



The
University
Of
Sheffield.

Search-Based Testing

Phil McMinn

University of Sheffield, UK

Overview

How and why Search-Based Testing Works

Examples

Temporal, Functional, Structural

Applications in Mutation Testing

Test suite prioritisation

Search-Based Test Data Generation

Testability Transformation

Input Domain Reduction

Empirical and Theoretical Studies

Future Directions

Acknowledgements

The material in some of these slides has kindly
been provided by:

Mark Harman (KCL/UCL)

Joachim Wegener (Berner & Matner)

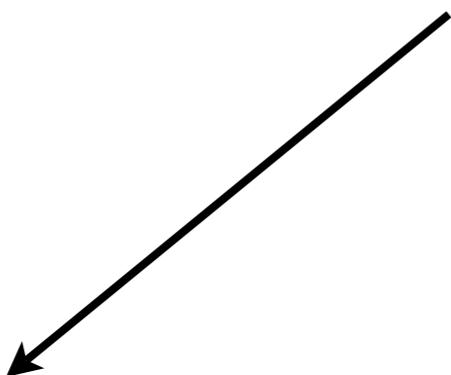
Conventional Testing

manual design of test cases / scenarios

Conventional Testing

manual design of test cases / scenarios

laborious,
time-consuming



Conventional Testing

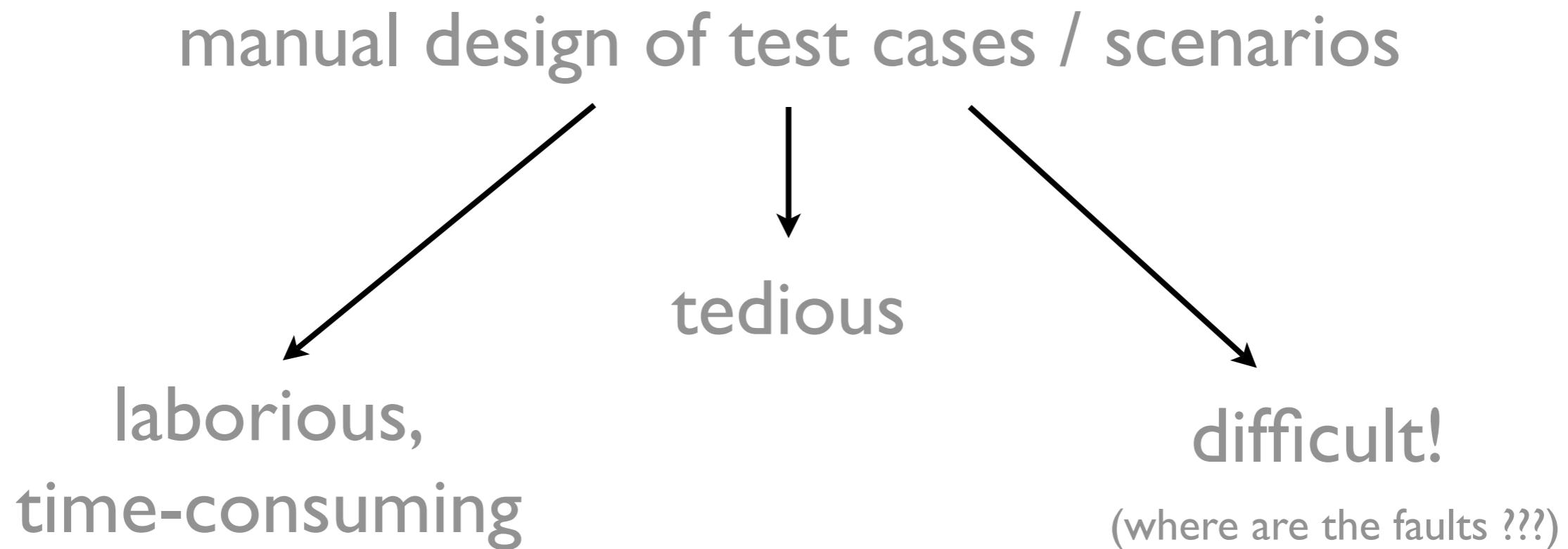
manual design of test cases / scenarios

```
graph TD; A[manual design of test cases / scenarios] --> B[tedious]; B --> C[laborious,  
time-consuming]
```

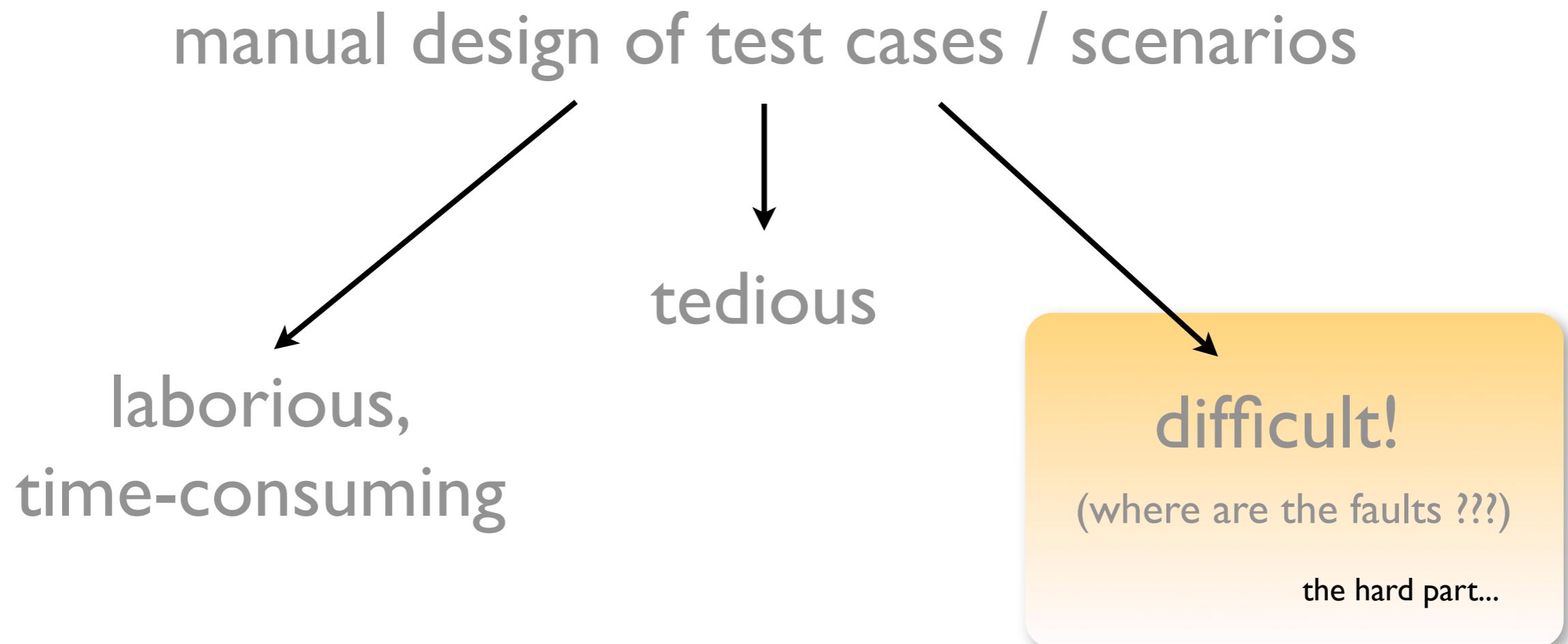
tedious

laborious,
time-consuming

Conventional Testing



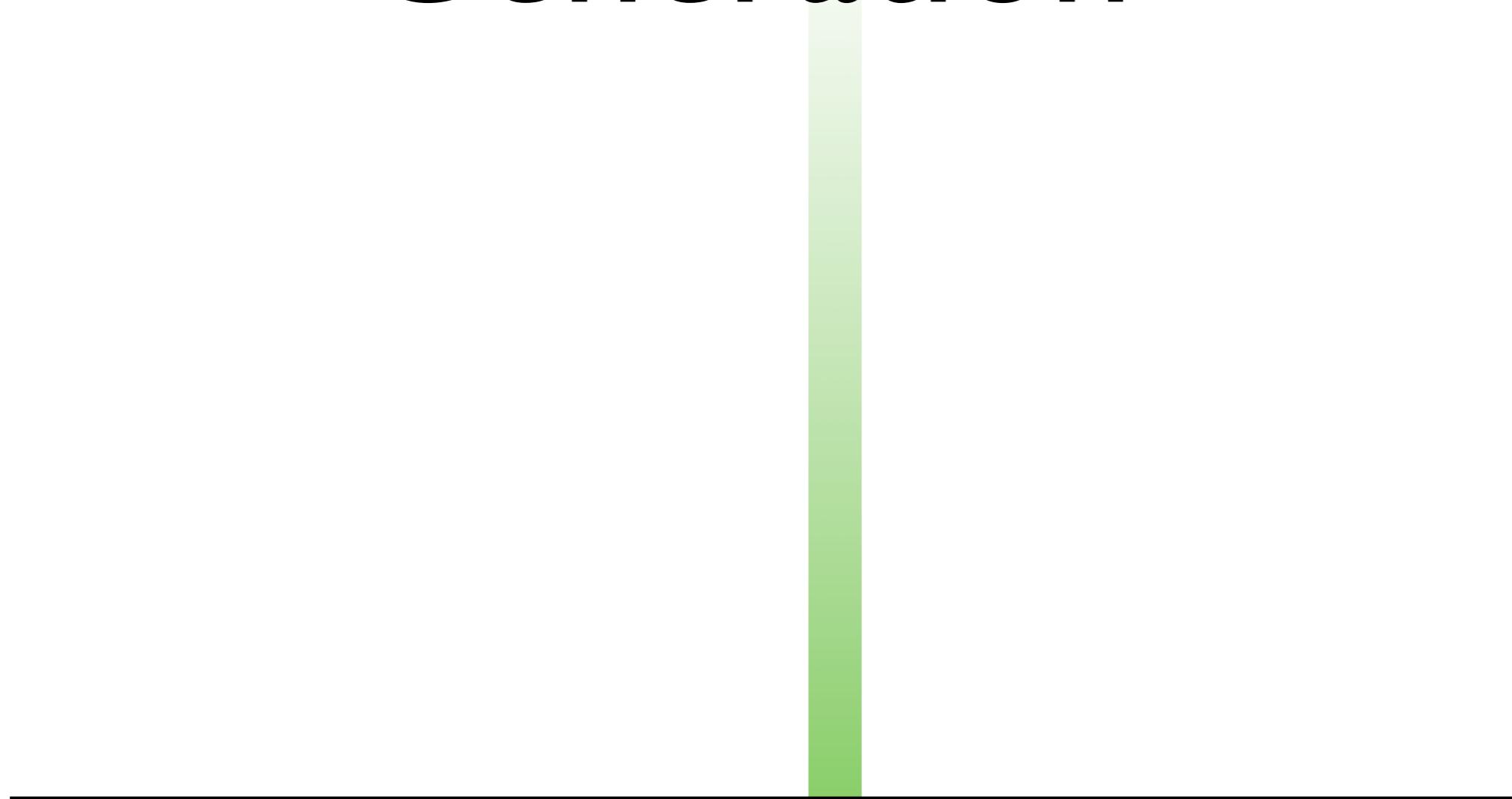
Conventional Testing



Random Test Data Generation

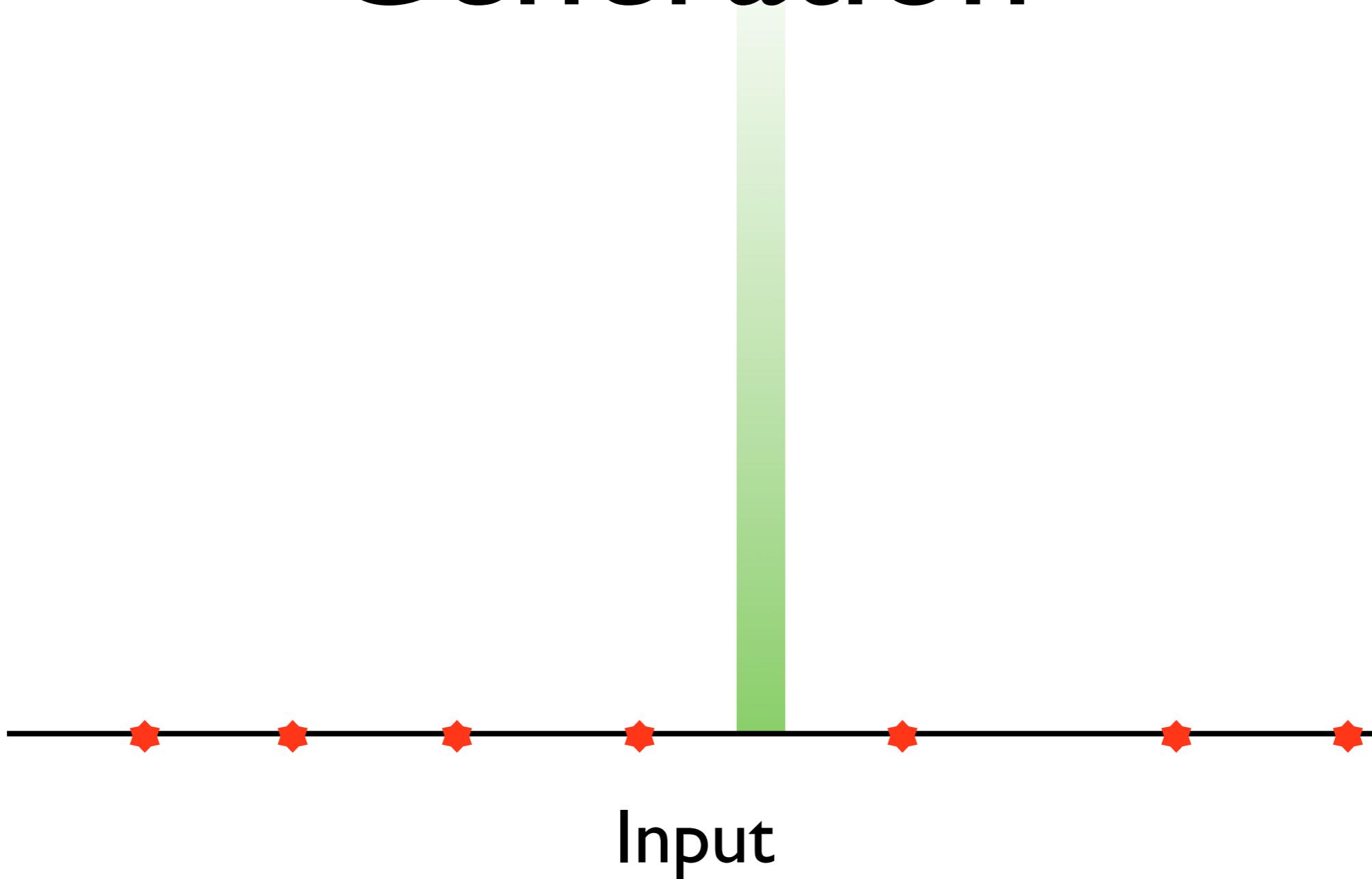
Input

Random Test Data Generation



Input

Random Test Data Generation



Search-Based Testing is an automated *search* of a potentially large input space

the search is guided by a
problem-specific ‘fitness function’

Search-Based Testing is an automated *search* of a potentially large input space

the search is guided by a
problem-specific ‘fitness function’

the **fitness function** guides the search
to the test goal

Fitness Function

The fitness function **scores** different inputs
to the system according to the test goal

Fitness Function

The fitness function **scores** different inputs to the system according to the test goal

which ones are ‘good’
(that we should develop/evolve further)



Fitness Function

The fitness function **scores** different inputs to the system according to the test goal

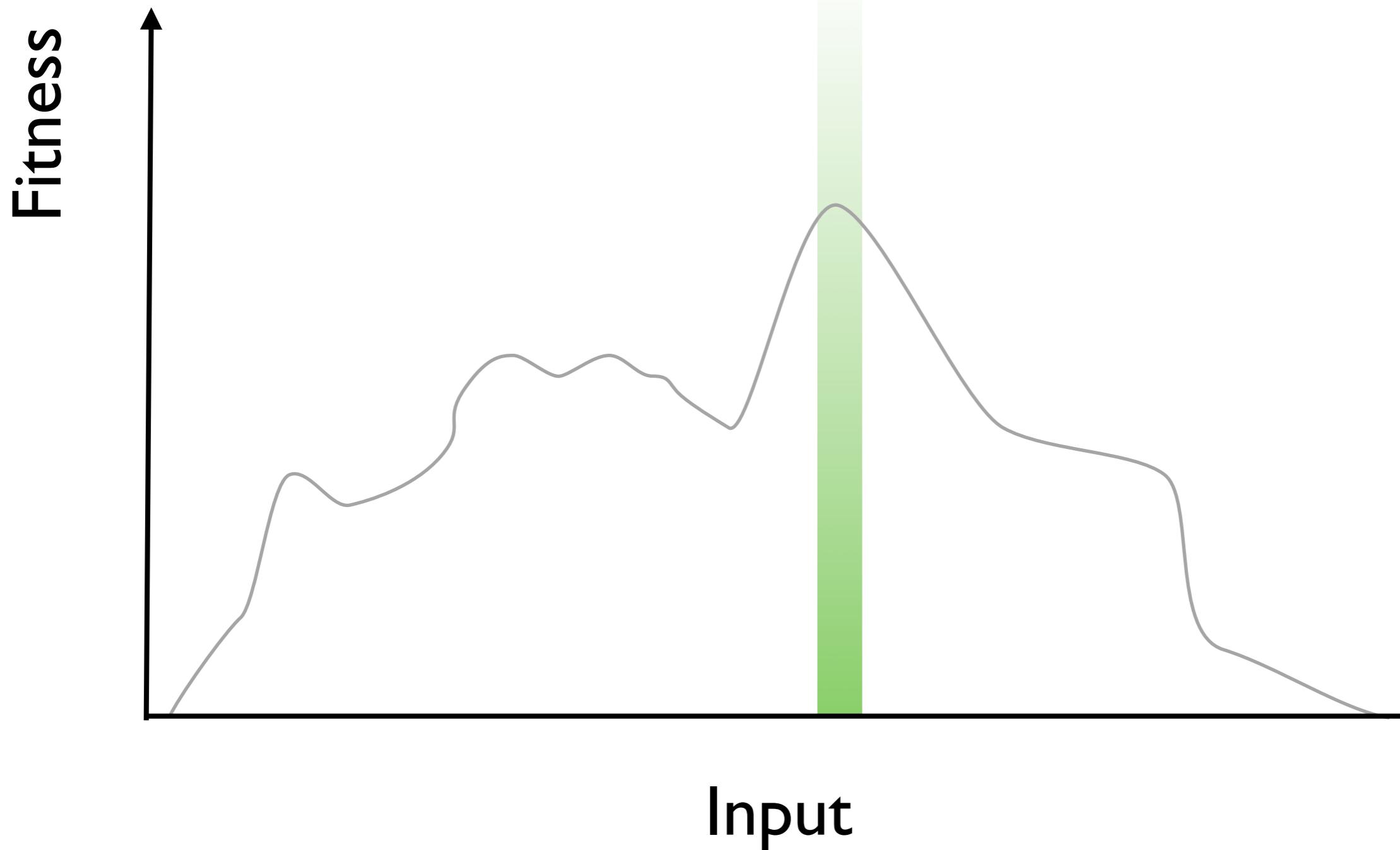
which ones are ‘good’
(that we should develop/evolve further)



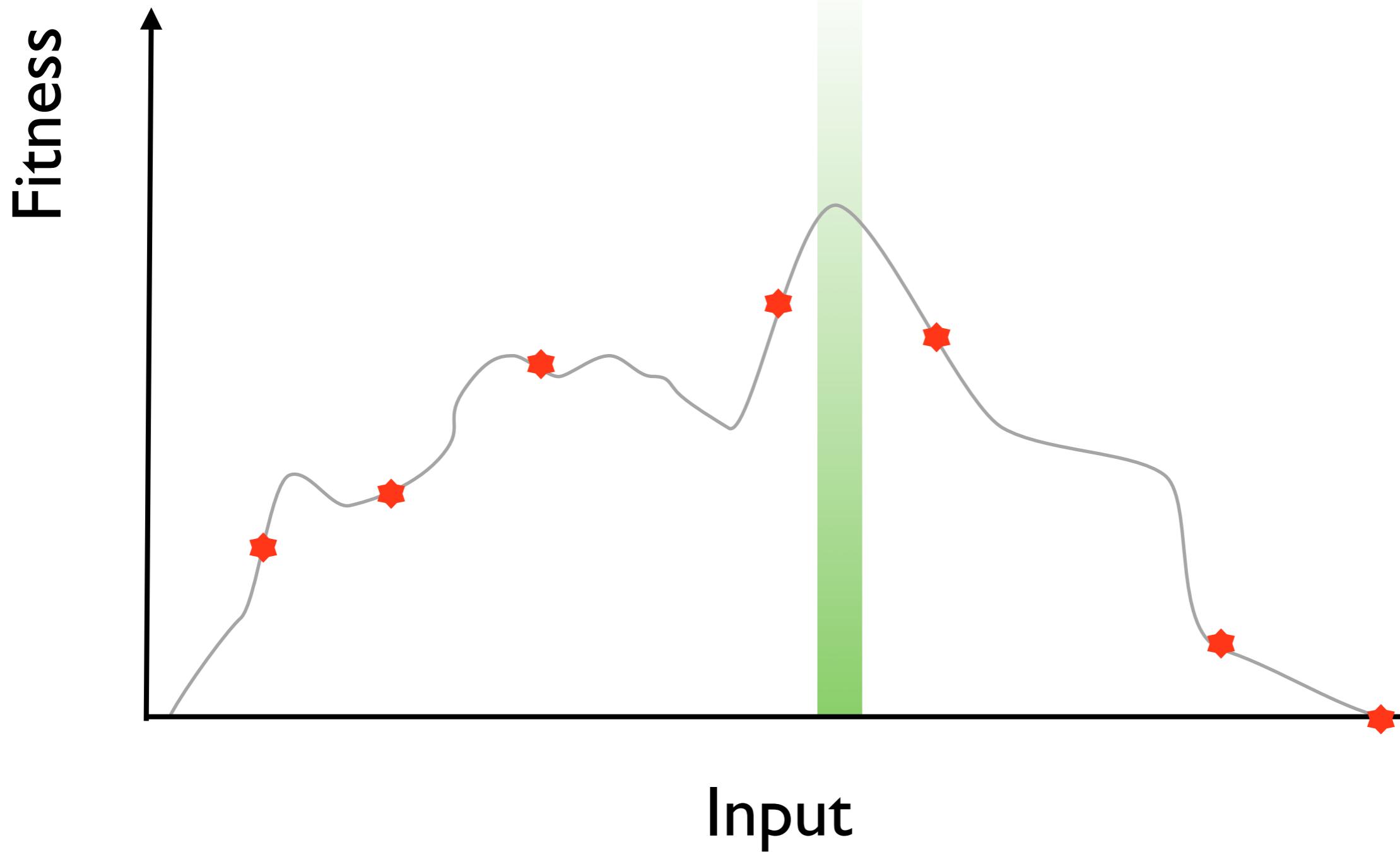
which ones are useless
(that we can forget about)



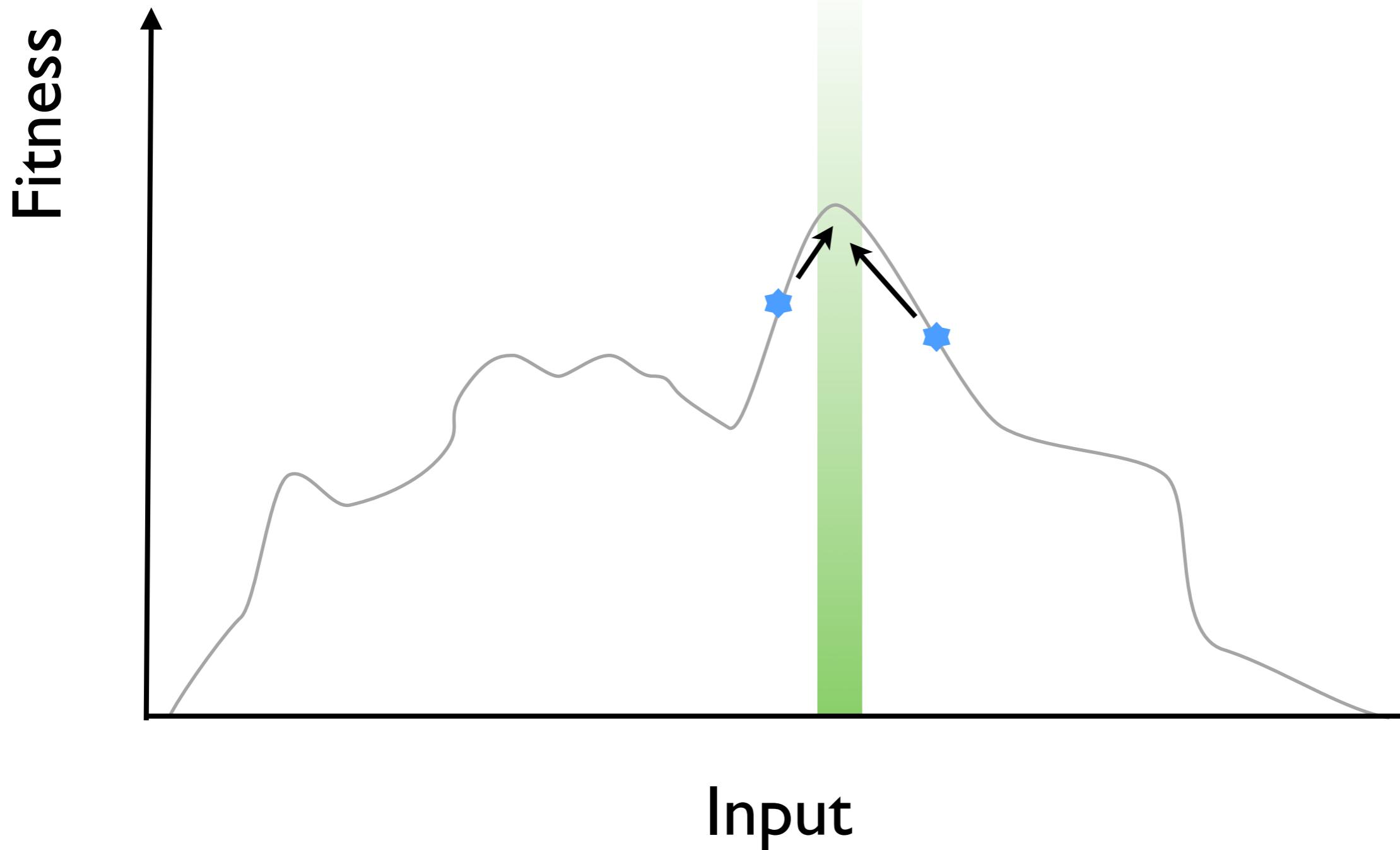
Fitness-guided search



Fitness-guided search



Fitness-guided search



First publication on SBST

Automatic Generation of Floating-Point Test Data
IEEE Transactions on Software Engineering, 1976

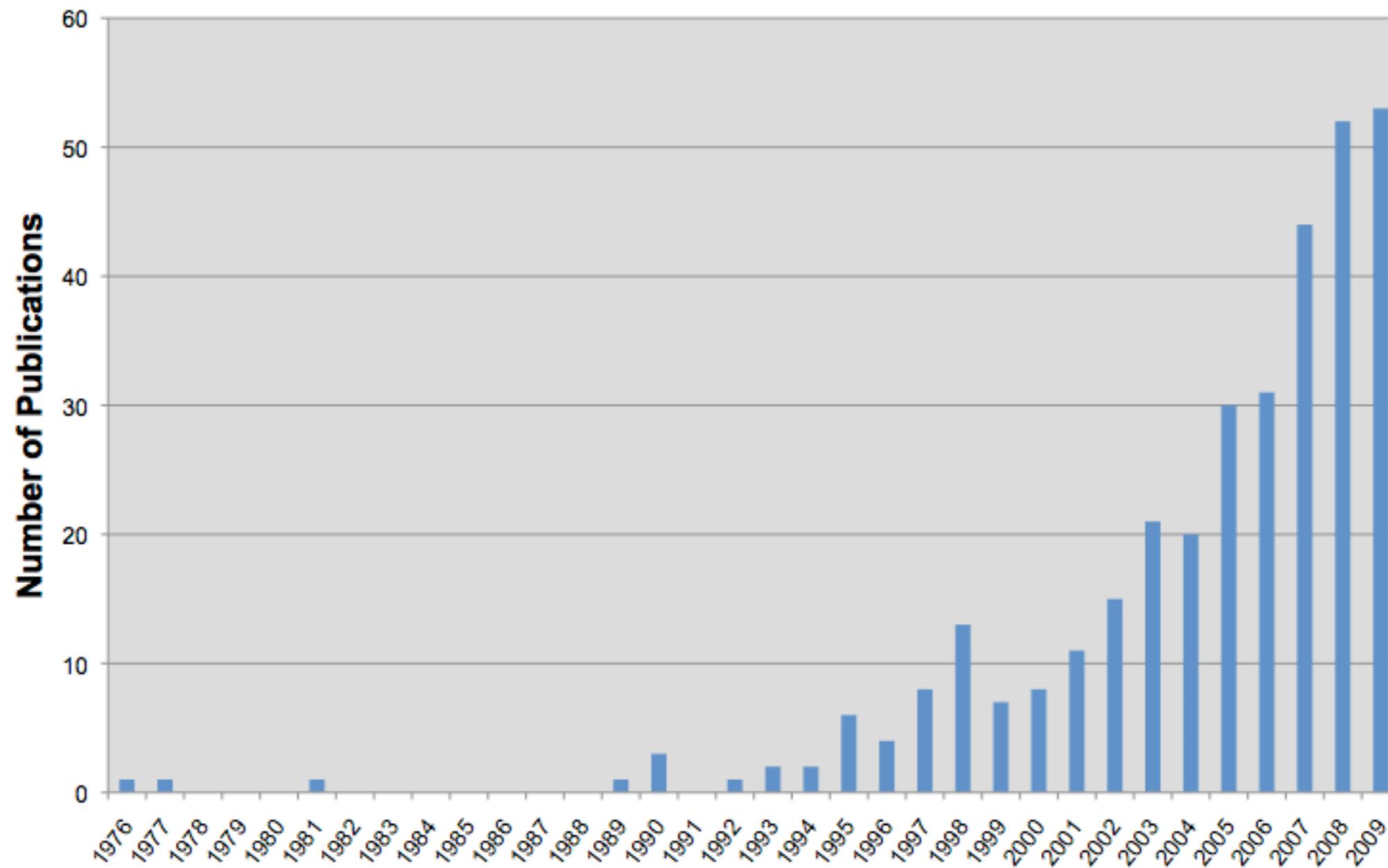
Webb Miller

David Spooner

Winner of the 2009 [Accomplishment by a Senior Scientist Award](#)
of the International Society for Computational Biology

2009 Time 100
Scientists and Thinkers

Publications since 1976



source: SEBASE publications repository <http://www.sebase.org>

International Search-Based Testing Workshop

co-located with ICST

4th event at ICST 2011
next year

check websites for
submission deadlines etc.:

<http://sites.google.com/site/icst2011/>

<http://sites.google.com/site/icst2011workshops/>



International Symposium on Search-Based Software Engineering

www.ssbse.org



Benevento, Italy.
7th - 9th September 2010



International Symposium on Search-Based Software Engineering

www.ssbse.org

2011: Co-location with FSE.
Szeged, Hungary



Phil McMinn
General Chair



Myra Cohen and Mel Ó Cinnéide
Program Chairs



Fitness Functions

Often easy

We often define metrics

Need not be complex

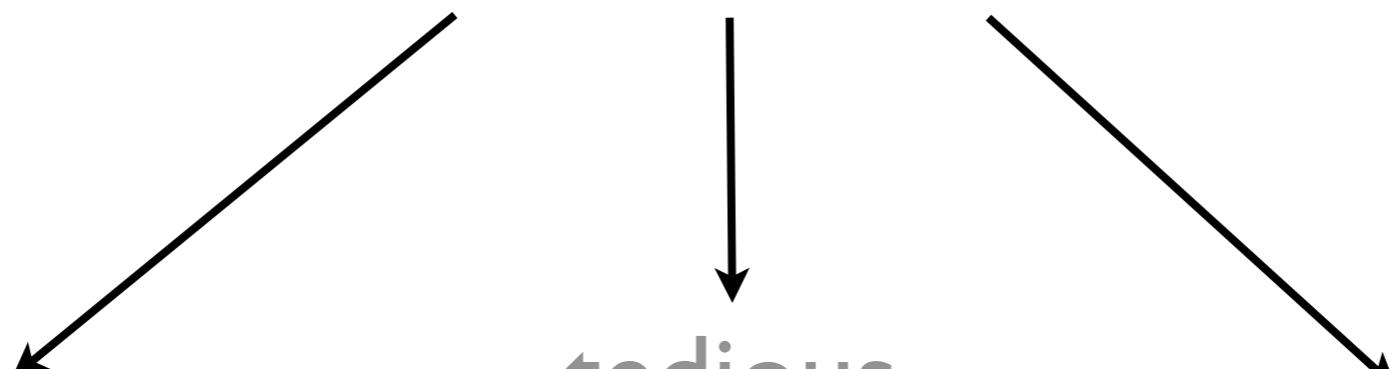
Conventional testing

manual design of test cases / scenarios

laborious,
time-consuming

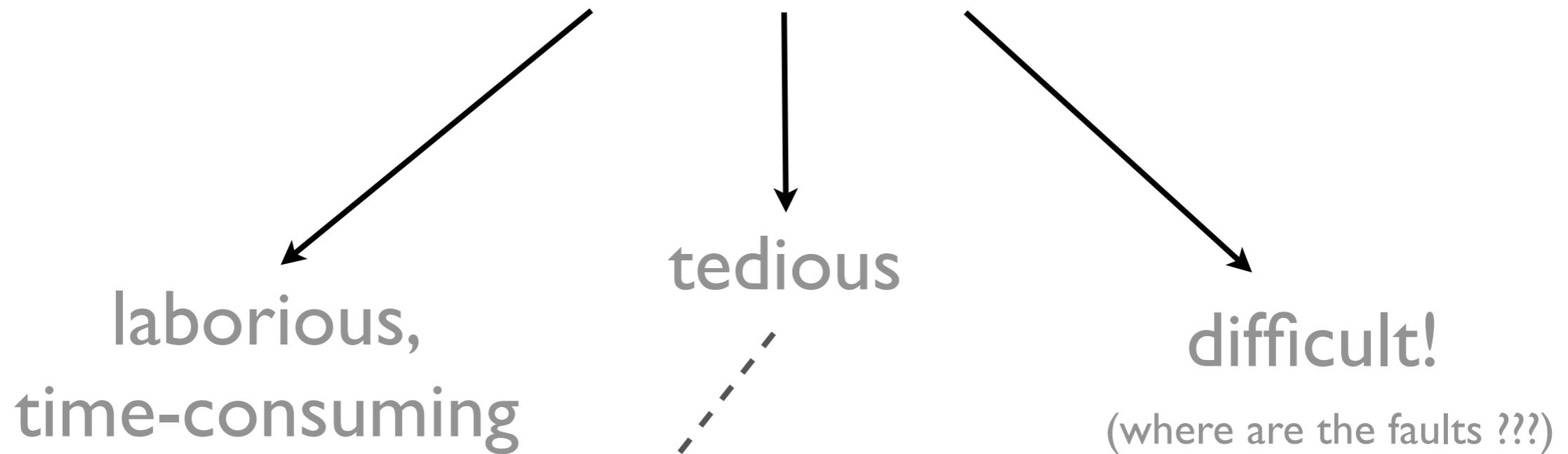
tedious

difficult!
(where are the faults ???)



Conventional testing

manual design of test cases / scenarios



Search-Based Testing:

automatic - may sometimes be
time consuming, but it is not a
human's time being consumed

Conventional testing

manual design of test cases / scenarios

laborious,
time-consuming

tedious

difficult!

(where are the faults ???)

