## **SBML Model Report**

# Model name: "Costa2014 - Computational Model of L. lactis Metabolism"



May 5, 2016

## 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by the following two authors: Audald Lloret i Villas<sup>1</sup> and Rafael Costa<sup>2</sup> at March 26<sup>th</sup> 2015 at 3:31 p. m. and last time modified at March 26<sup>th</sup> 2015 at 4:41 p. m. Table 1 gives an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	2
species types	0	species	26
events	0	constraints	0
reactions	21	function definitions	21
global parameters	0	unit definitions	1
rules	0	initial assignments	0

#### **Model Notes**

Costa2014 - Computational Model of L. lactisMetabolism

This model is described in the article: An extended dynamic model of Lactococcus lactis metabolism for mannitol and 2,3-butanediol production. Costa RS, Hartmann A, Gaspar P, Neves AR, Vinga S.Mol Biosyst 2014 Mar; 10(3): 628-639

<sup>&</sup>lt;sup>1</sup>EMBL-EBI, lloret@ebi.ac.uk

 $<sup>^2</sup> INESC-ID \, / \, IST, \, University \, of \, Lisbon, \, {\tt rafael.s.costa@tecnico.ulisboa.pt}$ 

#### Abstract:

Biomedical research and biotechnological production are greatly benefiting from the results provided by the development of dynamic models of microbial metabolism. Although several kinetic models of Lactococcus lactis (a Lactic Acid Bacterium (LAB) commonly used in the dairy industry) have been developed so far, most of them are simplified and focus only on specific metabolic pathways. Therefore, the application of mathematical models in the design of an engineering strategy for the production of industrially important products by L. lactis has been very limited. In this work, we extend the existing kinetic model of L. lactis central metabolism to include industrially relevant production pathways such as mannitol and 2,3-butanediol. In this way, we expect to study the dynamics of metabolite production and make predictive simulations in L. lactis. We used a system of ordinary differential equations (ODEs) with approximate Michaelis-Menten-like kinetics for each reaction, where the parameters were estimated from multivariate time-series metabolite concentrations obtained by our team through in vivo Nuclear Magnetic Resonance (NMR). The results show that the model captures observed transient dynamics when validated under a wide range of experimental conditions. Furthermore, we analyzed the model using global perturbations, which corroborate experimental evidence about metabolic responses upon enzymatic changes. These include that mannitol production is very sensitive to lactate dehydrogenase (LDH) in the wild type (W.T.) strain, and to mannitol phosphoenolpyruvate: a phosphotransferase system (PTS(Mtl)) in a LDH mutant strain. LDH reduction has also a positive control on 2,3-butanediol levels. Furthermore, it was found that overproduction of mannitol-1-phosphate dehydrogenase (MPD) in a LDH/PTS(Mtl) deficient strain can increase the mannitol levels. The results show that this model has prediction capability over new experimental conditions and offers promising possibilities to elucidate the effect of alterations in the main metabolism of L. lactis, with application in strain optimization.

This model is hosted on BioModels Database and identified by: BIOMD0000000572.

To cite BioModels Database, please use: BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models.

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#### 2 Unit Definitions

This is an overview of five unit definitions of which four are predefined by SBML and not mentioned in the model.

#### 2.1 Unit substance

Name substance

**Definition** mmol

## 2.2 Unit volume

**Notes** Litre is the predefined SBML unit for volume.

**Definition** 1

#### 2.3 Unit area

Notes Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition** m<sup>2</sup>

## 2.4 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

#### 2.5 Unit time

**Notes** Second is the predefined SBML unit for time.

**Definition** s

## 3 Compartments

This model contains two compartments.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
compartment_1 compartment_2			3 3	0.047	l litre	<b>1</b>	

## 3.1 Compartment compartment\_1

This is a three dimensional compartment with a constant size of 0.047 litre.

Name Intracellular

## **3.2 Compartment** compartment\_2

This is a three dimensional compartment with a constant size of one litre.

Name Extracellular

# 4 Species

This model contains 26 species. Section 7 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
G6P	G6P	compartment_1	$mmol \cdot l^{-1}$		
ATP	ATP	${ t compartment}_{ t 1}$	$\operatorname{mmol} \cdot 1^{-1}$		$\Box$
ADP	ADP	${\tt compartment\_1}$	$\text{mmol} \cdot 1^{-1}$		$\Box$
Pint	Pint	${\tt compartment\_1}$	$mmol \cdot l^{-1}$		
F6P	F6P	${\tt compartment\_1}$	$mmol \cdot l^{-1}$		
FBP	FBP	${ t compartment}_{ t 1}$	$\text{mmol} \cdot 1^{-1}$		$\Box$
G3P	G3P	${\tt compartment\_1}$	$\operatorname{mmol} \cdot 1^{-1}$		
BPG	BPG	${\tt compartment\_1}$	$\operatorname{mmol} \cdot 1^{-1}$		
PEP	PEP	${\tt compartment\_1}$	$\operatorname{mmol} \cdot 1^{-1}$		$\Box$
NAD	NAD	${\tt compartment\_1}$	$\text{mmol} \cdot 1^{-1}$		$\Box$
NADH	NADH	${\tt compartment\_1}$	$mmol \cdot l^{-1}$		
PYR	PYR	${\tt compartment\_1}$	$mmol \cdot l^{-1}$		
AcetCoA	AcetCoA	${\tt compartment\_1}$	$mmol \cdot l^{-1}$		
Acetoin	Acetoin	${\tt compartment\_1}$	$\operatorname{mmol} \cdot 1^{-1}$		
Mannitol	Mannitol	${\tt compartment\_1}$	$\operatorname{mmol} \cdot 1^{-1}$		
Mannitol1Phosphate	Mannitol1Phosphate	${\tt compartment\_1}$	$\operatorname{mmol} \cdot 1^{-1}$		
CoA	CoA	${\tt compartment\_1}$	$mmol \cdot l^{-1}$		$\Box$
Pext	Pext	compartment_2	$mmol \cdot l^{-1}$		$\Box$
Lactate	Lactate	compartment_2	$\operatorname{mmol} \cdot 1^{-1}$		$\Box$
Ethanol	Ethanol	compartment_2	$mmol \cdot l^{-1}$		
Acetate	Acetate	compartment_2	$\operatorname{mmol} \cdot 1^{-1}$		$\Box$
Butanediol	Butanediol	compartment_2	$\text{mmol} \cdot 1^{-1}$		

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
Glucose	Glucose	${\tt compartment\_2}$	$mmol \cdot l^{-1}$		$\Box$
Acetoin_Ext	Acetoin_Ext	${\tt compartment\_2}$	$mmol \cdot l^{-1}$		
${\tt Mannitol\_Ext}$	Mannitol_Ext	${\tt compartment\_2}$	$\mathrm{mmol}\cdot \mathrm{l}^{-1}$		
Formate	Formate	${\tt compartment\_2}$	$\text{mmol} \cdot 1^{-1}$		$\Box$

#### 5 Function definitions

This is an overview of 21 function definitions.

#### **5.1 Function definition** function\_4\_PTS\_Glc

Name function\_4\_PTS\_Glc

**Arguments** [FBP], [G6P], [Glucose], [PEP], [PYR], [Pint], Vmax\_PTS\_Glc, kaPint\_PTS\_Glc, kiFBP\_PTS\_Glc, kmG6P\_PTS\_Glc, kmGlucose\_PTS\_Glc, kmPEP\_PTS\_Glc, kmPYR\_PTS\_Glc

#### **Mathematical Expression**

$$\frac{[Pint]}{[Pint] + kaPint\_PTS\_Glc} \cdot \frac{kiFBP\_PTS\_Glc}{[FBP] + kiFBP\_PTS\_Glc} \cdot Vmax\_PTS\_Glc \cdot \frac{[Glucose]}{kmGlucose\_PTS\_Glc} \cdot \frac{[PEP]}{kmPEP\_PTS\_Glc} \cdot \frac{[PEP]}{kmGlucose\_PTS\_Glc} \cdot \frac{[PEP]}{kmPEP\_PTS\_Glc} \cdot \frac{[PEP]}{kmGPP\_PTS\_Glc} \cdot \frac{[PFP]}{kmPEP\_PTS\_Glc} \cdot \frac{[PFP]}{kmPEP$$

#### **5.2 Function definition** function\_4\_ATPase

Name function\_4\_ATPase

**Arguments** [ATP], Vmax\_ATPase, kmATP\_ATPase, nATPase

#### **Mathematical Expression**

$$Vmax\_ATPase \cdot \frac{\left(\frac{[ATP]}{kmATP\_ATPase}\right)^{nATPase}}{\left(\frac{[ATP]}{kmATP\_ATPase}\right)^{nATPase} + 1}$$
(2)

## **5.3 Function definition** function\_4\_P\_transp

Name function\_4\_P\_transp

**Arguments** [ADP], [ATP], [Pext], [Pint], Vmax\_Ptransport, kiPint\_Ptransport, kmADP\_Ptransport, kmPext\_Ptransport, kmPint\_Ptransport

$$\frac{\frac{kiPint\_Ptransport}{[Pint]+kiPint\_Ptransport} \cdot Vmax\_Ptransport \cdot \frac{[ATP]}{kmATP\_Ptransport} \cdot \frac{[Pext]}{kmPext\_Ptransport}}{\left(1 + \frac{[Pext]}{kmPext\_Ptransport}\right) \cdot \left(1 + \frac{[ATP]}{kmATP\_Ptransport}\right) + \left(1 + \frac{[Pint]}{kmPint\_Ptransport} + \left(\frac{[Pint]}{kmPint\_Ptransport}\right)^2\right) \cdot \left(1 + \frac{[ADP]}{kmADP\_Ptransport}\right)}$$

## **5.4 Function definition** function\_4\_PGI

Name function\_4\_PGI

**Arguments** [F6P], [G6P], Keq\_PGI, Vmax\_PGI, kmF6P\_PGI, kmG6P\_PGI

#### **Mathematical Expression**

$$\frac{\text{Vmax\_PGI} \cdot \frac{[\text{G6P}]}{\text{kmG6P\_PGI}} - \frac{\text{Vmax\_PGI}}{\text{Keq\_PGI}} \cdot \frac{[\text{F6P}]}{\text{kmG6P\_PGI}}}{1 + \frac{[\text{G6P}]}{\text{kmG6P\_PGI}} + \frac{[\text{F6P}]}{\text{kmF6P\_PGI}}}$$

$$(4)$$

#### **5.5 Function definition** function\_4\_PFK

Name function\_4\_PFK

**Arguments** [ADP], [ATP], [F6P], [FBP], Vmax\_PFK, kmADP\_PFK, kmATP\_PFK, kmF6P\_PFK, kmFBP\_PFK

#### **Mathematical Expression**

$$\frac{\text{Vmax\_PFK} \cdot \frac{[\text{F6P}]}{\text{kmF6P\_PFK}} \cdot \frac{[\text{ATP}]}{\text{kmATP\_PFK}}}{\left(1 + \frac{[\text{F6P}]}{\text{kmF6P\_PFK}}\right) \cdot \left(1 + \frac{[\text{ATP}]}{\text{kmATP\_PFK}}\right) + \left(1 + \frac{[\text{FBP}]}{\text{kmFBP\_PFK}}\right) \cdot \left(1 + \frac{[\text{ADP}]}{\text{kmADP\_PFK}}\right) - 1}$$

#### **5.6 Function definition** function\_4\_FBA

Name function\_4\_FBA

Arguments [FBP], [G3P], Keq\_FBA, Vmax\_FBA, kmFBP\_FBA, kmG3P\_FBA

## **Mathematical Expression**

$$\frac{Vmax\_FBA \cdot \frac{[FBP]}{kmFBP\_FBA} - \frac{Vmax\_FBA}{Keq\_FBA} \cdot \frac{[G3P]^2}{kmFBP\_FBA}}{1 + \frac{[FBP]}{kmFBP\_FBA} + \frac{[G3P]}{kmG3P\_FBA} + \left(\frac{[G3P]}{kmG3P\_FBA}\right)^2}$$
(6)

