

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. An **Evens** number is an integer whose digits are all even. For example 2426 is an Evens number but 3224 is not.

Write a function named *isEvens* that returns 1 if its integer argument is an Evens number otherwise it returns 0.

The function signature is
int isEvens (int n)

2. An array is defined to be a **Magic** array if the sum of the primes in the array is equal to the first element of the array. If there are no primes in the array, the first element must be 0. So {21, 3, 7, 9, 11, 4, 6} is a Magic array because 3, 7, 11 are the primes in the array and they sum to 21 which is the first element of the array. {13, 4, 4, 4, 4} is also a Magic array because the sum of the primes is 13 which is also the first element. Other Magic arrays are {10, 5, 5}, {0, 6, 8, 20} and {3}. {8, 5, -5, 5, 3} is **not** a Magic array because the sum of the primes is $5+5+3 = 13$. Note that -5 is not a prime because prime numbers are positive.

Write a function named *isMagicArray* that returns 1 if its integer array argument is a Magic array. Otherwise it returns 0.

If you are writing in Java or C#, the function signature is
int isMagicArray (int[] a)

If you are writing in C or C++, the function signature is
int isMagicArray (int a[], int len) where *len* is the number of elements in the array.

You may assume that a function named *isPrime* exists that returns 1 if its int argument is a prime, otherwise it returns 0. **You do not have to write this function!** You are allowed to use it.

3. An array is defined to be **complete** if the conditions (a), (d) and (e) below hold.

- a. The array contains even numbers
- b. Let *min* be the smallest even number in the array.
- c. Let *max* be the largest even number in the array.
- d. *min* does not equal *max*
- e. All numbers between *min* and *max* are in the array

For example {-5, 6, 2, 3, 2, 4, 5, 11, 8, 7} is complete because

- a. The array contains even numbers
- b. 2 is the smallest even number
- c. 8 is the largest even number
- d. 2 does not equal 8
- e. the numbers 3, 4, 5, 6, 7 are in the array.

Examples of arrays that are **not** complete are:

- {5, 7, 9, 13} condition (a) does not hold, there are no even numbers.
- {2, 2} condition (d) does not hold
- {2, 6, 3, 4} condition (e) does not hold (5 is missing)

Write a function named *isComplete* that returns 1 if its array argument is a complete array. Otherwise it returns 0.

If you are writing in Java or C#, the function signature is
int isComplete (int[] a)

If you are writing in C or C++, the function signature is
int isComplete (int a[], int len) where *len* is the number of elements in the array.

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. A **primeproduct** is a positive integer that is the product of exactly two primes greater than 1. For example, 22 is primeproduct since $22 = 2 \times 11$ and both 2 and 11 are primes greater than 1. Write a function named *isPrimeProduct* with an integer parameter that returns 1 if the parameter is a primeproduct, otherwise it returns 0. Recall that a prime number is a positive integer with no factors other than 1 and itself.

You may assume that there exists a function named *isPrime(int m)* that returns 1 if its *m* is a prime number. You do not need to write *isPrime*. You are allowed to use this function.

The function signature
int isPrimeProduct(int n)

2. An array is called **balanced** if its even numbered elements (*a*[0], *a*[2], etc.) are even and its odd numbered elements (*a*[1], *a*[3], etc.) are odd.

Write a function named *isBalanced* that accepts an array of integers and returns 1 if the array is balanced, otherwise it returns 0.

Examples: {2, 3, 6, 7} is balanced since *a*[0] and *a*[2] are even, *a*[1] and *a*[3] are odd. {6, 7, 2, 3, 12} is balanced since *a*[0], *a*[2] and *a*[4] are even, *a*[1] and *a*[3] are odd.

{7, 15, 2, 3} is not balanced since *a*[0] is odd.

{16, 6, 2, 3} is not balanced since *a*[1] is even.

If you are programming in Java or C#, the function signature is
int isBalanced(int[] a)

If you are programming in C or C++, the function signature is
int isBalanced(int a[], int len)
where *len* is the number of elements in the array.

3. An array with an odd number of elements is said to be **centered** if all elements (except the middle one) are strictly greater than the value of the middle element. Note that only arrays with an odd number of elements have a middle element. Write a function named *isCentered* that accepts an integer array and returns 1 if it is a centered array, otherwise it returns 0.

Examples: {5, 3, 3, 4, 5} is not a centered array (the middle element 3 is not strictly less than all other elements), {3, 2, 1, 4, 5} is centered (the middle element 1 is strictly less than all other elements), {3,

$\{2, 1, 4, 1\}$ is not centered (the middle element 1 is not strictly less than all other elements), $\{3, 2, 1, 1, 4, 6\}$ is not centered (no middle element since array has even number of elements), $\{\}$ is not centered (no middle element), $\{1\}$ is centered (satisfies the condition vacuously).

If you are programming in Java or C#, the function signature is
int isCentered(int[] a)

If you are programming in C or C++, the function signature is
int isCentered(int a[], int len)
where *len* is the number of elements in the array.

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. Given a positive integer k , another positive integer n is said to have k -small factors if n can be written as a product $u \cdot v$ where u and v are both less than k . For instance, 20 has 10-small factors since both 4 and 5 are less than 10 and $4 \cdot 5 = 20$. (For the same reason, it is also true to say that 20 has 6-small factors, 7-small factors, 8-small factors, etc). However, 22 does not have 10-small factors since the only way to factor 22 is as $22 = 2 \cdot 11$, and 11 is not less than 10.

Write a function *hasKSmallFactors* with signature

boolean hasKSmallFactors(int k, int n)

which returns true if n has k -small factors. The function should return false if either k or n is not positive.

Examples:

hasKSmallFactors(7, 30) is true (since $5 \cdot 6 = 30$ and $5 < 7, 6 < 7$).

hasKSmallFactors(6, 14) is false (since the only way to factor 14 is $2 \cdot 7 = 14$ and 7 not less than 6)

hasKSmallFactors(6, 30) is false (since $5 \cdot 6 = 30$, 6 not less than 6; $3 \cdot 10 = 30$, 10 not less than 6; $2 \cdot 15 = 30$, 15 not less than 6)

2. Write a function *fill* with signature

int[] fill(int[] arr, int k, int n)

which does the following: It returns an integer array *arr2* of length n whose first k elements are the same as the first k elements of *arr*, and whose remaining elements consist of repeating blocks of the first k elements. You can assume array *arr* has at least k elements. The function should return null if either k or n is not positive.

Examples:

fill({1,2,3,5, 9, 12,-2,-1}, 3, 10) returns {1,2,3,1,2,3,1,2,3,1}.

fill({4, 2, -3, 12}, 1, 5) returns {4, 4, 4, 4, 4}.

fill({2, 6, 9, 0, -3}, 0, 4) returns null.

3. An array is said to be **hollow** if it contains 3 or more zeroes in the middle that are preceded and followed by the same number of non-zero elements. Write a function named *isHollow* that accepts an

integer array and returns 1 if it is a hollow array, otherwise it returns 0

Examples: `isHollow({1,2,4,0,0,0,3,4,5})` returns 1. `isHollow ({1,2,0,0,0,3,4,5})` returns 0. `isHollow ({1,2,4,9, 0,0,0,3,4, 5})` returns 0. `isHollow ({1,2, 0,0, 3,4})` returns 0.

If you are programming in Java or C#, the function signature is
`int isHollow(int[] a).`

If you are C or C++ programmer
`int isHollow(int[] a, int len)`
where *len* is the number of elements in the array.

There are 3 questions on this test. You have 2 hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string functions. No sorting allowed. No additional arrays allowed. Try to write a simple, elegant and correct code.

1. Write a function named **minDistance** that returns the smallest distance between two factors of a number. For example, consider $13013 = 1 \cdot 7 \cdot 11 \cdot 13$. Its factors are 1, 7, 11, 13 and 13013. **minDistance**(13013) would return 2 because the smallest distance between any two factors is 2 ($13 - 11 = 2$). As another example, **minDistance** (8) would return 1 because the factors of 8 are 1, 2, 4, 8 and the smallest distance between any two factors is 1 ($2 - 1 = 1$).

The function signature is
`int minDistance(int n)`

2. A **wave array** is defined to an array which does **not** contain two even numbers or two odd numbers in adjacent locations. So {7, 2, 9, 10, 5}, {4, 11, 12, 1, 6}, {1, 0, 5} and {2} are all **wave arrays**. But {2, 6, 3, 4} is not a wave array because the even numbers 2 and 6 are adjacent to each other.

Write a function named *isWave* that returns 1 if its array argument is a Wave array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is
`int isWave (int [] a)`

If you are programming in C or C++, the function signature is
`int isWave (int a[], int len)` where *len* is the number of elements in the array.

3. An array is defined to be a **Bean array** if it meets the following conditions
a. If it contains a 9 then it also contains a 13.
b. If it contains a 7 then it does **not** contain a 16.

So {1, 2, 3, **9**, 6, **13**} and {3, 4, 6, **7**, 13, 15}, {1, 2, 3, 4, 10, 11, 12} and {3, 6, 9, 5, 7, 13, 6, 17} are Bean arrays. The following arrays are **not** Bean arrays:
a. { 9, 6, 18} (contains a 9 but no 13)
b. {4, 7, 16} (contains both a 7 and a 16)

Write a function named *isBean* that returns 1 if its array argument is a Bean array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isBean (int[] a)

If you are programming in C or C++, the function signature is

int isBean (int a[], int len) where len is the number of elements in the array.

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. Write a function named **countDigit** that returns the number of times that a given digit appears in a positive number. For example countDigit(32121, 1) would return 2 because there are two 1s in 32121.

Other examples:

countDigit(33331, 3) returns 4

countDigit(33331, 6) returns 0

countDigit(3, 3) returns 1

The function should return -1 if either argument is negative, so

countDigit(-543, 3) returns -1.

The function signature is

int countDigit(int n, int digit)

Hint: Use modulo base 10 and integer arithmetic to isolate the digits of the number.

2. A *Bunker array* is defined to be an array in which **at least one** odd number is immediately followed by a prime number. So {4, 9, 6, 7, 3} is a Bunker array because the odd number 7 is immediately followed by the prime number 3. But {4, 9, 6, 15, 21} is not a Bunker array because none of the odd numbers are immediately followed by a prime number.

Write a function named **isBunkerArray** that returns 1 if its array argument is a Bunker array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isBunkerArray(int [] a)

If you are programming in C or C++, the function signature is

int isBunkerArray(int a[], int len) where len is the number of elements in the array.

You may assume that there exists a function isPrime that returns 1 if its argument is a prime, otherwise it returns 0. **You do not have to write this function.**

3. A *Meera array* is defined to be an array such that for all values n in the array, the value $2*n$ is not in the array. So {3, 5, -2} is a Meera array because $3*2$, $5*2$ and $-2*2$ are not in the array. But {8, 3, 4} is not a Meera array because for $n=4$, $2*n=8$ is in the array.

Write a function named **isMeera** that returns 1 if its array argument is a Meera array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isMeera(int [ ] a)
```

If you are programming in C or C++, the function signature is
`int isMeera(int a[], int len)` where `len` is the number of elements in the array.

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. A **Meera number** is a number such that the number of nontrivial factors is a factor of the number. For example, 6 is a Meera number because 6 has two nontrivial factors : 2 and 3. (A nontrivial factor is a factor other than 1 and the number). Thus 6 has two nontrivial factors. Now, 2 is a factor of 6. Thus the number of nontrivial factors is a factor of 6. Hence 6 is a Meera number. Another Meera number is 30 because 30 has 2, 3, 5, 6, 10, 15 as nontrivial factors. Thus 30 has 6 nontrivial factors. Note that 6 is a factor of 30. So 30 is a Meera Number. However 21 is **not** a Meera number. The nontrivial factors of 21 are 3 and 7. Thus the number of nontrivial factors is 2. Note that 2 is not a factor of 21. Therefore, 21 is not a Meera number.

Write a function named *isMeera* that returns 1 if its integer argument is a Meera number, otherwise it returns 0.

The signature of the function is
`int isMeera(int n)`

2. A **Bunker array** is an array that contains the value 1 if and only if it contains a prime number. The array {7, 6, 10, 1} is a Bunker array because it contains a prime number (7) and also contains a 1. The array {7, 6, 10} is **not** a Bunker array because it contains a prime number (7) but does not contain a 1. The array {6, 10, 1} is **not** a Bunker array because it contains a 1 but does not contain a prime number.

It is okay if a Bunker array contains more than one value 1 and more than one prime, so the array {3, 7, 1, 8, 1} is a Bunker array (3 and 7 are the primes).

Write a function named *isBunker* that returns 1 if its array argument is a Bunker array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is
`int isBunker(int [] a)`

If you are programming in C or C++, the function signature is
`int isBunker(int a[], int len)` where `len` is the number of elements in the array.

3. A **Nice array** is defined to be an array where for every value `n` in the array, there is also an element `n-1` or `n+1` in the array.

For example, {2, 10, 9, 3} is a Nice array because

$$2 = 3 - 1$$

$$10 = 9 + 1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Nice arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Nice array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isNice* that returns 1 if its array argument is a Nice array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

