Scala Days, 13 June 2019

Compiling to Preserve Our Privacy

Manohar Jonnalagedda Jakob Odersky





def avg(salaries: List[Int]) =
 salaries.sum / salaries.length
avg(A :: B :: C :: Nil)









B = 100

Dimitar



A = 1000

Manohar



C = 70



A = 1000 $0 = d = d_1 + d_2 + d_3$



B = 100 $0 = j = j_1 + j_2 + j_3$



C = 70 $0 = m = m_1 + m_2 + m_3$

```
type SecretNum = Int // in this example
type SharedNum = List[SecretNum]
def createZeroShares(players: Int): SharedNum = {
  val rands =
    List.fill(players - 1) (util.Random.nextInt)
  val diff = -rands.sum
  diff :: rands
val d = createZeroShares(3) // locally by d
val j = createZeroShares(3) // locally by j
val m = createZeroShares(3) // locally by m
```



A = 1000 $0 = d = d_1 + d_2 + d_3$



B = 100 $0 = j = j_1 + j_2 + j_3$

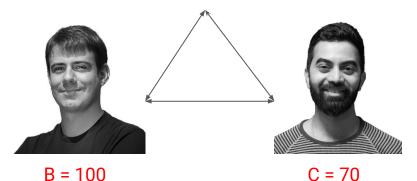


C = 70 $0 = m = m_1 + m_2 + m_3$

```
type SecretNum = Int // in this example
type SharedNum = List[SecretNum]
def createZeroShares
                                           dNum = {
  val rands =
    List.fill(pl/
                      Secret shares (elements
  val diff = -r
                       of the list) reside with
                          different players
  diff :: rands
val d = createZeroShares(3) // locally by d
val j = createZeroShares(3) // locally by j
val m = createZeroShares(3) // locally by m
```



A = 1000 $0 = d = d_1 + d_2 + d_3$



 $0 = j = j_1 + j_2 + j_3$

```
0 = m = m_1 + m_2 + m_3
```

```
type SecretNum = Int // in this example
type SharedNum = List[SecretNum]
def createZeroShares(players: Int): SharedNum = {
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  val diff = -rands.sum
  diff :: rands
val d = createZeroShares(3) // locally by d
val j = createZeroShares(3) // locally by j
val m = createZeroShares(3) // locally by m
```







	d	d ₁	d ₂	d_3
shared zeroes	j	j ₁	j ₂	j ₃
	m	m ₁	m ₂	m ₃
data		Α	В	С
shared sum		S ₁	S ₂	S ₃

sum

$$S = S_1 + S_2 + S_3$$







	d	d ₁	d ₂	d ₃
shared zeroes	j	j ₁	j ₂	j ₃
	m	m ₁	m ₂	m ₃
data		Α	В	С
shared sum		S ₁	S ₂	S ₃

$$S = S_1 + S_2 + S_3$$

Secret shares for zero are distributed

sum







	d	d ₁	d_2	d ₃
shared zeroes	j	j ₁	j ₂	j ₃
	m	m ₁	m ₂	m ₃
data		Α	В	С
shared sum		S ₁	S ₂	S ₃

$$S = S_1 + S_2 + S_3$$

sum

Shared sums are revealed publicly







shared sum		3330	6380	-8540
data		1000	100	70
	0	4330	-1220	-3110
shared zeroes	0	-4000	4000	0
	0	2000	3500	-5500

sum

1170







	0	2000	3500	-5500
shared zeroes	0	-4000	4000	0
	0	4330	-1220	-3110
data		1000	100	70
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sum

1170

avg = 390







	0	2000	3500	-5500
shared zeroes	0	-4000	4000	0
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sum