Search-Based Testing:
automatic - may sometimes be
time consuming, but it is not a
human's time being consumed

Search-Based Testing:
a good fitness function
will lead the search to
the faults

Generating vs Checking

Conventional Software Testing Research

Write a method to construct test cases

Search-Based Testing

Write a method
to determine how good a test case is

Generating vs Checking

Conventional Software Testing Research

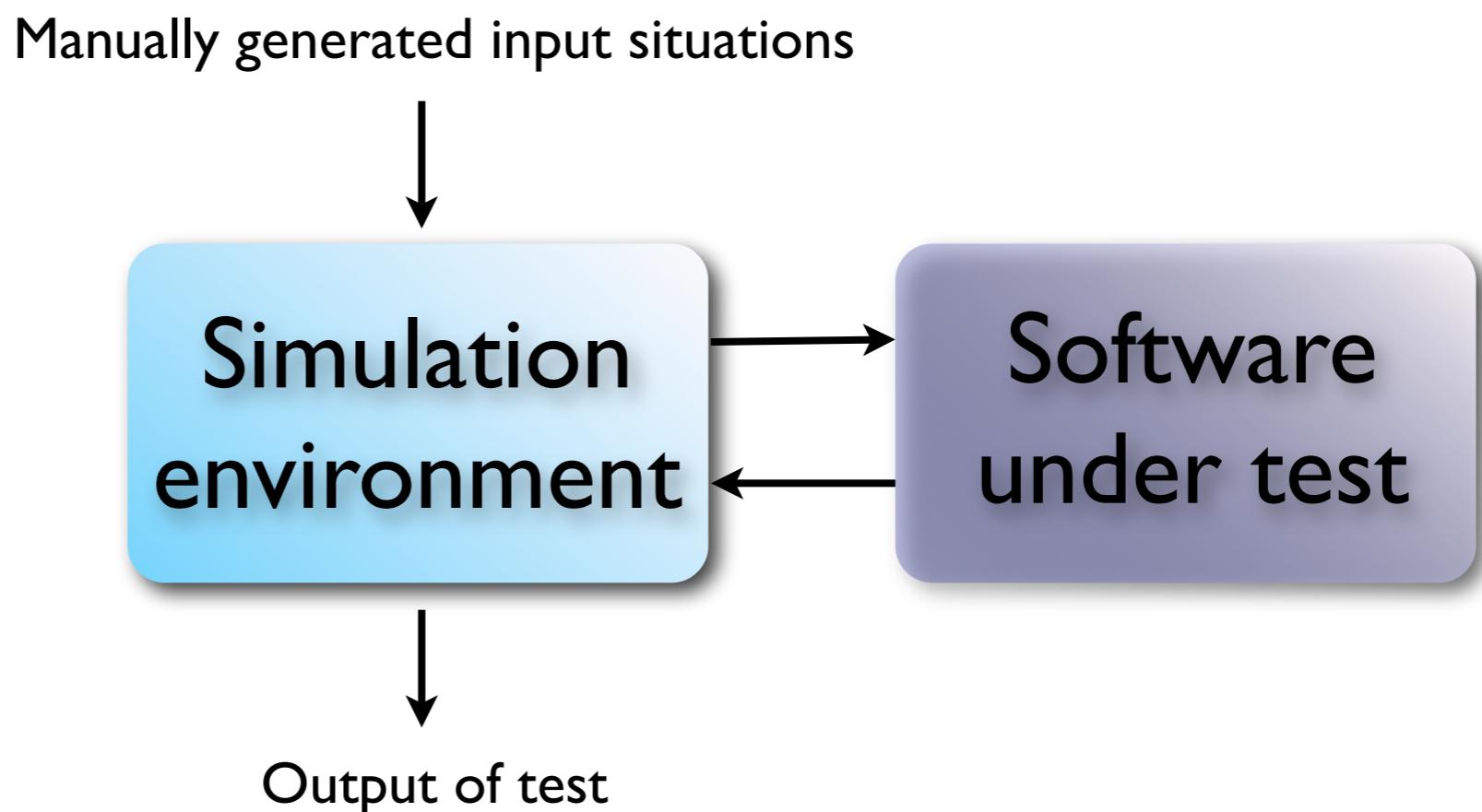
Write a method to construct test cases

Search-Based Testing

Write a **fitness function**
to determine how good a test case is

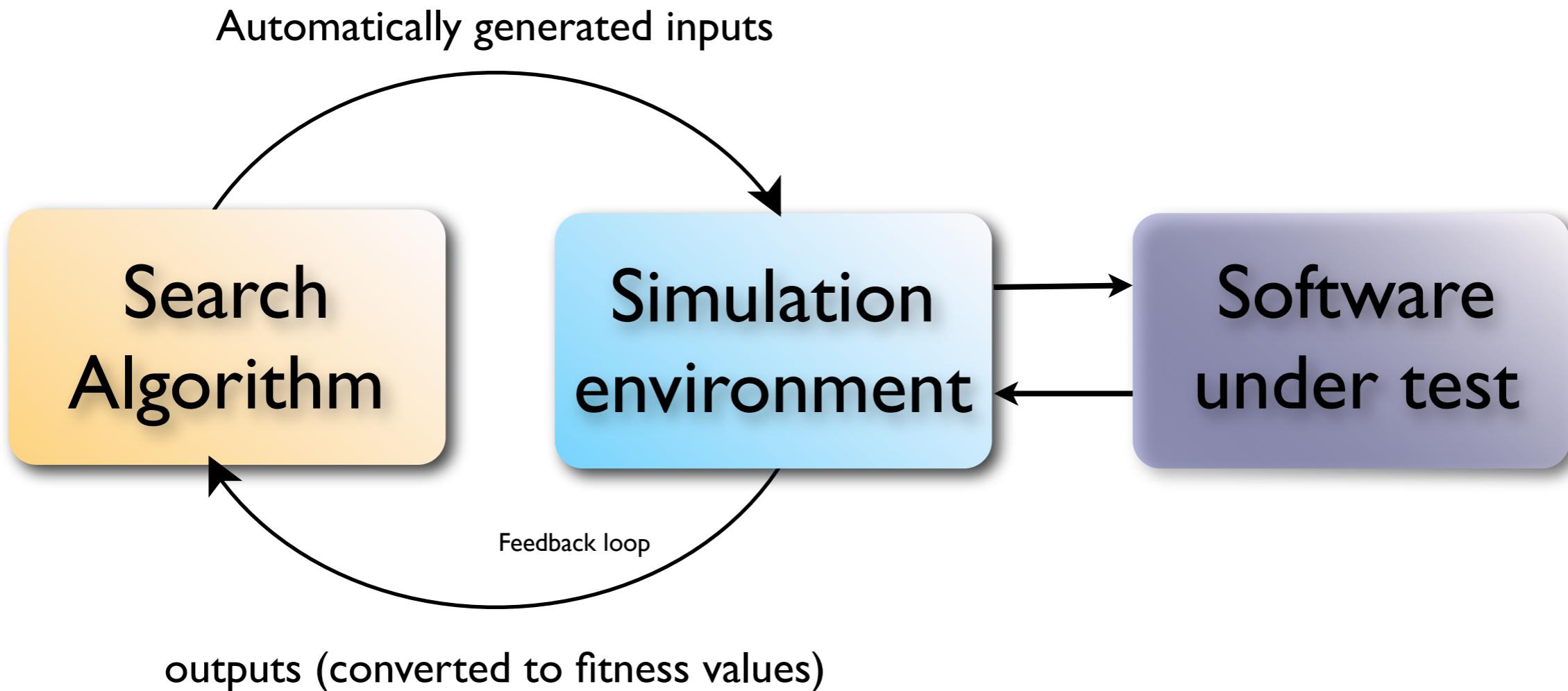
Test setup

Usual approach to testing

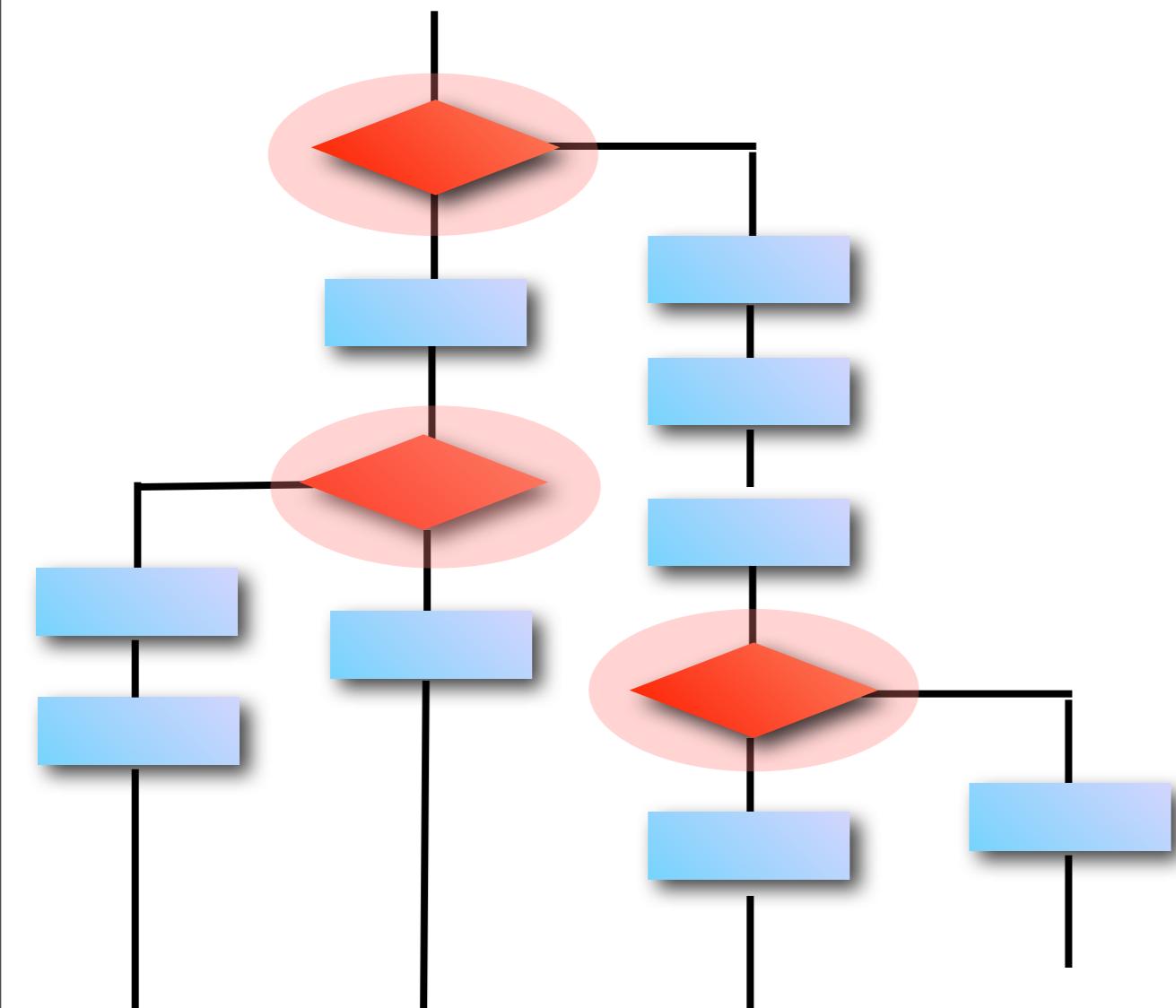


Test setup

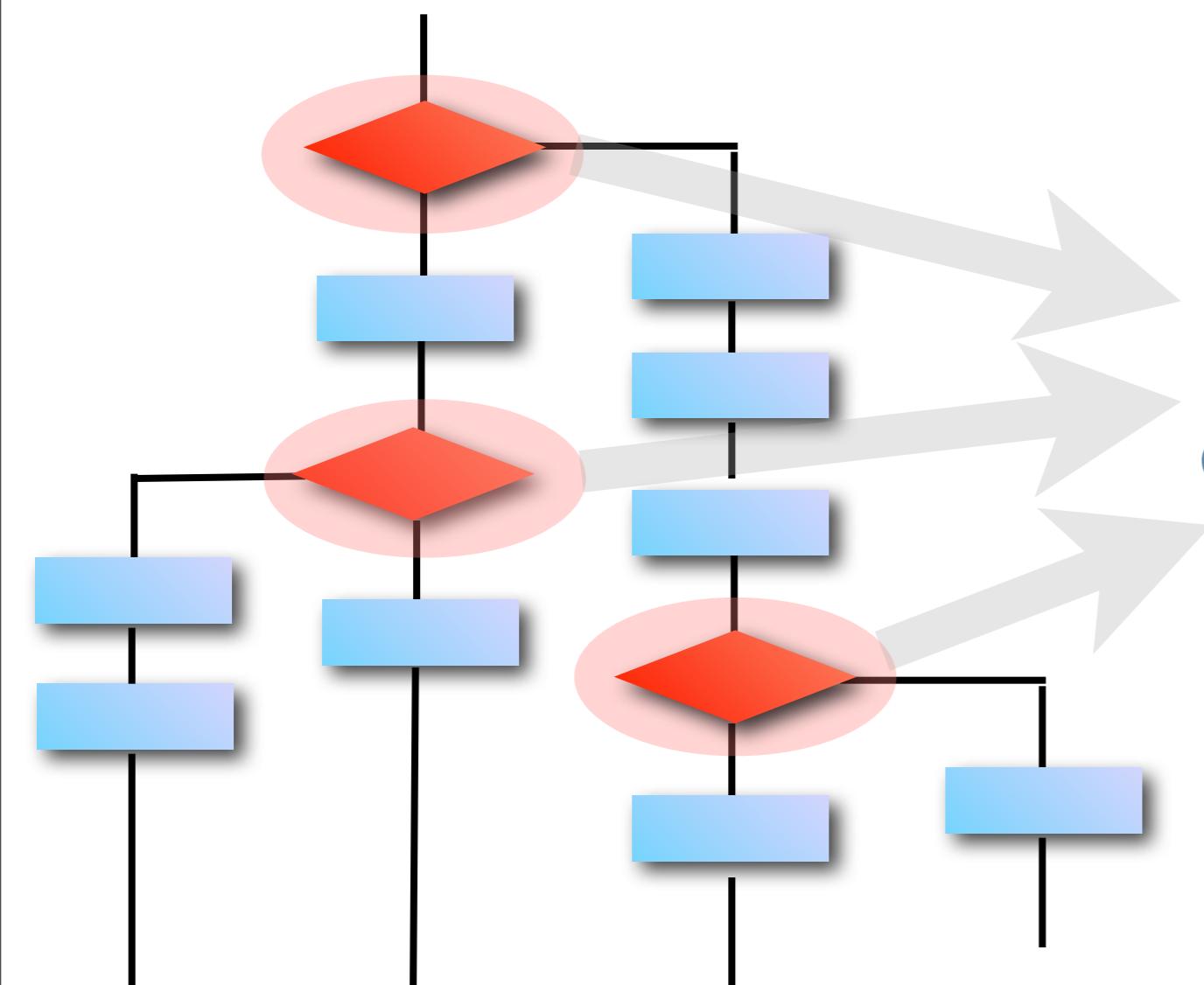
Search-Based Testing approach



Structural testing

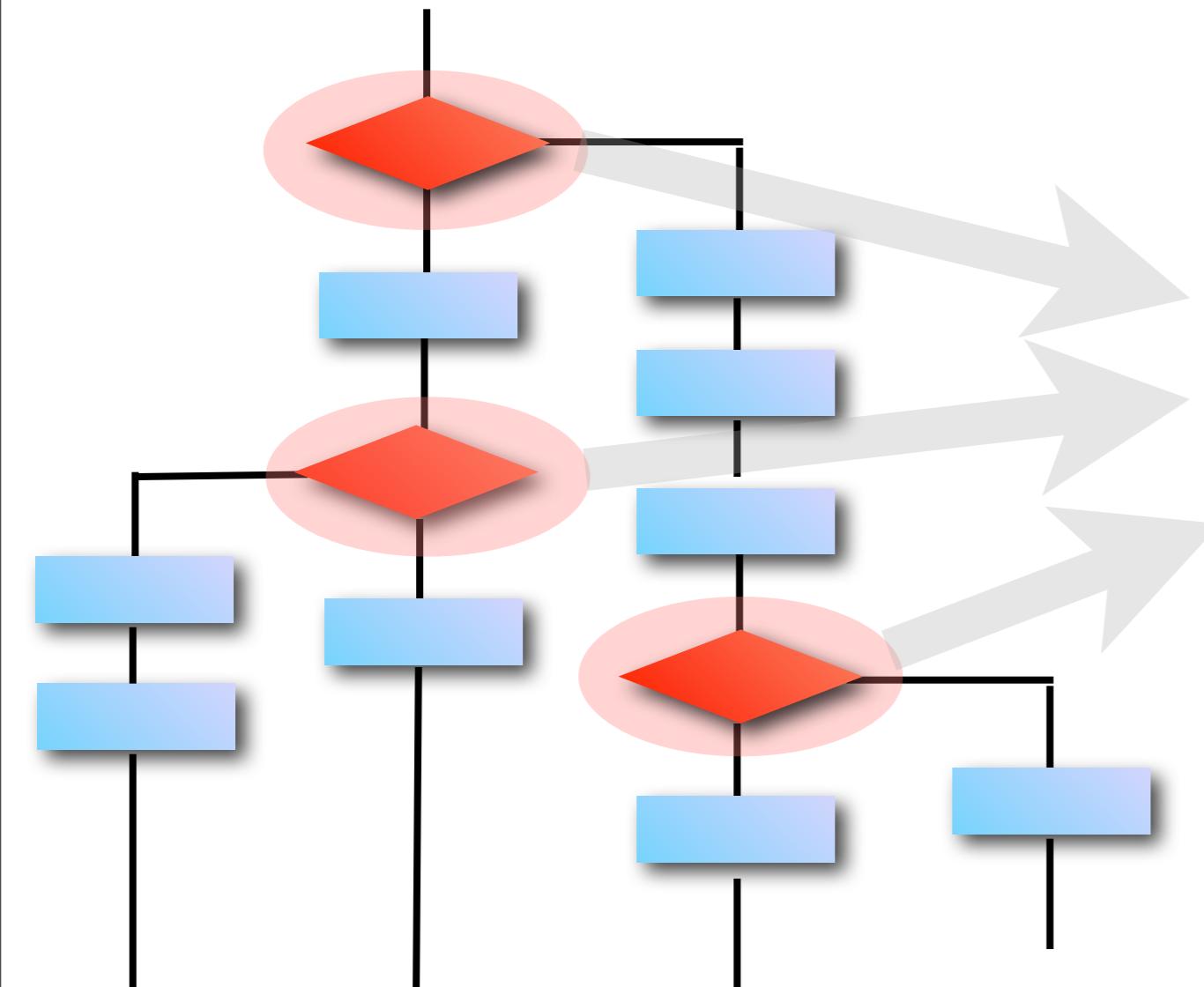


Structural testing



fitness function analyses
the outcome of
decision statements and the
values of variables in
predicates

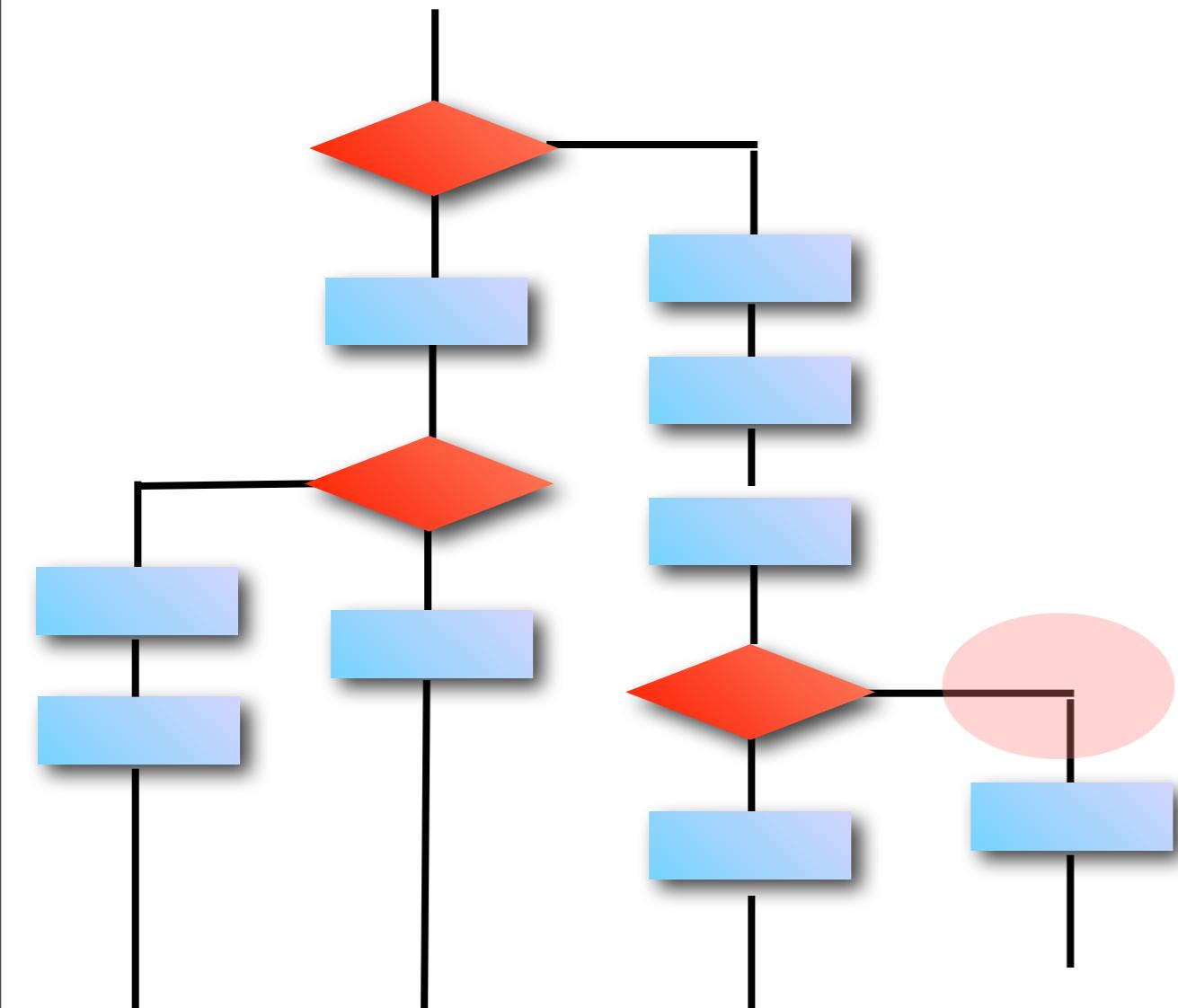
Structural testing



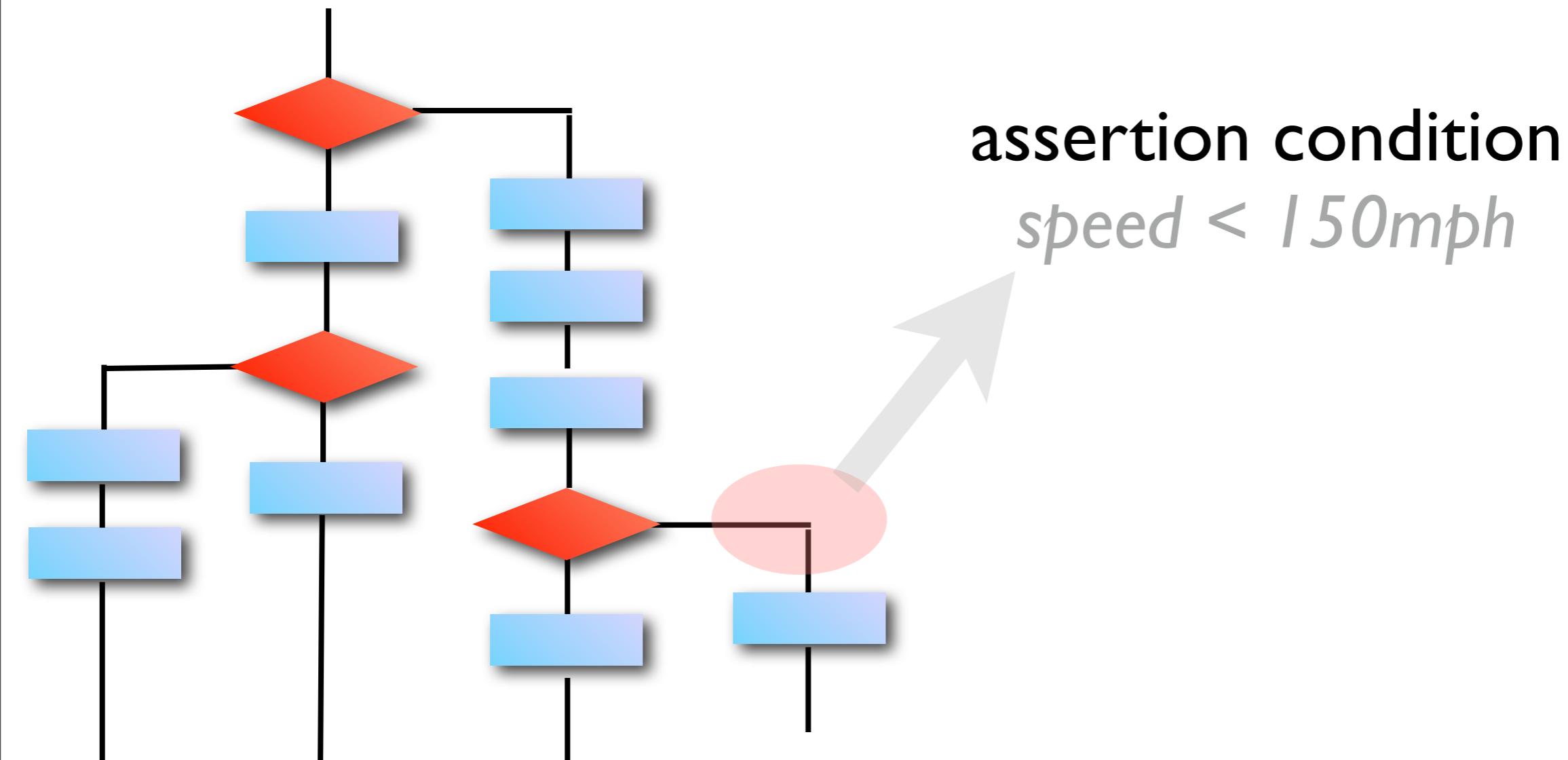
fitness function analyses
the outcome of
decision statements and the
values of variables in
predicates

More later ...

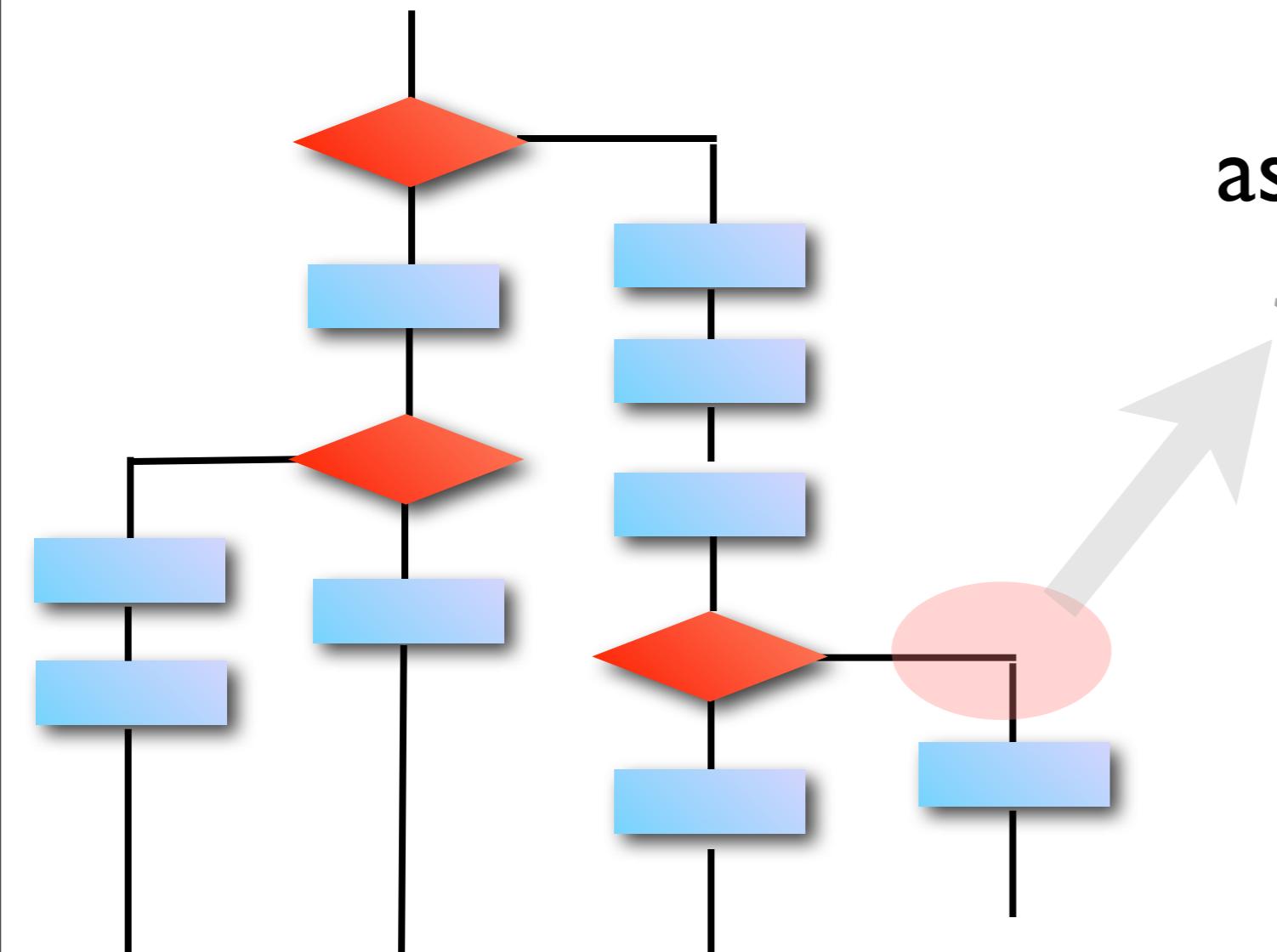
Assertion testing



Assertion testing



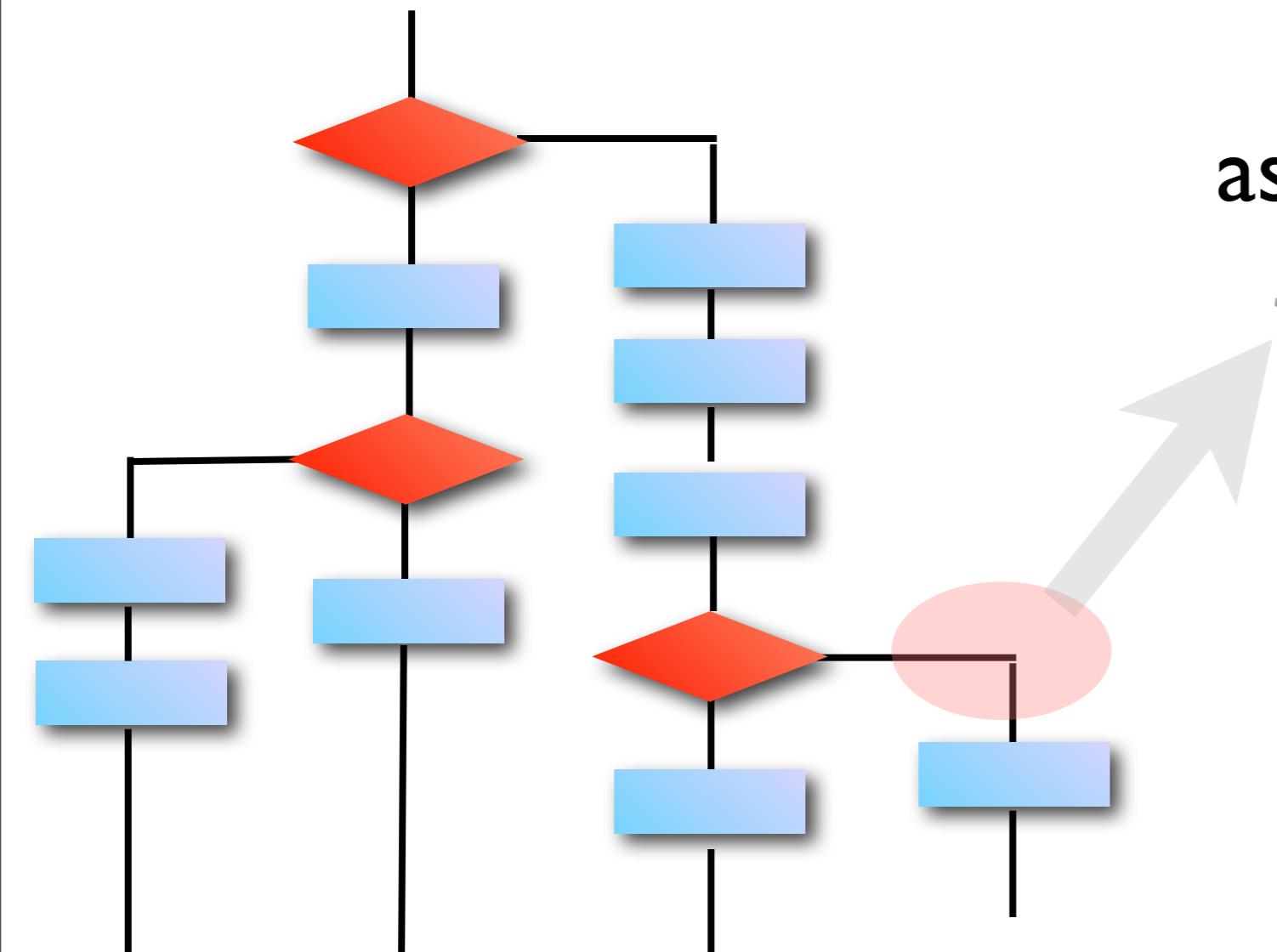
Assertion testing



assertion condition
speed < 150mph

fitness function:
 $f = 150 - \text{speed}$

Assertion testing



assertion condition
 $speed < 150\text{mph}$

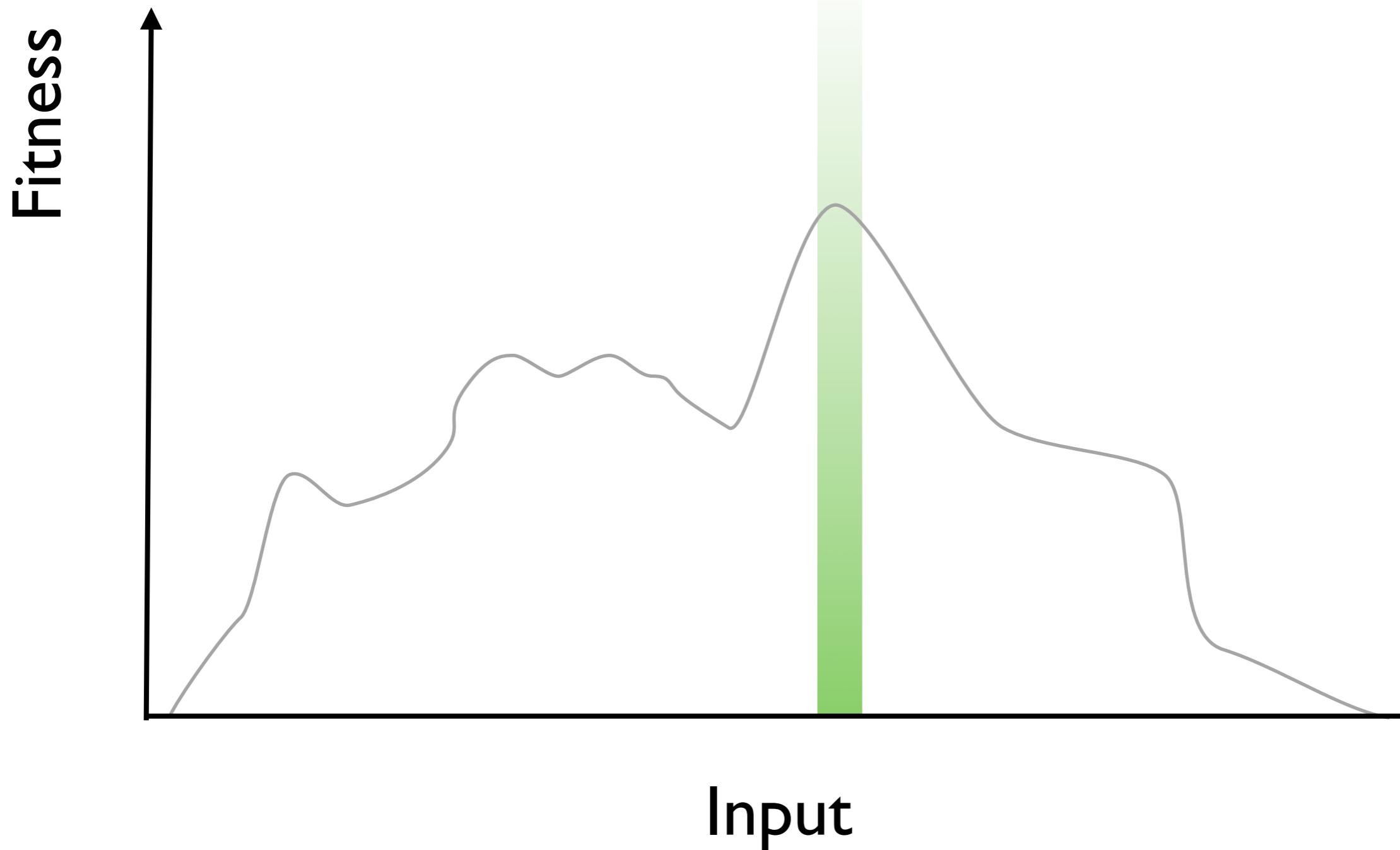
fitness function:
 $f = 150 - \text{speed}$

fitness minimised

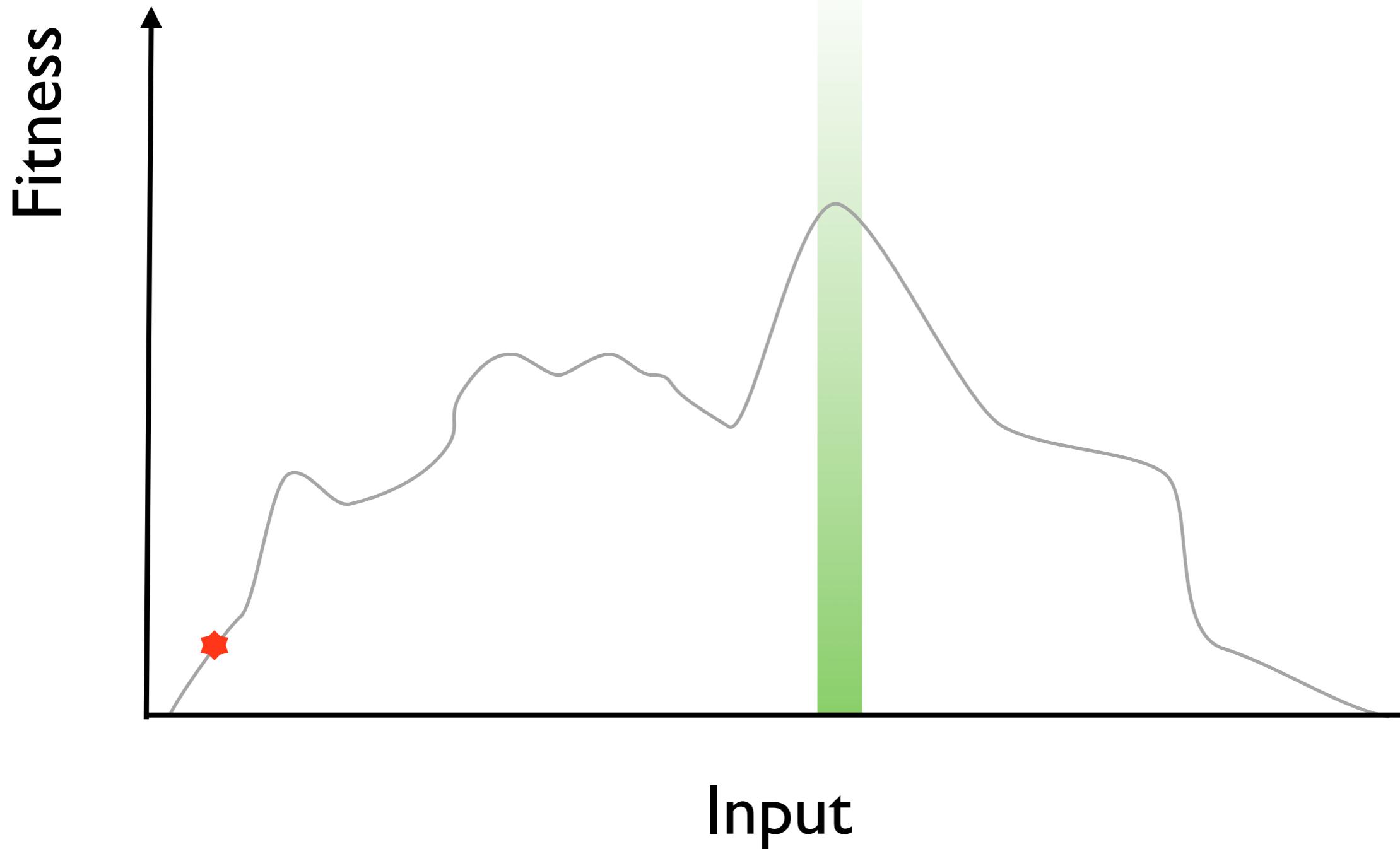
If f is zero or less a **fault is found**

