

SBML Model Report

Model name: “Barr2017 - Dynamics of p21 in hTert-RPE1 cells”



May 17, 2018

1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by the following two authors: Frank Stefan Heldt¹ and Emma Louise Fairbanks² at June ninth 2016 at 5:37 p. m. and last time modified at December sixth 2017 at 4:28 p. m. Table 1 gives an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	20
events	0	constraints	0
reactions	35	function definitions	14
global parameters	31	unit definitions	3
rules	3	initial assignments	0

Model Notes

Barr2017 - Dynamics of p21 in hTert-RPE1cellsThis deterministic model reveals that a bistable switch created by Cdt2, promotes irreversible S-phase entry by keeping p21 levels low, prevents premature S-phase exit upon DNA damage

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This model is described in the article: [DNA damage during S-phase mediates the proliferation-quiescence decision in the subsequent G1 via p21 expression](#). Barr AR, Cooper S, Heldt FS, Butera F, Stoy H, Mansfeld J, Novk B, Bakal C. Nat Commun 2017 Mar; 8: 14728

Abstract:

Following DNA damage caused by exogenous sources, such as ionizing radiation, the tumour suppressor p53 mediates cell cycle arrest via expression of the CDK inhibitor, p21. However, the role of p21 in maintaining genomic stability in the absence of exogenous DNA-damaging agents is unclear. Here, using live single-cell measurements of p21 protein in proliferating cultures, we show that naturally occurring DNA damage incurred over S-phase causes p53-dependent accumulation of p21 during mother G2- and daughter G1-phases. High p21 levels mediate G1 arrest via CDK inhibition, yet lower levels have no impact on G1 progression, and the ubiquitin ligases CRL4Cdt2 and SCFSkp2 couple to degrade p21 prior to the G1/S transition. Mathematical modelling reveals that a bistable switch, created by CRL4Cdt2, promotes irreversible S-phase entry by keeping p21 levels low, preventing premature S-phase exit upon DNA damage. Thus, we characterize how p21 regulates the proliferation-quiescence decision to maintain genomic stability.

This model is hosted on [BioModels Database](#) and identified by: [BIOMD0000000660](#).

To cite BioModels Database, please use: [Chelliah V et al. BioModels: ten-year anniversary. Nucl. Acids Res. 2015, 43\(Database issue\):D542-8.](#)

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2 Unit Definitions

This is an overview of five unit definitions of which two are predefined by SBML and not mentioned in the model.

2.1 Unit volume

Name volume

Definition ml

2.2 Unit time

Name time

Definition 60 s

2.3 Unit substance

Name substance

Definition mmol

2.4 Unit area

Notes Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

Definition m^2

2.5 Unit length

Notes Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

Definition m

3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
Cell	Cell		3	1	litre	<input checked="" type="checkbox"/>	

3.1 Compartment Cell

This is a three dimensional compartment with a constant size of one ml.

Name Cell

4 Species

This model contains 20 species. The boundary condition of five of these species is set to true so that these species' amount cannot be changed by any reaction. Section 9 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condition
MrnaP21	MrnaP21	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
MrnaCy	MrnaCy	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
MrnaP53	MrnaP53	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
P21	P21	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
Cy	Cy	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
CyP21	CyP21	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
aPcna	aPcna	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
Rc	Rc	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
pRc	pRc	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
aRc	aRc	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
iRc	iRc	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
Dna	Dna	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
Dam	Dam	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
P53	P53	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
Skp2	Skp2	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>
Cdt2	Cdt2	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>
iPcna	iPcna	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
tP21	tP21	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input checked="" type="checkbox"/>
tCy	tCy	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input checked="" type="checkbox"/>
tPcna	tPcna	Cell	$\text{mmol} \cdot \text{ml}^{-1}$	<input type="checkbox"/>	<input checked="" type="checkbox"/>

5 Parameters

This model contains 31 global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
kSyMrna	kSyMrna		0.020		✓
kSyMrnaP53	kSyMrnaP53		0.080		✓
kDeMrna	kDeMrna		0.020		✓
kSyP21	kSyP21		0.002		✓
kDeP21	kDeP21		0.003		✓
kDeP21Cy	kDeP21Cy		0.007		✓
kDeP21aRc	kDeP21aRc		1.000		✓
kSyCy	kSyCy		0.005		✓
kAsCyP21	kAsCyP21		1.000		✓
kDsCyP21	kDsCyP21		0.050		✓
kDeCy	kDeCy		0.002		✓
kDeCyCy	kDeCyCy		$2 \cdot 10^{-4}$		✓
kImPc	kImPc		0.003		✓
kExPc	kExPc		0.006		✓
kPhRc	kPhRc		0.100		✓
kDpRc	kDpRc		0.010		✓
jCy	jCy		1.800		✓
n	n		6.000		✓
kAsRcPc	kAsRcPc		0.010		✓
kDsRcPc	kDsRcPc		0.001		✓
kAsPcP21	kAsPcP21		100.000		✓
kDsPcP21	kDsPcP21		0.010		✓
kSyDna	kSyDna		0.007		✓
kSyP53	kSyP53		0.050		✓
kDeP53	kDeP53		0.050		✓
jP53	jP53		0.010		✓
kGeDam	kGeDam		0.001		✓
kGeDamArc	kGeDamArc		0.005		✓
kReDam	kReDam		0.001		✓
kReDamP53	kReDamP53		0.005		✓
jDam	jDam		0.500		✓

6 Function definitions

This is an overview of 14 function definitions.

6.1 Function definition `Constant_flux_irreversible`

Name Constant flux (irreversible)

Argument v

Mathematical Expression

$$v \quad (1)$$

6.2 Function definition `rDsRc`

Name Function for Dissassembly of RC

Arguments $[Dna]$, $[Rc]$

Mathematical Expression

$$\begin{cases} 0 & \text{if } [Dna] < 1 \\ \begin{cases} 1 \cdot [Rc] & \text{if } [Dna] > 1 \\ 0.5 \cdot [Rc] & \text{otherwise} \end{cases} & \text{otherwise} \end{cases} \quad (2)$$

6.3 Function definition `rDeP21_1`

Name Function for Degradation of p21

Arguments $[Cdt2]$, $[Cy]$, $[P21]$, $[Skp2]$, $[aRc]$, $kDeP21$, $kDeP21Cy$, $kDeP21aRc$

Mathematical Expression

$$(kDeP21 + kDeP21Cy \cdot [Skp2] \cdot [Cy] + kDeP21aRc \cdot [Cdt2] \cdot [aRc]) \cdot [P21] \quad (3)$$

6.4 Function definition `rDeCy_1`

Name Function for Degradation of cyclins

Arguments $[Cy]$, $[Skp2]$, $kDeCy$, $kDeCyCy$

Mathematical Expression

$$(kDeCy + kDeCyCy \cdot [Skp2] \cdot [Cy]) \cdot [Cy] \quad (4)$$

6.5 Function definition `rDeCy_2`

Name Function for Degradation of cyclin in CDK2:Cyclin:p21 complexes

Arguments $[Cy]$, $[CyP21]$, $[Skp2]$, $kDeCy$, $kDeCyCy$

Mathematical Expression

$$(kDeCy + kDeCyCy \cdot [Skp2] \cdot [Cy]) \cdot [CyP21] \quad (5)$$

6.6 Function definition $rDeP21_2$

Name Function for Degradation of p21 in CDK2:Cyclin:p21 complexes

Arguments [Cdt2], [Cy], [CyP21], [Skp2], [aRc], kDeP21, kDeP21Cy, kDeP21aRc

Mathematical Expression

$$(kDeP21 + kDeP21Cy \cdot [Skp2] \cdot [Cy] + kDeP21aRc \cdot [Cdt2] \cdot [aRc]) \cdot [CyP21] \quad (6)$$