## **5.7 Function definition** function\_4\_GAPDH

Name function\_4\_GAPDH

**Arguments** [BPG], [G3P], Keq\_GAPDH, [NAD], [NADH], [Pint], Vmax\_GAPDH, kmBPG\_GAPDH, kmG3P\_GAPDH, kmNADH\_GAPDH, kmNADLGAPDH, kmPint\_GAPDH

$$\frac{V_{max\_GAPDH} \cdot \frac{[G3P]}{kmG3P\_GAPDH} \cdot \frac{[NAD]}{kmNAD\_GAPDH} \cdot \frac{[Pint]}{kmPint\_GAPDH} - \frac{V_{max\_GAPDH}}{Keq\_GAPDH} \cdot \frac{[BPG]}{kmG3P\_GAPDH} \cdot \frac{[NADH]}{kmNAD\_GAPDH} \cdot \frac{1}{kmNAD\_GAPDH} \cdot \frac{1}{kmPint\_GAPDH} \cdot \frac{1}{kmNAD\_GAPDH} \cdot \frac{1}{kmNAD\_G$$

#### **5.8 Function definition** function\_4\_ENO

Name function\_4\_ENO

**Arguments** [ADP], [ATP], [BPG], Keq\_ENO, [PEP], Vmax\_ENO, kmADP\_ENO, kmATP\_ENO, kmBPG\_ENO, kmPEP\_ENO

#### **Mathematical Expression**

$$\frac{V max\_ENO \cdot \frac{[BPG]}{kmBPG\_ENO} \cdot \frac{[ADP]}{kmADP\_ENO} - \frac{V max\_ENO}{keq\_ENO} \cdot \frac{[PEP]}{kmBPG\_ENO} \cdot \frac{[ATP]}{kmADP\_ENO}}{\left(1 + \frac{[BPG]}{kmBPG\_ENO}\right) \cdot \left(1 + \frac{[ADP]}{kmADP\_ENO}\right) + \left(1 + \frac{[PEP]}{kmPEP\_ENO}\right) \cdot \left(1 + \frac{[ATP]}{kmATP\_ENO}\right) - 1}$$

#### 5.9 Function definition function\_4\_PYK

Name function\_4\_PYK

**Arguments** [ADP], [ATP], [FBP], [PEP], [PYR], [Pint], Vmax\_PYK, kaFBP\_PYK, kiPint\_PYK, kmADP\_PYK, kmATP\_PYK, kmPEP\_PYK, kmPYR\_PYK, nPYK

#### **Mathematical Expression**

$$\frac{\frac{[\text{FBP}]}{[\text{FBP}] + ka\text{FBP\_PYK}} \cdot \frac{ki\text{Pint\_PYK}^{nPYK}}{[\text{Pint}]^{nPYK} + ki\text{Pint\_PYK}^{nPYK}} \cdot Vmax\_PYK \cdot \frac{[\text{ADP}]}{km\text{ADP\_PYK}} \cdot \frac{[\text{PEP}]}{km\text{PEP\_PYK}}}{\left(1 + \frac{[\text{ADP}]}{km\text{ADP\_PYK}}\right) \cdot \left(1 + \frac{[\text{PEP}]}{km\text{PEP\_PYK}}\right) + \left(1 + \frac{[\text{ATP}]}{km\text{ATP\_PYK}}\right) \cdot \left(1 + \frac{[\text{PYR}]}{km\text{PYR\_PYK}}\right) - 1}$$

#### 5.10 Function definition function\_4\_LDH

Name function\_4\_LDH

**Arguments** [FBP], [Lactate], [NAD], [NADH], [PYR], [Pint], Vmax\_LDH, kaFBP\_LDH, kiPint\_LDH, kmLactate\_LDH, kmNADH\_LDH, kmNAD\_LDH, kmPYR\_LDH

#### **Mathematical Expression**

$$\frac{\frac{[FBP]}{[FBP]+kaFBP\_LDH} \cdot \frac{kiPint\_LDH}{[Pint]+kiPint\_LDH} \cdot Vmax\_LDH \cdot \frac{[PYR]}{kmPYR\_LDH} \cdot \frac{[NADH]}{kmNADH\_LDH}}{\left(1 + \frac{[PYR]}{kmPYR\_LDH}\right) \cdot \left(1 + \frac{[NADH]}{kmNADH\_LDH}\right) + \left(1 + \frac{[Lactate]}{kmLactate\_LDH}\right) \cdot \left(1 + \frac{[NAD]}{kmNADL\_DH}\right) - 1}$$

$$(10)$$

#### 5.11 Function definition function\_4\_PFL

Name function\_4\_PFL

**Arguments** [AcetCoA], [CoA], [Formate], [G3P], Keq\_PFL, KmCoA\_PFL, [PYR], Vmax\_PFL, kiG3P\_PFL, kmAcetCoA\_PFL, kmFormate\_PFL, kmPYR\_PFL

#### **Mathematical Expression**

$$\frac{\frac{\text{kiG3P\_PFL}}{[G3P] + \text{kiG3P\_PFL}} \cdot \left(\text{Vmax\_PFL} \cdot \frac{[\text{PYR}]}{\text{kmPYR\_PFL}} \cdot \frac{[\text{CoA}]}{\text{KmCoA\_PFL}} - \frac{\text{Vmax\_PFL}}{\text{Keq\_PFL}} \cdot \frac{[\text{AcetCoA}]}{\text{kmPYR\_PFL}} \cdot \frac{[\text{Formate}]}{\text{KmCoA\_PFL}}\right)}{\left(1 + \frac{[\text{PYR}]}{\text{kmPYR\_PFL}}\right) \cdot \left(1 + \frac{[\text{CoA}]}{\text{KmCoA\_PFL}}\right) + \left(1 + \frac{[\text{AcetCoA}]}{\text{kmAcetCoA\_PFL}}\right) \cdot \left(1 + \frac{[\text{Formate}]}{\text{kmFormate\_PFL}}\right) - 1} \right)}$$

$$(11)$$

#### **5.12 Function definition** function\_4\_AE

Name function\_4\_AE

**Arguments** [ATP], [AcetCoA], [CoA], [Ethanol], [NAD], [NADH], Vmax\_AE, kiATP\_AE, kmAcetCoA\_AE, kmCoA\_AE, kmEthanol\_AE, kmNADH\_AE, kmNAD\_AE

#### **Mathematical Expression**

$$\frac{\frac{\text{kiATP\_AE}}{[\text{ATP}] + \text{kiATP\_AE}} \cdot \text{Vmax\_AE} \cdot \frac{[\text{AcetCoA}]}{\text{kmAcetCoA\_AE}} \cdot \left(\frac{[\text{NADH}]}{\text{kmNADH\_AE}}\right)^2}{\left(1 + \frac{[\text{NADH}]}{\text{kmNADH\_AE}} + \left(\frac{[\text{NADH}]}{\text{kmNADH\_AE}}\right)^2\right) \cdot \left(1 + \frac{[\text{AcetCoA}]}{\text{kmAcetCoA\_AE}}\right) + \left(1 + \frac{[\text{Ethanol}]}{\text{kmEthanol\_AE}}\right) \cdot \left(1 + \frac{[\text{CoA}]}{\text{kmCoA\_AE}}\right) \cdot \left(1 + \frac{[\text{NADH}]}{\text{kmNADA\_AE}}\right)}$$

#### 5.13 Function definition function\_4\_ACK

Name function\_4\_ACK

**Arguments** [ADP], [ATP], [AcetCoA], [Acetate], [CoA], Vmax\_ACK, kmADP\_ACK, kmATP\_ACK, kmAcetCoA\_ACK, kmAcetate\_ACK, kmCoA\_ACK

#### **Mathematical Expression**

$$\frac{V \text{max\_ACK} \cdot \frac{[\text{AcetCoA}]}{km\text{AcetCoA\_ACK}} \cdot \frac{[\text{ADP}]}{km\text{ADP\_ACK}}}{\left(1 + \frac{[\text{AcetCoA}]}{km\text{AcetCoA\_ACK}}\right) \cdot \left(1 + \frac{[\text{ADP}]}{km\text{ADP\_ACK}}\right) + \left(1 + \frac{[\text{Acetate}]}{km\text{Acetate\_ACK}}\right) \cdot \left(1 + \frac{[\text{ATP}]}{km\text{ATP\_ACK}}\right) \cdot \left(1 + \frac{[\text{CoA}]}{km\text{CoA\_ACK}}\right) - 1}$$

#### **5.14 Function definition** function\_4\_ALS

Name function\_4\_ALS

Arguments [Acetoin], Keq\_ALS, [PYR], Vmax\_ALS, kmAcetoin\_ALS, kmPYR\_ALS

$$\frac{V max\_ALS \cdot \left(\frac{[PYR]}{kmPYR\_ALS}\right)^2 - \frac{V max\_ALS}{Keq\_ALS} \cdot \frac{[Acetoin]}{kmPYR\_ALS}}{1 + \frac{[PYR]}{kmPYR\_ALS} + \left(\frac{[PYR]}{kmPYR\_ALS}\right)^2 + 1 + \frac{[Acetoin]}{kmAcetoin\_ALS} - 1}$$
(14)

## **5.15 Function definition** function\_4\_BDH

Name function\_4\_BDH

**Arguments** [Acetoin], [Butanediol], Keq\_BDH, [NAD], [NADH], Vmax\_BDH, kmAcetoin\_BDH, kmButanediol\_BDH, kmNADH\_BDH, kmNAD\_BDH

#### **Mathematical Expression**

$$\frac{V max\_BDH \cdot \frac{[Acetoin]}{kmAcetoin\_BDH} \cdot \frac{[NADH]}{kmNADH\_BDH} - \frac{V max\_BDH}{Keq\_BDH} \cdot \frac{[Butanediol]}{kmAcetoin\_BDH} \cdot \frac{[NAD]}{kmNADH\_BDH}}{\left(1 + \frac{[Acetoin]}{kmAcetoin\_BDH}\right) \cdot \left(1 + \frac{[NADH]}{kmNADH\_BDH}\right) + \left(1 + \frac{[Butanediol]}{kmButanediol\_BDH}\right) \cdot \left(1 + \frac{[NAD]}{kmNAD\_BDH}\right) - 1}$$

$$(15)$$

#### **5.16 Function definition** function\_4\_MPD

Name function\_4\_MPD

**Arguments** [F6P], Keq\_MPD, [Mannitol1Phosphate], [NAD], [NADH], Vmax\_MPD, kiF6P\_MPD, kmF6P\_MPD, kmNADH\_MPD, kmNADH\_MPD

#### **Mathematical Expression**

$$\frac{\frac{\text{kiF6P\_MPD}}{[\text{F6P}] + \text{kiF6P\_MPD}} \cdot \left(\text{Vmax\_MPD} \cdot \frac{[\text{F6P}]}{\text{kmF6P\_MPD}} \cdot \frac{[\text{NADH}]}{\text{kmNADH\_MPD}} - \frac{\text{Vmax\_MPD}}{\text{Keq\_MPD}} \cdot \frac{[\text{Mannitol1Phosphate}]}{\text{kmF6P\_MPD}} \cdot \frac{[\text{NAD}]}{\text{kmNADH\_MPD}} \right)}{\left(1 + \frac{[\text{F6P}]}{\text{kmF6P\_MPD}}\right) \cdot \left(1 + \frac{[\text{NADH}]}{\text{kmNADH\_MPD}}\right) + \left(1 + \frac{[\text{Mannitol1Phosphate}]}{\text{kmMannitol1Phosphate}}\right) \cdot \left(1 + \frac{[\text{NAD}]}{\text{kmNAD\_MPD}}\right) - 1}$$

#### **5.17 Function definition** function\_4\_MP

Name function\_4\_MP

Arguments [Mannitol], [Mannitol1Phosphate], Vmax\_MP, kmMannitol1Phosphate\_MP, kmMannitol\_MP

#### **Mathematical Expression**

$$\frac{Vmax\_MP \cdot \frac{[Mannitol1Phosphate]}{kmMannitol1Phosphate\_MP}}{1 + \frac{[Mannitol1Phosphate]}{kmMannitol1Phosphate\_MP} + 1 + \frac{[Mannitol]}{kmMannitol\_MP} - 1}$$

$$(17)$$

## **5.18 Function definition** function\_4\_PTS\_Man

Name function\_4\_PTS\_Man

**Arguments** [Mannitol1Phosphate], [Mannitol\_Ext], [PEP], [PYR], Vmax\_PTS\_Man, kmMannitol1Phosphate\_PTS\_Nan, kmPYR\_PTS\_Man, kmPYR\_PTS\_Man

$$\frac{Vmax\_PTS\_Man \cdot \frac{[Mannitol\_Ext]}{kmMannitolExt\_PTS\_Man} \cdot \frac{[PEP]}{kmPEP\_PTS\_Man}}{\left(1 + \frac{[Mannitol\_Ext]}{kmMannitolExt\_PTS\_Man}\right) \cdot \left(1 + \frac{[PEP]}{kmPEP\_PTS\_Man}\right) + \left(1 + \frac{[Mannitol1Phosphate]}{kmMannitol1Phosphate\_PTS\_Man}\right) \cdot \left(1 + \frac{[PYR]}{kmPYR\_PTS\_Man}\right) - 1}$$

