# **SBML Model Report**

# Model name: "Arnold2011\_Zhu2009\_CalvinCycle"



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# 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by the following three authors: Vijayalakshmi Chelliah<sup>1</sup>, Anne Arnold<sup>2</sup> and Zoran Nikoloski<sup>3</sup> at October 19<sup>th</sup> 2011 at 2:52 p.m. and last time modified at April 20<sup>th</sup> 2012 at 7:51 p.m. Table 1 provides an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	8
events	0	constraints	0
reactions	7	function definitions	2
global parameters	0	unit definitions	2
rules	1	initial assignments	0

# **Model Notes**

This model is from the article:

# A quantitative comparison of CalvinBenson cycle models

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Anne Arnold, Zoran Nikoloski <u>Trends in Plant Science</u> 2011 Oct 14. 22001849,

# **Abstract:**

The Calvin-Benson cycle (CBC) provides the precursors for biomass synthesis necessary for plant growth. The dynamic behavior and yield of the CBC depend on the environmental conditions and regulation of the cellular state. Accurate quantitative models hold the promise of identifying the key determinants of the tightly regulated CBC function and their effects on the responses in future climates. We provide an integrative analysis of the largest compendium of existing models for photosynthetic processes. Based on the proposed ranking, our framework facilitates the discovery of best-performing models with regard to metabolomics data and of candidates for metabolic engineering.

**Note:** Model of the Calvin cycle by Zhu et al. (2009, DOI:10.1016/j.nonrwa.2008.01.021). The initial metabolite values are chosen from the data set of Zhu et al. (2007, DOI:10.1104/pp.107.103713). A detailed description of all modifications is given in the model described by Arnold and Nikoloski (2011, PMID:22001849).

# 2 Unit Definitions

This is an overview of five unit definitions of which three are predefined by SBML and not mentioned in the model.

#### 2.1 Unit volume

**Definition** 1

# 2.2 Unit substance

**Definition** mmol

# 2.3 Unit area

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition** m<sup>2</sup>

# 2.4 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

#### 2.5 Unit time

**Notes** Second is the predefined SBML unit for time.

**Definition** s

# 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
chloroplast	chloroplast		3	1	litre		

# 3.1 Compartment chloroplast

This is a three dimensional compartment with a constant size of one litre.

Name chloroplast

# 4 Species

This model contains eight species. The boundary condition of three of these species is set to true so that these species' amount cannot be changed by any reaction. Section 8 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
RuBP	RuBP	chloroplast	$\operatorname{mmol} \cdot 1^{-1}$		
PGA	PGA	chloroplast	$\operatorname{mmol} \cdot 1^{-1}$		
DPGA	DPGA	chloroplast	$\operatorname{mmol} \cdot 1^{-1}$		
GAP	GAP	chloroplast	$\operatorname{mmol} \cdot 1^{-1}$		
Ru5P	Ru5P	chloroplast	$\operatorname{mmol} \cdot 1^{-1}$		
ADP	ADP	chloroplast	$\operatorname{mmol} \cdot 1^{-1}$		
ATP	ATP	chloroplast	$\operatorname{mmol} \cdot 1^{-1}$	$\overline{\mathscr{L}}$	$\overline{\mathbf{Z}}$
Pi	Pi	chloroplast	$\text{mmol} \cdot l^{-1}$		$\overline{\mathbf{Z}}$

# 5 Function definitions

This is an overview of two function definitions.

# **5.1 Function definition** function\_1

Name Henri-Michaelis-Menten (irreversible)

Arguments substrate, Km, V

**Mathematical Expression** 

$$\frac{V \cdot substrate}{Km + substrate} \tag{1}$$

# **5.2 Function definition** function\_2

Name MM s2 - reg

Arguments Vm, s1, s2, K1, K2

**Mathematical Expression** 

$$\frac{Vm \cdot s1 \cdot s2}{(s1 + K1) \cdot (s2 + K2)} \tag{2}$$

# 6 Rule

This is an overview of one rule.

