapter09/4

http://sanghyukchun.github.io/70/

Maximum likelyhood estimation

X: Observed data tensor

Z: Hidden data tensor

p(): Probability distribution

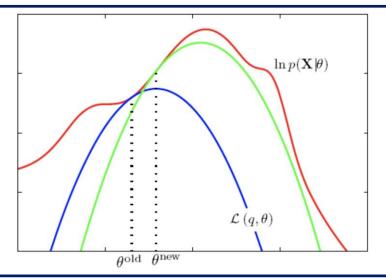
q(): Probability distribution of Z

 θ : Parameter

$$\ln p(\mathbf{X}|\theta) = L(q,\theta) + KL(q||p)$$

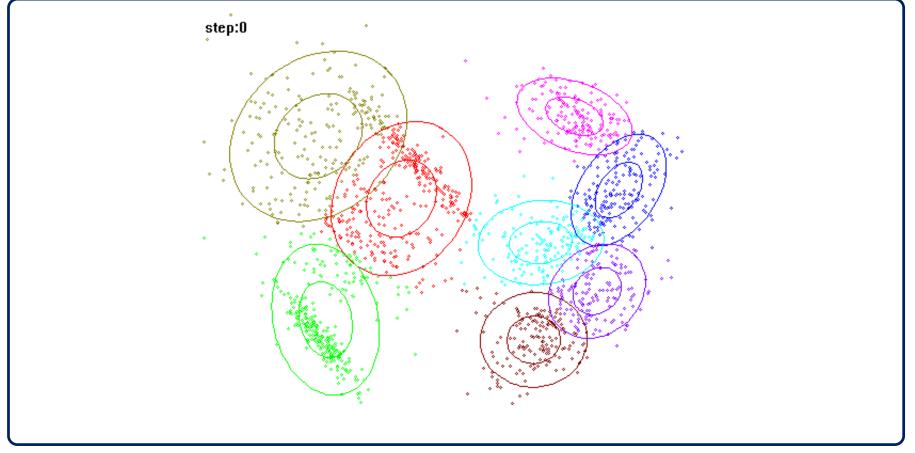
$$L(q, \theta) = \sum_{\mathbf{Z}} p(\mathbf{Z}|\mathbf{X}, \theta^{old}) \ln p(\mathbf{X}, \mathbf{Z}|\theta) - \sum_{\mathbf{Z}} p(\mathbf{Z}|\mathbf{X}, \theta^{old}) \ln p(\mathbf{Z}|\mathbf{X}, \theta^{old}) = Q(\theta, \theta^{old}) + const$$

M-step



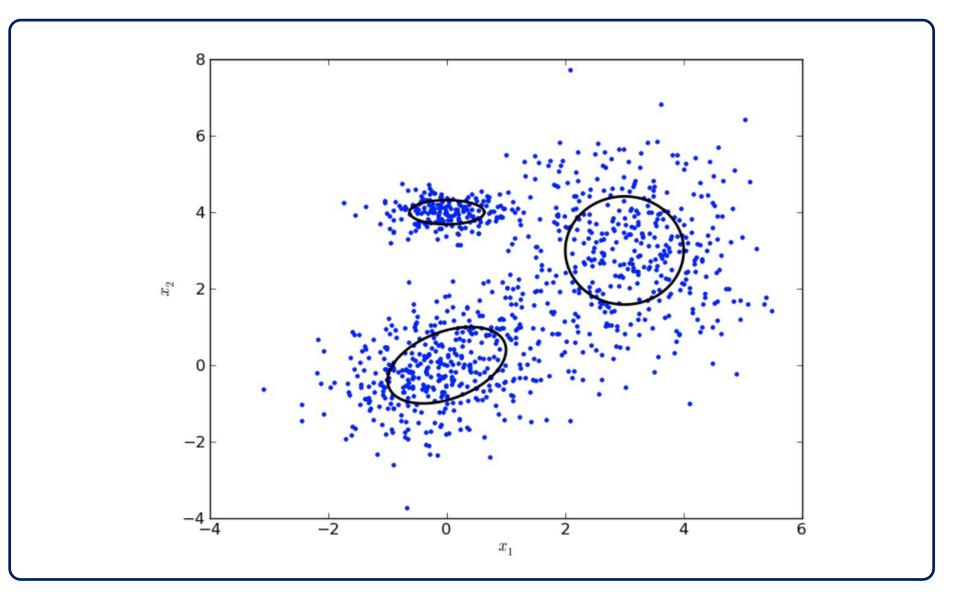
GMM Result

$$\ln p(X|\pi,\mu,\Sigma) = \sum_{i}^{n} \ln \sum_{j}^{k} \pi_{j} N(x_{i}|\mu_{j},\Sigma_{j})$$