## **5.19 Function definition** function\_4\_Acetoin\_transp

Name function\_4\_Acetoin\_transp

Arguments [Acetoin\_Ext], Vmax\_Acetoin\_transp, kmAcetoin\_transp, kmAcetoin\_Ext\_Acetoin\_transp, kmAcetoin\_Ext\_Acetoin\_transp

#### **Mathematical Expression**

$$\frac{Vmax\_Acetoin\_transp \cdot \frac{[Acetoin]}{kmAcetoin\_Acetoin\_transp}}{1 + \frac{[Acetoin]}{kmAcetoin\_Acetoin\_transp} + \frac{[Acetoin\_Ext]}{kmAcetoin\_Ext\_Acetoin\_transp}}$$

$$(19)$$

## **5.20 Function definition** function\_4\_Mannitol\_transp

Name function\_4\_Mannitol\_transp

**Arguments** [Mannitol], [Mannitol\_Ext], Vmax\_Mannitol\_transp, kmMannitol\_Ext\_Mannitol\_transp, kmMannitol\_Mannitol\_transp

## **Mathematical Expression**

$$\frac{Vmax\_Mannitol\_transp \cdot \frac{[Mannitol]}{kmMannitol\_Mannitol\_transp}}{1 + \frac{[Mannitol]}{kmMannitol\_Mannitol\_transp} + \frac{[Mannitol\_Ext]}{kmMannitol\_Ext\_Mannitol\_transp}}$$

$$(20)$$

#### **5.21 Function definition** function\_4\_FBPase

Name function\_4\_FBPase

Arguments [F6P], [FBP], [Pint], Vmax\_FBPase, kmF6P\_FBPase, kmFBP\_FBPase, kmPint\_FBPase

$$\frac{Vmax\_FBPase \cdot \frac{[FBP]}{kmFBP\_FBPase}}{\frac{[FBP]}{kmFBP\_FBPase} + \left(1 + \frac{[F6P]}{kmF6P\_FBPase}\right) \cdot \left(1 + \frac{[Pint]}{kmPint\_FBPase}\right)} \tag{21}$$

12

## 6 Reactions

This model contains 21 reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 4: Overview of all reactions

No	Id	Name	Reaction Equation	SBO
1	re12	PTS_Glc	Glucose + PEP FBP, Pint, FBP, G6P, CPYR	Glucose, PEP, PYR, Pint G6P+
2	re13	ATPase	$ATP \xrightarrow{ATP} ADP + Pint$	
3	re14	P_transp	Pext + ATP Pint, ADP, ATP, Pext, P	$\stackrel{\text{lint}}{\longrightarrow} 2  \text{Pint} +$
			ADP	
4	re15	PGI	$G6P \xrightarrow{F6P, G6P} F6P$	
5	re16	PFK	$F6P + ATP \xrightarrow{ADP, ATP, F6P, FBP} FBP$	+ ADP
6	re17	FBA	$FBP \xrightarrow{FBP, G3P} 2G3P$	
7	re18	GAPDH	$G3P + Pint + NAD = \frac{BPG, G3P, NAD, NAD}{Pint}$ $NADH$	NADH, Pint BPG+
8	re20	ENO	$BPG + ADP \xrightarrow{ADP, ATP, BPG, PEP} PI$	EP + ATP
9	re21	PYK	PEP+ADP FBP, Pint, ADP, ATP, FBI	$P, PEP, PYR, Pint \rightarrow PYR +$
			ATP	
10	re22	LDH	PYR+NADH FBP, Pint, FBP, Lactate	$\underbrace{P, NAD, NADH, PYR, Pint}_{Lact}$ Lact
			NAD	
11	re23	PDH	$PYR + CoA \leftarrow G3P, AcetCoA, CoA, For$	mate, G3P, PYR AcetCoA+
			Formate	

N⁰	Id	Name	Reaction Equation SBO	
12	re24	AE	AcetCoA + 2 NADH ATP, ATP, AcetCoA, CoA, Ethanol, NAD, NADH 2 NAD + CoA	Ethanol+
13	re25	AC	AcetCoA + ADP $\xrightarrow{\text{ADP, ATP, AcetCoA, Acetate, CoA}}$ Acetate + ATP + CoA	
14	re26	PA	2 PYR Acetoin, PYR Acetoin	
15	re27	AB	Acetoin + NADH Acetoin, Butanediol, NAD, NADH Butanediol +	
16	re28	MPD	NAD F6P+NADH F6P, F6P, Mannitol1Phosphate, NAD, NADH NAD Mannitol1F	Phosphate+
17	re29	MP	Mannitol1Phosphate Mannitol, Mannitol1Phosphate Mannitol	
18	re30	PTS_Man	Mannitol_Ext+PEP Mannitol1Phosphate, Mannitol_Ext, PEP, PYR PYR  Mannitol_Ext+PEP Mannitol1Phosphate, Mannitol_Ext, PEP, PYR	nnitol1Phosph
19	re31	Acetoin_transp	Acetoin Acetoin Acetoin Ext Acetoin Ext	
20	re32	Mannitol_transp	Mannitol Mannitol Ext Mannitol Ext	
21	re33	FBPase	$FBP \xrightarrow{F6P, FBP, Pint} F6P + Pint$	

## **6.1 Reaction** re12

This is an irreversible reaction of two reactants forming two products influenced by eight modifiers.

Name PTS\_Glc

## **Reaction equation**

$$Glucose + PEP \xrightarrow{FBP, Pint, FBP, G6P, Glucose, PEP, PYR, Pint} G6P + PYR$$
 (22)

#### **Reactants**

Table 5: Properties of each reactant.

Id	Name	SBO
Glucose		
PEP	PEP	

#### **Modifiers**

Table 6: Properties of each modifier.

Id	Name	SBO
FBP	FBP	
Pint	Pint	
FBP	FBP	
G6P	G6P	
Glucose	Glucose	
PEP	PEP	
PYR	PYR	
Pint	Pint	

#### **Products**

Table 7: Properties of each product.

Id	Name	SBO
G6P	G6P	
PYR	PYR	

#### **Kinetic Law**

#### **Derived unit** contains undeclared units

$$v_1 = \text{function\_4\_PTS\_Glc}([FBP], [G6P], [Glucose], [PEP], [PYR], [Pint], Vmax\_PTS\_Glc, \\ kaPint\_PTS\_Glc, kiFBP\_PTS\_Glc, kmG6P\_PTS\_Glc, kmGlucose\_PTS\_Glc, \\ kmPEP\_PTS\_Glc, kmPYR\_PTS\_Glc)$$
 (23)

$$= \frac{\frac{[Pint]}{[Pint] + kaPint\_PTS\_Glc} \cdot \frac{kiFBP\_PTS\_Glc}{[FBP] + kiFBP\_PTS\_Glc} \cdot Vmax\_PTS\_Glc \cdot \frac{[Glucose]}{kmGlucose\_PTS\_Glc} \cdot \frac{[PEP]}{kmPEP\_PTS\_Glc}}{\left(1 + \frac{[Glucose]}{kmGlucose\_PTS\_Glc}\right) \cdot \left(1 + \frac{[PEP]}{kmPEP\_PTS\_Glc}\right) + \left(1 + \frac{[G6P]}{kmG6P\_PTS\_Glc}\right) \cdot \left(1 + \frac{[PYR]}{kmPYR\_PTS\_Glc}\right) - 1}$$

Table 8: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax_PTS_Glc	Vmax_PTS_Glc		3.711		
kaPint_PTS-	kaPint_PTS_Glc		0.071		$\square$
_Glc					
kiFBP_PTS-	kiFBP_PTS_Glc		1.169		
_Glc					
$kmG6P_PTS-$	kmG6P_PTS_Glc		0.285		$\square$
_Glc					
kmGlucose-	kmGlucose_PTS-		0.049		$\square$
_PTS_Glc	_Glc				
kmPEP_PTS-	kmPEP_PTS_Glc		0.306		
_Glc					
kmPYR_PTS-	kmPYR_PTS_Glc		1.960		
_Glc					_

#### 6.2 Reaction re13

This is an irreversible reaction of one reactant forming two products influenced by one modifier.

Name ATPase

## **Reaction equation**

$$ATP \xrightarrow{ATP} ADP + Pint$$
 (25)

#### Reactant

Table 9: Properties of each reactant.

Id	Name	SBO
ATP	ATP	

#### **Modifier**

Table 10: Properties of each modifier.

Id	Name	SBO
ATP	ATP	

#### **Products**

Table 11: Properties of each product.

Id	Name	SBO
ADP	ADP	
Pint	Pint	

#### **Kinetic Law**

## Derived unit contains undeclared units

$$v_2 = \text{vol (compartment\_1)}$$
  
· function\_4\_ATPase ([ATP], Vmax\_ATPase, kmATP\_ATPase, nATPase) (26)

 $function\_4\_ATPase \, ([ATP], Vmax\_ATPase, kmATP\_ATPase, nATPase)$ 

$$= V_{\text{max\_ATPase}} \cdot \frac{\left(\frac{[\text{ATP}]}{\text{kmATP\_ATPase}}\right)^{\text{nATPase}}}{\left(\frac{[\text{ATP}]}{\text{kmATP\_ATPase}}\right)^{\text{nATPase}}} + 1$$
(27)

 $function\_4\_ATPase ([ATP], Vmax\_ATPase, kmATP\_ATPase, nATPase)$ 

$$= V_{\text{max\_ATPase}} \cdot \frac{\left(\frac{[\text{ATP}]}{\text{kmATP\_ATPase}}\right)^{\text{nATPase}}}{\left(\frac{[\text{ATP}]}{\text{kmATP\_ATPase}}\right)^{\text{nATPase}} + 1}$$
(28)

Table 12: Properties of each parameter.

Id	Name	SBO Value	Unit Constant
Vmax_ATPase	Vmax_ATPase kmATP_ATPase	3.290 4.342	Ø Ø
nATPase	nATPase	3.000	<b>v</b> <b>v</b>

## 6.3 Reaction re14

This is an irreversible reaction of two reactants forming two products influenced by five modifiers.

## Name P\_transp

## **Reaction equation**

$$Pext + ATP \xrightarrow{Pint, ADP, ATP, Pext, Pint} 2 Pint + ADP$$
 (29)

## Reactants

Table 13: Properties of each reactant.

Id	Name	SBO
Pext	Pext	
ATP	ATP	

## **Modifiers**

Table 14: Properties of each modifier.

Id	Name	SBO
Pint	Pint	
ADP	ADP	
ATP	ATP	
Pext	Pext	
Pint	Pint	

## **Products**

Table 15: Properties of each product.

Name	SBO
	Pint ADP

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_3 = function\_4\_P\_transp([ADP], [ATP], [Pext], [Pint], Vmax\_Ptransport, kiPint\_Ptransport, kmADP\_Ptransport, kmATP\_Ptransport, kmPext\_Ptransport, kmPint\_Ptransport)$$

$$(30)$$

function\_4\_P\_transp ([ADP], [ATP], [Pext], [Pint], Vmax\_Ptransport, kiPint\_Ptransport, kmADP\_Ptransport, kmATP\_Ptransport, kmPext\_Ptransport, kmPint\_Ptransport) (31)

$$= \frac{\frac{\text{kiPint\_Ptransport}}{\text{kiPint\_Ptransport}} \cdot \text{Vmax\_Ptransport} \cdot \frac{\text{[ATP]}}{\text{kmATP\_Ptransport}} \cdot \frac{\text{[Pext]}}{\text{kmPext\_Ptransport}} \cdot \frac{\text{[Pext]}}{\text{kmPext\_Ptransport}}}{\left(1 + \frac{\text{[Pext]}}{\text{kmPext\_Ptransport}}\right) \cdot \left(1 + \frac{\text{[ATP]}}{\text{kmATP\_Ptransport}}\right) + \left(1 + \frac{\text{[Pint]}}{\text{kmPint\_Ptransport}} + \left(\frac{\text{[Pint]}}{\text{kmPint\_Ptransport}}\right)^2\right) \cdot \left(1 + \frac{\text{[ADP]}}{\text{kmADP\_Ptransport}}\right)}$$

Table 16: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax-	Vmax_Ptransport		3.596		$\blacksquare$
$_{ t L}$ Ptransport					
kiPint-	kiPint_Ptransport		0.561		
$_{ extsf{L}}$ Ptransport					
kmADP-	kmADP_Ptransport		0.192		
$_{ m L}$ Ptransport					
kmATP-	kmATP_Ptransport		0.523		
$_{ t L}$ Ptransport					
kmPext-	kmPext_Ptransport		0.750		
$_{ t L}$ Ptransport					
kmPint-	kmPint_Ptransport		0.303		
$_{ m LPtransport}$	_				_

## 6.4 Reaction re15

This is a reversible reaction of one reactant forming one product influenced by two modifiers.