6.7 Function definition $rDeP21_3$

Name Function for Degradation of p21 in PCNA:p21 complexes

Arguments [Cdt2], [Cy], [Skp2], [aRc], [iPcna], kDeP21, kDeP21Cy, kDeP21aRc

Mathematical Expression

$$(kDeP21 + kDeP21Cy \cdot [Skp2] \cdot [Cy] + kDeP21aRc \cdot [Cdt2] \cdot [aRc]) \cdot [iPcna] \quad (7)$$

6.8 Function definition $rPhRc_1$

Name Function for Phosphorylation/priming of replication complexes

Arguments [Cy], [Rc], jCy, kPhRc, n

Mathematical Expression

$$\frac{kPhRc \cdot [Cy]^n}{jCy^n + [Cy]^n} \cdot [Rc] \quad (8)$$

6.9 Function definition $rDeP21_4$

Name Function for Degradation of p21 in inactive replication complexes

Arguments [Cdt2], [Cy], [Skp2], [aRc], [iRc], kDeP21, kDeP21Cy, kDeP21aRc

Mathematical Expression

$$(kDeP21 + kDeP21Cy \cdot [Skp2] \cdot [Cy] + kDeP21aRc \cdot [Cdt2] \cdot [aRc]) \cdot [iRc] \quad (9)$$

6.10 Function definition $rDsRc_1$

Name Function for Dissassembly of pRC

Arguments [Dna], [pRc]

Mathematical Expression

$$\begin{cases} 0 & \text{if } [Dna] < 1 \\ \begin{cases} 1 \cdot [pRc] & \text{if } [Dna] > 1 \\ 0.5 \cdot [pRc] & \text{otherwise} \end{cases} & \text{otherwise} \end{cases} \quad (10)$$

6.11 Function definition r_{DsRc_2}

Name Function for Dissassembly of aRC

Arguments [Dna], [aRc]

Mathematical Expression

$$\begin{cases} 0 & \text{if [Dna] < 1} \\ \begin{cases} 1 \cdot [aRc] & \text{if [Dna] > 1} \\ 0.5 \cdot [aRc] & \text{otherwise} \end{cases} & \text{otherwise} \end{cases} \quad (11)$$

6.12 Function definition r_{DsRc_3}

Name Function for Dissassembly of iRC

Arguments [Dna], [iRc]

Mathematical Expression

$$\begin{cases} 0 & \text{if [Dna] < 1} \\ \begin{cases} 1 \cdot [iRc] & \text{if [Dna] > 1} \\ 0.5 \cdot [iRc] & \text{otherwise} \end{cases} & \text{otherwise} \end{cases} \quad (12)$$

6.13 Function definition r_{DeP53_1}

Name Function for Degradation of p53

Arguments [Dam], [P53], jP53, kDeP53

Mathematical Expression

$$\frac{kDeP53}{jP53 + [Dam]} \cdot [P53] \quad (13)$$

6.14 Function definition r_{ReDam_1}

Name Function for Repair of DNA damage

Arguments [Dam], [P53], jDam, kReDam, kReDamP53

Mathematical Expression

$$\left(kReDam + \frac{kReDamP53 \cdot [P53]}{jDam + [Dam]} \right) \cdot [Dam] \quad (14)$$

7 Rules

This is an overview of three rules.

7.1 Rule t_{P21}

Rule t_{P21} is an assignment rule for species t_{P21} :

$$t_{P21} = [P21] + [CyP21] + [iPcna] + [iRc] \quad (15)$$

Derived unit $\text{mmol} \cdot \text{ml}^{-1}$

7.2 Rule t_{Cy}

Rule t_{Cy} is an assignment rule for species t_{Cy} :

$$t_{Cy} = [Cy] + [CyP21] \quad (16)$$

Derived unit $\text{mmol} \cdot \text{ml}^{-1}$

7.3 Rule t_{Pcna}

Rule t_{Pcna} is an assignment rule for species t_{Pcna} :

$$t_{Pcna} = [aPcna] + [iPcna] + [aRc] + [iRc] \quad (17)$$

Derived unit $\text{mmol} \cdot \text{ml}^{-1}$

8 Reactions

This model contains 35 reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	Synthesis_of-_p21_mRNAs	Synthesis of p21 mRNAs	$\emptyset \longrightarrow \text{MrnaP21}$	
2	Synthesis_of-_p21_mRNAs_by-_p53	Synthesis of p21 mRNAs by p53	$\text{P53} \longrightarrow \text{MrnaP21} + \text{P53}$	
3	Synthesis_of-_cyclin_mRNAs	Synthesis of cyclin mRNAs	$\emptyset \longrightarrow \text{MrnaCy}$	
4	Synthesis_of-_p53_mRNAs	Synthesis of p53 mRNAs	$\emptyset \longrightarrow \text{MrnaP53}$	
5	Degradation_of-_p21_mRNAs	Degradation of p21 mRNAs	$\text{MrnaP21} \longrightarrow \emptyset$	
6	Degradation_of-_cyclin_mRNAs	Degradation of cyclin mRNAs	$\text{MrnaCy} \longrightarrow \emptyset$	
7	Degradation_of-_p53_mRNAs	Degradation of p53 mRNAs	$\text{MrnaP53} \longrightarrow \emptyset$	
8	Synthesis_of-_p21	Synthesis of p21	$\text{MrnaP21} \longrightarrow \text{MrnaP21} + \text{P21}$	
9	Degradation_of-_p21	Degradation of p21	$\text{P21} \xrightarrow{\text{Skp2, Cy, Cdt2, aRc}} \emptyset$	
10	Synthesis_of-_cyclins	Synthesis of cyclins	$\text{MrnaCy} \longrightarrow \text{MrnaCy} + \text{Cy}$	

Nº	Id	Name	Reaction Equation	SBO
11	Degradation_of-_cyclins	Degradation of cyclins	$\text{Cy} \xrightarrow{\text{Skp2, Cy}} \emptyset$	
12	Association-_and-_dissociation-_of_CDK2-_Cyclin_and_p21	Association and dissociation of CDK2:Cyclin and p21	$\text{Cy} + \text{P21} \rightleftharpoons \text{CyP21}$	
13	Degradation-_of_cyclin_in-_CDK2_Cyclin-_p21_complexes	Degradation of cyclin in CDK2:Cyclin:p21 complexes	$\text{CyP21} \xrightarrow{\text{Skp2, Cy}} \text{P21}$	
14	Degradation_of-_p21_in_CDK2-_Cyclin_p21-_complexes	Degradation of p21 in CDK2:Cyclin:p21 complexes	$\text{CyP21} \xrightarrow{\text{Skp2, Cy, Cdt2, aRc}} \text{Cy}$	
15	Import_of-_active_PCNA	Import of active PCNA	$\emptyset \longrightarrow \text{aPcna}$	
16	Export_of-_active_PCNA	Export of active PCNA	$\text{aPcna} \longrightarrow \emptyset$	
17	Export_of-_inactive_PCNA	Export of inactive PCNA	$\text{iPcna} \longrightarrow \text{P21}$	
18	Association-_and-_dissociation-_of_PCNA_and_p21	Association and dissociation of PCNA and p21	$\text{aPcna} + \text{P21} \rightleftharpoons \text{iPcna}$	

Nº	Id	Name	Reaction Equation	SBO
19	Degradation_of- _p21_in_PCNA- _p21_complexes	Degradation of p21 in PCNA:p21 complexes	$iPcna \xrightarrow{Skp2, Cy, Cdt2, aRc} aPcna$	
20	Phosphorylation- _priming_of- _replication- _complexes	Phosphorylation/priming of replication complexes	$Rc \xrightarrow{Cy} pRc$	
21	Dephosphorylation- _of- _replication- _complexes	Dephosphorylation of replication complexes	$pRc \longrightarrow Rc$	
22	Association- _and- _dissociation- _of_active- _PCNA_and- _replication- _complexes	Association and dissociation of active PCNA and replication complexes	$aPcna + pRc \rightleftharpoons aRc$	
23	Association- _and- _dissociation- _of_inactive- _PCNA_and- _replication- _complexes	Association and dissociation of inactive PCNA and replication complexes	$iPcna + pRc \rightleftharpoons iRc$	