1170







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sum

1170







	d	d ₁	d_2	d_3
shared zeroes	j	j ₁	j ₂	j ₃
	m	m ₁	m ₂	m ₃
data		А	В	С
shared sum		S ₁	S ₂	S ₃

$$S = S_1 + S_2 + S_3$$

```
def add(x: SharedNum, y: SharedNum): SharedNum =
  x.zip(y).map(addSecret)
def addSecret(x: SecretNum, y: SecretNum): SecretNum =
  x + y
def reveal(x: SharedNum): Int = x.sum
// shared zeroes
val d = createZeroShares(3)
val j = createZeroShares(3)
val m = createZeroShares(3)
val data: SharedNum = A :: B :: C :: Nil
val sharedSum = add(add(d, \dot{j}), add(m, data))
val sum
              = reveal(sharedSum)
```







	d	d ₁	d ₂	d ₃
shared zeroes	j	j ₁	j ₂	j ₃
	m	m ₁	m ₂	m ₃
data		А	В	С
shared sum		S ₁	S ₂	S ₃

$$S = S_1 + S_2 + S_3$$

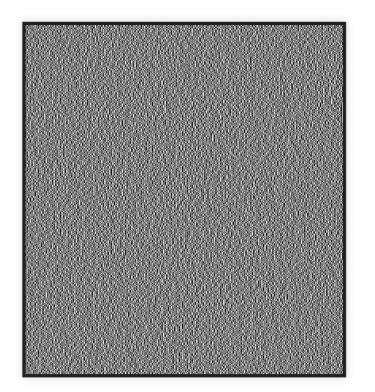
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def reveal(x: SharedNum): Int = x.sum
// shared zeroes
val d = createZeroShares(3)
val j = createZeroShares(3)
val m = createZeroShares(3)
val data: SharedNum = A :: B :: C :: Nil
val sharedSum
                    = add(add(d, j), add(m, data))
                                              d + j + m + data
val sum
                    = reveal(sharedSum)
```

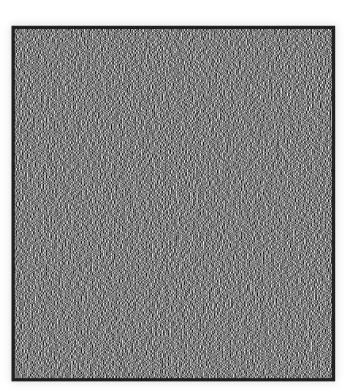
Secure multi-party computation (MPC)

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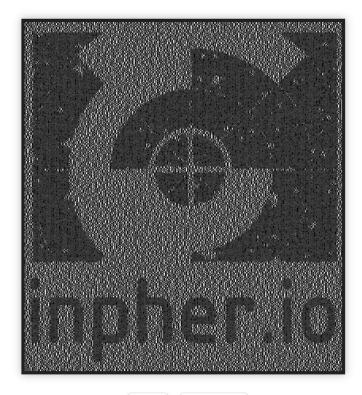
subfield of cryptography with the goal of creating methods for parties to **jointly compute a function** over their inputs **while keeping those inputs private**.

Secret Shared Data





Reveal Secret Shared Data



Reveal

Secret Share

Further operations on SharedNum?

- 1. Addition
- 2. ...
- 3. ...
- 4. ..

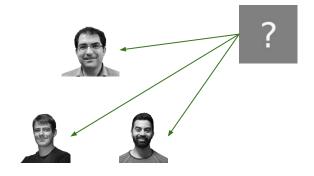
Further operations on SharedNum?

- 1. Addition
- 2. Multiplication
- 3. ...
- 4. ..

Multiplications on SharedNum

```
def mult(x: SharedNum, y: SharedNum) : SharedNum = ???
```

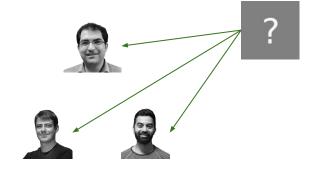
• is more efficient with a trusted dealer



Multiplications on SharedNum

