SBML Model Report

Model name: "Dunster2014 - WBC Interactions (Model1)"



March 14, 2017

1 General Overview

This is a document in SBML Level 3 Version 1 format. This model was created by Thawfeek Varusai¹ at August 16th 2016 at 3:36 p.m. and last time modified at August 17th 2016 at 1:39 p.m. Table 1 provides an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	4
events	0	constraints	0
reactions	10	function definitions	10
global parameters	8	unit definitions	5
rules	0	initial assignments	0

Model Notes

Dunster2014 - WBC Interactions (Model1)

This is a sub-model of a three step modelling study of the inflammatory response. The model includes distinct populations of

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white blood cells namely, macrophages and active and apoptotic neutrophil populations. Neutrophil apoptosis rate is predicted to be crucial for the qualitative nature of the system.

This model is described in the article: The resolution of inflammation: a mathematical model of neutrophil and macrophage interactions. Dunster JL, Byrne HM, King JR. Bull. Math. Biol. 2014 Aug; 76(8): 1953-1980

Abstract:

There is growing interest in inflammation due to its involvement in many diverse medical conditions, including Alzheimer's disease, cancer, arthritis and asthma. The traditional view that resolution of inflammation is a passive process is now being superceded by an alternative hypothesis whereby its resolution is an active, anti-inflammatory process that can be manipulated therapeutically. This shift in mindset has stimulated a resurgence of interest in the biological mechanisms by which inflammation resolves. The anti-inflammatory processes central to the resolution of inflammation revolve around macrophages and are closely related to proinflammatory processes mediated by neutrophils and their ability to damage healthy tissue. We develop a spatially averaged model of inflammation centring on its resolution, accounting for populations of neutrophils and macrophages and incorporating both pro- and anti-inflammatory processes. Our ordinary differential equation model exhibits two outcomes that we relate to healthy and unhealthy states. We use bifurcation analysis to investigate how variation in the system parameters affects its outcome. We find that therapeutic manipulation of the rate of macrophage phagocytosis can aid in resolving inflammation but success is critically dependent on the rate of neutrophil apoptosis. Indeed our model predicts that an effective treatment protocol would take a dual approach, targeting macrophage phagocytosis alongside neutrophil apoptosis.

This model is hosted on BioModels Database and identified by: BIOMD0000000616.

To cite BioModels Database, please use: BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models.

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2 Unit Definitions

This is an overview of five unit definitions.

2.1 Unit length

Name length

Definition m

2.2 Unit area

Name area

 $\textbf{Definition}\ m^2$

2.3 Unit volume

Name volume

Definition 1

2.4 Unit time

Name time

Definition s

2.5 Unit substance

Name substance

Definition mol

3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
default_compartment	Soft_Tissue	0000410	3	1		Ø	

3.1 Compartment default_compartment

This is a three dimensional compartment with a constant size of one litre.

Name Soft_Tissue

SBO:0000410 implicit compartment

4 Species

This model contains four species. Section 8 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
n	n	default_compartment	$\text{mol} \cdot l^{-1}$		
С	c	${\tt default_compartment}$	$\text{mol} \cdot 1^{-1}$		\Box
a	a	${\tt default_compartment}$	$\text{mol} \cdot 1^{-1}$		\Box
m	m	${\tt default_compartment}$	$\text{mol} \cdot l^{-1}$		\Box

5 Parameters

This model contains eight global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO Value U	Init Constant
		0.100	
vt	vt		\mathbf{Z}
Gat	Gat	1.000	\square
Tt	Tt	0.001	\square
Gmt	Gmt	0.010	\square
alt	alt	0.050	\square
Bat	Bat	0.100	
Α	A	1.000	
t1	t1	10.000	$ \overline{\mathbf{Z}} $

6 Function definitions

This is an overview of ten function definitions.