Name PGI

## **Reaction equation**

$$G6P \xrightarrow{F6P, G6P} F6P \tag{32}$$

## Reactant

Table 17: Properties of each reactant.

Id	Name	SBO
G6P	G6P	

#### **Modifiers**

Table 18: Properties of each modifier.

Id	Name	SBO
F6P	F6P	
G6P	G6P	

#### **Product**

Table 19: Properties of each product.

	•	
Id	Name	SBO
F6P	F6P	

#### **Kinetic Law**

#### **Derived unit** contains undeclared units

$$v_4 = \text{vol} (\text{compartment\_1})$$
  
 $\cdot \text{function\_4\_PGI} ([\text{F6P}], [\text{G6P}], \text{Keq\_PGI}, \text{Vmax\_PGI}, \text{kmF6P\_PGI}, \text{kmG6P\_PGI})$ 
(33)

 $function\_4\_PGI([F6P],[G6P],Keq\_PGI,Vmax\_PGI,kmF6P\_PGI,kmG6P\_PGI)$ 

$$= \frac{V_{\text{max}} PGI \cdot \frac{[G6P]}{kmG6P PGI} - \frac{V_{\text{max}} PGI}{keq PGI} \cdot \frac{[F6P]}{kmG6P PGI}}{1 + \frac{[G6P]}{kmG6P PGI} + \frac{[F6P]}{kmF6P PGI}}$$
(34)

function\_4\_PGI([F6P], [G6P], Keq\_PGI, Vmax\_PGI, kmF6P\_PGI, kmG6P\_PGI)

$$= \frac{V_{\text{max}}PGI \cdot \frac{[G6P]}{kmG6P} - \frac{V_{\text{max}}PGI}{Keq} \cdot \frac{[F6P]}{kmG6P}}{1 + \frac{[G6P]}{kmG6P} + \frac{[F6P]}{kmF6P}}$$
(35)

Table 20: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
Keq_PGI	Keq_PGI	0.430	$\overline{Z}$
${\tt Vmax\_PGI}$	Vmax_PGI	21.681	
kmF6P_PGI	kmF6P_PGI	3.139	
$kmG6P\_PGI$	kmG6P_PGI	0.199	$\checkmark$

## 6.5 Reaction re16

This is an irreversible reaction of two reactants forming two products influenced by four modifiers.

#### Name PFK

## **Reaction equation**

$$F6P + ATP \xrightarrow{ADP, ATP, F6P, FBP} FBP + ADP$$
 (36)

#### **Reactants**

Table 21: Properties of each reactant.

Id	Name	SBO
F6P	F6P	
ATP	ATP	

#### **Modifiers**

Table 22: Properties of each modifier.

Id	Name	SBO
ADP	ADP	
ATP	ATP	
F6P	F6P	
FBP	FBP	

## **Products**

Table 23: Properties of each product.

Id	Name	SBO
FBP	FBP	
ADP	ADP	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_5 = \text{vol} (\text{compartment\_1}) \cdot \text{function\_4\_PFK} ([\text{ADP}], [\text{ATP}], [\text{F6P}], [\text{FBP}], \text{Vmax\_PFK}, \\ \text{kmADP\_PFK}, \text{kmATP\_PFK}, \text{kmF6P\_PFK}, \text{kmFBP\_PFK})$$
(37)

function\_4\_PFK ([ADP], [ATP], [F6P], [FBP], Vmax\_PFK, kmADP\_PFK, kmATP\_PFK, kmF6P\_PFK, kmFBP\_PFK)

$$= \frac{V_{\text{max\_PFK}} \cdot \frac{[\text{F6P}]}{km\text{F6P\_PFK}} \cdot \frac{[\text{ATP}]}{km\text{ATP\_PFK}}}{\left(1 + \frac{[\text{F6P}]}{km\text{F6P\_PFK}}\right) \cdot \left(1 + \frac{[\text{ATP}]}{km\text{ATP\_PFK}}\right) + \left(1 + \frac{[\text{FBP}]}{km\text{FBP\_PFK}}\right) \cdot \left(1 + \frac{[\text{ADP}]}{km\text{ADP\_PFK}}\right) - 1}$$
(38)

function\_4\_PFK ([ADP], [ATP], [F6P], [FBP], Vmax\_PFK, kmADP\_PFK, kmATP\_PFK, kmF6P\_PFK, kmFBP\_PFK)

$$= \frac{\text{Vmax\_PFK} \cdot \frac{[\text{F6P}]}{\text{kmF6P\_PFK}} \cdot \frac{[\text{ATP}]}{\text{kmATP\_PFK}}}{\left(1 + \frac{[\text{F6P}]}{\text{kmF6P\_PFK}}\right) \cdot \left(1 + \frac{[\text{ATP}]}{\text{kmATP\_PFK}}\right) + \left(1 + \frac{[\text{FBP}]}{\text{kmFBP\_PFK}}\right) \cdot \left(1 + \frac{[\text{ADP}]}{\text{kmADP\_PFK}}\right) - 1}$$
(39)

Table 24: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax_PFK	Vmax_PFK		18.358		$\overline{Z}$
$kmADP\_PFK$	kmADP_PFK		10.736		
$kmATP\_PFK$	kmATP_PFK		0.062		
$kmF6P\_PFK$	kmF6P_PFK		1.020		$\overline{\checkmark}$
kmFBP_PFK	kmFBP_PFK		86.805		<u> </u>

#### 6.6 Reaction re17

This is a reversible reaction of one reactant forming one product influenced by two modifiers.

#### Name FBA

#### **Reaction equation**

$$FBP \xrightarrow{FBP, G3P} 2G3P \tag{40}$$

#### Reactant

Table 25: Properties of each reactant.

Id	Name	SBO
FBP	FBP	

#### **Modifiers**

Table 26: Properties of each modifier.

Id	Name	SBO
FBP	FBP	
G3P	G3P	

#### **Product**

Table 27: Properties of each product.

Id	Name	SBO
G3P	G3P	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$\begin{array}{c} \nu_6 = vol \, (compartment\_1) \cdot function\_4\_FBA \, ([FBP], [G3P], Keq\_FBA, Vmax\_FBA, \\ kmFBP\_FBA, kmG3P\_FBA) \end{array}$$

 $function\_4\_FBA ([FBP], [G3P], Keq\_FBA, Vmax\_FBA, kmFBP\_FBA, kmG3P\_FBA)$ 

$$= \frac{\text{Vmax\_FBA} \cdot \frac{[\text{FBP}]}{\text{kmFBP\_FBA}} - \frac{\text{Vmax\_FBA}}{\text{Keq\_FBA}} \cdot \frac{[\text{G3P}]^2}{\text{kmFBP\_FBA}}}{1 + \frac{[\text{FBP}]}{\text{kmFBP\_FBA}} + \frac{[\text{G3P}]}{\text{kmG3P\_FBA}} + \left(\frac{[\text{G3P}]}{\text{kmG3P\_FBA}}\right)^2}$$

$$(42)$$

 $function\_4\_FBA ([FBP], [G3P], Keq\_FBA, Vmax\_FBA, kmFBP\_FBA, kmG3P\_FBA)$ 

$$= \frac{\text{Vmax}.\text{FBA} \cdot \frac{[\text{FBP}]}{\text{kmFBP}.\text{FBA}} - \frac{\text{Vmax}.\text{FBA}}{\text{Keq}.\text{FBA}} \cdot \frac{[\text{G3P}]^2}{\text{kmFBP}.\text{FBA}}}{1 + \frac{[\text{FBP}]}{\text{kmFBP}.\text{FBA}} + \frac{[\text{G3P}]}{\text{kmG3P}.\text{FBA}} + \left(\frac{[\text{G3P}]}{\text{kmG3P}.\text{FBA}}\right)^2}$$

$$(43)$$

Table 28: Properties of each parameter.

Id	Name	SBO Value	Unit	Constant
Keq_FBA	Keq_FBA	0.056		$\overline{Z}$
${\tt Vmax\_FBA}$	Vmax_FBA	56.131		$\square$
$kmFBP\_FBA$	kmFBP_FBA	0.301		
${\tt kmG3P\_FBA}$	kmG3P_FBA	10.106		

#### 6.7 Reaction re18

This is a reversible reaction of three reactants forming two products influenced by five modifiers.

## Name GAPDH

## **Reaction equation**

$$G3P + Pint + NAD \xrightarrow{BPG, G3P, NAD, NADH, Pint} BPG + NADH$$
 (44)

#### **Reactants**

Table 29: Properties of each reactant.

Id	Name	SBO
G3P	G3P	
Pint	Pint	
NAD	NAD	

## **Modifiers**

Table 30: Properties of each modifier.

Id	Name	SBO
BPG	BPG	
G3P	G3P	
NAD	NAD	

Id	Name	SBO
NADH	NADH	
Pint	Pint	

#### **Products**

Table 31: Properties of each product.

Id	Name	SBO
BPG	BPG	
NADH	NADH	

#### **Kinetic Law**

#### Derived unit contains undeclared units

$$v_7 = vol (compartment\_1) \cdot function\_4\_GAPDH ([BPG], [G3P], Keq\_GAPDH, [NAD], [NADH], \\ [Pint], Vmax\_GAPDH, kmBPG\_GAPDH, kmG3P\_GAPDH, kmNADH\_GAPDH, \\ kmNAD\_GAPDH, kmPint\_GAPDH)$$
 (45)

$$kmNAD\_GAPDH, kmPint\_GAPDH) = \frac{Vmax\_GAPDH \cdot \frac{[G3P]}{kmG3P\_GAPDH} \cdot \frac{[NAD]}{kmNAD\_GAPDH} \cdot \frac{[Pint]}{kmPint\_GAPDH} - \frac{Vmax\_GAPDH}{Keq\_GAPDH}}{\left(1 + \frac{[G3P]}{kmG3P\_GAPDH}\right) \cdot \left(1 + \frac{[Pint]}{kmPint\_GAPDH}\right) \cdot \left(1 + \frac{[NAD]}{kmNAD\_GAPDH}\right) + \left(1 + \frac{[NAD]}{kmNAD\_GAPDH}\right)}$$

$$kmNAD\_GAPDH, kmPint\_GAPDH) = \frac{Vmax\_GAPDH \cdot \frac{[G3P]}{kmG3P\_GAPDH} \cdot \frac{[NAD]}{kmNAD\_GAPDH} \cdot \frac{[Pint]}{kmPint\_GAPDH} - \frac{Vmax\_GAPDH}{Keq\_GAPDH}}{\left(1 + \frac{[G3P]}{kmG3P\_GAPDH}\right) \cdot \left(1 + \frac{[Pint]}{kmPint\_GAPDH}\right) \cdot \left(1 + \frac{[NAD]}{kmNAD\_GAPDH}\right) + \left(1 + \frac{[NAD]}{kmNAD\_GAPDH}\right)}$$

Table 32: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
${\tt Keq\_GAPDH}$	Keq_GAPDH		$7 \cdot 10^{-4}$		Ø
${\tt Vmax\_GAPDH}$	Vmax_GAPDH		30.006		
${\tt kmBPG\_GAPDH}$	$kmBPG\_GAPDH$		0.048		$\square$
${\tt kmG3P\_GAPDH}$	kmG3P_GAPDH		0.182		$\square$

Id	Name	SBO	Value	Unit	Constant
kmNADH_GAPDH	kmNADH-		0.643		
kmNAD_GAPDH	_GAPDH kmNAD_GAPDH		0.048		<b>√</b>
kmPint_GAPDH	kmPint_GAPDH		6.753		<b>Z</b>

## 6.8 Reaction re20

This is a reversible reaction of two reactants forming two products influenced by four modifiers.

#### Name ENO

## **Reaction equation**

$$BPG + ADP \xrightarrow{ADP, ATP, BPG, PEP} PEP + ATP$$
 (48)

#### **Reactants**

Table 33: Properties of each reactant.

Id	Name	SBO
BPG	BPG	
ADP	ADP	

#### **Modifiers**

Table 34: Properties of each modifier.

Id	Name	SBO
ADP	ADP	
ATP	ATP	
BPG	BPG	
PEP	PEP	

#### **Products**

Table 35: Properties of each product.