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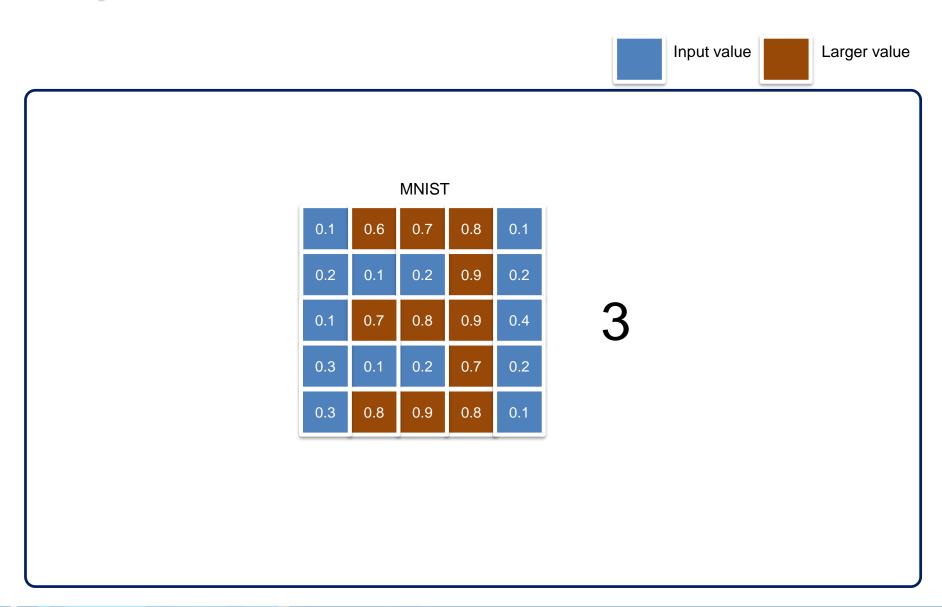
Example



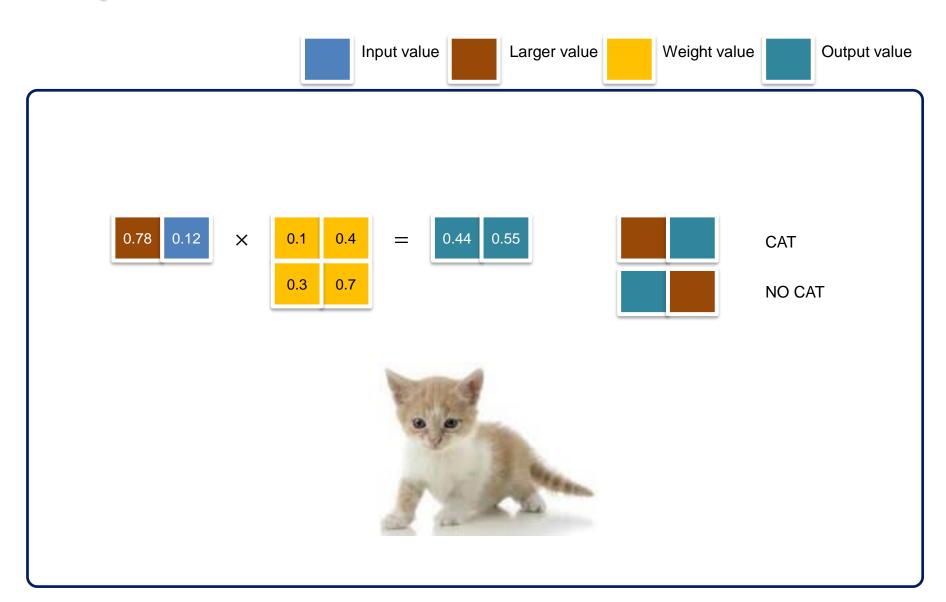
http://norman3.github.io/prml/docs/chapter09/4

