

SBML Model Report

Model name: “Wodarz2007 - Cytomegalovirus infection model with cytotoxic T lymphocyte and natural killer cell response”



May 17, 2018

1 General Overview

This is a document in SBML Level 2 Version 4 format. This model was created by the following two authors: Catherine Lloyd¹ and Matthew Grant Roberts² at June 25th 2010 at 1:17 p. m. and last time modified at March twelveth 2018 at 10:38 a. m. Table 1 provides an overview of the quantities of all components of this model.

Table 1: Number of components in this model, which are described in the following sections.

Element	Quantity	Element	Quantity
compartment types	0	compartments	1
species types	0	species	16
events	0	constraints	0
reactions	30	function definitions	6
global parameters	20	unit definitions	1
rules	1	initial assignments	0

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Model Notes

This is a model from the article:

Dynamics of killer T cell inflation in viral infections.

Wodarz D, Sierro S, Klennerman P. *J R Soc Interface* 2007 Jun 22;4(14):533-43 [17251133](#) ,

Abstract:

Upon acute viral infection, a typical cytotoxic T lymphocyte (CTL) response is characterized by a phase of expansion and contraction after which it settles at a relatively stable memory level. Recently, experimental data from mice infected with murine cytomegalovirus (MCMV) showed different and unusual dynamics. After acute infection had resolved, some antigen specific CTL started to expand over time despite the fact that no replicative virus was detectable. This phenomenon has been termed as „CTL memory inflation,. In order to examine the dynamics of this system further, we developed a mathematical model analysing the impact of innate and adaptive immune responses. According to this model, a potentially important contributor to CTL inflation is competition between the specific CTL response and an innate natural killer (NK) cell response. Inflation occurs most readily if the NK cell response is more efficient than the CTL at reducing virus load during acute infection, but thereafter maintains a chronic virus load which is sufficient to induce CTL proliferation. The model further suggests that weaker NK cell mediated protection can correlate with more pronounced CTL inflation dynamics over time. We present experimental data from mice infected with MCMV which are consistent with the theoretical predictions. This model provides valuable information and may help to explain the inflation of CMV specific CD8+T cells seen in humans as they age.

This model was taken from the [CellML repository](#) and automatically converted to SBML.

The original model was: [Wodarz D, Sierro S, Klennerman P. \(2007\) - version=1.0](#)

The original CellML model was created by:

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2 Unit Definitions

This is an overview of five unit definitions of which four are predefined by SBML and not mentioned in the model.

2.1 Unit time

Name time

Definition 3600 s

2.2 Unit substance

Notes Mole is the predefined SBML unit for substance.

Definition mol

2.3 Unit volume

Notes Litre is the predefined SBML unit for volume.

Definition l

2.4 Unit area

Notes Square metre is the predefined SBML unit for area since SBML Level 2 Version 1.

Definition m²

2.5 Unit length

Notes Metre is the predefined SBML unit for length since SBML Level 2 Version 1.

Definition m

3 Compartment

This model contains one compartment.

Table 2: Properties of all compartments.

Id	Name	SBO	Spatial Dimensions	Size	Unit	Constant	Outside
COMpartment	Mouse		3	1	litre	<input checked="" type="checkbox"/>	

3.1 Compartment COMpartment

This is a three dimensional compartment with a constant size of one litre.

Name Mouse

4 Species

This model contains 16 species. Section 9 provides further details and the derived rates of change of each species.

Table 3: Properties of each species.

Id	Name	Compartment	Derived Unit	Constant	Boundary Condition
x	x	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
y_0	y_0	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
y_1	y_1	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
L	L	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
v	v	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
z_a	z_a	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
m_0	m_0	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
m_1	m_1	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
m_2	m_2	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
m_3	m_3	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
m_4	m_4	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
m_5	m_5	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
m_6	m_6	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
m_7	m_7	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
m_8	m_8	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>
z_i	z_i	COMpartment	$\text{mol} \cdot \text{l}^{-1}$	<input type="checkbox"/>	<input type="checkbox"/>

5 Parameters

This model contains 20 global parameters.

Table 4: Properties of each parameter.

