# **SBML Model Report**

# Model name: "Vernoux2011\_AuxinSignaling-\_AuxinSingleStepInput"



May 6, 2016

#### 1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by the following three authors: Vijayalakshmi Chelliah<sup>1</sup>, Farcot Etienne<sup>2</sup> and Teva Vernoux<sup>3</sup> at April first 2011 at 10:17 a. m. and last time modified at August 23<sup>rd</sup> 2011 at 2:13 p. m. Table 1 shows an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element Quant	
compartment types	0	compartments	1
species types	0	species	6
events	0	constraints	0
reactions	12	function definitions	0
global parameters	23	unit definitions	0
rules	4	initial assignments	0

#### **Model Notes**

This model is from the article:

The auxin signalling network translates dynamic input into robust patterning at the shoot apex.

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Vernoux T, Brunoud G, Farcot E, Morin V, Van den Daele H, Legrand J, Oliva M, Das P, Larrieu A, Wells D, Gudon Y, Armitage L, Picard F, Guyomarc'h S, Cellier C, Parry G, Koumproglou R, Doonan JH, Estelle M, Godin C, Kepinski S, Bennett M, De Veylder L, Traas J. Mol Syst Biol. 2011 Jul 5;7:508. 21734647,

#### **Abstract:**

The plant hormone auxin is thought to provide positional information for patterning during development. It is still unclear, however, precisely how auxin is distributed across tissues and how the hormone is sensed in space and time. The control of gene expression in response to auxin involves a complex network of over 50 potentially interacting transcriptional activators and repressors, the auxin response factors (ARFs) and Aux/IAAs. Here, we perform a large-scale analysis of the Aux/IAA-ARF pathway in the shoot apex of Arabidopsis, where dynamic auxin-based patterning controls organogenesis. A comprehensive expression map and full interactome uncovered an unexpectedly simple distribution and structure of this pathway in the shoot apex. A mathematical model of the Aux/IAA-ARF network predicted a strong bufferingcapacity along with spatial differences in auxin sensitivity. We then tested and confirmed these predictions using a novel auxin signalling sensor that reports input into the signalling pathway, in conjunction with the published DR5 transcriptional output reporter. Our results provide evidence that the auxin signalling network is essential to create robust patterns at the shoot apex.

#### Note:

Figure 3 of the supplementary material of the reference article has been reproduced here. Time evolution of all the variables in the model are plotted, under the influence of a step input of auxin level (auxin=5, when time>1000; 0.11, otherwise). pi\_A is varied between 0 and 2 by steps of 0.1.

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To cite BioModels Database, please use: Li C, Donizelli M, Rodriguez N, Dharuri H, Endler L, Chelliah V, Li L, He E, Henry A, Stefan MI, Snoep JL, Hucka M, Le Novre N, Laibe C (2010) BioModels Database: An enhanced, curated and annotated resource for published quantitative kinetic models. BMC Syst Biol., 4:92.

#### 2 Unit Definitions

This is an overview of five unit definitions which are all predefined by SBML and not mentioned in the model.

#### 2.1 Unit substance

**Notes** Mole is the predefined SBML unit for substance.

**Definition** mol

#### 2.2 Unit volume

**Notes** Litre is the predefined SBML unit for volume.

**Definition** 1

# 2.3 Unit area

**Notes** Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

**Definition** m<sup>2</sup>

# 2.4 Unit length

**Notes** Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

**Definition** m

#### 2.5 Unit time

Notes Second is the predefined SBML unit for time.

**Definition** s

# 3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
compartment_0000001	c_1	0000290	3	1	litre	$\checkmark$	

# 3.1 Compartment compartment\_0000001

This is a three dimensional compartment with a constant size of one litre.

Name  $c_1$ 

SBO:0000290 physical compartment

# 4 Species

This model contains six species. Section 8 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condi- tion
Ī	Aux/IAA	compartment_0000001	$\operatorname{mol} \cdot 1^{-1}$		
A	ARF	compartment_0000001	$\text{mol} \cdot l^{-1}$		
$D_{-}II$	Aux/IAA:Aux/IAA	compartment_0000001	$\text{mol} \cdot l^{-1}$		
$D_{-}IA$	Aux/IAA:ARF	compartment_0000001	$\text{mol} \cdot 1^{-1}$		$\Box$
R	mRNA	${\tt compartment\_0000001}$	$\text{mol} \cdot l^{-1}$		
aux	auxin	$compartment\_0000001$	$\text{mol} \cdot l^{-1}$		