6.1 Function definition Function_for_R2

Name Function for R2

 $\textbf{Arguments} \ \ ModelValue_4, vol\left(default_compartment\right), [n]$

Mathematical Expression

$$\frac{\text{ModelValue_4} \cdot [n]}{\text{vol (default_compartment)}} \tag{1}$$

6.2 Function definition Function_for_R1

Name Function for R1

Arguments [c], vol (default_compartment)

Mathematical Expression

$$\frac{[c]}{\text{vol}\left(\text{default_compartment}\right)} \tag{2}$$

6.3 Function definition Function_for_R6

Name Function for R6

Arguments [c], vol (default_compartment)

Mathematical Expression

$$\frac{[c]}{\text{vol}\left(\text{default_compartment}\right)} \tag{3}$$

6.4 Function definition Function_for_R8

Name Function for R8

Arguments Dunster2014_Model1_WBC_Interactions, ModelValue_10, ModelValue_11, ModelValue_8, vol (default_compartment)

Mathematical Expression

$$\frac{\text{ModelValue_8} \cdot \begin{cases} \left(\text{sinDunster2014_Model1_WBC_Interactions} \right)^2 & \text{if Dunster2014_Model1_WBC_Interactions} < 10 \\ 0 & \text{otherwise} \end{cases}}{\text{vol}\left(\text{default_compartment} \right)}$$

6.5 Function definition Function_for_R5

Name Function for R5

Arguments ModelValue_6, [a], vol (default_compartment), [m]

Mathematical Expression

$$\frac{\text{ModelValue_6} \cdot [m] \cdot [a]}{\text{vol (default_compartment)}}$$
 (5)

6.6 Function definition Function_for_R10

Name Function for R10

Arguments [c], vol (default_compartment)

Mathematical Expression

$$\frac{[c]}{\text{vol}\left(\text{default_compartment}\right)} \tag{6}$$

6.7 Function definition Function_for_R3

Name Function for R3

 $\textbf{Arguments} \ \ ModelValue_4, \ vol\left(default_compartment\right), \ [n]$

Mathematical Expression

$$\frac{\text{ModelValue_4} \cdot [n]}{\text{vol (default_compartment)}} \tag{7}$$

6.8 Function definition Function_for_R4

Name Function for R4

Arguments ModelValue_5, [a], vol (default_compartment)

Mathematical Expression

$$\frac{\text{ModelValue_5} \cdot [a]}{\text{vol (default_compartment)}}$$
 (8)

6.9 Function definition Function_for_R9

Name Function for R9

Arguments ModelValue_5, ModelValue_9, [a], vol (default_compartment)

Mathematical Expression

$$\frac{\text{ModelValue_5} \cdot \frac{[a]^2}{\text{ModelValue_9}^2 + [a]^2}}{\text{vol (default_compartment)}} \tag{9}$$

6.10 Function definition Function_for_R7

Name Function for R7

Arguments ModelValue_7, vol (default_compartment), [m]

Mathematical Expression

$$\frac{\text{ModelValue_7} \cdot [\text{m}]}{\text{vol}(\text{default_compartment})}$$
 (10)

7 Reactions

This model contains ten reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

N⁰	Id	Name	Reaction Equation	SBO
1	R1	R1	$\emptyset \stackrel{C}{\rightleftharpoons} n$	
		R2	$ \emptyset \stackrel{\underline{C}}{\rightleftharpoons} n \\ n \stackrel{\underline{\longrightarrow}}{\rightleftharpoons} \emptyset $	
3	R3	R3	$\emptyset \stackrel{\underline{n}}{\rightleftharpoons} a$ $a \stackrel{}{\rightleftharpoons} \emptyset$	
4	R4	R4	$a \rightleftharpoons \emptyset$	
5	R5	R5	$a \stackrel{\mathbf{m}}{\rightleftharpoons} \emptyset$	
6	R6	R6	$\emptyset \stackrel{C}{\rightleftharpoons} m$	
7	R7	R7	$ m \rightleftharpoons \emptyset $ $ \emptyset \rightleftharpoons c $	
8	R8	R8	$\emptyset \rightleftharpoons c$	
9	R9	R9	$ \emptyset \stackrel{a}{\rightleftharpoons} c c {\rightleftharpoons} \emptyset $	
10	R10	R10	c ==== ∅	

7.1 Reaction R1

This is a reversible reaction of no reactant forming one product influenced by one modifier.

Name R1

Reaction equation

$$\emptyset \stackrel{\mathsf{C}}{\rightleftharpoons} \mathsf{n}$$
 (11)

Modifier

Table 6: Properties of each modifier.

Id	Name	SBO
С	c	

Product

Table 7: Properties of each product.

