

SBML Model Report

Model name:
“Friedland2009_Ara_RTC3_counter”



May 6, 2016

1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by Lukas Endler¹ at January 19th 2011 at 2:14 a. m. and last time modified at April eighth 2016 at 4:55 p. m. Table 1 provides an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	8
events	6	constraints	0
reactions	15	function definitions	0
global parameters	36	unit definitions	0
rules	2	initial assignments	0

Model Notes

This is the model of the RTC3 counter described in the article:

Synthetic gene networks that count.

Friedland AE, Lu TK, Wang X, Shi D, Church G, Collins JJ. Science. 2009 May 29;324(5931):1199-202. PMID:[19478183](#), DOI:[10.1126/science.1172005](#)

Abstract:

Synthetic gene networks can be constructed to emulate digital circuits and devices, giving one

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the ability to program and design cells with some of the principles of modern computing, such as counting. A cellular counter would enable complex synthetic programming and a variety of biotechnology applications. Here, we report two complementary synthetic genetic counters in *Escherichia coli* that can count up to three induction events: the first, a riboregulated transcriptional cascade, and the second, a recombinase-based cascade of memory units. These modular devices permit counting of varied user-defined inputs over a range of frequencies and can be expanded to count higher numbers.

The 3 arabinose pulses are implemented using events, one for the start of pulses and one for the end. The variable `pulse_flag` changes arabinose consumption to fit behaviour during pulses and in between. To simulate two pulses only, set the pulse length of the third pulse to a negative value (though with an absolute value smaller than the pulse interval length).

Originally created by libAntimony v1.4 (using libSBML 3.4.1)

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To cite BioModels Database, please use: Li C, Donizelli M, Rodriguez N, Dharuri H, Endler L, Chelliah V, Li L, He E, Henry A, Stefan MI, Snoep JL, Hucka M, Le Novre N, Laibe C (2010) BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models. *BMC Syst Biol.*, 4:92.

2 Unit Definitions

This is an overview of five unit definitions which are all predefined by SBML and not mentioned in the model.

2.1 Unit `substance`

Notes Mole is the predefined SBML unit for `substance`.

Definition `mol`

2.2 Unit `volume`

Notes Litre is the predefined SBML unit for `volume`.

Definition `l`

2.3 Unit `area`

Notes Square metre is the predefined SBML unit for `area` since SBML Level 2 Version 1.

Definition `m2`

2.4 Unit length

Notes Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

Definition m

2.5 Unit time

Notes Second is the predefined SBML unit for time.

Definition s

3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
cell		0000290	3	1	litre	<input checked="" type="checkbox"/>	

3.1 Compartment cell

This is a three dimensional compartment with a constant size of one litre.

SBO:0000290 physical compartment

4 Species

This model contains eight species. Section 9 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condition
taRNA		cell	$\text{mol} \cdot \text{l}^{-1}$	\square	\square
mT7cr		cell	$\text{mol} \cdot \text{l}^{-1}$	\square	\square
mGFPcr		cell	$\text{mol} \cdot \text{l}^{-1}$	\square	\square
pT7		cell	$\text{mol} \cdot \text{l}^{-1}$	\square	\square
pGFP		cell	$\text{mol} \cdot \text{l}^{-1}$	\square	\square
ara		cell	$\text{mol} \cdot \text{l}^{-1}$	\square	\square
pT3		cell	$\text{mol} \cdot \text{l}^{-1}$	\square	\square
mT3cr		cell	$\text{mol} \cdot \text{l}^{-1}$	\square	\square