# 6.1 Rule Pi

Rule Pi is an assignment rule for species Pi:

$$Pi = 15 - 2 \cdot ([RuBP] + [DPGA] + [ATP]) - ([PGA] + [GAP] + [Ru5P] + [ADP]) \quad (3)$$

# 7 Reactions

This model contains seven reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 4: Overview of all reactions

N⁰	Id	Name	Reaction Equation	SBO
1	RuBisCO	RuBisCO	$RuBP \longrightarrow 2PGA$	
2	PGA_K	PGA kinase	$PGA + ATP \longrightarrow ADP + DPGA$	
3	GAP_DH	GAP dehydrogenase	$DPGA \longrightarrow GAP + Pi$	
4	GAP2Ru5P	GAP to Ru5P	$GAP \longrightarrow 0.6 Ru5P$	
5	Ru5P_K	Ru5P kinase	$Ru5P + ATP \longrightarrow RuBP + ADP$	
6	PGA2sink	PGA to sink	$PGA \longrightarrow \emptyset$	
7	GAP2sink	GAP to sink	$GAP \longrightarrow \emptyset$	

# 7.1 Reaction RuBisCO

This is an irreversible reaction of one reactant forming one product.

#### Name RuBisCO

# **Reaction equation**

$$RuBP \longrightarrow 2PGA \tag{4}$$

# Reactant

Table 5: Properties of each reactant.

Id	Name	SBO
RuBP	RuBP	

# **Product**

Table 6: Properties of each product.

Id	Name	SBO
PGA	PGA	

# **Kinetic Law**

$$v_1 = \text{vol}\left(\text{chloroplast}\right) \cdot \text{function}_{-1}\left([\text{RuBP}], \text{Km}, \text{V}\right)$$
 (5)

$$function\_1 \, (substrate, Km, V) = \frac{V \cdot substrate}{Km + substrate} \tag{6} \label{eq:function}$$

$$function\_1 (substrate, Km, V) = \frac{V \cdot substrate}{Km + substrate}$$
 (7)

Table 7: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Km	Km	0000027	1.00		
V	V	0000009	3.78		$\mathbf{Z}$

# 7.2 Reaction PGA\_K

This is an irreversible reaction of two reactants forming two products.

Name PGA kinase

# **Reaction equation**

$$PGA + ATP \longrightarrow ADP + DPGA \tag{8}$$

# **Reactants**

Table 8: Properties of each reactant.

Id	Name	SBO
PGA	PGA	
ATP	ATP	

# **Products**

Table 9: Properties of each product.

Id	Name	SBO
ADP	ADP	
DPGA	DPGA	

# **Kinetic Law**

$$v_2 = \text{vol}\left(\text{chloroplast}\right) \cdot \text{function} \cdot 2\left(\text{Vm}, [\text{PGA}], [\text{ATP}], \text{K1}, \text{K2}\right)$$
 (9)

function\_2 (Vm, s1, s2, K1, K2) = 
$$\frac{Vm \cdot s1 \cdot s2}{(s1 + K1) \cdot (s2 + K2)}$$
 (10)

function\_2 (Vm, s1, s2, K1, K2) = 
$$\frac{Vm \cdot s1 \cdot s2}{(s1 + K1) \cdot (s2 + K2)}$$
(11)

Table 10: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vm	Vm	0000009	11.75		<b>✓</b>
K1	<b>K</b> 1	0000009	0.24		$\mathbf{Z}$
K2	K2	0000009	0.39		$\mathbf{Z}$

# 7.3 Reaction GAP\_DH

This is an irreversible reaction of one reactant forming two products.

Name GAP dehydrogenase

# **Reaction equation**

$$DPGA \longrightarrow GAP + Pi \tag{12}$$

# Reactant

Table 11: Properties of each reactant.

Id	Name	SBO
DPGA	DPGA	

#### **Products**

Table 12: Properties of each product.