http://sanghyukchun.github.io/70/

Simplification MNIST



Simplification

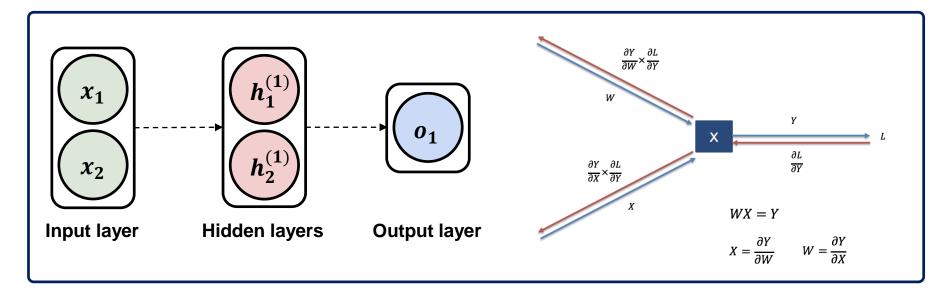


Example

Data

```
float x1[10]={0.67, 0.89, 0.78, 0.87, 0.72, 0.85, 0.69, 0.81, 0.73, 0.89};
float x2[10]={0.11, 0.12, 0.12, 0.13, 0.10, 0.16, 0.09, 0.11, 0.08, 0.01};
int label[10] = {0, 0, 0, 0, 0, 0, 0, 0, 0};
w1=0.1;
w2=0.4;
w3=0.3;
w4=0.7;
```

Logic



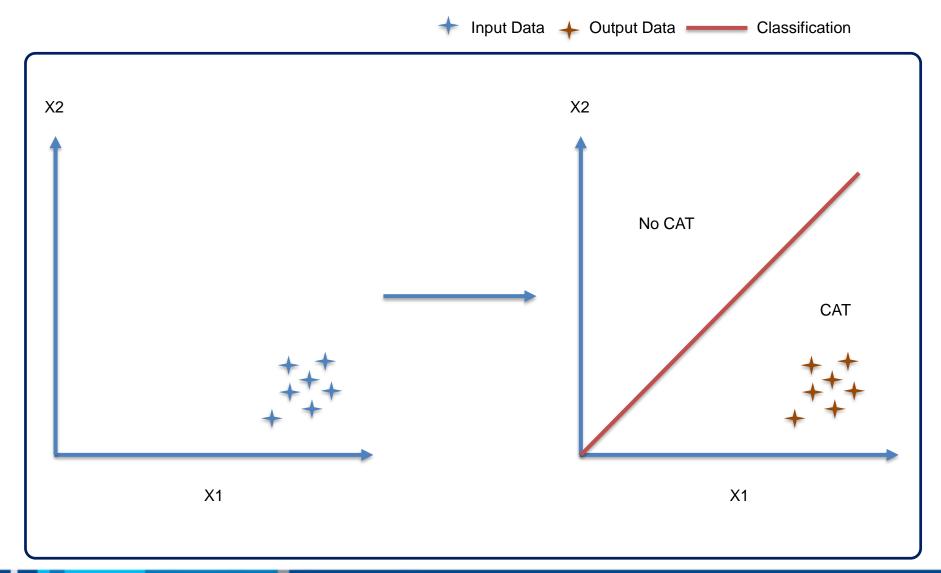
Result

w3=0.3:

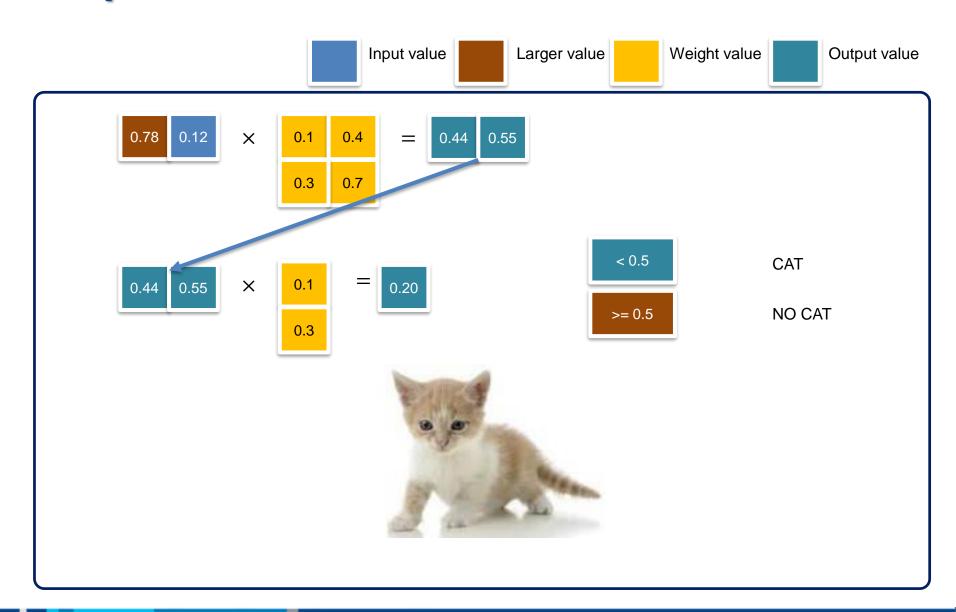
```
Without unsupervised pre-training
       epoch)0 acc)0.00000 w1)0.10448 w2)0.39552 w3)0.10448 w4)0.39552
       o1)0.44349 o2)0.55651
       epoch)6 acc)0.00000 w1)0.13099
                                      w2)0.36901 w3)0.13100
                                                              w4)0.36900
       o1)0.45877 o2)0.54123
       epoch)12 acc)0.00000 w1)0.15695 w2)0.34305 w3)0.15696
                                                               w4)0.34304
       epoch) 18 acc) 0.00000 w1) 0.18237 w2) 0.31763 w3) 0.18237
                                                               w4)0.31763
w1=0.1:
       01)0.47528 02)0.52472
w2=0.4;
       epoch)24 acc)0.00000 w1)0.20725 w2)0.29275 w3)0.20725 w4)0.29275
       epoch)30 acc)0.00000 w1)0.23161 w2)0.26839 w3)0.23161 w4)0.26839
w4=0.7:
       o1)0.50059 o2)0.49941
       epoch)36 acc)100.00000 w1)0.25545 w2)0.24455 w3)0.25545 w4)0.24455
```

```
With unsupervised pre-training
o1)0.64805 o2)0.35195
epoch)0 acc)100.00000 w1)0.89393 w2)0.10607 w3)0.89393 w4)0.10607
```

Representation graph



Simplification

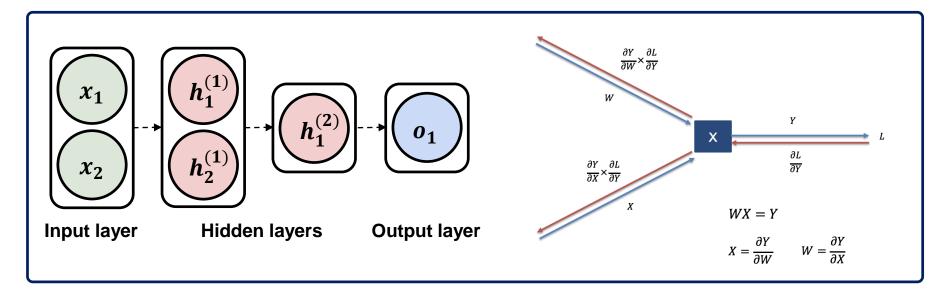


Example

Data

```
float x1[10]={0.67, 0.89, 0.78, 0.87, 0.72, 0.85, 0.69, 0.81, 0.73, 0.89};
float x2[10]={0.11, 0.12, 0.12, 0.13, 0.10, 0.16, 0.09, 0.11, 0.08, 0.01};
int label[10] = {0, 0, 0, 0, 0, 0, 0, 0, 0};
w1=0.1;
w2=0.4;
w3=0.3;
w4=0.7;
w5=-0.7;
w6=0.9;
```