5 Parameters

This model contains 36 global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
cAra			$3 \cdot 10^{-4}$		<input checked="" type="checkbox"/>
pulse_flag			0.000		<input type="checkbox"/>
dAra			0.120		<input checked="" type="checkbox"/>
sT			0.847		<input checked="" type="checkbox"/>
k_ara			0.057		<input checked="" type="checkbox"/>
s0_taRNA			$8 \cdot 10^{-4}$		<input checked="" type="checkbox"/>
d_taRNA			0.118		<input checked="" type="checkbox"/>
s0_mT7cr			0.025		<input checked="" type="checkbox"/>
d_mT7			0.071		<input checked="" type="checkbox"/>
s0_mGFPcr			0.012		<input checked="" type="checkbox"/>
k_pT3			3.006		<input checked="" type="checkbox"/>
n3			0.889		<input checked="" type="checkbox"/>
km3			7.908		<input checked="" type="checkbox"/>
d_mGFP			0.070		<input checked="" type="checkbox"/>
s0_pT7			$3 \cdot 10^{-4}$		<input checked="" type="checkbox"/>
s_pT7k			0.077		<input checked="" type="checkbox"/>
s0_pGFP			0.101		<input checked="" type="checkbox"/>
s_pGFPk			0.992		<input checked="" type="checkbox"/>
d_pT7			0.006		<input checked="" type="checkbox"/>
d_pGFP			0.003		<input checked="" type="checkbox"/>
s0_mT3cr			$3 \cdot 10^{-4}$		<input checked="" type="checkbox"/>
k_pT7			3.801		<input checked="" type="checkbox"/>
n7			2.602		<input checked="" type="checkbox"/>
km7			3.046		<input checked="" type="checkbox"/>
d_mT3			0.070		<input checked="" type="checkbox"/>
s0_pT3			0.000		<input checked="" type="checkbox"/>
s_pT3k			0.012		<input checked="" type="checkbox"/>
d_pT3			0.007		<input checked="" type="checkbox"/>
pulse- _interval			20.000		<input checked="" type="checkbox"/>
pulse1_start			0.010		<input checked="" type="checkbox"/>
pulse1- _length			11.000		<input checked="" type="checkbox"/>
pulse_conc			0.010		<input checked="" type="checkbox"/>
pulse2_start			0.000		<input type="checkbox"/>
pulse2- _length			11.000		<input checked="" type="checkbox"/>

Id	Name	SBO	Value	Unit	Constant
pulse3_start			0.000		<input type="checkbox"/>
pulse3_length			22.000		<input checked="" type="checkbox"/>

6 Rules

This is an overview of two rules.

6.1 Rule `pulse2_start`

Rule `pulse2_start` is an assignment rule for parameter `pulse2_start`:

$$\text{pulse2_start} = \text{pulse1_start} + \text{pulse1_length} + \text{pulse_interval} \quad (1)$$

6.2 Rule `pulse3_start`

Rule `pulse3_start` is an assignment rule for parameter `pulse3_start`:

$$\text{pulse3_start} = \text{pulse2_start} + \text{pulse2_length} + \text{pulse_interval} \quad (2)$$

7 Events

This is an overview of six events. Each event is initiated whenever its trigger condition switches from `false` to `true`. A delay function postpones the effects of an event to a later time point. At the time of execution, an event can assign values to species, parameters or compartments if these are not set to constant.

7.1 Event `pulse_start1`

Trigger condition

$$(\text{time} \geq \text{pulse1_start}) \wedge (\text{time} \leq \text{pulse1_start} + \text{pulse1_length}) \quad (3)$$

Assignments

$$\text{pulse_flag} = 1 \quad (4)$$

$$\text{ara} = \text{pulse_conc} \quad (5)$$

7.2 Event `pulse_start2`

Trigger condition

$$(\text{time} \geq \text{pulse2_start}) \wedge (\text{time} \leq \text{pulse2_start} + \text{pulse2_length}) \quad (6)$$

Assignments

$$\text{pulse_flag} = 1 \quad (7)$$

$$\text{ara} = \text{pulse_conc} \quad (8)$$

7.3 Event `pulse_start3`

Trigger condition

$$(\text{time} \geq \text{pulse3_start}) \wedge (\text{time} \leq \text{pulse3_start} + \text{pulse3_length}) \quad (9)$$

Assignments

$$\text{pulse_flag} = 1 \quad (10)$$

$$\text{ara} = \text{pulse_conc} \quad (11)$$

7.4 Event `pulse_end1`

Trigger condition

$$(\text{time} < \text{pulse2_start}) \wedge (\text{time} > \text{pulse1_start} + \text{pulse1_length}) \quad (12)$$

Assignment

$$\text{pulse_flag} = 0 \quad (13)$$

7.5 Event `pulse_end2`

Trigger condition

$$(\text{time} < \text{pulse3_start}) \wedge (\text{time} > \text{pulse2_start} + \text{pulse2_length}) \quad (14)$$