Id	Name	SBO
n	n	

Kinetic Law

Derived unit $1^{-1} \cdot mol$

$$v_1 = \text{vol}\left(\text{default_compartment}\right) \cdot \text{Function_for_R1}\left([c], \text{vol}\left(\text{default_compartment}\right)\right)$$
 (12)

$$Function_for_R1\left([c], vol\left(default_compartment\right)\right) = \frac{[c]}{vol\left(default_compartment\right)} \tag{13}$$

$$Function_for_R1\left([c], vol\left(default_compartment\right)\right) = \frac{[c]}{vol\left(default_compartment\right)} \tag{14}$$

7.2 Reaction R2

This is a reversible reaction of one reactant forming no product.

Name R2

Reaction equation

$$n \rightleftharpoons \emptyset$$
 (15)

Reactant

Table 8: Properties of each reactant.

Id	Name	SBO
n	n	

Kinetic Law

Derived unit contains undeclared units

$$v_2 = \text{vol}\left(\text{default_compartment}\right) \cdot \text{Function_for_R2}\left(\text{vt}, \text{vol}\left(\text{default_compartment}\right), [n]\right)$$
 (16)

$$Function_for_R2 \, (ModelValue_4, vol \, (default_compartment) \, , [n]) = \frac{ModelValue_4 \cdot [n]}{vol \, (default_compartment)} \end{(17)}$$

$$Function_for_R2 \, (ModelValue_4, vol \, (default_compartment) \, , [n]) = \frac{ModelValue_4 \cdot [n]}{vol \, (default_compartment)} \end{(18)}$$

7.3 Reaction R3

This is a reversible reaction of no reactant forming one product influenced by one modifier.

Name R3

Reaction equation

$$\emptyset \stackrel{\underline{n}}{\rightleftharpoons} a$$
 (19)

Modifier

Table 9: Properties of each modifier.

Id	Name	SBO
n	n	

Product

Table 10: Properties of each product.

Kinetic Law

Derived unit contains undeclared units

$$v_3 = \text{vol}\left(\text{default_compartment}\right) \cdot \text{Function_for_R3}\left(\text{vt}, \text{vol}\left(\text{default_compartment}\right), [n]\right)$$
 (20)

$$Function_for_R3 \, (ModelValue_4, vol \, (default_compartment) \, , [n]) = \frac{ModelValue_4 \cdot [n]}{vol \, (default_compartment)} \, . \eqno(21)$$

$$Function_for_R3 \, (ModelValue_4, vol \, (default_compartment) \, , [n]) = \frac{ModelValue_4 \cdot [n]}{vol \, (default_compartment)} \end{substitute}$$

7.4 Reaction R4

This is a reversible reaction of one reactant forming no product.

Name R4

Reaction equation

$$a \rightleftharpoons \emptyset$$
 (23)

Reactant

Table 11: Properties of each reactant.

Kinetic Law

Derived unit contains undeclared units

$$v_4 = \text{vol}\left(\text{default_compartment}\right) \cdot \text{Function_for_R4}\left(\text{Gat}, [a], \text{vol}\left(\text{default_compartment}\right)\right)$$
 (24)

$$Function_for_R4 \\ (ModelValue_5, [a], vol \\ (default_compartment)) = \frac{ModelValue_5 \cdot [a]}{vol \\ (default_compartment)}$$
 (25)

$$Function_for_R4 \\ (ModelValue_5, [a], vol \\ (default_compartment)) = \frac{ModelValue_5 \cdot [a]}{vol \\ (default_compartment)}$$
 (26)

7.5 Reaction R5

This is a reversible reaction of one reactant forming no product influenced by one modifier.

Name R5

Reaction equation

$$a \stackrel{\text{m}}{\rightleftharpoons} \emptyset$$
 (27)

Reactant

Table 12: Properties of each reactant.

Id	Name	SBO
a	a	

Modifier

Table 13: Properties of each modifier.