```
def mult(x: SharedNum, y: SharedNum) : SharedNum = ???
```

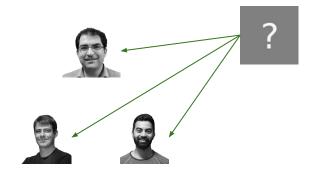
- is more efficient with a trusted dealer
- requires some precomputed random values
 - Beaver triplets
 - Used for mask and reveal



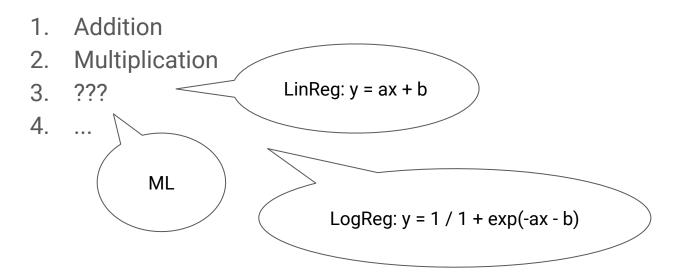
Multiplications on SharedNum

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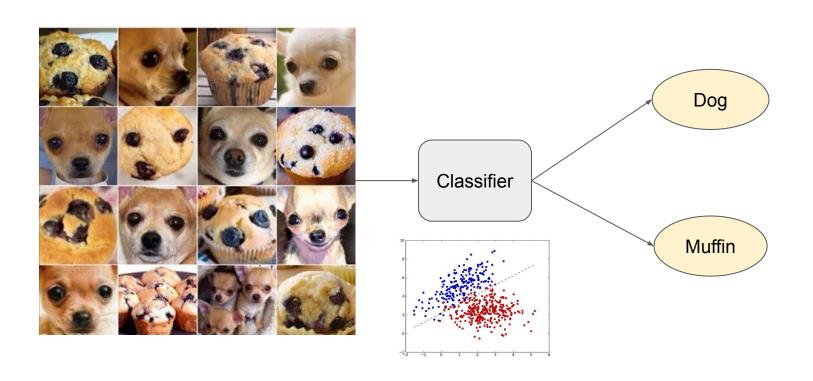
- is more efficient with a trusted dealer
- requires some precomputed random values
 - Beaver triplets
 - Used for mask and reveal
- come talk to us to know more!



Further operations on SharedNum?



Classification: Chihuahua or Muffin?



Further operations on SharedNum?

- 1. Addition
- 2. Multiplication
- 3. ???
- 4. Real-world (i.e. profit)

The Real World

- Financial Services
 - Fraud detection
 - Credit risk modeling
- Healthcare and Genomics
 - Compliance
- Defense and Manufacturing
 - o Predictive maintenance
- Digital Marketing
 - ML Feature/Label aggregation



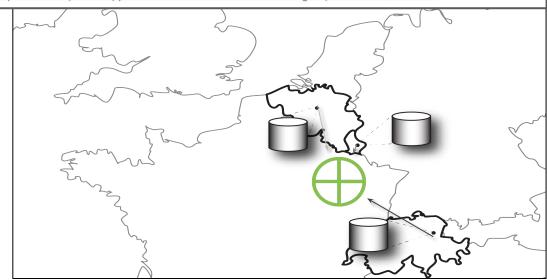


CIO JOURNAL.

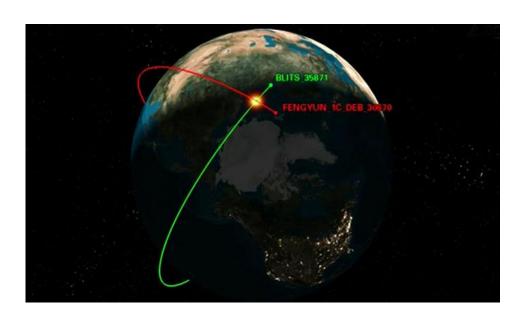


ING Belgium Sees Opportunities for 'Secret' Sharing of Encrypted Data

Zero-knowledge computing would let companies analyze encrypted information without revealing any secret information



Privacy-preserving satellite collision detection

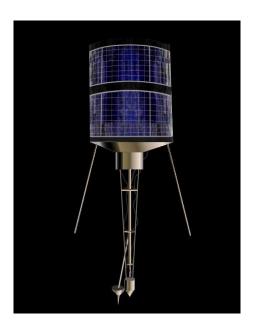


- Predicting collisions of satellites
- Satellite trajectories are private
- Satellite operators nonetheless perform conjunction analysis
- Need to evaluate non-linear functions with high numerical precision

Iridium 33 and Kosmos-2251 Satellite Collision



- Collision 2009
- 11,700 m/s
- 789 km above Siberia
- More than 2000 debris
- ISS special maneuvers





Inpher XOR Secret Computing ™