Nº	Id	Name	Reaction Equation	SBO
24	Association- and- dissociation- of_p21_and- replication- complexes	Association and dissociation of p21 and replication complexes	$aRc + P21 \rightleftharpoons iRc$	
25	Degradation- of_p21_in- inactive- replication- complexes	Degradation of p21 in inactive replication complexes	$iRc \xrightarrow{Skp2, Cy, Cdt2, aRc} aRc$	
26	Synthesis_of- DNA	Synthesis of DNA	$aRc \longrightarrow aRc + Dna$	
27	Dissassembly- of_RC	Dissassembly of RC	$Rc \xrightarrow{Dna} \emptyset$	
28	Dissassembly- of_pRC	Dissassembly of pRC	$pRc \xrightarrow{Dna} \emptyset$	
29	Dissassembly- of_aRC	Dissassembly of aRC	$aRc \xrightarrow{Dna} aPcna$	
30	Dissassembly- of_iRC	Dissassembly of iRC	$iRc \xrightarrow{Dna} iPcna$	
31	Synthesis_of- p53	Synthesis of p53	$MrnaP53 \longrightarrow MrnaP53 + P53$	
32	Degradation_of- p53	Degradation of p53	$P53 \xrightarrow{Dam} \emptyset$	
33	Induction_of- DNA_damage	Induction of DNA damage	$\emptyset \longrightarrow Dam$	

Nº	Id	Name	Reaction Equation	SBO
34	Induction_of- _DNA_damage_by- _replication	Induction of DNA damage by replication	$aRc \longrightarrow aRc + Dam$	
35	Repair_of_DNA- _damage	Repair of DNA damage	$Dam \xrightarrow{P53} \emptyset$	

8.1 Reaction `Synthesis_of_p21_mRNAs`

This is an irreversible reaction of no reactant forming one product.

Name Synthesis of p21 mRNAs

Reaction equation



Product

Table 6: Properties of each product.

Id	Name	SBO
MrnaP21	MrnaP21	

Kinetic Law

Derived unit contains undeclared units

$$v_1 = \text{vol}(\text{Cell}) \cdot \text{Constant_flux_irreversible}(\text{kSyMrna}) \quad (19)$$

$$\text{Constant_flux_irreversible}(v) = v \quad (20)$$

$$\text{Constant_flux_irreversible}(v) = v \quad (21)$$

8.2 Reaction `Synthesis_of_p21_mRNAs_by_p53`

This is an irreversible reaction of one reactant forming two products.

Name Synthesis of p21 mRNAs by p53

Reaction equation



Reactant

Table 7: Properties of each reactant.

Id	Name	SBO
P53	P53	

Products

Table 8: Properties of each product.

Id	Name	SBO
MrnaP21	MrnaP21	
P53	P53	

Kinetic Law

Derived unit contains undeclared units

$$v_2 = \text{vol}(\text{Cell}) \cdot k_{\text{SyMrnaP53}} \cdot [\text{P53}] \quad (23)$$

8.3 Reaction `Synthesis_of_cyclin_mRNAs`

This is an irreversible reaction of no reactant forming one product.

Name Synthesis of cyclin mRNAs

Reaction equation



Product

Table 9: Properties of each product.

Id	Name	SBO
MrnaCy	MrnaCy	

Kinetic Law

Derived unit contains undeclared units

$$v_3 = \text{vol}(\text{Cell}) \cdot \text{Constant_flux_irreversible}(k_{\text{SyMrna}}) \quad (25)$$

$$\text{Constant_flux_irreversible}(v) = v \quad (26)$$

$$\text{Constant_flux_irreversible}(v) = v \quad (27)$$

8.4 Reaction Synthesis_of_p53_mRNAs

This is an irreversible reaction of no reactant forming one product.

Name Synthesis of p53 mRNAs

Reaction equation



Product

Table 10: Properties of each product.

Id	Name	SBO
MrnaP53	MrnaP53	

Kinetic Law

Derived unit contains undeclared units

$$v_4 = \text{vol}(\text{Cell}) \cdot \text{Constant_flux_irreversible}(\text{kSyMrna}) \quad (29)$$

$$\text{Constant_flux_irreversible}(v) = v \quad (30)$$

$$\text{Constant_flux_irreversible}(v) = v \quad (31)$$

8.5 Reaction Degradation_of_p21_mRNAs

This is an irreversible reaction of one reactant forming no product.

Name Degradation of p21 mRNAs

Reaction equation



Reactant

Table 11: Properties of each reactant.

Id	Name	SBO
MrnaP21	MrnaP21	

Kinetic Law

Derived unit contains undeclared units

$$v_5 = \text{vol}(\text{Cell}) \cdot k_{\text{DeMrna}} \cdot [\text{MrnaP21}] \quad (33)$$

8.6 Reaction Degradation_of_cyclin_mRNAs

This is an irreversible reaction of one reactant forming no product.

Name Degradation of cyclin mRNAs

Reaction equation



Reactant

Table 12: Properties of each reactant.

Id	Name	SBO
MrnaCy	MrnaCy	

Kinetic Law

Derived unit contains undeclared units

$$v_6 = \text{vol}(\text{Cell}) \cdot k_{\text{DeMrna}} \cdot [\text{MrnaCy}] \quad (35)$$

8.7 Reaction Degradation_of_p53_mRNAs

This is an irreversible reaction of one reactant forming no product.

Name Degradation of p53 mRNAs

Reaction equation



Reactant

Table 13: Properties of each reactant.

Id	Name	SBO
MrnaP53	MrnaP53	

Kinetic Law

Derived unit contains undeclared units

$$v_7 = \text{vol}(\text{Cell}) \cdot k_{\text{DeMrna}} \cdot [\text{MrnaP53}] \quad (37)$$

8.8 Reaction `Synthesis_of_p21`

This is an irreversible reaction of one reactant forming two products.

Name `Synthesis of p21`

Reaction equation



Reactant

Table 14: Properties of each reactant.

Id	Name	SBO
MrnaP21	MrnaP21	

Products

Table 15: Properties of each product.

Id	Name	SBO
MrnaP21	MrnaP21	
P21	P21	

Kinetic Law

Derived unit contains undeclared units

$$v_8 = \text{vol}(\text{Cell}) \cdot k_{\text{SyP21}} \cdot [\text{MrnaP21}] \quad (39)$$

8.9 Reaction Degradation_of_p21

This is an irreversible reaction of one reactant forming no product influenced by four modifiers.

Name Degradation of p21

Reaction equation



Reactant

Table 16: Properties of each reactant.

Id	Name	SBO
P21	P21	

Modifiers

Table 17: Properties of each modifier.

