

## SBML Model Report

### Model name: “Tyson2003\_Substrate\_Depletion\_Osc”



May 6, 2016

## 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by Lukas Endler<sup>1</sup> at February tenth 2011 at 3:49 a. m. and last time modified at April sixth 2014 at 8:01 p. m. Table 1 shows an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	5
events	0	constraints	0
reactions	5	function definitions	1
global parameters	11	unit definitions	6
rules	4	initial assignments	0

## Model Notes

This is an SBML implementation the model of the substrate depletion oscillator (figure 2c) described in the article:

**Sniffers, buzzers, toggles and blinkers: dynamics of regulatory and signaling pathways in the cell.**

Tyson JJ, Chen KC, Novak B. Curr Opin Cell Biol. 2003 Apr;15(2):221-31. PubmedID: [12648679](#);

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DOI: [10.1016/S0955-0674\(03\)00017-6](https://doi.org/10.1016/S0955-0674(03)00017-6);

**Abstract:**

The physiological responses of cells to external and internal stimuli are governed by genes and proteins interacting in complex networks whose dynamical properties are impossible to understand by intuitive reasoning alone. Recent advances by theoretical biologists have demonstrated that molecular regulatory networks can be accurately modeled in mathematical terms. These models shed light on the design principles of biological control systems and make predictions that have been verified experimentally.

Originally created by libAntimony v1.4 (using libSBML 3.4.1)

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To cite BioModels Database, please use: [Li C, Donizelli M, Rodriguez N, Dharuri H, Endler L, Chelliah V, Li L, He E, Henry A, Stefan MI, Snoep JL, Hucka M, Le Novre N, Laibe C \(2010\) BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models. BMC Syst Biol., 4:92.](#)

## 2 Unit Definitions

This is an overview of nine unit definitions of which three are predefined by SBML and not mentioned in the model.

### 2.1 Unit `time`

**Name** `s`

**Definition** `s`

### 2.2 Unit `substance`

**Name** `mole`

**Definition** `mol`

### 2.3 Unit `per_s`

**Name** `per_s`

**Definition**  $s^{-1}$

### 2.4 Unit `M_per_s`

**Name** `M_per_s`

**Definition**  $\text{mol} \cdot s^{-1} \cdot l^{-1}$

## 2.5 Unit M

**Name** M

**Definition**  $\text{mol} \cdot \text{l}^{-1}$

## 2.6 Unit per\_M\_per\_s

**Name** per\_M\_per\_s

**Definition**  $\text{mol}^{-1} \cdot \text{l} \cdot \text{s}^{-1}$

## 2.7 Unit volume

**Notes** Litre is the predefined SBML unit for volume.

**Definition** l

## 2.8 Unit area

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition**  $\text{m}^2$

## 2.9 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

# 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
env		0000290	3	1	litre	<input checked="" type="checkbox"/>	

### 3.1 Compartment env

This is a three dimensional compartment with a constant size of one litre.

**SBO:0000290** physical compartment

## 4 Species

This model contains five species. The boundary condition of three of these species is set to `true` so that these species' amount cannot be changed by any reaction. Section 9 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
R		env	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
X		env	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
S		env	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input checked="" type="checkbox"/>
Ep		env	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input checked="" type="checkbox"/>
E		env	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input checked="" type="checkbox"/>

## 5 Parameters

This model contains eleven global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
k0_prime		0000035	0.01	s <sup>-1</sup>	<input checked="" type="checkbox"/>
k0		0000036	0.40	mol <sup>-1</sup> · l · s <sup>-1</sup>	<input checked="" type="checkbox"/>
k1		0000035	1.00	s <sup>-1</sup>	<input checked="" type="checkbox"/>
k2		0000356	1.00	s <sup>-1</sup>	<input checked="" type="checkbox"/>
k3		0000186	1.00	s <sup>-1</sup>	<input checked="" type="checkbox"/>
J3		0000002	0.05	dimensionless	<input checked="" type="checkbox"/>
k4		0000186	0.30	mol · s <sup>-1</sup> · l <sup>-1</sup>	<input checked="" type="checkbox"/>
J4		0000002	0.05	dimensionless	<input checked="" type="checkbox"/>
Et		0000196	1.00	mol · l <sup>-1</sup>	<input checked="" type="checkbox"/>
Km3		0000027	0.00	mol · l <sup>-1</sup>	<input type="checkbox"/>
Km4		0000027	0.00	mol · l <sup>-1</sup>	<input type="checkbox"/>

## 6 Function definition

This is an overview of one function definition.

### 6.1 Function definition `goldbeter_koshland`

**Arguments** v1, v2, J1, J2

**Mathematical Expression**

$$\frac{2 \cdot v1 \cdot J2}{v2 - v1 + J1 \cdot v2 + J2 \cdot v1 + \left( (v2 - v1 + J1 \cdot v2 + J2 \cdot v1)^2 - 4 \cdot (v2 - v1) \cdot v1 \cdot J2 \right)^{\frac{1}{2}}} \quad (1)$$

## 7 Rules

This is an overview of four rules.