```
int isNice(int[] a)
```

If you are programming in C or C++, the function signature is

```
int isNice(int a[], int len) where len is the number of elements in the array.
```

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is two functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. An integer is defined to be “continuous factored” if it can be expressed as the product of two or more continuous integers greater than 1.

Examples of “continuous factored” integers are:

$$6 = 2 * 3.$$

$$60 = 3 * 4 * 5$$

$$120 = 4 * 5 * 6$$

$$90 = 9 * 10$$

Examples of integers that are NOT “continuous factored” are: 99 = 9*11, 121=11*11, 2=2, 13=13

Write a function named ***isContinuousFactored(int n)*** that returns 1 if *n* is continuous factored and 0 otherwise.

2. Consider the prime number 11. Note that 13 is also a prime and 13 – 11 = 2. So, 11 and 13 are known as twin primes. Similarly, 29 and 31 are twin primes. So is 71 and 73. However, there are many primes for which there is no twin. Examples are 23, 67. A **twin array** is defined to an array which every prime that has a twin appear with a twin. Some examples are

```
{3, 5, 8, 10, 27}, // 3 and 5 are twins and both are present
```

```
{11, 9, 12, 13, 23}, // 11 and 13 are twins and both are present, 23 has no twin
```

```
{5, 3, 14, 7, 18, 67}. // 3 and 5 are twins, 5 and 7 are twins, 67 has no twin
```

The following are NOT twin arrays:

```
{13, 14, 15, 3, 5} // 13 has a twin prime and it is missing in the array
```

```
{1, 17, 8, 25, 67} // 17 has a twin prime and it is missing in the array
```

Write a function named *isTwin(int[] arr)* that returns 1 if its array argument is a Twin array, otherwise it returns 0.

3. Let us define two arrays as “set equal” if every element in one is also in the other and vice-versa. For example, any two of the following are equal to one another: {1, 9, 12}, {12, 1, 9}, {9, 1, 12, 1}, {1, 9, 12, 9, 12, 1, 9}. Note that {1, 7, 8} is not set equal to {1, 7, 1} or {1, 7, 6}.

Write a function named *isSetEqual(int[] a, int[] b)* that returns 1 if its array arguments are set equal, otherwise it returns 0.

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is two functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. An integer is defined to be a **Smart** number if it is an element in the infinite sequence 1, 2, 4, 7, 11, 16 ... Note that $2-1=1$, $4-2=2$, $7-4=3$, $11-7=4$, $16-11=5$ so for $k>1$, the k th element of the sequence is equal to the $k-1$ th element + $k-1$. For example, for $k=6$, 16 is the k th element and is equal to 11 (the $k-1$ th element) + 5 ($k-1$).

Write function named *isSmart* that returns 1 if its argument is a Smart number, otherwise it returns 0. So *isSmart(11)* returns 1, *isSmart(22)* returns 1 and *isSmart(8)* returns 0 .

The function signature is
`int isSmart(int n)`

2. An array is defined to be a **Nice** array if the sum of the primes in the array is equal to the first element of the array. If there are no primes in the array, the first element must be 0. So {21, 3, 7, 9, 11 4, 6} is a Nice array because 3, 7, 11 are the primes in the array and they sum to 21 which is the first element of the array. {13, 4, 4,4, 4} is also a Nice array because the sum of the primes is 13 which is also the first element. Other Nice arrays are {10, 5, 5}, {0, 6, 8, 20} and {3}. {8, 5, -5, 5, 3} is **not** a Nice array because the sum of the primes is $5+5+3 = 13$ but the first element of the array is 8. Note that -5 is not a prime because prime numbers are positive.

Write a function named *isNiceArray* that returns 1 if its integer array argument is a Nice array. Otherwise it returns 0.

The function signature is
`int isNiceArray (int[] a)`

You may assume that a function named *isPrime* exists that returns 1 if its int argument is a prime, otherwise it returns 0. **You do ***not*** have to write this function!** You just have to call it.

3. An array is defined to be **complete** if all its elements are greater than 0 and all even numbers that are less than the maximum even number are in the array.

For example {2, 3, 2, 4, 11, 6, 10, 9, 8} is complete because

- all its elements are greater than 0
- the maximum even integer is 10

c. all even numbers that are less than 10 (2, 4, 6, 8) are in the array.

But {2, 3, 3, 6} is **not** complete because the even number 4 is missing. {2, -3, 4, 3, 6} is **not** complete because it contains a negative number.

Write a function named *isComplete* that returns 1 if its array argument is a complete array. Otherwise it returns 0.

The function signature is
`int isComplete (int[] a)`

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

Two integers are defined to be **factor equal**, if they have the same number of factors. For example, integers 10 and 33 are factor equal because, 10 has four factors: 1, 2, 5, 10 and 33 also has four factors: 1, 3, 11, 33. On the other hand, 9 and 10 are not factor equal since 9 has only three factors: 1, 3, 9 and 10 has four factors: 1, 2, 5, 10.

Write a function named *factorEqual*(*int n, int m*) that returns 1 if *n* and *m* are factor equal and 0 otherwise.

The signature of the function is
`int factorEqual(int n, int m)`

2. Define a **Meera array** to be an array *a* if it satisfies two conditions:

- (a) $a[i]$ is less than i for $i = 0$ to $a.length-1$.
- (b) sum of all elements of *a* is 0.

For example, {-4, 0, 1, 0, 2, 1} is a Meera array because

$$-4 = a[0] < 0$$

$$0 = a[1] < 1$$

$$1 = a[2] < 2$$

$$0 = a[3] < 3$$

$$2 = a[4] < 4$$

$$1 = a[5] < 5$$

$$\text{and } -4 + 0 + 1 + 0 + 2 + 1 = 0$$

{-8, 0, 0, 8, 0} is not a Meera array because $a[3]$ is 8 which is not less than 3. Thus condition (a) fails. {-8, 0, 0, 2, 0} is not a Meera array because $-8 + 2 = -6$ not equal to zero. Thus condition (b) fails.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is
`int isMeera (int[] a)`

If you are programming in C or C++, the function signature is
`int isMeera (int a[], int len)` where *len* is the number of elements in the array.

3. Define a **Triple array** to be an array where every value occurs exactly three times.

For example, {3, 1, 2, 1, 3, 1, 3, 2, 2} is a Triple array.

The following arrays are **not** Triple arrays

{2, 5, 2, 5, 5, 2, 5} (5 occurs four times instead of three times)

{3, 1, 1, 1} (3 occurs once instead of three times)

Write a function named *isTriple* that returns 1 if its array argument is a Triple array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isTriple (int[] a)

If you are programming in C or C++, the function signature is

int isTriple (int a[], int len) where len is the number of elements in the array.

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. A **Fibonacci number** is a number in the sequence 1, 1, 2, 3, 5, 8, 13, 21,.... Note that first two Fibonacci numbers are 1 and any Fibonacci number other than the first two is the sum of the previous two Fibonacci numbers. For example, $2 = 1 + 1$, $3 = 2 + 1$, $5 = 3 + 2$ and so on.

Write a function named *isFibonacci* that returns 1 if its integer argument is a Fibonacci number, otherwise it returns 0.

The signature of the function is

int isFibonacci (int n)

2. A **Meera array** is an array that contains the value 0 if and only if it contains a prime number. The array {7, 6, 0, 10, 1} is a Meera array because it contains a prime number (7) and also contains a 0. The array {6, 10, 1} is a Meera array because it contains no prime number and also contains no 0.

The array {7, 6, 10} is **not** a Meera array because it contains a prime number (7) but does not contain a 0. The array {6, 10, 0} is **not** a Meera array because it contains a 0 but does not contain a prime number.

It is okay if a Meera array contains more than one value 0 and more than one prime, so the array {3, 7, 0, 8, 0, 5} is a Meera array (3, 5 and 7 are the primes and there are two zeros.).

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write isPrime, you can just call it.

If you are programming in Java or C#, the function signature is

int isMeera(int[] a)

If you are programming in C or C++, the function signature is

int isMeera(int a[], int len) where len is the number of elements in the array.

3. A **Bean array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Bean array because

$2 = 3-1$

$10 = 9+1$

$3 = 2 + 1$

$$9 = 10 - 1$$

Other Bean arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Bean array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isBean* that returns 1 if its array argument is a *Bean* array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

int isBean(int[] a)

If you are programming in C or C++, the function signature is

int isBean(int a[], int len) where *len* is the number of elements in the array.

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not write main method. If you write, you are just wasting your time! Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. A **fancy number** is a number in the sequence 1, 1, 5, 17, 61,Note that first two fancy numbers are 1 and any fancy number other than the first two is sum of the three times previous one and two times the one before that. See below:

1,

1,

$$3*1 + 2*1 = 5$$

$$3*5 + 2*1 = 17$$

$$3*17 + 2*5 = 61$$

Write a function named *isFancy* that returns 1 if its integer argument is a Fancy number, otherwise it returns 0.

The signature of the function is

int isFancy(int n)

2. A **Meera array** is an array that contains the value 1 if and only if it contains 9. The array {7, 9, 0, 10, 1} is a Meera array because it contains 1 and 9. The array {6, 10, 8} is a Meera array because it contains no 1 and also contains no 9.

The array {7, 6, 1} is **not** a Meera array because it contains 1 but does not contain a 9. The array {9, 10, 0} is **not** a Meera array because it contains a 9 but does not contain 1.

It is okay if a Meera array contains more than one value 1 and more than one 9, so the array {1, 1, 0, 8, 0, 9, 9, 1} is a Meera array.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

If you are programming in Java or C#, the function signature is

int isMeera(int[] a)

If you are programming in C or C++, the function signature is

int isMeera(int a[], int len) where *len* is the number of elements in the array.

3. A **Bean array** is defined to be an integer array where for every value *n* in the array, there is also an element $2n$, $2n+1$ or $n/2$ in the array.

For example, {4, 9, 8} is a Bean array because

For 4, 8 is present; for 9, 4 is present; for 8, 4 is present.

Other Bean arrays include {2, 2, 5, 11, 23}, {7, 7, 3, 6} and {0}.

The array {3, 8, 4} is **not** a Bean array because of the value 3 which requires that the array contains either the value 6, 7 or 1 and none of these values are in the array.

Write a function named *isBean* that returns 1 if its array argument is a *Bean* array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

int isBean(int[] a)

If you are programming in C or C++, the function signature is

int isBean(int a[], int len) where *len* is the number of elements in the array.

There are 3 questions on this test. You have two hours to finish it. Please do your own work.

All you need to write is three functions. Please do not write main method. If you write, you are just wasting your time! Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. An integer is defined to be a **Bunker** number if it is an element in the infinite sequence 1, 2, 4, 7, 11, 16, 22, ... Note that $2-1=1$, $4-2=2$, $7-4=3$, $11-7=4$, $16-11=5$ so for $k>1$, the k th element of the sequence is equal to the $k-1$ th element + $k-1$. E.G., for $k=6$, 16 is the k th element and is equal to 11 (the $k-1$ th element) + 5 ($k-1$).

Write function named *isBunker* that returns 1 if its argument is a Bunker number, otherwise it returns 0. So *isBunker*(11) returns 1, *isBunker*(22) returns 1 and *isBunker*(8) returns 0 .

The function signature is

int isBunker (int n)

2. Define a **Dual array** to be an array where every value occurs exactly twice.

For example, {1, 2, 1, 3, 3, 2} is a dual array.

The following arrays are **not** Dual arrays

{2, 5, 2, 5, 5} (5 occurs three times instead of two times)

{3, 1, 1, 2, 2} (3 occurs once instead of two times)

Write a function named *isDual* that returns 1 if its array argument is a Dual array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isDual (int[] a)

If you are programming in C or C++, the function signature is

int isDual (int a[], int len) where *len* is the number of elements in the array.

3. An array is defined to be a **Filter array** if it meets the following conditions

a. If it contains 9 then it also contains 11.

b. If it contains 7 then it does **not** contain 13.

So {1, 2, 3, **9**, 6, **11**} and {3, 4, 6, **7**, 14, 16}, {1, 2, 3, 4, 10, 11, 13} and {3, 6, 5, 5, 13, 6, 13} are Filter arrays. The following arrays are **not** Filter arrays: {9, 6, 18} (contains 9 but no 11), {4, 7, 13} (contains both 7 and 13)

Write a function named *isFilter* that returns 1 if its array argument is a Filter array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isFilter(int[] a)

If you are programming in C or C++, the function signature is

int isFilter(int a[], int len) where *len* is the number of elements in the array.

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not write main method. If you write, you are just wasting your time! Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

Question 1. An array is called **balanced** if its even numbered elements ($a[0]$, $a[2]$, etc.) are even and its odd numbered elements ($a[1]$, $a[3]$, etc.) are odd. Write a function named *isBalanced* that accepts an array of integers and returns 1 if the array is balanced, otherwise it returns 0. Examples: {2, 3, 6, 7} is balanced since

$a[0]$ and $a[2]$ are even, $a[1]$ and $a[3]$ are odd. $\{6, 7, 2, 3, 12\}$ is balanced since $a[0]$, $a[2]$ and $a[4]$ are even, $a[1]$ and $a[3]$ are odd. $\{7, 15, 2, 3\}$ is not balanced since $a[0]$ is odd. $\{16, 6, 2, 3\}$ is not balanced since $a[1]$ is even.

If you are programming in Java or C#, the function signature is

int isBalanced(int[] a)

If you are programming in C or C++, the function signature is

int isBalanced(int a[], int len)

where *len* is the number of elements in the array.

Question 2. An array is defined to be **odd-heavy** if it contains at least one odd element and every odd element is greater than every even element. So $\{11, 4, 9, 2, 8\}$ is odd-heavy because the two odd elements (11 and 9) are greater than all the even elements. And $\{11, 4, 9, 2, 3, 10\}$ is not odd-heavy because the even element 10 is greater than the odd element 9. Write a function called *isOddHeavy* that accepts an integer array and returns 1 if the array is odd-heavy; otherwise it returns 0. Some other examples: $\{1\}$ is odd-heavy, $\{2\}$ is not odd-heavy, $\{1, 1, 1, 1\}$ is odd-heavy, $\{2, 4, 6, 8, 11\}$ is odd-heavy, $\{-2, -4, -6, -8, -11\}$ is not odd-heavy.

If you are programming in Java or C#, the function signature is

int isOddHeavy(int[] a)

If you are programming in C or C++, the function signature is

int isOddHeavy(int a[], int len)

where *len* is the number of elements in the array.

Question 3. A **normal** number is defined to be one that has no odd factors, except for 1 and possibly itself. Write a method named *isNormal* that returns 1 if its integer argument is normal, otherwise it returns 0. The function signature is

int isNormal(int n)

Examples: 1, 2, 3, 4, 5, 7, 8 are normal numbers. 6 and 9 are not normal numbers since 3 is an odd factor. 10 is not a normal number since 5 is an odd factor.

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not write main method. If you write, you are just wasting your time! Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

Question 1. An array with an odd number of elements is said to be **centered** if all elements (except the middle one) are strictly greater than the value of the middle element. Note that only arrays with an odd number of elements have a middle element. Write a function named *isCentered* that accepts an integer array and returns 1 if it is a centered array, otherwise it returns 0. Examples: $\{1, 2, 3, 4, 5\}$ is not a centered array (the middle element 3 is not strictly less than all other elements), $\{3, 2, 1, 4, 5\}$ is centered (the middle element 1 is strictly less than all other elements), $\{3, 2, 1, 4, 1\}$ is not centered (the middle element 1 is not strictly less than all other elements), $\{3, 2, 1, 1, 4, 6\}$ is not centered (no middle element since array has even number of elements), $\{\}$ is not centered (no middle element), $\{1\}$ is centered (satisfies the condition vacuously).

If you are programming in Java or C#, the function signature is

int isCentered(int[] a)

If you are programming in C or C++, the function signature is

int isCentered(int a[], int len)

where *len* is the number of elements in the array.

Question 2. An array is said to be **dual** if it has an even number of elements and each pair of consecutive even and odd elements sum to the same value. Write a function named *isDual* that accepts an array of integers and returns 1 if the array is dual, otherwise it returns 0. Examples: $\{1, 2, 3, 0\}$ is a dual array (because $1+2 = 3+0 = 3$), $\{1, 2, 2, 1, 3, 0\}$ is a dual array (because $1+2 = 2+1 = 3+0 = 3$), $\{1, 1, 2, 2\}$ is not a dual array (because $1+1$ is not equal to $2+2$), $\{1, 2, 1\}$ is not a dual array (because array does not have an even number of elements), $\{\}$ is a dual array.

If you are programming in Java or C#, the function signature is