Id	Name	SBO
Skp2	Skp2	
Cy	Cy	
Cdt2	Cdt2	
aRc	aRc	

Kinetic Law

Derived unit contains undeclared units

$$v_9 = \text{vol}(\text{Cell}) \cdot r_{\text{DeP21_1}}([\text{Cdt2}], [\text{Cy}], [\text{P21}], [\text{Skp2}], [\text{aRc}], k_{\text{DeP21}}, k_{\text{DeP21Cy}}, k_{\text{DeP21aRc}}) \quad (41)$$

$$\begin{aligned} & r_{\text{DeP21_1}}([\text{Cdt2}], [\text{Cy}], [\text{P21}], [\text{Skp2}], [\text{aRc}], k_{\text{DeP21}}, k_{\text{DeP21Cy}}, k_{\text{DeP21aRc}}) \\ &= (k_{\text{DeP21}} + k_{\text{DeP21Cy}} \cdot [\text{Skp2}] \cdot [\text{Cy}] + k_{\text{DeP21aRc}} \cdot [\text{Cdt2}] \cdot [\text{aRc}]) \cdot [\text{P21}] \end{aligned} \quad (42)$$

$$\begin{aligned} & rDeP21_1 ([Cdt2], [Cy], [P21], [Sklp2], [aRc], kDeP21, kDeP21Cy, kDeP21aRc) \\ & = (kDeP21 + kDeP21Cy \cdot [Sklp2] \cdot [Cy] + kDeP21aRc \cdot [Cdt2] \cdot [aRc]) \cdot [P21] \end{aligned} \quad (43)$$

8.10 Reaction *Synthesis_of_cyclins*

This is an irreversible reaction of one reactant forming two products.

Name Synthesis of cyclins

Reaction equation



Reactant

Table 18: Properties of each reactant.

Id	Name	SBO
MrnaCy	MrnaCy	

Products

Table 19: Properties of each product.

Id	Name	SBO
MrnaCy	MrnaCy	
Cy	Cy	

Kinetic Law

Derived unit contains undeclared units

$$v_{10} = \text{vol}(\text{Cell}) \cdot kSyCy \cdot [MrnaCy] \quad (45)$$

8.11 Reaction *Degradation_of_cyclins*

This is an irreversible reaction of one reactant forming no product influenced by two modifiers.

Name Degradation of cyclins

Reaction equation



Reactant

Table 20: Properties of each reactant.

Id	Name	SBO
Cy	Cy	

Modifiers

Table 21: Properties of each modifier.

Id	Name	SBO
Skp2	Skp2	
Cy	Cy	

Kinetic Law

Derived unit contains undeclared units

$$v_{11} = \text{vol}(\text{Cell}) \cdot \text{rDeCy_1}([\text{Cy}], [\text{Skp2}], \text{kDeCy}, \text{kDeCyCy}) \quad (47)$$

$$\text{rDeCy_1}([\text{Cy}], [\text{Skp2}], \text{kDeCy}, \text{kDeCyCy}) = (\text{kDeCy} + \text{kDeCyCy} \cdot [\text{Skp2}] \cdot [\text{Cy}]) \cdot [\text{Cy}] \quad (48)$$

$$\text{rDeCy_1}([\text{Cy}], [\text{Skp2}], \text{kDeCy}, \text{kDeCyCy}) = (\text{kDeCy} + \text{kDeCyCy} \cdot [\text{Skp2}] \cdot [\text{Cy}]) \cdot [\text{Cy}] \quad (49)$$

8.12 Reaction Association and dissociation of CDK2:Cyclin and p21

This is a reversible reaction of two reactants forming one product.

Name Association and dissociation of CDK2:Cyclin and p21

Reaction equation



Reactants

Table 22: Properties of each reactant.

Id	Name	SBO
Cy	Cy	
P21	P21	

Product

Table 23: Properties of each product.

Id	Name	SBO
CyP21	CyP21	

Kinetic Law

Derived unit contains undeclared units

$$v_{12} = \text{vol}(\text{Cell}) \cdot (k_{\text{AsCyP21}} \cdot [\text{Cy}] \cdot [\text{P21}] - k_{\text{DsCyP21}} \cdot [\text{CyP21}]) \quad (51)$$

8.13 Reaction Degradation_of_cyclin_in_CDK2_Cyclin_p21_complexes

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

Name Degradation of cyclin in CDK2:Cyclin:p21 complexes

Reaction equation



Reactant

Table 24: Properties of each reactant.

Id	Name	SBO
CyP21	CyP21	

Modifiers

Table 25: Properties of each modifier.

Id	Name	SBO
Skp2	Skp2	
Cy	Cy	

Product

Table 26: Properties of each product.

Id	Name	SBO
P21	P21	

Kinetic Law

Derived unit contains undeclared units

$$v_{13} = \text{vol}(\text{Cell}) \cdot \text{rDeCy_2}([\text{Cy}], [\text{CyP21}], [\text{Skp2}], \text{kDeCy}, \text{kDeCyCy}) \quad (53)$$

$$\begin{aligned} &\text{rDeCy_2}([\text{Cy}], [\text{CyP21}], [\text{Skp2}], \text{kDeCy}, \text{kDeCyCy}) \\ &= (\text{kDeCy} + \text{kDeCyCy} \cdot [\text{Skp2}] \cdot [\text{Cy}]) \cdot [\text{CyP21}] \end{aligned} \quad (54)$$

$$\begin{aligned} &\text{rDeCy_2}([\text{Cy}], [\text{CyP21}], [\text{Skp2}], \text{kDeCy}, \text{kDeCyCy}) \\ &= (\text{kDeCy} + \text{kDeCyCy} \cdot [\text{Skp2}] \cdot [\text{Cy}]) \cdot [\text{CyP21}] \end{aligned} \quad (55)$$

8.14 Reaction Degradation_of_p21_in_CDK2_Cyclin_p21_complexes

This is an irreversible reaction of one reactant forming one product influenced by four modifiers.

Name Degradation of p21 in CDK2:Cyclin:p21 complexes

Reaction equation



Reactant

Table 27: Properties of each reactant.

Id	Name	SBO
CyP21	CyP21	

Modifiers

Table 28: Properties of each modifier.

Id	Name	SBO
Skp2	Skp2	
Cy	Cy	
Cdt2	Cdt2	
aRc	aRc	

Product

Table 29: Properties of each product.

Id	Name	SBO
Cy	Cy	

Kinetic Law

Derived unit contains undeclared units

$$v_{14} = \text{vol}(\text{Cell}) \cdot \text{rDeP21_2}([Cdt2], [Cy], [CyP21], [Skp2], [aRc], kDeP21, kDeP21Cy, kDeP21aRc) \quad (57)$$

$$\begin{aligned} &\text{rDeP21_2}([Cdt2], [Cy], [CyP21], [Skp2], [aRc], kDeP21, kDeP21Cy, kDeP21aRc) \\ &= (kDeP21 + kDeP21Cy \cdot [Skp2] \cdot [Cy] + kDeP21aRc \cdot [Cdt2] \cdot [aRc]) \cdot [CyP21] \end{aligned} \quad (58)$$

$$\begin{aligned} &\text{rDeP21_2}([Cdt2], [Cy], [CyP21], [Skp2], [aRc], kDeP21, kDeP21Cy, kDeP21aRc) \\ &= (kDeP21 + kDeP21Cy \cdot [Skp2] \cdot [Cy] + kDeP21aRc \cdot [Cdt2] \cdot [aRc]) \cdot [CyP21] \end{aligned} \quad (59)$$

8.15 Reaction `Import_of_active_PCNA`

This is an irreversible reaction of no reactant forming one product.

Name Import of active PCNA

Reaction equation



Product

Table 30: Properties of each product.

Id	Name	SBO
aPcna	aPcna	

Kinetic Law

Derived unit contains undeclared units

$$v_{15} = \text{vol}(\text{Cell}) \cdot \text{Constant_flux_irreversible}(\text{kImPc}) \quad (61)$$

$$\text{Constant_flux_irreversible}(v) = v \quad (62)$$

$$\text{Constant_flux_irreversible}(v) = v \quad (63)$$

8.16 Reaction `Export_of_active_PCNA`

This is an irreversible reaction of one reactant forming no product.

Name Export of active PCNA

Reaction equation



Reactant

Table 31: Properties of each reactant.