Id	Name	SBO
GAP	GAP	_
Pi	Pi	

# **Kinetic Law**

$$v_3 = \text{vol}\left(\text{chloroplast}\right) \cdot \text{function}_{-1}\left([\text{DPGA}], \text{Km}, \text{V}\right)$$
 (13)

$$function_{-}1 (substrate, Km, V) = \frac{V \cdot substrate}{Km + substrate}$$
 (14)

$$function\_1 (substrate, Km, V) = \frac{V \cdot substrate}{Km + substrate}$$
 (15)

Table 13: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Km	Km	0000027	0.50		lacksquare
V	V	0000009	5.04		

# 7.4 Reaction GAP2Ru5P

This is an irreversible reaction of one reactant forming one product.

Name GAP to Ru5P

# **Reaction equation**

$$GAP \longrightarrow 0.6 Ru5P \tag{16}$$

#### Reactant

Table 14: Properties of each reactant.

Id	Name	SBO
GAP	GAP	

# **Product**

Table 15: Properties of each product.

Id	Name	SBO
Ru5P	Ru5P	

# **Kinetic Law**

$$v_4 = \text{vol}\left(\text{chloroplast}\right) \cdot \text{function}_1\left([\text{GAP}], \text{Km}, \text{V}\right)$$
 (17)

$$function\_1 (substrate, Km, V) = \frac{V \cdot substrate}{Km + substrate}$$
 (18)

$$function\_1 \, (substrate, Km, V) = \frac{V \cdot substrate}{Km + substrate} \tag{19} \label{eq:19}$$

Table 16: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Km	Km	0000027	0.84		lacksquare
V	V	0000009	3.05		

# 7.5 Reaction Ru5P\_K

This is an irreversible reaction of two reactants forming two products.

Name Ru5P kinase

# **Reaction equation**

$$Ru5P + ATP \longrightarrow RuBP + ADP \tag{20}$$

#### **Reactants**

Table 17: Properties of each reactant.

Id	Name	SBO
Ru5P	Ru5P	
ATP	ATP	

#### **Products**

Table 18: Properties of each product.

Id	Name	SBO
RuBP	RuBP	
ADP	ADP	

# **Kinetic Law**

$$v_5 = vol\left(chloroplast\right) \cdot function_2\left(Vm, [Ru5P], [ATP], K1, K2\right) \tag{21}$$

$$function_{-}2 (Vm, s1, s2, K1, K2) = \frac{Vm \cdot s1 \cdot s2}{(s1 + K1) \cdot (s2 + K2)} \tag{22} \label{eq:22}$$

$$function_{-}2\left(Vm, s1, s2, K1, K2\right) = \frac{Vm \cdot s1 \cdot s2}{(s1 + K1) \cdot (s2 + K2)} \tag{23}$$

Table 19: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Vm	Vm	0000009	8.000		
K1	K1	0000009	0.150		$\mathbf{Z}$
K2	K2	0000009	0.059		

# 7.6 Reaction PGA2sink

This is an irreversible reaction of one reactant forming no product.

Name PGA to sink

**Notes** changed velocity in accordance with the authors (Lei et al. (2011))

# **Reaction equation**

$$PGA \longrightarrow \emptyset \tag{24}$$

#### Reactant

Table 20: Properties of each reactant.

Id	Name	SBO
PGA	PGA	

# **Kinetic Law**

$$v_6 = \text{vol}\left(\text{chloroplast}\right) \cdot \text{function\_1}\left([\text{PGA}], \text{Km}, \text{V}\right)$$
 (25)

$$function\_1 \, (substrate, Km, V) = \frac{V \cdot substrate}{Km + substrate} \tag{26} \label{eq:26}$$

$$function\_1 \, (substrate, Km, V) = \frac{V \cdot substrate}{Km + substrate} \tag{27} \label{eq:27}$$

Table 21: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Km	Km	0000027	0.75		$ \overline{\mathscr{A}} $
V	V	0000009	3.00		$\square$

# 7.7 Reaction GAP2sink

This is an irreversible reaction of one reactant forming no product.