# **5 Parameters**

This model contains 23 global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
pi_I	pi_I	0000153	1.000		
$d_r$	d_r	0000356	0.007		
$d_A$	$d_A$	0000356	0.003		
$d_{-}II$	d_II	0000356	0.003		
$\mathtt{d}_{-}\mathtt{IA}$	d_IA	0000356	0.003		
$k_{-}II$	k_II	0000341	1.000		
$k_{-}IA$	k_IA	0000341	1.000		
$B_{-}d$	$B_{-}d$	0000282	100.000		$ \overline{\checkmark} $
$\mathtt{f}\_\mathtt{A}$	$f_A$	0000009	10.000		$ \overline{\checkmark} $
$\mathtt{gamma}_{-}\mathtt{I}$	gamma_I	0000009	10.000		
$K_{\mathtt{aux}}$	K_aux	0000282	1.000		
$K_{-}II$	$K_{-}II$	0000282	10.000		
$K_{-}IA$	$K_{-}IA$	0000282	10.000		
$\mathtt{f}_{-}\mathtt{c}$	f_c	0000009	10.000		$ \overline{\checkmark} $
$w_A$	$w_A$	0000481	10.000		
$w_{-}I$	w_I	0000481	10.000		
$w_D$	$w_D$	0000481	10.000		
$d_{-}I$	d_I	0000356	0.050		$ \overline{\checkmark} $
$\mathtt{pi}_{-}\!\mathtt{A}$	pi_A	0000153	1.000		
kAm	$k_{-}Am$	0000009	10.000		
${\tt kprime\_IA}$	kprime_IA	0000338	10.000		
${\tt kprime\_II}$	kprime_II	0000338	10.000		$\Box$
aux_basal	aux_basal	0000009	0.110		

# 6 Rules

This is an overview of four rules.

# 6.1 Rule aux

Rule aux is an assignment rule for species aux:

$$aux = \begin{cases} 5 & \text{if time} > 1000\\ 0 & \text{otherwise} \end{cases} \tag{1}$$

# 6.2 Rule kprime\_IA

Rule kprime\_IA is an assignment rule for parameter kprime\_IA:

$$kprime\_IA = K\_IA \cdot k\_IA$$
 (2)

# 6.3 Rule kprime\_II

Rule kprime\_II is an assignment rule for parameter kprime\_II:

$$kprime_{I}I = K_{I}I \cdot k_{I}I$$
 (3)

#### **6.4 Rule** aux\_basal

Rule  $aux\_basal$  is an assignment rule for parameter  $aux\_basal$ :

$$aux\_basal = \frac{1}{K\_aux \cdot (gamma\_I - 1)} \tag{4}$$

# 7 Reactions

This model contains twelve reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

N₀	Id	Name	Reaction Equation	SBO
1	reac_DIA	reac_DIA	$A + I \rightleftharpoons D\_IA$	0000526
2	reac_DII	reac_DII	$I + I \rightleftharpoons D_{II}$	0000526
3	reac_degrI	reac_degrI	$I \xrightarrow{aux} \emptyset$	0000179
4	${\tt reac\_degrA}$	reac_degrA	$A \longrightarrow \emptyset$	0000179
5	${\tt reac\_degrDIA}$	reac_degrDIA	$D\_IA \longrightarrow \emptyset$	0000179
6	${\tt reac\_degrDII}$	reac_degrDII	$D_{-}II \longrightarrow \emptyset$	0000179
7	reac_DIAxA	reac_DIAxA	$D\_IA \xrightarrow{aux} A$	0000180
8	reac_DIIxI	reac_DIIxI	$D_{\perp}II \xrightarrow{aux} I$	0000180
9	${\tt reac\_degrR}$	reac_degrR	$R \longrightarrow \emptyset$	0000179
10	reac_prodI	reac_prodI	$\emptyset \xrightarrow{\mathbf{R}} \mathbf{I}$	0000393
11	${\tt reac\_prodA}$	reac_prodA	$\emptyset \longrightarrow A$	0000393
12	reac_prodR	reac_prodR	$\emptyset \xrightarrow{A, D\_IA, I} R$	0000393

#### 7.1 Reaction reac\_DIA

This is a reversible reaction of two reactants forming one product.

Name reac\_DIA

SBO:0000526 protein complex formation

# **Reaction equation**

$$A + I \Longrightarrow D I A$$
 (5)

#### **Reactants**

Table 6: Properties of each reactant.