Id	Name	SBO	Value	Unit	Constant
R0	R0		15.909		<input type="checkbox"/>
a0	a0		0.100		<input checked="" type="checkbox"/>
a1	a1		0.200		<input checked="" type="checkbox"/>
k	k		1.000		<input checked="" type="checkbox"/>
u	u		1.000		<input checked="" type="checkbox"/>
lambda	lambda		10.000		<input checked="" type="checkbox"/>
d	d		0.100		<input checked="" type="checkbox"/>
beta	beta		0.100		<input checked="" type="checkbox"/>
gamma	gamma		0.500		<input checked="" type="checkbox"/>
alpha	alpha		0.200		<input checked="" type="checkbox"/>
phi	phi		0.100		<input checked="" type="checkbox"/>
eta	eta		0.010		<input checked="" type="checkbox"/>
pa	pa		10^{-6}		<input checked="" type="checkbox"/>
ca	ca		15.500		<input checked="" type="checkbox"/>
r	r		1.000		<input checked="" type="checkbox"/>
ba	ba		0.100		<input checked="" type="checkbox"/>
p_i	p_i		1.000		<input checked="" type="checkbox"/>
ci	ci		12.000		<input checked="" type="checkbox"/>
bi	bi		0.100		<input checked="" type="checkbox"/>
xi	xi		0.010		<input checked="" type="checkbox"/>

6 Function definitions

This is an overview of six function definitions.

6.1 Function definition `Constant_flux_irreversible`

Name Constant flux (irreversible)

Argument [v]

Mathematical Expression

$$[v] \quad (1)$$

6.2 Function definition `function`

Name `function`

Arguments `parameter`, `modifier`, `substrate`

Mathematical Expression

$$\text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (2)$$

6.3 Function definition `function_1`

Name `function_1`

Arguments `param`, `mod`

Mathematical Expression

$$\text{param} \cdot \text{mod} \quad (3)$$

6.4 Function definition `function_2`

Name `function_2`

Arguments `parameter`, `modifier`

Mathematical Expression

$$\text{parameter} \cdot \text{modifier} \quad (4)$$

6.5 Function definition `function_3`

Name `function_3`

Arguments `c_a`, `y0`, `y1`, `za`

Mathematical Expression

$$\text{c_a} \cdot (\text{y0} + \text{y1}) \cdot \text{za} \quad (5)$$

6.6 Function definition `function_4`

Name `function_4`

Arguments `c_i`, `y0`, `y1`, `zi`

Mathematical Expression

$$\text{c_i} \cdot (\text{y0} + \text{y1}) \cdot \text{zi} \quad (6)$$

7 Rule

This is an overview of one rule.

7.1 Rule R_0

Rule R_0 is an assignment rule for parameter R_0 :

$$R_0 = \frac{\lambda \cdot \eta}{d \cdot a_1 \cdot (a_0 + \eta)} \cdot \left(\beta + \frac{\gamma \cdot \phi}{\phi + d} \right) \quad (7)$$

8 Reactions

This model contains 30 reactions. All reactions are listed in the following table and are subsequently described in detail. If a reaction is affected by a modifier, the identifier of this species is written above the reaction arrow.

Table 5: Overview of all reactions

Nº	Id	Name	Reaction Equation	SBO
1	Host_cell- _proliferation	Host cell proliferation	$\emptyset \longrightarrow x$	
2	Host_cell_death	Host cell death	$x \longrightarrow \emptyset$	
3	Infection_1	Infection 1	$x \xrightarrow{v} y_0$	
4	Infection_2	Infection 2	$x \xrightarrow{v} L$	
5	Infected_cell- _death_1	Infected cell death 1	$y_0 \longrightarrow \emptyset$	
6	Infected_cell- _infection- _progression_1	Infected cell infection progression 1	$y_0 \longrightarrow y_1$	
7	Infected_cell- _infection- _progression_2	Infected cell infection progression 2	$L \longrightarrow y_0$	
8	CTL_induced- _infected_cell- _death_1	CTL-induced infected cell death 1	$y_0 \xrightarrow{z_a} \emptyset$	
9	Infected_cell- _death_2	Infected cell death 2	$y_1 \longrightarrow \emptyset$	
10	CTL_induced- _infected_cell- _death_2	CTL-induced infected cell death 2	$y_1 \xrightarrow{z_a} \emptyset$	