Search Techniques

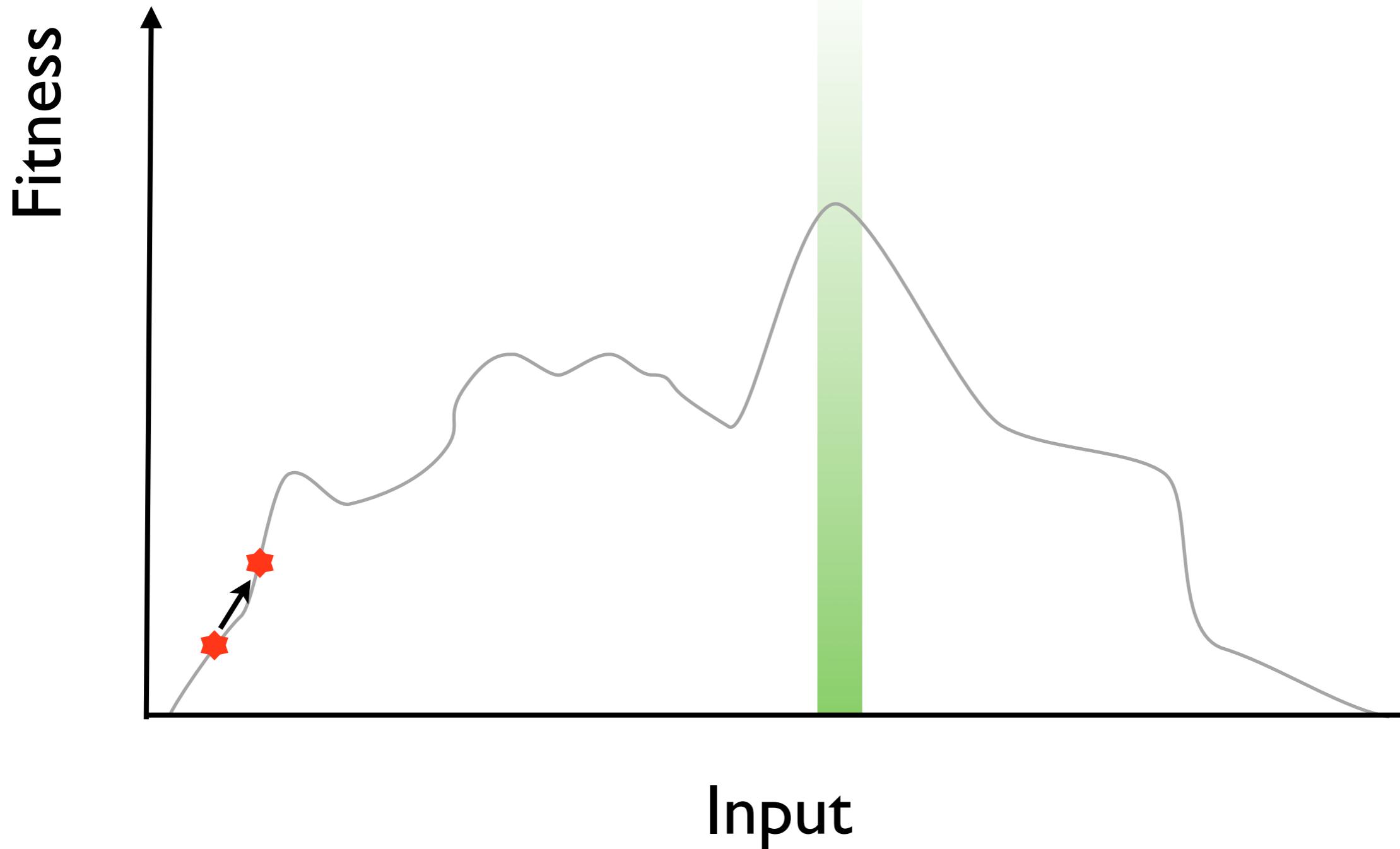
Hill Climbing



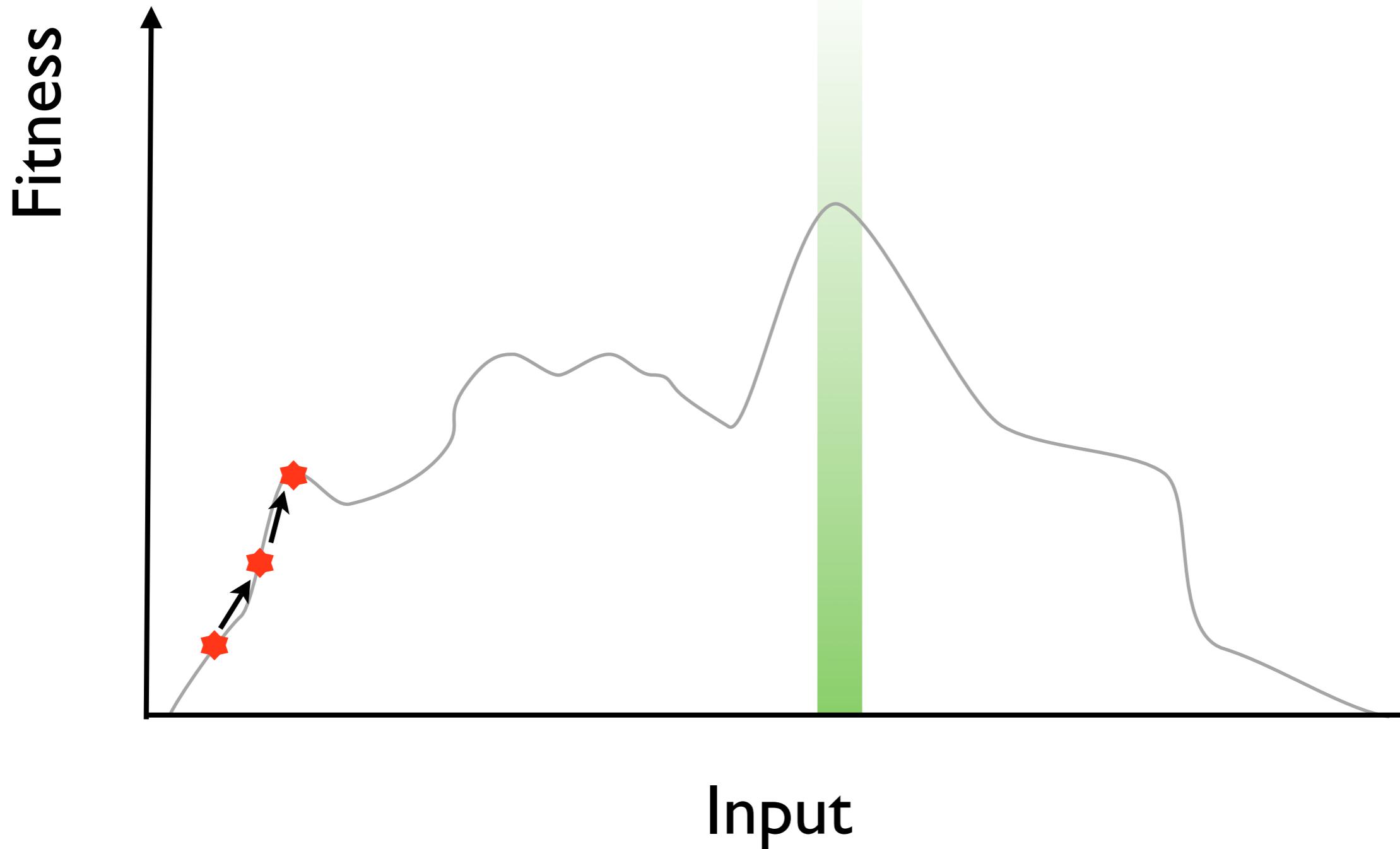
Hill Climbing



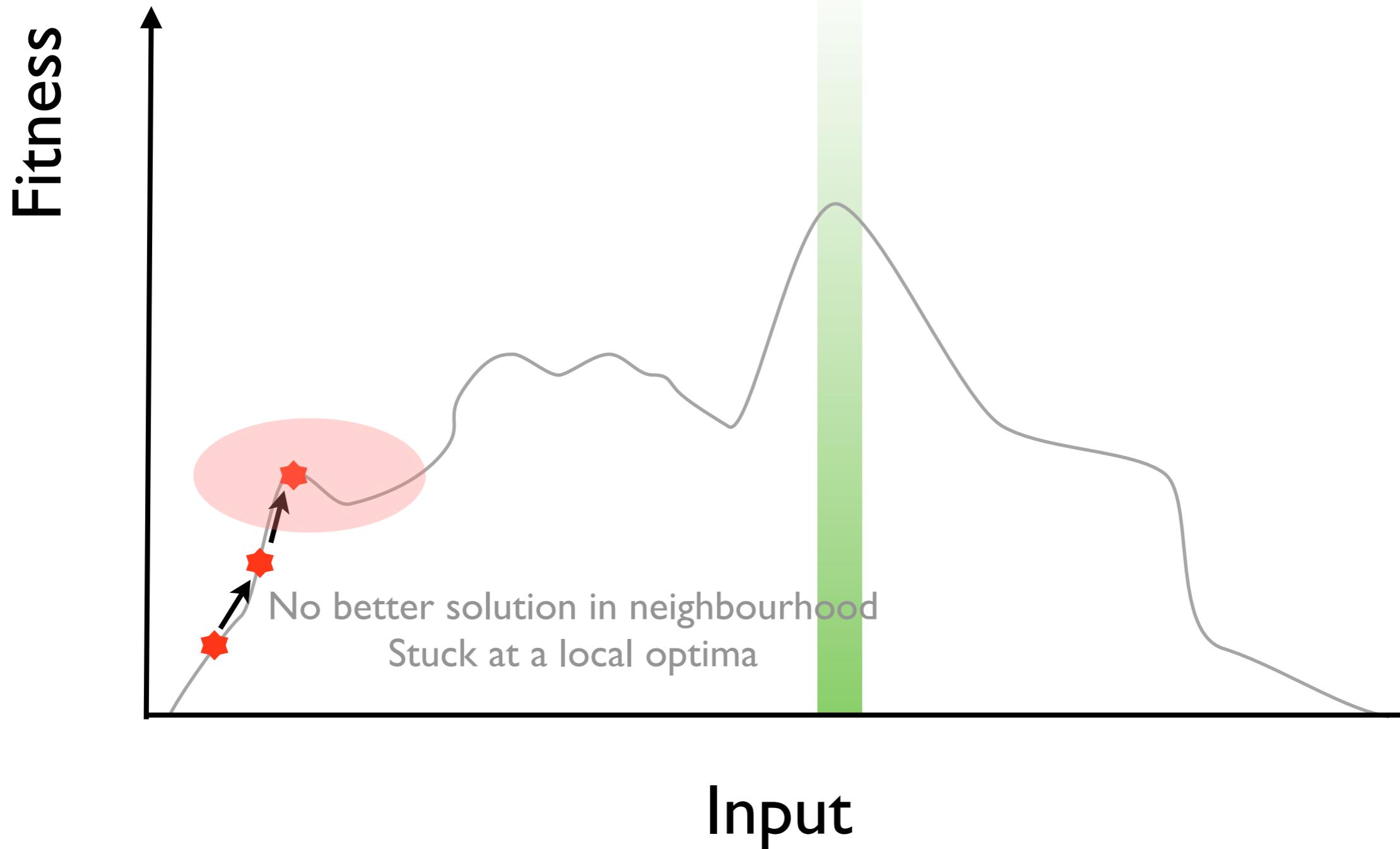
Hill Climbing



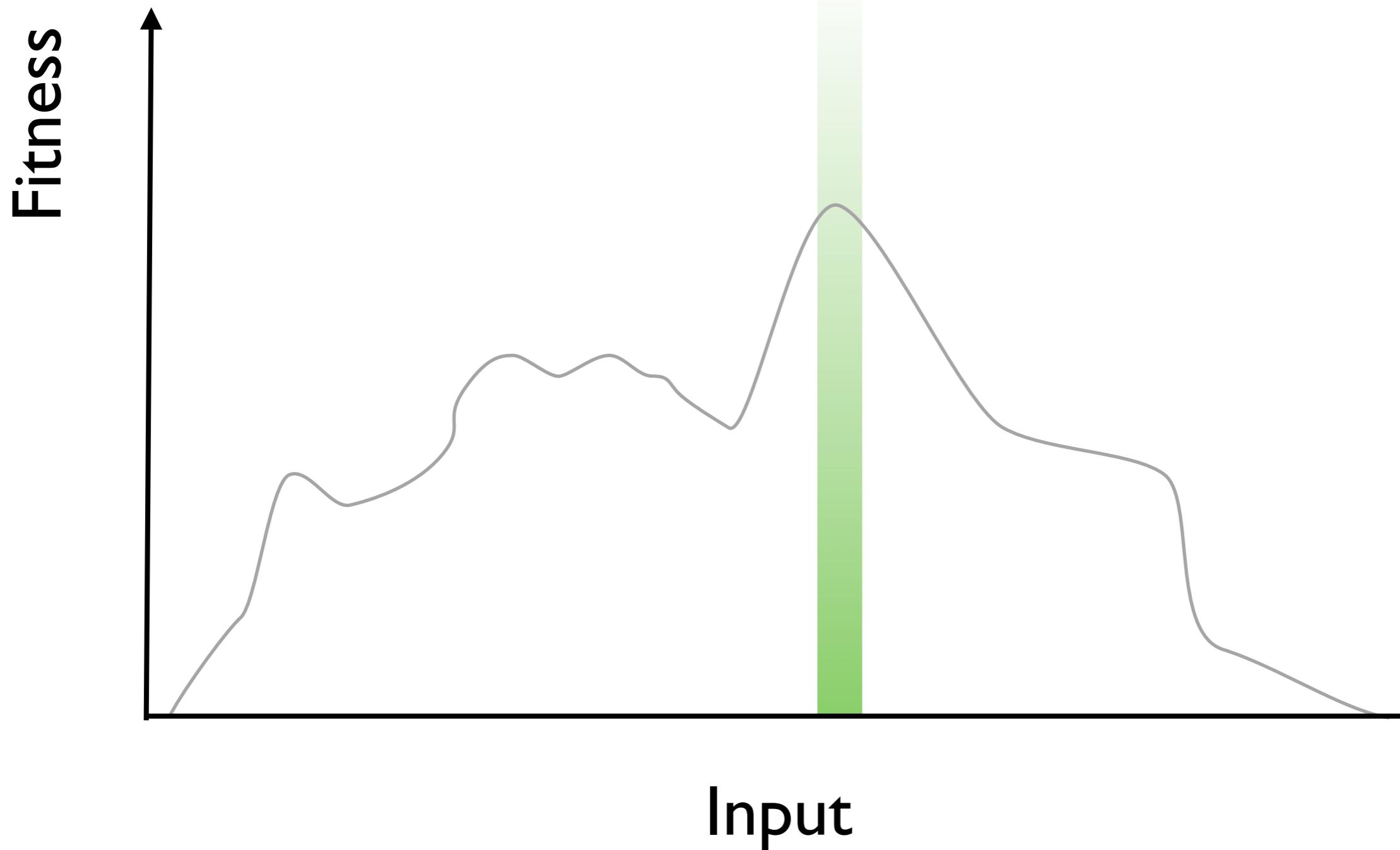
Hill Climbing



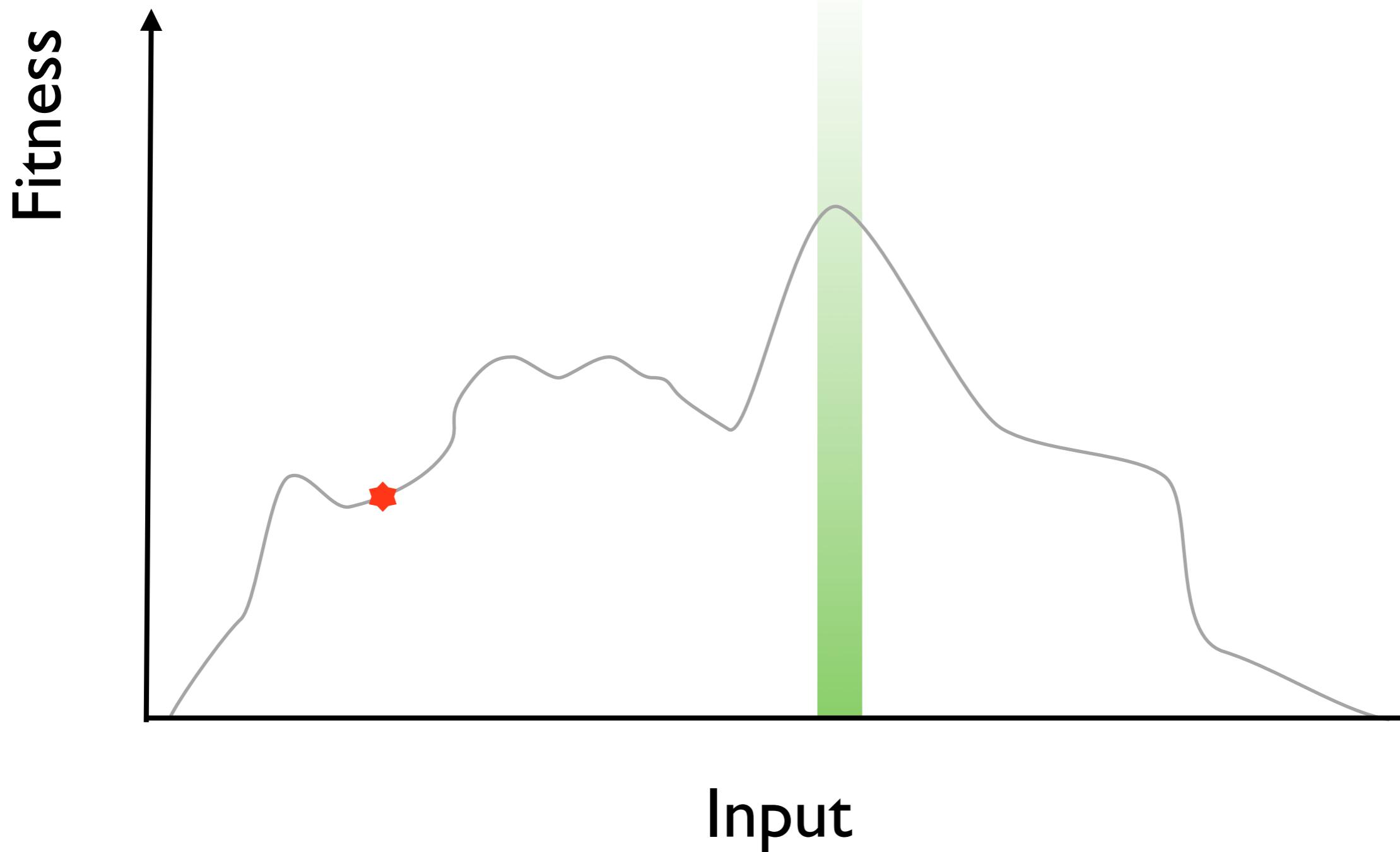
Hill Climbing



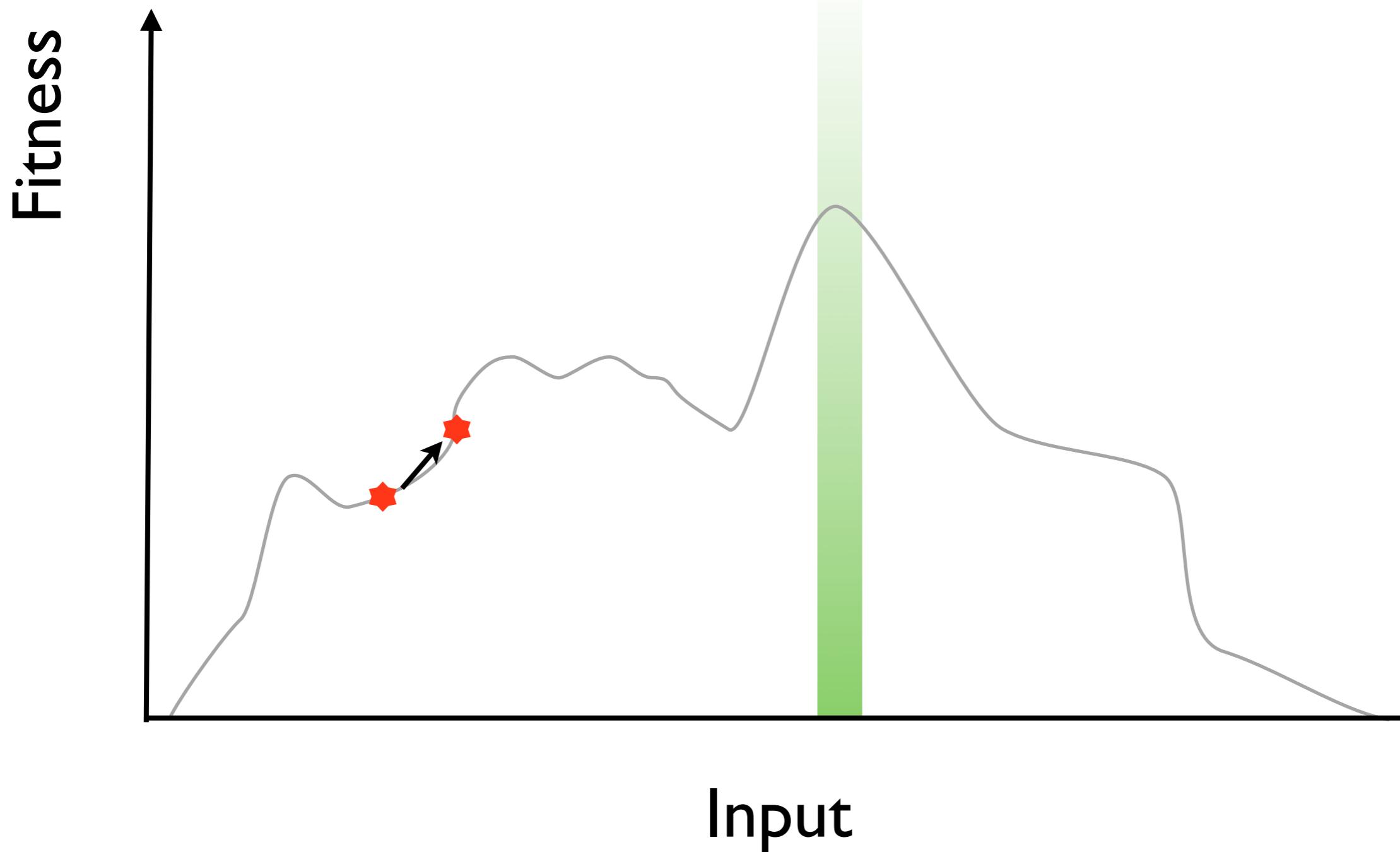
Hill Climbing - Restarts



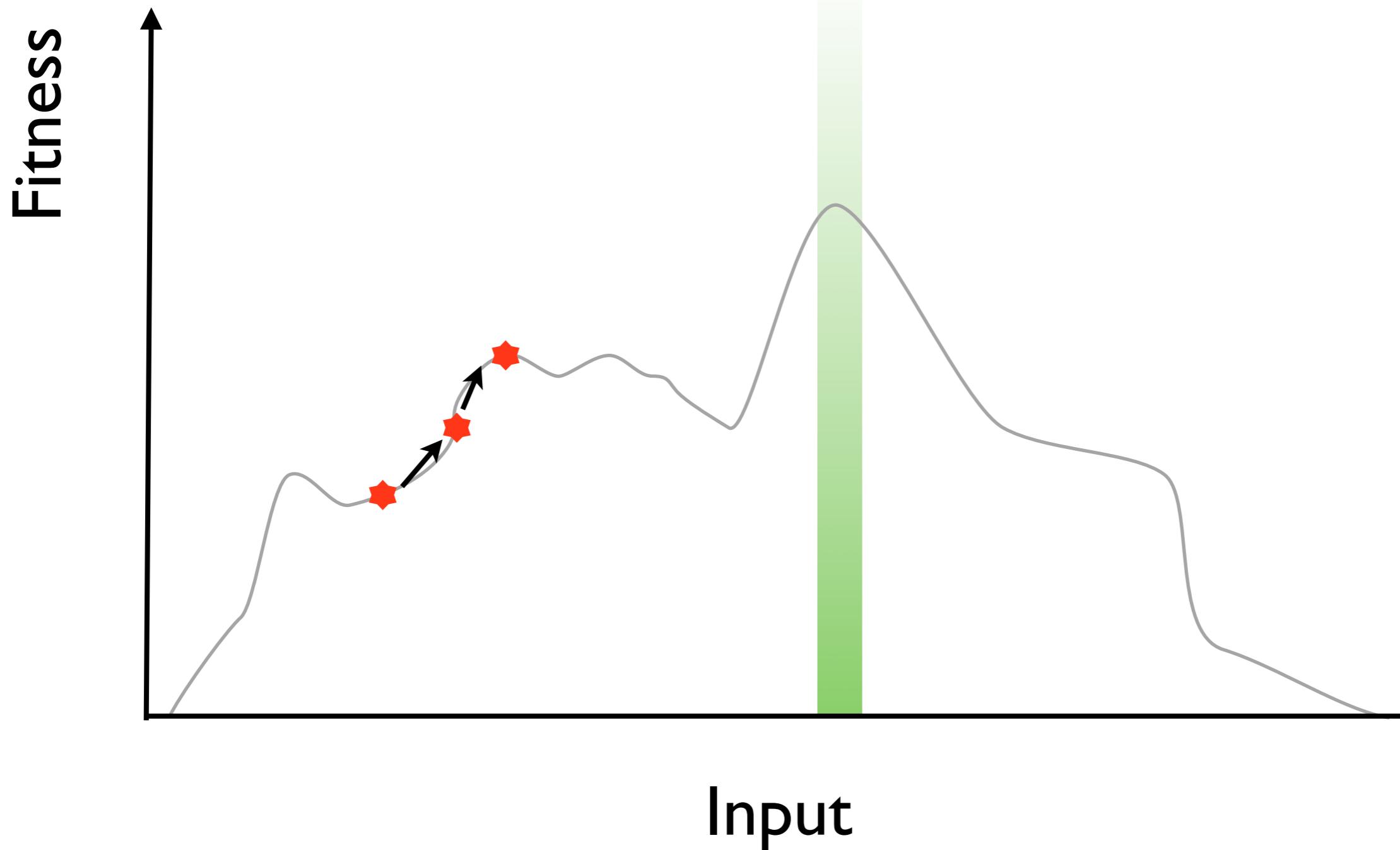
Hill Climbing - Restarts



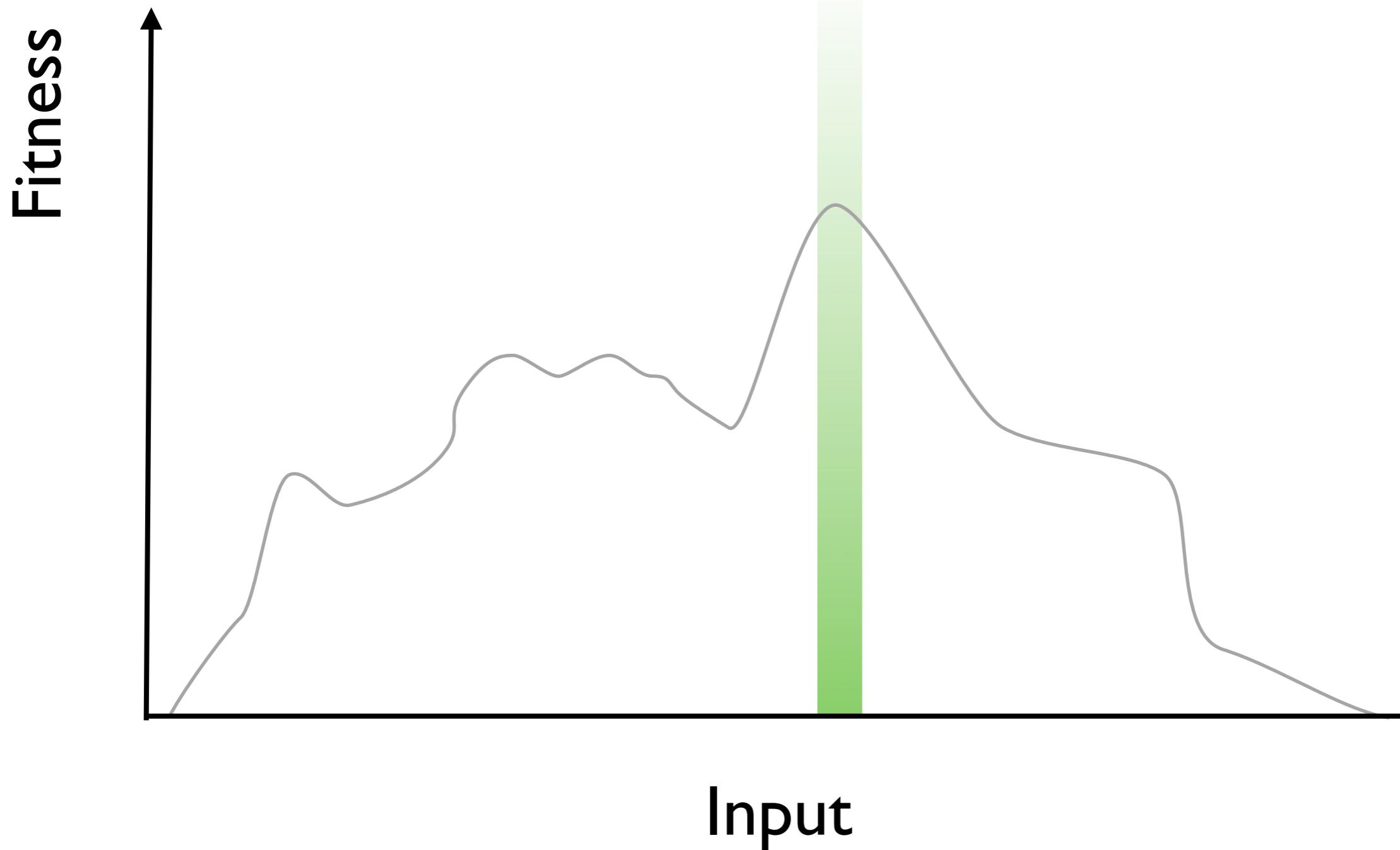
Hill Climbing - Restarts



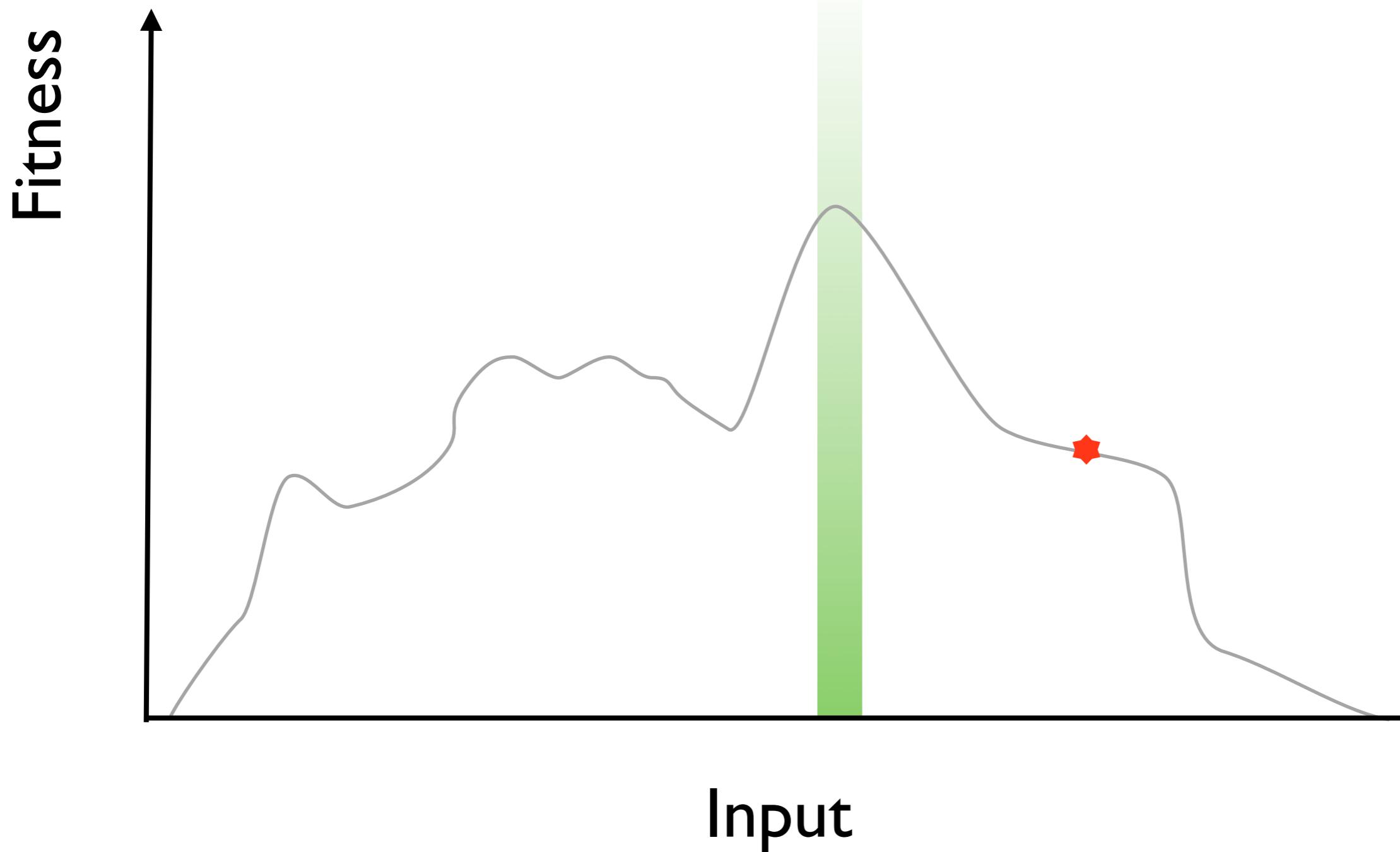
Hill Climbing - Restarts



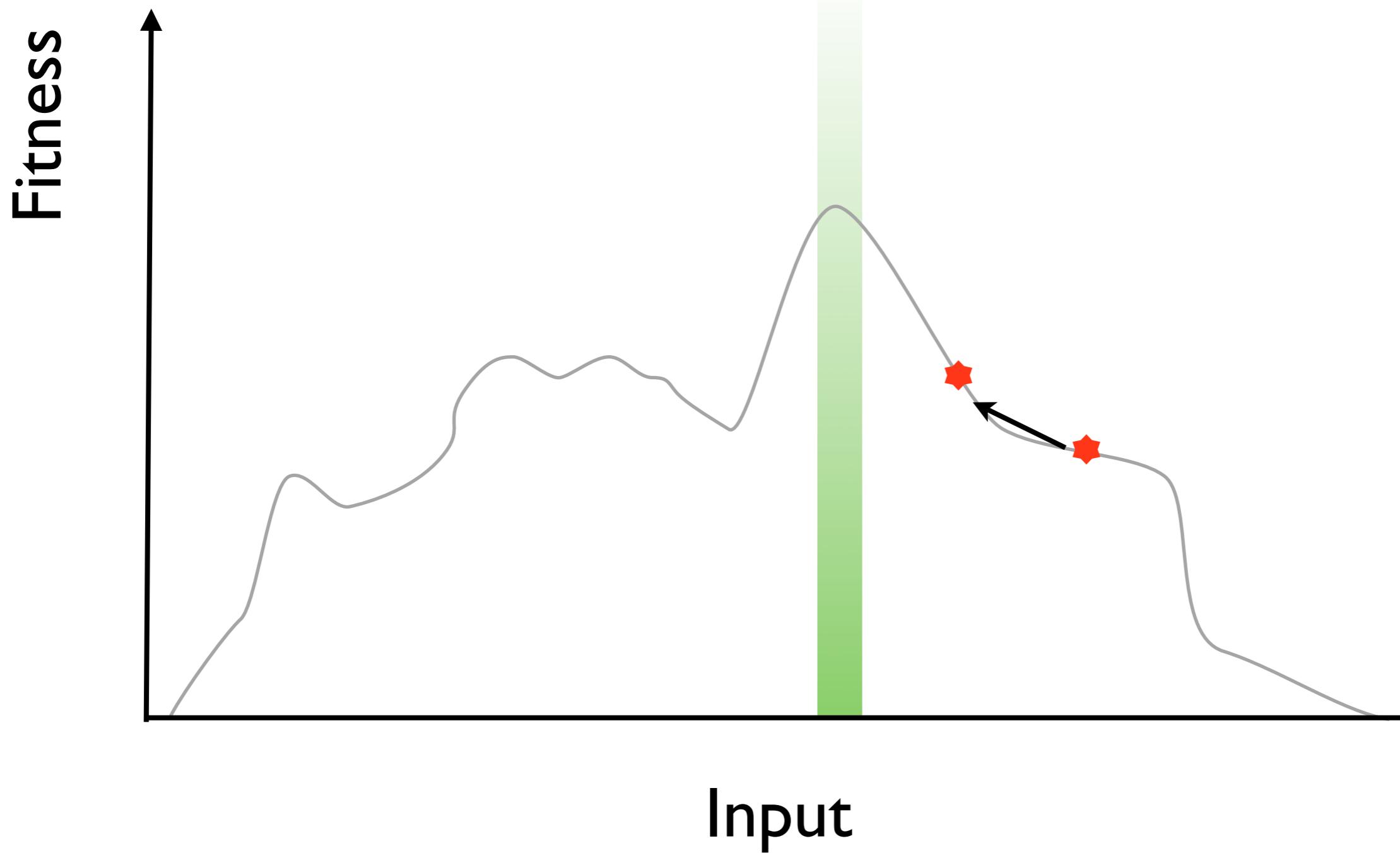
Hill Climbing - Restarts



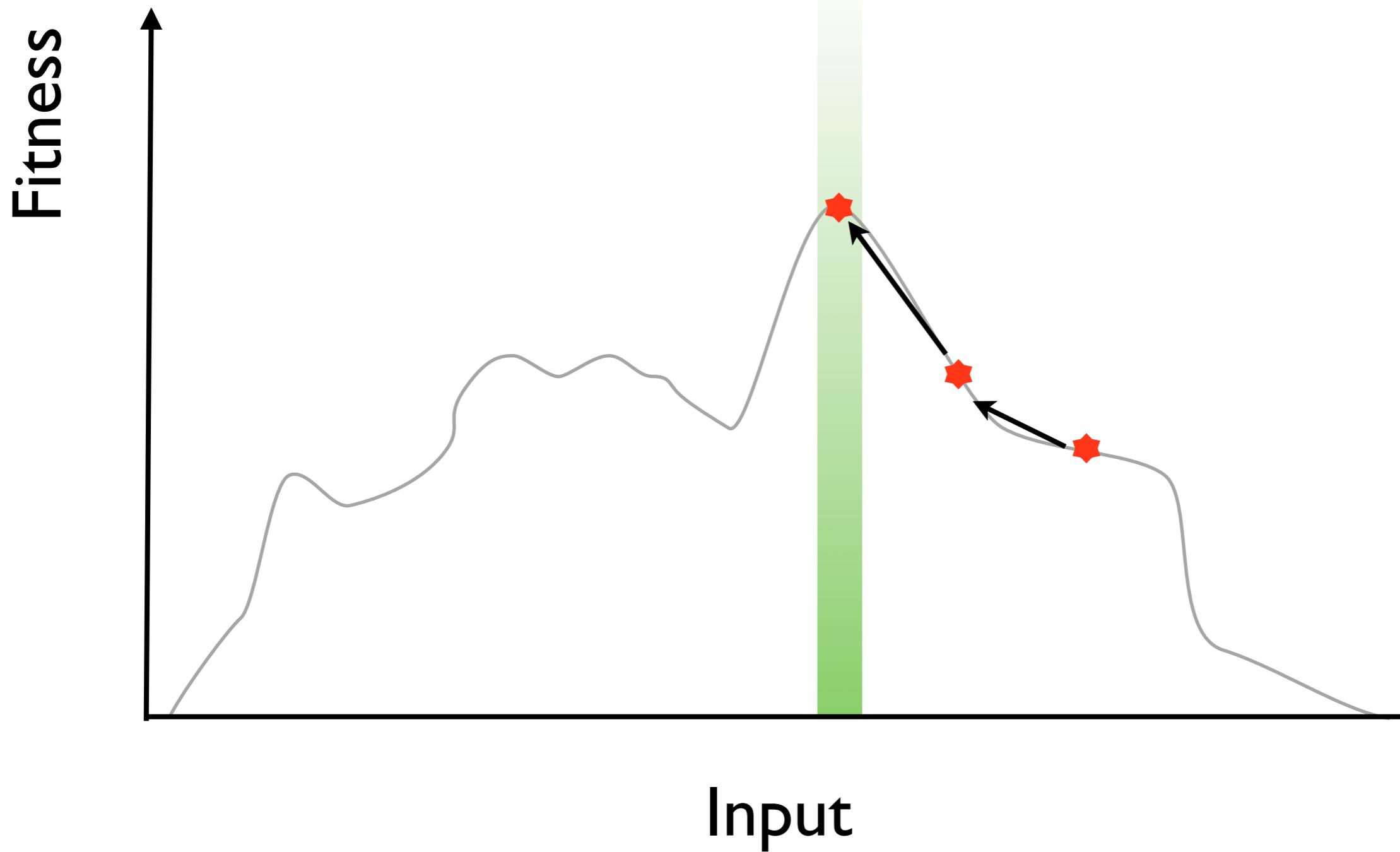
Hill Climbing - Restarts



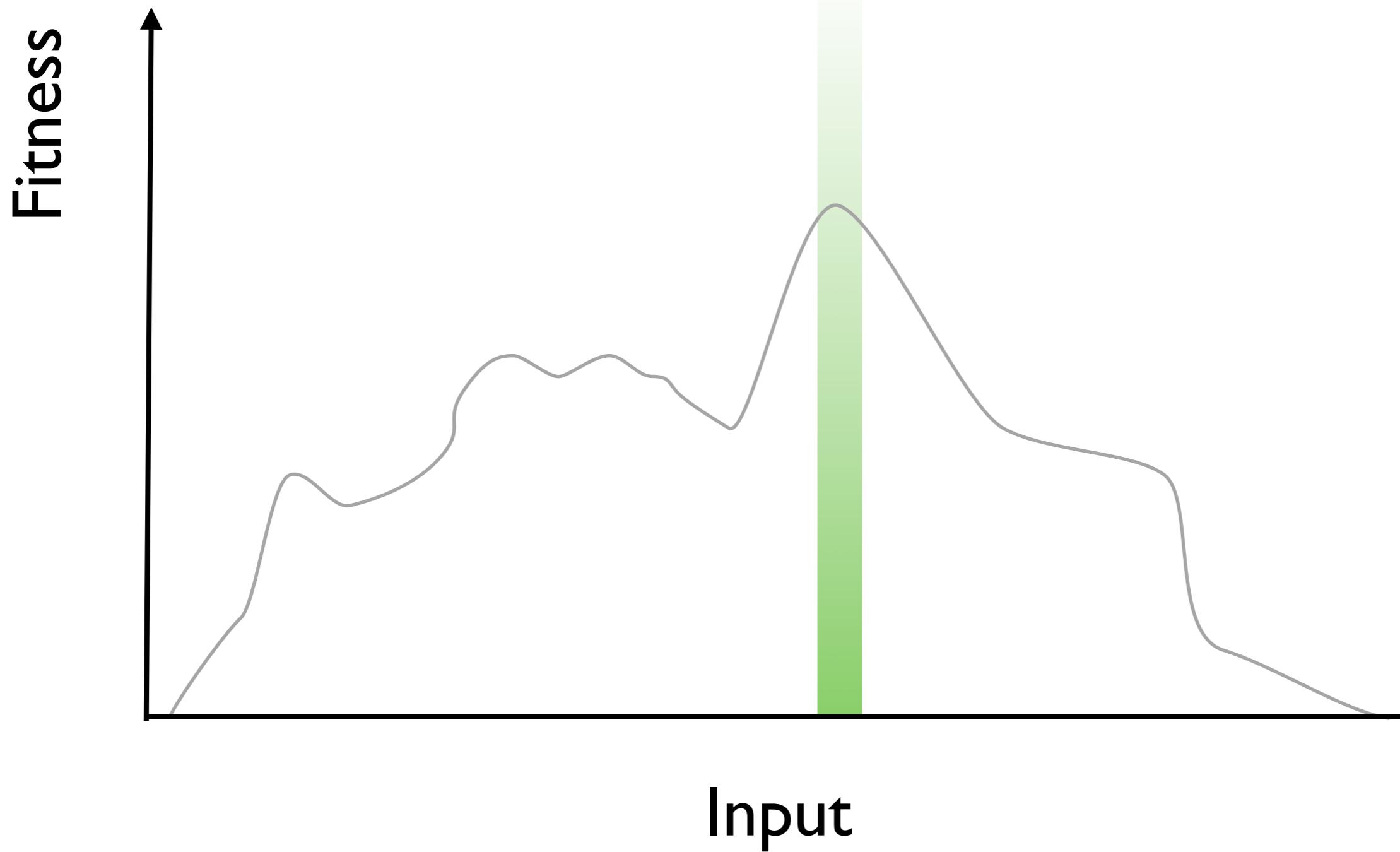
Hill Climbing - Restarts



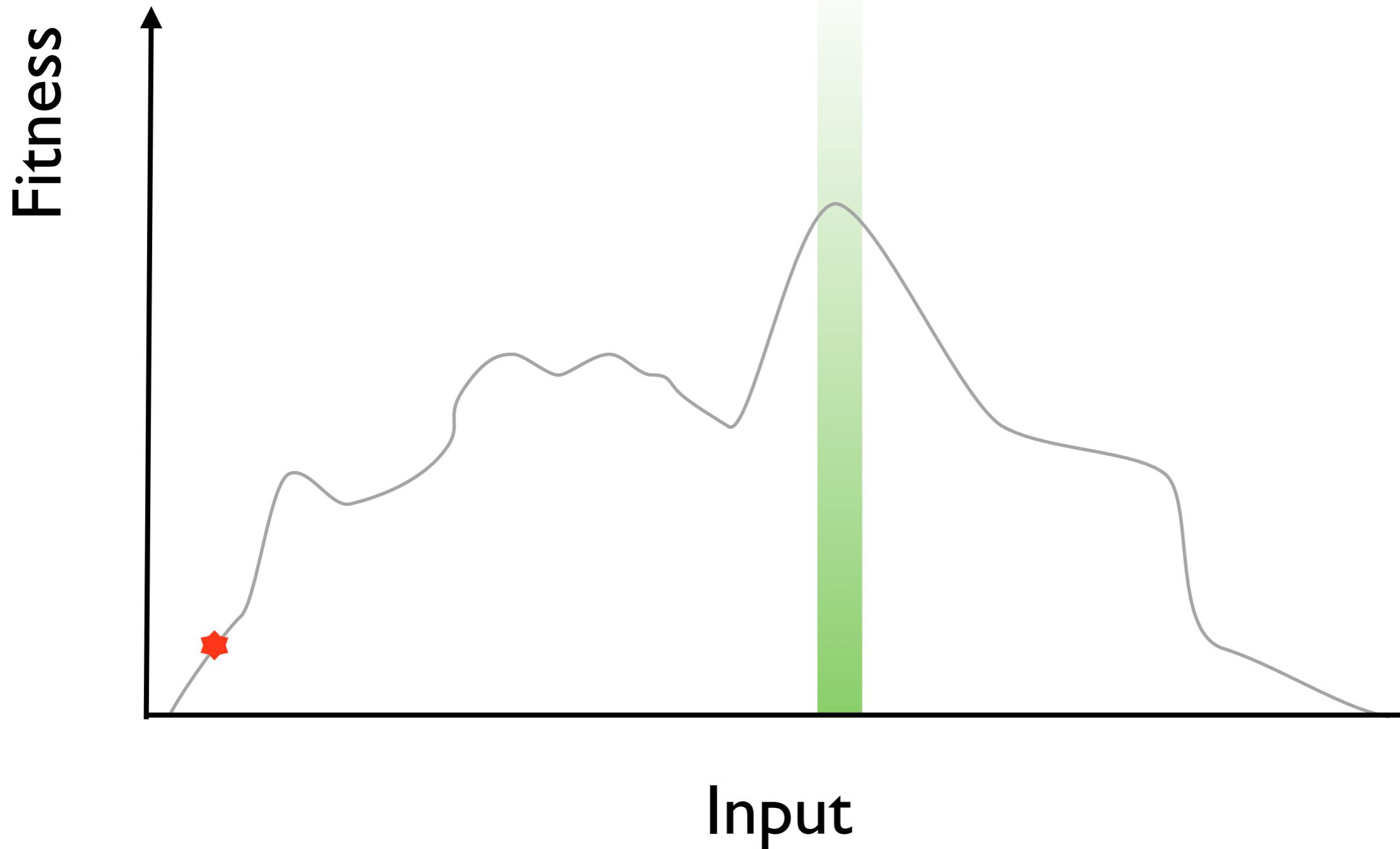
Hill Climbing - Restarts



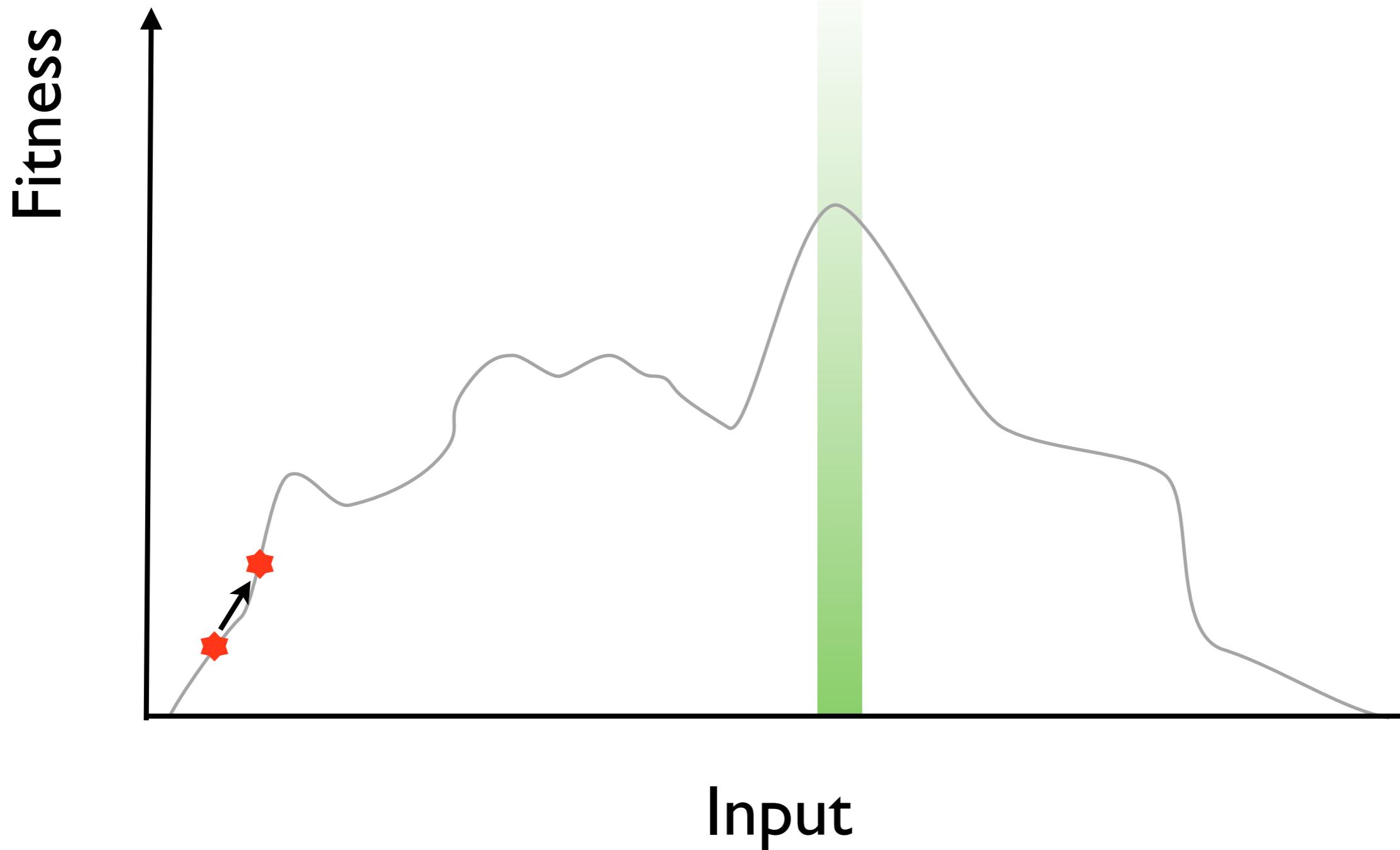
Simulated Annealing



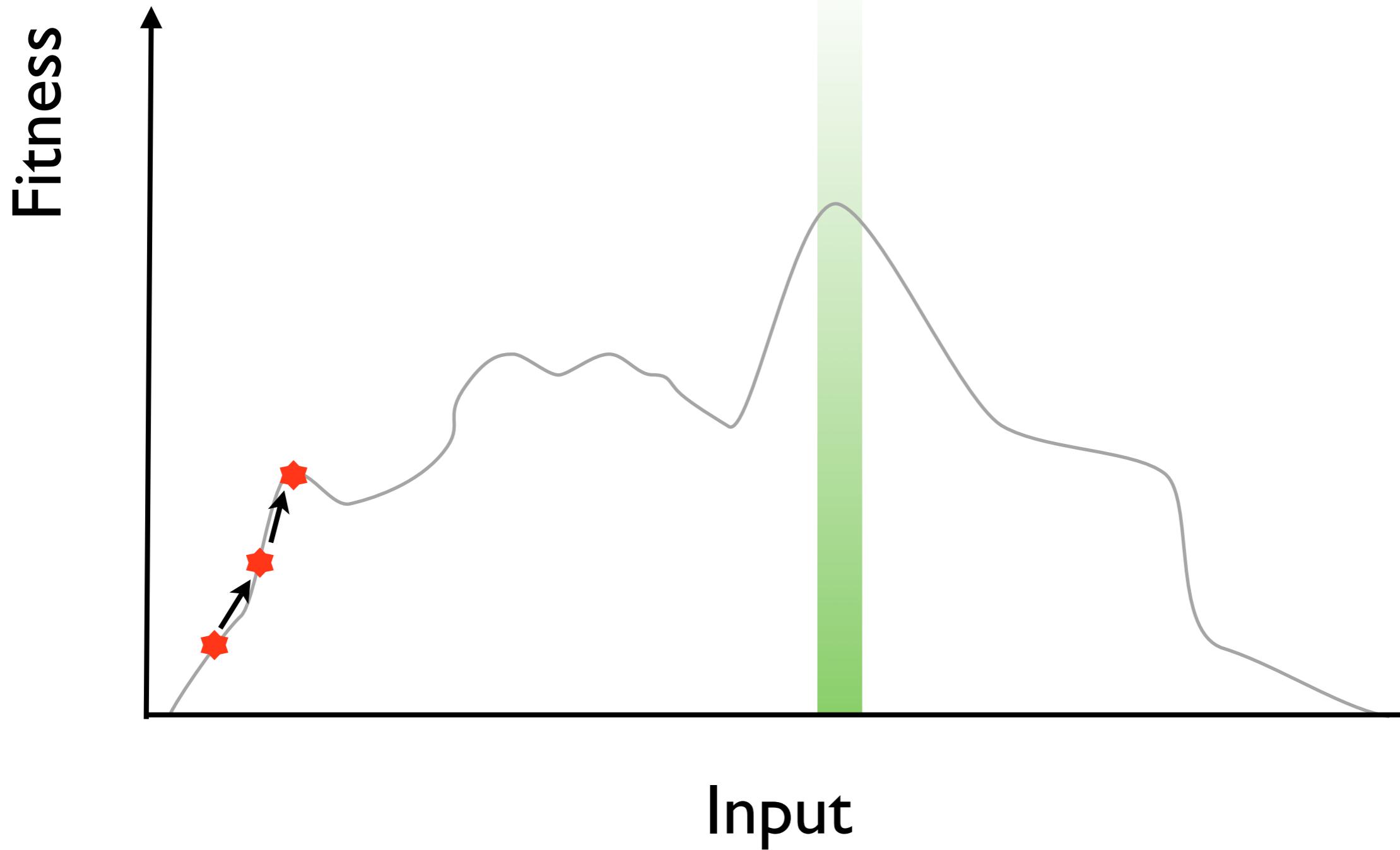
Simulated Annealing



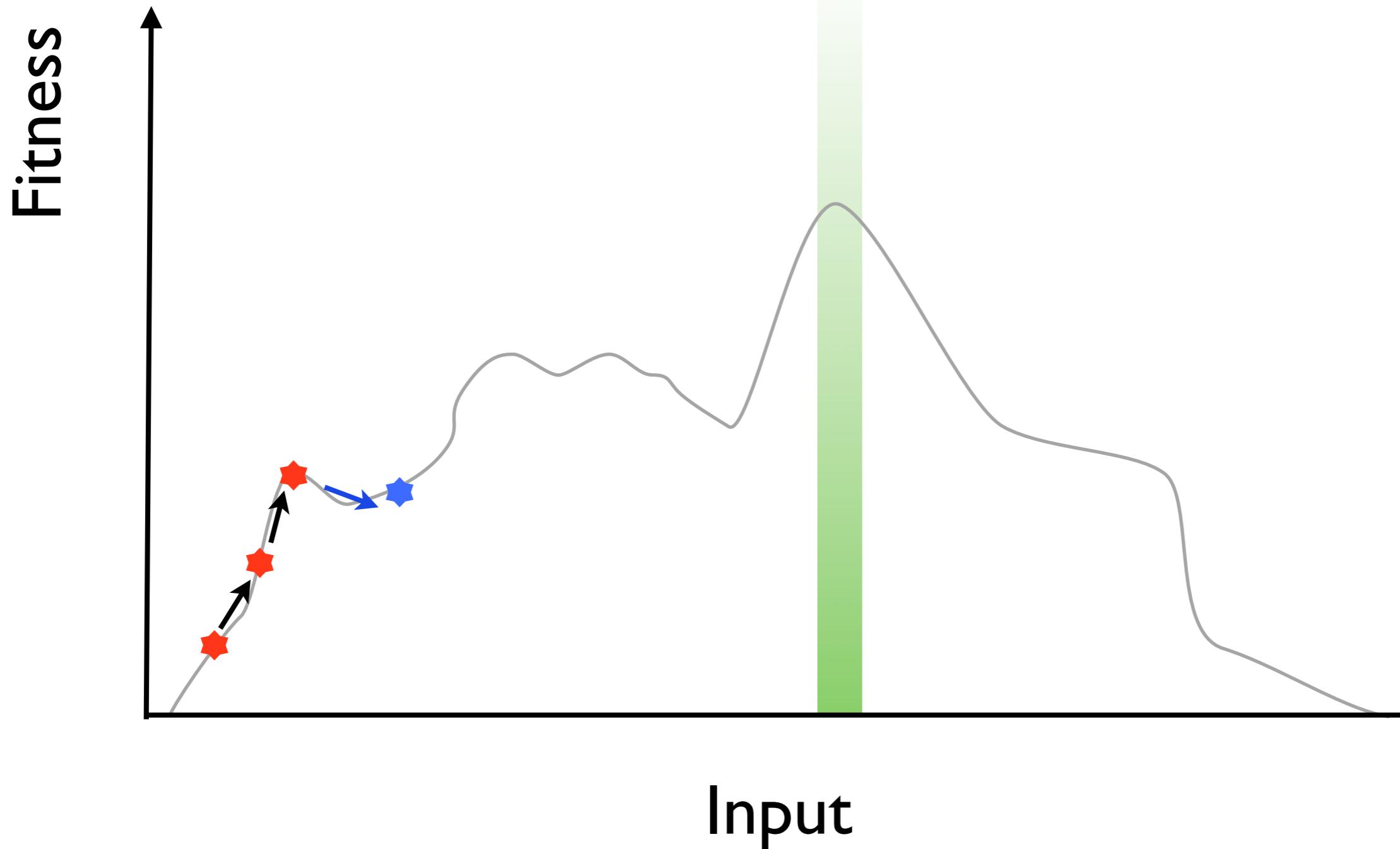
Simulated Annealing



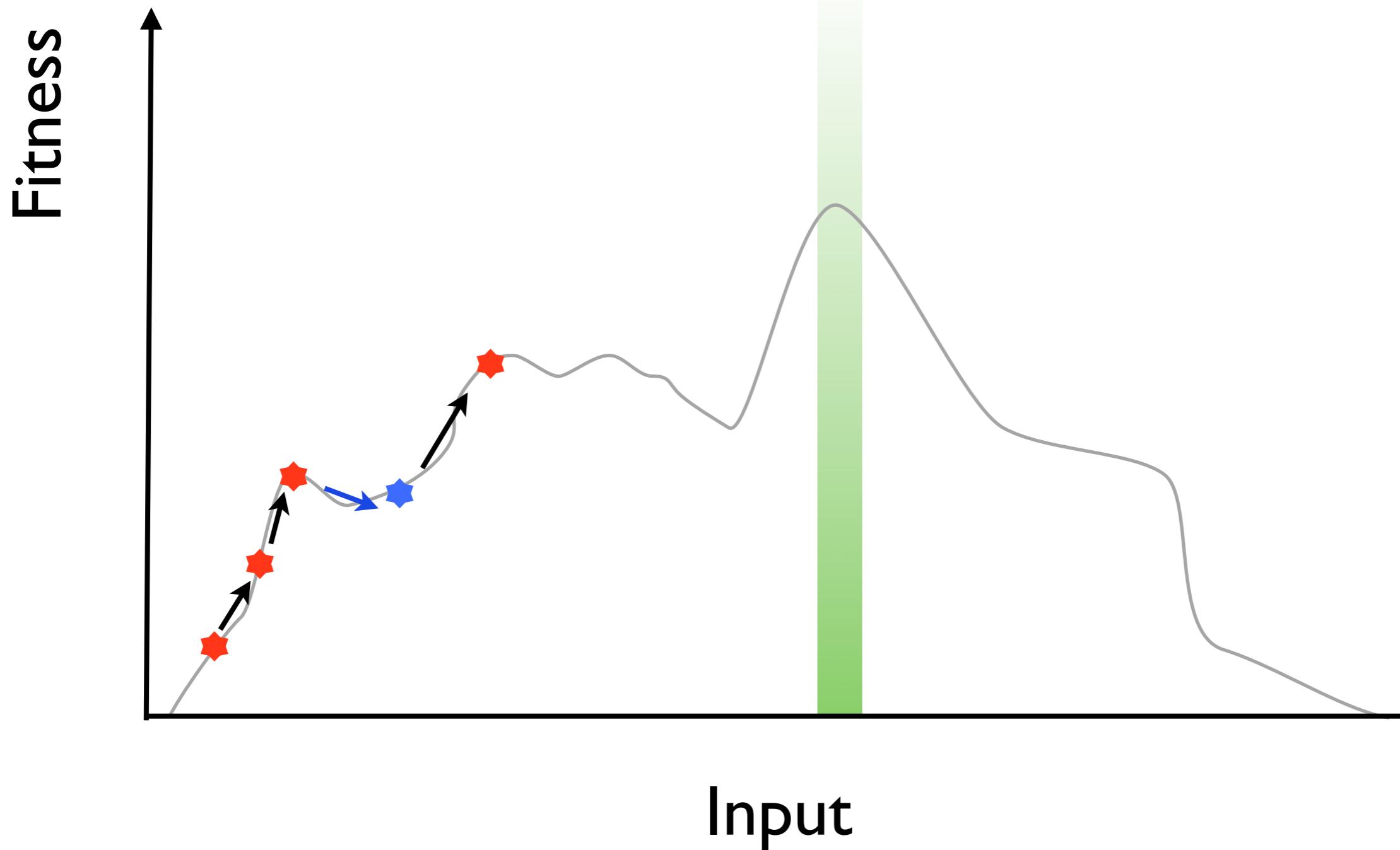
Simulated Annealing