```
int isDual(int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isDual(int a[ ], int len)
```

where *len* is the number of elements in the array.

Question 3. A non-empty array of length *n* is called an **array of all possibilities**, if it contains all numbers between 0 and *n* - 1 inclusive. Write a method named *isAllPossibilities* that accepts an integer array and returns 1 if the array is an array of all possibilities, otherwise it returns 0. Examples {1, 2, 0, 3} is an array of all possibilities, {3, 2, 1, 0} is an array of all possibilities, {1, 2, 4, 3} is not an array of all possibilities, (because 0 not included and 4 is too big), {0, 2, 3} is not an array of all possibilities, (because 1 is not included), {0} is an array of all possibilities, {} is not an array of all possibilities (because array is empty).

If you are programming in Java or C#, the function signature is

```
int isAllPossibilities(int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isAllPossibilities(int a[ ], int len)
```

where *len* is the number of elements in the array.

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. Write a function named **factorTwoCount** that returns the number of times that 2 divides the argument.

For example, factorTwoCount(48) returns 4 because

48/2 = 24

24/2 = 12

12/2 = 6

6/2 = 3

2 does not divide 3 evenly.

Another example: factorTwoCount(27) returns 0 because 2 does not divide 27.

The function signature is

```
int factorTwoCount(int n);
```

2. A **Daphne array** is defined to be an array that contains at least one odd number and begins and ends with the same number of even numbers.

So {**4, 8, 6**, 3, 2, 9, 8, 11, 8, 13, **12, 12, 6**} is a Daphne array because it begins with three even numbers and ends with three even numbers and it contains at least one odd number

The array {2, 4, 6, 8, 6} is not a Daphne array because it does not contain an odd number.

The array {**2, 8**, 7, **10, -4, 6**} is not a Daphne array because it begins with two even numbers but ends with three even numbers.

Write a function named *isDaphne* that returns 1 if its array argument is a Daphne array. Otherwise, it returns 0.

If you are writing in Java or C#, the function signature is

```
int isDaphne (int[ ] a)
```

If you are writing in C or C++, the function signature is
`int isDaphne (int a[], int len)` where len is the number of elements in the array.

3. Write a function called **goodSpread** that returns 1 if no value in its array argument occurs more than 3 times in the array.

For example, `goodSpread(new int[] {2, 1, 2, 5, 2, 1, 5, 9})` returns 1 because no value occurs more than three times.

But `goodSpread(new int[] {3, 1, 3, 1, 3, 5, 5, 3})` returns 0 because the value 3 occurs four times.

If you are writing in Java or C#, the function signature is
`int goodSpread (int[] a)`

If you are writing in C or C++, the function signature is
`int goodSpread (int a[], int len)` where len is the number of elements in the array.

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. Write a function named **factorTwoCount** that returns the number of times that 2 divides the argument.

For example, `factorTwoCount(48)` returns 4 because

$48/2 = 24$

$24/2 = 12$

$12/2 = 6$

$6/2 = 3$

2 does not divide 3 evenly.

Another example: `factorTwoCount(27)` returns 0 because 2 does not divide 27.

The function signature is
`int factorTwoCount(int n);`

2. A **Daphne array** is defined to be an array that contains at least one odd number and begins and ends with the same number of even numbers.

So {4, 8, 6, 3, 2, 9, 8, 11, 8, 13, 12, 12, 6} is a Daphne array because it begins with three even numbers and ends with three even numbers and it contains at least one odd number

The array {2, 4, 6, 8, 6} is not a Daphne array because it does not contain an odd number.

The array {2, 8, 7, 10, -4, 6} is not a Daphne array because it begins with two even numbers but ends with three even numbers.

Write a function named *isDaphne* that returns 1 if its array argument is a Daphne array. Otherwise, it returns 0.

If you are writing in Java or C#, the function signature is
`int isDaphne (int[] a)`

If you are writing in C or C++, the function signature is
`int isDaphne (int a[], int len)` where len is the number of elements in the array.

3. Write a function called **goodSpread** that returns 1 if no value in its array argument occurs more than 3 times in the array.

For example, `goodSpread(new int[] {2, 1, 2, 5, 2, 1, 5, 9})` returns 1 because no value occurs more than three times.

But `goodSpread(new int[] {3, 1, 3, 1, 3, 5, 5, 3})` returns 0 because the value 3 occurs four times.

If you are writing in Java or C#, the function signature is
`int goodSpread (int[] a)`

If you are writing in C or C++, the function signature is
`int goodSpread (int a[], int len)` where len is the number of elements in the array.

There are three questions on this test. You have two hours to complete it. Please do your own work.

1. Write a function named *sumDigits* that sums the digits of its integer argument. For example `sumDigits(3114)` returns 9, `sumDigits(-6543)` returns 18 and `sumDigits(0)` returns 0.

The signature of the function is
`int sumDigits (int n)`

2. Define a **Meera array** to be an array where `a[n]` is less than `n` for `n = 0` to `a.length-1`.

For example, `{-4, 0, 1, 0, 2}` is a Meera array because

`a[0] < 0`

`a[1] < 1`

`a[2] < 2`

`a[3] < 3`

`a[4] < 4`

`{-1, 0, 0, 8, 0}` is not a Meera array because `a[3]` is 8 which is not less than 3.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is
`int isMeera (int[] a)`

If you are programming in C or C++, the function signature is
`int isMeera (int a[], int len)` where len is the number of elements in the array.

3. Define a **Dual array** to be an array where every value occurs exactly twice.

For example, `{1, 2, 1, 3, 3, 2}` is a dual array.

The following arrays are **not** Dual arrays

`{2, 5, 2, 5, 5}` (5 occurs three times instead of two times)

{3, 1, 1, 2, 2} (3 occurs once instead of two times)

Write a function named *isDual* that returns 1 if its array argument is a Dual array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is
`int isDual (int[] a)`

If you are programming in C or C++, the function signature is
`int isDual (int a[], int len)` where len is the number of elements in the array.

Hint: you need a nested loop.

There are three questions on this test. You have two hours to complete it. Please do your own work.

1. An integer is defined to be a **Guthrie** number if it is an element in the infinite sequence 1, 2, 4, 7, 11, 16 ... Note that $2-1=1$, $4-2=2$, $7-4=3$, $11-7=4$, $16-11=5$ so for $k>1$, the k th element of the sequence is equal to the $k-1$ th element + $k-1$. E.G., for $k=6$, 16 is the k th element and is equal to 11 (the $k-1$ th element) + $k-1$.

Write function named *isGuthrie* that returns 1 if its argument is a Guthrie number, otherwise it returns 0. So *isGuthrie*(11) returns 1, *isGuthrie*(22) returns 1 and *isGuthrie*(8) returns 0.

The function signature is
`int isGuthrie (int n)`

2. An array is defined to be a **Bean** array if the sum of the primes in the array is equal to the first element of the array. If there are no primes in the array, the first element must be 0. So {21, 3, 7, 9, 11, 4, 6} is a Bean array because 3, 7, 11 are the primes in the array and they sum to 21 which is the first element of the array. {13, 4, 4, 4, 4} is also a Bean array because the sum of the primes is 13 which is also the first element. Other Bean arrays are {10, 5, 5}, {0, 6, 8, 20} and {3}. {8, 5, -5, 3} is **not** a Bean array because the sum of the primes is $5+5+3=13$ but the first element of the array is 8. Note that -5 is not a prime because prime numbers are positive.

Write a function named *isBeanArray* that returns 1 if its integer array argument is a Bean array. Otherwise it returns 0.

If you are writing in Java or C#, the function signature is
`int isBeanArray (int[] a)`

If you are writing in C or C++, the function signature is
`int isBeanArray (int a[], int len)` where len is the number of elements in the array.

You may assume that a function named *isPrime* exists that returns 1 if its int argument is a prime, otherwise it returns 0. **You do *not* have to write this function!** You just have to call it.

3. An array is defined to be **complete** if all its elements are greater than 0 and all even numbers that are less than the maximum even number are in the array.

For example {2, 3, 2, 4, 11, 6, 10, 9, 8} is complete because

- a. all its elements are greater than 0
- b. the maximum even integer is 10
- c. all even numbers that are less than 10 (2, 4, 6, 8) are in the array.

But {2, 3, 3, 6} is **not** complete because the even number 4 is missing. {2, -3, 4, 3, 6} is **not** complete because it contains a negative number.

Write a function named *isComplete* that returns 1 if its array argument is a complete array. Otherwise it returns 0.

If you are writing in Java or C#, the function signature is
`int isComplete (int[] a)`

If you are writing in C or C++, the function signature is

`int isComplete (int a[], int len)` where `len` is the number of elements in the array.

There are three questions on this test. You have 2 hours to complete it. Please do your own work.

1. An integer is defined to be a **Bunker** number if it is an element in the infinite sequence 1, 2, 4, 7, 11, 16, 22, ... Note that $2-1=1$, $4-2=2$, $7-4=3$, $11-7=4$, $16-11=5$ so for $k>1$, the k th element of the sequence is equal to the $k-1$ th element + $k-1$. E.G., for $k=6$, 16 is the k th element and is equal to 11 (the $k-1$ th element) + 5 ($k-1$).

Write function named *isBunker* that returns 1 if its argument is a Bunker number, otherwise it returns 0. So *isBunker*(11) returns 1, *isBunker*(22) returns 1 and *isBunker*(8) returns 0.

The function signature is
int isBunker (int n)

2. Define a **Dual array** to be an array where every value occurs exactly twice.

For example, {1, 2, 1, 3, 3, 2} is a dual array.

The following arrays are **not** Dual arrays
{2, 5, 2, 5, 5} (5 occurs three times instead of two times)
{3, 1, 1, 2, 2} (3 occurs once instead of two times)

Write a function named *isDual* that returns 1 if its array argument is a Dual array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is
int isDual (int[] a)

If you are programming in C or C++, the function signature is
int isDual (int a[], int len) where *len* is the number of elements in the array.

3. An array is defined to be a **Filter array** if it meets the following conditions
a. If it contains 9 then it also contains 11.
b. If it contains 7 then it does **not** contain 13.

So {1, 2, 3, **9**, 6, **11**} and {3, 4, 6, **7**, 14, 16}, {1, 2, 3, 4, 10, 11, 13} and {3, 6, 5, 5, 13, 6, 13} are Filter arrays. The following arrays are **not** Filter arrays: {9, 6, 18} (contains 9 but no 11), {4, 7, 13} (contains both 7 and 13)

Write a function named *isFilter* that returns 1 if its array argument is a Filter array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is
int isFilter(int[] a)

If you are programming in C or C++, the function signature is
int isFilter(int a[], int len) where *len* is the number of elements in the array.

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. A **Fibonacci number** is a number in the sequence 1, 1, 2, 3, 5, 8, 13, 21,.... Note that first two Fibonacci numbers are 1 and any Fibonacci number other than the first two is the sum of the previous two Fibonacci numbers. For example, $2 = 1 + 1$, $3 = 2 + 1$, $5 = 3 + 2$ and so on.

Write a function named *isFibonacci* that returns 1 if its integer argument is a Fibonacci number, otherwise it returns 0.

The signature of the function is
int isFibonacci (int n)

2. A **Meera array** is an array that contains the value 0 if and only if it contains a prime number. The array {7, 6, 0, 10, 1} is a Meera array because it contains a prime number (7) and also contains a 0. The array {6, 10, 1} is a Meera array because it contains no prime number and also contains no 0.

The array {7, 6, 10} is **not** a Meera array because it contains a prime number (7) but does not contain a 0. The array {6, 10, 0} is **not** a Meera array because it contains a 0 but does not contain a prime number.

It is okay if a Meera array contains more than one value 0 and more than one prime, so the array {3, 7, 0, 8, 0, 5} is a Meera array (3, 5 and 7 are the primes and there are two zeros.).

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is
int isMeera(int [] a)

If you are programming in C or C++, the function signature is
int isMeera(int a[], int len) where *len* is the number of elements in the array.

3. A **Bean array** is defined to be an array where for every value *n* in the array, there is also an element *n-1* or *n+1* in the array.

For example, {2, 10, 9, 3} is a Bean array because

$2 = 3-1$
 $10 = 9+1$
 $3 = 2 + 1$
 $9 = 10 -1$

Other Bean arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Bean array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isBean* that returns 1 if its array argument is a *Bean* array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is
int isBean(int[] a)

If you are programming in C or C++, the function signature is
int isBean(int a[], int len) where *len* is the number of elements in the array.

There are 3 questions on this test. You have 2 hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string functions. No sorting allowed. No additional arrays allowed. Try to write a simple, elegant and correct code.

1. Write a function named **minDistance** that returns the smallest distance between two factors of a number. For example, consider $13013 = 1 \cdot 7 \cdot 11 \cdot 13$. Its factors are 1, 7, 11, 13 and 13013. **minDistance**(13013) would return 2 because the smallest distance between any two factors is 2 ($13 - 11 = 2$). As another example, **minDistance**(8) would return 1 because the factors of 8 are 1, 2, 4, 8 and the smallest distance between any two factors is 1 ($2 - 1 = 1$).

The function signature is
int **minDistance**(int n)

2. A **wave array** is defined to an array which does **not** contain two even numbers or two odd numbers in adjacent locations. So {7, 2, 9, 10, 5}, {4, 11, 12, 1, 6}, {1, 0, 5} and {2} are all **wave arrays**. But {2, 6, 3, 4} is not a wave array because the even numbers 2 and 6 are adjacent to each other.

Write a function named *isWave* that returns 1 if its array argument is a Wave array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is
int isWave (int [] a)

If you are programming in C or C++, the function signature is
int isWave (int a[], int len) where len is the number of elements in the array.

3. An array is defined to be a **Bean array** if it meets the following conditions
a. If it contains a 9 then it also contains a 13.
b. If it contains a 7 then it does **not** contain a 16.

So {1, 2, 3, **9**, 6, **13**} and {3, 4, 6, **7**, 13, 15}, {1, 2, 3, 4, 10, 11, 12} and {3, 6, 9, 5, 7, 13, 6, 17} are Bean arrays. The following arrays are **not** Bean arrays:

- a. { 9, 6, 18} (contains a 9 but no 13)
- b. {4, 7, 16} (contains both a 7 and a 16)

Write a function named *isBean* that returns 1 if its array argument is a Bean array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is
int isBean (int[] a)

If you are programming in C or C++, the function signature is
int isBean (int a[], int len) where len is the number of elements in the array.

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. A **Meera number** is a number such that the number of nontrivial factors is a factor of the number. For example, 6 is a Meera number because 6 has two nontrivial factors : 2 and 3. (A nontrivial factor is a factor other than 1 and the number). Thus 6 has two nontrivial factors. Now, 2 is a factor of 6. Thus the number of nontrivial factors is a factor of 6. Hence 6 is a Meera number. Another Meera number is 30 because 30 has 2, 3, 5, 6, 10, 15 as nontrivial factors. Thus 30 has 6 nontrivial factors. Note that 6 is a factor of 30. So 30 is a Meera Number. However 21 is **not** a Meera number. The nontrivial factors of 21 are 3 and 7. Thus the number of nontrivial factors is 2. Note that 2 is not a factor of 21. Therefore, 21 is not a Meera number.

Write a function named *isMeera* that returns 1 if its integer argument is a Meera number, otherwise it returns 0.

The signature of the function is