Nº	Id	Name	Reaction Equation	SBO
11	Infected_cell- _death_3	Infected cell death 3	$L \longrightarrow \emptyset$	
12	Virus_particle- _production	Virus particle production	$\emptyset \xrightarrow{y_1} v$	
13	Viral_particle- _degradation	Viral particle degradation	$v \longrightarrow \emptyset$	
14	Precursor- _T_cell- _differentiation- _2	Precursor T-cell differentiation 2	$\emptyset \xrightarrow{m_8} z_a$	
15	Infection- _induced_CTL- _proliferation- _stimulation	Infection-induced CTL proliferation stimulation	$\emptyset \xrightarrow{y_0, y_1} z_a$	
16	CTL_cell_death	CTL cell death	$z_a \longrightarrow \emptyset$	
17	Naive_CTL- _division_1	Naive CTL division 1	$m_0 \longrightarrow 2 m_1$	
18	Naive_CTL- _division_2	Naive CTL division 2	$m_1 \longrightarrow 2 m_2$	
19	Naive_CTL- _division_3	Naive CTL division 3	$m_2 \longrightarrow 2 m_3$	
20	Naive_CTL- _division_4	Naive CTL division 4	$m_3 \longrightarrow 2 m_4$	
21	Naive_CTL- _division_5	Naive CTL division 5	$m_4 \longrightarrow 2 m_5$	
22	Naive_CTL- _division_6	Naive CTL division 6	$m_5 \longrightarrow 2 m_6$	

Nº	Id	Name	Reaction Equation	SBO
23	Naive_CTL- _division_7	Naive CTL division 7	$m_6 \longrightarrow 2 m_7$	
24	Naive_CTL- _division_8	Naive CTL division 8	$m_7 \longrightarrow 2 m_8$	
25	Precursor- _T_cell- _differentiation- _1	Precursor T-cell differentiation 1	$m_8 \longrightarrow \emptyset$	
26	NK_cell- _production	NK cell production	$\emptyset \longrightarrow z_i$	
27	NK_infection- _induced- _production	NK infection-induced production	$\emptyset \xrightarrow{y_0, y_1} z_i$	
28	NK_cell_death	NK cell death	$z_i \longrightarrow \emptyset$	
29	NK_induced- _infected_cell- _death_1	NK-induced infected cell death 1	$y_0 \xrightarrow{z_i} \emptyset$	
30	NK_induced- _infected_cell- _death_2	NK-induced infected cell death 2	$y_1 \xrightarrow{z_i} \emptyset$	

8.1 Reaction `Host_cell_proliferation`

This is an irreversible reaction of no reactant forming one product.

Name Host cell proliferation

Reaction equation



Product

Table 6: Properties of each product.

Id	Name	SBO
x	x	

Kinetic Law

Derived unit contains undeclared units

$$v_1 = \text{vol}(\text{COMpartment}) \cdot \text{Constant_flux_irreversible}(\text{lambda}) \quad (9)$$

$$\text{Constant_flux_irreversible}([v]) = [v] \quad (10)$$

$$\text{Constant_flux_irreversible}([v]) = [v] \quad (11)$$

8.2 Reaction `Host_cell_death`

This is an irreversible reaction of one reactant forming no product.

Name Host cell death

Reaction equation



Reactant

Table 7: Properties of each reactant.

Id	Name	SBO
x	x	

Kinetic Law

Derived unit contains undeclared units

$$v_2 = \text{vol}(\text{COMpartment}) \cdot d \cdot [x] \quad (13)$$

8.3 Reaction *Infection_1*

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

Name Infection 1

Reaction equation



Reactant

Table 8: Properties of each reactant.

Id	Name	SBO
x	x	

Modifier

Table 9: Properties of each modifier.

Id	Name	SBO
v	v	

Product

Table 10: Properties of each product.

Id	Name	SBO
y_0	y_0	

Kinetic Law

Derived unit contains undeclared units

$$v_3 = \text{vol}(\text{COMpartment}) \cdot \text{function}(\text{beta}, [v], [x]) \quad (15)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (16)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (17)$$

8.4 Reaction Infection_2

This is an irreversible reaction of one reactant forming one product influenced by one modifier.

Name Infection 2

Reaction equation



Reactant

Table 11: Properties of each reactant.

Id	Name	SBO
x	x	

Modifier

Table 12: Properties of each modifier.

Id	Name	SBO
v	v	

Product

Table 13: Properties of each product.