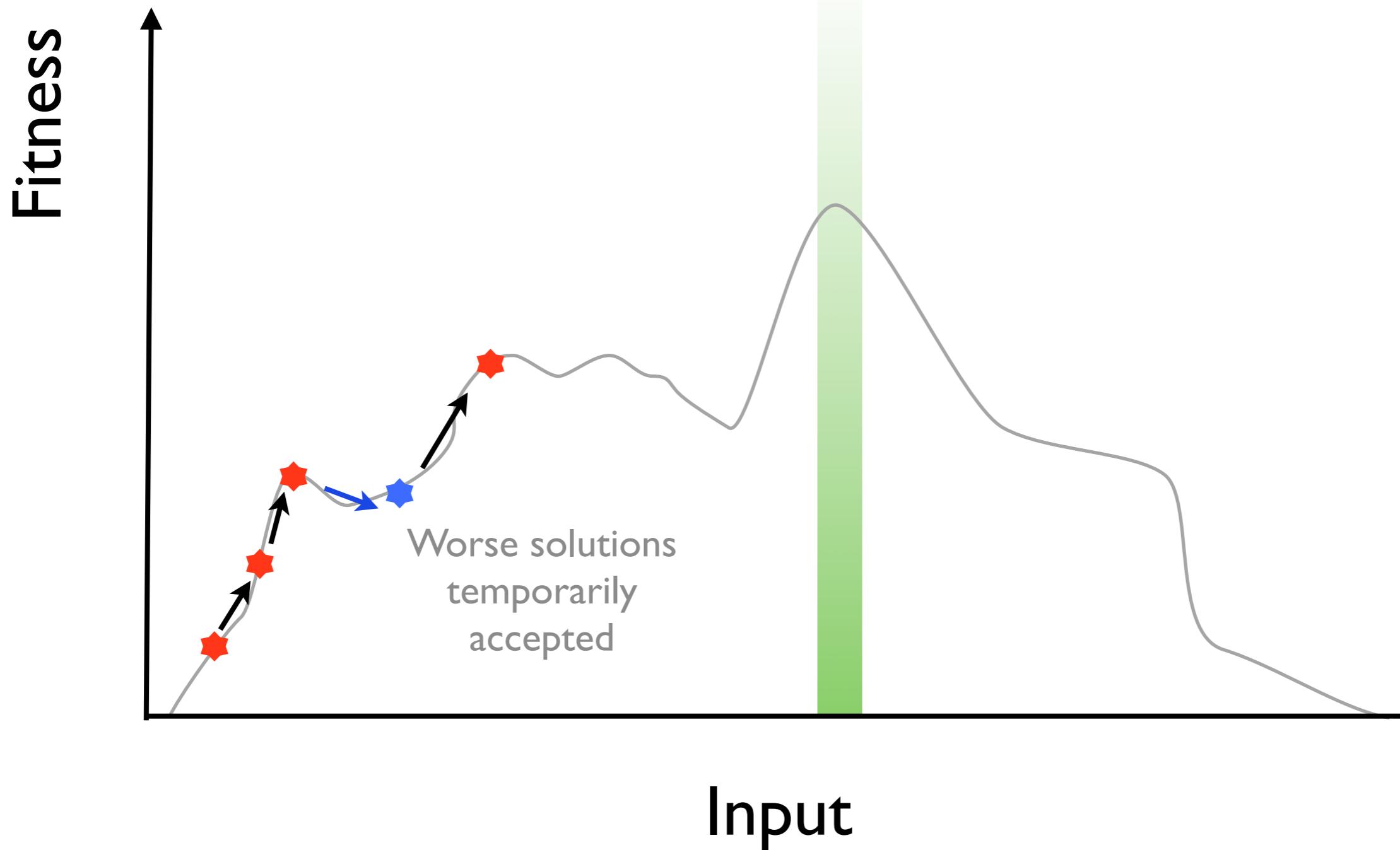
Simulated Annealing



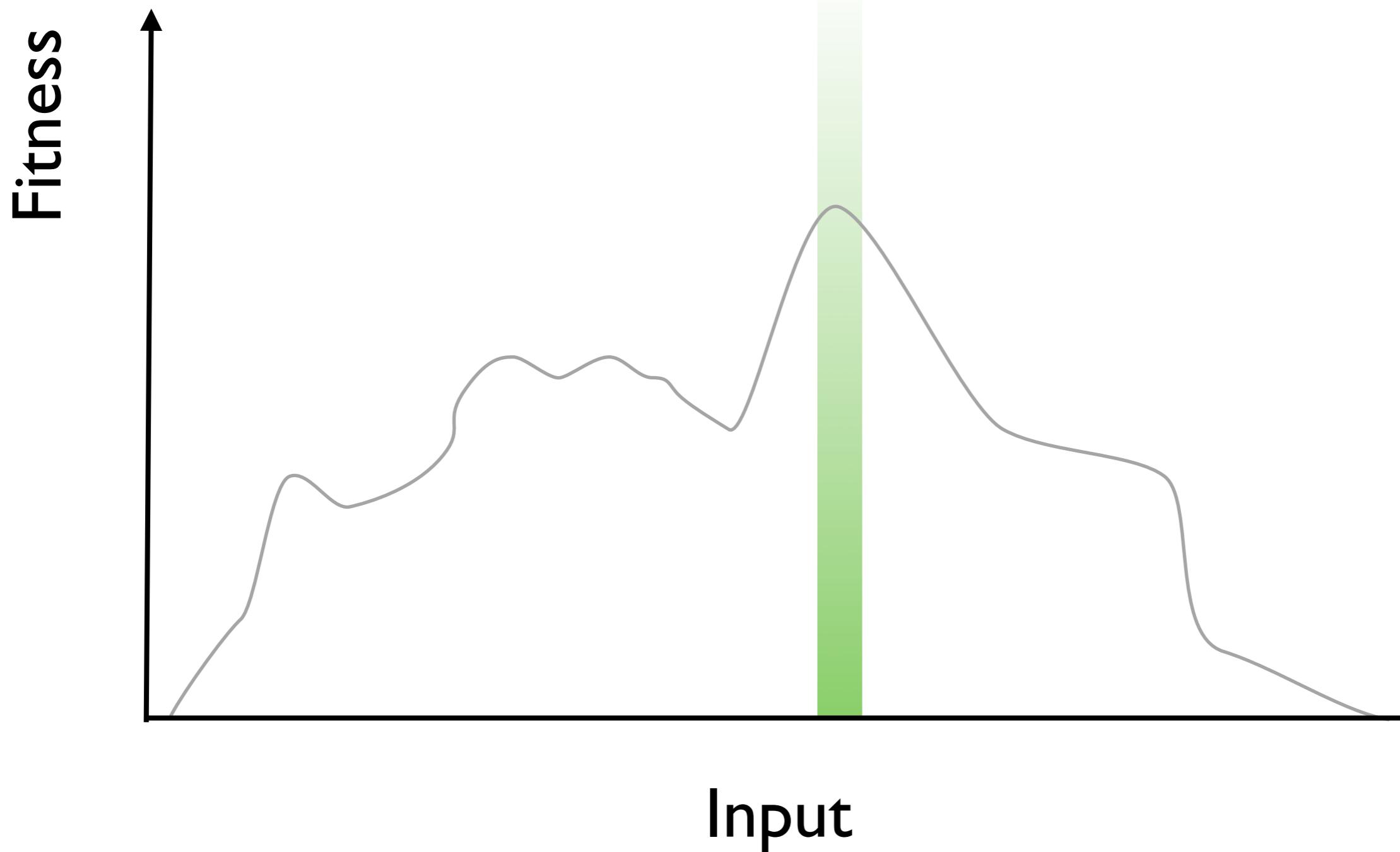
Simulated Annealing



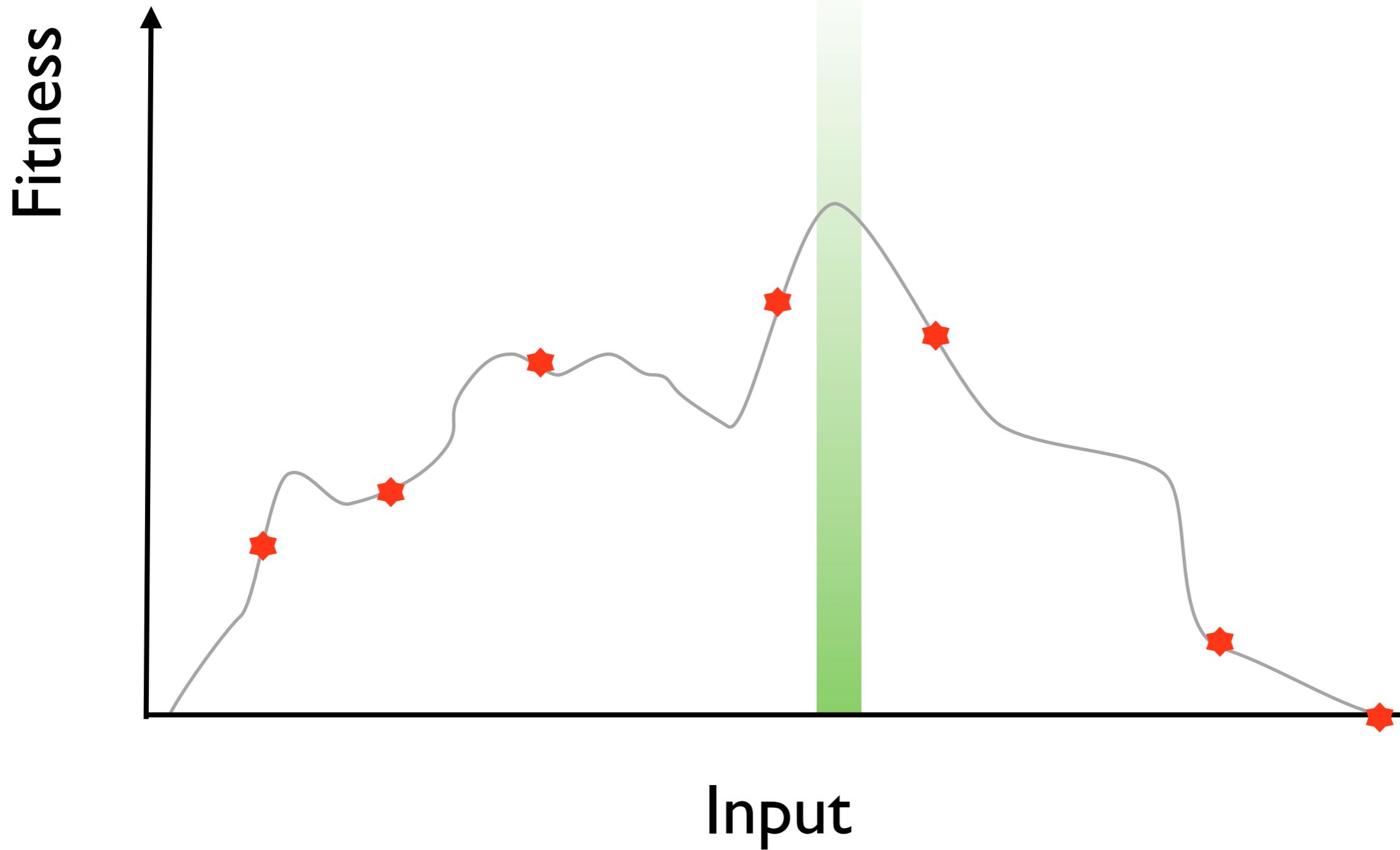
Simulated Annealing



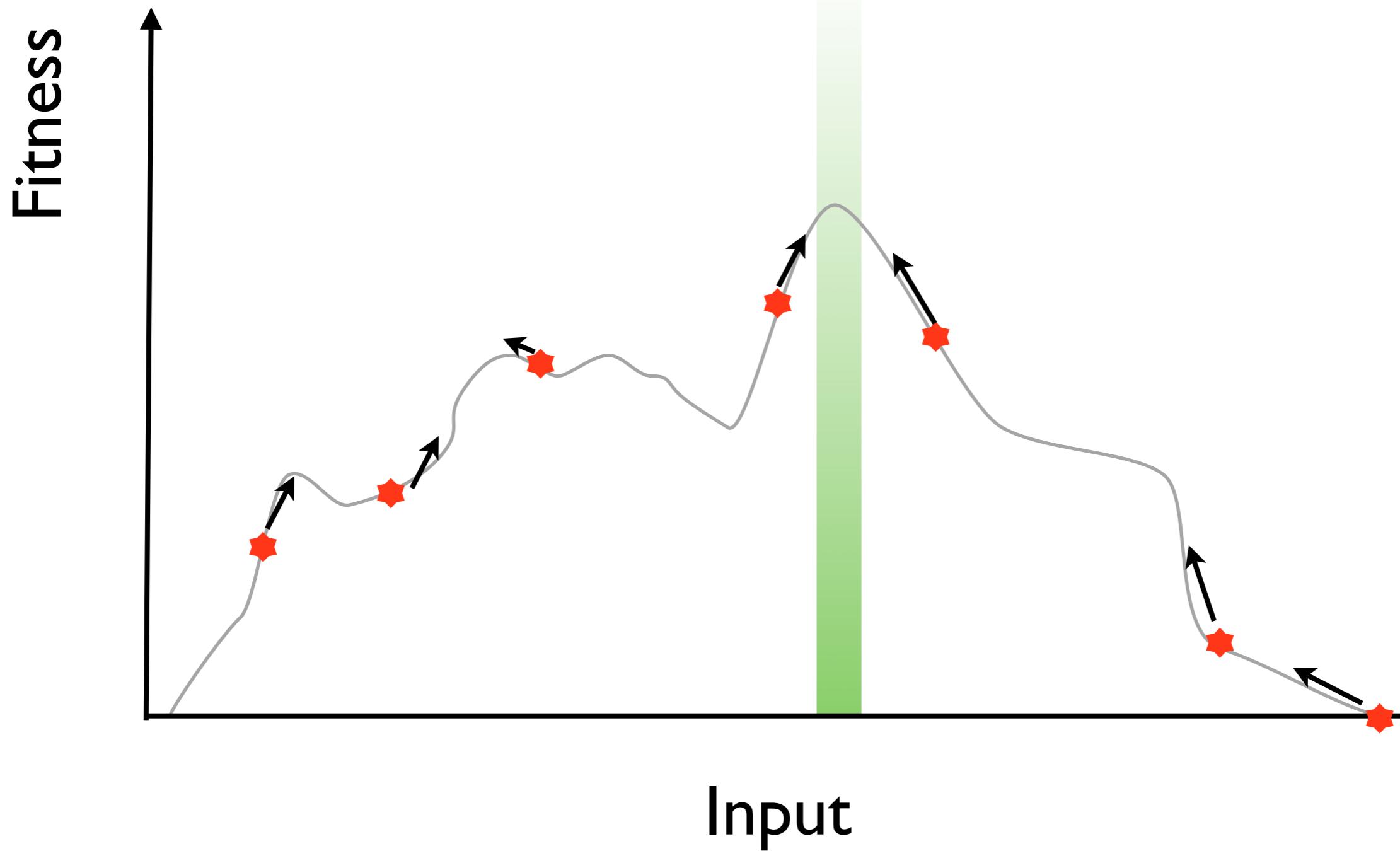
Evolutionary Algorithm



Evolutionary Algorithm



Evolutionary Algorithm



Evolutionary Algorithms

inspired by Darwinian Evolution and concept of
survival of the fittest

Crossover

Mutation

Crossover

```
void test_me(int a, int b, int c, int d) {  
    if (a == b) {  
        if (c == d) {  
            // branch we want to execute  
        }  
    }  
    ...  
}
```

a	b	c	d
10	10	20	40

a	b	c	d
20	-5	80	80

Crossover

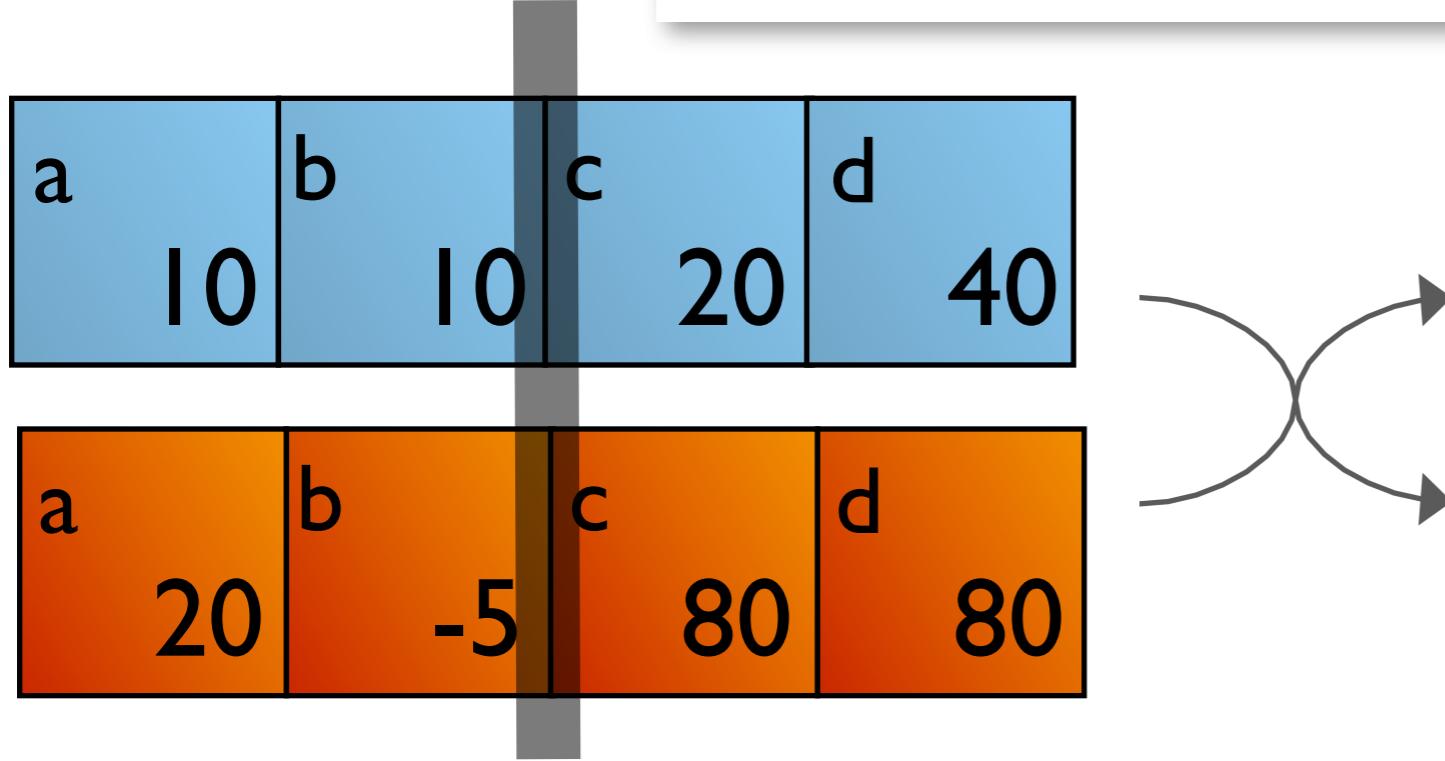
```
void test_me(int a, int b, int c, int d) {  
    if (a == b) {  
        if (c == d) {  
            // branch we want to execute  
        }  
    }  
    ...  
}
```

a	b	c	d
10	10	20	40

a	b	c	d
20	-5	80	80

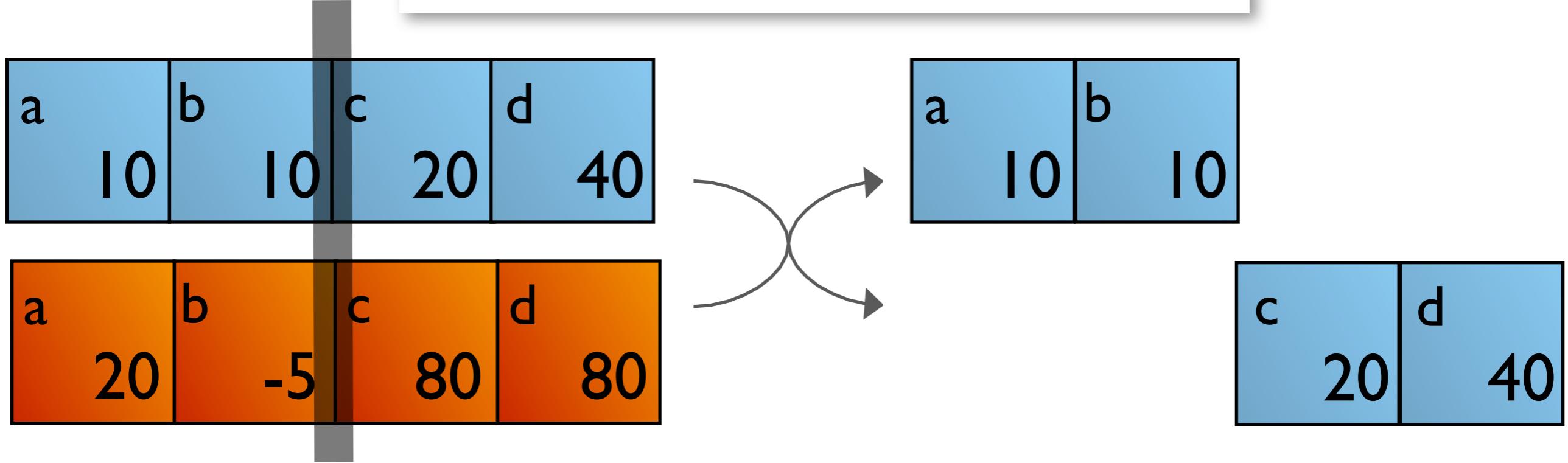
Crossover

```
void test_me(int a, int b, int c, int d) {  
    if (a == b) {  
        if (c == d) {  
            // branch we want to execute  
        }  
    }  
    ...  
}
```