```
int isMeera(int n)
```

2. A **Bunker array** is an array that contains the value 1 if and only if it contains a prime number. The array {7, 6, 10, 1} is a Bunker array because it contains a prime number (7) and also contains a 1. The array {7, 6, 10} is **not** a Bunker array because it contains a prime number (7) but does not contain a 1. The array {6, 10, 1} is **not** a Bunker array because it contains a 1 but does not contain a prime number.

It is okay if a Bunker array contains more than one value 1 and more than one prime, so the array {3, 7, 1, 8, 1} is a Bunker array (3 and 7 are the primes).

Write a function named *isBunker* that returns 1 if its array argument is a Bunker array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

```
int isBunker(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBunker(int a[ ], int len) where len is the number of elements in the array.
```

3. A **Nice array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Nice array because

$$2 = 3-1$$

$$10 = 9+1$$

$$3 = 2 + 1$$

$$9 = 10 -1$$

Other Nice arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Nice array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isNice* that returns 1 if its array argument is a Nice array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

```
int isNice(int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isNice(int a[ ], int len) where len is the number of elements in the array.
```

There are three questions on this test. You have two hours to complete it. Please do your own work.

1. A **Pascal number** is a number that is the sum of the integers from 1 to j for some j . For example 6 is a Pascal number because $6 = 1 + 2 + 3$. Here j is 3. Another Pascal number is 15 because $15 = 1 + 2 + 3 + 4 + 5$. An example of a number that is not a Pascal number is 7 because it falls between the Pascal numbers 6 and 10.

Write a function named *isPascal* that returns 1 if its integer argument is a Pascal number, otherwise it returns 0.

The signature of the function is

```
int isPascal (int n)
```

2. A **Meera array** is an array that contains the value 1 if and only if it contains a prime number. The array {7, 6, 10, 1} is a Meera array because it contains a prime number (7) and also contains a 1. The array {7, 6, 10} is **not** a Meera array because it contains a prime number (7) but does not contain a 1. The array {6, 10, 1} is **not** a Meera array because it contains a 1 but does not contain a prime number.

It is okay if a Meera array contains more than one value 1 and more than one prime, so the array {3, 7, 1, 8, 1} is a Meera array (3 and 7 are the primes).

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

```
int isMeera (int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isMeera (int a[ ], int len) where len is the number of elements in the array.
```

3. A **Suff array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Suff array because

$$2 = 3 - 1$$

$$10 = 9 + 1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Suff arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Suff array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isSuff* that returns 1 if its array argument is a Suff array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

```
int isSuff (int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isSuff (int a[ ], int len) where len is the number of elements in the array.
```

March 7, 2015

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

QUESTION 1. An array is called ***balanced*** if its even numbered elements (a[0], a[2], etc.) are even and its odd numbered elements (a[1], a[3], etc.) are odd. Write a function named *isBalanced* that accepts an array of integers and returns 1 if the array is balanced, otherwise it returns 0. Examples: {2, 3, 6, 7} is balanced since a[0] and a[2] are even, a[1] and a[3] are odd. {6, 7, 2, 3, 12} is balanced since a[0], a[2] and a[4] are even, a[1] and a[3] are odd. {7, 15, 2, 3} is not balanced since a[0] is odd. {16, 6, 2, 3} is not balanced since a[1] is even.

If you are programming in Java or C#, the function signature is