Id	Name	SBO
PEP	PEP	
ATP	ATP	

Id	Name	SBO

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_8 = \text{vol} (\text{compartment\_1}) \cdot \text{function\_4\_ENO} ([\text{ADP}], [\text{ATP}], [\text{BPG}], \text{Keq\_ENO}, [\text{PEP}], \\ \text{Vmax\_ENO}, \text{kmADP\_ENO}, \text{kmATP\_ENO}, \text{kmBPG\_ENO}, \text{kmPEP\_ENO})$$
(49)

function\_4\_ENO([ADP], [ATP], [BPG], Keq\_ENO, [PEP], Vmax\_ENO, kmADP\_ENO, kmATP\_ENO, kmBPG\_ENO, kmPEP\_ENO)

$$= \frac{\text{Vmax\_ENO} \cdot \frac{[\text{BPG}]}{\text{kmBPG\_ENO}} \cdot \frac{[\text{ADP}]}{\text{kmADP\_ENO}} - \frac{\text{Vmax\_ENO}}{\text{Keq\_ENO}} \cdot \frac{[\text{PEP}]}{\text{kmBPG\_ENO}} \cdot \frac{[\text{ATP}]}{\text{kmADP\_ENO}}}{\left(1 + \frac{[\text{BPG}]}{\text{kmBPG\_ENO}}\right) \cdot \left(1 + \frac{[\text{ADP}]}{\text{kmADP\_ENO}}\right) + \left(1 + \frac{[\text{PEP}]}{\text{kmPEP\_ENO}}\right) \cdot \left(1 + \frac{[\text{ATP}]}{\text{kmATP\_ENO}}\right) - 1}}$$
(50)

function\_4\_ENO ([ADP], [ATP], [BPG], Keq\_ENO, [PEP], Vmax\_ENO, kmADP\_ENO, kmATP\_ENO, kmBPG\_ENO, kmPEP\_ENO)

$$= \frac{\text{Vmax\_ENO} \cdot \frac{[\text{BPG}]}{\text{kmBPG\_ENO}} \cdot \frac{[\text{ADP}]}{\text{kmADP\_ENO}} - \frac{\text{Vmax\_ENO}}{\text{Keq\_ENO}} \cdot \frac{[\text{PEP}]}{\text{kmBPG\_ENO}} \cdot \frac{[\text{ATP}]}{\text{kmADP\_ENO}}}{\left(1 + \frac{[\text{BPG}]}{\text{kmBPG\_ENO}}\right) \cdot \left(1 + \frac{[\text{ADP}]}{\text{kmADP\_ENO}}\right) + \left(1 + \frac{[\text{PEP}]}{\text{kmPEP\_ENO}}\right) \cdot \left(1 + \frac{[\text{ATP}]}{\text{kmATP\_ENO}}\right) - 1}}$$
(51)

Table 36: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
Keq_ENO	Keq_ENO	27.550	Ø
$Vmax\_ENO$	Vmax_ENO	29.132	
kmADP_ENO	kmADP_ENO	0.413	
$kmATP\_ENO$	kmATP_ENO	0.748	
$kmBPG\_ENO$	kmBPG_ENO	0.024	
kmPEP_ENO	kmPEP_ENO	1.389	$\square$

#### 6.9 Reaction re21

This is an irreversible reaction of two reactants forming two products influenced by eight modifiers.

#### Name PYK

## **Reaction equation**

$$PEP + ADP \xrightarrow{FBP, Pint, ADP, ATP, FBP, PEP, PYR, Pint} PYR + ATP$$
 (52)

#### **Reactants**

Table 37: Properties of each reactant.

Id	Name	SBO
PEP	PEP	
ADP	ADP	

#### **Modifiers**

Table 38: Properties of each modifier.

Id	Name	SBO
FBP	FBP	
Pint	Pint	
ADP	ADP	
ATP	ATP	
FBP	FBP	
PEP	PEP	
PYR	PYR	
Pint	Pint	

#### **Products**

Table 39: Properties of each product.

Id	Name	SBO
PYR	PYR	
ATP	ATP	

## **Kinetic Law**

#### **Derived unit** contains undeclared units

function\_4\_PYK ([ADP], [ATP], [FBP], [PEP], [PYR], [Pint], Vmax\_PYK, kaFBP\_PYK, kiPint\_PYK, kmADP\_PYK, kmATP\_PYK, kmPEP\_PYK, kmPYR\_PYK, nPYK)

$$= \frac{\frac{[FBP]}{[FBP] + kaFBP\_PYK} \cdot \frac{kiPint\_PYK^{nPYK}}{[Pint]^{nPYK} + kiPint\_PYK^{nPYK}} \cdot Vmax\_PYK \cdot \frac{[ADP]}{kmADP\_PYK} \cdot \frac{[PEP]}{kmADP\_PYK}}{\left(1 + \frac{[ADP]}{kmADP\_PYK}\right) \cdot \left(1 + \frac{[PEP]}{kmPEP\_PYK}\right) + \left(1 + \frac{[ATP]}{kmATP\_PYK}\right) \cdot \left(1 + \frac{[PYR]}{kmPYR\_PYK}\right) - 1}$$
(54)

function\_4\_PYK ([ADP], [ATP], [FBP], [PEP], [PYR], [Pint], Vmax\_PYK, kaFBP\_PYK, kiPint\_PYK, kmADP\_PYK, kmATP\_PYK, kmPEP\_PYK, kmPYR\_PYK, nPYK)

$$= \frac{\frac{[\text{FBP}]}{[\text{FBP}] + \text{kaFBP\_PYK}} \cdot \frac{\text{kiPint\_PYK}^{\text{nPYK}}}{[\text{Pint}]^{\text{nPYK}} + \text{kiPint\_PYK}^{\text{nPYK}}} \cdot \text{Vmax\_PYK} \cdot \frac{[\text{ADP}]}{\text{kmADP\_PYK}} \cdot \frac{[\text{PEP}]}{\text{kmPEP\_PYK}}}{\left(1 + \frac{[\text{ADP}]}{\text{kmADP\_PYK}}\right) \cdot \left(1 + \frac{[\text{PEP}]}{\text{kmPEP\_PYK}}\right) + \left(1 + \frac{[\text{ATP}]}{\text{kmATP\_PYK}}\right) \cdot \left(1 + \frac{[\text{PYR}]}{\text{kmPYR\_PYK}}\right) - 1}$$
(55)

Table 40: Properties of each parameter.

		1			
Id	Name	SBO	Value	Unit	Constant
Vmax_PYK	Vmax_PYK		2.224		lacksquare
$kaFBP\_PYK$	kaFBP_PYK		0.039		$\square$
${\tt kiPint\_PYK}$	kiPint_PYK		3.701		
$kmADP\_PYK$	kmADP_PYK		3.077		$   \overline{\mathbf{A}} $
$kmATP\_PYK$	kmATP_PYK		29.603		$\square$
$kmPEP\_PYK$	kmPEP_PYK		0.331		
$kmPYR\_PYK$	$kmPYR\_PYK$		96.423		
nPYK	nPYK		3.000		

## 6.10 Reaction re22

This is an irreversible reaction of two reactants forming two products influenced by eight modifiers.

#### Name LDH

#### **Reaction equation**

$$PYR + NADH \xrightarrow{FBP, Pint, FBP, Lactate, NAD, NADH, PYR, Pint} Lactate + NAD \qquad (56)$$

#### **Reactants**

Table 41: Properties of each reactant.

Id	Name	SBO
PYR	PYR	
NADH	NADH	

#### **Modifiers**

Table 42: Properties of each modifier.

Id	Name	SBO
FBP	FBP	
Pint	Pint	
FBP	FBP	
Lactate	Lactate	
NAD	NAD	
NADH	NADH	
PYR	PYR	
Pint	Pint	

#### **Products**

Table 43: Properties of each product.

Id	Name	SBO
Lactate	Lactate	
NAD	NAD	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{10} = \text{function\_4\_LDH}([FBP], [Lactate], [NAD], [NADH], [PYR], [Pint], Vmax\_LDH, kaFBP\_LDH, kiPint\_LDH, kmLactate\_LDH, kmNADH_LDH, kmNAD_LDH, kmPYR\_LDH)$$
 (57)

function\_4\_LDH ([FBP], [Lactate], [NAD], [NADH], [PYR], [Pint], Vmax\_LDH, kaFBP\_LDH, kiPint\_LDH, kmLactate\_LDH, kmNADH\_LDH, kmNAD\_LDH, kmPYR\_LDH)

$$= \frac{\frac{[\text{FBP}]}{[\text{FBP}] + \text{kaFBP\_LDH}} \cdot \frac{\text{kiPint\_LDH}}{[\text{Pint}] + \text{kiPint\_LDH}} \cdot \text{Vmax\_LDH} \cdot \frac{[\text{PYR}]}{\text{kmPYR\_LDH}} \cdot \frac{[\text{NADH}]}{\text{kmNADH\_LDH}}}{\left(1 + \frac{[\text{PYR}]}{\text{kmPYR\_LDH}}\right) \cdot \left(1 + \frac{[\text{NADH}]}{\text{kmNADH\_LDH}}\right) + \left(1 + \frac{[\text{Lactate}]}{\text{kmLactate\_LDH}}\right) \cdot \left(1 + \frac{[\text{NAD}]}{\text{kmNADL\_DH}}\right) - 1}}$$
(58)

Table 44: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax_LDH	Vmax_LDH		566.598		<b></b> ✓
$kaFBP\_LDH$	kaFBP_LDH		0.018		$\overline{\mathbf{Z}}$
${\tt kiPint\_LDH}$	kiPint_LDH		0.068		$ \mathbf{Z} $
kmLactate-	kmLactate_LDH		94.120		$\overline{\mathbf{Z}}$
_LDH					
$kmNADH\_LDH$	kmNADH_LDH		0.144		
$kmNAD\_LDH$	kmNAD_LDH		3.084		$\overline{\mathbf{Z}}$
kmPYR_LDH	kmPYR_LDH		0.010		$\square$

## 6.11 Reaction re23

This is a reversible reaction of two reactants forming two products influenced by six modifiers.

#### Name PDH

## **Reaction equation**

$$PYR + CoA \xrightarrow{G3P, AcetCoA, CoA, Formate, G3P, PYR} AcetCoA + Formate$$
 (59)

#### **Reactants**

Table 4<u>5</u>: Properties of each reactant.

Id	Name	SBO
PYR	PYR	
CoA	CoA	

## **Modifiers**

Table 46: Properties of each modifier.

Id	Name	SBO
G3P	G3P	
AcetCoA	AcetCoA	
CoA	CoA	
Formate	Formate	
G3P	G3P	
PYR	PYR	

#### **Products**

Table 47: Properties of each product.

Id	Name	SBO
AcetCoA	AcetCoA	
Formate	Formate	

#### **Kinetic Law**

#### Derived unit contains undeclared units

$$v_{11} = \text{function\_4\_PFL}([\text{AcetCoA}], [\text{CoA}], [\text{Formate}], [\text{G3P}], \text{Keq\_PFL}, \text{KmCoA\_PFL}, [\text{PYR}], \\ \text{Vmax\_PFL}, \text{kiG3P\_PFL}, \text{kmAcetCoA\_PFL}, \text{kmFormate\_PFL}, \text{kmPYR\_PFL}) \\ (60)$$

$$\begin{split} & \text{function\_4\_PFL}([\text{AcetCoA}], [\text{CoA}], [\text{Formate}], [\text{G3P}], \text{Keq\_PFL}, \text{KmCoA\_PFL}, \\ & [\text{PYR}], \text{Vmax\_PFL}, \text{kiG3P\_PFL}, \text{kmAcetCoA\_PFL}, \text{kmFormate\_PFL}, \text{kmPYR\_PFL}) \\ & = \frac{\frac{\text{kiG3P\_PFL}}{[\text{G3P}] + \text{kiG3P\_PFL}} \cdot \left( \text{Vmax\_PFL} \cdot \frac{[\text{PYR}]}{\text{kmPYR\_PFL}} \cdot \frac{[\text{CoA}]}{\text{KmCoA\_PFL}} - \frac{\text{Vmax\_PFL}}{\text{Keq\_PFL}} \cdot \frac{[\text{AcetCoA}]}{\text{kmPYR\_PFL}} \cdot \frac{[\text{Formate}]}{\text{KmCoA\_PFL}} \right)}{\left( 1 + \frac{[\text{PYR}]}{\text{kmPYR\_PFL}} \right) \cdot \left( 1 + \frac{[\text{CoA}]}{\text{kmCoA\_PFL}} \right) + \left( 1 + \frac{[\text{AcetCoA}]}{\text{kmAcetCoA\_PFL}} \right) \cdot \left( 1 + \frac{[\text{Formate}]}{\text{kmFormate\_PFL}} \right) - 1} \end{aligned}$$

Table 48: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
10	Name	200	varue	UIII	Constant
Keq_PFL	Keq_PFL		650.000		
${\tt KmCoA\_PFL}$	KmCoA_PFL		0.124		
${\tt Vmax\_PFL}$	Vmax_PFL		0.002		$\overline{\mathbf{Z}}$
kiG3P_PFL	kiG3P_PFL		0.511		$\overline{\mathbf{Z}}$
kmAcetCoA- _PFL	kmAcetCoA_PFL		7.343		$\overline{\mathbf{Z}}$
kmFormate- _PFL	kmFormate_PFL		54.269		
kmPYR_PFL	kmPYR_PFL		5.777		Ø

## 6.12 Reaction re24

This is an irreversible reaction of two reactants forming three products influenced by seven modifiers.