Id	Name	SBO
m	m	

Kinetic Law

Derived unit contains undeclared units

$$v_5 = \text{vol}\left(\text{default_compartment}\right) \cdot \text{Function_for_R5}\left(\text{Tt}, [a], \text{vol}\left(\text{default_compartment}\right), [m]\right)$$
 (28)

$$\begin{aligned} & Function_for_R5 \, (ModelValue_6, [a], vol \, (default_compartment) \,, [m]) \\ &= \frac{ModelValue_6 \cdot [m] \cdot [a]}{vol \, (default_compartment)} \end{aligned} \tag{29}$$

$$\begin{aligned} & Function_for_R5 \, (ModelValue_6, [a], vol \, (default_compartment) \,, [m]) \\ &= \frac{ModelValue_6 \cdot [m] \cdot [a]}{vol \, (default_compartment)} \end{aligned} \tag{30}$$

7.6 Reaction R6

This is a reversible reaction of no reactant forming one product influenced by one modifier.

Name R6

Reaction equation

$$\emptyset \stackrel{\mathbf{c}}{\rightleftharpoons} \mathbf{m}$$
 (31)

Modifier

Table 14: Properties of each modifier.

Id	Name	SBO
С	c	

Product

Table 15: Properties of each product.

Id	Name	SBO
m	m	

Kinetic Law

Derived unit $1^{-1} \cdot mol$

$$v_6 = \text{vol}\left(\text{default_compartment}\right) \cdot \text{Function_for_R6}\left([c], \text{vol}\left(\text{default_compartment}\right)\right) \quad (32)$$

$$Function_for_R6\left([c], vol\left(default_compartment\right)\right) = \frac{[c]}{vol\left(default_compartment\right)} \tag{33}$$

$$Function_for_R6\left([c], vol\left(default_compartment\right)\right) = \frac{[c]}{vol\left(default_compartment\right)} \tag{34}$$

7.7 Reaction R7

This is a reversible reaction of one reactant forming no product.

Name R7

Reaction equation

$$m \rightleftharpoons \emptyset$$
 (35)

Reactant

Table 16: Properties of each reactant.

Id	Name	SBO
m	m	

Kinetic Law

Derived unit contains undeclared units

$$v_7 = \text{vol} (\text{default_compartment}) \cdot \text{Function_for_R7} (\text{Gmt}, \text{vol} (\text{default_compartment}), [m])$$
 (36)

$$Function_for_R7 \\ (ModelValue_7, vol \\ (default_compartment), [m]) = \frac{ModelValue_7 \cdot [m]}{vol \\ (default_compartment)} \\ (37)$$

$$Function_for_R7 \\ (ModelValue_7, vol \\ (default_compartment), [m]) = \frac{ModelValue_7 \cdot [m]}{vol \\ (default_compartment)} \\ (38)$$

7.8 Reaction R8

This is a reversible reaction of no reactant forming one product.

Name R8

Reaction equation

$$\emptyset \rightleftharpoons c$$
 (39)

Product

Table 17: Properties of each product.

Id	Name	SBO
С	c	

Kinetic Law

Derived unit contains undeclared units

$$v_8 = \text{vol} (\text{default_compartment}) \cdot \text{Function_for_R8} (\text{time}, A, t1, alt, vol (\text{default_compartment}))} \tag{40}$$
 Function_for_R8 (Dunster2014_Model1_WBC_Interactions, \tag{41}) \text{ModelValue_10, ModelValue_11, ModelValue_8, vol (default_compartment))} \text{ModelValue_8} \cdot \begin{cases} \{ (\sin Dunster2014_Model1_WBC_Interactions)^2 & \text{if Dunster2014_Model1_WBC_Interactions} \\ 0 & \text{otherwise} \end{cases} \text{Vol (default_compartment)} \text{Vol (default_compartment)} \text{ModelValue_10, ModelValue_11, ModelValue_8, vol (default_compartment))} \text{ModelValue_8} \cdot \begin{cases} \{ (\sin Dunster2014_Model1_WBC_Interactions)^2 & \text{if Dunster2014_Model1_WBC_Interactions} \\ 0 & \text{otherwise} \end{cases} \text{Vol Dunster2014_Model1_WBC_Interactions} \\ \text{Otherwise} \end{cases} \text{Vol Dunster2014_Model1_WBC_Interactions} \\ \text{Otherwise} \\ \text{Otherwise} \end{cases} \text{Vol Dunster2014_Model1_WBC_Interactions} \\ \text{Otherwise} \\ \text{Otherwise} \\ \text{Otherwise} \\ \text{Otherwise} \\ \text{Otherwise} \\ \text{Otherwise} \\ \end{cases} \text{Otherwise} \\ \end{cases} \text{Otherwise} \\ \te

7.9 Reaction R9

This is a reversible reaction of no reactant forming one product influenced by one modifier.