Id	Name	SBO
A	ARF	
Ι	Aux/IAA	

#### **Product**

Table 7: Properties of each product.

Id	Name	SBO
$D_{-}IA$	Aux/IAA:ARF	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_1 = k_I A \cdot [I] \cdot [A] - kprime_I A \cdot [D_I A]$$
(6)

#### 7.2 Reaction reac\_DII

This is a reversible reaction of two reactants forming one product.

Name reac\_DII

SBO:0000526 protein complex formation

# **Reaction equation**

$$I + I \rightleftharpoons D II$$
 (7)

#### **Reactants**

Table 8: Properties of each reactant.

Id	Name	SBO
Ι	Aux/IAA	
Ι	Aux/IAA	

#### **Product**

Table 9: Properties of each product.

Id	Name	SBO
D_II	Aux/IAA:Aux/IAA	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_2 = k_I I \cdot [I] \cdot [I] - kprime_I I \cdot [D_I I]$$
(8)

# 7.3 Reaction reac\_degrI

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name reac\_degrI

SBO:0000179 degradation

# **Reaction equation**

$$I \xrightarrow{aux} \emptyset \tag{9}$$

#### Reactant

Table 10: Properties of each reactant.

Id	Name	SBO
I	Aux/IAA	

# Modifier

Table 11: Properties of each modifier.

Id	Name	SBO
aux	auxin	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_3 = \frac{\text{gamma} \cdot I \cdot d \cdot I \cdot K_{\text{-}aux} \cdot [aux]}{K_{\text{-}aux} \cdot [aux] + 1} \cdot [I]$$
(10)

# 7.4 Reaction reac\_degrA

This is an irreversible reaction of one reactant forming no product.

Name reac\_degrA

SBO:0000179 degradation

#### **Reaction equation**

$$A \longrightarrow \emptyset \tag{11}$$

#### Reactant

Table 12: Properties of each reactant.

Id	Name	SBO
A	ARF	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_4 = \mathbf{d} \cdot [\mathbf{A}] \tag{12}$$

# 7.5 Reaction reac\_degrDIA

This is an irreversible reaction of one reactant forming no product.

Name reac\_degrDIA

SBO:0000179 degradation

# **Reaction equation**

$$D.IA \longrightarrow \emptyset \tag{13}$$

#### Reactant

Table 13: Properties of each reactant.

Id	Name	SBO
$D_{-}IA$	Aux/IAA:ARF	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_5 = d_IA \cdot [D_IA] \tag{14}$$

# 7.6 Reaction reac\_degrDII

This is an irreversible reaction of one reactant forming no product.

Name reac\_degrDII

SBO:0000179 degradation

#### **Reaction equation**

$$D_{\perp}II \longrightarrow \emptyset \tag{15}$$

#### Reactant

Table 14: Properties of each reactant.

Id	Name	SBO
$D_{-}II$	Aux/IAA:Aux/IAA	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_6 = d \coprod \cdot [D \coprod] \tag{16}$$

#### 7.7 Reaction reac\_DIAxA

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

Name reac\_DIAxA

SBO:0000180 dissociation

#### **Reaction equation**

$$D\_IA \xrightarrow{aux} A$$
 (17)

#### Reactant

Table 15: Properties of each reactant.

Id	Name	SBO
$D_{-}IA$	Aux/IAA:ARF	

#### **Modifier**

Table 16: Properties of each modifier.

Id	Name	SBO
aux	auxin	

#### **Product**

Table 17: Properties of each product.

Id	Name	SBO
Α	ARF	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_7 = \frac{\text{gamma\_I} \cdot \text{d\_I} \cdot \text{K\_aux} \cdot [\text{aux}]}{\text{K\_aux} \cdot [\text{aux}] + 1} \cdot [\text{D\_IA}]$$
 (18)

#### 7.8 Reaction reac\_DIIxI

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

Name reac\_DIIxI

SBO:0000180 dissociation

#### **Reaction equation**

$$D_{-}II \xrightarrow{aux} I$$
 (19)

#### Reactant

Table 18: Properties of each reactant.

14010	ro: rroperties or each r	ouctuiit.
Id	Name	SBO
D_II	Aux/IAA:Aux/IAA	

#### **Modifier**

Table 19: Properties of each modifier.