### 7.1 Rule `Km3`

Rule Km3 is an assignment rule for parameter Km3:

$$Km3 = J3 \cdot Et \quad (2)$$

**Derived unit** mol · l<sup>-1</sup>

## 7.2 Rule $K_{m4}$

Rule  $K_{m4}$  is an assignment rule for parameter  $K_{m4}$ :

$$K_{m4} = J_4 \cdot E_t \quad (3)$$

**Derived unit**  $\text{mol} \cdot \text{l}^{-1}$

## 7.3 Rule $E_p$

Rule  $E_p$  is an assignment rule for species  $E_p$ :

$$E_p = \text{goldbeter\_koshland}(k_3 \cdot [R], k_4, J_3, J_4) \cdot E_t \quad (4)$$

## 7.4 Rule $E$

Rule  $E$  is an assignment rule for species  $E$ :

$$E = E_t - [E_p] \quad (5)$$

**Derived unit**  $\text{mol} \cdot \text{l}^{-1}$

# 8 Reactions

This model contains five reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	r0		$X \xrightarrow{Ep} R$	0000182
2	r1		$\emptyset \xrightarrow{S} X$	0000176
3	r2		$R \longrightarrow \emptyset$	0000179
4	r3		$E \xrightarrow{R} Ep$	0000216
5	r4		$Ep \longrightarrow E$	0000330

### 8.1 Reaction r0

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

**SBO:0000182** conversion

#### Reaction equation



#### Reactant

Table 6: Properties of each reactant.

Id	Name	SBO
X		

#### Modifier

Table 7: Properties of each modifier.

Id	Name	SBO
Ep		0000462

#### Product

Table 8: Properties of each product.

Id	Name	SBO
R		

#### Kinetic Law

**Derived unit**  $s^{-1} \cdot \text{mol}$

$$v_1 = \text{vol}(\text{env}) \cdot (k0\_prime + k0 \cdot [Ep]) \cdot [X] \quad (7)$$

### 8.2 Reaction r1

This is an irreversible reaction of no reactant forming one product influenced by one modifier.

**SBO:0000176** biochemical reaction



## Reaction equation



## Modifier

Table 9: Properties of each modifier.

Id	Name	SBO
S		0000461

## Product

Table 10: Properties of each product.

Id	Name	SBO
X		

## Kinetic Law

**SBO:0000049** mass action rate law for first order irreversible reactions, continuous scheme

**Derived unit**  $s^{-1} \cdot \text{mol}$

$$v_2 = \text{vol}(\text{env}) \cdot k_1 \cdot [S] \quad (9)$$

## 8.3 Reaction r2

This is an irreversible reaction of one reactant forming no product.

**SBO:0000179** degradation

## Reaction equation



## Reactant

Table 11: Properties of each reactant.

Id	Name	SBO
R		

## Kinetic Law

**SBO:0000049** mass action rate law for first order irreversible reactions, continuous scheme

**Derived unit**  $\text{s}^{-1} \cdot \text{mol}$

$$v_3 = \text{vol}(\text{env}) \cdot k_2 \cdot [\text{R}] \quad (11)$$

## 8.4 Reaction r3

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

**SBO:0000216** phosphorylation

## Reaction equation



## Reactant

Table 12: Properties of each reactant.

Id	Name	SBO
E		

## Modifier

Table 13: Properties of each modifier.

Id	Name	SBO
R		0000461

## Product

Table 14: Properties of each product.

Id	Name	SBO
Ep		

## Kinetic Law

**SBO:0000430** enzymatic rate law for modulated unireactant enzymes

**Derived unit**  $\text{s}^{-1} \cdot \text{mol}$

$$v_4 = \frac{\text{vol}(\text{env}) \cdot k_3 \cdot [\text{R}] \cdot [\text{E}]}{K_{m3} + [\text{E}]} \quad (13)$$

## 8.5 Reaction $r_4$

This is an irreversible reaction of one reactant forming one product.

**SBO:0000330** dephosphorylation

### Reaction equation



### Reactant

Table 15: Properties of each reactant.

Id	Name	SBO
Ep		

### Product

Table 16: Properties of each product.