Logic



Code

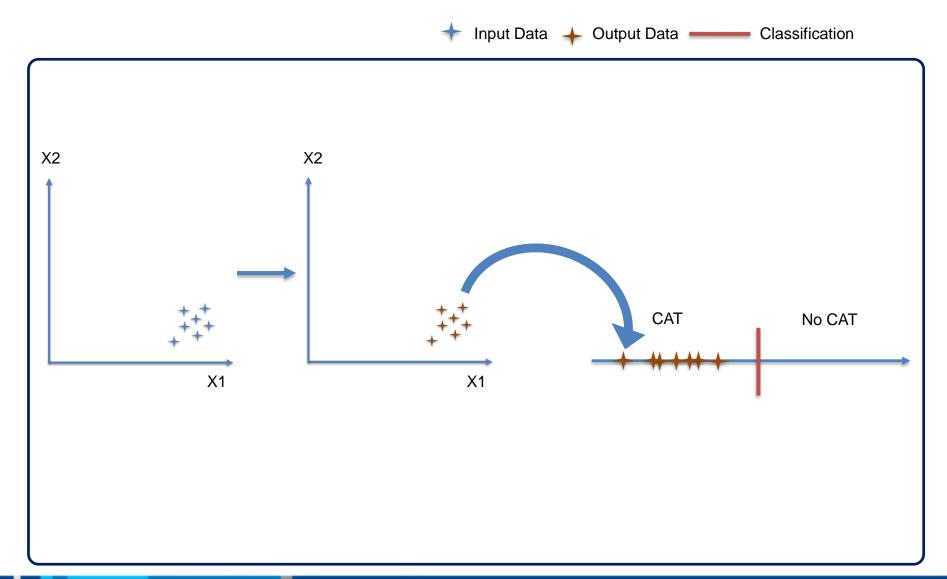
Supervised learning

```
o1=x1[i]*w1+x2[i]*w3;
o2=x1[i]*w2+x2[i]*w4;
o3=o1*w5+o2*w6;
o3 = exp(o3);
if(label[i] == 0)
    if(o3 < 0.5) acc++;
}else
    if(o3 >= 0.5) acc++;
    03=03-1;
dw6=o2*o3:
dw5=o1*o3;
dx2=w6*o3;
dx1=w5*o3;
dw4=dx2*x2[i]:
dw3=dx1*x2[i]:
dw2=dx2*x1[i]:
dw1=dx1*x1[i]:
w1=w1-0.001*dw1:
w2=w2-0.001*dw2:
w3=w3-0.001*dw3:
w4=w4-0.001*dw4:
w5=w5-0.001*dw5:
w6=w6-0.001*dw6;
```

Unsupervised learning

```
// first laver
                                       //second layer
o1=x1[i]*w1+x2[i]*w3;
                                       o3=o1*w5+o2*w6;
o2=x1[i]*w2+x2[i]*w4;
                                       o4=o3*w5;
                                       o5=o3*w6;
if(o1 == x1[i] && o2 == x2[i]) acc++;
                                       if(o1 == x1[i] && o2 == x2[i]) acc++;
ol=ol-x1[i]:
02=02-x2[i]:
                                       04=04-01;
                                       05=05-02;
dw4=o2*x2[i]:
                                       dw5=03*04;
dw3=o1*x2[i]:
dw2=o2*x1[i]:
                                       dw6=o3*o5;
dw1=o1*x1[i]:
                                       dx3=04*w5+05*w6;
                                       w5=w5-0.1*dw5;
                                       w6=w5-0.1*dw6;
w1=w1-0.1*dw1:
w2=w2-0.1*dw2:
                                       dw5=o1*dx3:
w3=w1-0.1*dw3:
                                       dw6=o2*dx3;
w4=w2-0.1*dw4;
                                       w5=w5-0.1*dw5;
                                       w6=w5-0.1*dw6:
```

Representation graph



Result

w4=0.7;

w6=0.9:

```
Without unsupervised pre-training
         o1)0.10000 o2)0.34500 o3)1.27188
         epoch)0 acc)0.00000 w1)0.10725 w2)0.39072 w3)0.30095 w4)0.69878 w5)-0.70147 w6)0.89496
         o1)0.23201 o2)0.19149 o3)0.97660
         epoch)30 acc)0.00000 w1)0.29868 w2)0.16963 w3)0.32602 w4)0.66982 w5)-0.76510 w6)0.79830
         o1)0.34330 o2)0.08336 o3)0.79679
w1=0.1:
         epoch)60 acc)0.00000 w1)0.46056 w2)0.01316 w3)0.34724 w4)0.64930 w5)-0.85001 w6)0.76259
w2=0.4;
         01)0.44168 02)-0.00035 03)0.66023
w3=0.3:
         epoch)90 acc)0.00000 w1)0.60374 w2)-0.10821 w3)0.36603 w4)0.63337 w5)-0.94247 w6)0.75670
         o1)0.52906 o2)-0.06785 o3)0.55006
         epoch)120 acc)60.00000 w1)0.73088 w2)-0.20616 w3)0.38273 w4)0.62050 w5)-1.03461 w6)0.76630
w5 = -0.7:
         epoch)137 acc)100.00000 w1)0.79626 w2)-0.25372 w3)0.39134 w4)0.61424 w5)-1.08486 w6)0.77547
```