## Name AE

## **Reaction equation**

AcetCoA + 2 NADH ATP, ACetCoA, CoA, Ethanol, NAD, NADH Ethanol + 2 NAD + CoA
(62)

#### **Reactants**

Table 49: Properties of each reactant.

Id	Name	SBO
AcetCoA	AcetCoA	
NADH	NADH	

#### **Modifiers**

Table 50: Properties of each modifier.

Id	Name	SBO
ATP	ATP	
ATP	ATP	
AcetCoA	AcetCoA	
CoA	CoA	
Ethanol	Ethanol	
NAD	NAD	
NADH	NADH	

#### **Products**

Table 51: Properties of each product.

Id	Name	SBO
Ethanol	Ethanol	
NAD	NAD	
CoA	CoA	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$= \frac{\frac{\text{kiATP\_AE}}{[\text{ATP}] + \text{kiATP\_AE}} \cdot \text{Vmax\_AE} \cdot \frac{[\text{AcetCoA}]}{\text{kmAcetCoA\_AE}} \cdot \left(\frac{[\text{NADH}]}{\text{kmNADH\_AE}}\right)^2}{\left(1 + \frac{[\text{NADH}]}{\text{kmNADH\_AE}} + \left(\frac{[\text{NADH}]}{\text{kmNADH\_AE}}\right)^2\right) \cdot \left(1 + \frac{[\text{AcetCoA}]}{\text{kmAcetCoA\_AE}}\right) + \left(1 + \frac{[\text{Ethanol}]}{\text{kmEthanol\_AE}}\right) \cdot \left(1 + \frac{[\text{CoA}]}{\text{kmCoA\_AE}}\right) \cdot \left(1 + \frac{[\text{NADH}]}{\text{kmNADH\_AE}}\right)}$$

Table 52: Properties of each parameter.

			1		
Id	Name	SBO	Value	Unit	Constant
Vmax_AE	Vmax_AE		2.118		
$kiATP\_AE$	kiATP_AE		6.281		
${\tt kmAcetCoA\_AE}$	kmAcetCoA_AE		7.380		
${\tt kmCoA\_AE}$	$kmCoA\_AE$		0.092		
${\tt kmEthanol\_AE}$	kmEthanol_AE		2.281		
$kmNADH\_AE$	kmNADHAE		0.431		
$kmNAD\_AE$	kmNAD_AE		1.314		$ \overline{\mathbf{Z}} $

## 6.13 Reaction re25

This is an irreversible reaction of two reactants forming three products influenced by five modifiers.

#### Name AC

#### **Reaction equation**

$$AcetCoA + ADP \xrightarrow{ADP, ATP, AcetCoA, Acetate, CoA} Acetate + ATP + CoA$$
 (65)

#### **Reactants**

Table 53: Properties of each reactant.

Id	Name	SBO
AcetCoA	AcetCoA	
ADP	ADP	

#### **Modifiers**

Table 54: Properties of each modifier.

Id	Name	SBO
ADP	ADP	
ATP	ATP	
AcetCoA	AcetCoA	
Acetate	Acetate	
CoA	CoA	

#### **Products**

Table 55: Properties of each product.

Id	Name	SBO
Acetate	Acetate	
ATP	ATP	
CoA	CoA	

#### **Kinetic Law**

#### **Derived unit** contains undeclared units

$$v_{13} = function\_4\_ACK ([ADP], [ATP], [AcetCoA], [Acetate], [CoA], Vmax\_ACK, kmADP\_ACK, kmATP\_ACK, kmAcetCoA\_ACK, kmAcetate\_ACK, kmCoA\_ACK)$$
 (66)

$$= \frac{\text{Vmax\_ACK} \cdot \frac{[\text{AcetCoA}]}{\text{kmAcetCoA\_ACK}} \cdot \frac{[\text{ADP}]}{\text{kmADP\_ACK}}}{\left(1 + \frac{[\text{AcetCoA}]}{\text{kmAcetCoA\_ACK}}\right) \cdot \left(1 + \frac{[\text{ADP}]}{\text{kmADP\_ACK}}\right) + \left(1 + \frac{[\text{Acetate}]}{\text{kmAcetate\_ACK}}\right) \cdot \left(1 + \frac{[\text{ATP}]}{\text{kmATP\_ACK}}\right) \cdot \left(1 + \frac{[\text{CoA}]}{\text{kmCoA\_ACK}}\right) - 1}$$

Table 56: Properties of each parameter.

		•			
Id	Name	SBO	Value	Unit	Constant
Vmax_ACK	Vmax_ACK		3.839		
$kmADP\_ACK$	kmADP_ACK		1.172		
${\tt kmATP\_ACK}$	kmATP_ACK		14.156		

Id	Name	SBO	Value	Unit	Constant
kmAcetCoA- _ACK	kmAcetCoA_ACK		0.558		Ø
kmAcetate- _ACK	kmAcetate_ACK		0.552		$\mathbf{Z}$
${\tt kmCoA\_ACK}$	kmCoA_ACK		0.173		

## **6.14 Reaction** re26

This is a reversible reaction of one reactant forming one product influenced by two modifiers.

#### Name PA

## **Reaction equation**

$$2PYR \xrightarrow{Acetoin, PYR} Acetoin$$
 (68)

#### Reactant

Table 57: Properties of each reactant.

Id	Name	SBO
PYR	PYR	

#### **Modifiers**

Table 58: Properties of each modifier.

Id	Name	SBO
Acetoin PYR	Acetoin PYR	

#### **Product**

Table 59: Properties of each product.

Id	Name	SBO
Acetoin	Acetoin	

#### **Kinetic Law**

#### **Derived unit** contains undeclared units

$$v_{14} = \text{vol} (\text{compartment\_1}) \cdot \text{function\_4\_ALS} ([\text{Acetoin}], \text{Keq\_ALS}, [\text{PYR}], \text{Vmax\_ALS}, \\ \text{kmAcetoin\_ALS}, \text{kmPYR\_ALS})$$
(69)

function\_4\_ALS ([Acetoin], Keq\_ALS, [PYR], Vmax\_ALS, kmAcetoin\_ALS,

$$kmPYR\_ALS) = \frac{Vmax\_ALS \cdot \left(\frac{[PYR]}{kmPYR\_ALS}\right)^2 - \frac{Vmax\_ALS}{keq\_ALS} \cdot \frac{[Acetoin]}{kmPYR\_ALS}}{1 + \frac{[PYR]}{kmPYR\_ALS} + \left(\frac{[PYR]}{kmPYR\_ALS}\right)^2 + 1 + \frac{[Acetoin]}{kmAcetoin\_ALS} - 1}$$
(70)

 $function\_4\_ALS\,([Acetoin], Keq\_ALS, [PYR], Vmax\_ALS, kmAcetoin\_ALS,$ 

$$kmPYR\_ALS) = \frac{Vmax\_ALS \cdot \left(\frac{[PYR]}{kmPYR\_ALS}\right)^2 - \frac{Vmax\_ALS}{Keq\_ALS} \cdot \frac{[Acetoin]}{kmPYR\_ALS}}{1 + \frac{[PYR]}{kmPYR\_ALS} + \left(\frac{[PYR]}{kmPYR\_ALS}\right)^2 + 1 + \frac{[Acetoin]}{kmAcetoin\_ALS} - 1}$$
(71)

Table 60: Properties of each parameter.

rue to out i repetites et euen paramieten						
ame	SBO	Value	Unit	Constant		
eq_ALS	90	000.000				
max_ALS		0.355				
mAcetoin_ALS		0.050				
mPYR_ALS		0.263				
	ame eq_ALS max_ALS mAcetoin_ALS	ame SBO eq_ALS 90 max_ALS mAcetoin_ALS	ame SBO Value eq_ALS 900000.000 max_ALS 0.355 mAcetoin_ALS 0.050	ame SBO Value Unit eq_ALS 900000.000 max_ALS 0.355 mAcetoin_ALS 0.050		

#### 6.15 Reaction re27

This is a reversible reaction of two reactants forming two products influenced by four modifiers.

#### Name AB

#### **Reaction equation**

$$Acetoin + NADH \xrightarrow{Acetoin, Butanediol, NAD, NADH} Butanediol + NAD$$
 (72)

#### Reactants

Table 61: Properties of each reactant.

Id	Name	SBO
Acetoin NADH	Acetoin NADH	

#### **Modifiers**

Table 62: Properties of each modifier.

Id	Name	SBO
Acetoin	Acetoin	
Butanediol	Butanediol	
NAD	NAD	
NADH	NADH	

#### **Products**

Table 63: Properties of each product.

Id	Name	SBO
Butanediol NAD	Butanediol NAD	

#### **Kinetic Law**

**Derived unit** contains undeclared units

 $v_{15} = \text{function\_4\_BDH}([\text{Acetoin}], [\text{Butanediol}], \text{Keq\_BDH}, [\text{NAD}], [\text{NADH}], \text{Vmax\_BDH}, \\ \text{kmAcetoin\_BDH}, \text{kmButanediol\_BDH}, \text{kmNADH\_BDH}, \text{kmNAD\_BDH})$  (73)

 $function\_4\_BDH ([Acetoin], [Butanediol], Keq\_BDH, [NAD], [NADH], Vmax\_BDH, kmAcetoin\_BDH, kmButanediol\_BDH, kmNADH\_BDH, kmNAD\_BDH) \\$ 

$$= \frac{\text{Vmax\_BDH} \cdot \frac{[\text{Acetoin}]}{\text{kmAcetoin\_BDH}} \cdot \frac{[\text{NADH}]}{\text{kmNADH\_BDH}} - \frac{\text{Vmax\_BDH}}{\text{Keq\_BDH}} \cdot \frac{[\text{Butanediol}]}{\text{kmAcetoin\_BDH}} \cdot \frac{[\text{NAD}]}{\text{kmNADH\_BDH}}}{\left(1 + \frac{[\text{Acetoin}]}{\text{kmAcetoin\_BDH}}\right) \cdot \left(1 + \frac{[\text{NADH}]}{\text{kmNADH\_BDH}}\right) + \left(1 + \frac{[\text{Butanediol}]}{\text{kmButanediol\_BDH}}\right) \cdot \left(1 + \frac{[\text{NAD}]}{\text{kmNADL\_BDH}}\right) - 1}$$
(74)

Table 64: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Keq_BDH	Keq_BDH		1400.000		
${\tt Vmax\_BDH}$	Vmax_BDH		2.286		$   \overline{\mathscr{L}} $
kmAcetoin-	kmAcetoin_BDH		5.624		$\mathbf{Z}$
_BDH					
kmButanediol-	kmButanediol-		1.807		$\mathbf{Z}$
_BDH	_BDH				
$kmNADH\_BDH$	kmNADH_BDH		3.549		$\mathbf{Z}$
$kmNAD\_BDH$	kmNAD_BDH		1.296		

## 6.16 Reaction re28

This is a reversible reaction of two reactants forming two products influenced by five modifiers.

## Name MPD

## **Reaction equation**

## **Reactants**

Table 65: Properties of each reactant.

	•	
Id	Name	SBO
F6P NADH	F6P NADH	

#### **Modifiers**

Table 66: Properties of each modifier.

Id	Name	SBO
F6P	F6P	
F6P	F6P	
Mannitol1Phosphate	Mannitol1Phosphate	
NAD	NAD	
NADH	NADH	

#### **Products**

Table 67: Properties of each product.