Name R9

Reaction equation

$$\emptyset \stackrel{a}{\rightleftharpoons} c$$
 (43)

Modifier

Table 18: Properties of each modifier.

Id	Name	SBO
a	a	

vol (default_compartmen

Product

Table 19: Properties of each product.

Id	Name	SBO
С	c	

Kinetic Law

Derived unit contains undeclared units

$$v_9 = vol\left(default_compartment\right) \cdot Function_for_R9\left(Gat, Bat, [a], vol\left(default_compartment\right)\right) \tag{44}$$

 $Function_for_R9 \, (ModelValue_5, ModelValue_9, [a], vol \, (default_compartment))$

$$= \frac{\text{ModelValue_5} \cdot \frac{[a]^2}{\text{ModelValue_9}^2 + [a]^2}}{\text{vol (default_compartment)}}$$
(45)

 $Function_for_R9 \, (ModelValue_5, ModelValue_9, [a], vol \, (default_compartment))$

$$= \frac{\text{ModelValue}_{-5} \cdot \frac{[a]^2}{\text{ModelValue}_{-9^2 + [a]^2}}}{\text{vol}\left(\text{default_compartment}\right)}$$
(46)

7.10 Reaction R10

This is a reversible reaction of one reactant forming no product.

Name R10

Reaction equation

$$c \rightleftharpoons \emptyset$$
 (47)

Reactant

Table 20: Properties of each reactant.

Id	Name	SBO
С	c	

Kinetic Law

Derived unit $1^{-1} \cdot \text{mol}$

$$v_{10} = \text{vol} \left(\text{default_compartment} \right) \cdot \text{Function_for_R10} \left([c], \text{vol} \left(\text{default_compartment} \right) \right)$$
 (48)

$$Function_for_R10([c], vol(default_compartment)) = \frac{[c]}{vol(default_compartment)}$$
 (49)

$$Function_for_R10([c], vol(default_compartment)) = \frac{[c]}{vol(default_compartment)}$$
 (50)

8 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the hasOnlySubstanceUnits flag may be set to false and spacialDimensions > 0 for certain species.

8.1 Species n

Name n

SBO:0000410 implicit compartment

Notes Active neutrophils

Initial concentration $0 \text{ mol} \cdot l^{-1}$

This species takes part in three reactions (as a reactant in R2 and as a product in R1 and as a modifier in R3).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathbf{n} = |v_1| - |v_2| \tag{51}$$

8.2 Species c

Name c

SBO:0000410 implicit compartment

Notes Pro-inammatory mediators

Initial concentration $0 \text{ mol} \cdot 1^{-1}$

This species takes part in five reactions (as a reactant in R10 and as a product in R8, R9 and as a modifier in R1, R6).

$$\frac{d}{dt}c = |v_8| + |v_9| - |v_{10}| \tag{52}$$

8.3 Species a

Name a

SBO:0000410 implicit compartment

Notes Apoptotic neutrophils

Initial concentration $0 \text{ mol} \cdot l^{-1}$

This species takes part in four reactions (as a reactant in R4, R5 and as a product in R3 and as a modifier in R9).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathbf{a} = |v_3| - |v_4| - |v_5| \tag{53}$$

8.4 Species m

Name m

SBO:0000410 implicit compartment

Notes Macrophages

Initial concentration $0 \text{ mol} \cdot l^{-1}$

This species takes part in three reactions (as a reactant in R7 and as a product in R6 and as a modifier in R5).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathbf{m} = |v_6| - |v_7| \tag{54}$$

A Glossary of Systems Biology Ontology Terms

SBO:0000410 implicit compartment: A compartment whose existence is inferred due to the presence of known material entities which must be bounded, allowing the creation of material entity pools

 $\mathfrak{BML2}^{AT}$ EX was developed by Andreas Dräger^a, Hannes Planatscher^a, Dieudonné M Wouamba^a, Adrian Schröder^a, Michael Hucka^b, Lukas Endler^c, Martin Golebiewski^d and Andreas Zell^a. Please see http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX for more information.

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