With unsupervised pre-training 01)0.69524 02)0.08476 03)0.54312 epoch)0 acc)60.00000 w1)0.89438 w2)0.11174 w3)0.89181 w4)0.10898 w5)-0.78652 w6)-0.78308 epoch)14 acc)100.00000 w1)0.93650 w2)0.15250 w3)0.89728 w4)0.11428 w5)-0.83996 w6)-0.79066

Result

```
Without unsupervised pre-training
          o1)0.10000 o2)0.34500 o3)1.14912
         epoch)0 acc)0.00000 w1)0.09356 w2)0.39818 w3)0.29916 w4)0.69976 w5)0.69874 w6)0.19548
          01)-0.02104 02)0.32061 03)1.01101
          epoch)30 acc)0.00000 w1)-0.08231 w2)0.36375 w3)0.27614 w4)0.69525 w5)0.68769 w6)0.07565
          01)-0.12792 02)0.31618 03)0.90652
          epoch)60 acc)0.00000 w1)-0.23801 w2)0.35806 w3)0.25576 w4)0.69449 w5)0.71545 w6)-0.02463
          o1)-0.22739 o2)0.32505 o3)0.81011
          epoch)90 acc)0.00000 w1)-0.38307 w2)0.37154 w3)0.23677 w4)0.69625 w5)0.76977
                                                                                        w6)-0.11368
          o1)-0.32136 o2)0.34276 o3)0.71504
          epoch)120 acc)0.00000 w1)-0.52010 w2)0.39775 w3)0.21883 w4)0.69968 w5)0.84148 w6)-0.19466
          o1)-0.40953 o2)0.36573 o3)0.62249
         epoch)150 acc)0.00000 w1)-0.64863 w2)0.43149 w3)0.20198 w4)0.70410 w5)0.92260 w6)-0.26850
         o1)-0.49100 o2)0.39111 o3)0.53625
w1=0.1;
         epoch)180 acc)60.00000 w1)-0.76731 w2)0.46863 w3)0.18641 w4)0.70898 w5)1.00656 w6)-0.33528
w2=0.4:
         o1)-0.52650 o2)0.40317 o3)0.49914
w3=0.3:
         epoch)194 acc)100.00000 w1)-0.81901 w2)0.48625 w3)0.17962 w4)0.71129 w5)1.04531 w6)-0.36404
w4=0.7;
w5 = -0.7:
         With unsupervised pre-training
w6=0.9:
          o1)0.69524 o2)0.08476 o3)1.86075
          epoch)0 acc)0.00000 w1)0.87869 w2)0.09595 w3)0.88975 w4)0.10692 w5)0.78007 w6)0.79425
          01)0.53924 02)-0.11122 03)1.18246
          epoch)30 acc)0.00000 w1)0.65892 w2)-0.18528 w3)0.86089 w4)0.07003 w5)0.46930 w6)0.80570
          o1)0.47420 o2)-0.25173 o3)0.92508
          epoch)60 acc)0.00000 w1)0.56626 w2)-0.38917 w3)0.84873 w4)0.04330 w5)0.29326 w6)0.87357
          o1)0.44352 o2)-0.37074 o3)0.75668
          epoch)90 acc)0.00000 w1)0.52258 w2)-0.56224 w3)0.84300 w4)0.02060 w5)0.16967
                                                                                        w6)0.96242
          o1)0.43045 o2)-0.47521 o3)0.62654
          epoch)120 acc)0.00000 w1)0.50410 w2)-0.71425 w3)0.84057 w4)0.00066 w5)0.07579 w6)1.05822
          o1)0.42700 o2)-0.56727 o3)0.52171
         epoch) 150 acc) 80,00000 w1) 0,49940 w2) -0,84817 w3) 0,83995 w4) -0,01693 w5) 0,00163 w6) 1,15296
          o1)0.42709 o2)-0.58987 o3)0.49734
         epoch)158 acc)100.00000 w1)0.49959 w2)-0.88105 w3)0.83997 w4)-0.02125 w5)-0.01558 w6)1.17742
```

Thank you