Id	Name	SBO
L	L	

Kinetic Law

Derived unit contains undeclared units

$$v_4 = \text{vol}(\text{COMpartment}) \cdot \text{function}(\text{gamma}, [v], [x]) \quad (19)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (20)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (21)$$

8.5 Reaction *Infected_cell_death_1*

This is an irreversible reaction of one reactant forming no product.

Name Infected cell death 1

Reaction equation



Reactant

Table 14: Properties of each reactant.

Id	Name	SBO
y_0	y_0	

Kinetic Law

Derived unit contains undeclared units

$$v_5 = \text{vol}(\text{COMpartment}) \cdot a_0 \cdot [y_0] \quad (23)$$

8.6 Reaction [Infected_cell_infection_progression_1](#)

This is an irreversible reaction of one reactant forming one product.

Name Infected cell infection progression 1

Reaction equation



Reactant

Table 15: Properties of each reactant.

Id	Name	SBO
y_0	y_0	

Product

Table 16: Properties of each product.

Id	Name	SBO
y_1	y_1	

Kinetic Law

Derived unit contains undeclared units

$$v_6 = \text{vol}(\text{COMpartment}) \cdot \text{eta} \cdot [y_0] \quad (25)$$

8.7 Reaction [Infected_cell_infection_progression_2](#)

This is an irreversible reaction of one reactant forming one product.

Name Infected cell infection progression 2

Reaction equation



Reactant

Table 17: Properties of each reactant.

Id	Name	SBO
L	L	

Product

Table 18: Properties of each product.

Id	Name	SBO
y_0	y_0	

Kinetic Law

Derived unit contains undeclared units

$$v_7 = \text{vol}(\text{COMpartment}) \cdot \text{phi} \cdot [\text{L}] \tag{27}$$

8.8 Reaction CTL_induced_infected_cell_death_1

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name CTL-induced infected cell death 1

Reaction equation



Reactant

Table 19: Properties of each reactant.

Id	Name	SBO
y_0	y_0	

Modifier

Table 20: Properties of each modifier.

Id	Name	SBO
<code>z_a</code>	<code>z_a</code>	

Kinetic Law

Derived unit contains undeclared units

$$v_8 = \text{vol}(\text{COMpartment}) \cdot \text{function}(\text{pa}, [\text{z_a}], [\text{y_0}]) \quad (29)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (30)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (31)$$

8.9 Reaction `Infected_cell_death_2`

This is an irreversible reaction of one reactant forming no product.

Name Infected cell death 2

Reaction equation



Reactant

Table 21: Properties of each reactant.

Id	Name	SBO
<code>y_1</code>	<code>y_1</code>	

Kinetic Law

Derived unit contains undeclared units

$$v_9 = \text{vol}(\text{COMpartment}) \cdot \text{a1} \cdot [\text{y_1}] \quad (33)$$

8.10 Reaction `CTL_induced_infected_cell_death_2`

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name CTL-induced infected cell death 2

Reaction equation



Reactant

Table 22: Properties of each reactant.

Id	Name	SBO
y_1	y_1	

Modifier

Table 23: Properties of each modifier.

Id	Name	SBO
z_a	z_a	

Kinetic Law

Derived unit contains undeclared units

$$v_{10} = \text{vol}(\text{COMpartment}) \cdot \text{function}(\text{pa}, [z_a], [y_1]) \quad (35)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (36)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (37)$$

8.11 Reaction `Infected_cell_death_3`

This is an irreversible reaction of one reactant forming no product.

Name Infected cell death 3

Reaction equation



Reactant

Table 24: Properties of each reactant.

Id	Name	SBO
L	L	

Kinetic Law**Derived unit** contains undeclared units

$$v_{11} = \text{vol}(\text{COMpartment}) \cdot d \cdot [\text{L}] \quad (39)$$

8.12 Reaction *Virus_particle_production*

This is an irreversible reaction of no reactant forming one product influenced by one modifier.

Name Virus particle production**Reaction equation****Modifier**

Table 25: Properties of each modifier.

Id	Name	SBO
y_1	y_1	

Product

Table 26: Properties of each product.