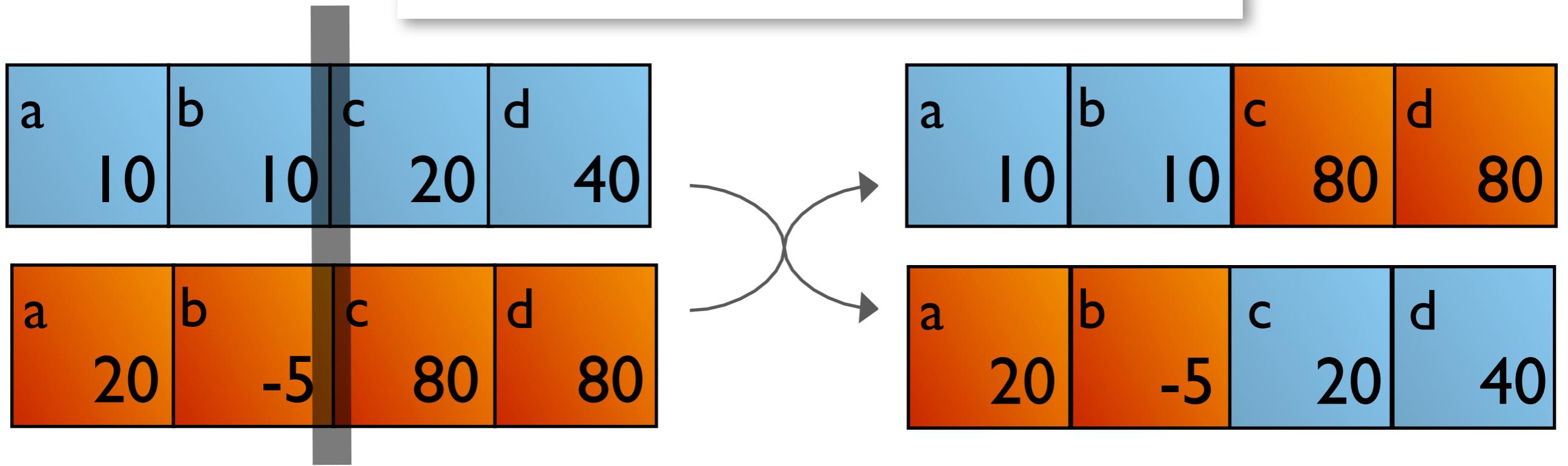
Crossover

```
void test_me(int a, int b, int c, int d) {  
    if (a == b) {  
        if (c == d) {  
            // branch we want to execute  
        }  
    }  
    ...  
}
```



Crossover

```
void test_me(int a, int b, int c, int d) {  
    if (a == b) {  
        if (c == d) {  
            // branch we want to execute  
        }  
    }  
    ...  
}
```



Mutation

```
void test_me(int a, int b, int c, int d) {  
    if (a == b) {  
        if (c == d) {  
            // branch we want to execute  
        }  
    }  
    ...  
}
```

a	b	c	d
10	10	20	40

Mutation

```
void test_me(int a, int b, int c, int d) {  
    if (a == b) {  
        if (c == d) {  
            // branch we want to execute  
        }  
    }  
    ...  
}
```

a	b	c	d
10	10	20	20

Mutation

```
void test_me(int a, int b, int c, int d) {  
    if (a == b) {  
        if (c == d) {  
            // branch we want to execute  
        }  
    }  
    ...  
}
```

a	b	c	d
10	10	20	40

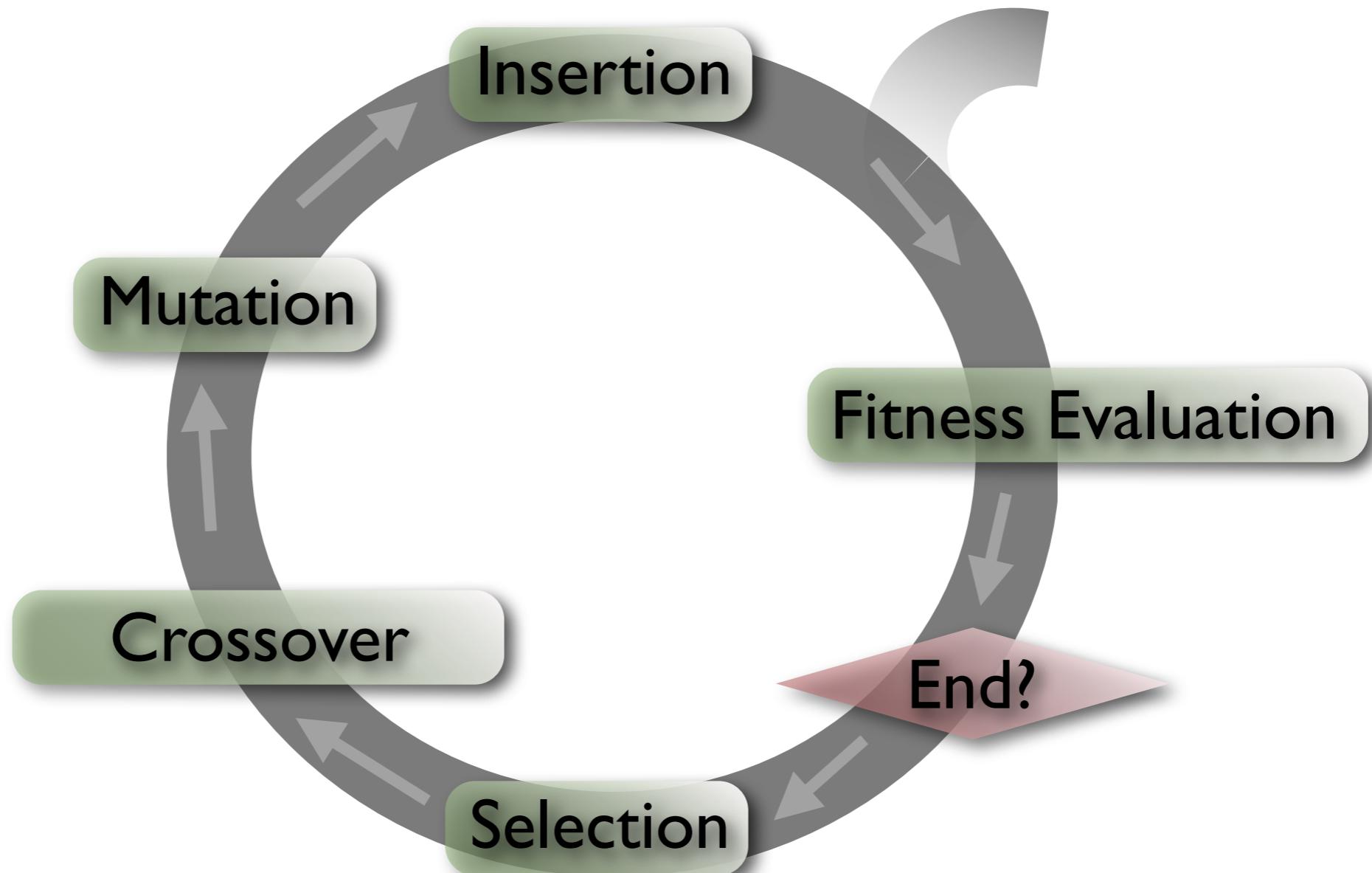
Mutation

```
void test_me(int a, int b, int c, int d) {  
    if (a == b) {  
        if (c == d) {  
            // branch we want to execute  
        }  
    }  
    ...  
}
```

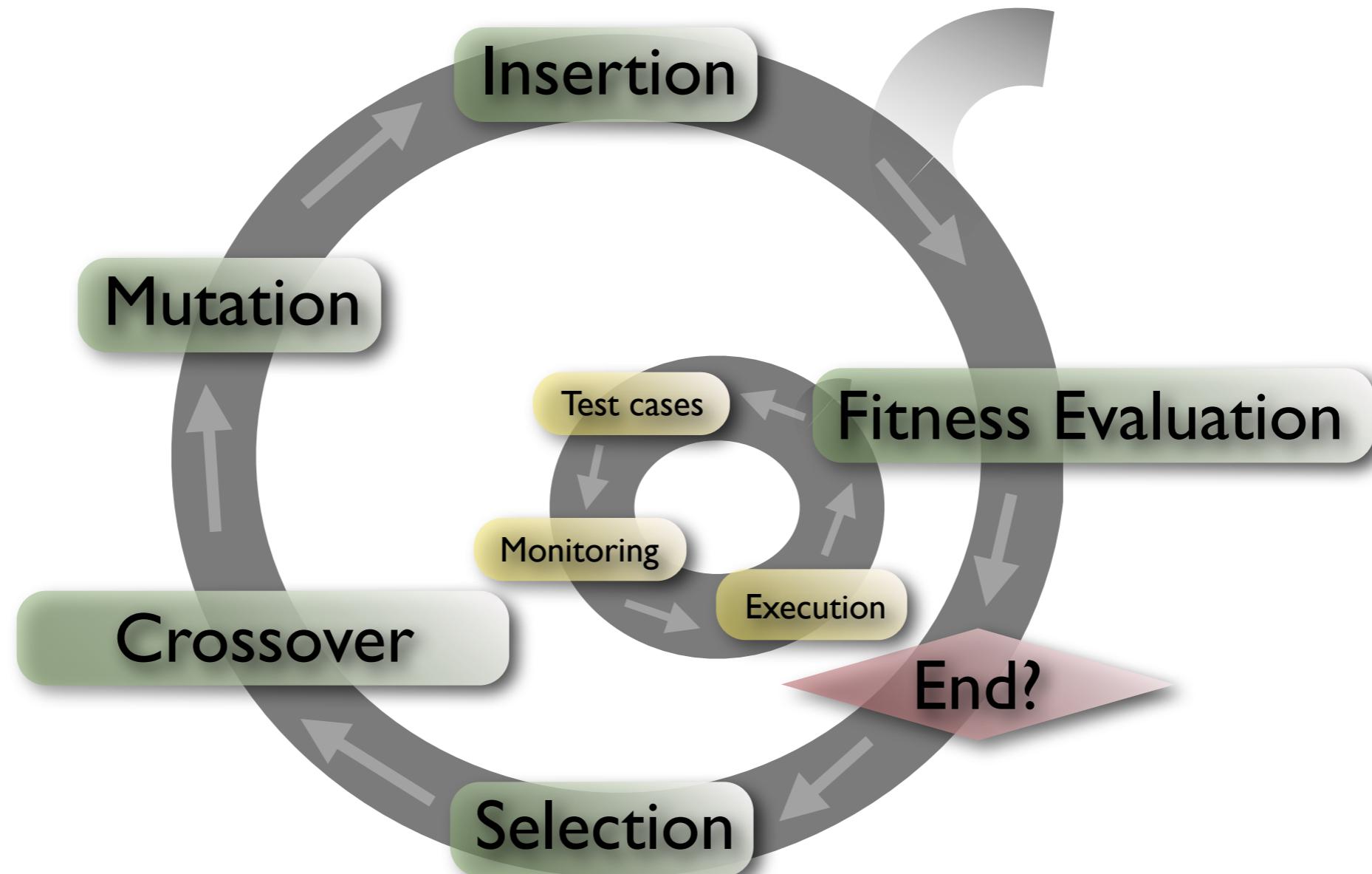
a 20	b 10	c 20	d 40
---------	---------	---------	---------

Evolutionary Testing

Evolutionary Testing



Evolutionary Testing

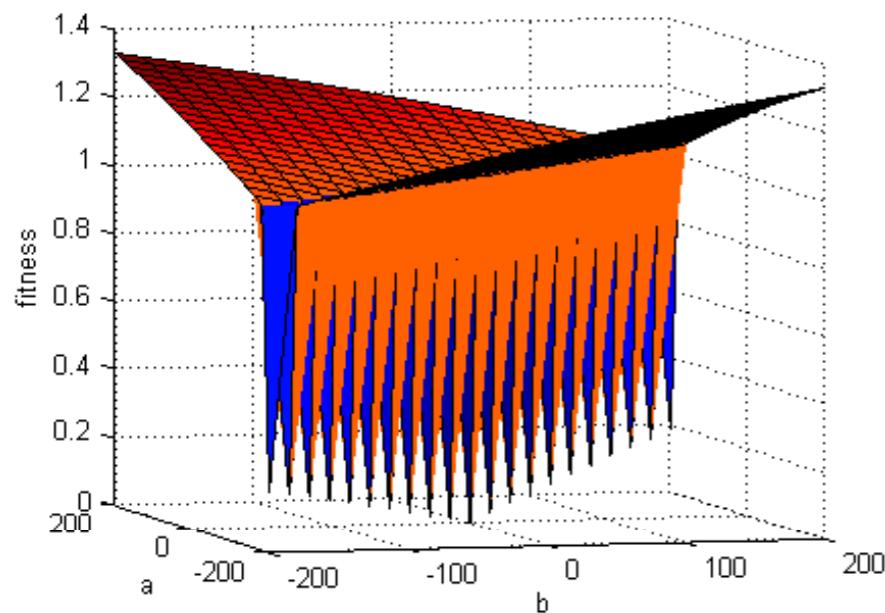


Which search method?

Depends on characteristics of the **search landscape**

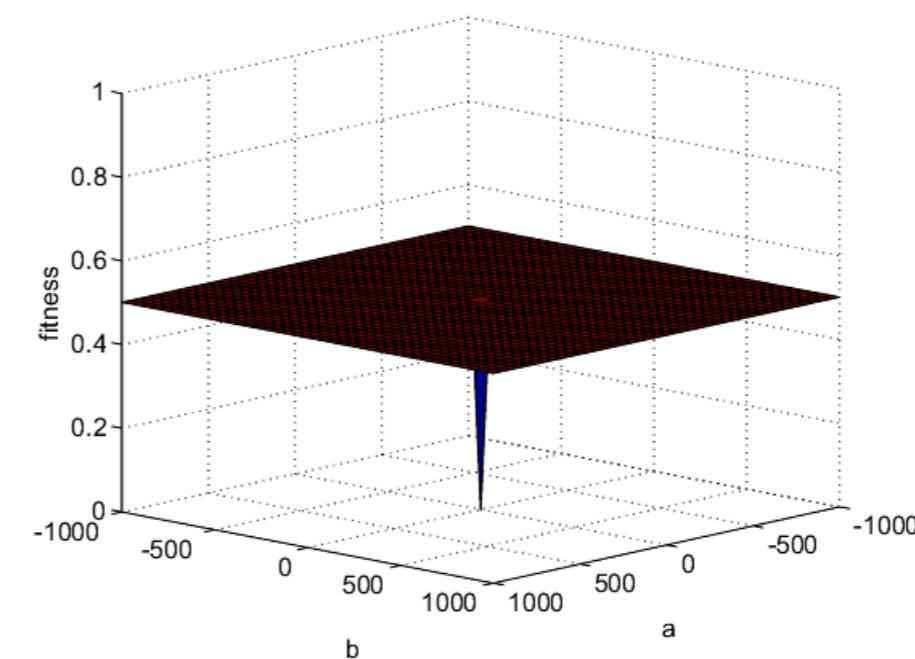
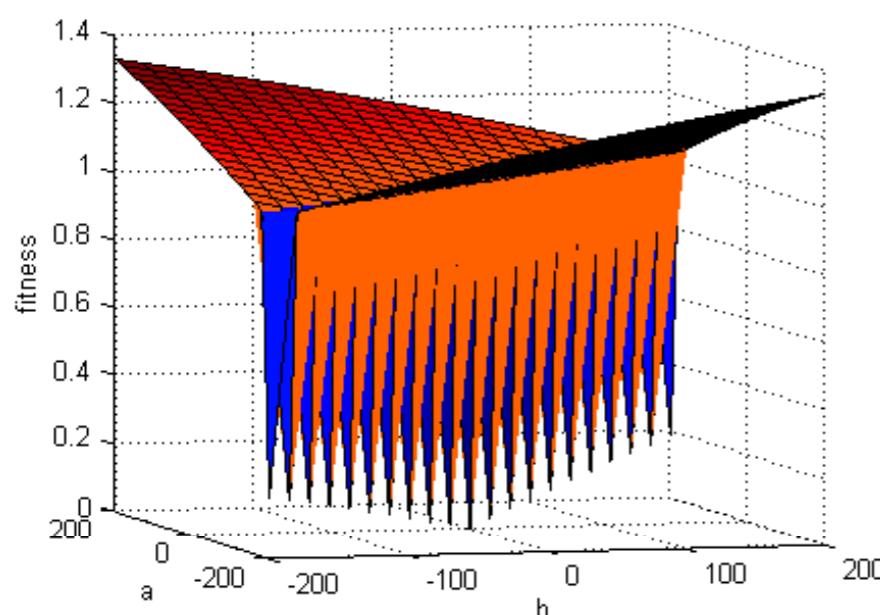
Which search method?

Depends on characteristics of the search landscape



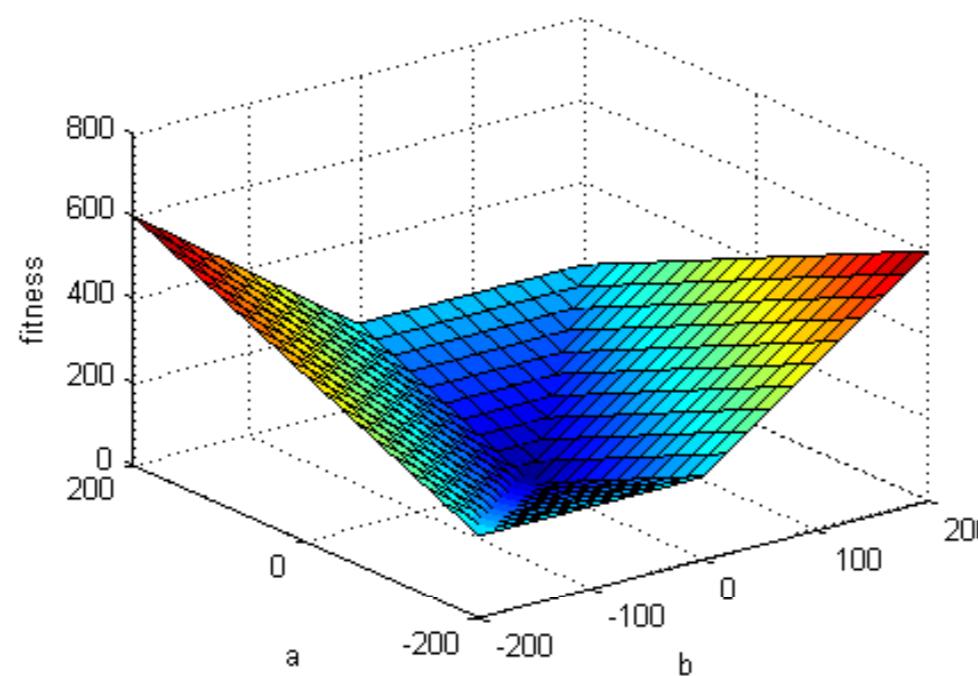
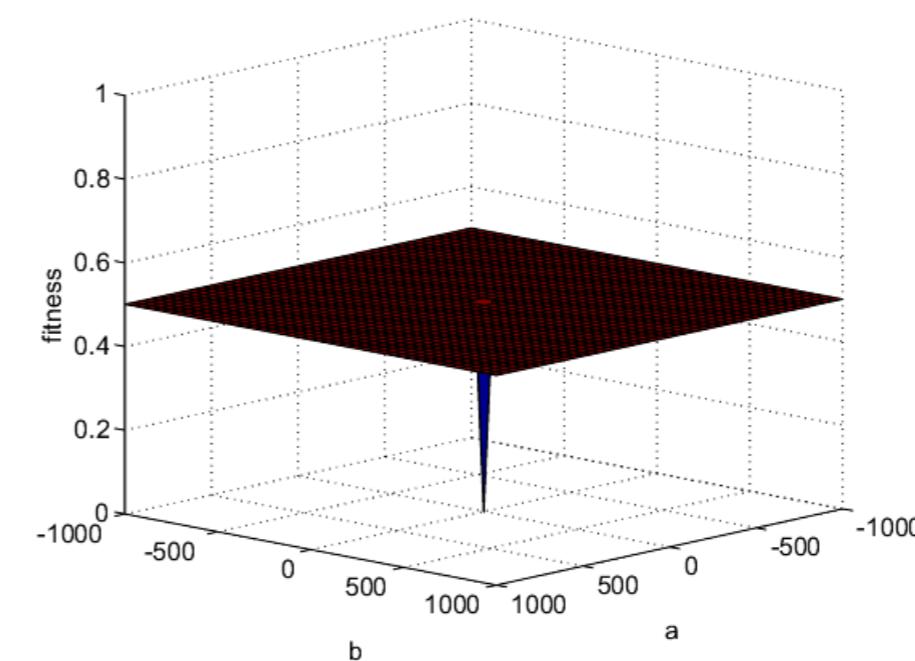
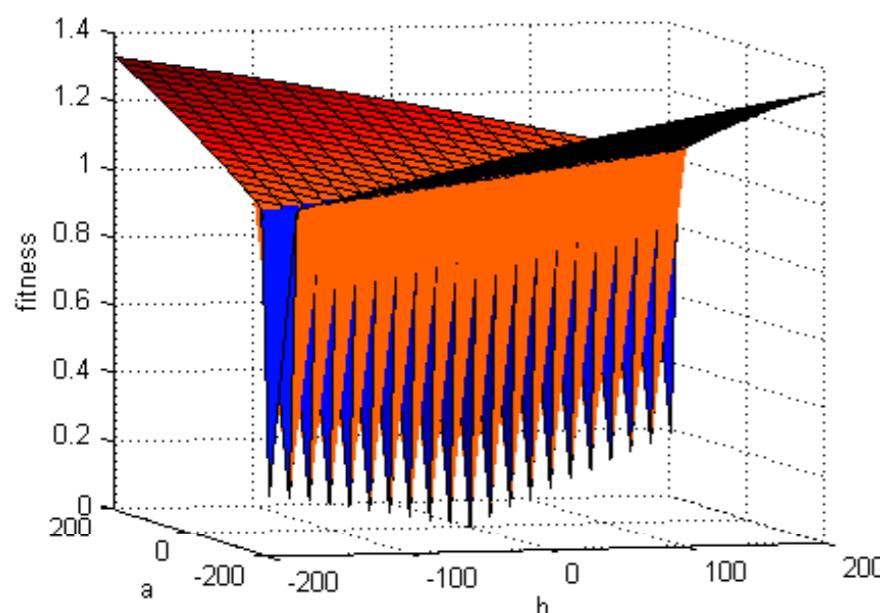
Which search method?

Depends on characteristics of the search landscape



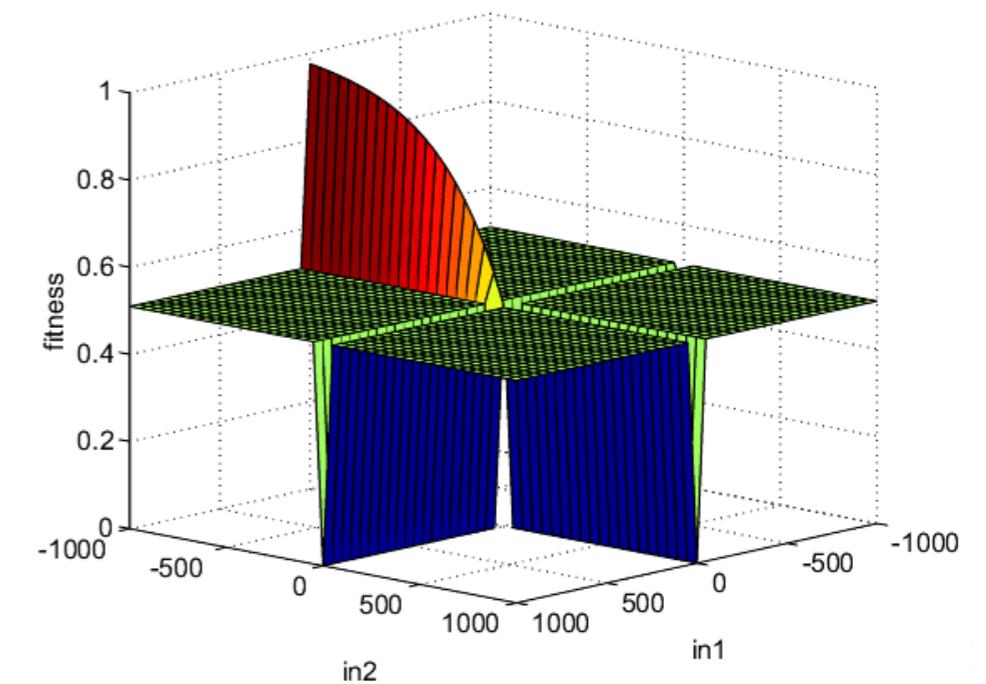
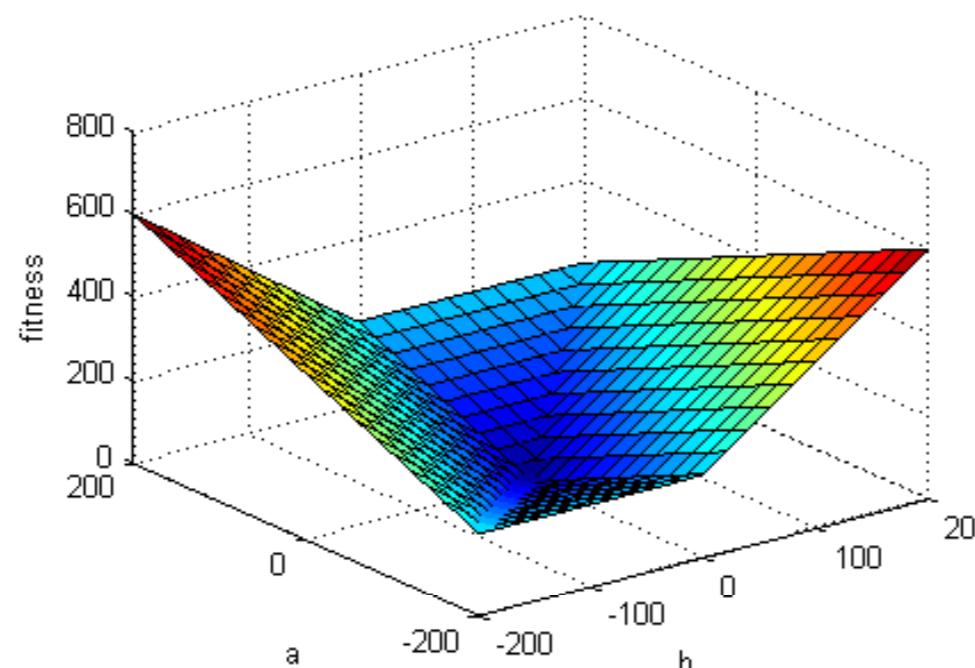
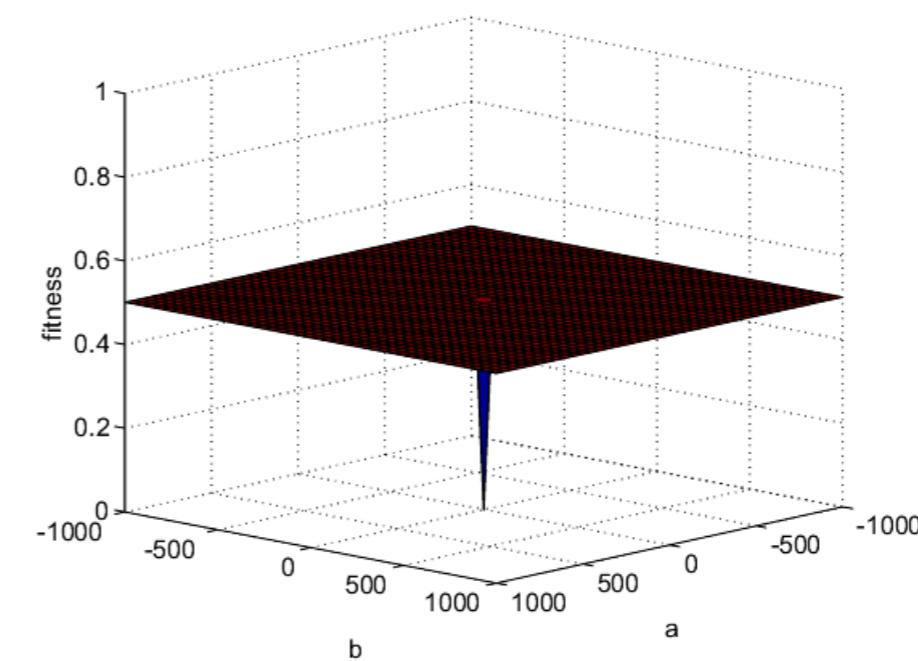
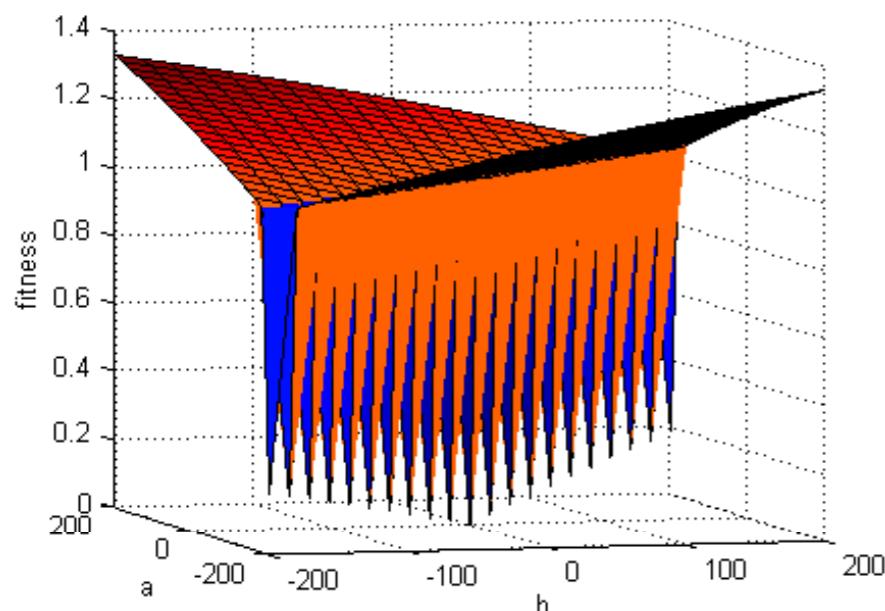
Which search method?

Depends on characteristics of the search landscape



Which search method?

Depends on characteristics of the search landscape



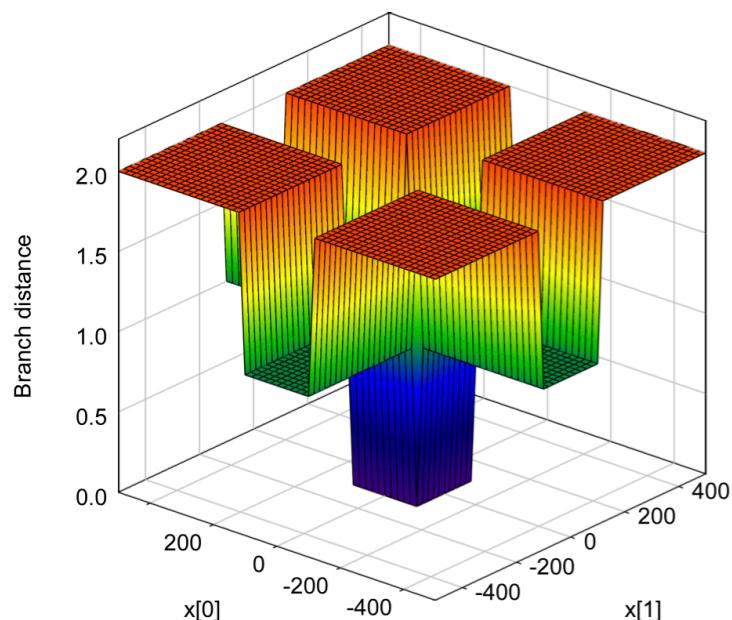
Which search method?

Some landscapes are
hard for some
searches but easy for
others

...and vice
versa...

Which search method?

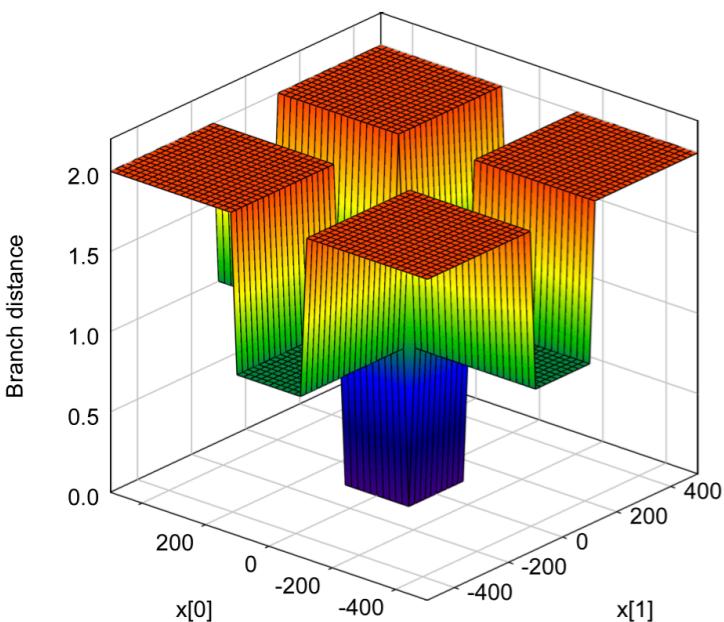
Some landscapes are
hard for some
searches but easy for
others



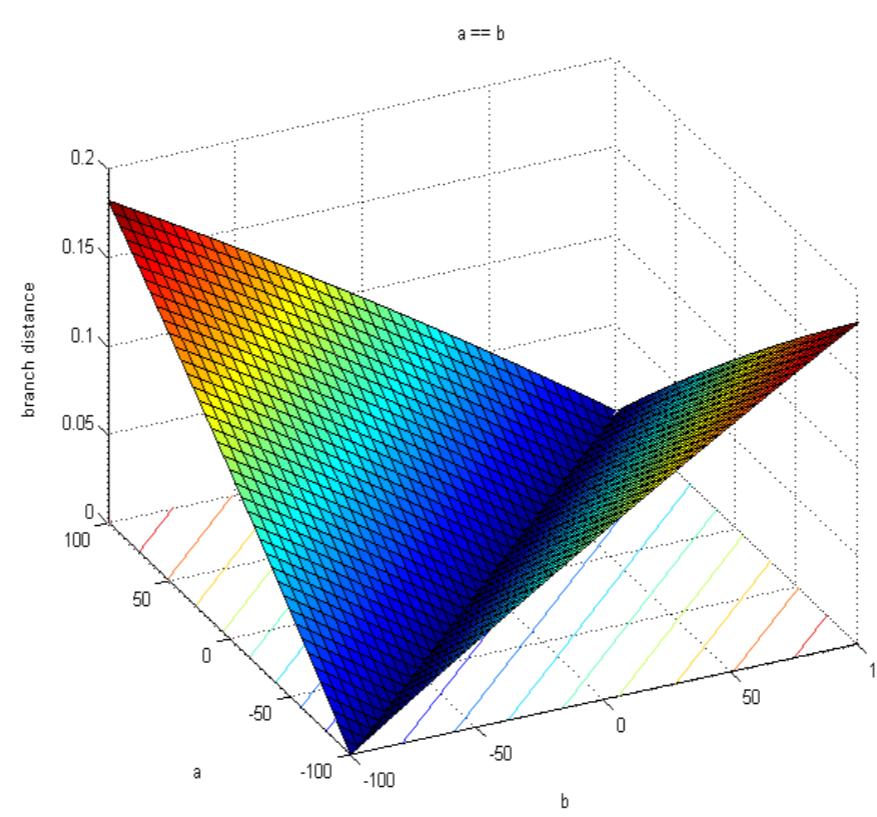
...and vice
versa...

Which search method?

Some landscapes are
hard for some
searches but easy for
others

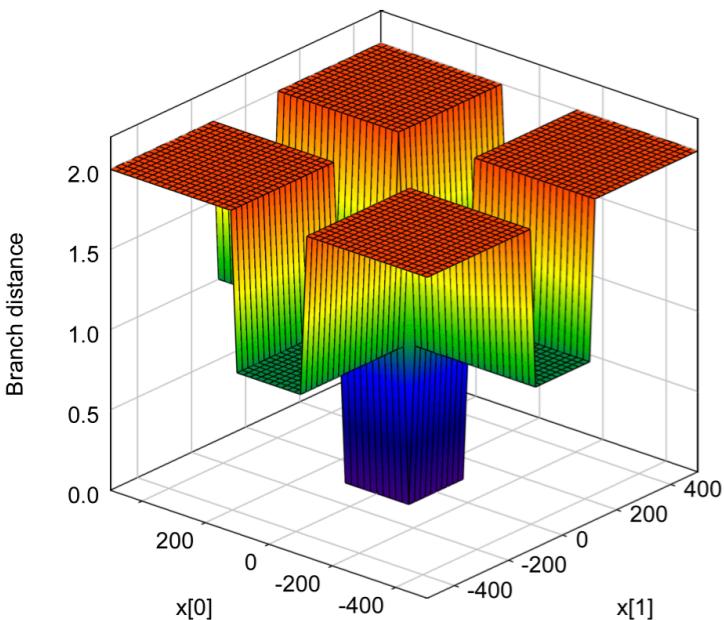


...and vice
versa...

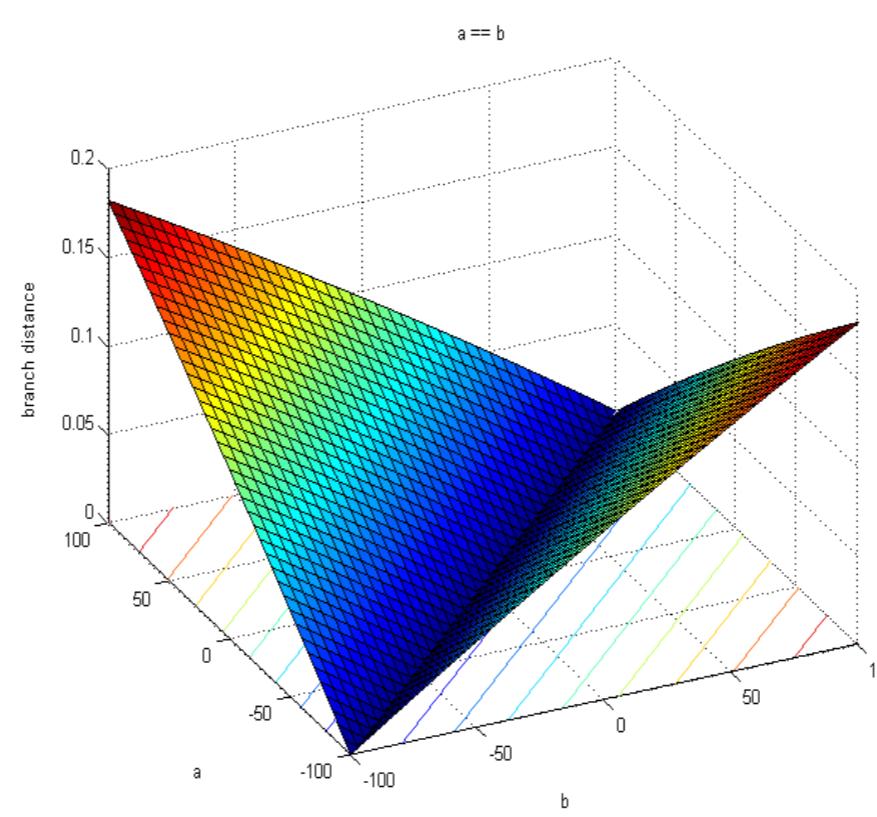


Which search method?

Some landscapes are
hard for some
searches but easy for
others



...and vice
versa...



more on
this later...