Id	Name	SBO
aux	auxin	

#### **Product**

Table 20: Properties of each product.

Id	Name	SBO
I	Aux/IAA	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_8 = \frac{\text{gamma\_I} \cdot \text{d\_I} \cdot \text{K\_aux} \cdot [\text{aux}]}{\text{K\_aux} \cdot [\text{aux}] + 1} \cdot [\text{D\_II}]$$
 (20)

# 7.9 Reaction reac\_degrR

This is an irreversible reaction of one reactant forming no product.

Name reac\_degrR

SBO:0000179 degradation

#### **Reaction equation**

$$R \longrightarrow \emptyset$$
 (21)

#### Reactant

Table 21: Properties of each reactant.

Id	Name	SBO
R	mRNA	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_9 = \mathbf{d}_{\mathbf{I}} \cdot [\mathbf{R}] \tag{22}$$

# 7.10 Reaction reac\_prodI

This is an irreversible reaction of no reactant forming one product influenced by one modifier.

Name reac\_prodI

SBO:0000393 production

# **Reaction equation**

$$\emptyset \xrightarrow{\mathbf{R}} \mathbf{I}$$
 (23)

#### **Modifier**

Table 22: Properties of each modifier.

Id	Name	SBO
R	mRNA	

#### **Product**

Table 23: Properties of each product.

Id	Name	SBO
I	Aux/IAA	

#### **Kinetic Law**

**Derived unit** contains undeclared units

$$v_{10} = \text{pi} \cdot I \cdot [R] \tag{24}$$

# 7.11 Reaction reac\_prodA

This is an irreversible reaction of no reactant forming one product.

Name reac\_prodA

SBO:0000393 production

# **Reaction equation**

$$\emptyset \longrightarrow A$$
 (25)

#### **Product**

Table 24: Properties of each product.

Id	Name	SBO
A	ARF	

#### **Kinetic Law**

Derived unit not available

$$v_{11} = pi\_A \tag{26}$$

# **7.12 Reaction** reac\_prodR

This is an irreversible reaction of no reactant forming one product influenced by three modifiers.

Name reac\_prodR

SBO:0000393 production

# **Reaction equation**

$$\emptyset \xrightarrow{A, D \perp IA, I} R \tag{27}$$

#### **Modifiers**

Table 25: Properties of each modifier.

Id	Name	SBO
A	ARF	
$\mathtt{D}_{-}\mathtt{IA}$	Aux/IAA:ARF	
I	Aux/IAA	

#### **Product**

Table 26: Properties of each product.

Id	Name	SBO
R	mRNA	

#### **Kinetic Law**

Derived unit contains undeclared units

$$v_{12} = \frac{1 + \frac{f\_c}{B\_d} \cdot [A] \cdot \left(1 + \frac{w\_A \cdot f\_A \cdot [A]}{B\_d}\right)}{1 + \frac{[A]}{B\_d} \cdot \left(1 + \frac{w\_A \cdot [A]}{B\_d}\right) + \frac{w\_I \cdot [A] \cdot [I]}{K\_IA \cdot B\_d} + \frac{w\_D \cdot [D\_IA]}{B\_d} + k\_Am}$$
(28)

# 8 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the hasOnlySubstanceUnits flag may be set to false and spacialDimensions > 0 for certain species.

#### 8.1 Species I

Name Aux/IAA

SBO:0000252 polypeptide chain

Initial concentration  $10 \text{ mol} \cdot l^{-1}$ 

This species takes part in seven reactions (as a reactant in reac\_DIA, reac\_DII, reac\_DII, reac\_DII, reac\_degrI and as a product in reac\_DIIxI, reac\_prodI and as a modifier in reac\_prodR).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathbf{I} = |v_8| + |v_{10}| - |v_1| - |v_2| - |v_2| - |v_3| \tag{29}$$

# 8.2 Species A

Name ARF

SBO:0000252 polypeptide chain

Initial concentration  $10 \text{ mol} \cdot l^{-1}$ 

This species takes part in five reactions (as a reactant in reac\_DIA, reac\_degrA and as a product in reac\_DIAxA, reac\_prodA and as a modifier in reac\_prodR).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathbf{A} = |v_7| + |v_{11}| - |v_1| - |v_4| \tag{30}$$