Assignment

$$\text{pulse_flag} = 0 \quad (15)$$

7.6 Event `pulse_end3`

Trigger condition

$$\text{time} > \text{pulse3_start} + \text{pulse3_length} \quad (16)$$

Assignment

$$\text{pulse_flag} = 0 \quad (17)$$

8 Reactions

This model contains 15 reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	r0		$\text{ara} \longrightarrow \emptyset$	0000179
2	r1a		$\emptyset \xrightarrow{\text{ara}} \text{taRNA}$	0000183
3	r1b		$\text{taRNA} \longrightarrow \emptyset$	0000179
4	r2a		$\emptyset \longrightarrow \text{mT7cr}$	0000183
5	r2b		$\text{mT7cr} \longrightarrow \emptyset$	0000179
6	r3a		$\emptyset \xrightarrow{\text{pT3}} \text{mGFPcr}$	0000183
7	r3b		$\text{mGFPcr} \longrightarrow \emptyset$	0000179
8	r6		$\emptyset \xrightarrow{\text{taRNA, mT7cr}} \text{pT7}$	0000184
9	r7		$\emptyset \xrightarrow{\text{taRNA, mGFPcr}} \text{pGFP}$	0000184
10	r8		$\text{pT7} \longrightarrow \emptyset$	0000179
11	r9		$\text{pGFP} \longrightarrow \emptyset$	0000179
12	r10a		$\emptyset \xrightarrow{\text{pT7}} \text{mT3cr}$	0000183
13	r10b		$\text{mT3cr} \longrightarrow \emptyset$	0000179
14	r11		$\emptyset \xrightarrow{\text{taRNA, mT3cr}} \text{pT3}$	0000184
15	r12		$\text{pT3} \longrightarrow \emptyset$	0000179

8.1 Reaction r0

This is an irreversible reaction of one reactant forming no product.

SBO:0000179 degradation

Reaction equation



Reactant

Table 6: Properties of each reactant.

Id	Name	SBO
ara		

Kinetic Law

Derived unit contains undeclared units

$$v_1 = \text{vol}(\text{cell}) \cdot \begin{cases} c\text{Ara} & \text{if } (\text{pulse_flag} = 1) \wedge ([\text{ara}] > 0) \\ d\text{Ara} \cdot [\text{ara}] & \text{otherwise} \end{cases} \quad (19)$$

8.2 Reaction r1a

This is an irreversible reaction of no reactant forming one product influenced by one modifier.

SBO:0000183 transcription

Reaction equation



Modifier

Table 7: Properties of each modifier.

Id	Name	SBO
ara		

Product

Table 8: Properties of each product.

Id	Name	SBO
taRNA		

Kinetic Law

Derived unit contains undeclared units

$$v_2 = \text{vol}(\text{cell}) \cdot \left(\frac{sT \cdot [\text{ara}]}{[\text{ara}] + k_{\text{ara}}} + s0_{\text{taRNA}} \right) \quad (21)$$

8.3 Reaction r1b

This is an irreversible reaction of one reactant forming no product.

SBO:0000179 degradation

Reaction equation



Reactant

Table 9: Properties of each reactant.

Id	Name	SBO
taRNA		

Kinetic Law

Derived unit contains undeclared units

$$v_3 = \text{vol}(\text{cell}) \cdot d_{\text{taRNA}} \cdot [\text{taRNA}] \quad (23)$$

8.4 Reaction r2a

This is an irreversible reaction of no reactant forming one product.

SBO:0000183 transcription

Reaction equation



Product

Table 10: Properties of each product.

Id	Name	SBO
mT7cr		

Kinetic Law

Derived unit contains undeclared units

$$v_4 = \text{vol}(\text{cell}) \cdot s0_mT7cr \quad (25)$$

8.5 Reaction r2b

This is an irreversible reaction of one reactant forming no product.

SBO:0000179 degradation

Reaction equation



Reactant

Table 11: Properties of each reactant.

Id	Name	SBO
mT7cr		

Kinetic Law

Derived unit contains undeclared units

$$v_5 = \text{vol}(\text{cell}) \cdot d_mT7 \cdot [mT7cr] \quad (27)$$

8.6 Reaction r3a

This is an irreversible reaction of no reactant forming one product influenced by one modifier.

SBO:0000183 transcription

Reaction equation



Modifier

Table 12: Properties of each modifier.

Id	Name	SBO
pT3		

Product

Table 13: Properties of each product.