Legal analysis of Inpher's secret computing technology under the GDPR

February 2018

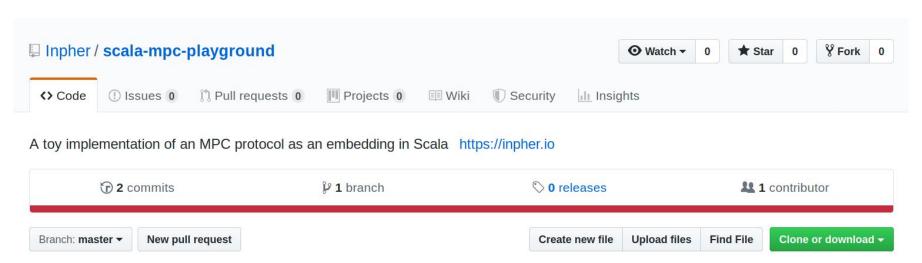
Inpher XOR Secret Computing technology and the underlying computing/analytics operations, will fall outside the scope of the GDPR. Data processed as part of such process do indeed not qualify as personal data in the sense of the GDPR for the reason that they do not or no longer relate to an identified or identifiable individual. The technology used to ensure that such data can not identify an individual meets and exceeds the criteria for a robust anonymization technique as described by the Article 29 Working Party in its Opinion of 10 April 2014 on Anonymization Techniques.



964294-v1\BRUDOCS

A Scala embedding

- Write code in linear algebra style, get secret compute with it for (almost) free!
- More Scala goodness for seamless DSL (Numeric, implicit Ops etc...)
- https://github.com/inpher/scala-mpc-playground



From library to full-blown compiler

- Computations distributed in reality
 - Must target a runtime that distributes computation and deploys

From library to full-blown compiler

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 - Must target a runtime that distributes computation and deploys
- Require static analysis of programs
 - Compute statistical distributions of intermediate values
 - Optimize for memory usage and communication

The DSL and the compiler

- The DSL: allows composable code in a linear algebra style
- Generates low-level, MPC-specific instructions

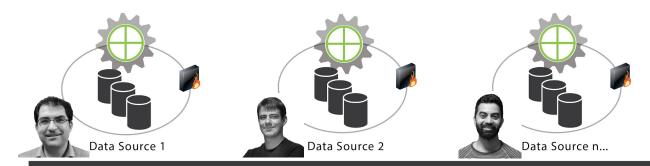
The DSL and the compiler

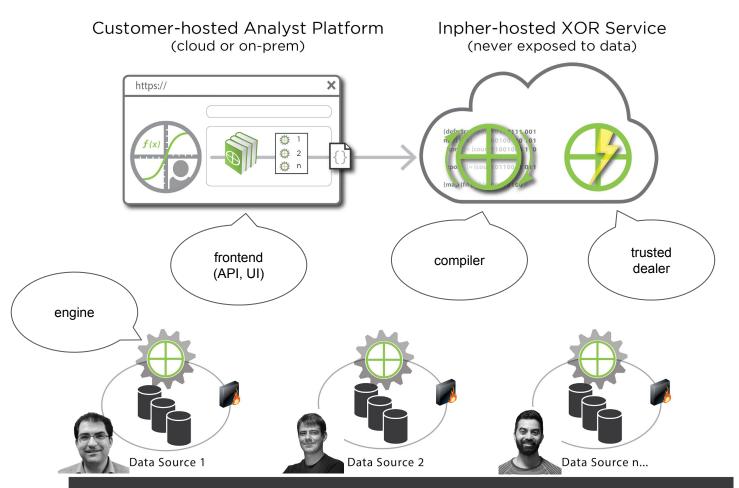
- The DSL: allows composable code in a linear algebra style
- Generates low-level, MPC-specific instructions
- Various static analysis passes