```
int isBalanced(int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBalanced(int a[ ], int len)
```

where *len* is the number of elements in the array.

QUESTION 2. An array is defined to be **odd-heavy** if it contains at least one odd element and every odd element is greater than every even element. So {11, 4, 9, 2, 8} is odd-heavy because the two odd elements (11 and 9) are greater than all the even elements. And {11, 4, 9, 2, 3, 10} is not odd-heavy because the even element 10 is greater than the odd element 9. Write a function called *isOddHeavy* that accepts an integer array and returns 1 if the array is odd-heavy; otherwise it returns 0. Some other examples: {1} is odd-heavy, {2} is not odd-heavy, {1, 1, 1, 1} is odd-heavy, {2, 4, 6, 8, 11} is odd-heavy, {-2, -4, -6, -8, -11} is not odd-heavy.

If you are programming in Java or C#, the function signature is

int isOddHeavy(int[] a)

If you are programming in C or C++, the function signature is

int isOddHeavy(int a[], int len)

where *len* is the number of elements in the array.

QUESTION 3. A **normal** number is defined to be one that has no odd factors, except for 1 and possibly itself. Write a method named *isNormal* that returns 1 if its integer argument is normal, otherwise it returns 0. The function signature is

int isNormal(int n)

Examples: 1, 2, 3, 4, 5, 7, 8 are normal numbers. 6 and 9 are not normal numbers since 3 is an odd factor. 10 is not a normal number since 5 is an odd factor.

March 21, 2015

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa. You are not allowed to use any additional data structures.

1. A **Meera number** is a number such that the number of nontrivial factors is a factor of the number. For example, 6 is a Meera number because 6 has two nontrivial factors : 2 and 3. (A nontrivial factor is a factor other than 1 and the number). Thus 6 has two nontrivial factors. Now, 2 is a factor of 6. Thus the number of nontrivial factors is a factor of 6. Hence 6 is a Meera number. Another Meera number is 30 because 30 has 2, 3, 5, 6, 10, 15 as nontrivial factors. Thus 30 has 6 nontrivial factors. Note that 6 is a factor of 30. So 30 is a Meera Number. However 21 is **not** a Meera number. The nontrivial factors of 21 are 3 and 7. Thus the number of nontrivial factors is 2. Note that 2 is not a factor of 21. Therefore, 21 is not a Meera number.

Write a function named *isMeera* that returns 1 if its integer argument is a Meera number, otherwise it returns 0.

The signature of the function is

int isMeera(int n)

2. A **Bunker array** is an array that contains the value 1 if and only if it contains a prime number. The array {7, 6, 10, 1} is a Bunker array because it contains a prime number (7) and also contains a 1. The array {7, 6, 10} is **not** a Bunker array because it contains a prime number (7) but does not contain a 1. The array {6, 10, 1} is **not** a Bunker array because it contains a 1 but does not contain a prime number.

It is okay if a Bunker array contains more than one value 1 and more than one prime, so the array {3, 7, 1, 8, 1} is a Bunker array (3 and 7 are the primes).

Write a function named *isBunker* that returns 1 if its array argument is a Bunker array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write isPrime, you can just call it.

If you are programming in Java or C#, the function signature is
int isBunker(int [] a)

If you are programming in C or C++, the function signature is
int isBunker(int a[], int len) where len is the number of elements in the array.

3. A **Nice array** is defined to be an array where for every value n in the array, there is also an element n-1 or n+1 in the array.

For example, {2, 10, 9, 3} is a Nice array because

$$2 = 3 - 1$$

$$10 = 9 + 1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Nice arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Nice array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isNice* that returns 1 if its array argument is a Nice array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is
int isNice(int[] a)

If you are programming in C or C++, the function signature is
int isNice(int a[], int len) where len is the number of elements in the array.

April 4, 2015

There are 3 questions on this test. You have 2 hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string functions. No sorting allowed. No additional arrays allowed. Try to write a simple, elegant and correct code.

1. Write a function named **minDistance** that returns the smallest distance between two factors of a number. For example, consider $13013 = 1 \cdot 7 \cdot 11 \cdot 13$. Its factors are 1, 7, 11, 13 and 13013. **minDistance**(13013) would return 2 because the smallest distance between any two factors is 2 ($13 - 11 = 2$). As another example, **minDistance**(8) would return 1 because the factors of 8 are 1, 2, 4, 8 and the smallest distance between any two factors is 1 ($2 - 1 = 1$).

The function signature is
`int minDistance(int n)`

2. A **wave array** is defined to an array which does **not** contain two even numbers or two odd numbers in adjacent locations. So {7, 2, 9, 10, 5}, {4, 11, 12, 1, 6}, {1, 0, 5} and {2} are all **wave arrays**. But {2, 6, 3, 4} is not a wave array because the even numbers 2 and 6 are adjacent to each other.

Write a function named *isWave* that returns 1 if its array argument is a Wave array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is
`int isWave (int [] a)`

If you are programming in C or C++, the function signature is
`int isWave (int a[], int len)` where len is the number of elements in the array.

3. An array is defined to be a **Bean array** if it meets the following conditions
a. If it contains a 9 then it also contains a 13.
b. If it contains a 7 then it does **not** contain a 16.

So {1, 2, 3, **9**, 6, **13**} and {3, 4, 6, **7**, 13, 15}, {1, 2, 3, 4, 10, 11, 12} and {3, 6, 9, 5, 7, 13, 6, 17} are Bean arrays. The following arrays are **not** Bean arrays:
a. { 9, 6, 18} (contains a 9 but no 13)
b. {4, 7, 16} (contains both a 7 and a 16)

Write a function named *isBean* that returns 1 if its array argument is a Bean array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is
`int isBean (int[] a)`

If you are programming in C or C++, the function signature is
`int isBean (int a[], int len)` where len is the number of elements in the array.

2015 April 18th test

There are three questions on this test. Please do your own work. All you need to write is three functions. Please do not use any String functions. No sorting allowed. No additional arrays or data structures allowed. Try to write a simple, elegant and correct

code. If you are not a Java or C# programmer, you can assume one more argument `int len`, to pass the length of the array.

Question 1. Write a function fill with signature

`int[] fill(int[] arr, int k, int n)`

which does the following: It returns an integer array `arr2` of length `n` whose first `k` elements are the same as the first `k` elements of `arr`, and whose remaining elements consist of repeating blocks of the first `k` elements. You can assume array `arr` has at least `k` elements. The function should return null if either `k` or `n` is not positive.

Examples: `fill({1,2,3,5, 9, 12,-2,-1}, 3, 10)` returns `{1,2,3,1,2,3,1,2,3,1}`. `Fill({4, 2, -3, 12}, 1, 5)` returns `{4, 4, 4, 4, 4}`. `fill({2, 6, 9, 0, -3}, 0, 4)` returns null.

Question 2. Write a function `sumIsPower` with signature

`boolean sumIsPower(int[] arr)`

which outputs true if the sum of the elements in the input array `arr` is a power of 2, false otherwise. Recall that the powers of 2 are 1, 2, 4, 8, 16, and so on. In general a number is a power of 2 if and only if it is of the form 2^n for some nonnegative integer `n`. You may assume (without verifying in your code) that all elements in the array are positive integers. If the input array `arr` is null, the return value should be false.

Examples: `sumIsPower({8,8,8,8})` is true since $8 + 8 + 8 + 8 = 32 = 2^5$. `sumIsPower({8,8,8})` is false, since $8 + 8 + 8 = 24$, not a power of 2.

Question 3. An array is said to be hollow if it contains 3 or more zeros in the middle that are preceded and followed by the same number of non-zero elements. Write a function named `isHollow` that accepts an integer array and returns 1 if it is a hollow array, otherwise it returns 0. The function signature is

`int isHollow(int[] a).`

Examples: `isHollow({1,2,4,0,0,0,3,4,5})` returns true. `isHollow ({1,2,0,0,0,3,4,5})` returns false. : `isHollow ({1,2,4,9, 0,0,0,3,4, 5})` returns false. `isHollow ({1,2, 0,0, 3,4})` returns false.

May 2nd 2015

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. A **Fibonacci number** is a number in the sequence 1, 1, 2, 3, 5, 8, 13, 21,... Note that first two Fibonacci numbers are 1 and any Fibonacci number other than the first two is the sum of the previous two Fibonacci numbers. For example, $2 = 1 + 1$, $3 = 2 + 1$, $5 = 3 + 2$ and so on.

Write a function named *isFibonacci* that returns 1 if its integer argument is a Fibonacci number, otherwise it returns 0.

The signature of the function is

int isFibonacci (int n)

2. A **Meera array** is an array that contains the value 0 if and only if it contains a prime number. The array {7, 6, 0, 10, 1} is a Meera array because it contains a prime number (7) and also contains a 0. The array {6, 10, 1} is a Meera array because it contains no prime number and also contains no 0.

The array {7, 6, 10} is **not** a Meera array because it contains a prime number (7) but does not contain a 0. The array {6, 10, 0} is **not** a Meera array because it contains a 0 but does not contain a prime number.

It is okay if a Meera array contains more than one value 0 and more than one prime, so the array {3, 7, 0, 8, 0, 5} is a Meera array (3, 5 and 7 are the primes and there are two zeros.).

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

int isMeera(int [] a)

If you are programming in C or C++, the function signature is

int isMeera(int a[], int len) where *len* is the number of elements in the array.

3. A **Bean array** is defined to be an array where for every value *n* in the array, there is also an element *n-1* or *n+1* in the array.

For example, {2, 10, 9, 3} is a Bean array because

$$2 = 3 - 1$$

$$10 = 9 + 1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Bean arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Bean array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isBean* that returns 1 if its array argument is a *Bean* array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

int isBean(int[] a)

If you are programming in C or C++, the function signature is

int isBean(int a[], int len) where *len* is the number of elements in the array.

May 16, 2015

There are three questions on this test. You have two hours to complete it. Please do your own work.

1. A **Riley** number is an integer whose digits are all even. For example 2426 is a Riley number but 3224 is not.

Write a function named *isRiley* that returns 1 if its integer argument is a Riley number otherwise it returns 0.

The function signature is

`int isRiley (int n)`

2. Write a function named *lastEven* that returns the index of the last even value in its array argument. For example, *lastEven* will return 3 if the array is {3, 2, 5, 6, 7}, because that is the index of 6 which is the last even value in the array.

If the array has no even numbers, the function should return -1.

If you are programming in Java or C#, the function signature is

`int lastEven (int[] a)`

If you are programming in C or C++, the function signature is

int lastEven (int a[], int len) where len is the number of elements in a.

3. Write a function named *countMax* that returns the number of times that the max value occurs in the array. For example, countMax would return 2 if the array is {6, 3, 1, 3, 4, 3, 6, 5} because 6 occurs 2 times in the array.

If you are programming in Java or C#, the function signature is

```
int countMax (int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int countMax (int a[ ], int len) where len is the number of elements in a.
```

May 30, 2015 Test

There are three questions on this test. You have two hours to finish it. Please do your own work.

1. An integer is defined to be an **even subset** of another integer n if every even factor of m is also a factor of n . For example 18 is an even subset of 12 because the even factors of 18 are 2 and 6 and these are both factors of 12. But 18 is not an even subset of 32 because 6 is not a factor of 32.

Write a function with signature **int isEvenSubset(int m, int n)** that returns 1 if m is an even subset of n , otherwise it returns 0.

2. A **twinoid** is defined to be an array that has exactly two even values that are adjacent to one another. For example {3, 3, 2, 6, 7} is a twinoid array because it has exactly two even values (2 and 6) and they are adjacent to one another. The following arrays are not twinoid arrays.

{3, 3, 2, 6, 6, 7} because it has three even values.

{3, 3, 2, 7, 6, 7} because the even values are not adjacent to one another

{3, 8, 5, 7, 3} because it has only one even value.

Write a function named **isTwinoid** that returns 1 if its array argument is a twinoid array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

`int isTwinoid (int [] a);`

If you are programming in C or C++, the function signature is

`int isTwinoid(int a[], int len)` where len is the number of elements in the array.

3. A **balanced** array is defined to be an array where for every value n in the array, -n also is in the array. For example {-2, 3, 2, -3} is a balanced array. So is {-2, 2, 2, 2}. But {-5, 2, -2} is not because 5 is not in the array.

Write a function named **isBalanced** that returns 1 if its array argument is a balanced array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

`int isBalanced (int [] a);`

If you are programming in C or C++, the function signature is

`int isBalanced(int a[], int len)` where len is the number of elements in the array.

June 13, 2015

This exam is two hours long and contains three questions. Please indent your code so it is easy for the grader to read it.

1. Write a method named **getExponent(n, p)** that returns the largest exponent x such that p^x evenly divides n. If p is ≤ 1 the method should return -1.

For example, `getExponent(162, 3)` returns 4 because $162 = 2^1 * 3^4$, therefore the value of x here is 4.

The method signature is
`int getExponent(int n, int p)`

Examples:

if n is	and p is	return	because
27	3	3	3^3 divides 27 evenly but 3^4 does not.
28	3	0	3^0 divides 28 evenly but 3^1 does not.
280	7	1	7^1 divides 280 evenly but 7^2 does not.
-250	5	3	5^3 divides -250 evenly but 5^4 does not.
18	1	-1	if $p \leq 1$ the function returns -1.
128	4	3	4^3 divides 128 evenly but 4^4 does not.

2. Define an array to be a 121 array if all its elements are either 1 or 2 and it begins with one or more 1s followed by a one or more 2s and then ends with the same number of 1s that it begins with. Write a method named **is121Array** that returns 1 if its array argument is a 121 array, otherwise, it returns 0.

If you are programming in Java or C#, the function signature is
int is121Array(int[] a)

If you are programming in C or C++, the function signature is
int is121Array(int a[], int len) where len is the number of elements in the array a.

Examples

a is	then function returns	reason
{1, 2, 1}	1	because the same number of 1s are at the beginning and end of the array and there is at least one 2 in between them.
{1, 1, 2, 2, 2, 1, 1}	1	because the same number of 1s are at the beginning and end of the array and there is at least one 2 in between them.
{1, 1, 2, 2, 2, 1, 1, 1}	0	Because the number of 1s at the end does not equal the number of 1s at the beginning.
{1, 1, 2, 1, 2, 1, 1}	0	Because the middle does not contain only 2s.
{1, 1, 1, 2, 2, 2, 1, 1, 1, 3}	0	Because the array contains a number other than 1 and 2.
{1, 1, 1, 1, 1, 1}	0	Because the array does not contain any 2s
{2, 2, 2, 1, 1, 1, 2, 2, 2, 1, 1}	0	Because the first element of the array is not a 1.
{1, 1, 1, 2, 2, 2, 1, 1, 2, 2}	0	Because the last element of the array is not a 1.
{2, 2, 2}	0	Because there are no 1s in the array.

3. An array is defined to be **maxmin equal** if it contains at least two **different** elements and the number of times the maximum value occur is the same as the number of times the minimum value occur. So {11, 4, 9, 11, 8, 5, 4, 10} is **maxmin equal**, because the max value 11 and min value 4 both appear two times in the array.

Write a function called *isMaxMinEqual* that accepts an integer array and returns 1 if the array is **maxmin equal**; otherwise it returns 0.

If you are programming in Java or C#, the function signature is
`int isMaxMinEqual(int[] a)`

If you are programming in C or C++, the function signature is
`int isMaxMinEqual(int a[], int len)` where *len* is the number of elements in the array

Some other examples:

if the input array is	<i>isMaxMinEqual</i> should return
{ }	0 (array must have at least two <i>different</i> elements)
{ 2 }	0 (array must have at least two <i>different</i> elements)
{ 1, 1, 1, 1, 1, 1 }	0 (array must have at least two <i>different</i> elements)
{ 2, 4, 6, 8, 11 }	1 (Both max value (11) and min value 2 appear exactly one time)
{ -2, -4, -6, -8, -11 }	1 (Both max value (-2) and min value -11 appear exactly one time)

June 27th Test 2015

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. An integer array is said to be *oddSpaced*, if the difference between the largest value and the smallest value is an odd number. Write a function *isOddSpaced(int[] a)* that will return 1 if it is *oddSpaced* and 0 otherwise. If array has less than two elements, function will return 0. If you are programming in C or C++, the function signature is:

`int isOddSpaced (int a[], int len)` where *len* is the number of elements in the array.

Examples

Array	Largest value	Smallest value	Difference	Return value
{ 100, 19, 131, 140 }	140	19	140 - 19 = 121	1
{ 200, 1, 151, 160 }	200	1	200 - 1 = 199	1

{200, 10, 151, 160}	200	10	$200 - 10 = 190$	0
{100, 19, -131, -140}	100	-140	$100 - (-140) = 240$	0
{80, -56, 11, -81}	80	-81	$-80 - 80 = -161$	1

2. An *Super array* is defined to be an array in which each element is greater than sum of all elements before that. See examples below:

{2, 3, 6, 13} is a *Super array*. Note that $2 < 3$, $2+3 < 6$, $2 + 3 + 6 < 13$.

{2, 3, 5, 11} is a NOT a *Super array*. Note that $2 + 3$ not less than 5.

Write a function named *isSuper* that returns 1 if its array argument is a *isSuper* array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

`int isSuper (int [] a)`

If you are programming in C or C++, the function signature is:

`int isSuper (int a[], int len)` where *len* is the number of elements in the array.

3. An *isSym* (even/odd Symmetric) *array* is defined to be an array in which even numbers and odd numbers appear in the same order from “*both directions*”. You can assume array has at least one element. See examples below:

{2, 7, 9, 10, 11, 5, 8} is a *isSym* array.

Note that from left to right or right to left we have even, odd, odd, even, odd, odd, even.

{9, 8, 7, 13, 14, 17} is a *isSym* array.

Note that from left to right or right to left we have {odd, even, odd, odd, even, odd}.

However, {2, 7, 8, 9, 11, 13, 10} is not a *isSym* array.

From left to right we have {even, odd, even, odd, odd, odd, even}.

From right to left we have {even, odd, odd, odd, even, odd, even},

which is not the same.

Write a function named *isSym* that returns 1 if its array argument is a *isSym* array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

int *isSym* (int [] a)

If you are programming in C or C++, the function signature is:

int *isSym* (int a[], int len) where *len* is the number of elements in the array.

July 11th 2015

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. Write a function named **factorTwoCount** that returns the number of times that 2 divides the argument.

For example, `factorTwoCount(48)` returns 4 because

$$48/2 = 24$$

$$24/2 = 12$$

$$12/2 = 6$$

$$6/2 = 3$$

2 does not divide 3 evenly.

Another example: `factorTwoCount(27)` returns 0 because 2 does not divide 27.

The function signature is

