

## SBML Model Report

**Model name:**  
**“Overgaard2007\_PDmodel\_IL21”**



May 5, 2016

### 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by the following three authors: Catherine Lloyd<sup>1</sup>, Vijayalakshmi Chelliah<sup>2</sup> and Rune Viig Overgaard<sup>3</sup> at November twelveth 2009 at 2:29 p. m. and last time modified at February 24<sup>th</sup> 2015 at 8:28 p. m. Table 1 gives an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	0
events	0	constraints	0
reactions	0	function definitions	0
global parameters	56	unit definitions	0
rules	27	initial assignments	0

### Model Notes

This a model from the article:

**PKPD model of interleukin-21 effects on thermoregulation in monkeys–application and evaluation of stochastic differential equations.**

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Overgaard RV, Holford N, Rytved KA, Madsen H. Pharm Res. 2007 Feb;24(2):298-309. [PUBMED](#),

**Abstract:**

**PURPOSE:** To describe the pharmacodynamic effects of recombinant human interleukin-21 (IL-21) on core body temperature in cynomolgus monkeys using basic mechanisms of heat regulation. A major effort was devoted to compare the use of ordinary differential equations (ODEs) with stochastic differential equations (SDEs) in pharmacokinetic pharmacodynamic (PKPD) modelling. **METHODS:** A temperature model was formulated including circadian rhythm, metabolism, heat loss, and a thermoregulatory set-point. This model was formulated as a mixed-effects model based on SDEs using NONMEM. **RESULTS:** The effects of IL-21 were on the set-point and the circadian rhythm of metabolism. The model was able to describe a complex set of IL-21 induced phenomena, including 1) disappearance of the circadian rhythm, 2) no effect after first dose, and 3) high variability after second dose. SDEs provided a more realistic description with improved simulation properties, and further changed the model into one that could not be falsified by the autocorrelation function. **CONCLUSIONS:** The IL-21 induced effects on thermoregulation in cynomolgus monkeys are explained by a biologically plausible model. The quality of the model was improved by the use of SDEs.

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## 2 Unit Definitions

This is an overview of five unit definitions which are all predefined by SBML and not mentioned in the model.

### 2.1 Unit substance

**Notes** Mole is the predefined SBML unit for substance.

**Definition** mol

### 2.2 Unit volume

**Notes** Litre is the predefined SBML unit for volume.

**Definition** l

### 2.3 Unit area

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition**  $\text{m}^2$

## 2.4 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

## 2.5 Unit time

**Notes** Second is the predefined SBML unit for time.

**Definition** s

# 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
COMpartment			3	1	litre	<input checked="" type="checkbox"/>	

## 3.1 Compartment COMpartment

This is a three dimensional compartment with a constant size of one litre.

# 4 Parameters

This model contains 56 global parameters.

Table 3: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
M	Metabolic rate		3.500		<input type="checkbox"/>
T	Temperature		38.785		<input type="checkbox"/>
BR	Bound Receptor		0.000		<input type="checkbox"/>
E_slow	Slow Effect		0.000		<input type="checkbox"/>
E_fast	Fast Effect		0.000		<input type="checkbox"/>
f_prime	Priming		0.000		<input type="checkbox"/>
T_a	ambient temperature		21.000		<input checked="" type="checkbox"/>

Id	Name	SBO	Value	Unit	Constant
T_b	baseline temperature		38.000		<input checked="" type="checkbox"/>
delta_T	temperature difference		1.570		<input checked="" type="checkbox"/>
kinc	kinc		0.026		<input checked="" type="checkbox"/>
tdose1	tdose1		24.000		<input checked="" type="checkbox"/>
tdose2	tdose2		72.000		<input checked="" type="checkbox"/>
tdose3	tdose3		120.000		<input checked="" type="checkbox"/>
M_c	circadian rhythm		0.000		<input type="checkbox"/>
t_day	t_day		17.500		<input checked="" type="checkbox"/>
t_night	t_night		6.730		<input checked="" type="checkbox"/>
tprime	tprime		0.000		<input type="checkbox"/>
day_length	day_length		86400.000		<input checked="" type="checkbox"/>
km	rate constant Metabolism		1.138		<input checked="" type="checkbox"/>
c	specific heat constant		3.470		<input checked="" type="checkbox"/>
k	heat conductance		0.000		<input type="checkbox"/>
pEtot	pEtot		0.144		<input checked="" type="checkbox"/>
kR	kR		5.350		<input checked="" type="checkbox"/>
AMT_dose	AMT_dose		3.000		<input checked="" type="checkbox"/>
pEf1	pEf1		1.000		<input checked="" type="checkbox"/>
pEs1	pEs1		0.200		<input checked="" type="checkbox"/>
pEf2	pEf2		3.570		<input checked="" type="checkbox"/>
pEs2	pEs2		2.430		<input checked="" type="checkbox"/>
pEf3	pEf3		8.000		<input checked="" type="checkbox"/>
pEs3	pEs3		50.000		<input checked="" type="checkbox"/>
f2_drug	f2_drug		0.000		<input type="checkbox"/>
T_day	T_day		0.000		<input type="checkbox"/>
T_night	T_night		0.000		<input type="checkbox"/>
kb	heat conductance baselinevalue		0.000		<input type="checkbox"/>
M_b	M_b		3.000		<input checked="" type="checkbox"/>
M_day	M_day		0.000		<input type="checkbox"/>
M_night	M_night		0.000		<input type="checkbox"/>
t_prime	t_prime		45.120		<input checked="" type="checkbox"/>
alpha	alpha		0.223		<input checked="" type="checkbox"/>
delta_high-dose	delta_high_dose		1.000		<input checked="" type="checkbox"/>
M_night-baseline	M_night_baseline		0.000		<input type="checkbox"/>
gNsTs1	gNsTs1		0.000		<input type="checkbox"/>