 - The **usual** (type-checking, dimension-checking)
 - The **MPC specific** (infer numerical parameters, optimise for memory/communication)

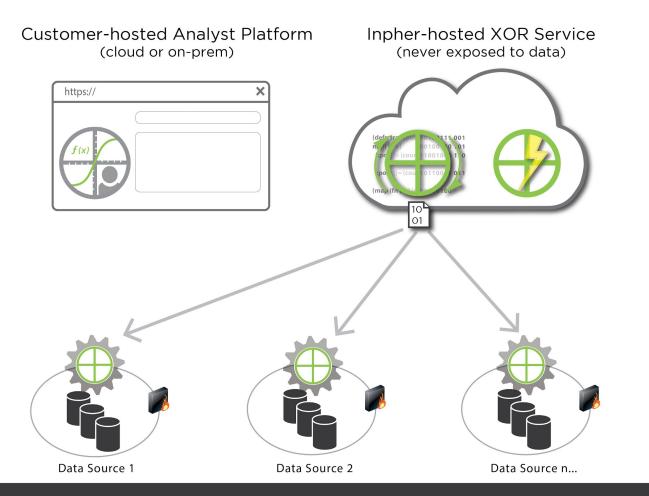
From library to full-blown compiler

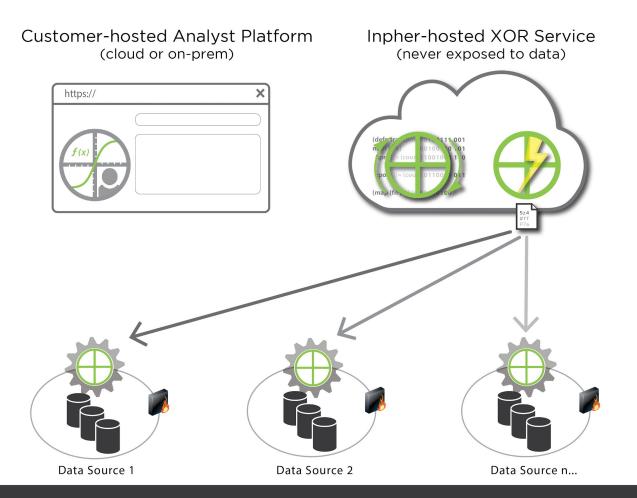
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The complete architecture







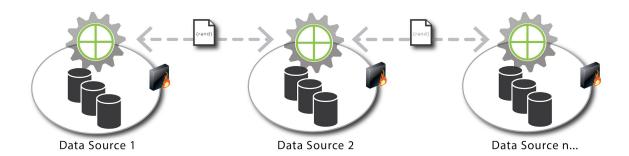


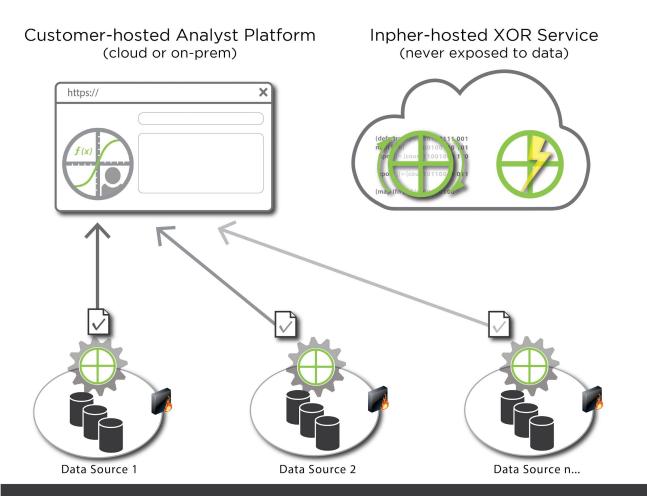
Customer-hosted Analyst Platform (cloud or on-prem)



Inpher-hosted XOR Service (never exposed to data)







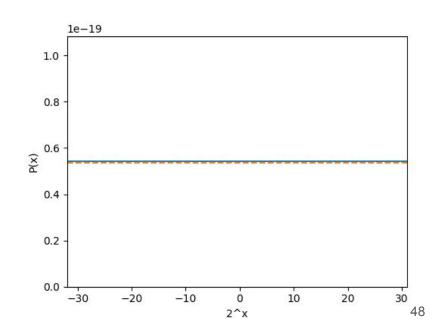
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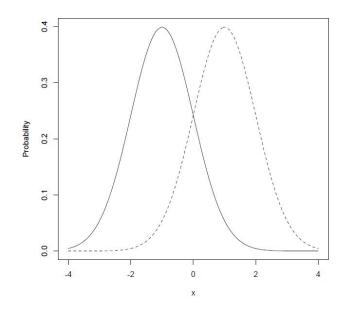
- Computations distributed in reality
 - Must target a runtime that distributes computation and deploys
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Masking numbers: some intuition

Masking integers

- Security: looking at two masked values, can I infer anything about their relationship? If so, how many computations?
- Uniform distribution possible over Z_n
 - information-theoretic security





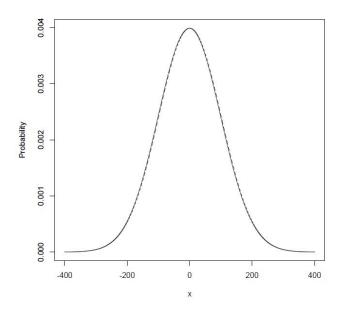


Figure: Masking $x = \pm 1$, $\sigma = 1$ Figure: Masking $x = \pm 1$, $\sigma = 100$

Computational security: an attacker needs to work a lot to distinguish two
masked values

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 masked values
- Masking and multiplying can blow up quickly

- Computational security: an attacker needs to work a lot to distinguish two
 masked values
- Masking and multiplying can blow up quickly
- Fixed-point representation as a solution:
 - Use different number representations at the back
 - Helps avoiding format explosion
- Needs to be analysed statically

An overview of the compiler

Linear Regression - Source