```
int factorTwoCount(int n);
```

2. A **Meera array** is defined to be an array that contains at least one odd number and begins and ends with the same number of even numbers.

So {**4, 8, 6**, 3, 2, 9, 8, 11, 8, 13, **12, 12, 6**} is a Meera array because it begins with three even numbers and ends with three even numbers and it contains at least one odd number

The array {2, 4, 6, 8, 6} is not a Meera array because it does not contain an odd number.

The array {**2, 8**, 7, **10, -4, 6**} is not a Meera array because it begins with two even numbers but ends with three even numbers.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array. Otherwise, it returns 0.

If you are writing in Java or C#, the function signature is

```
int isMeera (int[ ] a)
```

If you are writing in C or C++, the function signature is

```
int isMeera (int a[ ], int len) where len is the number of elements in the array.
```

3. Write a function called **goodSpread** that returns 1 if no value in its array argument occurs more than 3 times in the array.

For example, `goodSpread(new int[] {2, 1, 2, 5, 2, 1, 5, 9})` returns 1 because no value occurs more than three times.

But `goodSpread(new int[] {3, 1, 3, 1, 3, 5, 5, 3})` returns 0 because the value 3 occurs four times.

If you are writing in Java or C#, the function signature is

```
int goodSpread (int[ ] a)
```

If you are writing in C or C++, the function signature is

```
int goodSpread (int a[ ], int len) where len is the number of elements in the array.
```

July 25, 2015

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. A **Fibonacci number** is a number in the sequence 1, 1, 2, 3, 5, 8, 13, 21,.... Note that first two Fibonacci numbers are 1 and any Fibonacci number other than the first two is the sum of the previous two Fibonacci numbers. For example, $2 = 1 + 1$, $3 = 2 + 1$, $5 = 3 + 2$ and so on.

Write a function named *isFibonacci* that returns 1 if its integer argument is a Fibonacci number, otherwise it returns 0.

The signature of the function is

int isFibonacci (int n)

2. A **Meera array** is an array that contains the value 0 if and only if it contains a prime number. The array {7, 6, 0, 10, 1} is a Meera array because it contains a prime number (7) and also contains a 0. The array {6, 10, 1} is a Meera array because it contains no prime number and also contains no 0.

The array {7, 6, 10} is **not** a Meera array because it contains a prime number (7) but does not contain a 0. The array {6, 10, 0} is **not** a Meera array because it contains a 0 but does not contain a prime number.

It is okay if a Meera array contains more than one value 0 and more than one prime, so the array {3, 7, 0, 8, 0, 5} is a Meera array (3, 5 and 7 are the primes and there are two zeros.).

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

int isMeera(int [] a)

If you are programming in C or C++, the function signature is

int isMeera(int a[], int len) where *len* is the number of elements in the array.

3. A **Bean array** is defined to be an array where for every value *n* in the array, there is also an element *n-1* or *n+1* in the array.

For example, {2, 10, 9, 3} is a Bean array because

$$2 = 3 - 1$$

$$10 = 9 + 1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Bean arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Bean array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isBean* that returns 1 if its array argument is a *Bean* array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

int isBean(int[] a)

If you are programming in C or C++, the function signature is

int isBean(int a[], int len) where *len* is the number of elements in the array.

Aug 8th 015

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. A **Meera number** is a number such that the number of nontrivial factors is a factor of the number. For example, 6 is a Meera number because 6 has two nontrivial factors : 2 and 3. (A nontrivial factor is a factor other than 1 and the number). Thus 6 has two nontrivial factors. Now, 2 is a factor of 6. Thus the number of nontrivial factors is a factor of 6. Hence 6 is a Meera number. Another Meera number is 30 because 30 has 2, 3, 5, 6, 10, 15 as nontrivial factors. Thus 30 has 6 nontrivial factors. Note that 6 is a factor of 30. So 30 is a Meera Number. However 21 is **not** a Meera number. The nontrivial factors of 21 are 3 and 7. Thus the number of nontrivial factors is 2. Note that 2 is not a factor of 21. Therefore, 21 is not a Meera number.

Write a function named *isMeera* that returns 1 if its integer argument is a Meera number, otherwise it returns 0.

The signature of the function is

int isMeera(int n)

2. A **Bunker array** is an array that contains the value 1 if and only if it contains a prime number. The array {7, 6, 10, 1} is a Bunker array because it contains a prime number (7)

and also contains a 1. The array {7, 6, 10} is **not** a Bunker array because it contains a prime number (7) but does not contain a 1. The array {6, 10, 1} is **not** a Bunker array because it contains a 1 but does not contain a prime number.

It is okay if a Bunker array contains more than one value 1 and more than one prime, so the array {3, 7, 1, 8, 1} is a Bunker array (3 and 7 are the primes).

Write a function named *isBunker* that returns 1 if its array argument is a Bunker array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

```
int isBunker(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBunker(int a[ ], int len) where len is the number of elements in the array.
```

3. A **Nice array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Nice array because

$$2 = 3-1$$

$$10 = 9+1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Nice arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Nice array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isNice* that returns 1 if its array argument is a Nice array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

```
int isNice(int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isNice(int a[ ], int len) where len is the number of elements in the array.
```

August 15, 2015

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. A **Fibonacci number** is a number in the sequence 1, 1, 2, 3, 5, 8, 13, 21,.... Note that first two Fibonacci numbers are 1 and any Fibonacci number other than the first two is the sum of the previous two Fibonacci numbers. For example, $2 = 1 + 1$, $3 = 2 + 1$, $5 = 3 + 2$ and so on.

Write a function named *isFibonacci* that returns 1 if its integer argument is a Fibonacci number, otherwise it returns 0.

The signature of the function is

int isFibonacci (int n)

2. A **Meera array** is an array that contains the value 0 if and only if it contains a prime number. The array {7, 6, 0, 10, 1} is a Meera array because it contains a prime number (7) and also contains a 0. The array {6, 10, 1} is a Meera array because it contains no prime number and also contains no 0.

The array {7, 6, 10} is **not** a Meera array because it contains a prime number (7) but does not contain a 0. The array {6, 10, 0} is **not** a Meera array because it contains a 0 but does not contain a prime number.

It is okay if a Meera array contains more than one value 0 and more than one prime, so the array {3, 7, 0, 8, 0, 5} is a Meera array (3, 5 and 7 are the primes and there are two zeros.).

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

int isMeera(int [] a)

If you are programming in C or C++, the function signature is

int isMeera(int a[], int len) where *len* is the number of elements in the array.

3. A **Bean array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Bean array because

$$2 = 3 - 1$$

$$10 = 9 + 1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Bean arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Bean array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isBean* that returns 1 if its array argument is a *Bean* array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

int isBean(int[] a)

If you are programming in C or C++, the function signature is

int isBean(int a[], int len) where *len* is the number of elements in the array.

September 5, 2015

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not write main method. If you write, you are just wasting your time! Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. An integer is defined to be a **Bunker** number if it is an element in the infinite sequence 1, 2, 4, 7, 11, 16, 22, ... Note that $2-1=1$, $4-2=2$, $7-4=3$, $11-7=4$, $16-11=5$ so for $k>1$, the k th element of the sequence is equal to the $k-1$ th element + $k-1$. E.G., for $k=6$, 16 is the k th element and is equal to 11 (the $k-1$ th element) + 5 ($k-1$).

Write function named *isBunker* that returns 1 if its argument is a Bunker number, otherwise it returns 0. So *isBunker*(11) returns 1, *isBunker*(22) returns 1 and *isBunker*(8) returns 0 .

The function signature is

int isBunker (int n)

2. Define a **Dual array** to be an array where every value occurs exactly twice.

For example, {1, 2, 1, 3, 3, 2} is a dual array.

The following arrays are **not** Dual arrays

{2, 5, 2, 5, 5} (5 occurs three times instead of two times)

{3, 1, 1, 2, 2} (3 occurs once instead of two times)

Write a function named *isDual* that returns 1 if its array argument is a Dual array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isDual (int[] a)

If you are programming in C or C++, the function signature is

int isDual (int a[], int len) where *len* is the number of elements in the array.

3. An array is defined to be a **Filter array** if it meets the following conditions

- a. If it contains 9 then it also contains 11.
- b. If it contains 7 then it does **not** contain 13.

So {1, 2, 3, **9**, 6, **11**} and {3, 4, 6, **7**, 14, 16}, {1, 2, 3, 4, 10, 11, 13} and {3, 6, 5, 5, 13, 6, 13} are Filter arrays. The following arrays are **not** Filter arrays: {9, 6, 18} (contains 9 but no 11), {4, 7, 13} (contains both 7 and 13)

Write a function named *isFilter* that returns 1 if its array argument is a Filter array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isFilter(int[] a)

If you are programming in C or C++, the function signature is

int isFilter(int a[], int len) where *len* is the number of elements in the array.

September 19 2015

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays

allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. An integer array is said to be *evenSpaced*, if the difference between the largest value and the smallest value is an even number. Write a function *isEvenSpaced(int[] a)* that will return 1 if it is *evenSpaced* and 0 otherwise. If array has less than two elements, function will return 0. If you are programming in C or C++, the function signature is:

`int isEvenSpaced (int a[], int len)` where *len* is the number of elements in the array.

Examples

Array	Largest value	Smallest value	Difference	Return value
{100, 19, 131, 140}	140	19	$140 - 19 = 121$	0
{200, 1, 151, 160}	200	1	$200 - 1 = 199$	0
{200, 10, 151, 160}	200	10	$200 - 10 = 190$	1
{100, 19, -131, -140}	100	-140	$100 - (-140) = 240$	1
{80, -56, 11, -81}	80	-81	$-80 - 80 = -161$	0

2. An *Sub array* is defined to be an array in which each element is greater than sum of all elements **after** that. See examples below:

{13, 6, 3, 2} is a *Sub array*. Note that $13 > 2 + 3 + 6$, $6 > 3 + 2$, $3 > 2$.

{11, 5, 3, 2} is a NOT a *Sub array*. Note that 5 is not greater than $3 + 2$.

Write a function named *isSub* that returns 1 if its array argument is a *Sub array*, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

`int isSub (int [] a)`

If you are programming in C or C++, the function signature is:

`int isSub (int a[], int len)` where *len* is the number of elements in the array.

3. An *isSym* (even/odd Symmetric) *array* is defined to be an array in which even numbers and odd numbers appear in the same order from “*both directions*”. You can assume array has at least one element. See examples below:

{2, 7, 9, 10, 11, 5, 8} is a *isSym* array.

Note that from left to right or right to left we have even, odd, odd, even, odd, odd, even.

{9, 8, 7, 13, 14, 17} is a *isSym* array.

Note that from left to right or right to left we have {odd, even, odd, odd, even, odd}.

However, {2, 7, 8, 9, 11, 13, 10} is not a *isSym* array.

From left to right we have {even, odd, even, odd, odd, odd, even}.

From right to left we have {even, odd, odd, odd, even, odd, even},

which is not the same.

Write a function named *isSym* that returns 1 if its array argument is a *isSym* array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

`int isSym (int [] a)`

If you are programming in C or C++, the function signature is:
`int isSym (int a[], int len)` where *len* is the number of elements in the array.

October 3rd 2015

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. A **Fibonacci number** is a number in the sequence 1, 1, 2, 3, 5, 8, 13, 21,.... Note that first two Fibonacci numbers are 1 and any Fibonacci number other than the first two is the sum of the previous two Fibonacci numbers. For example, $2 = 1 + 1$, $3 = 2 + 1$, $5 = 3 + 2$ and so on.

Write a function named *isFibonacci* that returns 1 if its integer argument is a Fibonacci number, otherwise it returns 0.

The signature of the function is

int isFibonacci (int n)

2. Write a function *sumIsPower* with signature

boolean sumIsPower(int[] arr)

which outputs true if the sum of the elements in the input array *arr* is a power of 2, false otherwise. Recall that the powers of 2 are 1, 2, 4, 8, 16, and so on. In general a number is a power of 2 if and only if it is of the form 2^n for some nonnegative integer *n*. You may assume (without verifying in your code) that all elements in the array are positive integers. If the input array *arr* is null, the return value should be false.

Examples:

`sumIsPower({8,8,8,8})` is true since $8 + 8 + 8 + 8 = 32 = 2^5$.

`sumIsPower({8,8,8})` is false, since $8 + 8 + 8 = 24$, not a power of 2.

3. A **wave array** is defined to an array which does **not** contain two even numbers or two odd numbers in adjacent locations. So {7, 2, 9, 10, 5}, {4, 11, 12, 1, 6}, {1, 0, 5} and {2} are all **wave arrays**. But {2, 6, 3, 4} is not a wave array because the even numbers 2 and 6 are adjacent to each other.

Write a function named *isWave* that returns 1 if its array argument is a Wave array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

`int isWave (int [] a)`

If you are programming in C or C++, the function signature is

`int isWave (int a[], int len)` where len is the number of elements in the array.

October 10, 2015

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

QUESTION 1. An array *a* is called *paired* if its even numbered elements (*a*[0], *a*[2], etc.) are odd and its odd numbered elements (*a*[1], *a*[3], etc.) are even. Write a function

named *isPaired* that accepts an array of integers and returns 1 if the array is paired, otherwise it returns 0. Examples: {7, 2, 3, 6, 7} is paired since a[0], a[2] and a[4] are odd, a[1] and a[3] are even. {7, 15, 9, 2, 3} is not paired since a[1] is odd. {17, 6, 2, 4} is not paired since a[2] is even.

If you are programming in Java or C#, the function signature is

int isPaired(int[] a)

If you are programming in C or C++, the function signature is

int isPaired(int a[], int len)

where *len* is the number of elements in the array.

QUESTION 2. An array is defined to be **odd-heavy** if it contains at least one odd element and every odd element is greater than every even element. So {11, 4, 9, 2, 8} is odd-heavy because the two odd elements (11 and 9) are greater than all the even elements. And {11, 4, 9, 2, 3, 10} is not odd-heavy because the even element 10 is greater than the odd element 9. Write a function called *isOddHeavy* that accepts an integer array and returns 1 if the array is odd-heavy; otherwise it returns 0. Some other examples: {1} is odd-heavy, {2} is not odd-heavy, {1, 1, 1, 1} is odd-heavy, {2, 4, 6, 8, 11} is odd-heavy, {-2, -4, -6, -8, -11} is not odd-heavy.

If you are programming in Java or C#, the function signature is

int isOddHeavy(int[] a)

If you are programming in C or C++, the function signature is

int isOddHeavy(int a[], int len)

where *len* is the number of elements in the array.

Nov 7th 2015

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. Write a function named **factorTwoCount** that returns the number of times that 2 divides the argument.

For example, factorTwoCount(48) returns 4 because

$$48/2 = 24$$

$$24/2 = 12$$

$$12/2 = 6$$

$$6/2 = 3$$

2 does not divide 3 evenly.

Another example: `factorTwoCount(27)` returns 0 because 2 does not divide 27.

The function signature is