Id	Name	SBO	Value	Unit	Constant
gNsTs2	gNsTs2		0.000		<input type="checkbox"/>
gNsTs3	gNsTs3		0.000		<input type="checkbox"/>
gNfTf1	gNfTf1		0.000		<input type="checkbox"/>
gNfTf2	gNfTf2		0.000		<input type="checkbox"/>
gNfTf3	gNfTf3		0.000		<input type="checkbox"/>
Ns	No. of transit com- partment (slow)		4.000		<input checked="" type="checkbox"/>
Nf	No. of transit com- partment (fast)		4.000		<input checked="" type="checkbox"/>
Ts	mean total delay (slow)		2.450		<input checked="" type="checkbox"/>
Tf	mena total delay (fast)		0.368		<input checked="" type="checkbox"/>
X1	X1		0.000		<input type="checkbox"/>
X2	X2		0.000		<input type="checkbox"/>
X3	X3		0.000		<input type="checkbox"/>
Kf	Kf		0.000		<input type="checkbox"/>
Ks	Ks		0.000		<input type="checkbox"/>

## 5 Rules

This is an overview of 27 rules.

### 5.1 Rule M

Rule M is a rate rule for parameter M:

$$\frac{d}{dt}M = km \cdot (M - M_c) \quad (1)$$

### 5.2 Rule T

Rule T is a rate rule for parameter T:

$$\frac{d}{dt}T = c^{-1} \cdot (M - k \cdot (T - T_a)) \quad (2)$$

### 5.3 Rule BR

Rule BR is a rate rule for parameter BR:

$$\frac{d}{dt}BR = f_{\text{prime}} \cdot (E_{\text{slow}} + E_{\text{fast}}) \cdot (1 - BR) - kR \cdot BR \quad (3)$$

#### 5.4 Rule `tprime`

Rule `tprime` is an assignment rule for parameter `tprime`:

$$tprime = time \cdot 3600 \cdot 1 - \left\lfloor \frac{time \cdot 3600 \cdot 1}{day\_length} \right\rfloor \cdot day\_length \quad (4)$$

#### 5.5 Rule `kb`

Rule `kb` is an assignment rule for parameter `kb`:

$$kb = \frac{M\_b}{T\_b - T\_a} \quad (5)$$

#### 5.6 Rule `T_day`

Rule `T_day` is an assignment rule for parameter `T_day`:

$$T\_day = T\_b + \frac{\delta T}{2} \quad (6)$$

#### 5.7 Rule `M_day`

Rule `M_day` is an assignment rule for parameter `M_day`:

$$M\_day = (kb + kinc \cdot (T\_day - T\_b)) \cdot (T\_day - T\_a) \quad (7)$$

#### 5.8 Rule `f_prime`

Rule `f_prime` is an assignment rule for parameter `f_prime`:

$$f\_prime = \delta high\_dose \cdot (1 + \exp(\alpha \cdot (time - (tdose1 + t\_prime))))^{-1} \quad (8)$$

#### 5.9 Rule `T_night`

Rule `T_night` is an assignment rule for parameter `T_night`:

$$T\_night = T\_b - \frac{\delta T}{2} \quad (9)$$

#### 5.10 Rule `M_night_baseline`

Rule `M_night_baseline` is an assignment rule for parameter `M_night_baseline`:

$$M\_night\_baseline = (kb + kinc \cdot (T\_night - T\_b)) \cdot (T\_night - T\_a) \quad (10)$$

#### 5.11 Rule `M_night`

Rule `M_night` is an assignment rule for parameter `M_night`:

$$M\_night = (1 - f\_prime) \cdot M\_night\_baseline + f\_prime \cdot M\_day \quad (11)$$

### 5.12 Rule $M_c$

Rule  $M_c$  is an assignment rule for parameter  $M_c$ :

$$M_c = \begin{cases} M_{\text{night}} & \text{if } \left( \frac{t_{\text{prime}}}{3600} \geq t_{\text{night}} \right) \wedge \left( \frac{t_{\text{prime}}}{3600} < t_{\text{day}} \right) \\ M_{\text{day}} & \text{otherwise} \end{cases} \quad (12)$$

