

SBML Model Report

Model name: “Koo2013 - Shear stress induced calcium influx and eNOS activation - Model 1”



May 5, 2016

1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by the following three authors: Nick Juty¹, Vijayalakshmi Chelliah² and Andrew Koo³ at August 19th 2013 at 1:33 p. m. and last time modified at April seventh 2014 at 2:58 a. m. Table 1 gives an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	3
species types	0	species	14
events	0	constraints	0
reactions	10	function definitions	0
global parameters	27	unit definitions	10
rules	0	initial assignments	0

2 Unit Definitions

This is an overview of ten unit definitions.

¹EMBL-EBI, juty@ebi.ac.uk

²EMBL-EBI, viji@ebi.ac.uk

³Massachusetts Institute of Technology, kooj@mit.edu

2.1 Unit time

Name time

Definition s

2.2 Unit substance

Name substance

Definition 10^{-9} mol

2.3 Unit area

Name area

Definition m^2

2.4 Unit length

Name length

Definition m

2.5 Unit volume

Name volume

Definition l

2.6 Unit sub_sec

Name sub_sec

Definition $10^{-9} \text{ mol} \cdot \text{s}^{-1}$

2.7 Unit inv_sec

Name inv_sec

Definition s^{-1}

2.8 Unit inv_sec_sub

Name inv_sec_sub

Definition $(10^{-9} \text{ mol})^{-1} \cdot \text{s}^{-1}$

2.9 Unit `nM_inv_s`

Name `nM_inv_s`

Definition $\text{nmol} \cdot \text{s}^{-1}$

2.10 Unit `inv_nM_s`

Name `inv_nM_s`

Definition $\text{nmol}^{-1} \cdot \text{s}^{-1}$

3 Compartments

This model contains three compartments.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
default			3	1	litre	✓	
c1	Cell		3	1	litre	✓	default
c2	ER		3	1	litre	✓	c1

3.1 Compartment `default`

This is a three dimensional compartment with a constant size of one litre.

3.2 Compartment `c1`

This is a three dimensional compartment with a constant size of one litre, which is surrounded by `default`.

Name `Cell`

3.3 Compartment `c2`

This is a three dimensional compartment with a constant size of one litre, which is surrounded by `c1` (Cell).

Name `ER`

4 Species

This model contains 14 species. Section 7 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condition
s1	Ca _{ex}	default	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s2	Ca _s	c2	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s3	Ca _c	c1	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s4	Ca _B	c1	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s5	s5	default	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s6	IP3	c1	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s7	s7	c1	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s8	s8	c1	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s9	s9	c1	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s10	s10	c1	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s11	s11	c1	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s12	TimeT	default	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s13	s13	default	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>
s119	Shear Stress	default	10 ⁻⁹ mol	<input type="checkbox"/>	<input type="checkbox"/>

5 Parameters

This model contains 27 global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
R_T	R_T		44000.000	dimensionless	✓
k1	k1		$6 \cdot 10^{-4}$	$10^{-9} \text{ mol} \cdot \text{s}^{-1}$	✓
k2	k2		1.000	s^{-1}	✓
k3	k3		3.320	s^{-1}	✓
k4	k4		2500.000	$10^{-9} \text{ mol} \cdot \text{s}^{-1}$	✓
k5	k5		$5 \cdot 10^{-11}$	$(10^{-9} \text{ mol})^{-1} \cdot \text{s}^{-1}$	✓
k6	k6		0.050	$(10^{-9} \text{ mol})^{-1} \cdot \text{s}^{-1}$	✓
k7	k7		150.000	s^{-1}	✓
K1	K1		0.000	10^{-9} mol	✓
K2	K2		200.000	10^{-9} mol	✓
K3	K3		150.000	10^{-9} mol	✓
K4	K4		80.000	10^{-9} mol	✓
K5	K5		321.000	10^{-9} mol	✓
K_hi	K_hi		380.000	10^{-9} mol	✓
k_CICR	k_CICR		1.000	dimensionless	✓
K_CICR	K_CICR		0.000	10^{-9} mol	✓
k_CCE	k_CCE		0.000	$(10^{-9} \text{ mol})^{-1} \cdot \text{s}^{-1}$	✓
B_T	B_T		120000.000	10^{-9} mol	✓
dot_Vp	dot_Vp		815.000	$10^{-9} \text{ mol} \cdot \text{s}^{-1}$	✓
dot_Vex	dot_Vex		9165.000	$10^{-9} \text{ mol} \cdot \text{s}^{-1}$	✓
dot_Vhi	dot_Vhi		2380.000	$10^{-9} \text{ mol} \cdot \text{s}^{-1}$	✓
dot_q_inpass	dot_q_inpass		3000.000	$10^{-9} \text{ mol} \cdot \text{s}^{-1}$	✓
Cao	Cao		100.000	10^{-9} mol	✓
tau_I	tau_I		66.000	10^{-9} mol	✓
tau_II	tau_II		0.010	10^{-9} mol	✓
half	half		0.500	dimensionless	✓
fracK	fracK		7071067.810	10^{-9} mol	✓