Id	Name	SBO
v	v	

Kinetic Law**Derived unit** contains undeclared units

$$v_{12} = \text{vol}(\text{COMpartment}) \cdot \text{function_1}(k, [y_1]) \quad (41)$$

$$\text{function_1}(\text{param}, \text{mod}) = \text{param} \cdot \text{mod} \tag{42}$$

$$\text{function_1}(\text{param}, \text{mod}) = \text{param} \cdot \text{mod} \tag{43}$$

8.13 Reaction `Viral_particle_degradation`

This is an irreversible reaction of one reactant forming no product.

Name Viral particle degradation

Reaction equation



Reactant

Table 27: Properties of each reactant.

Id	Name	SBO
v	v	

Kinetic Law

Derived unit contains undeclared units

$$v_{13} = \text{vol}(\text{COMpartment}) \cdot u \cdot [v] \tag{45}$$

8.14 Reaction `Precursor_T_cell_differentiation_2`

This is an irreversible reaction of no reactant forming one product influenced by one modifier.

Name Precursor T-cell differentiation 2

Reaction equation



Modifier

Table 28: Properties of each modifier.

Id	Name	SBO
m_8	m_8	

Product

Table 29: Properties of each product.

Id	Name	SBO
z_a	z_a	

Kinetic Law

Derived unit contains undeclared units

$$v_{14} = \text{vol}(\text{COMpartment}) \cdot \text{function_2}(\alpha, [\text{m_8}]) \quad (47)$$

$$\text{function_2}(\text{parameter}, \text{modifier}) = \text{parameter} \cdot \text{modifier} \quad (48)$$

$$\text{function_2}(\text{parameter}, \text{modifier}) = \text{parameter} \cdot \text{modifier} \quad (49)$$

8.15 Reaction *Infection_induced_CTL_proliferation_stimulation*

This is an irreversible reaction of no reactant forming one product influenced by two modifiers.

Name Infection-induced CTL proliferation stimulation

Reaction equation



Modifiers

Table 30: Properties of each modifier.

Id	Name	SBO
y_0	y_0	
y_1	y_1	

Product

Table 31: Properties of each product.

Id	Name	SBO
<code>z_a</code>	<code>z_a</code>	

Kinetic Law

Derived unit contains undeclared units

$$v_{15} = \text{vol}(\text{COMpartment}) \cdot \text{function_3}(\text{ca}, [y_0], [y_1], [z_a]) \quad (51)$$

$$\text{function_3}(\text{c_a}, y_0, y_1, z_a) = \text{c_a} \cdot (y_0 + y_1) \cdot z_a \quad (52)$$

$$\text{function_3}(\text{c_a}, y_0, y_1, z_a) = \text{c_a} \cdot (y_0 + y_1) \cdot z_a \quad (53)$$

8.16 Reaction `CTL_cell_death`

This is an irreversible reaction of one reactant forming no product.

Name CTL cell death

Reaction equation



Reactant

Table 32: Properties of each reactant.

Id	Name	SBO
<code>z_a</code>	<code>z_a</code>	

Kinetic Law

Derived unit contains undeclared units

$$v_{16} = \text{vol}(\text{COMpartment}) \cdot \text{ba} \cdot [z_a] \quad (55)$$

8.17 Reaction [Naive_CTL_division_1](#)

This is an irreversible reaction of one reactant forming one product.

Name Naive CTL division 1

Reaction equation



Reactant

Table 33: Properties of each reactant.

Id	Name	SBO
m_0	m_0	

Product

Table 34: Properties of each product.

Id	Name	SBO
m_1	m_1	

Kinetic Law

Derived unit contains undeclared units

$$v_{17} = \text{vol}(\text{COMpartment}) \cdot r \cdot [m_0] \quad (57)$$

8.18 Reaction [Naive_CTL_division_2](#)

This is an irreversible reaction of one reactant forming one product.

Name Naive CTL division 2

Reaction equation



Reactant

Table 35: Properties of each reactant.

Id	Name	SBO
m_1	m_1	

Product

Table 36: Properties of each product.

Id	Name	SBO
m_2	m_2	

Kinetic Law

Derived unit contains undeclared units

$$v_{18} = \text{vol}(\text{COMpartment}) \cdot r \cdot [\text{m}_1] \tag{59}$$

8.19 Reaction [Naive_CTL_division_3](#)

This is an irreversible reaction of one reactant forming one product.

Name Naive CTL division 3

Reaction equation



Reactant

Table 37: Properties of each reactant.

Id	Name	SBO
m_2	m_2	

Product

Table 38: Properties of each product.