Id	Name	SBO
mGFPcr		

Kinetic Law

Derived unit contains undeclared units

$$v_6 = \text{vol}(\text{cell}) \cdot \left(s0_mGFPcr + \frac{k_pT3 \cdot [\text{pT3}]^{n3}}{km3^{n3} + [\text{pT3}]^{n3}} \right) \quad (29)$$

8.7 Reaction r3b

This is an irreversible reaction of one reactant forming no product.

SBO:0000179 degradation

Reaction equation



Reactant

Table 14: Properties of each reactant.

Id	Name	SBO
mGFPcr		

Kinetic Law

Derived unit contains undeclared units

$$v_7 = \text{vol}(\text{cell}) \cdot d_{\text{mGFP}} \cdot [\text{mGFPcr}] \quad (31)$$

8.8 Reaction r6

This is an irreversible reaction of no reactant forming one product influenced by two modifiers.

SBO:0000184 translation

Reaction equation



Modifiers

Table 15: Properties of each modifier.

Id	Name	SBO
	taRNA	
	mT7cr	

Product

Table 16: Properties of each product.

Id	Name	SBO
	pT7	

Kinetic Law

Derived unit contains undeclared units

$$v_8 = \text{vol}(\text{cell}) \cdot (s_{0\text{-pT7}} \cdot [\text{mT7cr}] + s_{\text{-pT7k}} \cdot [\text{mT7cr}] \cdot [\text{taRNA}]) \quad (33)$$

8.9 Reaction r7

This is an irreversible reaction of no reactant forming one product influenced by two modifiers.

SBO:0000184 translation

Reaction equation



Modifiers

Table 17: Properties of each modifier.

Id	Name	SBO
	taRNA	
	mGFPcr	

Product

Table 18: Properties of each product.

Id	Name	SBO
	pGFP	

Kinetic Law

Derived unit contains undeclared units

$$v_9 = \text{vol}(\text{cell}) \cdot (s_0\text{-pGFP} \cdot [\text{mGFPcr}] + s\text{-pGFPk} \cdot [\text{mGFPcr}] \cdot [\text{taRNA}]) \quad (35)$$

8.10 Reaction r8

This is an irreversible reaction of one reactant forming no product.

SBO:0000179 degradation

Reaction equation



Reactant

Table 19: Properties of each reactant.

Id	Name	SBO
	pT7	

Kinetic Law

Derived unit contains undeclared units

$$v_{10} = \text{vol}(\text{cell}) \cdot d_{\text{pT7}} \cdot [\text{pT7}] \quad (37)$$

8.11 Reaction r9

This is an irreversible reaction of one reactant forming no product.

SBO:0000179 degradation

Reaction equation



Reactant

Table 20: Properties of each reactant.

Id	Name	SBO
	pGFP	

Kinetic Law

Derived unit contains undeclared units

$$v_{11} = \text{vol}(\text{cell}) \cdot d_{\text{pGFP}} \cdot [\text{pGFP}] \quad (39)$$

8.12 Reaction r10a

This is an irreversible reaction of no reactant forming one product influenced by one modifier.

SBO:0000183 transcription

Reaction equation



Modifier

Table 21: Properties of each modifier.

Id	Name	SBO
pT7		

Product

Table 22: Properties of each product.

Id	Name	SBO
mT3cr		

Kinetic Law

Derived unit contains undeclared units

$$v_{12} = \text{vol}(\text{cell}) \cdot \left(s0_mT3cr + \frac{k_pT7 \cdot [pT7]^{n7}}{km7^{n7} + [pT7]^{n7}} \right) \quad (41)$$

8.13 Reaction r10b

This is an irreversible reaction of one reactant forming no product.

SBO:0000179 degradation

Reaction equation



Reactant

Table 23: Properties of each reactant.

Id	Name	SBO
mT3cr		

Kinetic Law

Derived unit contains undeclared units

$$v_{13} = \text{vol}(\text{cell}) \cdot d_mT3 \cdot [mT3cr] \quad (43)$$

8.14 Reaction r_{11}

This is an irreversible reaction of no reactant forming one product influenced by two modifiers.

SBO:0000184 translation

Reaction equation



Modifiers

Table 24: Properties of each modifier.

Id	Name	SBO
	taRNA	
	mT3cr	

Product

Table 25: Properties of each product.