Id	Name	SBO
aPcna	aPcna	

Kinetic Law

Derived unit contains undeclared units

$$v_{16} = \text{vol}(\text{Cell}) \cdot k_{\text{ExpC}} \cdot [\text{aPcna}] \quad (65)$$

8.17 Reaction `Export_of_inactive_PCNA`

This is an irreversible reaction of one reactant forming one product.

Name Export of inactive PCNA

Reaction equation



Reactant

Table 32: Properties of each reactant.

Id	Name	SBO
iPcna	iPcna	

Product

Table 33: Properties of each product.

Id	Name	SBO
P21	P21	

Kinetic Law

Derived unit contains undeclared units

$$v_{17} = \text{vol}(\text{Cell}) \cdot k_{\text{ExpC}} \cdot [\text{iPcna}] \quad (67)$$

8.18 Reaction `Association_and_dissociation_of_PCNA_and_p21`

This is a reversible reaction of two reactants forming one product.

Name Association and dissociation of PCNA and p21

Reaction equation



Reactants

Table 34: Properties of each reactant.

Id	Name	SBO
aPcna	aPcna	
P21	P21	

Product

Table 35: Properties of each product.

Id	Name	SBO
iPcna	iPcna	

Kinetic Law

Derived unit contains undeclared units

$$v_{18} = \text{vol}(\text{Cell}) \cdot (k_{\text{AsPcP21}} \cdot [\text{aPcna}] \cdot [\text{P21}] - k_{\text{DsPcP21}} \cdot [\text{iPcna}]) \quad (69)$$

8.19 Reaction Degradation_of_p21_in_PCNA_p21_complexes

This is an irreversible reaction of one reactant forming one product influenced by four modifiers.

Name Degradation of p21 in PCNA:p21 complexes

Reaction equation



Reactant

Table 36: Properties of each reactant.

Id	Name	SBO
iPcna	iPcna	

Modifiers

Table 37: Properties of each modifier.

Id	Name	SBO
Skp2	Skp2	
Cy	Cy	
Cdt2	Cdt2	
aRc	aRc	

Product

Table 38: Properties of each product.

Id	Name	SBO
aPcna	aPcna	

Kinetic Law

Derived unit contains undeclared units

$$v_{19} = \text{vol}(\text{Cell}) \cdot \text{rDeP21_3}([Cdt2], [Cy], [Skp2], [aRc], [iPcna], kDeP21, kDeP21Cy, kDeP21aRc) \quad (71)$$

$$\begin{aligned} &\text{rDeP21_3}([Cdt2], [Cy], [Skp2], [aRc], [iPcna], kDeP21, kDeP21Cy, kDeP21aRc) \\ &= (kDeP21 + kDeP21Cy \cdot [Skp2] \cdot [Cy] + kDeP21aRc \cdot [Cdt2] \cdot [aRc]) \cdot [iPcna] \end{aligned} \quad (72)$$

$$\begin{aligned} &\text{rDeP21_3}([Cdt2], [Cy], [Skp2], [aRc], [iPcna], kDeP21, kDeP21Cy, kDeP21aRc) \\ &= (kDeP21 + kDeP21Cy \cdot [Skp2] \cdot [Cy] + kDeP21aRc \cdot [Cdt2] \cdot [aRc]) \cdot [iPcna] \end{aligned} \quad (73)$$

8.20 Reaction Phosphorylation priming of replication complexes

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

Name Phosphorylation/priming of replication complexes

Reaction equation



Reactant

Table 39: Properties of each reactant.

Id	Name	SBO
Rc	Rc	

Modifier

Table 40: Properties of each modifier.

Id	Name	SBO
Cy	Cy	

Product

Table 41: Properties of each product.

Id	Name	SBO
pRc	pRc	

Kinetic Law**Derived unit** contains undeclared units

$$v_{20} = \text{vol}(\text{Cell}) \cdot \text{rPhRc_1}([\text{Cy}], [\text{Rc}], j\text{Cy}, k\text{PhRc}, n) \quad (75)$$

$$\text{rPhRc_1}([\text{Cy}], [\text{Rc}], j\text{Cy}, k\text{PhRc}, n) = \frac{k\text{PhRc} \cdot [\text{Cy}]^n}{j\text{Cy}^n + [\text{Cy}]^n} \cdot [\text{Rc}] \quad (76)$$

$$\text{rPhRc_1}([\text{Cy}], [\text{Rc}], j\text{Cy}, k\text{PhRc}, n) = \frac{k\text{PhRc} \cdot [\text{Cy}]^n}{j\text{Cy}^n + [\text{Cy}]^n} \cdot [\text{Rc}] \quad (77)$$

8.21 Reaction *Dephosphorylation_of_replication_complexes*

This is an irreversible reaction of one reactant forming one product.

Name Dephosphorylation of replication complexes**Reaction equation**

Reactant

Table 42: Properties of each reactant.

Id	Name	SBO
pRc	pRc	

Product

Table 43: Properties of each product.

Id	Name	SBO
Rc	Rc	

Kinetic Law

Derived unit contains undeclared units

$$v_{21} = \text{vol}(\text{Cell}) \cdot k_{\text{DpRc}} \cdot [\text{pRc}] \quad (79)$$

8.22 Reaction Association_and_dissociation_of_active_PCNA_and-replication_complexes

This is a reversible reaction of two reactants forming one product.

Name Association and dissociation of active PCNA and replication complexes

Reaction equation



Reactants

Table 44: Properties of each reactant.

Id	Name	SBO
aPcna	aPcna	
pRc	pRc	

Product

Table 45: Properties of each product.

Id	Name	SBO
aRc	aRc	

Kinetic Law

Derived unit contains undeclared units

$$v_{22} = \text{vol}(\text{Cell}) \cdot (k_{\text{AsRcPc}} \cdot [\text{aPcna}] \cdot [\text{pRc}] - k_{\text{DsRcPc}} \cdot [\text{aRc}]) \quad (81)$$

8.23 Reaction Association and dissociation of inactive PCNA and replication complexes

This is a reversible reaction of two reactants forming one product.

Name Association and dissociation of inactive PCNA and replication complexes

Reaction equation



Reactants

Table 46: Properties of each reactant.

Id	Name	SBO
iPcna	iPcna	
pRc	pRc	

Product

Table 47: Properties of each product.

Id	Name	SBO
iRc	iRc	

Kinetic Law

Derived unit contains undeclared units

$$v_{23} = \text{vol}(\text{Cell}) \cdot (k_{\text{AsRcPc}} \cdot [\text{iPcna}] \cdot [\text{pRc}] - k_{\text{DsRcPc}} \cdot [\text{iRc}]) \quad (83)$$

8.24 Reaction

[Association and dissociation of p21 and replication complexes](#)

This is a reversible reaction of two reactants forming one product.

Name Association and dissociation of p21 and replication complexes

Reaction equation



Reactants

Table 48: Properties of each reactant.

Id	Name	SBO
aRc	aRc	
P21	P21	

Product

Table 49: Properties of each product.

Id	Name	SBO
iRc	iRc	

Kinetic Law

Derived unit contains undeclared units

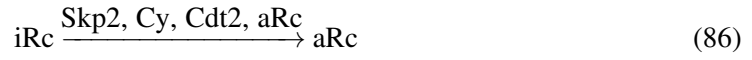
$$v_{24} = \text{vol}(\text{Cell}) \cdot (k_{\text{AsPcP21}} \cdot [\text{aRc}] \cdot [\text{P21}] - k_{\text{DsPcP21}} \cdot [\text{iRc}]) \quad (85)$$

8.25 Reaction [Degradation of p21 in inactive replication complexes](#)

This is an irreversible reaction of one reactant forming one product influenced by four modifiers.

Name Degradation of p21 in inactive replication complexes

Reaction equation



Reactant

Table 50: Properties of each reactant.