6 Reactions

This model contains ten reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	re3	re1	$s4 \xrightarrow{s3, s4, s3, s4} s3$	
2	re4		$s5 \xrightarrow{s1, s2, s1, s2, s1} s2$	
3	re5		$s7 \xrightarrow{s3, s12, s119, s12, s3, s12, s3} s6$	
4	re6		$s6 \xrightarrow{s6, s6} s8$	
5	re7		$s2 \xrightarrow{s6, s3, s6, s2, s3, s6, s2} s3$	
6	re8		$s3 \xrightarrow{s3, s3} s9$	
7	re9		$s3 \xrightarrow{s3, s3} s10$	
8	re10		$s11 \longrightarrow s3$	
9	re11		$s13 \longrightarrow s12$	
10	re12		$s3 \xrightarrow{s3, s3} s9$	

6.1 Reaction re3

This is an irreversible reaction of one reactant forming one product influenced by four modifiers.

Name re1

Reaction equation



Reactant

Table 6: Properties of each reactant.

Id	Name	SBO
s4	Ca_B	

Modifiers

Table 7: Properties of each modifier.

Id	Name	SBO
s3	Ca_c	
s4	Ca_B	
s3	Ca_c	
s4	Ca_B	

Product

Table 8: Properties of each product.

Id	Name	SBO
s3	Ca_c	

Kinetic Law

Derived unit $s^{-1} \cdot 10^{-9} \text{ mol}$

$$v_1 = k6 \cdot s3 \cdot (B_T - s4) + k7 \cdot s4$$

(2)

6.2 Reaction re4

This is an irreversible reaction of one reactant forming one product influenced by five modifiers.

Reaction equation



Reactant

Table 9: Properties of each reactant.

Id	Name	SBO
s5	s5	

Modifiers

Table 10: Properties of each modifier.

Id	Name	SBO
s1	Ca_ex	
s2	Ca_s	
s1	Ca_ex	
s2	Ca_s	
s1	Ca_ex	

Product

Table 11: Properties of each product.

Id	Name	SBO
s2	Ca_s	

Kinetic Law

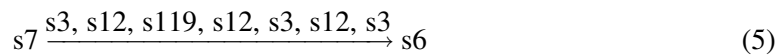
Derived unit $s^{-1} \cdot 10^{-9} \text{ mol}$

$$v_2 = k_CCE \cdot \left(\frac{\text{fracK} \cdot \text{Cao}}{\text{K3} + \text{Cao}} - s2 \right) \cdot (s1 - s2) \quad (4)$$

6.3 Reaction re5

This is an irreversible reaction of one reactant forming one product influenced by seven modifiers.

Reaction equation



Reactant

Table 12: Properties of each reactant.

Id	Name	SBO
s7	s7	

Modifiers

Table 13: Properties of each modifier.

Id	Name	SBO
s3	Ca_c	
s12	TimeT	
s119	Shear Stress	
s12	TimeT	
s3	Ca_c	
s12	TimeT	
s3	Ca_c	

Product

Table 14: Properties of each product.

Id	Name	SBO
s6	IP3	

Kinetic Law

Derived unit $9.999999999999998 \cdot 10^{-10} \text{ mol} \cdot \text{s}^{-1}$

$$v_3 = \frac{k1 \cdot \left(R_T - \text{half} \cdot R_T \cdot \left(\exp\left(\frac{s12}{\text{tau}_I}\right) + \exp\left(\frac{s12}{\text{tau}_{II}}\right) + \frac{\left(\exp\left(\frac{s12}{\text{tau}_I}\right) - \exp\left(\frac{s12}{\text{tau}_{II}}\right)\right) \cdot (\text{tau}_I + \text{tau}_{II})}{\text{tau}_I - \text{tau}_{II}} \right) \right)}{K1 + s3} \quad (6)$$

6.4 Reaction re6

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

Reaction equation



Reactant

Table 15: Properties of each reactant.

Id	Name	SBO
s6	IP3	

Modifiers

Table 16: Properties of each modifier.

Id	Name	SBO
s6	IP3	
s6	IP3	

Product

Table 17: Properties of each product.

