

## SBML Model Report

# Model name: “Baker2013 - Cytokine Mediated Inflammation in Rheumatoid Arthritis - Age Dependant”



May 6, 2016

## 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by Vincent Knight-Schrijver<sup>1</sup> at September 25<sup>th</sup> 2014 at 1:46 p.m. and last time modified at April eighth 2016 at 5:41 p.m. Table 1 provides an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	2
events	0	constraints	0
reactions	0	function definitions	0
global parameters	8	unit definitions	3
rules	3	initial assignments	0

## Model Notes

Baker2013 - Cytokine Mediated Inflammation in Rheumatoid Arthritis - Age Dependant This model by Baker M. 2013, describes the interaction between pro and anti-inflammatory cytokine signalling in rheumatoid arthritis.

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Using two ordinary differential equations, the first model [\[BIOMD0000000550\]](#) analyses bifurcation and describes different pathological states by altering inflammatory regulation parameters. The second model [\[BIOMD0000000549\]](#) includes the effect that ageing has on pro-inflammatory signalling, allowing for time-dependant properties and disease progression to be observed. The author also describes potential dosing for reversal of the disease state.

This model is described in the article: [Mathematical modelling of cytokine-mediated inflammation in rheumatoid arthritis](#). Baker M, Denman-Johnson S, Brook BS, Gaywood I, Owen MR. Math Med Biol 2013 Dec; 30(4): 311-337

**Abstract:**

Rheumatoid arthritis (RA) is a chronic inflammatory disease preferentially affecting the joints and leading, if untreated, to progressive joint damage and disability. Cytokines, a group of small inducible proteins, which act as intercellular messengers, are key regulators of the inflammation that characterizes RA. They can be classified into pro-inflammatory and anti-inflammatory groups. Numerous cytokines have been implicated in the regulation of RA with complex up and down regulatory interactions. This paper considers a two-variable model for the interactions between pro-inflammatory and anti-inflammatory cytokines, and demonstrates that mathematical modelling may be used to investigate the involvement of cytokines in the disease process. The model displays a range of possible behaviours, such as bistability and oscillations, which are strongly reminiscent of the behaviour of RA e.g. genetic susceptibility and remitting-relapsing disease. We also show that the dose regimen as well as the dose level are important factors in RA treatments.

This model is hosted on [BioModels Database](#) and identified by: [BIOMD0000000549](#).

To cite BioModels Database, please use: [BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models](#).

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## 2 Unit Definitions

This is an overview of five unit definitions of which two are predefined by SBML and not mentioned in the model.

### 2.1 Unit volume

**Name** volume

**Definition** dimensionless

### 2.2 Unit time

**Name** time

**Definition** dimensionless

### 2.3 Unit `substance`

**Name** substance

**Definition** dimensionless

### 2.4 Unit `area`

**Notes** Square metre is the predefined SBML unit for `area` since SBML Level 2 Version 1.

**Definition**  $\text{m}^2$

### 2.5 Unit `length`

**Notes** Metre is the predefined SBML unit for `length` since SBML Level 2 Version 1.

**Definition** m

## 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
compartment_1	Synovium		3	1	dimensionless	<input checked="" type="checkbox"/>	

### 3.1 Compartment `compartment_1`

This is a three dimensional compartment with a constant size of one dimensionless.

**Name** Synovium

**Notes** Compartment notes: `{\textquotestraightdblbase}`The synovium is modelled as a spatial

## 4 Species

This model contains two species. The boundary condition of two of these species is set to `true` so that these species' amount cannot be changed by any reaction. Section 7 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condition
species_1	a	compartment_1	dimensionless dimensionless <sup>-1</sup>	· <input type="checkbox"/>	<input checked="" type="checkbox"/>
species_2	p	compartment_1	dimensionless dimensionless <sup>-1</sup>	· <input type="checkbox"/>	<input checked="" type="checkbox"/>

## 5 Parameters

This model contains eight global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
parameter_1	alpha1		0.025		<input checked="" type="checkbox"/>
parameter_2	alpha2		1.000		<input type="checkbox"/>
parameter_3	alpha3		0.500		<input checked="" type="checkbox"/>
parameter_4	alpha4		7.000		<input checked="" type="checkbox"/>
parameter_5	gamma		1.250		<input checked="" type="checkbox"/>
parameter_6	alpha2T		15.000		<input checked="" type="checkbox"/>
parameter_7	alpha2_min		1.000		<input checked="" type="checkbox"/>
parameter_8	alpha2_max		50.000		<input checked="" type="checkbox"/>

## 6 Rules

This is an overview of three rules.

### 6.1 Rule `parameter_2`

Rule `parameter_2` is an assignment rule for parameter `parameter_2`:

$$\text{parameter\_2} = \text{parameter\_7} + \frac{(\text{parameter\_8} - \text{parameter\_7}) \cdot \text{time}^2}{\text{parameter\_6}^2 + \text{time}^2} \quad (1)$$

### 6.2 Rule `species_1`

Rule `species_1` is a rate rule for species `species_1`:

$$\frac{d}{dt} \text{species\_1} = [\text{species\_1}] + \text{parameter\_4} \cdot \frac{[\text{species\_2}]^2}{\text{parameter\_3}^2 + [\text{species\_2}]^2} \quad (2)$$

### 6.3 Rule `species_2`

Rule `species_2` is a rate rule for species `species_2`:

$$\begin{aligned} \frac{d}{dt} \text{species\_2} = & \text{parameter\_5} \cdot [\text{species\_2}] + \frac{1}{1 + [\text{species\_1}]^2} \\ & \cdot \left( \text{parameter\_1} + \text{parameter\_2} \cdot \frac{[\text{species\_2}]^2}{1 + [\text{species\_2}]^2} \right) \end{aligned} \quad (3)$$

## 7 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

### 7.1 Species `species_1`

**Name** `a`

**Notes** Anti-inflammatory cytokine concentration (dimensionless)

**Initial concentration** `0.00577667577789773 dimensionless · dimensionless-1`

**Involved in rule** `species_1`

One rule determines the species' quantity.

### 7.2 Species `species_2`

**Name** `p`

**Notes** Pro-inflammatory cytokine concentration (dimensionless)

**Initial concentration** `0.0203298264712407 dimensionless · dimensionless-1`

**Involved in rule** `species_2`

One rule determines the species' quantity.

SBML2<sup>A</sup>TeX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

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