Id	Name	SBO
iRc	iRc	

Modifiers

Table 51: Properties of each modifier.

Id	Name	SBO
Skp2	Skp2	
Cy	Cy	
Cdt2	Cdt2	
aRc	aRc	

Product

Table 52: Properties of each product.

Id	Name	SBO
aRc	aRc	

Kinetic Law

Derived unit contains undeclared units

$$v_{25} = \text{vol}(\text{Cell}) \cdot \text{rDeP21_4}([\text{Cdt2}], [\text{Cy}], [\text{Skp2}], [\text{aRc}], [\text{iRc}], \text{kDeP21}, \text{kDeP21Cy}, \text{kDeP21aRc}) \quad (87)$$

$$\begin{aligned} & \text{rDeP21_4}([\text{Cdt2}], [\text{Cy}], [\text{Skp2}], [\text{aRc}], [\text{iRc}], \text{kDeP21}, \text{kDeP21Cy}, \text{kDeP21aRc}) \\ &= (\text{kDeP21} + \text{kDeP21Cy} \cdot [\text{Skp2}] \cdot [\text{Cy}] + \text{kDeP21aRc} \cdot [\text{Cdt2}] \cdot [\text{aRc}]) \cdot [\text{iRc}] \end{aligned} \quad (88)$$

$$\begin{aligned} & rDeP21_4([Cdt2], [Cy], [Sklp2], [aRc], [iRc], kDeP21, kDeP21Cy, kDeP21aRc) \\ & = (kDeP21 + kDeP21Cy \cdot [Sklp2] \cdot [Cy] + kDeP21aRc \cdot [Cdt2] \cdot [aRc]) \cdot [iRc] \end{aligned} \quad (89)$$

8.26 Reaction *Synthesis_of_DNA*

This is an irreversible reaction of one reactant forming two products.

Name Synthesis of DNA

Reaction equation



Reactant

Table 53: Properties of each reactant.

Id	Name	SBO
aRc	aRc	

Products

Table 54: Properties of each product.

Id	Name	SBO
aRc	aRc	
Dna	Dna	

Kinetic Law

Derived unit contains undeclared units

$$v_{26} = \text{vol}(\text{Cell}) \cdot kSyDna \cdot [aRc] \quad (91)$$

8.27 Reaction *Dissassembly_of_RC*

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name Dissassembly of RC

Reaction equation



Reactant

Table 55: Properties of each reactant.

Id	Name	SBO
Rc	Rc	

Modifier

Table 56: Properties of each modifier.

Id	Name	SBO
Dna	Dna	

Kinetic Law

Derived unit contains undeclared units

$$v_{27} = \text{vol}(\text{Cell}) \cdot \text{rDsRc}([\text{Dna}], [\text{Rc}]) \quad (93)$$

$$\text{rDsRc}([\text{Dna}], [\text{Rc}]) = \begin{cases} 0 & \text{if } [\text{Dna}] < 1 \\ \begin{cases} 1 \cdot [\text{Rc}] & \text{if } [\text{Dna}] > 1 \\ 0.5 \cdot [\text{Rc}] & \text{otherwise} \end{cases} & \text{otherwise} \end{cases} \quad (94)$$

$$\text{rDsRc}([\text{Dna}], [\text{Rc}]) = \begin{cases} 0 & \text{if } [\text{Dna}] < 1 \\ \begin{cases} 1 \cdot [\text{Rc}] & \text{if } [\text{Dna}] > 1 \\ 0.5 \cdot [\text{Rc}] & \text{otherwise} \end{cases} & \text{otherwise} \end{cases} \quad (95)$$

8.28 Reaction Dissassembly_of_pRC

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name Dissassembly of pRC

Reaction equation



Reactant

Table 57: Properties of each reactant.

Id	Name	SBO
pRc	pRc	

Modifier

Table 58: Properties of each modifier.

Id	Name	SBO
Dna	Dna	

Kinetic Law

Derived unit contains undeclared units

$$v_{28} = \text{vol}(\text{Cell}) \cdot \text{rDsRc}_1([\text{Dna}], [\text{pRc}]) \quad (97)$$

$$\text{rDsRc}_1([\text{Dna}], [\text{pRc}]) = \begin{cases} 0 & \text{if } [\text{Dna}] < 1 \\ \begin{cases} 1 \cdot [\text{pRc}] & \text{if } [\text{Dna}] > 1 \\ 0.5 \cdot [\text{pRc}] & \text{otherwise} \end{cases} & \text{otherwise} \end{cases} \quad (98)$$

$$\text{rDsRc}_1([\text{Dna}], [\text{pRc}]) = \begin{cases} 0 & \text{if } [\text{Dna}] < 1 \\ \begin{cases} 1 \cdot [\text{pRc}] & \text{if } [\text{Dna}] > 1 \\ 0.5 \cdot [\text{pRc}] & \text{otherwise} \end{cases} & \text{otherwise} \end{cases} \quad (99)$$

8.29 Reaction Dissassembly_of_aRC

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

Name Dissassembly of aRC

Reaction equation



Reactant

Table 59: Properties of each reactant.

Id	Name	SBO
aRc	aRc	

Modifier

Table 60: Properties of each modifier.

Id	Name	SBO
Dna	Dna	

Product

Table 61: Properties of each product.

Id	Name	SBO
aPcna	aPcna	

Kinetic Law

Derived unit contains undeclared units

$$v_{29} = \text{vol}(\text{Cell}) \cdot \text{rDsRc}_2([\text{Dna}], [\text{aRc}]) \quad (101)$$

$$\text{rDsRc}_2([\text{Dna}], [\text{aRc}]) = \begin{cases} 0 & \text{if } [\text{Dna}] < 1 \\ \begin{cases} 1 \cdot [\text{aRc}] & \text{if } [\text{Dna}] > 1 \\ 0.5 \cdot [\text{aRc}] & \text{otherwise} \end{cases} & \text{otherwise} \end{cases} \quad (102)$$

$$\text{rDsRc}_2([\text{Dna}], [\text{aRc}]) = \begin{cases} 0 & \text{if } [\text{Dna}] < 1 \\ \begin{cases} 1 \cdot [\text{aRc}] & \text{if } [\text{Dna}] > 1 \\ 0.5 \cdot [\text{aRc}] & \text{otherwise} \end{cases} & \text{otherwise} \end{cases} \quad (103)$$

8.30 Reaction Dissassembly_of_iRC

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

Name Dissassembly of iRC

Reaction equation



Reactant

Table 62: Properties of each reactant.

Id	Name	SBO
iRc	iRc	

Modifier

Table 63: Properties of each modifier.

Id	Name	SBO
Dna	Dna	

Product

Table 64: Properties of each product.

Id	Name	SBO
iPcna	iPcna	

Kinetic Law

Derived unit contains undeclared units

$$v_{30} = \text{vol}(\text{Cell}) \cdot \text{rDsRc_3}([\text{Dna}], [\text{iRc}]) \quad (105)$$

$$\text{rDsRc_3}([\text{Dna}], [\text{iRc}]) = \begin{cases} 0 & \text{if } [\text{Dna}] < 1 \\ 1 \cdot [\text{iRc}] & \text{if } [\text{Dna}] > 1 \\ 0.5 \cdot [\text{iRc}] & \text{otherwise} \end{cases} \quad (106)$$

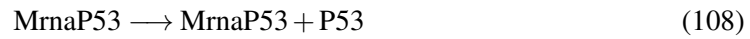
$$rDsRc_3([Dna], [iRc]) = \begin{cases} 0 & \text{if } [Dna] < 1 \\ \begin{cases} 1 \cdot [iRc] & \text{if } [Dna] > 1 \\ 0.5 \cdot [iRc] & \text{otherwise} \end{cases} & \text{otherwise} \end{cases} \quad (107)$$

8.31 Reaction Synthesis_of_p53

This is an irreversible reaction of one reactant forming two products.