Id	Name	SBO
E		

## Kinetic Law

**SBO:0000199** normalised enzymatic rate law for unireactant enzymes

**Derived unit**  $\text{mol} \cdot \text{s}^{-1}$

$$v_5 = \frac{\text{vol}(\text{env}) \cdot k_4 \cdot [\text{Ep}]}{K_{m4} + [\text{Ep}]} \quad (15)$$

## 9 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

### 9.1 Species R

**SBO:0000285** material entity of unspecified nature

**Initial concentration**  $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [r2](#) and as a product in [r0](#) and as a modifier in [r3](#)).

$$\frac{d}{dt}R = v_1 - v_3 \quad (16)$$

### 9.2 Species X

**SBO:0000285** material entity of unspecified nature

**Initial concentration**  $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in [r0](#) and as a product in [r1](#)).

$$\frac{d}{dt}X = v_2 - v_1 \quad (17)$$

### 9.3 Species S

**SBO:0000285** material entity of unspecified nature

**Initial concentration**  $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in one reaction (as a modifier in [r1](#)), which does not influence its rate of change because this species is on the boundary of the reaction system:

$$\frac{d}{dt}S = 0 \quad (18)$$

### 9.4 Species Ep

**SBO:0000252** polypeptide chain

**Involved in rule** [Ep](#)

This species takes part in three reactions (as a reactant in [r4](#) and as a product in [r3](#) and as a modifier in [r0](#)). Not these but one rule determines the species' quantity because this species is on the boundary of the reaction system.

## 9.5 Species [E](#)

**SBO:0000252** polypeptide chain

**Involved in rule** [E](#)

This species takes part in two reactions (as a reactant in [r3](#) and as a product in [r4](#)). Not these but one rule determines the species' quantity because this species is on the boundary of the reaction system.

## A Glossary of Systems Biology Ontology Terms

**SBO:0000002 quantitative systems description parameter:** A numerical value that defines certain characteristics of systems or system functions. It may be part of a calculation, but its value is not determined by the form of the equation itself, and may be arbitrarily assigned

**SBO:0000027 Michaelis constant:** Substrate concentration at which the velocity of reaction is half its maximum. Michaelis constant is an experimental parameter. According to the underlying molecular mechanism it can be interpreted differently in terms of microscopic constants

**SBO:0000035 forward unimolecular rate constant, continuous case:** Numerical parameter that quantifies the forward velocity of a chemical reaction involving only one reactant. This parameter encompasses all the contributions to the velocity except the quantity of the reactant. It is to be used in a reaction modelled using a continuous framework

**SBO:0000036 forward bimolecular rate constant, continuous case:** Numerical parameter that quantifies the forward velocity of a chemical reaction involving two reactants. This parameter encompasses all the contributions to the velocity except the quantity of the reactants. It is to be used in a reaction modelled using a continuous framework

**SBO:0000049 mass action rate law for first order irreversible reactions, continuous scheme:** Reaction scheme where the products are created from the reactants and the change of a product quantity is proportional to the product of reactant activities. The reaction scheme does not include any reverse process that creates the reactants from the products. The change of a product quantity is proportional to the quantity of one reactant. It is to be used in a reaction modelled using a continuous framework.

**SBO:0000176 biochemical reaction:** An event involving one or more chemical entities that modifies the electrochemical structure of at least one of the participants.

**SBO:0000179 degradation:** Complete disappearance of a physical entity

**SBO:0000182 conversion:** Biochemical reaction that results in the modification of some covalent bonds

- SBO:0000186 maximal velocity:** Limiting maximal velocity of an enzymatic reaction, reached when the substrate is in large excess and all the enzyme is complexed.
- SBO:0000196 concentration of an entity pool:** The amount of an entity per unit of volume.
- SBO:0000199 normalised enzymatic rate law for unireactant enzymes:** Kinetics of enzymes that react only with one substance, their substrate. The total enzyme concentration is considered to be equal to 1, therefore the maximal velocity equals the catalytic constant.
- SBO:0000216 phosphorylation:** Addition of a phosphate group ( $\text{-H}_2\text{PO}_4$ ) to a chemical entity
- SBO:0000252 polypeptide chain:** Naturally occurring macromolecule formed by the repetition of amino-acid residues linked by peptidic bonds. A polypeptide chain is synthesized by the ribosome. CHEBI:1654
- SBO:0000285 material entity of unspecified nature:** Material entity whose nature is unknown or irrelevant
- SBO:0000290 physical compartment:** Specific location of space, that can be bounded or not. A physical compartment can have 1, 2 or 3 dimensions
- SBO:0000330 dephosphorylation:** Removal of a phosphate group ( $\text{-H}_2\text{PO}_4$ ) from a chemical entity.
- SBO:0000356 decay constant:** Kinetic constant characterising a mono-exponential decay. It is the inverse of the mean lifetime of the continuant being decayed. Its unit is “per tim”.
- SBO:0000430 enzymatic rate law for modulated unireactant enzymes:** Kinetics of enzymes that react with one substance, and whose activity may be positively or negatively modulated
- SBO:0000461 essential activator:** A substance that is absolutely required for occurrence and stimulation of a reaction
- SBO:0000462 non-essential activator:** An activator which is not necessary for an enzymatic reaction, but whose presence will further increase enzymatic activity.

SBML<sup>2</sup>TeX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

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