Id	Name	SBO
m_3	m_3	

Kinetic Law

Derived unit contains undeclared units

$$v_{19} = \text{vol}(\text{COMpartment}) \cdot r \cdot [\text{m}_2] \quad (61)$$

8.20 Reaction Naive_CTL_division_4

This is an irreversible reaction of one reactant forming one product.

Name Naive CTL division 4

Reaction equation



Reactant

Table 39: Properties of each reactant.

Id	Name	SBO
m_3	m_3	

Product

Table 40: Properties of each product.

Id	Name	SBO
m_4	m_4	

Kinetic Law

Derived unit contains undeclared units

$$v_{20} = \text{vol}(\text{COMpartment}) \cdot r \cdot [\text{m}_3] \quad (63)$$

8.21 Reaction Naive_CTL_division_5

This is an irreversible reaction of one reactant forming one product.

Name Naive CTL division 5

Reaction equation



Reactant

Table 41: Properties of each reactant.

Id	Name	SBO
m_4	m_4	

Product

Table 42: Properties of each product.

Id	Name	SBO
m_5	m_5	

Kinetic Law

Derived unit contains undeclared units

$$v_{21} = \text{vol}(\text{COMpartment}) \cdot r \cdot [m_4]$$

(65)

8.22 Reaction Naive_CTL_division_6

This is an irreversible reaction of one reactant forming one product.

Name Naive CTL division 6

Reaction equation



Reactant

Table 43: Properties of each reactant.

Id	Name	SBO
m_5	m_5	

Product

Table 44: Properties of each product.

Id	Name	SBO
m_6	m_6	

Kinetic Law

Derived unit contains undeclared units

$$v_{22} = \text{vol}(\text{COMpartment}) \cdot r \cdot [\text{m}_5] \quad (67)$$

8.23 Reaction Naive_CTL_division_7

This is an irreversible reaction of one reactant forming one product.

Name Naive CTL division 7

Reaction equation



Reactant

Table 45: Properties of each reactant.

Id	Name	SBO
m_6	m_6	

Product

Table 46: Properties of each product.

Id	Name	SBO
m_7	m_7	

Kinetic Law

Derived unit contains undeclared units

$$v_{23} = \text{vol}(\text{COMpartment}) \cdot r \cdot [\text{m}_6] \quad (69)$$

8.24 Reaction Naive_CTL_division_8

This is an irreversible reaction of one reactant forming one product.

Name Naive CTL division 8

Reaction equation



Reactant

Table 47: Properties of each reactant.

Id	Name	SBO
m_7	m_7	

Product

Table 48: Properties of each product.

Id	Name	SBO
m_8	m_8	

Kinetic Law

Derived unit contains undeclared units

$$v_{24} = \text{vol}(\text{COMpartment}) \cdot r \cdot [\text{m}_7] \quad (71)$$

8.25 Reaction Precursor_T_cell_differentiation_1

This is an irreversible reaction of one reactant forming no product.

Name Precursor T-cell differentiation 1

Reaction equation



Reactant

Table 49: Properties of each reactant.

Id	Name	SBO
m_8	m_8	

Kinetic Law

Derived unit contains undeclared units

$$v_{25} = \text{vol}(\text{COMpartment}) \cdot r \cdot [m_8] \quad (73)$$

8.26 Reaction NK_cell_production

This is an irreversible reaction of no reactant forming one product.

Name NK cell production

Reaction equation



Product

Table 50: Properties of each product.

Id	Name	SBO
z_i	z_i	

Kinetic Law

Derived unit contains undeclared units

$$v_{26} = \text{vol}(\text{COMpartment}) \cdot \text{Constant_flux_irreversible}(\text{xi}) \quad (75)$$

$$\text{Constant_flux_irreversible}([v]) = [v] \quad (76)$$

$$\text{Constant_flux_irreversible}([v]) = [v] \quad (77)$$

8.27 Reaction NK_infection_induced_production

This is an irreversible reaction of no reactant forming one product influenced by two modifiers.

Name NK infection-induced production

Reaction equation



Modifiers

Table 51: Properties of each modifier.

Id	Name	SBO
y_0	y_0	
y_1	y_1	

Product

Table 52: Properties of each product.