Name Synthesis of p53

Reaction equation



Reactant

Table 65: Properties of each reactant.

Id	Name	SBO
MrnaP53	MrnaP53	

Products

Table 66: Properties of each product.

Id	Name	SBO
MrnaP53	MrnaP53	
P53	P53	

Kinetic Law

Derived unit contains undeclared units

$$v_{31} = \text{vol}(\text{Cell}) \cdot k\text{SyP53} \cdot [\text{MrnaP53}] \quad (109)$$

8.32 Reaction Degradation_of_p53

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name Degradation of p53

Reaction equation



Reactant

Table 67: Properties of each reactant.

Id	Name	SBO
P53	P53	

Modifier

Table 68: Properties of each modifier.

Id	Name	SBO
Dam	Dam	

Kinetic Law

Derived unit contains undeclared units

$$v_{32} = \text{vol}(\text{Cell}) \cdot \text{rDeP53_1}([\text{Dam}], [\text{P53}], \text{jP53}, \text{kDeP53}) \quad (111)$$

$$\text{rDeP53_1}([\text{Dam}], [\text{P53}], \text{jP53}, \text{kDeP53}) = \frac{\text{kDeP53}}{\text{jP53} + [\text{Dam}]} \cdot [\text{P53}] \quad (112)$$

$$\text{rDeP53_1}([\text{Dam}], [\text{P53}], \text{jP53}, \text{kDeP53}) = \frac{\text{kDeP53}}{\text{jP53} + [\text{Dam}]} \cdot [\text{P53}] \quad (113)$$

8.33 Reaction Induction of DNA damage

This is an irreversible reaction of no reactant forming one product.

Name Induction of DNA damage

Reaction equation



Product

Table 69: Properties of each product.

Id	Name	SBO
Dam	Dam	

Kinetic Law

Derived unit contains undeclared units

$$v_{33} = \text{vol}(\text{Cell}) \cdot \text{Constant_flux_irreversible}(\text{kGeDam}) \quad (115)$$

$$\text{Constant_flux_irreversible}(v) = v \quad (116)$$

$$\text{Constant_flux_irreversible}(v) = v \quad (117)$$

8.34 Reaction *Induction_of_DNA_damage_by_replication*

This is an irreversible reaction of one reactant forming two products.

Name Induction of DNA damage by replication

Reaction equation



Reactant

Table 70: Properties of each reactant.

Id	Name	SBO
aRc	aRc	

Products

Table 71: Properties of each product.

Id	Name	SBO
aRc	aRc	
Dam	Dam	

Kinetic Law

Derived unit contains undeclared units

$$v_{34} = \text{vol}(\text{Cell}) \cdot k_{\text{GeDamArc}} \cdot [\text{aRc}] \quad (119)$$

8.35 Reaction `Repair_of_DNA_damage`

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name Repair of DNA damage

Reaction equation



Reactant

Table 72: Properties of each reactant.

Id	Name	SBO
Dam	Dam	

Modifier

Table 73: Properties of each modifier.

Id	Name	SBO
P53	P53	

Kinetic Law

Derived unit contains undeclared units

$$v_{35} = \text{vol}(\text{Cell}) \cdot r_{\text{ReDam}_1}([\text{Dam}], [\text{P53}], j_{\text{Dam}}, k_{\text{ReDam}}, k_{\text{ReDamP53}}) \quad (121)$$

$$\begin{aligned} & r_{\text{ReDam}_1}([\text{Dam}], [\text{P53}], j_{\text{Dam}}, k_{\text{ReDam}}, k_{\text{ReDamP53}}) \\ &= \left(k_{\text{ReDam}} + \frac{k_{\text{ReDamP53}} \cdot [\text{P53}]}{j_{\text{Dam}} + [\text{Dam}]} \right) \cdot [\text{Dam}] \end{aligned} \quad (122)$$

$$\begin{aligned} & \text{rReDam_1} ([\text{Dam}], [\text{P53}], j_{\text{Dam}}, k_{\text{ReDam}}, k_{\text{ReDamP53}}) \\ &= \left(k_{\text{ReDam}} + \frac{k_{\text{ReDamP53}} \cdot [\text{P53}]}{j_{\text{Dam}} + [\text{Dam}]} \right) \cdot [\text{Dam}] \end{aligned} \quad (123)$$

9 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the `hasOnlySubstanceUnits` flag may be set to `false` and `spacialDimensions > 0` for certain species.

9.1 Species `MrnaP21`

Name `MrnaP21`

Initial concentration $1 \text{ mmol} \cdot \text{ml}^{-1}$

This species takes part in five reactions (as a reactant in [Degradation_of_p21_mRNAs](#), [Synthesis_of_p21](#) and as a product in [Synthesis_of_p21_mRNAs](#), [Synthesis_of_p21_mRNAs_by_p53](#), [Synthesis_of_p21](#)).

$$\frac{d}{dt} \text{MrnaP21} = v_1 + v_2 + v_8 - v_5 - v_8 \quad (124)$$

9.2 Species `MrnaCy`

Name `MrnaCy`

Notes mRNAs encoding for both CyclinA:Cdk2 and CyclinE:Cdk2 complexes

Initial concentration $1 \text{ mmol} \cdot \text{ml}^{-1}$

This species takes part in four reactions (as a reactant in [Degradation_of_cyclin_mRNAs](#), [Synthesis_of_cyclins](#) and as a product in [Synthesis_of_cyclin_mRNAs](#), [Synthesis_of_cyclins](#)).

$$\frac{d}{dt} \text{MrnaCy} = v_3 + v_{10} - v_6 - v_{10} \quad (125)$$

9.3 Species MrnaP53

Name MrnaP53

Initial concentration 1 mmol · ml⁻¹

This species takes part in four reactions (as a reactant in [Degradation_of_p53_mRNAs](#), [Synthesis_of_p53](#) and as a product in [Synthesis_of_p53_mRNAs](#), [Synthesis_of_p53](#)).

$$\frac{d}{dt}\text{MrnaP53} = v_4 + v_{31} - v_7 - v_{31} \quad (126)$$

9.4 Species P21

Name P21

Initial concentration 0.72 mmol · ml⁻¹

This species takes part in seven reactions (as a reactant in [Degradation_of_p21](#), [Association_and_dissociation_of_CDK2_Cyclin_and_p21](#), [Association_and_dissociation_of_PCNA_and_p21](#), [Association_and_dissociation_of_p21_and_replication_complexes](#) and as a product in [Synthesis_of_p21](#), [Degradation_of_cyclin_in_CDK2_Cyclin_p21_complexes](#), [Export_of_inactive_PCNA](#)).

$$\frac{d}{dt}\text{P21} = v_8 + v_{13} + v_{17} - v_9 - v_{12} - v_{18} - v_{24} \quad (127)$$

9.5 Species Cy

Name Cy

Notes Both CyclinA:Cdk2 and CyclinE:Cdk2 complexes

Initial concentration 0.4 mmol · ml⁻¹

This species takes part in eleven reactions (as a reactant in [Degradation_of_cyclins](#), [Association_and_dissociation_of_CDK2_Cyclin_and_p21](#) and as a product in [Synthesis_of_cyclins](#), [Degradation_of_p21_in_CDK2_Cyclin_p21_complexes](#) and as a modifier in [Degradation_of_p21](#), [Degradation_of_cyclins](#), [Degradation_of_cyclin_in_CDK2_Cyclin_p21_complexes](#), [Degradation_of_p21_in_CDK2_Cyclin_p21_complexes](#), [Degradation_of_p21_in_PCNA_p21_complexes](#), [Phosphorylation_priming_of_replication_complexes](#), [Degradation_of_p21_in_inactive_replication_complexes](#)).