```
def solve(A: Matrix, b: Vector): Vector {
  var nrows: Int = xor.rows(A);
  var ncols: Int = xor.cols(A);

  var P: Matrix = xor.orthrand(nrows, ncols, -6);
  var Q: Matrix = xor.orthrand(nrows, ncols, -6);

  var PAQ: Matrix = P * A * Q;
  var Pb: Vector = P * b;

  xor.reveal(PAQ);
  xor.reveal(PAQ);
  var r: Vector = xor.publicSolve(PAQ, Pb);
  return Q * r;
}
```

```
def linreg(y: Vector, X: Matrix): Vector {
  var A: Matrix = xor.transpose(X) * X;
  var b: Vector = xor.transpose(X) * y;
  return solve(A, b);
}

def main() {
  var X: Matrix = xor.input("X");
  var y: Vector = xor.input("y");
  var theta: Vector = linreg(y, X);
  xor.output(theta, "thetas");
}
```

Linear Regression - Source

```
def solve(A: Matrix, b: Vector): Vector {
 var nrows: Int = xor.rows(A);
 var ncols: Int = xor.col
                             builtin
 var P: Matrix = xor.orthrand(nrows, ncols, -6);
 var Q: Matrix = xor.orthrand(nrows, ncols, -6);
 var PAQ: Matrix = P * A * Q;
  var Pb: Vector = P * b;
 xor.reveal(PAQ);
 xor.reveal(Pb);
 var r: Vector = xor.publicSolve(PAQ, Pb);
  return Q * r;
                           builtin
```

```
def linreg(y: Vector, X: Matrix): Vector {
  var A: Matrix = xor.transpose(X) * X;
  var b: Vector = xor.transpose(X) * y;
  return solve(A, b);
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builtin

def main() {
  var X: Matrix = xor.input("X");
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}

builtin
```

manojoport in ~/workspace/inpher/xor-compiler ± master {4} U:1 ?:5				
Index	Phase	Brief		
0	parse	Parses the program.		
1	namer	Enters symbols for all top-level functions.		
2	typer	Checks that the program is well typed, and performs some basic type inference.		
3	anf	Transform the program in A-normal form.		
4	ssa	Transforms the tree into its Static Single-Assignment (SSA) form.		
5	inline	Inlines all functions called by the main function into its body.		
6	tuple-elimination	Eliminates tuples creation and projections.		
7	copy-propagation	Removes intermediate variables from assign-chains, and other unused variables.		
8	constant-fold	Performs basic partial evaluation and folds constants through the program.		
9	dimension-checking	Checks the dimensions of all matrices, and ensures that the operations are valid.		
10	desugaring	Transforms a user-level program into one that operates on MPC-level primitives only.		
11	visibility	Tracks and sets the visibility of all values.		
12	plaintext-param	Computes plaintext parameters pMsb and pLsb.		
13	mask-resolution	Resolves masking parameters from plaintext parameters.		
14	builtin-params-resolution	Computes extra parameters specific to builtins.		
15	codegen	Generates a compiled-program.bin that can be executed by an appropriate backend.		



```
command-line options to pass to the underlying JVM

-n, --print-symbols
include symbols when printing tree

-f, --print-full-type
include the full type when printing tree

-c, --print-full-type
include the full type when printing tree

-c, --print-tode
print human friendly representation of generated code

-print print human friendly representation of generated code

-print all phases, in the order in which they are executed, and exit

Control options

-N, --warning warn>
enable/disable warning <warn>

-N, --warning warn>
disable all warnings

disable all warnings

-O, --optinize (level)
enable optimizations level <level>
- anable optimizations level <level>
- anable optimizations level <level>
- anable optimizations level < evalue>

- AUTHORS

Inpher, Inc.