### 5.13 Rule $f2\_drug$

Rule  $f2\_drug$  is an assignment rule for parameter  $f2\_drug$ :

$$f2\_drug = 0 \quad (13)$$

### 5.14 Rule $k$

Rule  $k$  is an assignment rule for parameter  $k$ :

$$k = k_b + k_{inc} \cdot (T - T_b \cdot (1 + p_{Etot} \cdot BR)) + f2\_drug \quad (14)$$

### 5.15 Rule $X1$

Rule  $X1$  is an assignment rule for parameter  $X1$ :

$$X1 = \frac{\text{time} - \text{tdose1}}{24} \quad (15)$$

### 5.16 Rule $X2$

Rule  $X2$  is an assignment rule for parameter  $X2$ :

$$X2 = \frac{\text{time} - \text{tdose2}}{24} \quad (16)$$

### 5.17 Rule $X3$

Rule  $X3$  is an assignment rule for parameter  $X3$ :

$$X3 = \frac{\text{time} - \text{tdose3}}{24} \quad (17)$$

### 5.18 Rule $K_f$

Rule  $K_f$  is an assignment rule for parameter  $K_f$ :

$$K_f = \frac{N_f}{T_f} \quad (18)$$

### 5.19 Rule $K_s$

Rule  $K_s$  is an assignment rule for parameter  $K_s$ :

$$K_s = \frac{N_s}{T_s} \quad (19)$$

### 5.20 Rule $g_{N_s T_s 1}$

Rule  $g_{N_s T_s 1}$  is an assignment rule for parameter  $g_{N_s T_s 1}$ :

$$g_{N_s T_s 1} = \begin{cases} \frac{K_s^{N_s}}{6} \cdot \exp(K_s \cdot X_1) \cdot X_1^{N_s-1} & \text{if } X_1 > 0 \\ 0 & \text{otherwise} \end{cases} \quad (20)$$

### 5.21 Rule $g_{N_s T_s 2}$

Rule  $g_{N_s T_s 2}$  is an assignment rule for parameter  $g_{N_s T_s 2}$ :

$$g_{N_s T_s 2} = \begin{cases} \frac{K_s^{N_s}}{6} \cdot \exp(K_s \cdot X_2) \cdot X_2^{N_s-1} & \text{if } X_2 > 0 \\ 0 & \text{otherwise} \end{cases} \quad (21)$$

### 5.22 Rule $g_{N_s T_s 3}$

Rule  $g_{N_s T_s 3}$  is an assignment rule for parameter  $g_{N_s T_s 3}$ :

$$g_{N_s T_s 3} = \begin{cases} \frac{K_s^{N_s}}{6} \cdot \exp(K_s \cdot X_3) \cdot X_3^{N_s-1} & \text{if } X_3 > 0 \\ 0 & \text{otherwise} \end{cases} \quad (22)$$

### 5.23 Rule $g_{N_f T_f 1}$

Rule  $g_{N_f T_f 1}$  is an assignment rule for parameter  $g_{N_f T_f 1}$ :

$$g_{N_f T_f 1} = \begin{cases} \frac{K_f^{N_f}}{6} \cdot \exp(K_f \cdot X_1) \cdot X_1^{N_f-1} & \text{if } X_1 > 0 \\ 0 & \text{otherwise} \end{cases} \quad (23)$$

### 5.24 Rule $g_{N_f T_f 2}$

Rule  $g_{N_f T_f 2}$  is an assignment rule for parameter  $g_{N_f T_f 2}$ :

$$g_{N_f T_f 2} = \begin{cases} \frac{K_f^{N_f}}{6} \cdot \exp(K_f \cdot X_2) \cdot X_2^{N_f-1} & \text{if } X_2 > 0 \\ 0 & \text{otherwise} \end{cases} \quad (24)$$



### 5.25 Rule $\text{gNfTf3}$

Rule  $\text{gNfTf3}$  is an assignment rule for parameter  $\text{gNfTf3}$ :

$$\text{gNfTf3} = \begin{cases} \frac{\text{Kf}^{\text{Nf}}}{6} \cdot \exp(\text{Kf} \cdot \text{X3}) \cdot \text{X3}^{\text{Nf}-1} & \text{if } \text{X3} > 0 \\ 0 & \text{otherwise} \end{cases} \quad (25)$$

### 5.26 Rule $\text{E\_slow}$

Rule  $\text{E\_slow}$  is an assignment rule for parameter  $\text{E\_slow}$ :

$$\text{E\_slow} = \text{AMT\_dose} \cdot \text{pEs2} \cdot (\text{gNsTs1} + \text{gNsTs2} + \text{gNsTs3}) \quad (26)$$

### 5.27 Rule $\text{E\_fast}$

Rule  $\text{E\_fast}$  is an assignment rule for parameter  $\text{E\_fast}$ :

$$\text{E\_fast} = \text{pEf2} \cdot (\text{gNfTf1} + \text{gNfTf2} + \text{gNfTf3}) \quad (27)$$

SBML<sup>2</sup>LaTeX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

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