```
int factorTwoCount(int n);
```

2. A **Meera array** is defined to be an array that contains at least one odd number and begins and ends with the same number of even numbers.

So {**4, 8, 6**, 3, 2, 9, 8, 11, 8, 13, **12, 12, 6**} is a Meera array because it begins with three even numbers and ends with three even numbers and it contains at least one odd number

The array {2, 4, 6, 8, 6} is not a Meera array because it does not contain an odd number.

The array {**2, 8**, 7, **10, -4, 6**} is not a Meera array because it begins with two even numbers but ends with three even numbers.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array. Otherwise, it returns 0.

If you are writing in Java or C#, the function signature is

int isMeera (int[] a)

If you are writing in C or C++, the function signature is

int isMeera (int a[], int len) where len is the number of elements in the array.

3. Write a function called **goodSpread** that returns 1 if no value in its array argument occurs more than 3 times in the array.

For example, goodSpread(new int[] {2, 1, 2, 5, 2, 1, 5, 9}) returns 1 because no value occurs more than three times.

But goodSpread(new int[] {3, 1, 3, 1, 3, 5, 5, 3}) returns 0 because the value 3 occurs four times.

If you are writing in Java or C#, the function signature is

int goodSpread (int[] a)

If you are writing in C or C++, the function signature is

int goodSpread (int a[], int len) where len is the number of elements in the array.

Nov 21st 2015

There are three questions on this test. Please do your own work. All you need to write is three functions. Please do not use any String functions. No sorting allowed. No additional arrays or data structures allowed. Try to write a simple, elegant and correct code. If you are not a Java or C# programmer, you can assume one more argument int len, to pass the length of the array.

Question 1. Write a function fill with signature

`int[] fill(int[] arr, int k, int n)`

which does the following: It returns an integer array arr2 of length n whose first k elements are the same as the first k elements of arr, and whose remaining elements consist of repeating blocks of the first k elements. You can assume array arr has at least k elements. The function should return null if either k or n is not positive.

Examples: `fill({1,2,3,5, 9, 12,-2,-1}, 3, 10)` returns `{1,2,3,1,2,3,1,2,3,1}`. `fill({4, 2, -3, 12}, 1, 5)` returns `{4, 4, 4, 4, 4}`. `fill({2, 6, 9, 0, -3}, 0, 4)` returns null.

Question 2. Write a function sumIsPower with signature

`boolean sumIsPower(int[] arr)`

which outputs true if the sum of the elements in the input array arr is a power of 2, false otherwise. Recall that the powers of 2 are 1, 2, 4, 8, 16, and so on. In general a number is a power of 2 if and only if it is of the form 2^n for some nonnegative integer n. You may assume (without verifying in your code) that all elements in the array are positive integers. If the input array arr is null, the return value should be false.

Examples: `sumIsPower({8,8,8,8})` is true since $8 + 8 + 8 + 8 = 32 = 2^5$. `sumIsPower({8,8,8})` is false, since $8 + 8 + 8 = 24$, not a power of 2.

Question 3. An array is said to be hollow if it contains 3 or more zeros in the middle that are preceded and followed by the same number of non-zero elements. Write a function named `isHollow` that accepts an integer array and returns 1 if it is a hollow array, otherwise it returns 0. The function signature is

`int isHollow(int[] a).`

Examples: `isHollow({1,2,4,0,0,0,3,4,5})` returns true. `isHollow ({1,2,0,0,0,3,4,5})` returns false. : `isHollow ({1,2,4,9, 0,0,0,3,4, 5})` returns false. `isHollow ({1,2, 0,0, 3,4})` returns false.

Dec 5th 2015

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. An integer is defined to be an **even subset** of another integer n if every even factor of m is also a factor of n . For example 18 is an even subset of 12 because the even factors of 18 are 2 and 6 and these are both factors of 12. But 18 is not an even subset of 32 because 6 is not a factor of 32.

Write a function with signature **int isEvenSubset(int m, int n)** that returns 1 if m is an even subset of n , otherwise it returns 0.

2. A **twinoid** is defined to be an array that has exactly two even values that are adjacent to one another. For example {3, 3, 2, 6, 7} is a twinoid array because it has exactly two even values (2 and 6) and they are adjacent to one another. The following arrays are not twinoid arrays.

{3, 3, 2, 6, 6, 7} because it has three even values.

{3, 3, 2, 7, 6, 7} because the even values are not adjacent to one another

{3, 8, 5, 7, 3} because it has only one even value.

Write a function named **isTwinoid** that returns 1 if its array argument is a twinoid array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

`int isTwinoid (int [] a);`

If you are programming in C or C++, the function signature is

`int isTwinoid(int a[], int len)` where `len` is the number of elements in the array.

3. A **balanced** array is defined to be an array where for every value n in the array, $-n$ also is in the array. For example {-2, 3, 2, -3} is a balanced array. So is {-2, 2, 2, 2}. But {-5, 2, -2} is not because 5 is not in the array.

Write a function named **isBalanced** that returns 1 if its array argument is a balanced array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

`int isBalanced (int [] a);`

If you are programming in C or C++, the function signature is

`int isBalanced(int a[], int len)` where `len` is the number of elements in the array.

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa. You are not allowed to use any additional data structures.

1. A **Meera number** is a number such that the number of nontrivial factors is a factor of the number. For example, 6 is a Meera number because 6 has two nontrivial factors : 2 and 3. (A nontrivial factor is a factor other than 1 and the number). Thus 6 has two nontrivial factors. Now, 2 is a factor of 6. Thus the number of nontrivial factors is a factor of 6. Hence 6 is a Meera number. Another Meera number is 30 because 30 has 2, 3, 5, 6, 10, 15 as nontrivial factors. Thus 30 has 6 nontrivial factors. Note that 6 is a factor of 30. So 30 is a Meera Number. However 21 is **not** a Meera number. The nontrivial factors of 21 are 3 and 7. Thus the number of nontrivial factors is 2. Note that 2 is not a factor of 21. Therefore, 21 is not a Meera number.

Write a function named *isMeera* that returns 1 if its integer argument is a Meera number, otherwise it returns 0.

The signature of the function is

```
int isMeera(int n)
```

2. A **Bunker array** is an array that contains the value 1 if and only if it contains a prime number. The array {7, 6, 10, 1} is a Bunker array because it contains a prime number (7) and also contains a 1. The array {7, 6, 10} is **not** a Bunker array because it contains a prime number (7) but does not contain a 1. The array {6, 10, 1} is **not** a Bunker array because it contains a 1 but does not contain a prime number.

It is okay if a Bunker array contains more than one value 1 and more than one prime, so the array {3, 7, 1, 8, 1} is a Bunker array (3 and 7 are the primes).

Write a function named *isBunker* that returns 1 if its array argument is a Bunker array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

```
int isBunker(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBunker(int a[ ], int len) where len is the number of elements in the array.
```

3. A **Nice array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Nice array because

$$2 = 3 - 1$$

$$10 = 9 + 1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Nice arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Nice array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isNice* that returns 1 if its array argument is a Nice array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

```
int isNice(int[] a)
```

If you are programming in C or C++, the function signature is

```
int isNice(int a[], int len) where len is the number of elements in the array.
```

Jan 9th 2016

There are 3 questions on this test. You have 2 hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string functions. No sorting allowed. No additional arrays allowed.

1. Write a function named **minDistance** that returns the smallest distance between two non-trivial factors of a number. For example, consider 63. Its non-trivial factors are 3, 7, 9 and 21. Thus **minDistance**(63) would return 2 because the smallest distance between any two non-trivial factors is 2 (9 - 7 = 2). As another example, **minDistance** (25) would return 0 because 25 has only one non-trivial factor: 5. Thus the smallest distance between any two non-trivial factors is 0 (5 - 5 = 0). Note that **minDistance**(11) would return -1 since 11 has no non-trivial factors.

The function signature is

int **minDistance**(int n)

2. A **wave array** is defined to an array which does **not** contain two even numbers or two odd numbers in adjacent locations. So {7, 2, 9, 10, 5}, {4, 11, 12, 1, 6}, {1, 0, 5} and {2} are all **wave arrays**. But {2, 6, 3, 4} is not a wave array because the even numbers 2 and 6 are adjacent to each other.

Write a function named *isWave* that returns 1 if its array argument is a Wave array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isWave (int [] a)

If you are programming in C or C++, the function signature is

int isWave (int a[], int len) where len is the number of elements in the array.

3. An array is defined to be a **Bean array** if it meets the following conditions

- a. If it contains a 9 then it also contains a 13.
- b. If it contains a 7 then it does **not** contain a 16.

So {1, 2, 3, **9**, 6, **13**} and {3, 4, 6, **7**, 13, 15}, {1, 2, 3, 4, 10, 11, 12} and {3, 6, 9, 5, 7, 13, 6, 17} are Bean arrays. The following arrays are **not** Bean arrays:

- a. { 9, 6, 18} (contains a 9 but no 13)
- b. {4, 7, 16} (contains both a 7 and a 16)

Write a function named *isBean* that returns 1 if its array argument is a Bean array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isBean (int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBean (int a[ ], int len) where len is the number of elements in the array.
```

Jan 23rd 2016

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not write main method. If you write, you are just wasting your time! Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. A **fancy number** is a number in the sequence 1, 1, 5, 17, 61,Note that first two fancy numbers are 1 and any fancy number other than the first two is sum of the three times previousone and two times the one before that. See below:

1,

1,

$$3*1 + 2*1 = 5$$

$$3*5 + 2*1 = 17$$

$$3*17 + 2*5 = 61$$

Write a function named *isFancy* that returns 1 if its integer argument is a Fancy number, otherwise it returns 0.

