



Maclaurin series approximation

What is the task about?

Writing a MATLAB function that calculates the approximate value of arctan(x) using the Maclaurin series approximation:

 $\arctan(x) = x - x^3/3 + x^5/5 - x^7/7 + \cdots$

The function should accept 3 parameters:

- value of x
- number of significant figures accuracy i.e. *n*
- the maximum number of iterations.

In the function, use $\varepsilon = (0.5 \times 10)\%$ in order to continue until the ε falls below this criteria.

The function should return 3 values:

- the approximate value of arctan(x) at the end of the program
- \mid final arepsilon
- the number of iterations it took.

The technique & code

The mechanism of the *Maclaurin series* approximation:

I. It can be SOLVED by Taylor with xi=0 which helps us to approximate the true value. As we do more iterations the approximation will get more better than before.

II. We should have initial value of X and fix the maximum number of iterations and the number of required significant figures.

III. In the output ,showing the program running from the command prompt for x = 0.4 and 0.8.

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The code

Pseudocode of a MATLAB function that calculates the approximate value of $\arctan(x)$:

```
function [i,arctan,approxi error]=Macseries arctan(x,n,iter)
clc
%x=input('Please enter the value of x: ');
%n=input('Please enter the value of n: ');
%iter=input('Enter the maximum number of iterations: ');
es= (0.5*10^(2-n))*100;
arctan=x;
for i=1:iter
arctan old=arctan;
\arctan=\arctan+(-1)^i * x^i * x^i
```

```
approxi error=abs((arctan-arctan old)*100/arctan);
if (approxi error<=es)
break;
end
i = i +1;
end

fprintf('Number of Iterations = %d\n',i)
fprintf('Final Approximated Result = %.8g\n',arctan);
fprintf('Percent True Relative Error after %d
iterations = %.8g\n',i,approxi error);
end</pre>
```

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The output samples

Showing the program running from the command prompt for x = 0.4 and 0.8.

As we use number of iteration equal 6. the significant figures are equal 4. The result conforms the true value for the epsilonS and epsilonA.