Id	Name	SBO
s8	s8	

Kinetic Law

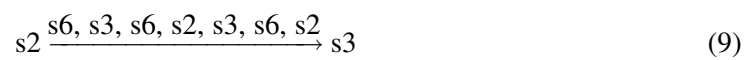
Derived unit $s^{-1} \cdot 10^{-9} \text{ mol}$

$$v_4 = k2 \cdot s6 \quad (8)$$

6.5 Reaction re7

This is an irreversible reaction of one reactant forming one product influenced by seven modifiers.

Reaction equation



Reactant

Table 18: Properties of each reactant.

Id	Name	SBO
s2	Ca_s	

Modifiers

Table 19: Properties of each modifier.

Id	Name	SBO
s6	IP3	
s3	Ca_c	
s6	IP3	
s2	Ca_s	
s3	Ca_c	
s6	IP3	
s2	Ca_s	

Product

Table 20: Properties of each product.

Id	Name	SBO
s3	Ca_c	

Kinetic Law

Derived unit $s^{-1} \cdot 10^{-9} \text{ mol}$

$$v_5 = k_3 \cdot \frac{k_{\text{CICR}} \cdot s_3}{K_{\text{CICR}} + s_3} \cdot \left(\frac{s_6}{K_2 + s_6} \right)^3 \cdot s_2 - k_4 \cdot \left(\frac{s_3}{K_3 + s_3} \right)^2 + k_5 \cdot s_2 \cdot s_2 \quad (10)$$

6.6 Reaction re8

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

Reaction equation



Reactant

Table 21: Properties of each reactant.

Id	Name	SBO
s3	Ca_c	

Modifiers

Table 22: Properties of each modifier.

Id	Name	SBO
s3	Ca_c	
s3	Ca_c	

Product

Table 23: Properties of each product.

Id	Name	SBO
s9	s9	

Kinetic Law

Derived unit 9.99999999999994 · 10⁻¹⁰ mol · s⁻¹

$$v_6 = \frac{\text{dot_Vhi} \cdot s3^4}{K_hi^4 + s3^4} \tag{12}$$

6.7 Reaction re9

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

Reaction equation



Reactant

Table 24: Properties of each reactant.

Id	Name	SBO
s3	Ca_c	

Modifiers

Table 25: Properties of each modifier.

Id	Name	SBO
s3	Ca_c	
s3	Ca_c	

Product

Table 26: Properties of each product.

Id	Name	SBO
s10	s10	

Kinetic Law

Derived unit $9.999999999999998 \cdot 10^{-10} \text{ mol} \cdot \text{s}^{-1}$

$$v_7 = \frac{\text{dot_Vex} \cdot s_3}{K_5 + s_3} \quad (14)$$

6.8 Reaction re10

This is an irreversible reaction of one reactant forming one product.

Reaction equation



Reactant

Table 27: Properties of each reactant.

Id	Name	SBO
s11	s11	

Product

Table 28: Properties of each product.

Id	Name	SBO
s3	Ca_c	

Kinetic Law

Derived unit $10^{-9} \text{ mol} \cdot \text{s}^{-1}$

$$v_8 = \text{dot.q.inpass} \quad (16)$$

6.9 Reaction re11

This is an irreversible reaction of one reactant forming one product.

Reaction equation



Reactant

Table 29: Properties of each reactant.

Id	Name	SBO
s13	s13	

Product

Table 30: Properties of each product.

Id	Name	SBO
s12	TimeT	

Kinetic Law

Derived unit $10^{-9} \text{ mol} \cdot \text{s}^{-1}$

$$v_9 = \text{unisec} \quad (18)$$

Table 31: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
unisec			1.0	$10^{-9} \text{ mol} \cdot \text{s}^{-1}$	<input checked="" type="checkbox"/>

6.10 Reaction re12

This is an irreversible reaction of one reactant forming one product influenced by two modifiers.

Reaction equation



Reactant

Table 32: Properties of each reactant.

Id	Name	SBO
s3	Ca_c	

Modifiers

Table 33: Properties of each modifier.

Id	Name	SBO
s3	Ca_c	
s3	Ca_c	

Product

Table 34: Properties of each product.

Id	Name	SBO
s9	s9	

Kinetic Law

Derived unit $1.0000000000000038 \cdot 10^{-9} \text{ mol} \cdot \text{s}^{-1}$

$$v_{10} = \frac{\text{dot_Vp} \cdot s3^2}{K4^2 + s3^2} \quad (20)$$

7 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

7.1 Species s_1

Name Ca_{ex}

Initial amount 1500000

Charge 0

This species takes part in three reactions (as a modifier in [re4](#), [re4](#), [re4](#)).

$$\frac{d}{dt}s_1 = 0 \quad (21)$$

7.2 Species s_2

Name Ca_s

Initial amount 2830000

Charge 0

This species takes part in six reactions (as a reactant in [re7](#) and as a product in [re4](#) and as a modifier in [re4](#), [re4](#), [re7](#), [re7](#)).