Id	Name	SBO
z_i	z_i	

Kinetic Law

Derived unit contains undeclared units

$$v_{27} = \text{vol}(\text{COMpartment}) \cdot \text{function_4}(\text{ci}, [y_0], [y_1], [z_i]) \quad (79)$$

$$\text{function_4}(c_i, y_0, y_1, z_i) = c_i \cdot (y_0 + y_1) \cdot z_i \quad (80)$$

$$\text{function_4}(c_i, y_0, y_1, z_i) = c_i \cdot (y_0 + y_1) \cdot z_i \quad (81)$$

8.28 Reaction `NK_cell_death`

This is an irreversible reaction of one reactant forming no product.

Name NK cell death

Reaction equation



Reactant

Table 53: Properties of each reactant.

Id	Name	SBO
<code>z_i</code>	<code>z_i</code>	

Kinetic Law

Derived unit contains undeclared units

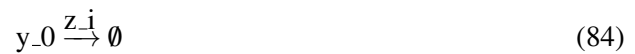
$$v_{28} = \text{vol}(\text{COMpartment}) \cdot b_i \cdot [z_i] \quad (83)$$

8.29 Reaction `NK_induced_infected_cell_death_1`

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name NK-induced infected cell death 1

Reaction equation



Reactant

Table 54: Properties of each reactant.

Id	Name	SBO
y_0	y_0	

Modifier

Table 55: Properties of each modifier.

Id	Name	SBO
z_i	z_i	

Kinetic Law

Derived unit contains undeclared units

$$v_{29} = \text{vol}(\text{COMpartment}) \cdot \text{function}(p_i, [z_i], [y_0]) \quad (85)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (86)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (87)$$

8.30 Reaction `NK_induced_infected_cell_death_2`

This is an irreversible reaction of one reactant forming no product influenced by one modifier.

Name NK-induced infected cell death 2

Reaction equation



Reactant

Table 56: Properties of each reactant.

Id	Name	SBO
y_1	y_1	

Modifier

Table 57: Properties of each modifier.

Id	Name	SBO
<code>z_i</code>	<code>z_i</code>	

Kinetic Law

Derived unit contains undeclared units

$$v_{30} = \text{vol}(\text{COMpartment}) \cdot \text{function}(p_i, [z_i], [y_1]) \quad (89)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (90)$$

$$\text{function}(\text{parameter}, \text{modifier}, \text{substrate}) = \text{parameter} \cdot \text{modifier} \cdot \text{substrate} \quad (91)$$

9 Derived Rate Equations

When interpreted as an ordinary differential equation framework, this model implies the following set of equations for the rates of change of each species.

Identifiers for kinetic laws highlighted in gray cannot be verified to evaluate to units of SBML substance per time. As a result, some SBML interpreters may not be able to verify the consistency of the units on quantities in the model. Please check if

- parameters without an unit definition are involved or
- volume correction is necessary because the `hasOnlySubstanceUnits` flag may be set to `false` and `spacialDimensions` > 0 for certain species.

9.1 Species `x`

Name `x`

Initial concentration $1 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in four reactions (as a reactant in [Host_cell_death](#), [Infection_1](#), [Infection_2](#) and as a product in [Host_cell_proliferation](#)).

$$\frac{d}{dt}x = v_1 - v_2 - v_3 - v_4 \quad (92)$$

9.2 Species y_0

Name y_0

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in eight reactions (as a reactant in [Infected_cell_death_1](#), [Infected_cell_infection_progression_1](#), [CTL_induced_infected_cell_death_1](#), [NK_induced_infected_cell_death_1](#) and as a product in [Infection_1](#), [Infected_cell_infection_progression_2](#) and as a modifier in [Infection_induced_CTL_proliferation_stimulation](#), [NK_infection_induced_production](#)).

$$\frac{d}{dt}y_0 = v_3 + v_7 - v_5 - v_6 - v_8 - v_{29} \quad (93)$$

9.3 Species y_1

Name y_1

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in seven reactions (as a reactant in [Infected_cell_death_2](#), [CTL_induced_infected_cell_death_2](#), [NK_induced_infected_cell_death_2](#) and as a product in [Infected_cell_infection_progression_1](#) and as a modifier in [Virus_particle_production](#), [Infection_induced_CTL_proliferation_stimulation](#), [NK_infection_induced_production](#)).