# 8.3 Species D\_II

Name Aux/IAA:Aux/IAA

SBO:0000286 multimer

Initial concentration  $10 \text{ mol} \cdot l^{-1}$ 

This species takes part in three reactions (as a reactant in reac\_degrDII, reac\_DIIxI and as a product in reac\_DII).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{D}_{-}\mathrm{II} = |v_2| - |v_6| - |v_8| \tag{31}$$

#### 8.4 Species D\_IA

Name Aux/IAA:ARF

SBO:0000297 protein complex

Initial concentration  $10 \text{ mol} \cdot l^{-1}$ 

This species takes part in four reactions (as a reactant in reac\_degrDIA, reac\_DIAxA and as a product in reac\_DIA and as a modifier in reac\_prodR).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathrm{D}_{-}\mathrm{IA} = |v_1| - |v_5| - |v_7| \tag{32}$$

#### 8.5 Species R

Name mRNA

SBO:0000278 messenger RNA

Initial concentration  $1 \text{ mol} \cdot l^{-1}$ 

This species takes part in three reactions (as a reactant in reac\_degrR and as a product in reac\_prodR and as a modifier in reac\_prodI).

$$\frac{\mathrm{d}}{\mathrm{d}t}\mathbf{R} = |v_{12}| - |v_9| \tag{33}$$

#### 8.6 Species aux

Name auxin

SBO:0000252 polypeptide chain

Initial concentration  $0.11 \text{ mol} \cdot l^{-1}$ 

Involved in rule aux

This species takes part in three reactions (as a modifier in reac\_degrI, reac\_DIAxA, reac\_DIIxI) and is also involved in one rule which determines this species' quantity.

# A Glossary of Systems Biology Ontology Terms

**SBO:000009 kinetic constant:** Numerical parameter that quantifies the velocity of a chemical reaction

**SBO:0000153 forward rate constant:** Numerical parameter that quantifies the forward velocity of a chemical reaction. This parameter encompasses all the contributions to the velocity except the quantity of the reactants

**SBO:0000179 degradation:** Complete disappearance of a physical entity

**SBO:0000180** dissociation: Transformation of a non-covalent complex that results in the formation of several independent biochemical entitie

**SBO:0000252 polypeptide chain:** Naturally occurring macromolecule formed by the repetition of amino-acid residues linked by peptidic bonds. A polypeptide chain is synthesized by the ribosome. CHEBI:1654

**SBO:0000278 messenger RNA:** A messenger RNA is a ribonucleic acid synthesized during the transcription of a gene, and that carries the information to encode one or several proteins

- **SBO:0000282 dissociation constant:** Equilibrium constant that measures the propensity of a larger object to separate (dissociate) reversibly into smaller components, as when a complex falls apart into its component molecules, or when a salt splits up into its component ions. The dissociation constant is usually denoted Kd and is the inverse of the affinity constant.
- **SBO:0000286 multimer:** Non-covalent association of identical, or pseudo-identical, entities. By pseudo-identical entities, we mean biochemical elements that differ chemically, although remaining globally identical in structure and/or function. Examples are homologous subunits in an hetero-oligomeric receptor
- **SBO:0000290 physical compartment:** Specific location of space, that can be bounded or not. A physical compartment can have 1, 2 or 3 dimensions
- **SBO:0000297 protein complex:** Macromolecular complex containing one or more polypeptide chains possibly associated with simple chemicals. CHEBI:3608
- **SBO:0000338 dissociation rate constant:** Rate with which a complex dissociates into its components
- **SBO:0000341 association rate constant:** Rate with which components associate into a complex
- **SBO:0000356 decay constant:** Kinetic constant characterising a mono-exponential decay. It is the inverse of the mean lifetime of the continuant being decayed. Its unit is "per tim".
- **SBO:0000393** production: Generation of a material or conceptual entity.
- **SBO:0000481 stoichiometric coefficient:** The stoichiometric coefficient represents the degree to which a chemical species participates in a reaction. It corresponds to the number of molecules of a reactant that are consumed or produced with each occurrence of a reaction event
- **SBO:0000526 protein complex formation:** The process by which two or more proteins interact non-covalently to form a protein complex (SBO:0000297)

SML2ATEX was developed by Andreas Dräger<sup>a</sup>, Hannes Planatscher<sup>a</sup>, Dieudonné M Wouamba<sup>a</sup>, Adrian Schröder<sup>a</sup>, Michael Hucka<sup>b</sup>, Lukas Endler<sup>c</sup>, Martin Golebiewski<sup>d</sup> and Andreas Zell<sup>a</sup>. Please see http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX for more information.

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