Ingredients for an optimising search algorithm

Representation

Neighbourhood

Fitness Function

Ingredients for Search-Based Testing

Representation

Neighbourhood

Fitness Function

Ingredients for Search-Based Testing

Representation	A method of encoding all possible inputs
Neighbourhood	Usually straightforward
Fitness Function	Inputs are already in data structures

Ingredients for Search-Based Testing

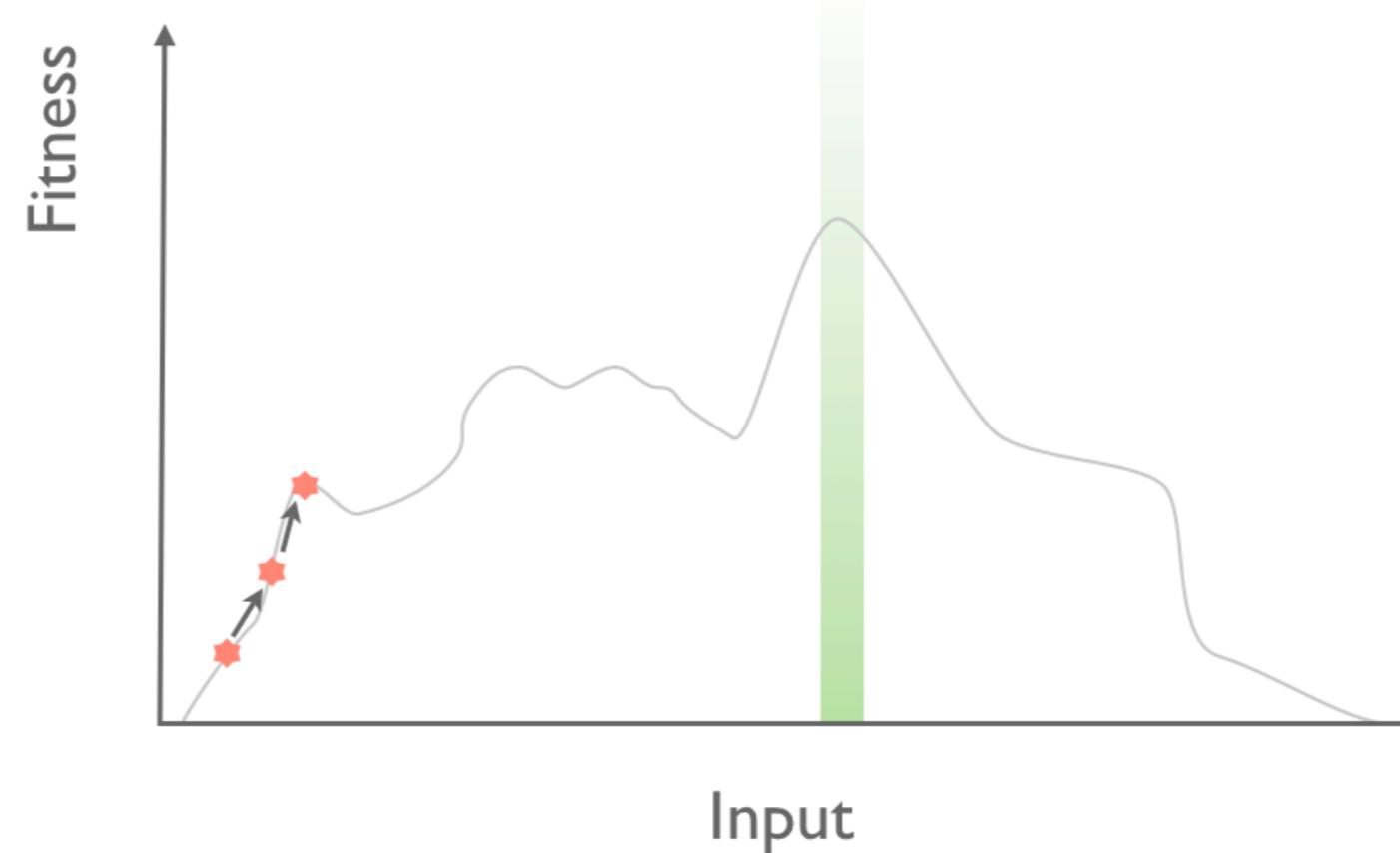
Representation

Part of our understanding of the problem

Neighbourhood

We need to know our near neighbours

Fitness Function



Ingredients for Search-Based Testing

Representation	Transformation of the test goal to a numerical function
Neighbourhood	
Fitness Function	Numerical values indicate how ‘good’ an input is

More search algorithms

More search algorithms

Tabu Search

Particle Swarm Optimisation

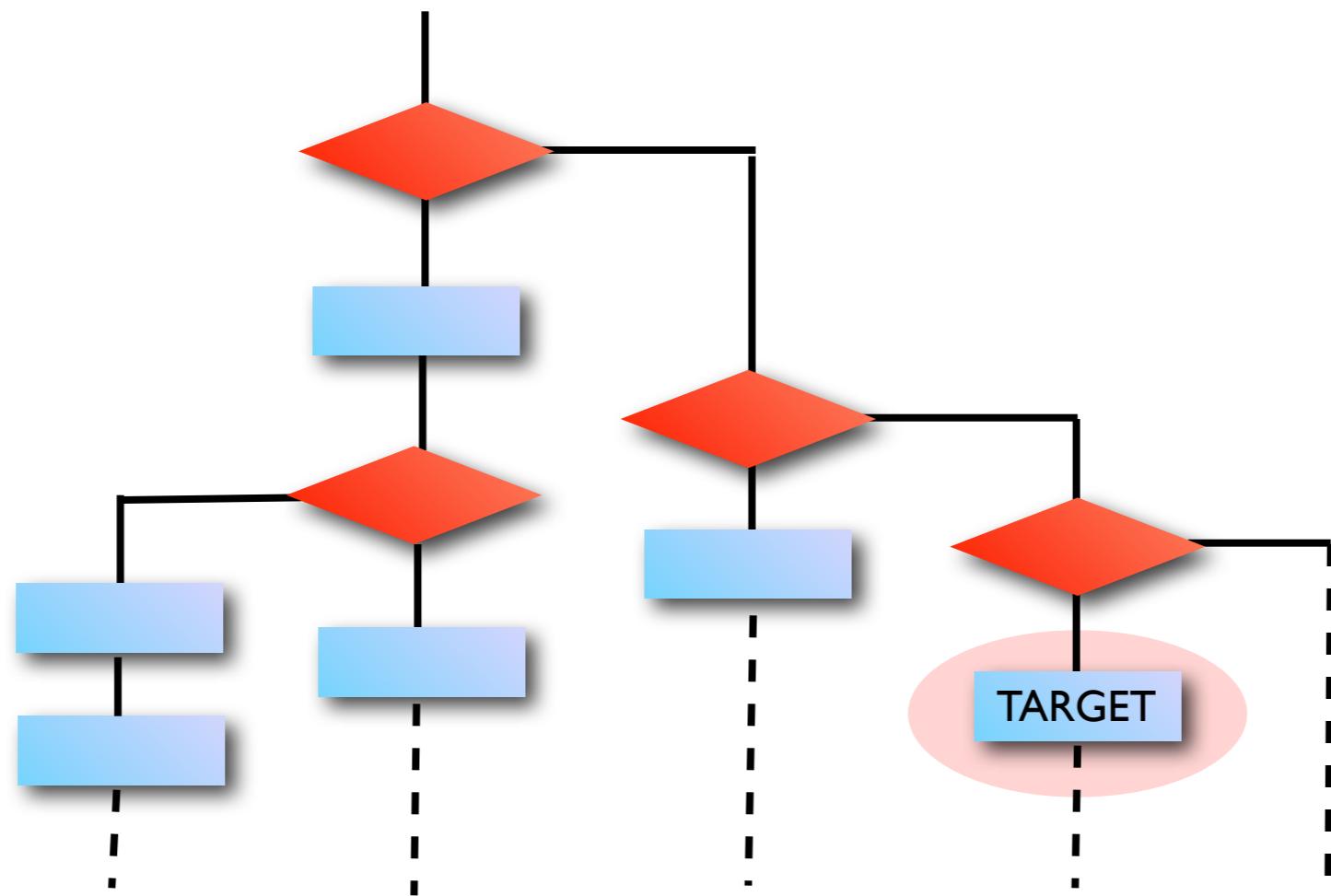
Ant Colony Optimisation

Genetic Programming

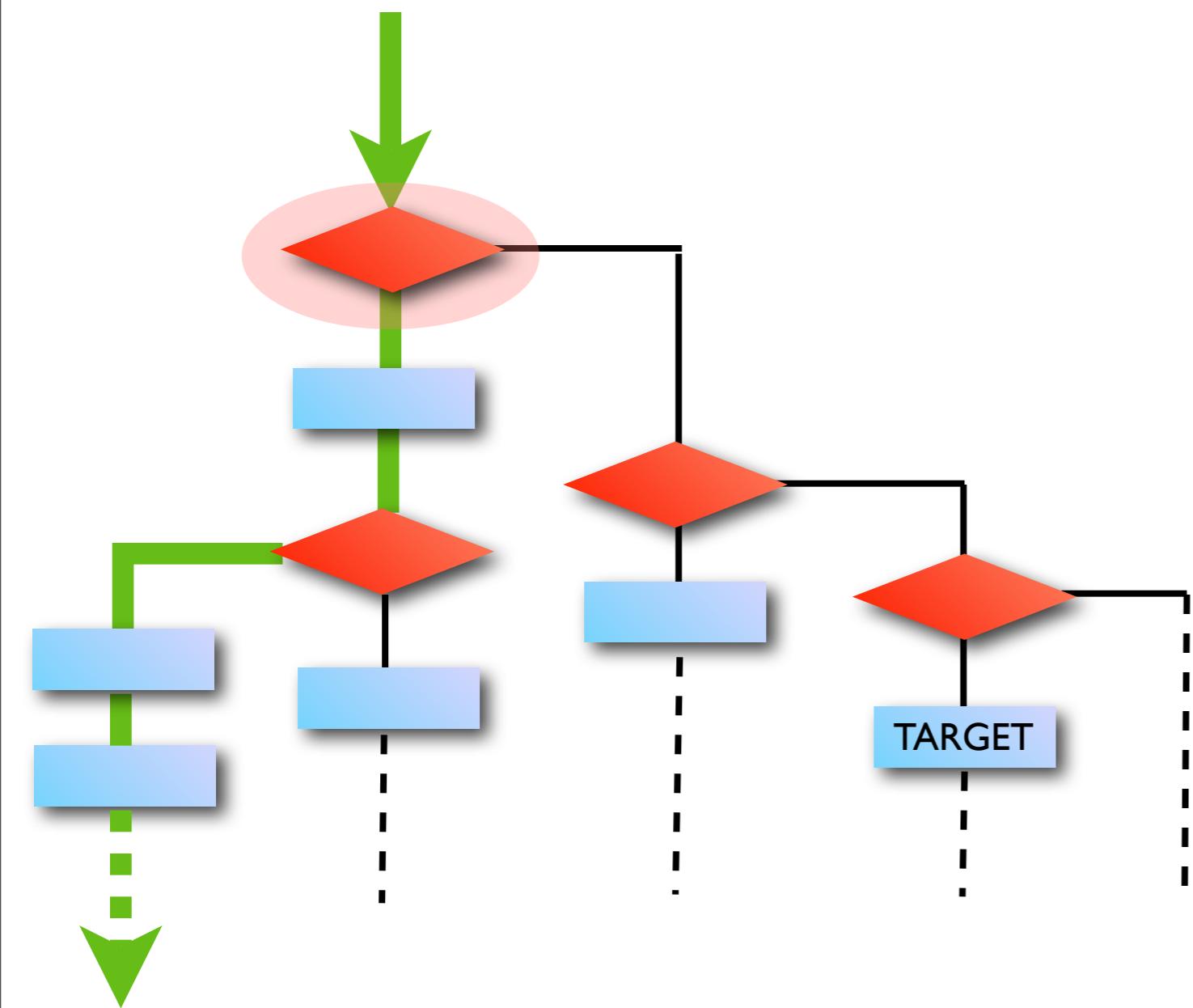
Estimation of Distribution Algorithms

Search-Based Structural Test Data Generation

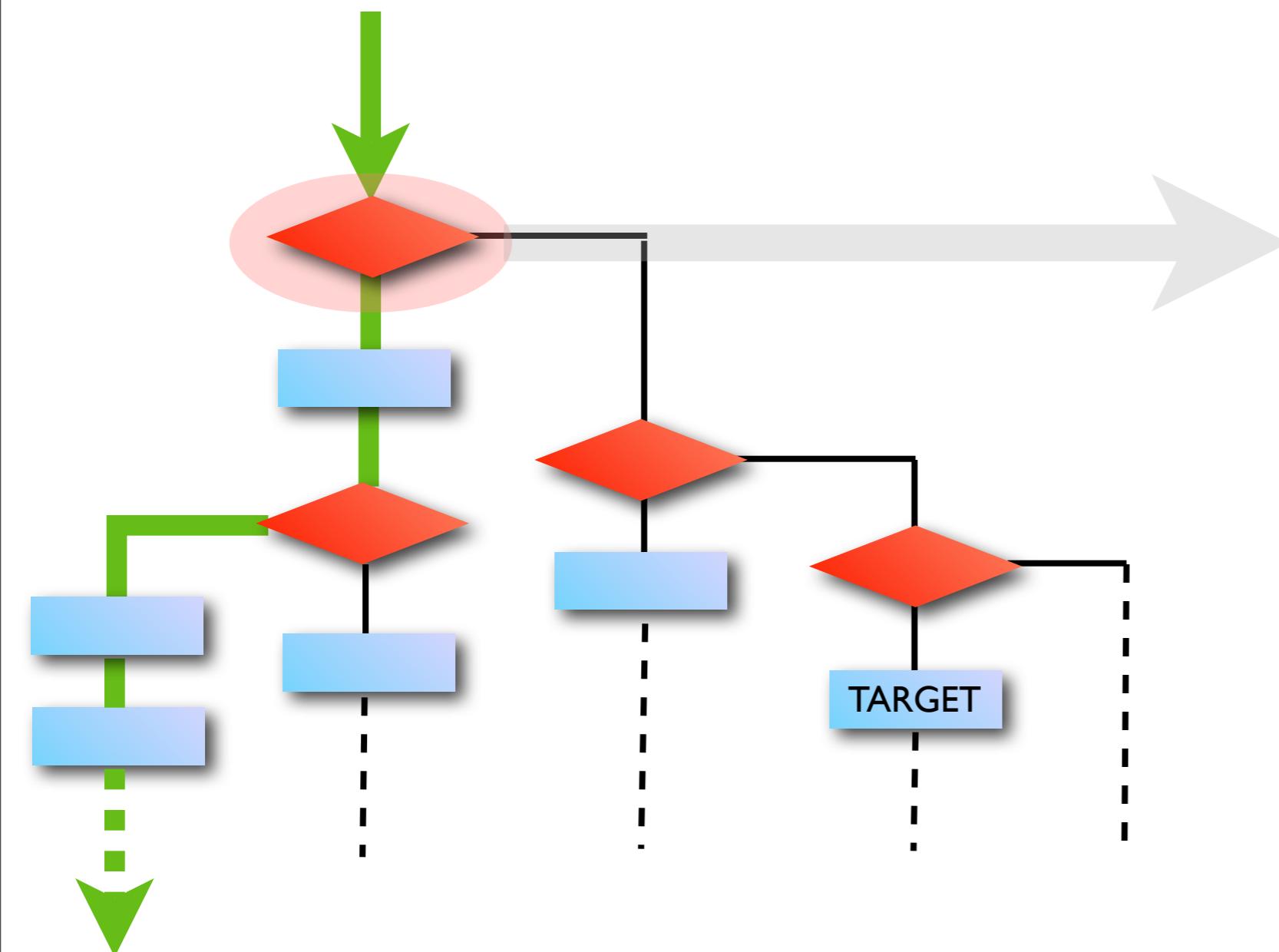
Covering a structure



Fitness evaluation

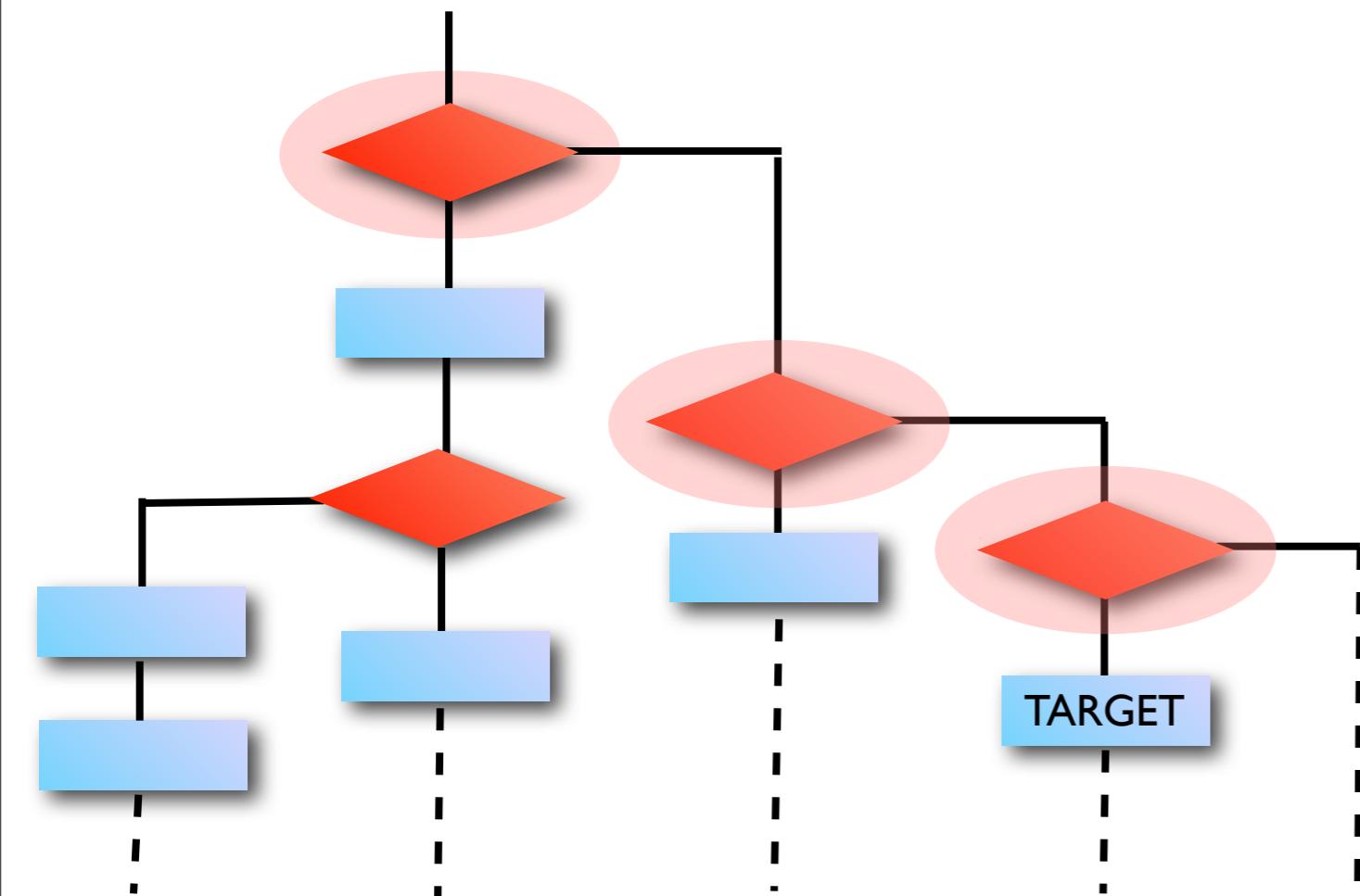


Fitness evaluation

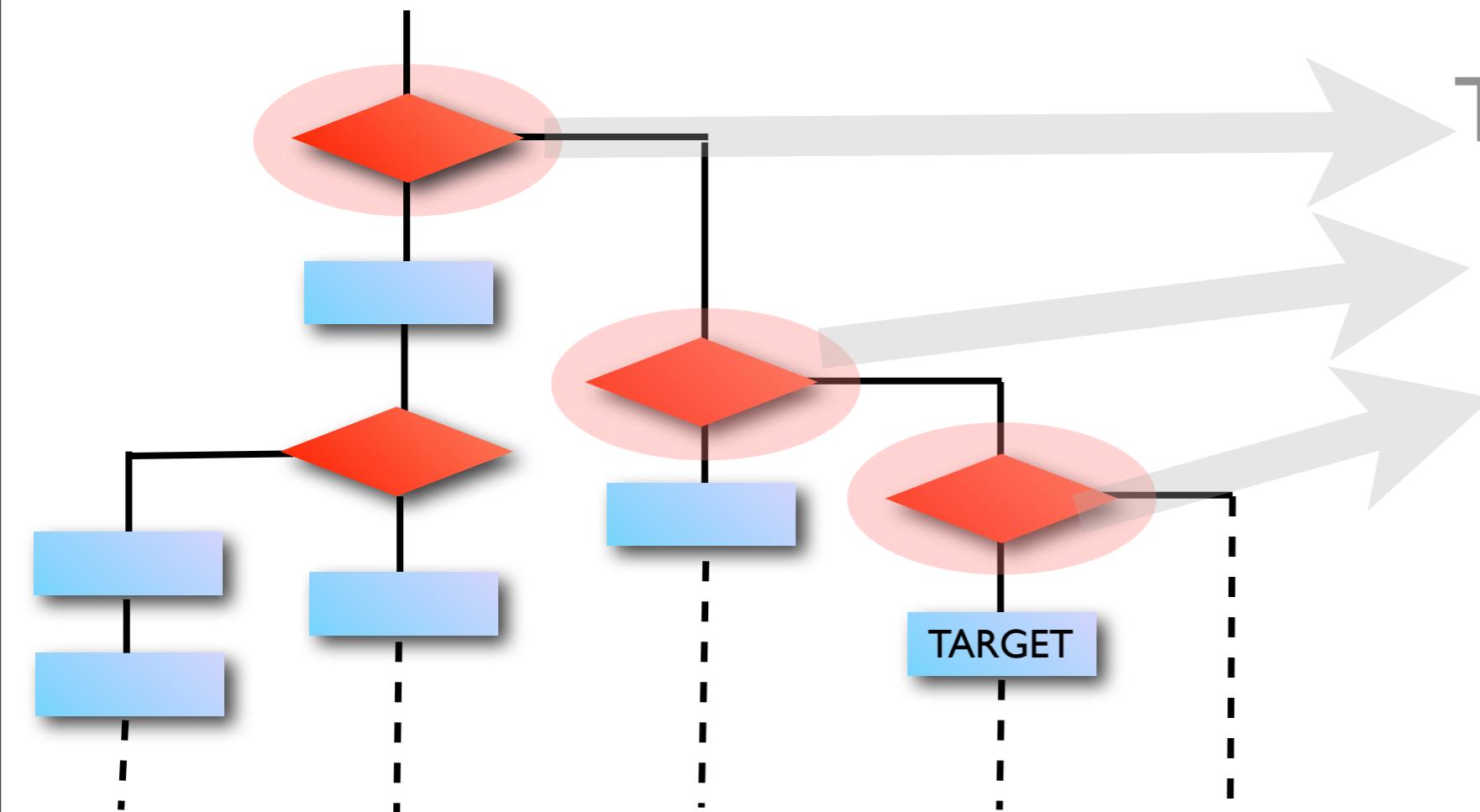


The test data
executes the
'wrong' path

Analysing control flow



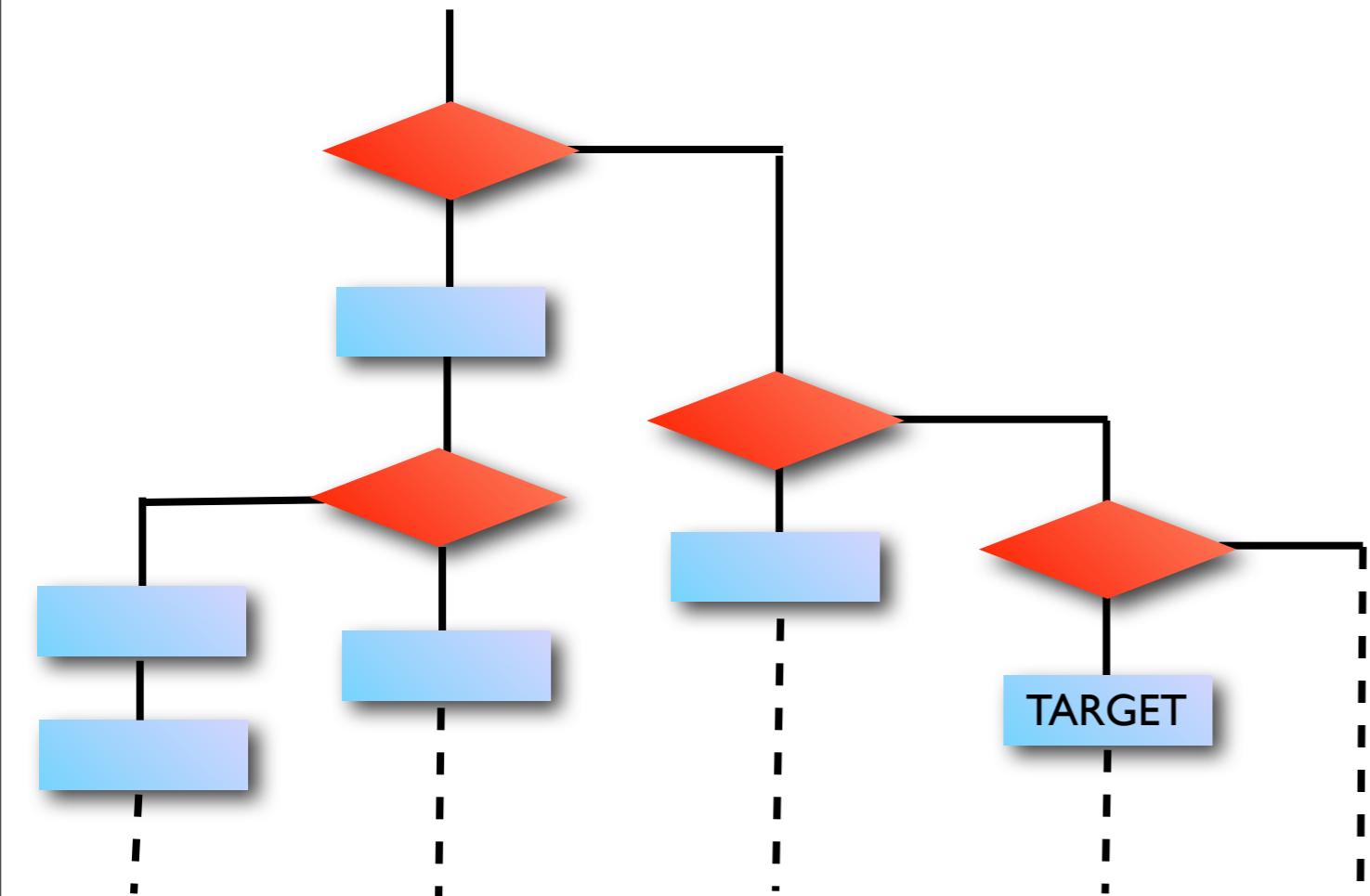
Analysing control flow



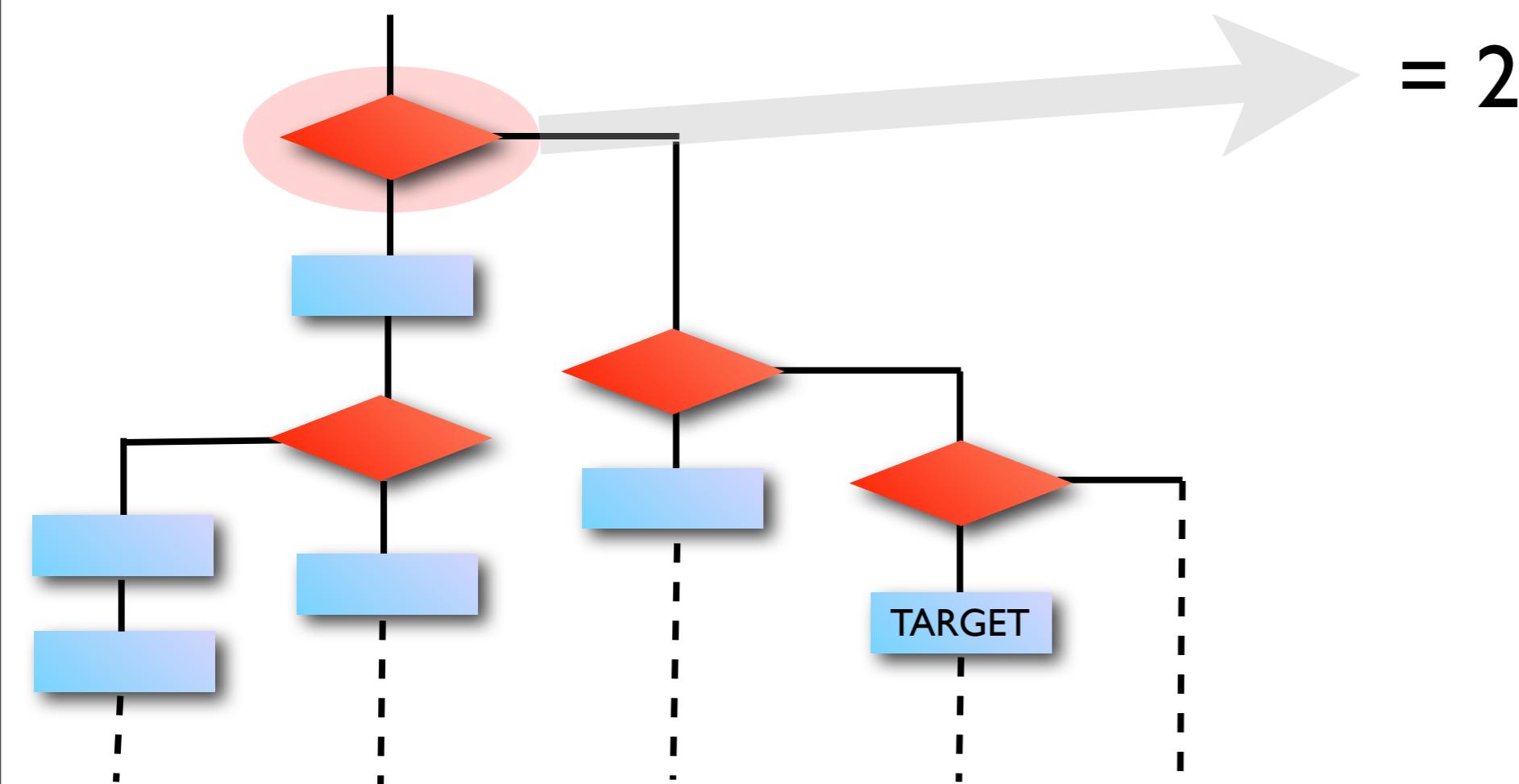
The outcomes at key decision statements matter.

These are the decisions on which the target is **control dependent**

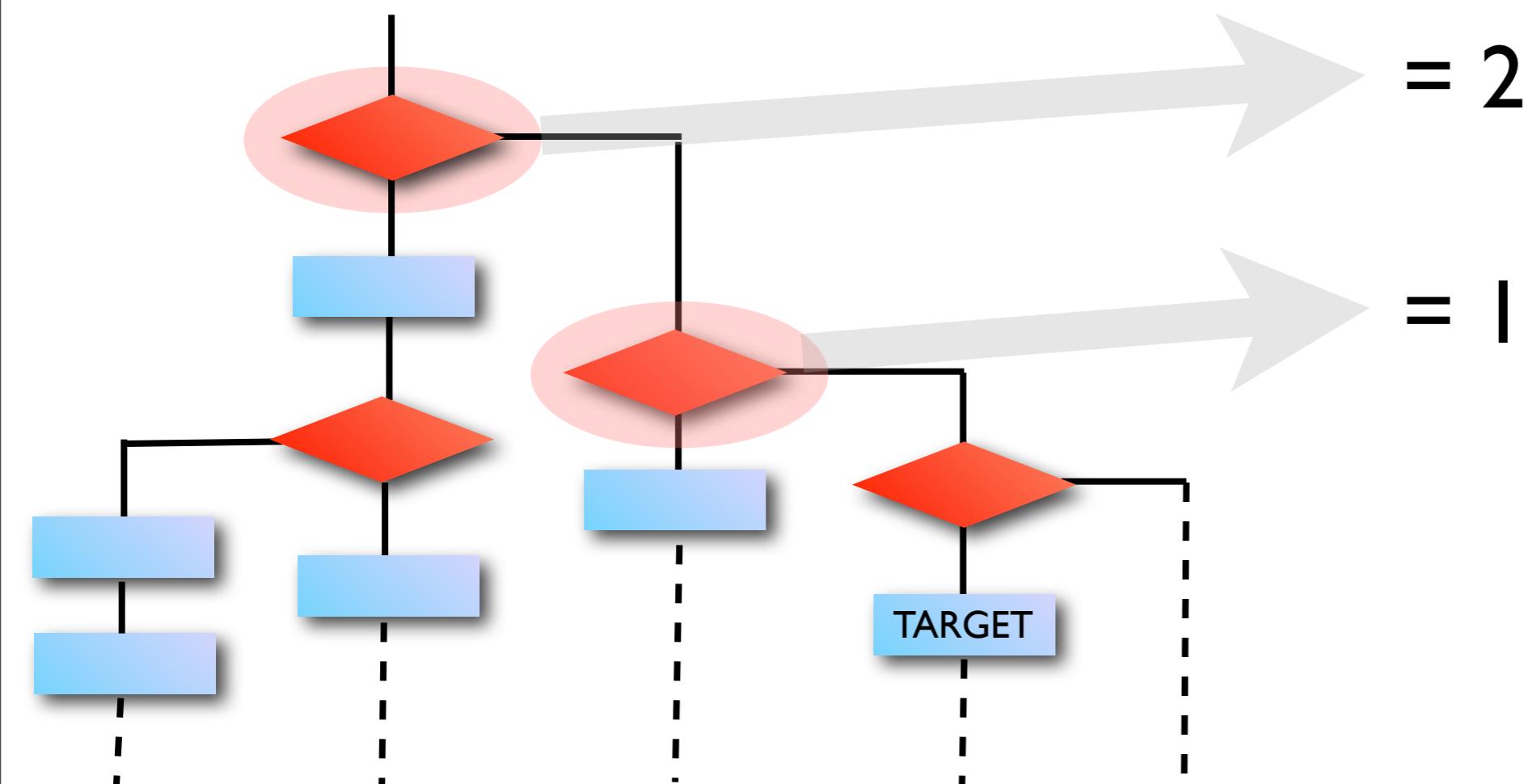
Approach Level



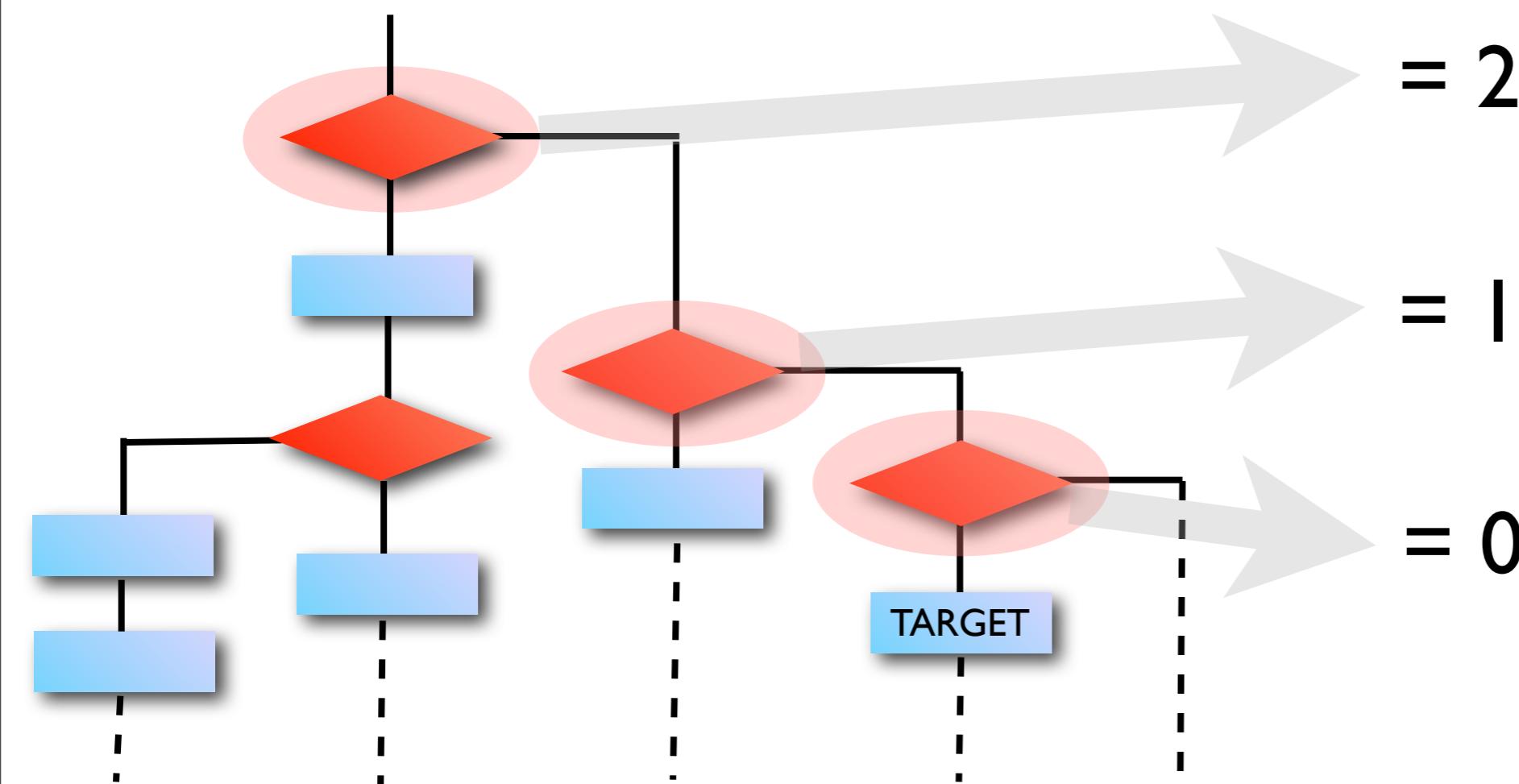
Approach Level



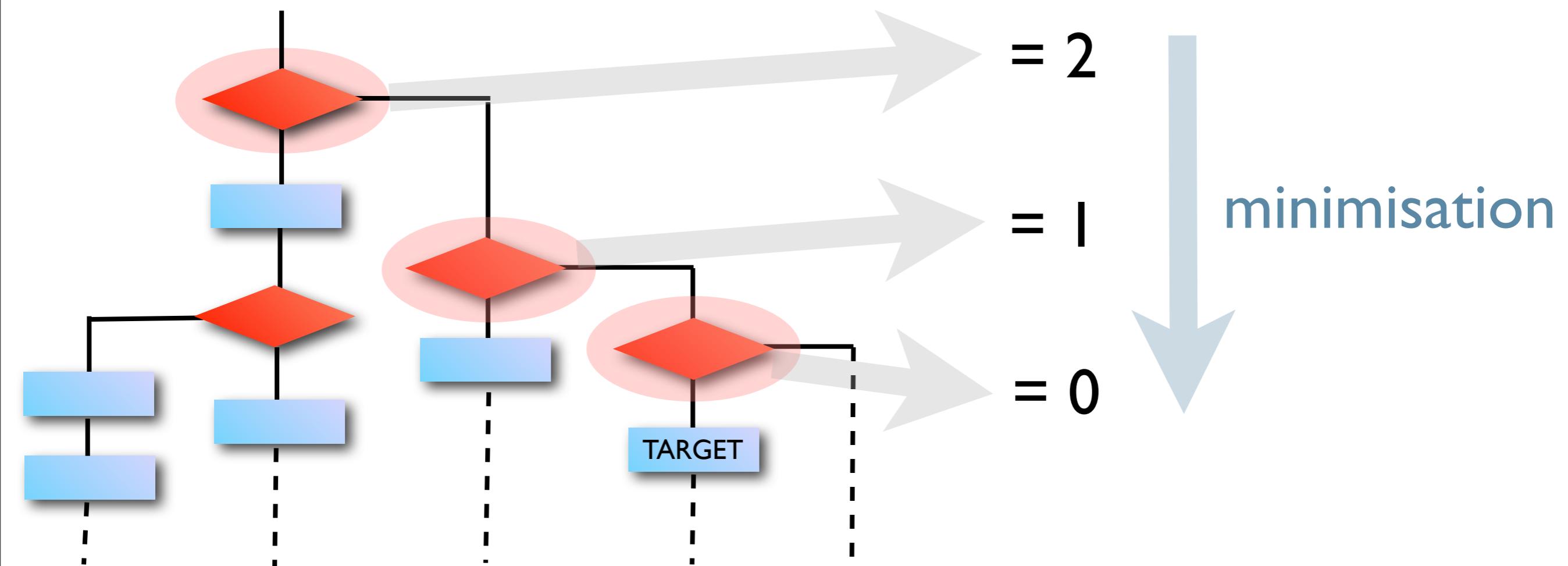
Approach Level



Approach Level



Approach Level



Analysing predicates

Approach level alone gives us coarse values

```
if (a == b) {  
    // ....  
}
```

a = 50, b = 0
a = 45, b = 5
a = 40, b = 10
a = 35, b = 15
a = 30, b = 20
a = 25, b = 25

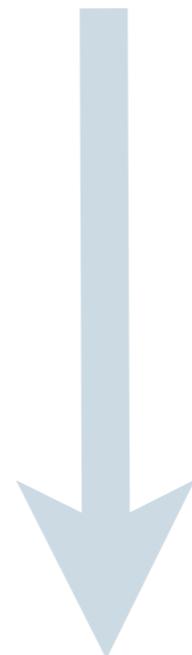
Analysing predicates

Approach level alone gives us coarse values

```
if (a == b) {  
    // ....  
}
```

a = 50, b = 0
a = 45, b = 5
a = 40, b = 10
a = 35, b = 15
a = 30, b = 20
a = 25, b = 25