-V, --verbose

Wannual page (stdin) line 47/104 (END) (press h for help or q to quit)

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```

```
6: CreateContainer(V6, F1MR<2,2,9,7,-43>);
    BeaverMod(PriV1, PriV1, V6, AW=(29, -20), BW=(29, -20), W=(9, -40), Pairing=4);
 8: CreateContainer(V8, F1MR<2,1,15,13,-37>);
     BeaverMod(PriV1, PriV3, V8, AW=(35,-20), BW=(35,-20), W=(15,-40), Pairing=4);
10:
11:
           CreateContainer(V11, F1MR<2,2,2,0,-6>);
12:
           RandomOrthogonalMatrix(V11);
           CreateContainer(V13, F1MR<2,2,2,0,-6>);
13:
14:
           RandomOrthogonalMatrix(V13);
15:
           CreateContainer(V15, F1MR<2,2,14,12,-38>);
16:
           BeaverMod(PriV11, PriV6, V15, AW=(52,-6), BW=(20,-38), W=(14,-44), Pairing=3);
17:
           CreateContainer(V17, F1MR<2,2,15,13,-37>);
           BeaverMod(PriV15, PriV13, V17, AW=(21,-37), BW=(52,-6), W=(15,-43), Pairing=(31,-37));
18:
19:
           CreateContainer(V19, F1MR<2,1,16,14,-36>);
           BeaverMod(PriV11, PriV8, V19, AW=(52,-6), BW=(22,-36), W=(16,-42), Pairing=3);
20:
21:
           Reveal(V17);
22:
           Reveal(V19):
23:
           CreateContainer(V23, F1MR<2,1,26,24,-26>);
24:
           PublicSolve(V17. V19. V23):
25:
           CreateContainer(V25, F1MR<2,1,27,25,-25>);
           BeaverMod(PriV13. PubV23, V25, AW=(52,-6), BW=(33,-25), W=(27,-31), Pairing=3);
26:
27:
```

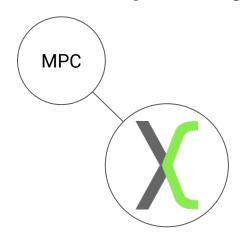
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     BeaverMod(PriV1, PriV3, V8, AW=(35,-20), BW=(35,-20), W=(15,-40), Pairing=4);
10:
11:
           CreateContainer(V11, F1MR<2,2,2,0,-6>);
12:
           RandomOrthogonalMatrix(V11);
           CreateContainer(V13, F1MR<2,2,2,0,-6>);
13:
14:
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15:
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           CreateContainer(V23, F1MR<2,1,26,24,-26>);
24:
           PublicSolve(V17. V19. V23):
           CreateContainer(V25, F1MR<2,1,27,25,-25>);
25:
           BeaverMod(PriV13. PubV23, V25, AW=(52,-6), BW=(33,-25), W=(27,-31), Pairing=3);
26:
27:
```

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           CreateContainer(V11, F1MR<2,2,2,0,-6>);
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27:
```