$$\frac{d}{dt}\text{Cy} = v_{10} + v_{14} - v_{11} - v_{12} \quad (128)$$

9.6 Species CyP21

Name CyP21

Notes Both CyclinA:Cdk2:p21 and CyclinE:Cdk2:p21 complexes

Initial concentration 0 mmol · ml⁻¹

This species takes part in three reactions (as a reactant in [Degradation_of_cyclin_in_CDK2-Cyclin_p21_complexes](#), [Degradation_of_p21_in_CDK2-Cyclin_p21_complexes](#) and as a product in [Association_and_dissociation_of_CDK2-Cyclin_and_p21](#)).

$$\frac{d}{dt}\text{CyP21} = v_{12} - v_{13} - v_{14} \quad (129)$$

9.7 Species aPcna

Name aPcna

Initial concentration 0.5 mmol · ml⁻¹

This species takes part in six reactions (as a reactant in [Export_of_active_PCNA](#), [Association_and_dissociation_of_PCNA_and_p21](#), [Association_and_dissociation_of_active_PCNA_and_replication_complexes](#) and as a product in [Import_of_active_PCNA](#), [Degradation_of_p21_in_PCNA_p21_complexes](#), [Dissassembly_of_aRC](#)).

$$\frac{d}{dt}\text{aPcna} = v_{15} + v_{19} + v_{29} - v_{16} - v_{18} - v_{22} \quad (130)$$

9.8 Species Rc

Name Rc

Initial concentration 1 mmol · ml⁻¹

This species takes part in three reactions (as a reactant in [Phosphorylation_priming_of_replication_complexes](#), [Dissassembly_of_RC](#) and as a product in [Dephosphorylation_of_replication_complexes](#)).

$$\frac{d}{dt}\text{Rc} = v_{21} - v_{20} - v_{27} \quad (131)$$

9.9 Species pRc

Name pRc

Initial concentration 0 mmol · ml⁻¹

This species takes part in five reactions (as a reactant in [Dephosphorylation_of_replication-complexes](#), [Association_and_dissociation_of_active_PCNA_and_replication_complexes](#), [Association_and_dissociation_of_inactive_PCNA_and_replication_complexes](#), [Dissassembly_of_pRC](#) and as a product in [Phosphorylation-priming_of_replication_complexes](#)).

$$\frac{d}{dt}pRc = v_{20} - v_{21} - v_{22} - v_{23} - v_{28} \quad (132)$$

9.10 Species aRc

Name aRc

Initial concentration 0 mmol · ml⁻¹

This species takes part in twelve reactions (as a reactant in [Association_and_dissociation_of_p21_and_replication_complexes](#), [Synthesis_of_DNA](#), [Dissassembly_of_aRC](#), [Induction_of_DNA_damage_by_replication](#) and as a product in [Association_and_dissociation_of_active_PCNA_and_replication_complexes](#), [Degradation_of_p21_in_inactive_replication_complexes](#), [Synthesis_of_DNA](#), [Induction_of_DNA_damage_by_replication](#) and as a modifier in [Degradation_of_p21](#), [Degradation_of_p21_in_CDK2_Cyclin_p21_complexes](#), [Degradation_of_p21_in_PCNA_p21_complexes](#), [Degradation_of_p21_in_inactive_replication_complexes](#)).

$$\frac{d}{dt}aRc = v_{22} + v_{25} + v_{26} + v_{34} - v_{24} - v_{26} - v_{29} - v_{34} \quad (133)$$

9.11 Species iRc

Name iRc

Initial concentration 0 mmol · ml⁻¹

This species takes part in four reactions (as a reactant in [Degradation_of_p21_in_inactive_replication_complexes](#), [Dissassembly_of_iRC](#) and as a product in [Association_and_dissociation_of_inactive_PCNA_and_replication_complexes](#), [Association_and_dissociation_of_p21_and_replication_complexes](#)).

$$\frac{d}{dt}iRc = v_{23} + v_{24} - v_{25} - v_{30} \quad (134)$$

9.12 Species Dna

Name Dna

Initial concentration 0 mmol · ml⁻¹

This species takes part in five reactions (as a product in [Synthesis_of_DNA](#) and as a modifier in [Dissassembly_of_RC](#), [Dissassembly_of_pRC](#), [Dissassembly_of_aRC](#), [Dissassembly_of_iRC](#)).

$$\frac{d}{dt}Dna = v_{26} \quad (135)$$

9.13 Species Dam

Name Dam

Initial concentration 0 mmol · ml⁻¹

This species takes part in four reactions (as a reactant in [Repair_of_DNA_damage](#) and as a product in [Induction_of_DNA_damage](#), [Induction_of_DNA_damage_by_replication](#) and as a modifier in [Degradation_of_p53](#)).

$$\frac{d}{dt}\text{Dam} = v_{33} + v_{34} - v_{35} \quad (136)$$

9.14 Species P53

Name P53

Initial concentration 0 mmol · ml⁻¹

This species takes part in five reactions (as a reactant in [Synthesis_of_p21_mRNAs_by_p53](#), [Degradation_of_p53](#) and as a product in [Synthesis_of_p21_mRNAs_by_p53](#), [Synthesis_of_p53](#) and as a modifier in [Repair_of_DNA_damage](#)).

$$\frac{d}{dt}\text{P53} = v_2 + v_{31} - v_2 - v_{32} \quad (137)$$

9.15 Species Skp2

Name Skp2

Initial concentration 1 mmol · ml⁻¹

This species takes part in six reactions (as a modifier in [Degradation_of_p21](#), [Degradation_of_cyclins](#), [Degradation_of_cyclin_in_CDK2_Cyclin_p21_complexes](#), [Degradation_of_p21_in_CDK2_Cyclin_p21_complexes](#), [Degradation_of_p21_in_PCNA_p21_complexes](#), [Degradation_of_p21_in_inactive_replication_complexes](#)), which do not influence its rate of change because this constant species is on the boundary of the reaction system:

$$\frac{d}{dt}\text{Skp2} = 0 \quad (138)$$

9.16 Species Cdt2

Name Cdt2

Initial concentration 1 mmol · ml⁻¹

This species takes part in four reactions (as a modifier in [Degradation_of_p21](#), [Degradation_of_p21_in_CDK2_Cyclin_p21_complexes](#), [Degradation_of_p21_in_PCNA_p21_complexes](#), [Degradation_of_p21_in_inactive_replication_complexes](#)), which do not influence its rate of change because this constant species is on the boundary of the reaction system:

$$\frac{d}{dt}Cdt2 = 0 \quad (139)$$

9.17 Species iPcna

Name iPcna

Initial concentration 0 mmol · ml⁻¹

This species takes part in five reactions (as a reactant in [Export_of_inactive_PCNA](#), [Degradation_of_p21_in_PCNA_p21_complexes](#), [Association_and_dissociation_of_inactive_PCNA_and_replication_complexes](#) and as a product in [Association_and_dissociation_of_PCNA_and_p21](#), [Dissassembly_of_iRC](#)).

$$\frac{d}{dt}iPcna = v_{18} + v_{30} - v_{17} - v_{19} - v_{23} \quad (140)$$

9.18 Species tP21

Name tP21

Initial concentration 0.72 mmol · ml⁻¹

Involved in rule [tP21](#)

One rule determines the species' quantity.

9.19 Species tCy

Name tCy

Notes Total level of both CyclinA:Cdk2 and CyclinE:Cdk2 complexes

Initial concentration 0.4 mmol · ml⁻¹

Involved in rule [tCy](#)

One rule determines the species' quantity.

9.20 Species tPcna

Name tPcna

Initial concentration 0.5 mmol · ml⁻¹

Involved in rule [tPcna](#)

One rule determines the species' quantity.

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