Id	Name	SBO
Mannitol1Phosphate	Mannitol1Phosphate NAD	

#### **Kinetic Law**

#### Derived unit contains undeclared units

$$v_{16} = vol (compartment\_1) \cdot function\_4\_MPD ([F6P], Keq\_MPD, [Mannitol1Phosphate], [NAD], \\ [NADH], Vmax\_MPD, kiF6P\_MPD, kmF6P\_MPD, kmMannitol1Phoshate\_MPD, \\ kmNADH\_MPD, kmNAD\_MPD)$$
 (76)

function\_4\_MPD ([F6P], Keq\_MPD, [Mannitol1Phosphate], [NAD], [NADH], Vmax\_MPD, kiF6P\_MPD, kmF6P\_MPD, kmMannitol1Phoshate\_MPD, kmNADH\_MPD,

$$kmNAD\_MPD) = \frac{\frac{kiF6P\_MPD}{[F6P]+kiF6P\_MPD} \cdot \left(Vmax\_MPD \cdot \frac{[F6P]}{kmF6P\_MPD} \cdot \frac{[NADH]}{kmNADH\_MPD} - \frac{Vmax\_MPD}{Keq\_MPD} \cdot \frac{[Mannitol1Phosphate]}{kmF6P\_MPD} \cdot \frac{[NADH]}{kmNADH\_MPD} - \frac{[NADH]}{kmNaDH\_MPD} \cdot \frac{[NADH]}{kmNaDH\_MPD} \cdot \frac{[NADH]}{kmNanitol1Phosphate]} \cdot \frac{[NADH]}{kmNaD\_MPD} \right)}{\left(1 + \frac{[F6P]}{kmF6P\_MPD}\right) \cdot \left(1 + \frac{[NADH]}{kmNADH\_MPD}\right) + \left(1 + \frac{[Mannitol1Phosphate]}{kmMannitol1Phosphate}\right) \cdot \left(1 + \frac{[NAD]}{kmNAD\_MPD}\right)}$$

function\_4\_MPD ([F6P], Keq\_MPD, [Mannitol1Phosphate], [NAD], [NADH], Vmax\_MPD, kiF6P\_MPD, kmF6P\_MPD, kmMannitol1Phoshate\_MPD, kmNADH\_MPD,

$$kmNAD\_MPD) = \frac{\frac{kiF6P\_MPD}{[F6P]+kiF6P\_MPD} \cdot \left(Vmax\_MPD \cdot \frac{[F6P]}{kmF6P\_MPD} \cdot \frac{[NADH]}{kmNADH\_MPD} - \frac{Vmax\_MPD}{Keq\_MPD} \cdot \frac{[Mannitol1Phosphate]}{kmF6P\_MPD} \cdot \frac{[NADH]}{kmNADH\_MPD} \cdot \frac{[NAD$$

Table 68: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Keq_MPD	Keq_MPD		200.000		$\checkmark$
Vmax_MPD	Vmax_MPD		1.327		$\overline{\mathbf{Z}}$
kiF6P_MPD	kiF6P_MPD		22.028		$\overline{\mathbf{Z}}$
$kmF6P\_MPD$	kmF6P_MPD		0.321		$\overline{\mathbf{Z}}$
kmMannitol1P	ho <b>skmMe</b> nnitol1Phoshat	e-	0.089		$\overline{\mathbf{Z}}$
_MPD	_MPD				
$kmNADH\_MPD$	kmNADH_MPD		0.030		
${\tt kmNAD\_MPD}$	$kmNAD\_MPD$		0.373		$\square$

## 6.17 Reaction re29

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

#### Name MP

## **Reaction equation**

$$\underline{\text{Mannitol1Phosphate}} \xrightarrow{\text{Mannitol}, \text{Mannitol1Phosphate}} \underline{\text{Mannitol}}$$
 (79)

## Reactant

Table 69: Properties of each reactant.

Id	Name	SBO
Mannitol1Phosphate	Mannitol1Phosphate	

## **Modifiers**

Table 70: Properties of each modifier.

Id	Name	SBO
Mannitol	Mannitol	
Mannitol1Phosphate	Mannitol1Phosphate	

## **Product**

Table 71: Properties of each product.

Id	Name	SBO
Mannitol	Mannitol	

## **Kinetic Law**

Derived unit contains undeclared units

$$v_{17} = vol(compartment_1) \cdot function_4\_MP([Mannitol], [Mannitol1Phosphate],$$
 (80)  

$$Vmax\_MP, kmMannitol1Phosphate\_MP, kmMannitol\_MP)$$

function\_4\_MP([Mannitol],[Mannitol1Phosphate],

Vmax\_MP, kmMannitol1Phosphate\_MP,

$$kmMannitol\_MP) = \frac{Vmax\_MP \cdot \frac{[Mannitol1Phosphate]}{kmMannitol1Phosphate\_MP}}{1 + \frac{[Mannitol1Phosphate]}{kmMannitol1Phosphate} + 1 + \frac{[Mannitol]}{kmMannitol\_MP} - 1}$$
(81)

function\_4\_MP([Mannitol], [Mannitol1Phosphate],

Vmax\_MP, kmMannitol1Phosphate\_MP,

$$kmMannitol\_MP) = \frac{Vmax\_MP \cdot \frac{[Mannitol1Phosphate]}{kmMannitol1Phosphate\_MP}}{1 + \frac{[Mannitol1Phosphate]}{kmMannitol1Phosphate} + 1 + \frac{[Mannitol]}{kmMannitol\_MP} - 1}$$
(82)

Table 72: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax_MP kmMannitol1Ph	Vmax_MP o <b>skphMæ</b> mitol1Phospl	nate-	3.486 3.516		<b>✓</b>
_MP kmMannitol- _MP	_MP kmMannitol_MP		0.239		Ø

#### 6.18 Reaction re30

This is an irreversible reaction of two reactants forming two products influenced by four modifiers.

Name PTS\_Man

## **Reaction equation**

$$Mannitol\_Ext + PEP \xrightarrow{Mannitol1Phosphate, Mannitol\_Ext, PEP, PYR} Mannitol1Phosphate + PYR$$

$$(83)$$

### Reactants

Table 73: Properties of each reactant.

Id	Name	SBO
Mannitol_Ext PEP	Mannitol_Ext PEP	

#### **Modifiers**

Table 74: Properties of each modifier.

Tueste / 11 Troperties of euch mountain				
Id	Name	SBO		
Mannitol1Phosphate	Mannitol1Phosphate			
${\tt Mannitol\_Ext}$	Mannitol_Ext			
PEP	PEP			
PYR	PYR			

#### **Products**

Table 75: Properties of each product.

Id	Name	SBO
Mannitol1Phosphate	Mannitol1Phosphate PYR	

### **Kinetic Law**

## Derived unit contains undeclared units

function\_4\_PTS\_Man ([Mannitol1Phosphate], [Mannitol\_Ext], [PEP], [PYR], Vmax\_PTS\_Man, kmMannitol1Phosphate\_PTS\_Man, kmPEP\_PTS\_Man, kmPYR\_PTS\_Man) (85)

$$= \frac{Vmax\_PTS\_Man \cdot \frac{[Mannitol\_Ext]}{kmMannitolExt\_PTS\_Man} \cdot \frac{[PEP]}{kmPEP\_PTS\_Man}}{\left(1 + \frac{[Mannitol\_Ext]}{kmMannitolExt\_PTS\_Man}\right) \cdot \left(1 + \frac{[PEP]}{kmPEP\_PTS\_Man}\right) + \left(1 + \frac{[Mannitol1Phosphate]}{kmMannitol1Phosphate\_PTS\_Man}\right) \cdot \left(1 + \frac{[PYR]}{kmPYR\_PTS\_Man}\right) - \frac{(PEP)}{kmPYR\_PTS\_Man} + \frac{(PEP$$

Table 76: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax_PTS_Man	Vmax_PTS_Man		4.449		Ø
kmMannitol1Ph	no <b>skphMcan</b> nitol1Phosph	nate-	0.363		$\square$
_PTS_Man	_PTS_Man				
${\tt kmMannitolExt}$	- kmMannitolExt-		0.013		$\square$
_PTS_Man	_PTS_Man				

Id	Name	SBO	Value	Unit	Constant
kmPEP_PTS- _Man	kmPEP_PTS_Man		2.208		<b>✓</b>
kmPYR_PTS- _Man	kmPYR_PTS_Man		0.344		Ø

## 6.19 Reaction re31

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

Name Acetoin\_transp

## **Reaction equation**

Acetoin 
$$\xrightarrow{\text{Acetoin.Ext}}$$
 Acetoin  $\xrightarrow{\text{Ext}}$  (86)

#### Reactant

Table 77: Properties of each reactant.

Id	Name	SBO
Acetoin	Acetoin	

## **Modifiers**

Table 78: Properties of each modifier.

Id	Name	SBO
Acetoin Acetoin_Ext	Acetoin Acetoin_Ext	

## **Product**

Table 79: Properties of each product.

Id	Name	SBO
Acetoin_Ext	Acetoin_Ext	

## **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{19} = \text{function\_4\_Acetoin\_transp}([\text{Acetoin}], [\text{Acetoin\_Ext}], \text{Vmax\_Acetoin\_transp}, \\ \text{kmAcetoin\_Acetoin\_transp}, \text{kmAcetoin\_Ext\_Acetoin\_transp})$$
 (87)

 $function\_4\_Acetoin\_transp ([Acetoin], [Acetoin\_Ext], Vmax\_Acetoin\_transp, kmAcetoin\_Acetoin\_transp, kmAcetoin\_Ext\_Acetoin\_transp)$ 

$$= \frac{V_{\text{max\_Acetoin\_transp}} \cdot \frac{[\text{Acetoin}]}{\text{kmAcetoin\_Acetoin\_transp}}}{1 + \frac{[\text{Acetoin}]}{\text{kmAcetoin\_Acetoin\_transp}} + \frac{[\text{Acetoin\_Ext}]}{\text{kmAcetoin\_Ext\_Acetoin\_transp}}}$$
(88)

Table 80: Properties of each parameter.

Id	Name	SBO Value Unit	Constant
Vmax- _Acetoin-	Vmax_Acetoin- _transp	1.601	
_transp kmAcetoin- _Acetoin- _transp	kmAcetoin- _Acetoin_transp	1.893	Ø
kmAcetoin- _Ext_Acetoin- _transp	kmAcetoin_Ext_Acetoin_transp	7.052	$\mathbf{Z}$

#### 6.20 Reaction re32

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

Name Mannitol\_transp

## **Reaction equation**

$$Mannitol \xrightarrow{Mannitol, Mannitol\_Ext} Mannitol\_Ext$$
 (89)

## Reactant

Table 81: Properties of each reactant.

Id	Name	SBO
Mannitol	Mannitol	

#### **Modifiers**

Table 82: Properties of each modifier.

	Tuest ez. Treperios er euem meemen.			
Id	Name	SBO		
Mannitol Mannitol_Ext	Mannitol Mannitol_Ext			

#### **Product**

Table 83: Properties of each product.

Id	Name	SBO
Mannitol_Ext	Mannitol_Ext	

## **Kinetic Law**

#### **Derived unit** contains undeclared units

$$v_{20} = \text{function\_4\_Mannitol\_transp}([\text{Mannitol}], [\text{Mannitol\_Ext}], \text{Vmax\_Mannitol\_transp}, \\ \text{kmMannitol\_Ext\_Mannitol\_transp}, \text{kmMannitol\_transp})$$
(90)

 $function\_4\_Mannitol\_transp ([Mannitol], [Mannitol\_Ext], Vmax\_Mannitol\_transp, \\ kmMannitol\_Ext\_Mannitol\_transp, kmMannitol\_Mannitol\_transp)$ 

$$= \frac{\text{Vmax\_Mannitol\_transp} \cdot \frac{[\text{Mannitol}]}{\text{kmMannitol\_Mannitol\_transp}}}{1 + \frac{[\text{Mannitol}]}{\text{kmMannitol\_Mannitol\_transp}} + \frac{[\text{Mannitol\_Mannitol\_transp}]}{\text{kmMannitol\_Ext\_Mannitol\_transp}}$$

$$(91)$$

Table 84: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vmax-	Vmax_Mannitol-		1.625		$\square$
_Mannitol-	_transp				
$_{ extsf{ iny transp}}$					
kmMannitol-	kmMannitol_Ext-		0.941		$\square$
_Ext-	_Mannitol_transp				
$_{ t Mannitol-}$					
$_{ extsf{ iny transp}}$					
kmMannitol-	kmMannitol-		0.022		<b></b>
_Mannitol-	_Mannitol_transp				_
$_{ extsf{ exitsf{ extsf{ extsf{ extsf{ extsf{ exitsf{ extsf{ exitit}}}}}}}}} }}}}}}}}}}}}}}}}}}}}}} } } } }$	•				

## 6.21 Reaction re33

This is an irreversible reaction of one reactant forming two products influenced by three modifiers.