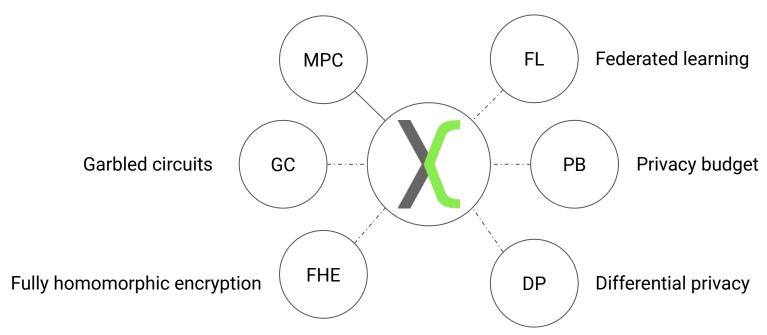
```
6: CreateContainer(V6, FlMR<2,2,9,7,-43>);
 7: BeaverMod(PriV1, PriV1, V6, AW=(29,-20), BW=(29,-20), W=(9,-40), Pairing=4);
 8: CreateContainer(V8, FlMR<2,1,15,13,-37>);
    BeaverMod(PriV1, PriV3, V8, AW=(35,-20), BW=(35,-20), W=(15,-40), Pairing=4);
10:
11:
           CreateContainer(V11, FlMR<2,2,2,0,-6>);
12:
           RandomOrthogonalMatrix(V11);
           CreateContainer(V13, F1MR<2,2,2,0,-6>);
13:
14:
           RandomOrthogonalMatrix(V13);
15:
           CreateContainer(V15, F1MR<2,2,14,12,-38>);
16:
           BeaverMod(PriV11, PriV6, V15, AW=(52,-6), BW=(20,-38), W=(14,-44), Pairing=3);
17:
           CreateContainer(V17, F1MR<2,2,15,13,-37>);
           BeaverMod(PriV15, PriV13, V17, AW=(21,-37), BW=(52,-6), W=(15,-43), Pairing=(31,-37)
18:
19:
           CreateContainer(V19, FlMR<2,1,16,14,-36>);
           BeaverMod(PriV11, PriV8, V19, AW=(52,-6), BW=(22,-36), W=(16,-42), Pairing=3);
20:
21:
           Reveal(V17);
22:
           Reveal(V19):
23:
           CreateContainer(V23, F1MR<2,1,26,24,-26>);
24:
           PublicSolve(V17. V19. V23):
25:
           CreateContainer(V25, F1MR<2,1,27,25,-25>);
           BeaverMod(PriV13. PubV23, V25, AW=(52,-6), BW=(33,-25), W=(27,-31), Pairing=3);
26:
27:
```

```
6: CreateContainer(V6, F1MR<2,2,9,7,-43>);
    BeaverMod(PriV1, PriV1, V6, AW=(29,-20), BW=(29,-20), W=(9,-40), Pairing=4);
 8: CreateContainer(V8, FlMR<2,1,15,13,-37>);
    BeaverMod(PriV1. PriV3, V8, AW=(35, -20), BW=(35, -20), W=(15, -40), Pairing=4);
10:
11:
           CreateContainer(V11, FlMR<2,2,2,0,-6>);
12:
           RandomOrthogonalMatrix(V11);
           CreateContainer(V13, F1MR<2,2,2,0,-6>);
13:
14:
           RandomOrthogonalMatrix(V13):
15:
           CreateContainer(V15, F1MR<2,2,14,12,-38>);
16:
           BeaverMod(PriV11, PriV6, V15, AW=(52,-6), BW=(20,-38), W=(14,-44), Pairing=3);
17:
           CreateContainer(V17, F1MR<2,2,15,13,-37>);
           BeaverMod(PriV15, PriV13, V17, AW=(21,-37), BW=(52,-6), W=(15,-43), Pairing=3);
18:
19:
           CreateContainer(V19, F1MR<2,1,16,14,-36>);
           BeaverMod(PriV11, PriV8, V19, AW=(52,-6), BW=(22,-36), W=(16,-42), Pairing=3);
20:
21:
           Reveal(V17);
22:
           Reveal(V19):
23:
           CreateContainer(V23, F1MR<2,1,26,24,-26>);
24:
           PublicSolve(V17. V19. V23):
25:
           CreateContainer(V25, F1MR<2,1,27,25,-25>);
26:
           BeaverMod(PriV13, PubV23, V25, AW=(52,-6), BW=(33,-25), W=(27,-31), Pairing=3);
27:
```

Compiling to preserve privacy - beyond MPC



Compiling to preserve privacy - beyond MPC



Team

-	Name	Handle	Salutation
8	Anton	@antonrd	Acolyte of the Pythonic Way, Builder of Builtins, Hero of the Seven Setups, and Supreme Sage of Artificial Intelligence
	Benedikt	@Picnixz	Disciple of Taz, Breaker of Changes, and Guardian of Precision
	Dimitar	@djetchev	The Omnipresent, Grand Master of Numbers, and Oracle of the Ivory Tower
	Iulian	@dragos	First of His Name, Champion of the Phases, and Elder of Scala
9	Jakob	@jodersky	Second of His Name, Writer of Compilers, and Prodigal Son
=	Manohar	@manojo	Ambassador to the High Council, Slayer of the Jirassic, and Chief Prophet of Linguistics

Team



Merci beaucoup!