$$\frac{d}{dt}s_2 = v_2 - v_5 \quad (22)$$

7.3 Species s_3

Name Ca_c

Initial amount 117.2

Charge 0

This species takes part in 19 reactions (as a reactant in [re8](#), [re9](#), [re12](#) and as a product in [re3](#), [re7](#), [re10](#) and as a modifier in [re3](#), [re3](#), [re5](#), [re5](#), [re5](#), [re7](#), [re7](#), [re8](#), [re8](#), [re9](#), [re9](#), [re12](#), [re12](#)).

$$\frac{d}{dt}s_3 = v_1 + v_5 + v_8 - v_6 - v_7 - v_{10} \quad (23)$$

7.4 Species s4

Name Ca₂B

SBO:0000297 protein complex

Initial amount 3870

Charge 0

This species takes part in three reactions (as a reactant in [re3](#) and as a modifier in [re3](#), [re3](#)).

$$\frac{d}{dt}s4 = -v_1 \quad (24)$$

7.5 Species s5

Name s5

SBO:0000291 empty set

Initial amount 0

Charge 0

This species takes part in one reaction (as a reactant in [re4](#)).

$$\frac{d}{dt}s5 = -v_2 \quad (25)$$

7.6 Species s6

Name IP3

Initial amount 0

Charge 0

This species takes part in seven reactions (as a reactant in [re6](#) and as a product in [re5](#) and as a modifier in [re6](#), [re6](#), [re7](#), [re7](#), [re7](#)).

$$\frac{d}{dt}s6 = v_3 - v_4 \quad (26)$$

7.7 Species s_7

Name s_7

SBO:0000291 empty set

Initial amount 0

Charge 0

This species takes part in one reaction (as a reactant in [re5](#)).

$$\frac{d}{dt}s_7 = -v_3 \quad (27)$$

7.8 Species s_8

Name s_8

SBO:0000291 empty set

Initial amount 0

Charge 0

This species takes part in one reaction (as a product in [re6](#)).

$$\frac{d}{dt}s_8 = v_4 \quad (28)$$

7.9 Species s_9

Name s_9

SBO:0000291 empty set

Initial amount 0

Charge 0

This species takes part in two reactions (as a product in [re8](#), [re12](#)).

$$\frac{d}{dt}s_9 = v_6 + v_{10} \quad (29)$$

7.10 Species s10

Name s10

SBO:0000291 empty set

Initial amount 0

Charge 0

This species takes part in one reaction (as a product in [re9](#)).

$$\frac{d}{dt}s_{10} = v_7 \quad (30)$$

7.11 Species s11

Name s11

SBO:0000291 empty set

Initial amount 0

Charge 0

This species takes part in one reaction (as a reactant in [re10](#)).

$$\frac{d}{dt}s_{11} = -v_8 \quad (31)$$

7.12 Species s12

Name TimeT

SBO:0000331 half-life

Initial amount 0

Charge 0

This species takes part in four reactions (as a product in [re11](#) and as a modifier in [re5](#), [re5](#), [re5](#)).

$$\frac{d}{dt}s_{12} = v_9 \quad (32)$$

7.13 Species s13

Name s13

SBO:0000291 empty set

Initial amount 0

Charge 0

This species takes part in one reaction (as a reactant in [re11](#)).

$$\frac{d}{dt}s13 = -v_9 \quad (33)$$

7.14 Species s119

Name Shear Stress

Initial amount 0

Charge 0

This species takes part in one reaction (as a modifier in [re5](#)).

$$\frac{d}{dt}s119 = 0 \quad (34)$$

A Glossary of Systems Biology Ontology Terms

SBO:0000291 empty set: Entity defined by the absence of any actual object. An empty set is often used to represent the source of a creation process or the result of a degradation process.

SBO:0000297 protein complex: Macromolecular complex containing one or more polypeptide chains possibly associated with simple chemicals. CHEBI:3608

SBO:0000331 half-life: Time interval over which a quantified entity is reduced to half its original value

SBML²TeX was developed by Andreas Dräger^a, Hannes Planatscher^a, Dieudonné M Wouamba^a, Adrian Schröder^a, Michael Hucka^b, Lukas Endler^c, Martin Golebiewski^d and Andreas Zell^a. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

^aCenter for Bioinformatics Tübingen (ZBIT), Germany

^bCalifornia Institute of Technology, Beckman Institute BNMC, Pasadena, United States

^cEuropean Bioinformatics Institute, Wellcome Trust Genome Campus, Hinxton, United Kingdom

^dEML Research gGmbH, Heidelberg, Germany