$$\frac{d}{dt}y_1 = v_6 - v_9 - v_{10} - v_{30} \quad (94)$$

9.4 Species L

Name L

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [Infected_cell_infection_progression_2](#), [Infected_cell_death_3](#) and as a product in [Infection_2](#)).

$$\frac{d}{dt}L = v_4 - v_7 - v_{11} \quad (95)$$

9.5 Species v

Name v

Initial concentration $1 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in four reactions (as a reactant in [Viral_particle_degradation](#) and as a product in [Virus_particle_production](#) and as a modifier in [Infection_1](#), [Infection_2](#)).

$$\frac{d}{dt}v = v_{12} - v_{13} \quad (96)$$

9.6 Species `z_a`

Name `z_a`

Initial concentration $1 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in five reactions (as a reactant in `CTL_cell_death` and as a product in `Precursor_T_cell_differentiation_2`, `Infection_induced_CTL_proliferation_stimulation` and as a modifier in `CTL_induced_infected_cell_death_1`, `CTL_induced_infected_cell_death_2`).

$$\frac{d}{dt}z_a = v_{14} + v_{15} - v_{16} \quad (97)$$

9.7 Species `m_0`

Name `m_0`

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in one reaction (as a reactant in `Naive_CTL_division_1`).

$$\frac{d}{dt}m_0 = -v_{17} \quad (98)$$

9.8 Species `m_1`

Name `m_1`

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in `Naive_CTL_division_2` and as a product in `Naive_CTL_division_1`).

$$\frac{d}{dt}m_1 = 2v_{17} - v_{18} \quad (99)$$

9.9 Species `m_2`

Name `m_2`

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in `Naive_CTL_division_3` and as a product in `Naive_CTL_division_2`).

$$\frac{d}{dt}m_2 = 2v_{18} - v_{19} \quad (100)$$

9.10 Species `m_3`

Name `m_3`

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in [Naive_CTL_division_4](#) and as a product in [Naive_CTL_division_3](#)).

$$\frac{d}{dt}m_3 = 2 v_{19} - v_{20} \quad (101)$$

9.11 Species `m_4`

Name `m_4`

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in [Naive_CTL_division_5](#) and as a product in [Naive_CTL_division_4](#)).

$$\frac{d}{dt}m_4 = 2 v_{20} - v_{21} \quad (102)$$

9.12 Species `m_5`

Name `m_5`

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in [Naive_CTL_division_6](#) and as a product in [Naive_CTL_division_5](#)).

$$\frac{d}{dt}m_5 = 2 v_{21} - v_{22} \quad (103)$$

9.13 Species `m_6`

Name `m_6`

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in [Naive_CTL_division_7](#) and as a product in [Naive_CTL_division_6](#)).

$$\frac{d}{dt}m_6 = 2 v_{22} - v_{23} \quad (104)$$

9.14 Species `m_7`

Name `m_7`

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in two reactions (as a reactant in [Naive_CTL_division_8](#) and as a product in [Naive_CTL_division_7](#)).

$$\frac{d}{dt}m_7 = 2 v_{23} - v_{24} \quad (105)$$

9.15 Species `m_8`

Name `m_8`

Initial concentration $0 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in three reactions (as a reactant in [Precursor_T_cell_differentiation_1](#) and as a product in [Naive_CTL_division_8](#) and as a modifier in [Precursor_T_cell_differentiation_2](#)).

$$\frac{d}{dt}m_8 = 2 v_{24} - v_{25} \quad (106)$$

9.16 Species `z_i`

Name `z_i`

Initial concentration $0.1 \text{ mol} \cdot \text{l}^{-1}$

This species takes part in five reactions (as a reactant in [NK_cell_death](#) and as a product in [NK_cell_production](#), [NK_infection_induced_production](#) and as a modifier in [NK_induced_infected_cell_death_1](#), [NK_induced_infected_cell_death_2](#)).

$$\frac{d}{dt}z_i = v_{26} + v_{27} - v_{28} \quad (107)$$

SBML²TeX was developed by Andreas Dräger^a, Hannes Planatscher^a, Dieudonné M Wouamba^a, Adrian Schröder^a, Michael Hucka^b, Lukas Endler^c, Martin Golebiewski^d and Andreas Zell^a. Please see <http://www.ra.cs.uni-tuebingen.de/software/SBML2LaTeX> for more information.

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