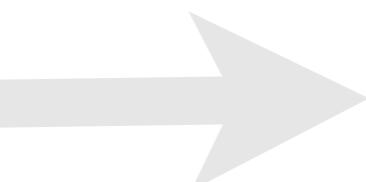
getting ‘closer’
to being true



Branch distance

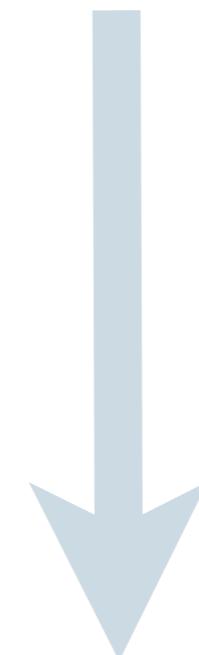
Associate a distance formula with different relational predicates

```
if (a == b) {  
    //....  
}
```



$\text{abs}(a-b)$

a = 50, b = 0	branch distance = 50
a = 45, b = 5	branch distance = 40
a = 40, b = 10	branch distance = 30
a = 35, b = 15	branch distance = 20
a = 30, b = 20	branch distance = 10
a = 25, b = 25	branch distance = 0



getting ‘closer’
to being true

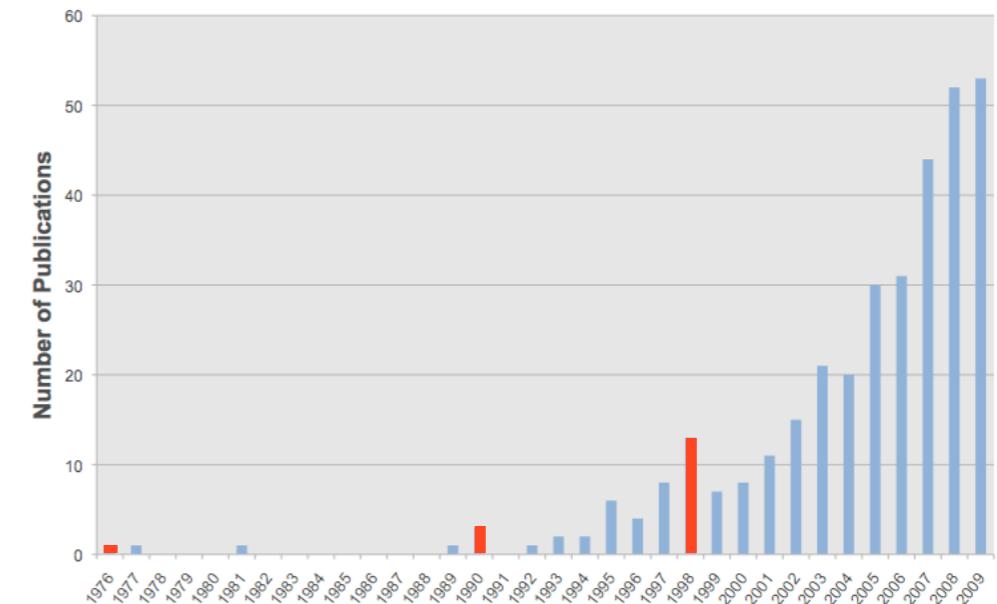
Branch distances for relational predicates

Relational predicate	Objective function obj
Boolean	if $TRUE$ then 0 else K
$a = b$	if $abs(a - b) = 0$ then 0 else $abs(a - b) + K$
$a \neq b$	if $abs(a - b) \neq 0$ then 0 else K
$a < b$	if $a - b < 0$ then 0 else $(a - b) + K$
$a \leq b$	if $a - b \leq 0$ then 0 else $(a - b) + K$
$a > b$	if $b - a < 0$ then 0 else $(b - a) + K$
$a \geq b$	if $b - a \leq 0$ then 0 else $(b - a) + K$
$\neg a$	Negation is moved inwards and propagated over a

Webb Miller & D. Spooner. Automatic Generation of Floating-Point Test Data. IEEE Trans. Software Eng. 1976

Bogdan Korel. Automated Software Test Data Generation. IEEE Trans. Software Eng. 1990

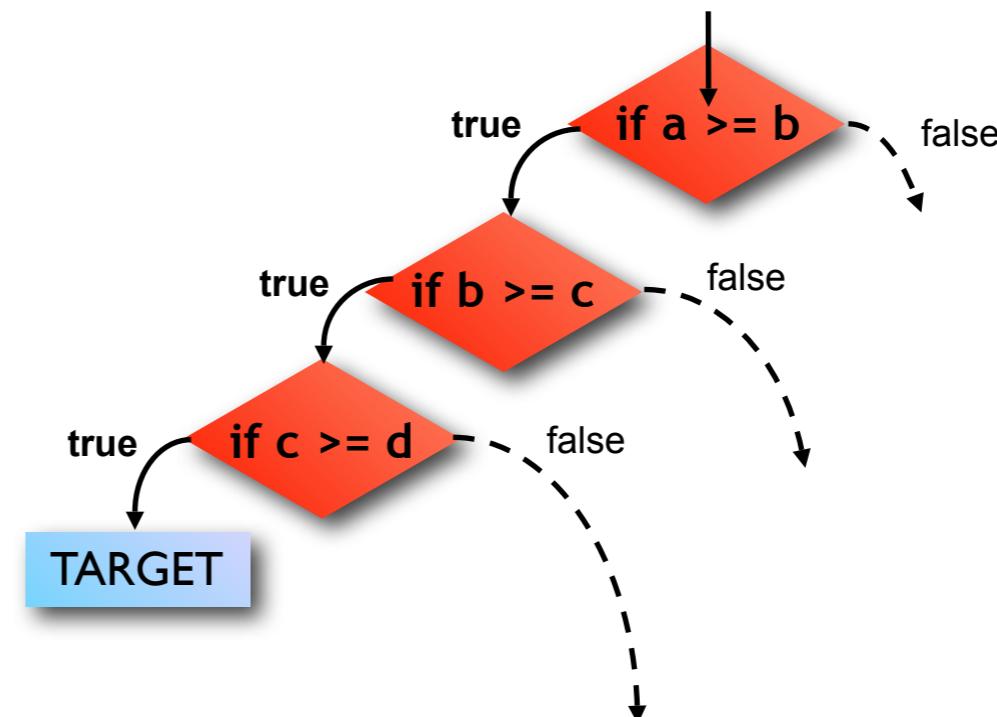
Nigel Tracey, John Clark & Keith Mander. The Way Forward for Unifying Dynamic Test-Case Generation: The Optimisation-Based Approach. 1998



Putting it all together

Fitness = approach Level + *normalised branch distance*

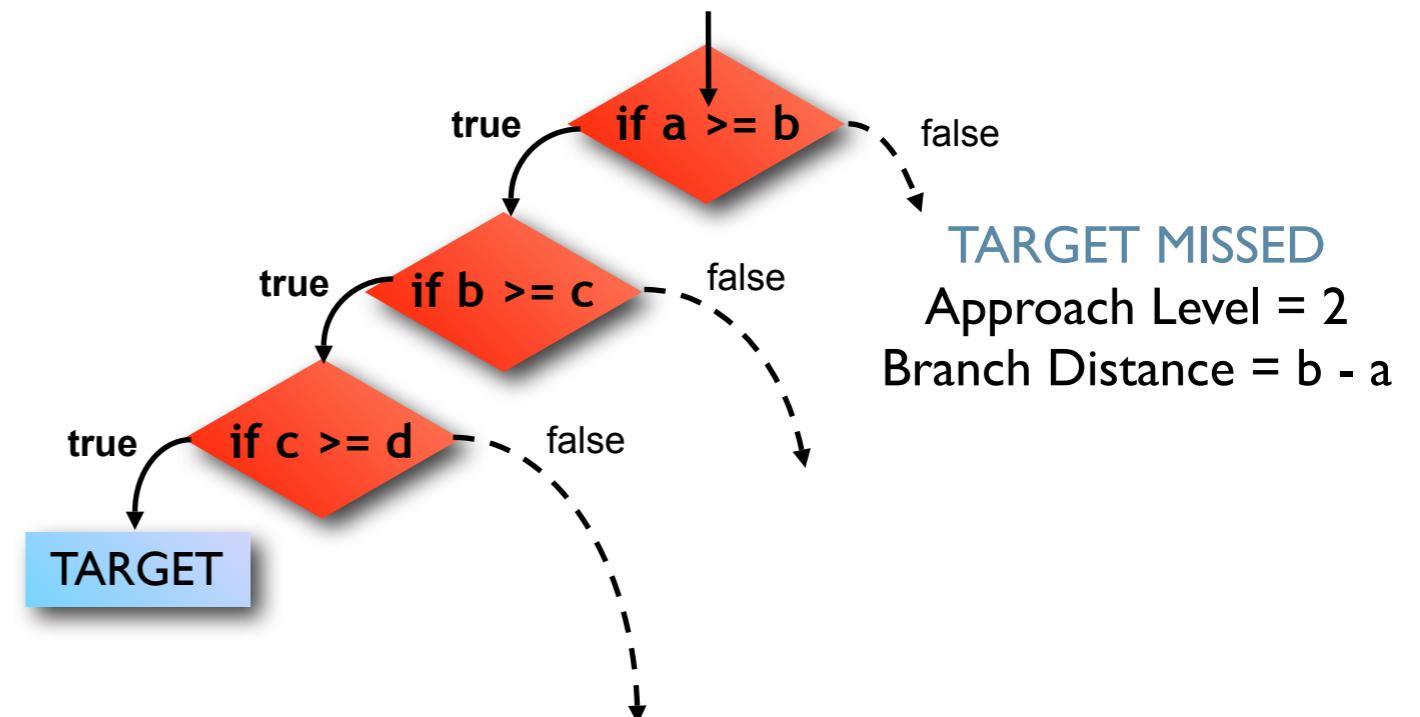
```
void f1(int a, int b, int c, int d)
{
    if (a > b)
    {
        if (b > c)
        {
            if (c > d)
            {
                // target
            }
        }
    }
}
```



Putting it all together

Fitness = approach Level + *normalised* branch distance

```
void f1(int a, int b, int c, int d)
{
    if (a > b)
    {
        if (b > c)
        {
            if (c > d)
            {
                // target
            }
        }
    }
}
```

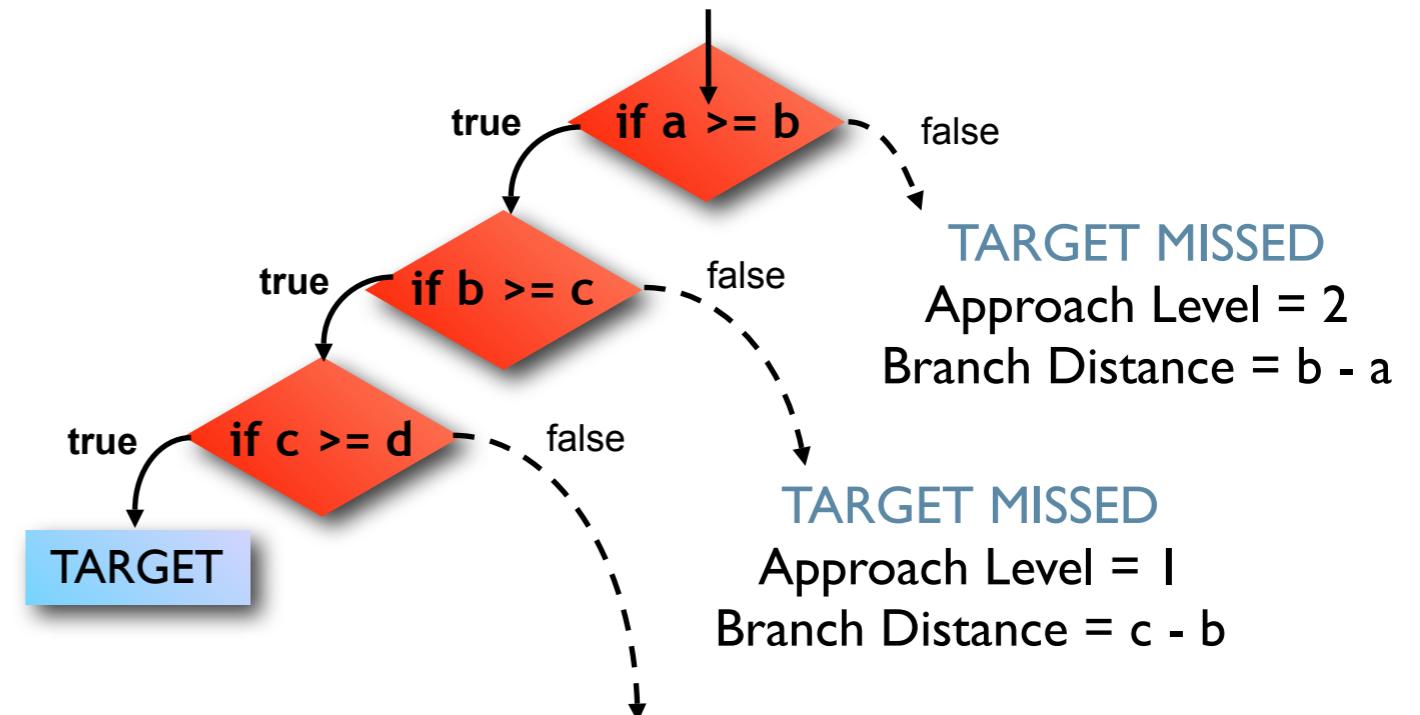


normalised branch distance between 0 and 1
indicates how close approach level is to being penetrated

Putting it all together

Fitness = approach Level + *normalised* branch distance

```
void f1(int a, int b, int c, int d)
{
    if (a > b)
    {
        if (b > c)
        {
            if (c > d)
            {
                // target
            }
        }
    }
}
```

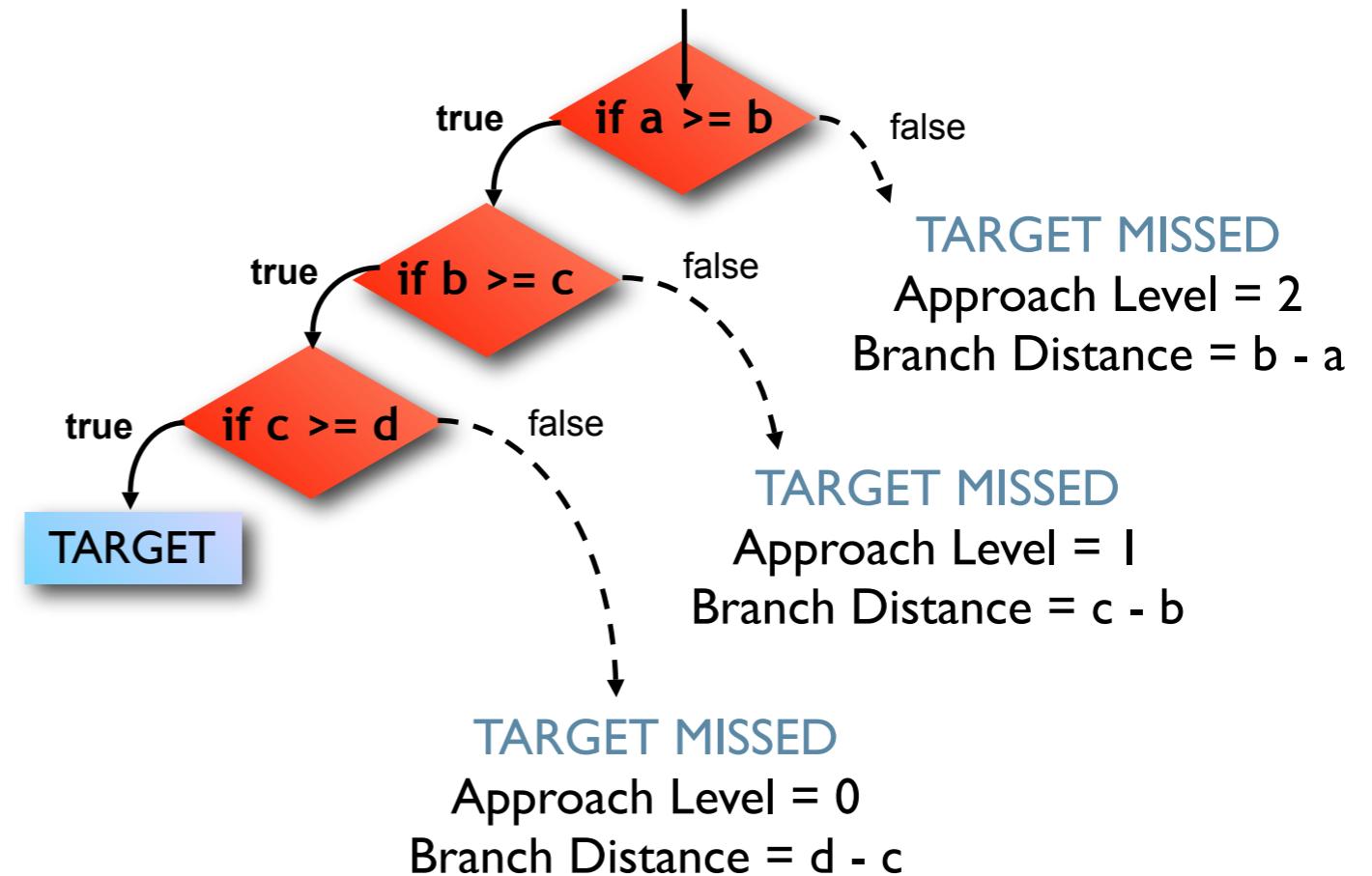


normalised branch distance between 0 and 1
indicates how close approach level is to being penetrated

Putting it all together

Fitness = approach Level + *normalised* branch distance

```
void f1(int a, int b, int c, int d)
{
    if (a > b)
    {
        if (b > c)
        {
            if (c > d)
            {
                // target
            }
        }
    }
}
```



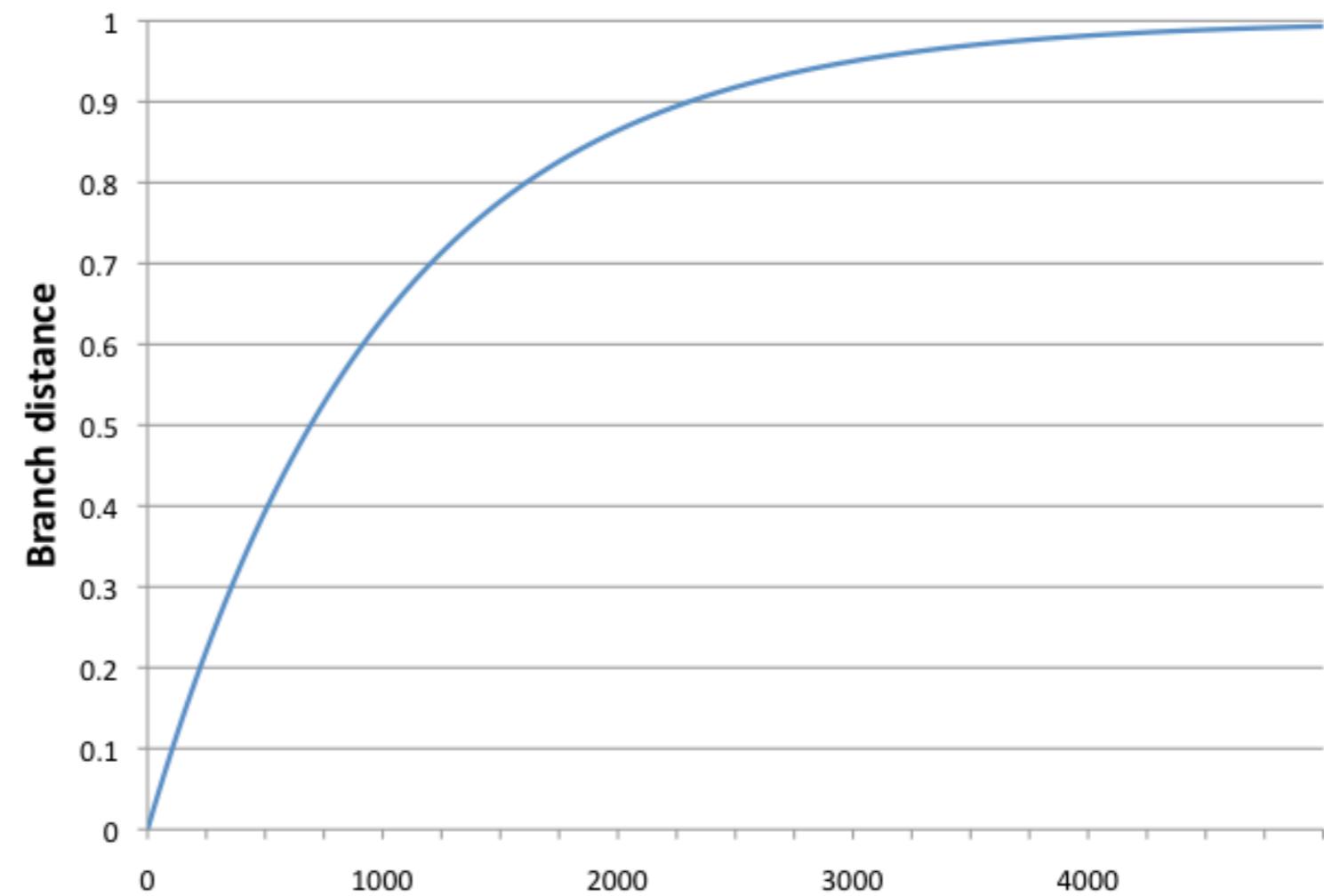
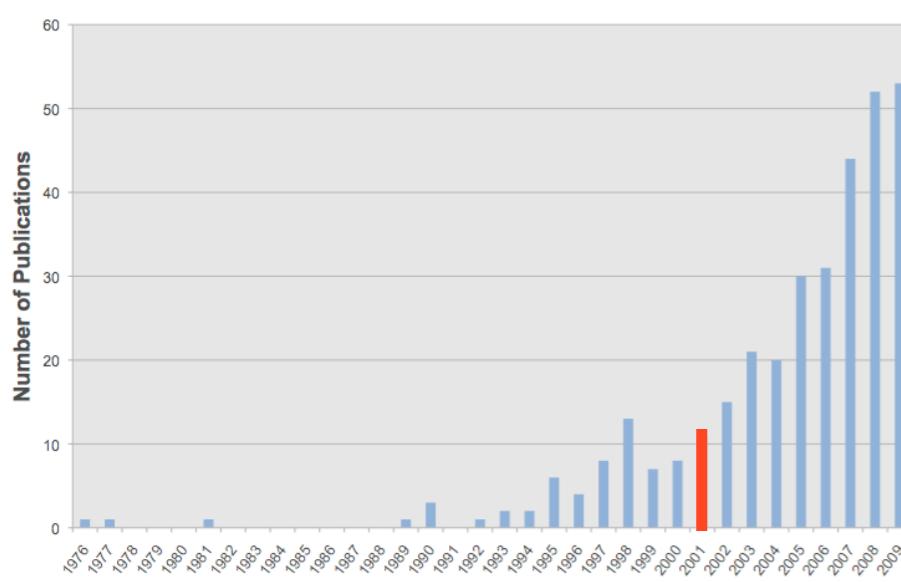
normalised branch distance between 0 and 1
indicates how close approach level is to being penetrated

Normalisation Functions

Since the ‘maximum’ branch distance is generally unknown
we need a non-standard normalisation function

$$1 - \alpha^{-x}$$

Baresel (2000), alpha = 1.001

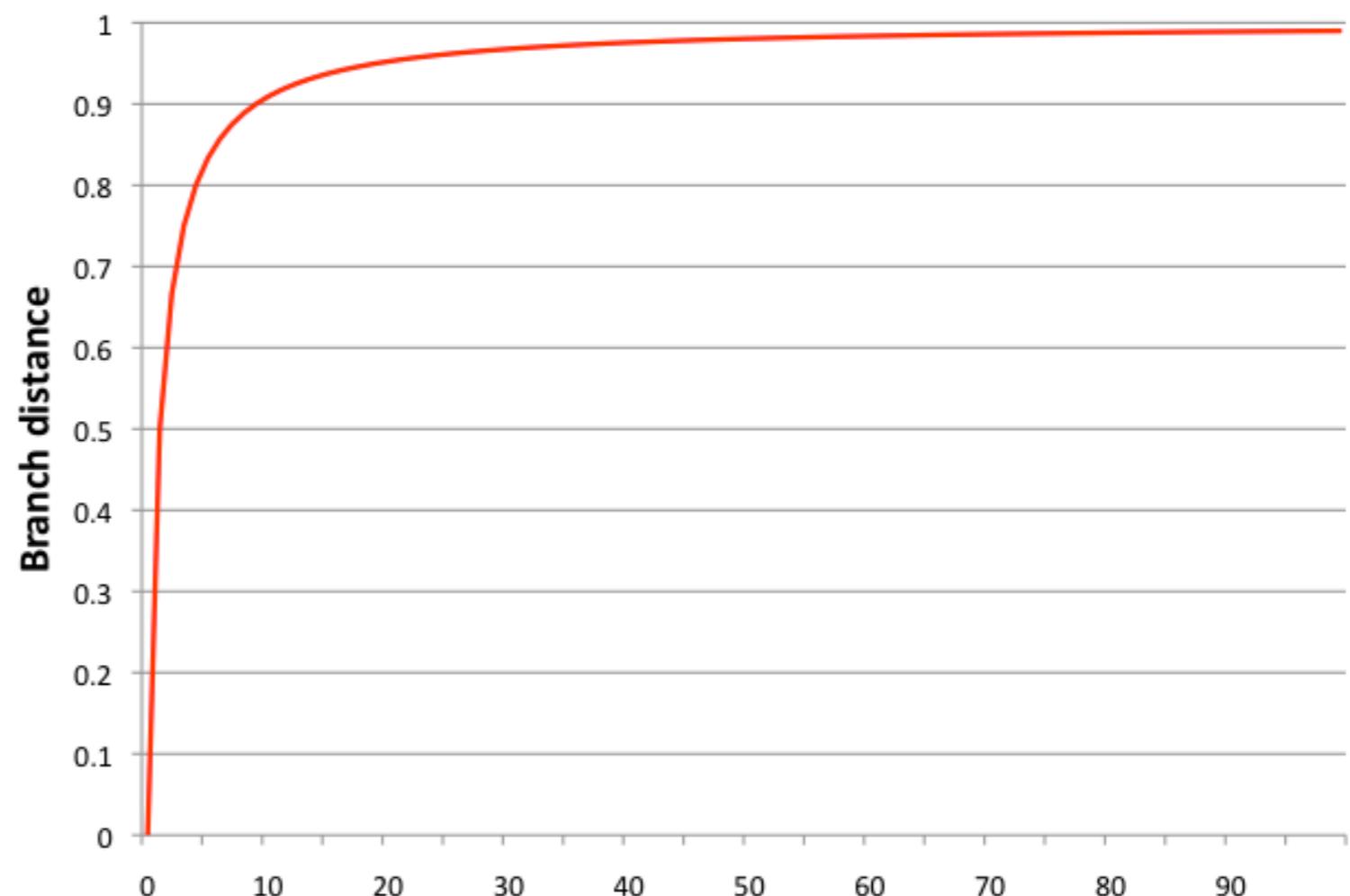


Normalisation Functions

Since the ‘maximum’ branch distance is generally unknown we need a non-standard normalisation function