Name FBPase

## **Reaction equation**

$$FBP \xrightarrow{F6P, FBP, Pint} F6P + Pint$$
 (92)

#### Reactant

Table 85: Properties of each reactant.

Id	Name	SBO
FBP	FBP	

#### **Modifiers**

Table 86: Properties of each modifier.

Id	Name	SBO
F6P	F6P	
FBP	FBP	
Pint	Pint	

## **Products**

Table 87: Properties of each product.

Id	Name	SBO
F6P	F6P	
Pint	Pint	

## **Kinetic Law**

Derived unit contains undeclared units

$$v_{21} = \text{vol}(\text{compartment\_1}) \cdot \text{function\_4\_FBPase}([F6P], [FBP], [Pint], Vmax\_FBPase, kmF6P\_FBPase, kmFBP\_FBPase, kmPint\_FBPase)$$
 (93)

 $function\_4\_FBPase ([F6P], [FBP], [Pint], Vmax\_FBPase, kmF6P\_FBPase, kmFBP\_FBPase, kmF6P\_FBPase, kmF6P\_FFPASe, km$ 

$$kmPint\_FBPase) = \frac{Vmax\_FBPase \cdot \frac{[FBP]}{kmFBP\_FBPase}}{\frac{[FBP]}{kmFBP\_FBPase} + \left(1 + \frac{[F6P]}{kmF6P\_FBPase}\right) \cdot \left(1 + \frac{[Pint]}{kmPint\_FBPase}\right)}$$
(94)

function\_4\_FBPase ([F6P], [FBP], [Pint], Vmax\_FBPase, kmF6P\_FBPase, kmFBP\_FBPase,

$$kmPint\_FBPase) = \frac{Vmax\_FBPase \cdot \frac{[FBP]}{kmFBP\_FBPase}}{\frac{[FBP]}{kmFBP\_FBPase} + \left(1 + \frac{[F6P]}{kmF6P\_FBPase}\right) \cdot \left(1 + \frac{[Pint]}{kmPint\_FBPase}\right)}$$
(95)

Id Name **SBO** Value Unit Constant Vmax\_FBPase Vmax\_FBPase 0.097 kmF6P\_FBPase  $kmF6P_FBPase$ 1.908 kmFBP\_FBPase  $kmFBP_FBPase$ 0.412 kmPintkmPint\_FBPase 0.011 \_FBPase

Table 88: Properties of each parameter.

# 7 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the hasOnlySubstanceUnits flag may be set to false and spacialDimensions > 0 for certain species.

#### 7.1 Species G6P

Name G6P

Initial concentration  $0 \text{ } mmol \cdot l^{-1}$ 

This species takes part in four reactions (as a reactant in re15 and as a product in re12 and as a modifier in re12, re15).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{G6P} = |v_1| - |v_4| \tag{96}$$

## 7.2 Species ATP

Name ATP

Initial concentration  $4.88632508879394 \text{ } \text{mmol} \cdot l^{-1}$ 

This species takes part in 14 reactions (as a reactant in re13, re14, re16 and as a product in re20, re21, re25 and as a modifier in re13, re14, re16, re20, re21, re24, re24, re25).

$$\frac{d}{dt}ATP = |v_8| + |v_9| + |v_{13}| - |v_2| - |v_3| - |v_5|$$
(97)

## 7.3 Species ADP

Name ADP

Initial concentration  $20.3856905308319 \text{ mmol} \cdot l^{-1}$ 

This species takes part in eleven reactions (as a reactant in re20, re21, re25 and as a product in re13, re14, re16 and as a modifier in re14, re16, re20, re21, re25).

$$\frac{d}{dt}ADP = |v_2| + |v_3| + |v_5| - |v_8| - |v_9| - |v_{13}|$$
(98)

## 7.4 Species Pint

Name Pint

Initial concentration  $38.26 \text{ } \text{mmol} \cdot l^{-1}$ 

This species takes part in 14 reactions (as a reactant in re18 and as a product in re13, re14, re33 and as a modifier in re12, re12, re14, re14, re14, re21, re21, re22, re22, re33).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{Pint} = |v_2| + 2|v_3| + |v_{21}| - |v_7| \tag{99}$$

## 7.5 Species F6P

Name F6P

Initial concentration  $0 \text{ mmol} \cdot 1^{-1}$ 

This species takes part in nine reactions (as a reactant in re16, re28 and as a product in re15, re33 and as a modifier in re15, re16, re28, re28, re33).

$$\frac{\mathrm{d}}{\mathrm{d}t} F6P = |v_4| + |v_{21}| - |v_5| - |v_{16}| \tag{100}$$

## 7.6 Species FBP

Name FBP

Initial concentration  $15.3 \text{ mmol} \cdot 1^{-1}$ 

This species takes part in twelve reactions (as a reactant in re17, re33 and as a product in re16 and as a modifier in re12, re12, re16, re17, re21, re21, re22, re22, re33).

$$\frac{\mathrm{d}}{\mathrm{d}t} \mathrm{FBP} = |v_5| - |v_6| - |v_{21}| \tag{101}$$

## 7.7 Species G3P

Name G3P

Initial concentration  $0 \text{ mmol} \cdot l^{-1}$ 

This species takes part in six reactions (as a reactant in re18 and as a product in re17 and as a modifier in re17, re18, re23, re23).

$$\frac{d}{dt}G3P = 2 v_6 - v_7 \tag{102}$$

## 7.8 Species BPG

Name BPG

Initial concentration  $1.26348531244692 \text{ mmol} \cdot 1^{-1}$ 

This species takes part in four reactions (as a reactant in re20 and as a product in re18 and as a modifier in re18, re20).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{BPG} = |v_7| - |v_8| \tag{103}$$

## 7.9 Species PEP

Name PEP

Initial concentration  $2.4790177588998 \text{ } \text{mmol} \cdot l^{-1}$ 

This species takes part in eight reactions (as a reactant in re12, re21, re30 and as a product in re20 and as a modifier in re12, re20, re21, re30).

$$\frac{d}{dt}PEP = |v_8| - |v_1| - |v_9| - |v_{18}| \tag{104}$$

## 7.10 Species NAD

#### Name NAD

Initial concentration  $4.67 \text{ } \text{mmol} \cdot l^{-1}$ 

This species takes part in ten reactions (as a reactant in re18 and as a product in re22, re24, re27, re28 and as a modifier in re18, re22, re24, re27, re28).

$$\frac{d}{dt}NAD = v_{10} + 2v_{12} + v_{15} + v_{16} - v_7$$
 (105)

## 7.11 Species NADH

#### Name NADH

Initial concentration  $2.03337939283534 \cdot 10^{-6} \text{ } \text{mmol} \cdot l^{-1}$ 

This species takes part in ten reactions (as a reactant in re22, re24, re27, re28 and as a product in re18 and as a modifier in re18, re22, re24, re27, re28).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{NADH} = |v_7| - |v_{10}| - 2|v_{12}| - |v_{15}| - |v_{16}|$$
(106)

## 7.12 Species PYR

#### Name PYR

Initial concentration  $0 \text{ mmol} \cdot l^{-1}$ 

This species takes part in twelve reactions (as a reactant in re22, re23, re26 and as a product in re12, re21, re30 and as a modifier in re12, re21, re22, re23, re26, re30).

$$\frac{d}{dt}PYR = |v_1| + |v_9| + |v_{18}| - |v_{10}| - |v_{11}| - 2|v_{14}|$$
(107)

## 7.13 Species AcetCoA

#### Name AcetCoA

## Initial concentration $0 \text{ } \mathrm{mmol} \cdot l^{-1}$

This species takes part in six reactions (as a reactant in re24, re25 and as a product in re23 and as a modifier in re23, re24, re25).

$$\frac{d}{dt}AcetCoA = |v_{11}| - |v_{12}| - |v_{13}|$$
 (108)

## 7.14 Species Acetoin

Name Acetoin

Initial concentration  $0 \text{ } \mathrm{mmol} \cdot l^{-1}$ 

This species takes part in six reactions (as a reactant in re27, re31 and as a product in re26 and as a modifier in re26, re27, re31).

$$\frac{d}{dt}Acetoin = |v_{14}| - |v_{15}| - |v_{19}|$$
 (109)

## 7.15 Species Mannitol

Name Mannitol

Initial concentration  $0 \text{ mmol} \cdot l^{-1}$ 

This species takes part in four reactions (as a reactant in re32 and as a product in re29 and as a modifier in re29, re32).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Mannitol} = v_{17} - v_{20} \tag{110}$$

## 7.16 Species Mannitol1Phosphate

Name Mannitol1Phosphate

Initial concentration  $0 \text{ mmol} \cdot l^{-1}$ 

This species takes part in six reactions (as a reactant in re29 and as a product in re28, re30 and as a modifier in re28, re29, re30).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{Mannitol1Phosphate} = |v_{16}| + |v_{18}| - |v_{17}| \tag{111}$$

## 7.17 Species CoA

Name CoA

Initial concentration  $1 \text{ mmol} \cdot l^{-1}$ 

This species takes part in six reactions (as a reactant in re23 and as a product in re24, re25 and as a modifier in re23, re24, re25).

$$\frac{d}{dt}CoA = |v_{12}| + |v_{13}| - |v_{11}| \tag{112}$$

## 7.18 Species Pext

Name Pext

Initial concentration  $50 \text{ } \text{mmol} \cdot l^{-1}$ 

This species takes part in two reactions (as a reactant in re14 and as a modifier in re14).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Pext} = -v_3 \tag{113}$$

## 7.19 Species Lactate

Name Lactate

Initial concentration  $0 \text{ mmol} \cdot l^{-1}$ 

This species takes part in two reactions (as a product in re22 and as a modifier in re22).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Lactate} = |v_{10}| \tag{114}$$

## 7.20 Species Ethanol

Name Ethanol

Initial concentration  $0 \text{ mmol} \cdot l^{-1}$ 

This species takes part in two reactions (as a product in re24 and as a modifier in re24).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Ethanol} = v_{12} \tag{115}$$

## 7.21 Species Acetate

Name Acetate

Initial concentration  $0 \text{ mmol} \cdot 1^{-1}$ 

This species takes part in two reactions (as a product in re25 and as a modifier in re25).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{Acetate} = v_{13} \tag{116}$$

## 7.22 Species Butanediol

Name Butanediol

Initial concentration  $0 \text{ } \mathrm{mmol} \cdot l^{-1}$ 

This species takes part in two reactions (as a product in re27 and as a modifier in re27).

$$\frac{\mathrm{d}}{\mathrm{d}t} \text{Butanediol} = v_{15} \tag{117}$$

## 7.23 Species Glucose

Name Glucose

Initial concentration  $80 \text{ } \text{mmol} \cdot l^{-1}$ 

This species takes part in two reactions (as a reactant in re12 and as a modifier in re12).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Glucose} = -v_1 \tag{118}$$

## 7.24 Species Acetoin\_Ext

Name Acetoin\_Ext

Initial concentration  $0 \text{ mmol} \cdot 1^{-1}$ 

This species takes part in two reactions (as a product in re31 and as a modifier in re31).

$$\frac{\mathrm{d}}{\mathrm{d}t} \operatorname{Acetoin} \operatorname{Ext} = v_{19} \tag{119}$$

## 7.25 Species Mannitol\_Ext

Name Mannitol\_Ext

Initial concentration  $0 \text{ mmol} \cdot 1^{-1}$ 

This species takes part in four reactions (as a reactant in re30 and as a product in re32 and as a modifier in re30, re32).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{Mannitol}\mathrm{Ext} = |v_{20}| - |v_{18}| \tag{120}$$

## 7.26 Species Formate

Name Formate

Initial concentration  $0 \text{ mmol} \cdot l^{-1}$ 

This species takes part in two reactions (as a product in re23 and as a modifier in re23).

$$\frac{\mathrm{d}}{\mathrm{d}t}\text{Formate} = v_{11} \tag{121}$$

SML2ATEX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX for more information.

<sup>&</sup>lt;sup>a</sup>Center for Bioinformatics Tübingen (ZBIT), Germany

<sup>&</sup>lt;sup>b</sup>California Institute of Technology, Beckman Institute BNMC, Pasadena, United States

<sup>&</sup>lt;sup>c</sup>European Bioinformatics Institute, Wellcome Trust Genome Campus, Hinxton, United Kingdom

<sup>&</sup>lt;sup>d</sup>EML Research gGmbH, Heidelberg, Germany