Name GAP to sink

# **Reaction equation**

$$GAP \longrightarrow \emptyset \tag{28}$$

# Reactant

Table 22: Properties of each reactant.

Id	Name	SBO
GAP	GAP	

# **Kinetic Law**

Derived unit contains undeclared units

$$v_7 = \text{vol}\left(\text{chloroplast}\right) \cdot \text{function\_1}\left([\text{GAP}], \text{Km}, \text{V}\right)$$
 (29)

$$function\_1 (substrate, Km, V) = \frac{V \cdot substrate}{Km + substrate}$$
 (30)

$$function\_1 (substrate, Km, V) = \frac{V \cdot substrate}{Km + substrate}$$
 (31)

Table 23: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
Km	Km	0000027	5.0		$\checkmark$
V	V	0000009	0.1		$   \overline{\mathbf{Z}} $

# 8 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the

consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the hasOnlySubstanceUnits flag may be set to false and spacialDimensions> 0 for certain species.

# 8.1 Species RuBP

Name RuBP

Initial concentration 2 mmol·l<sup>-1</sup>

This species takes part in two reactions (as a reactant in RuBisCO and as a product in Ru5P\_K).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{RuBP} = |v_5| - |v_1| \tag{32}$$

# 8.2 Species PGA

Name PGA

Initial concentration  $2.4 \text{ } \text{mmol} \cdot l^{-1}$ 

This species takes part in three reactions (as a reactant in PGA\_K, PGA2sink and as a product in RuBisCO).

$$\frac{d}{dt}PGA = 2|v_1| - |v_2| - |v_6| \tag{33}$$

# 8.3 Species DPGA

Name DPGA

Initial concentration  $0.0011 \text{ mmol} \cdot l^{-1}$ 

This species takes part in two reactions (as a reactant in GAP\_DH and as a product in PGA\_K).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{DPGA} = v_2 - v_3 \tag{34}$$

# 8.4 Species GAP

Name GAP

Initial concentration 0.02 mmol·l<sup>-1</sup>

This species takes part in three reactions (as a reactant in GAP2Ru5P, GAP2sink and as a product in GAP\_DH).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{GAP} = |v_3| - |v_4| - |v_7| \tag{35}$$

# 8.5 Species Ru5P

Name Ru5P

Initial concentration  $0.0501 \text{ mmol} \cdot l^{-1}$ 

This species takes part in two reactions (as a reactant in Ru5P\_K and as a product in GAP2Ru5P).

$$\frac{d}{dt}Ru5P = 0.6 v_4 - v_5 \tag{36}$$

# 8.6 Species ADP

Name ADP

Initial concentration  $0.82 \text{ mmol} \cdot 1^{-1}$ 

This species takes part in two reactions (as a product in PGA\_K, Ru5P\_K), which do not influence its rate of change because this constant species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{ADP} = 0\tag{37}$$

# 8.7 Species ATP

Name ATP

Initial concentration 0.68 mmol·l<sup>-1</sup>

This species takes part in two reactions (as a reactant in PGA\_K, Ru5P\_K), which do not influence its rate of change because this constant species is on the boundary of the reaction system:

$$\frac{\mathrm{d}}{\mathrm{d}t}ATP = 0 \tag{38}$$

# 8.8 Species Pi

Name Pi

Initial concentration  $6.3477 \text{ } \text{mmol} \cdot l^{-1}$ 

Involved in rule Pi

This species takes part in one reaction (as a product in GAP\_DH). Not this but one rule determines the species' quantity because this species is on the boundary of the reaction system.

# A Glossary of Systems Biology Ontology Terms

**SBO:000009 kinetic constant:** Numerical parameter that quantifies the velocity of a chemical reaction

**SBO:0000027** Michaelis constant: Substrate concentration at which the velocity of reaction is half its maximum. Michaelis constant is an experimental parameter. According to the underlying molecular mechanism it can be interpreted differently in terms of microscopic constants

SBML2LATEX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX for more information.

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