$$\frac{x}{x + \beta}$$

Arcuri (2010), beta = 1



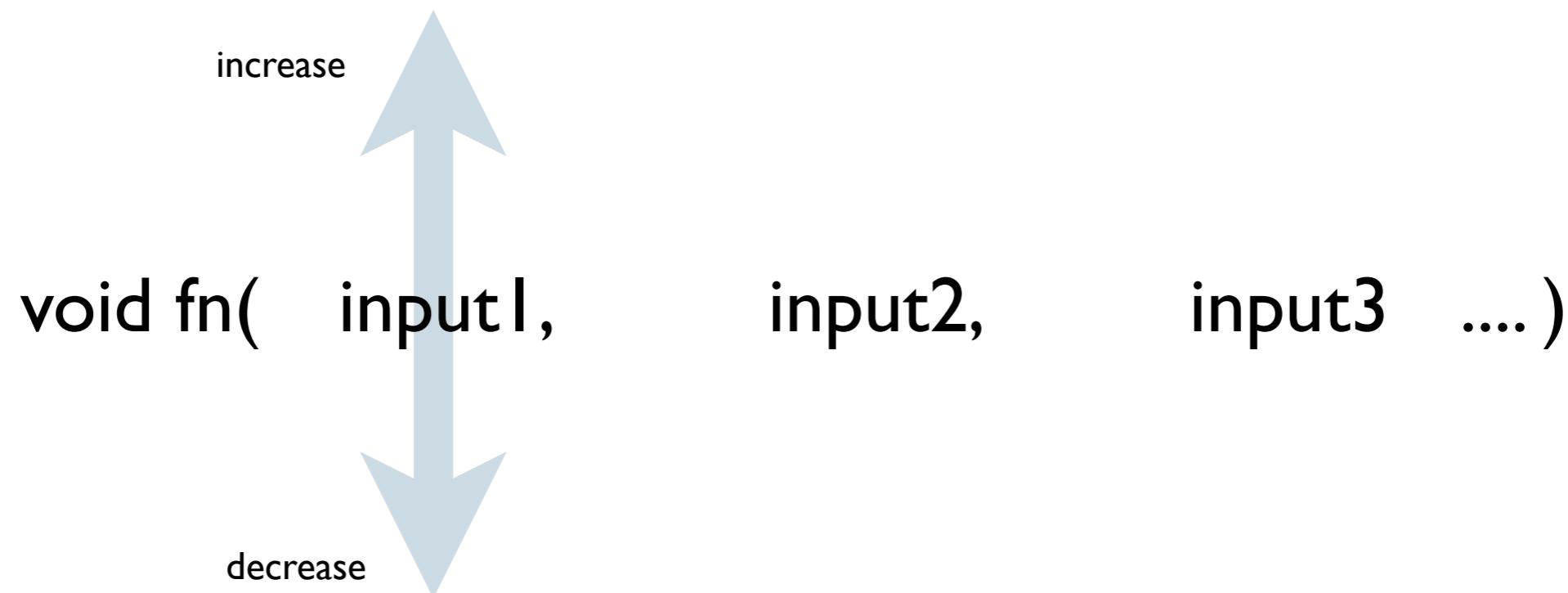
Alternating Variable Method

‘Probe’ moves

```
void fn(  input1,      input2,      input3  .... )
```

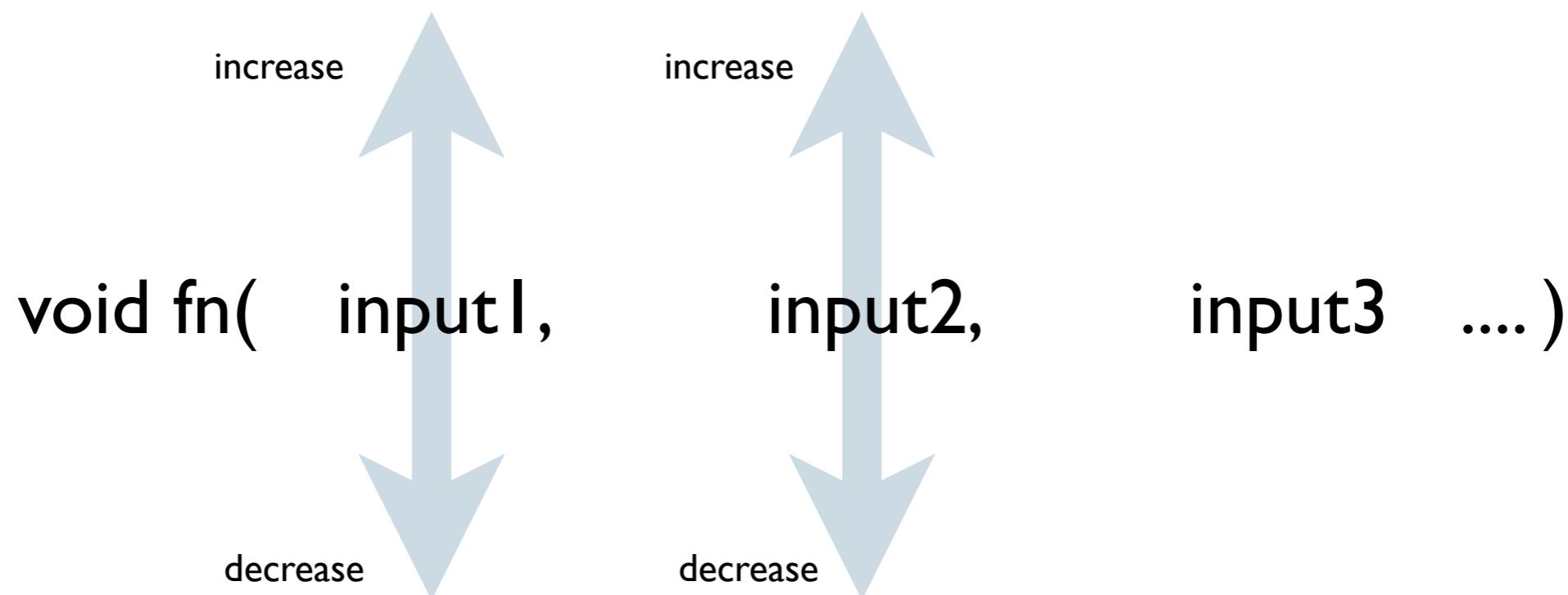
Alternating Variable Method

‘Probe’ moves



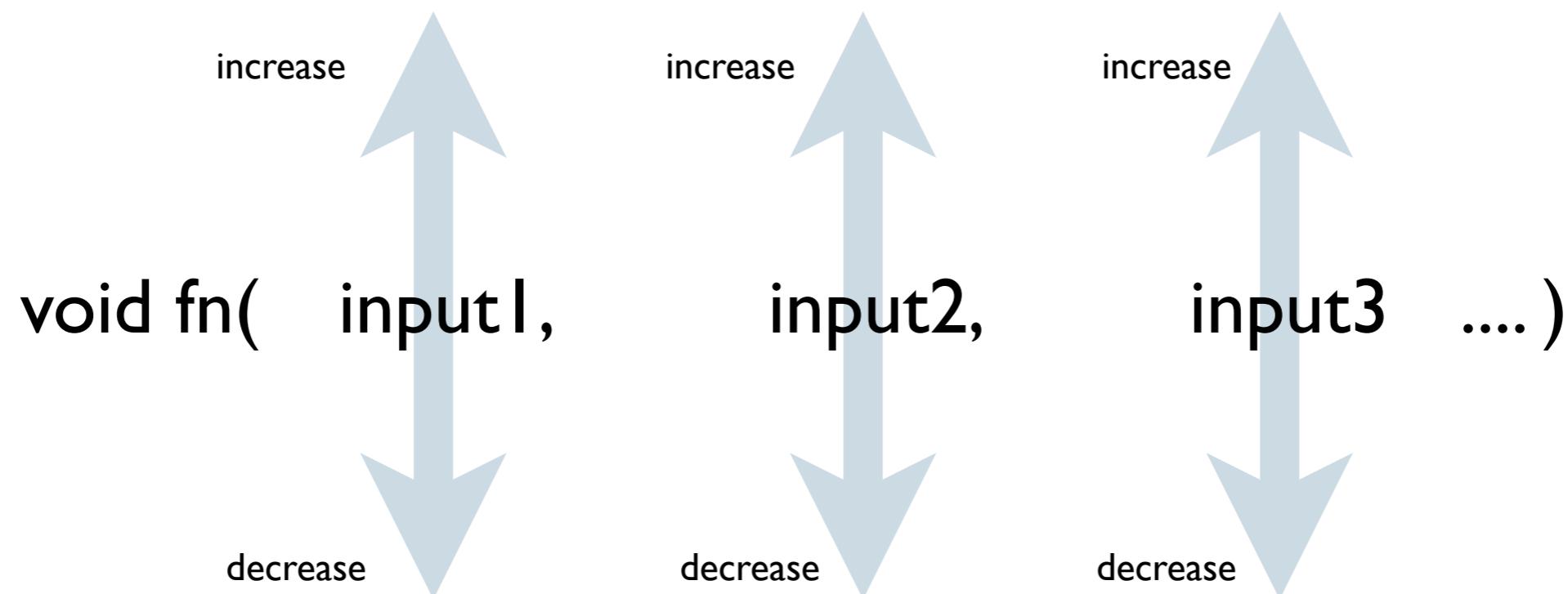
Alternating Variable Method

‘Probe’ moves



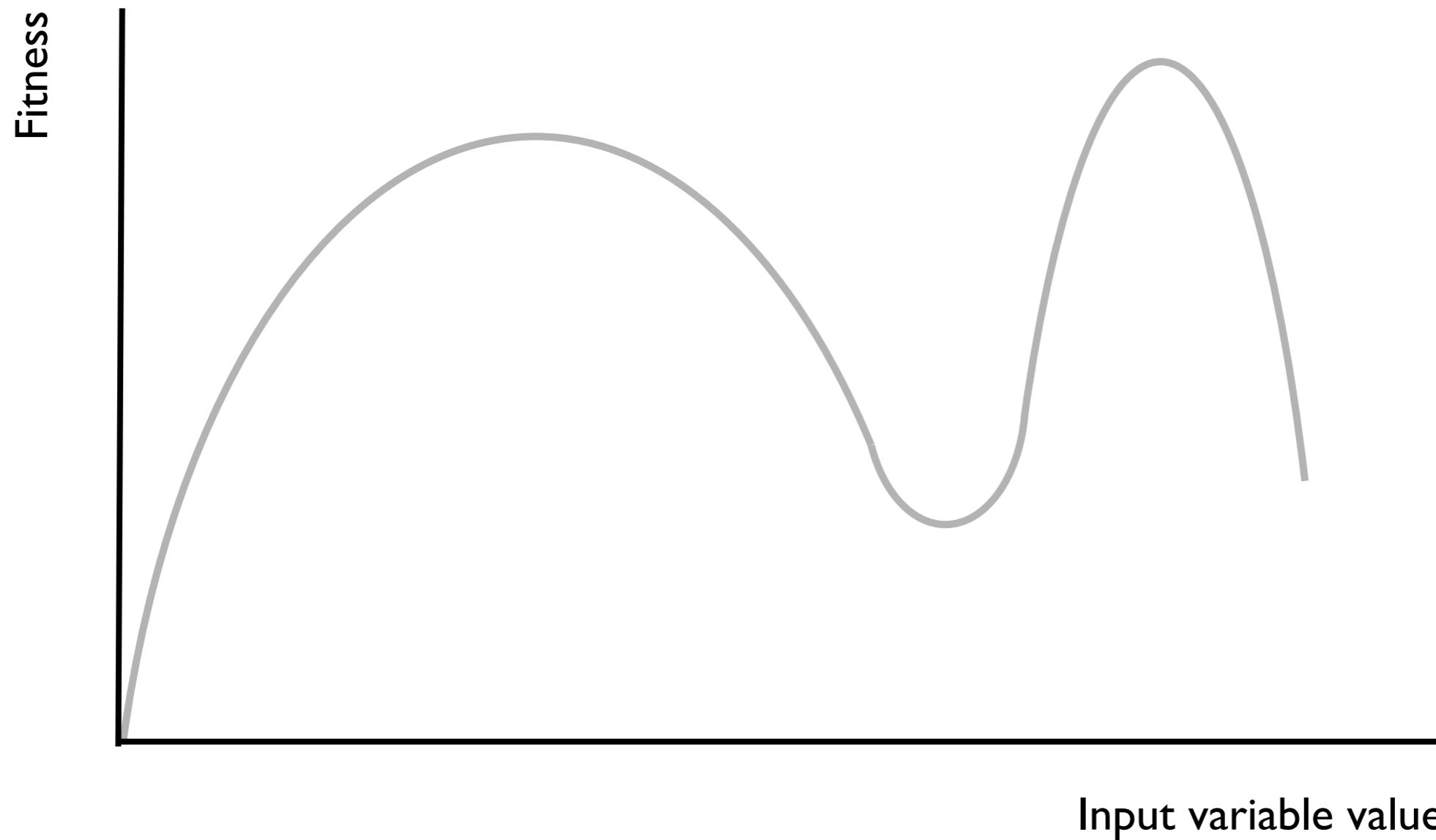
Alternating Variable Method

‘Probe’ moves



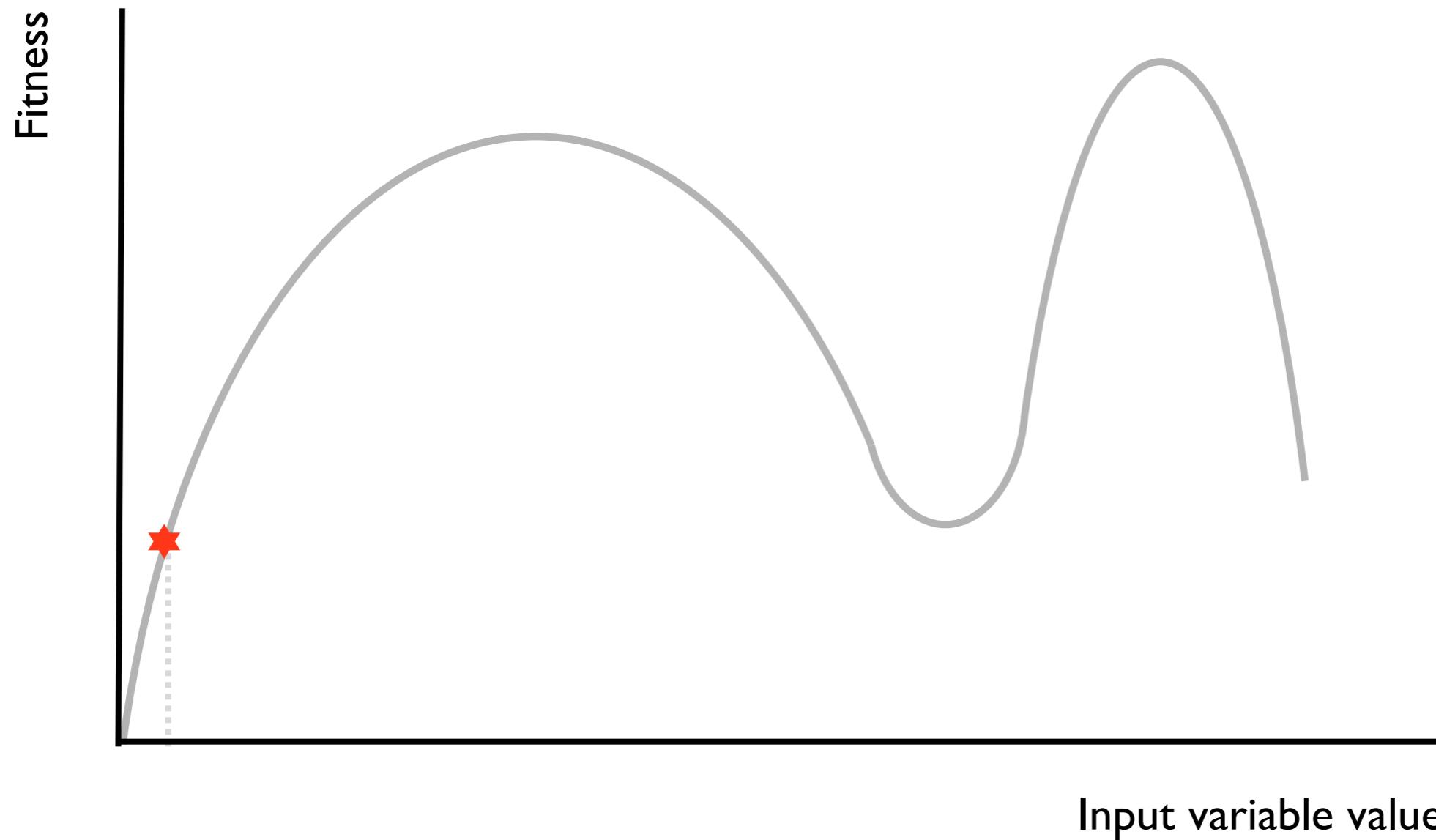
Alternating Variable Method

Accelerated hill climb



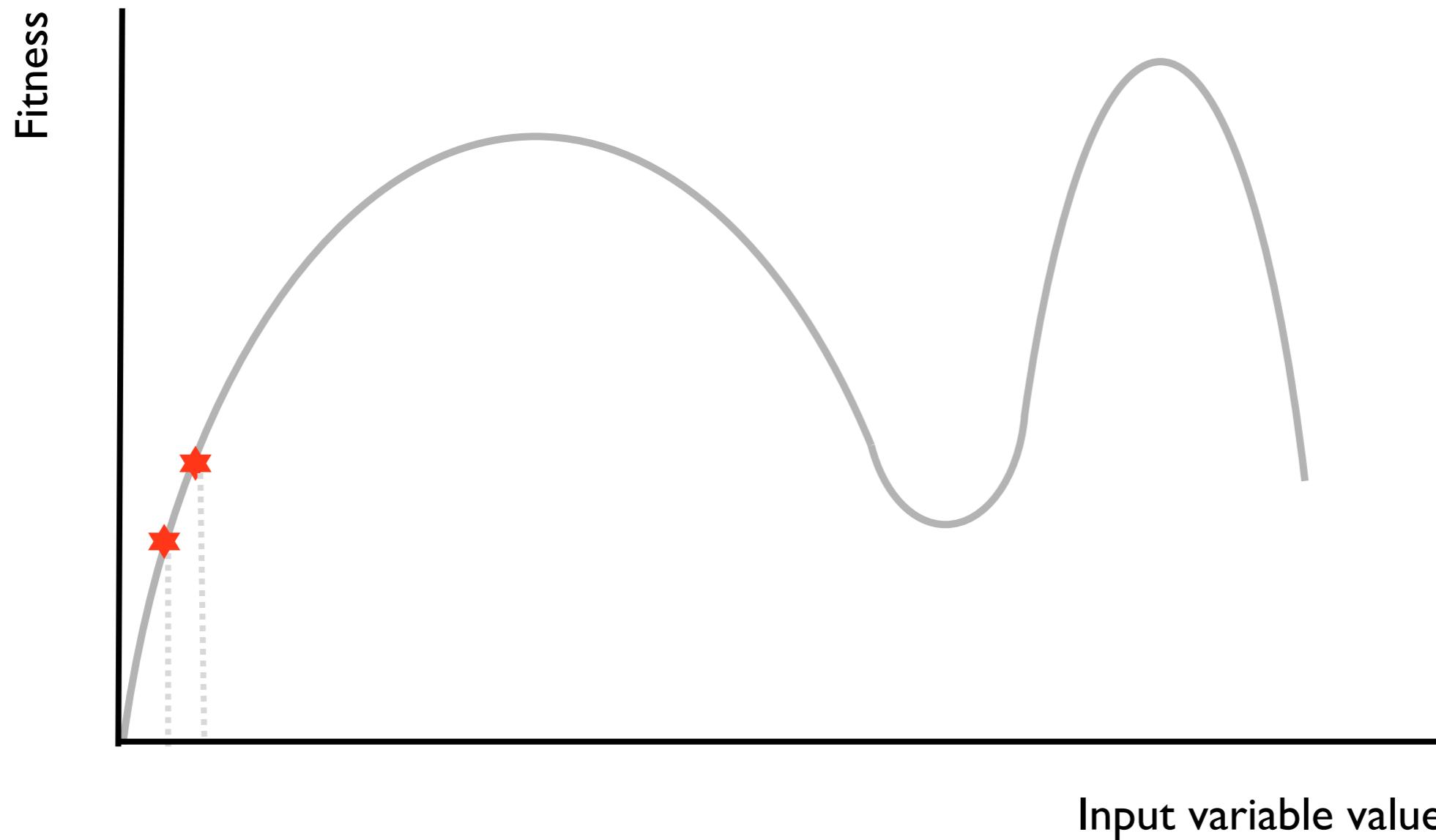
Alternating Variable Method

Accelerated hill climb



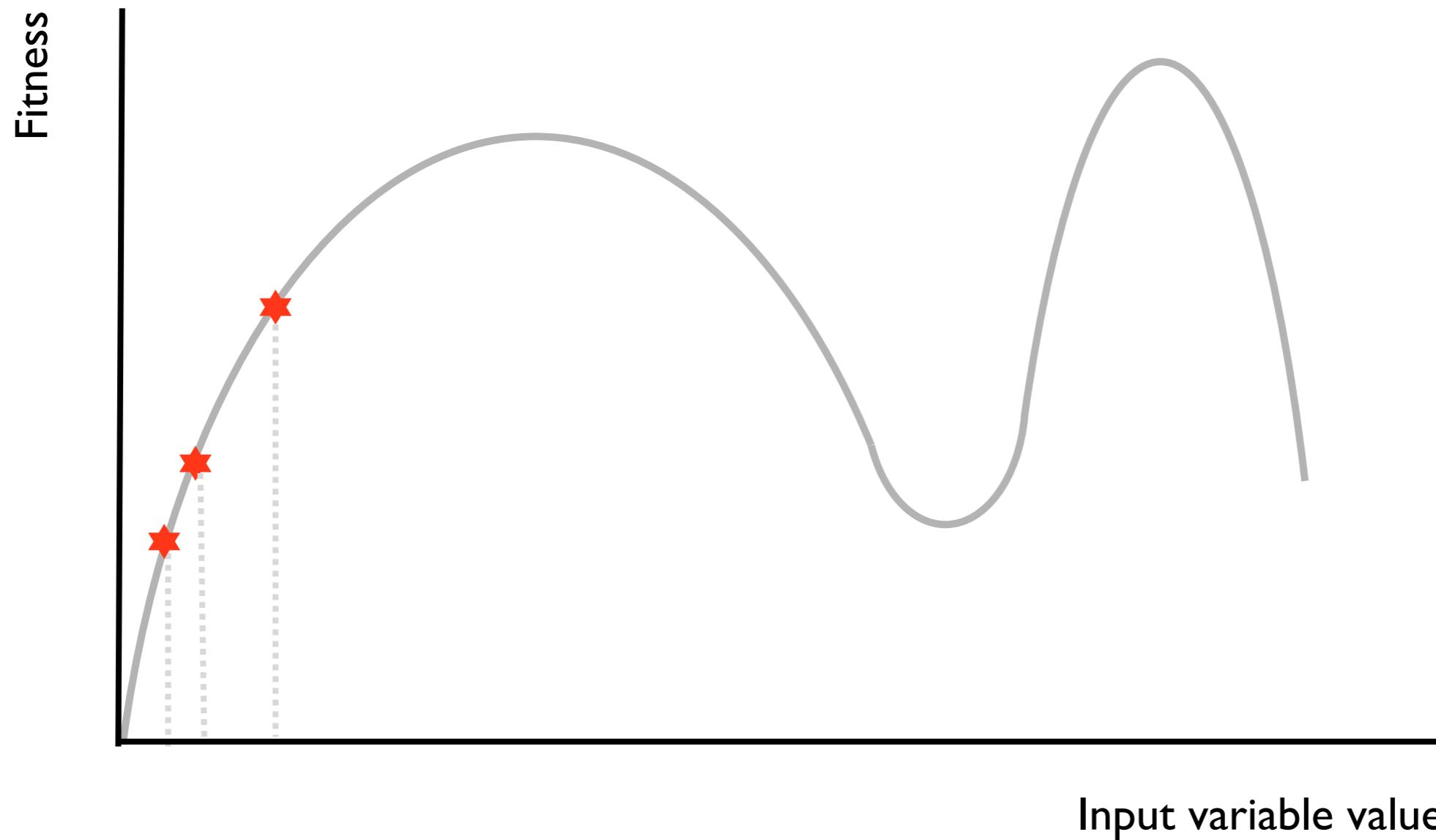
Alternating Variable Method

Accelerated hill climb



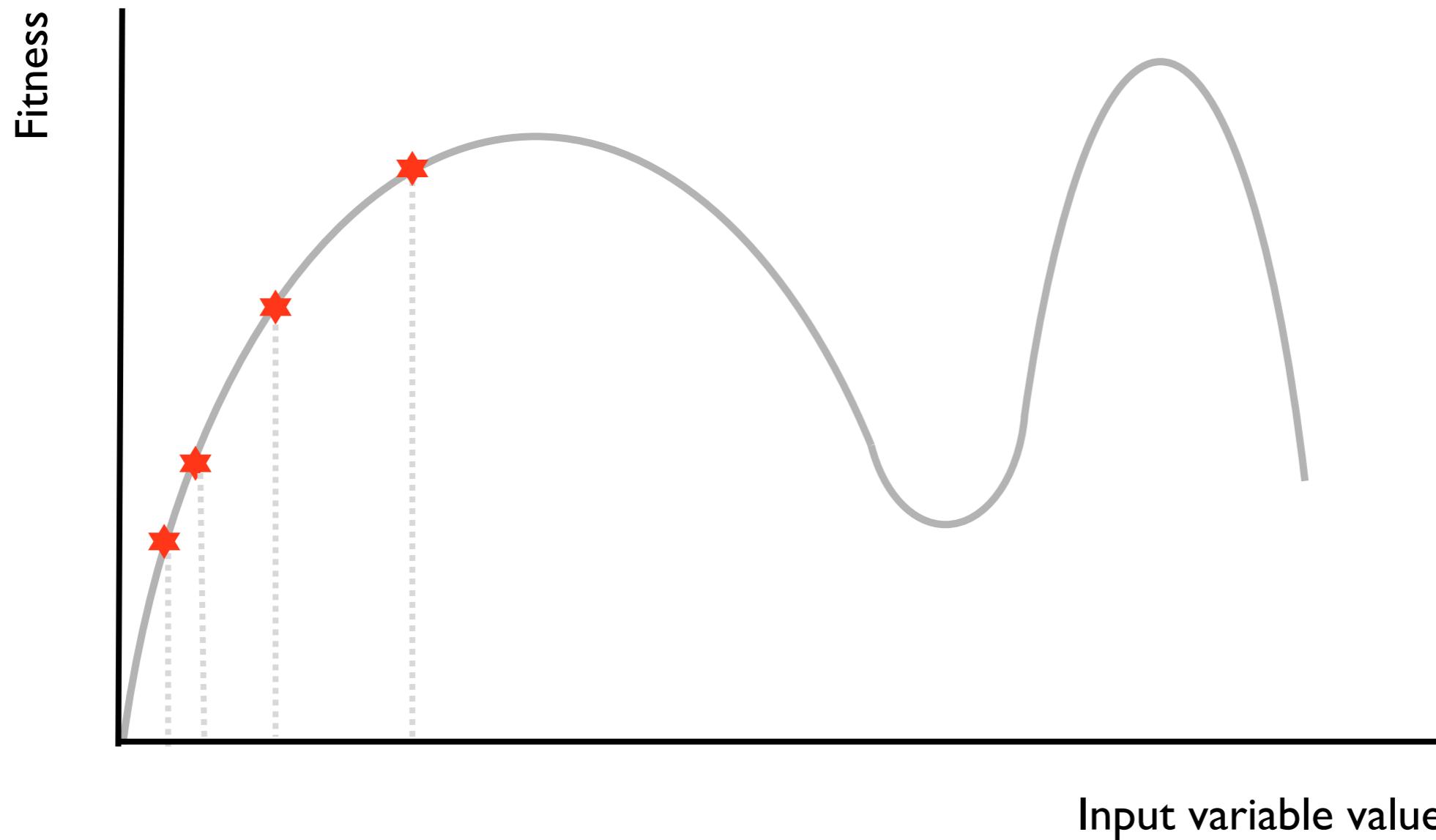
Alternating Variable Method

Accelerated hill climb



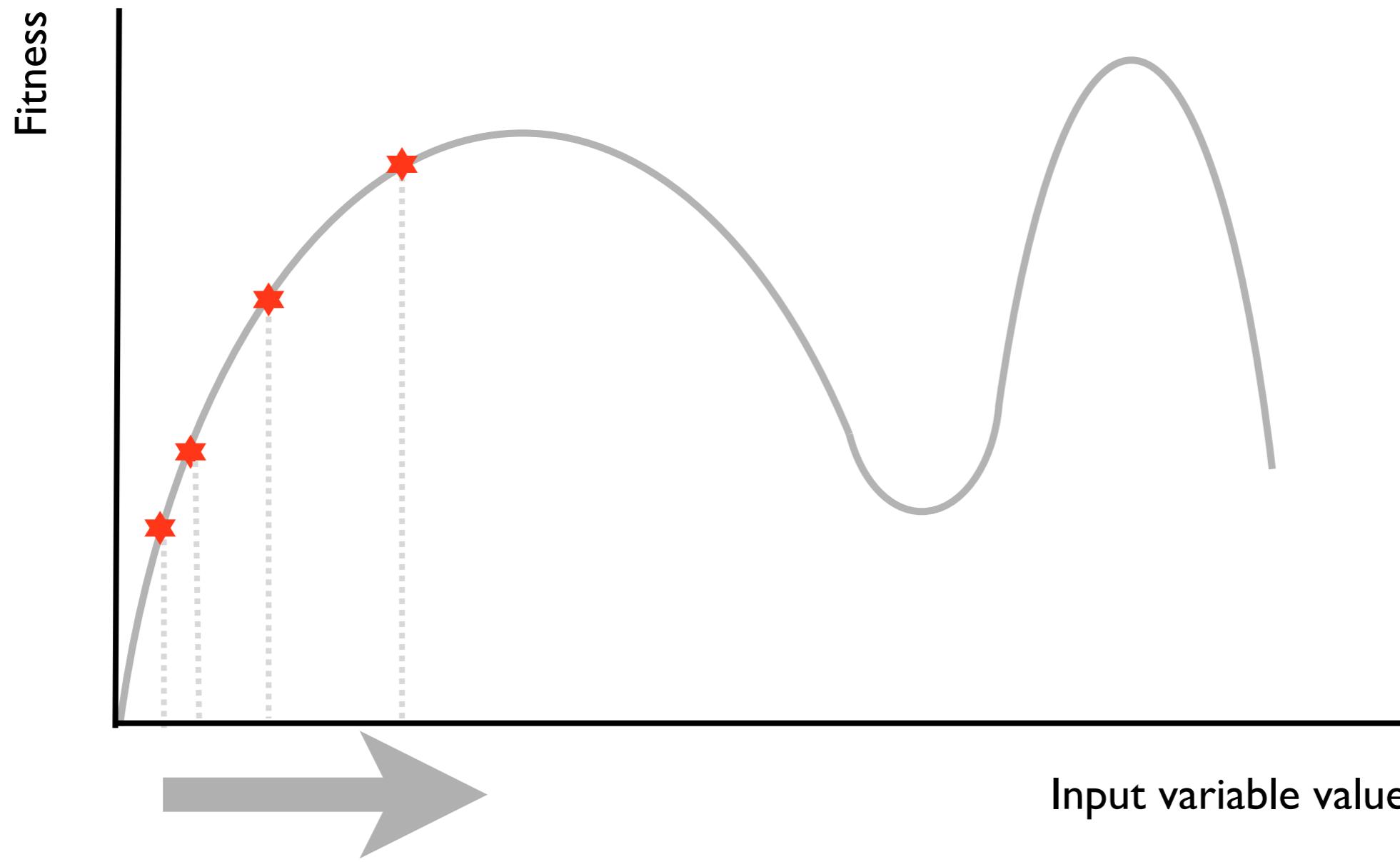
Alternating Variable Method

Accelerated hill climb



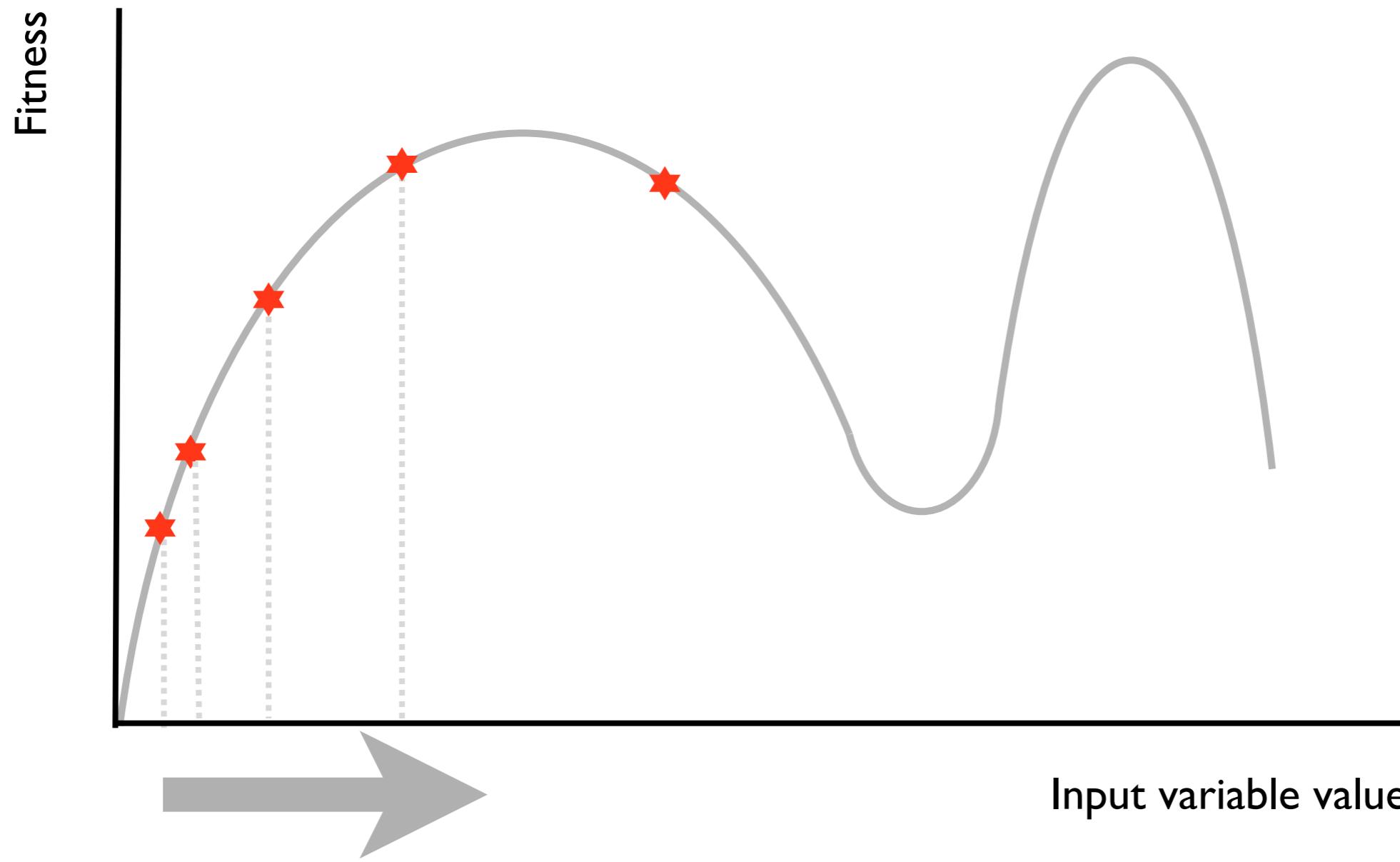
Alternating Variable Method

Accelerated hill climb



Alternating Variable Method

Accelerated hill climb



Alternating Variable Method

I. Randomly generate start point

a=10, b=20, c=30

```
void example(int a, int b, ...) {  
    if (a == 0) {  
        ...  
    }  
  
    if (b == 0) {  
        // target  
    }  
  
    ...  
}
```

Alternating Variable Method

I. Randomly generate start point

a=10, b=20, c=30

2. ‘Probe’ moves on a

a=9, b=20, c=30

a=11, b=20, c=30

no effect

```
void example(int a, int b, ...) {  
    if (a == 0) {  
        ...  
    }  
  
    if (b == 0) {  
        // target  
    }  
    ...  
}
```

Alternating Variable Method

I. Randomly generate start point

a=10, b=20, c=30

2. ‘Probe’ moves on a

a=9, b=20, c=30

a=11, b=20, c=30



3. ‘Probe’ moves on b

a=10, b=19, c=30



```
void example(int a, int b, ...) {  
    if (a == 0) {  
        ...  
    }  
  
    if (b == 0) {  
        // target  
    }  
    ...  
}
```

Alternating Variable Method

I. Randomly generate start point

a=10, b=20, c=30

2. ‘Probe’ moves on a

a=9, b=20, c=30

a=11, b=20, c=30



3. ‘Probe’ moves on b

a=10, b=19, c=30



4. Accelerated moves in direction of improvement

```
void example(int a, int b, ...) {  
    if (a == 0) {  
        ...  
    }  
  
    if (b == 0) {  
        // target  
    }  
    ...  
}
```

A search-based test data generator tool

I nput **G**eneration **U**sing **A**utomated **N**ovel **A**lgorithms

IGUANA

(Java)

Test object

**(C code compiled
to a DLL)**

IGUANA
(Java)

inputs

Test object

**(C code compiled
to a DLL)**

IGUANA (Java)

inputs

Test object

(C code compiled
to a DLL)

fitness
computation

information from
test object
instrumentation

IGUANA (Java)

search algorithm

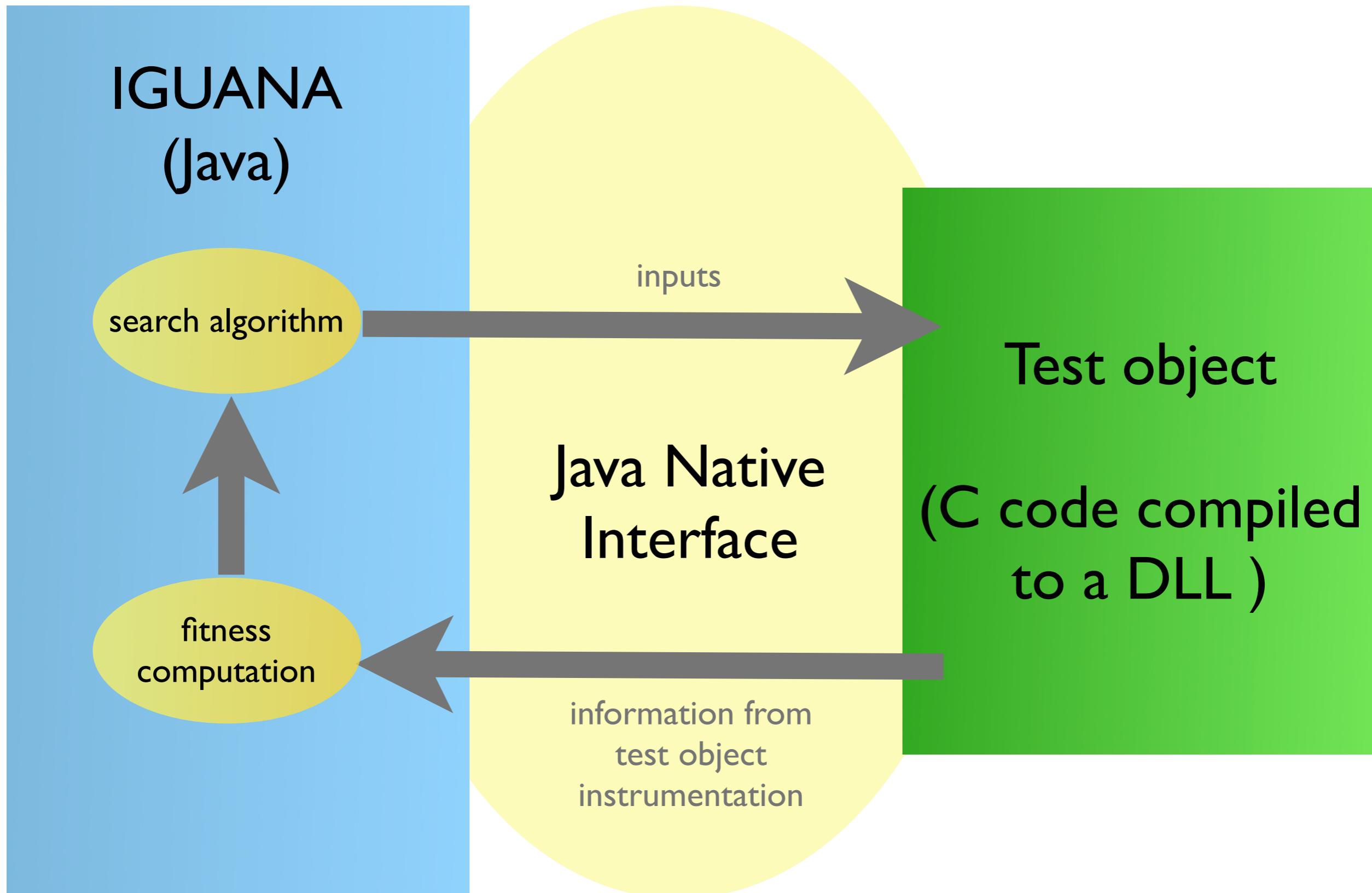
fitness
computation

inputs

Test object

(C code compiled
to a DLL)

information from
test object
instrumentation



A function for testing

```
int test_me(int a, int b, int c)
{
    int flag = 0;

    if (a == b) {
        if (b == c) {
            return 1;
        }
    }

    if (a == 0) {
        flag = 1;
    }

    if (flag && b == 0) {
        return 2;
    }

    return -1;
}
```

Test Object Preparation

I. Parse the code and extract control dependency graph

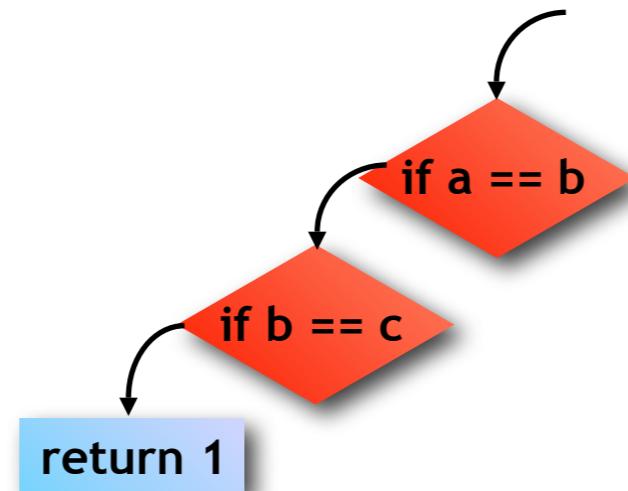
```
int test_me(int a, int b, int c)
{
    int flag = 0;

    if (a == b) {
        if (b == c) {
            return 1;
        }
    }

    if (a == 0) {
        flag = 1;
    }

    if (flag && b == 0) {
        return 2;
    }

    return -1;
}
```



“which decisions are key for the execution of individual structural targets” ?

Test Object Preparation

2. Instrument the code

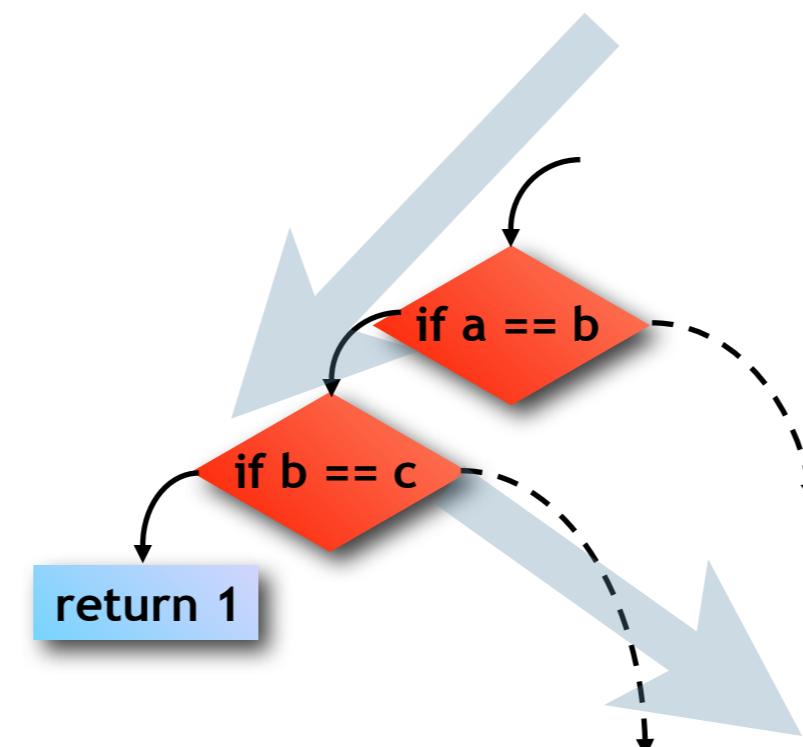
```
int test_me(int a, int b, int c)
{
    int flag = 0;

    if (a == b) {
        if (b == c) {
            return 1;
        }
    }

    if (a == 0) {
        flag = 1;
    }

    if (flag && b == 0) {
        return 2;
    }

    return -1;
}
```



for monitoring control flow
and variable values in
predicates

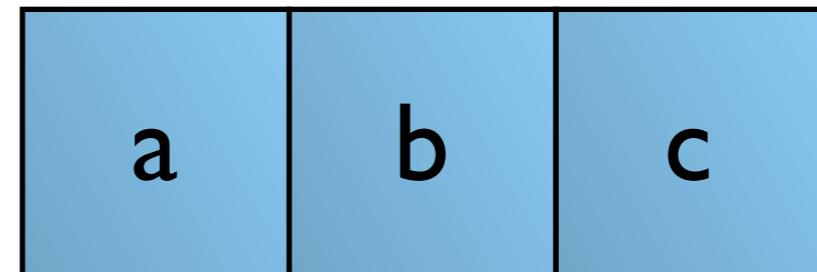
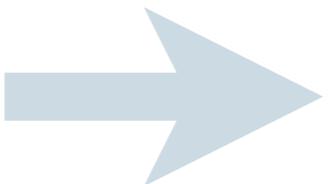
Test Object Preparation

3. Map inputs to a vector

```
int test_me(int a,  
           int b,  
           int c)
```

```
{
```

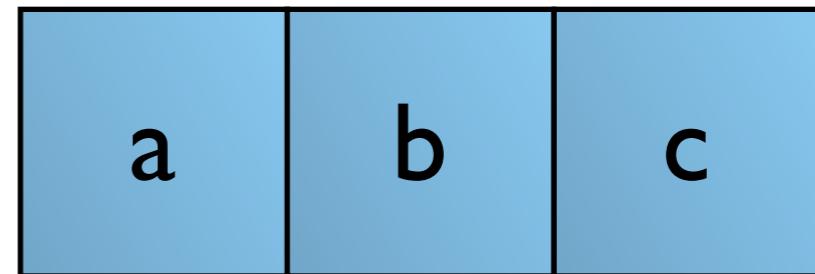
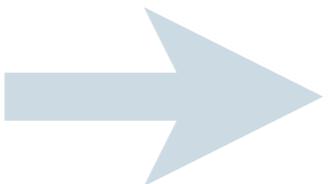
```
    . . .
```



Test Object Preparation

3. Map inputs to a vector

```
int test_me(int a,  
           int b,  
           int c)  
{  
    ...  
}
```

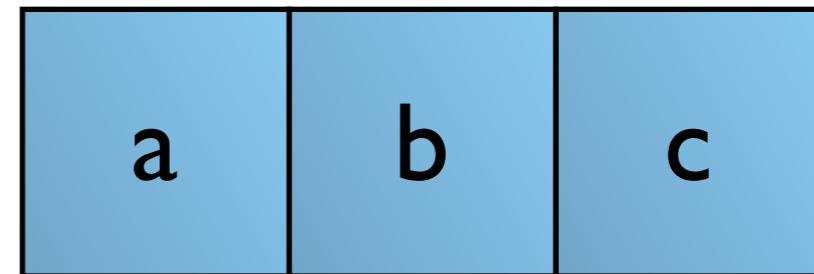
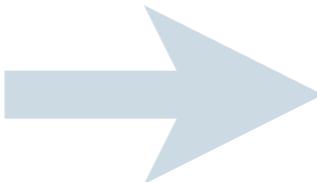


Straightforward in many cases

Test Object Preparation

3. Map inputs to a vector

```
int test_me(int a,  
           int b,  
           int c)  
{  
    ...  
}
```



Straightforward in many cases

Inputs composed of dynamic data structures are harder to compose

Instrumentation

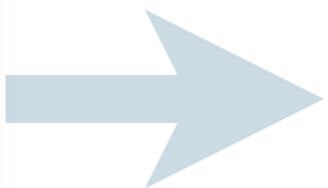
```
int test_me(int a, int b, int c)
{
    int flag = 0;

    if (a == b) {
        if (b == c) {
            return 1;
        }
    }

    if (a == 0) {
        flag = 1;
    }

    if (flag && b == 0) {
        return 2;
    }

    return -1;
}
```



```
int test_me(int a, int b, int c)
{
    int flag = 0;

    if (node(1, equals(0, a, b))) {
        if (node(2, equals(0, b, c))) {
            return 1;
        }
    }

    if (node(4, equals(0, a, 0))) {
        flag = 1;
    }

    if (node(6, is_true(0, flag) && equals(1, b, 0))) {
        return 2;
    }

    return -1;
}
```

Instrumentation

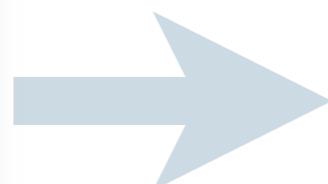
```
int test_me(int a, int b, int c)
{
    int flag = 0;

    if (a == b) {
        if (b == c) {
            return 1;
        }
    }

    if (a == 0) {
        flag = 1;
    }

    if (flag && b == 0) {
        return 2;
    }

    return -1;
}
```



```
int test_me(int a, int b, int c)
{
    int flag = 0;

    if (node(1, equals(0, a, b))) {
        if (node(2, equals(0, b, c))) {
            return 1;
        }
    }

    if (node(4, equals(0, a, 0))) {
        flag = 1;
    }

    if (node(6, is_true(0, flag) && equals(1, b, 0))) {
        return 2;
    }

    return -1;
}
```

Each branching condition is replaced by a call to the function node(...)

```
int test_me(int a, int b, int c)
{
    int flag = 0;

    if (node(1, equals(0, a, b))) {
        if (node(2, equals(0, b, c))) {
            return 1;
        }
    }

    if (node(4, equals(0, a, 0))) {
        flag = 1;
    }

    if (node(6, is_true(0, flag) && equals(1, b, 0))) {
        return 2;
    }

    return -1;
}
```

the instrumentation should only observe the program and not alter its behaviour

The first parameter is
the control flow
graph node ID of the
decision statement

```
int test_me(int a, int b, int c)
{
    int flag = 0;

    if (node(1, equals(0, a, b))) {
        if (node(2, equals(0, b, c))) {
            return 1;
        }
    }

    if (node(4, equals(0, a, 0))) {
        flag = 1;
    }

    if (node(6, is_true(0, flag) && equals(1, b, 0))) {
        return 2;
    }

    return -1;
}
```

The second parameter is a boolean condition that
replicates the structure in the original program
(i.e. including short-circuiting)

```
int test_me(int a, int b, int c)
{
    int flag = 0;

    if (node(1, equals(0, a, b))) {
        if (node(2, equals(0, b, c))) {
            return 1;
        }
    }

    if (node(4, equals(0, a, 0))) {
        flag = 1;
    }

    if (node(6, is_true(0, flag) && equals(1, b, 0))) {
        return 2;
    }

    return -1;
}
```

Relational predicates are replaced with functions that compute branch distance.

The instrumentation tells us:

Which decision nodes were executed

and their outcome (branch distances)

Therefore we can find which decision control flow diverged from a target for an input....

... and compute the approach level
from the control dependence graph

... and lookup the branch distance



Input: <20, 20, 30>

```
int test_me(int a, int b, int c)
{
    int flag = 0;

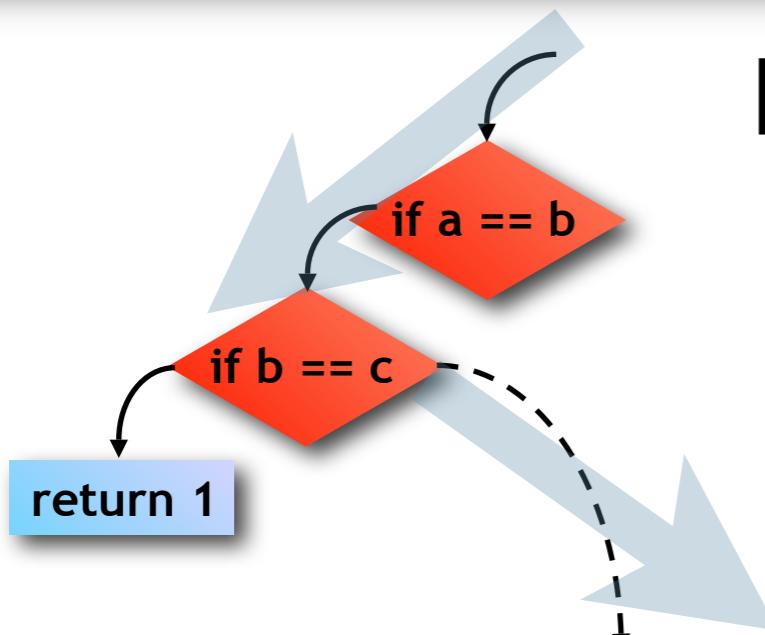
    if (node(1, equals(0, a, b))) {
        if (node(2, equals(0, b, c))) {
            return 1;
        }
    }

    if (node(4, equals(0, a, 0))) {
        flag = 1;
    }

    if (node(6, is_true(0, flag) && equals(1, b, 0))) {
        return 2;
    }

    return -1;
}
```

NODE	T	F
1	0	1
2	10	0
4	20	0
....		



Diverged at node 2

approach level: 0

branch distance: 10

fitness = 0.009945219