Id	Name	SBO
	pT3	

Kinetic Law

Derived unit contains undeclared units

$$v_{14} = \text{vol}(\text{cell}) \cdot (s_{0_pT3} \cdot [\text{mT3cr}] + s_{_pT3k} \cdot [\text{taRNA}] \cdot [\text{mT3cr}]) \quad (45)$$

8.15 Reaction r_{12}

This is an irreversible reaction of one reactant forming no product.

SBO:0000179 degradation

Reaction equation



Reactant

Table 26: Properties of each reactant.

Id	Name	SBO
pT3		

Kinetic Law

Derived unit contains undeclared units

$$v_{15} = \text{vol}(\text{cell}) \cdot d_pT3 \cdot [pT3] \quad (47)$$

9 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the `hasOnlySubstanceUnits` flag may be set to `false` and `spacialDimensions` > 0 for certain species.

9.1 Species taRNA

SBO:0000250 ribonucleic acid

Initial concentration 0.006796941377 mol · l⁻¹

This species takes part in five reactions (as a reactant in [r1b](#) and as a product in [r1a](#) and as a modifier in [r6](#), [r7](#), [r11](#)).

$$\frac{d}{dt} \text{taRNA} = v_2 - v_3 \quad (48)$$

9.2 Species mT7cr

SBO:0000250 ribonucleic acid

Initial concentration 0.3569405099 mol · l⁻¹

This species takes part in three reactions (as a reactant in [r2b](#) and as a product in [r2a](#) and as a modifier in [r6](#)).

$$\frac{d}{dt} \text{mT7cr} = v_4 - v_5 \quad (49)$$

9.3 Species `mGFPcr`

SBO:0000250 ribonucleic acid

Initial concentration $0.176991329 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [r3b](#) and as a product in [r3a](#) and as a modifier in [r7](#)).

$$\frac{d}{dt}mGFPcr = v_6 - v_7 \quad (50)$$

9.4 Species `pT7`

SBO:0000252 polypeptide chain

Initial concentration $0.05230744612 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [r8](#) and as a product in [r6](#) and as a modifier in [r10a](#)).

$$\frac{d}{dt}pT7 = v_8 - v_{10} \quad (51)$$

9.5 Species `pGFP`

SBO:0000252 polypeptide chain

Initial concentration $6.338921181 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in [r9](#) and as a product in [r7](#)).

$$\frac{d}{dt}pGFP = v_9 - v_{11} \quad (52)$$

9.6 Species `ara`

SBO:0000247 simple chemical

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

Involved in events [pulse_start1](#), [pulse_start2](#), [pulse_start3](#)

This species takes part in two reactions (as a reactant in [r0](#) and as a modifier in [r1a](#)).

$$\frac{d}{dt}ara = -v_1 \quad (53)$$

Furthermore, three events influence this species' rate of change.

9.7 Species pT3

SBO:0000252 polypeptide chain

Initial concentration $6.41674 \cdot 10^{-5} \text{ mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [r12](#) and as a product in [r11](#) and as a modifier in [r3a](#)).

$$\frac{d}{dt}pT3 = v_{14} - v_{15} \quad (54)$$

9.8 Species mT3cr

SBO:0000250 ribonucleic acid

Initial concentration $0.00566438 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [r10b](#) and as a product in [r10a](#) and as a modifier in [r11](#)).

$$\frac{d}{dt}mT3cr = v_{12} - v_{13} \quad (55)$$

A Glossary of Systems Biology Ontology Terms

SBO:0000179 degradation: Complete disappearance of a physical entity

SBO:0000183 transcription: Process through which a DNA sequence is copied to produce a complementary RNA

SBO:0000184 translation: Process in which a polypeptide chain is produced from a messenger RNA

SBO:0000247 simple chemical: Simple, non-repetitive chemical entity

SBO:0000250 ribonucleic acid: Macromolecule formed by a repetition of ribonucleosides linked by phosphodiester bonds. CHEBI:3369

SBO:0000252 polypeptide chain: Naturally occurring macromolecule formed by the repetition of amino-acid residues linked by peptidic bonds. A polypeptide chain is synthesized by the ribosome. CHEBI:1654

SBO:0000290 physical compartment: Specific location of space, that can be bounded or not. A physical compartment can have 1, 2 or 3 dimensions

SBML²LaTeX was developed by Andreas Dräger^a, Hannes Planatscher^a, Dieudonné M Wouamba^a, Adrian Schröder^a, Michael Hucka^b, Lukas Endler^c, Martin Golebiewski^d and Andreas Zell^a. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

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