The signature of the function is

int isFancy(int n)

2. A **Meera array** is an array that contains the value 1 if and only if it contains 9. The array {7, 9, 0, 10, 1} is a Meera array because it contains 1 and 9. The array {6, 10, 8} is a Meera array because it contains no 1 and also contains no 9.

The array {7, 6, 1} is **not** a Meera array because it contains 1 but does not contain a 9. The array {9, 10, 0} is **not** a Meera array because it contains a 9 but does not contain 1.

It is okay if a Meera array contains more than one value 1 and more than one 9, so the array {1, 1, 0, 8, 0, 9, 9, 1} is a Meera array.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

If you are programming in Java or C#, the function signature is

int isMeera(int [] a)

If you are programming in C or C++, the function signature is

int isMeera(int a[], int len) where *len* is the number of elements in the array.

3. A **Bean array** is defined to be an integer array where for every value n in the array, there is also an element $2n$, $2n+1$ or $n/2$ in the array.

For example, {4, 9, 8} is a Bean array because

For 4, 8 is present; for 9, 4 is present; for 8, 4 is present.

Other Bean arrays include {2, 2, 5, 11, 23}, {7, 7, 3, 6} and {0}.

The array {3, 8, 4} is **not** a Bean array because of the value 3 which requires that the array contains either the value 6, 7 or 1 and none of these values are in the array.

Write a function named *isBean* that returns 1 if its array argument is a *Bean* array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

int isBean(int[] a)

If you are programming in C or C++, the function signature is

int isBean(int a[], int len) where *len* is the number of elements in the array.

Feb 13, 2016

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. Write a function named **factorTwoCount** that returns the number of times that 2 divides the argument.

For example, `factorTwoCount(48)` returns 4 because

$$48/2 = 24$$

$$24/2 = 12$$

$$12/2 = 6$$

$$6/2 = 3$$

2 does not divide 3 evenly.

Another example: `factorTwoCount(27)` returns 0 because 2 does not divide 27.

The function signature is

```
int factorTwoCount(int n);
```

2. A **Meera array** is defined to be an array that contains at least one odd number and begins and ends with the same number of even numbers.

So {**4, 8, 6**, 3, 2, 9, 8, 11, 8, 13, **12, 12, 6**} is a Meera array because it begins with three even numbers and ends with three even numbers and it contains at least one odd number

The array {2, 4, 6, 8, 6} is not a Meera array because it does not contain an odd number.

The array {**2, 8**, 7, **10, -4, 6**} is not a Meera array because it begins with two even numbers but ends with three even numbers.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array. Otherwise, it returns 0.

If you are writing in Java or C#, the function signature is

```
int isMeera (int[ ] a)
```

If you are writing in C or C++, the function signature is

```
int isMeera (int a[ ], int len) where len is the number of elements in the array.
```

3. Write a function called **goodSpread** that returns 1 if no value in its array argument occurs more than 3 times in the array.

For example, `goodSpread(new int[] {2, 1, 2, 5, 2, 1, 5, 9})` returns 1 because no value occurs more than three times.

But `goodSpread(new int[] {3, 1, 3, 1, 3, 5, 5, 3})` returns 0 because the value 3 occurs four times.

If you are writing in Java or C#, the function signature is

```
int goodSpread (int[ ] a)
```

If you are writing in C or C++, the function signature is

```
int goodSpread (int a[ ], int len) where len is the number of elements in the array.
```

Feb 27, 2016

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. An integer array is said to be *evenSpaced*, if the difference between the largest value and the smallest value is an even number. Write a function *isEvenSpaced(int[] a)* that will return 1 if it is *evenSpaced* and 0 otherwise. If array has less than two elements, function will return 0. If you are programming in C or C++, the function signature is:

int *isEvenSpaced* (int a[], int len) where *len* is the number of elements in the array.

Examples

Array	Largest value	Smallest value	Difference	Return value
{100, 19, 131, 140}	140	19	$140 - 19 = 121$	0
{200, 1, 151, 160}	200	1	$200 - 1 = 199$	0
{200, 10, 151, 160}	200	10	$200 - 10 = 190$	1
{100, 19, -131, -140}	100	-140	$100 - (-140) = 240$	1
{80, -56, 11, -81}	80	-81	$-80 - 80 = -161$	0

2. An *Sub array* is defined to be an array in which each element is greater than sum of all elements **after** that. See examples below:

{13, 6, 3, 2} is a *Sub array*. Note that $13 > 2 + 3 + 6$, $6 > 3 + 2$, $3 > 2$.

{11, 5, 3, 2} is a NOT a *Sub array*. Note that 5 is not greater than $3 + 2$.

Write a function named *isSub* that returns 1 if its array argument is a *Sub array*, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

int *isSub* (int [] a)

If you are programming in C or C++, the function signature is:

int *isSub* (int a[], int len) where *len* is the number of elements in the array.

3. An *isSym* (even/odd Symmetric) *array* is defined to be an array in which even numbers and odd numbers appear in the same order from “*both directions*”. You can assume array has at least one element. See examples below:

{2, 7, 9, 10, 11, 5, 8} is a *isSym* array.

Note that from left to right or right to left we have even, odd, odd, even, odd, odd, even.

{9, 8, 7, 13, 14, 17} is a *isSym* array.

Note that from left to right or right to left we have {odd, even, odd, odd, even, odd}.

However, {2, 7, 8, 9, 11, 13, 10} is not a *isSym* array.

From left to right we have {even, odd, even, odd, odd, odd, even}.

From right to left we have {even, odd, odd, odd, even, odd, even},

which is not the same.

Write a function named *isSym* that returns 1 if its array argument is a *isSym* array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

`int isSym (int [] a)`

If you are programming in C or C++, the function signature is:

`int isSym (int a[], int len)` where *len* is the number of elements in the array.

March 12, 2016

There are three questions on this test. You have two hours to complete it. Please do your own work.

1. A **Pascal number** is a number that is the sum of the integers from 1 to *j* for some *j*. For example 6 is a Pascal number because $6 = 1 + 2 + 3$. Here *j* is 3. Another Pascal number is 15 because $15 = 1 + 2 + 3 + 4 + 5$. An example of a number that is not a Pascal number is 7 because it falls between the Pascal numbers 6 and 10.

Write a function named *isPascal* that returns 1 if its integer argument is a Pascal number, otherwise it returns 0.

The signature of the function is

`int isPascal (int n)`

2. A **Meera array** is an array that contains the value 1 if and only if it contains a prime number. The array {7, 6, 10, 1} is a Meera array because it contains a prime number (7) and also contains a 1. The array {7, 6, 10} is **not** a Meera array because it contains a prime number (7) but does not contain a 1. The array {6, 10, 1} is **not** a Meera array because it contains a 1 but does not contain a prime number.

It is okay if a Meera array contains more than one value 1 and more than one prime, so the array {3, 7, 1, 8, 1} is a Meera array (3 and 7 are the primes).

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

```
int isMeera (int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isMeera (int a[ ], int len) where len is the number of elements in the array.
```

3. A **Suff array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Suff array because

$$2 = 3-1$$

$$10 = 9+1$$

$$3 = 2 + 1$$

$$9 = 10 -1$$

Other Suff arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Suff array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isSuff* that returns 1 if its array argument is a Suff array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

```
int isSuff (int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isSuff (int a[ ], int len) where len is the number of elements in the array.
```

March 26 2016

This exam is two hours long and contains three questions. Please indent your code so it is easy for the grader to read it.

1. Write a method named **getExponent(n, p)** that returns the largest exponent x such that p^x evenly divides n . If p is ≤ 1 the method should return -1.

For example, `getExponent(162, 3)` returns 4 because $162 = 2^1 * 3^4$, therefore the value of x here is 4.

The method signature is

```
int getExponent(int n, int p)
```

Examples:

if n is	and p is	return	because
27	3	3	3^3 divides 27 evenly but 3^4 does not.
28	3	0	3^0 divides 28 evenly but 3^1 does

280	7	1	not. 7 ¹ divides 280 evenly but 7 ² does not.
-250	5	3	5 ³ divides -250 evenly but 5 ⁴ does not.
18	1	-1	if p <=1 the function returns -1.
128	4	3	4 ³ divides 128 evenly but 4 ⁴ does not.

2. Define an array to be a 121 array if all its elements are either 1 or 2 and it begins with one or more 1s followed by a one or more 2s and then ends with the same number of 1s that it begins with. Write a method named **is121Array** that returns 1 if its array argument is a 121 array, otherwise, it returns 0.

If you are programming in Java or C#, the function signature is

```
int is121Array(int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int is121Array(int a[ ], int len) where len is the number of elements in the array a.
```

Examples

a is	then function returns	reason
{1, 2, 1}	1	because the same number of 1s are at the beginning and end of the array and there is at least one 2 in between them.
{1, 1, 2, 2, 2, 1, 1}	1	because the same number of 1s are at the beginning and end of the array and there is at least one 2 in between them.
{1, 1, 2, 2, 2, 1, 1, 1}	0	Because the number of 1s at the end does not equal the number of 1s at the beginning.
{1, 1, 2, 1, 2, 1, 1}	0	Because the middle does not contain only 2s.
{1, 1, 1, 2, 2, 2, 1, 1, 1, 3}	0	Because the array contains a number other than 1 and 2.
{1, 1, 1, 1, 1, 1}	0	Because the array does not contain any 2s
{2, 2, 2, 1, 1, 1, 2, 2, 2, 1, 1}	0	Because the first element of the array is not a 1.
{1, 1, 1, 2, 2, 2, 1, 1, 2, 2}	0	Because the last element of the array is not a 1.
{2, 2, 2}	0	Because there are no 1s in the array.

3. An array is defined to be **maxmin equal** if it contains at least two **different** elements and the number of times the maximum value occur is the same as the number of times the minimum value occur. So {11, 4, 9, 11, 8, 5, 4, 10} is **maxmin equal**, because the max value 11 and min value 4 both appear two times in the array.

Write a function called *isMaxMinEqual* that accepts an integer array and returns 1 if the array is **maxmin equal**; otherwise it returns 0.

If you are programming in Java or C#, the function signature is

`int isMaxMinEqual(int[] a)`

If you are programming in C or C++, the function signature is

`int isMaxMinEqual(int a[], int len)` where len is the number of elements in the array

Some other examples:

if the input array is	<i>isMaxMinEqual</i> should return
{ }	0 (array must have at least two <i>different</i> elements)
{ 2 }	0 (array must have at least two <i>different</i> elements)
{ 1, 1, 1, 1, 1, 1 }	0 (array must have at least two <i>different</i> elements)
{ 2, 4, 6, 8, 11 }	1 (Both max value (11) and min value 2 appear exactly one time)
{ -2, -4, -6, -8, -11 }	1 (Both max value (-2) and min value -11 appear exactly one time)

April 9th 2016

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. Write a function named **countDigit** that returns the number of times that a given digit appears in a positive number. For example `countDigit(32121, 1)` would return 2 because there are two 1s in 32121. Other examples:

`countDigit(33331, 3)` returns 4

`countDigit(33331, 6)` returns 0

`countDigit(3, 3)` returns 1

The function should return -1 if either argument is negative, so

`countDigit(-543, 3)` returns -1.

The function signature is

`int countDigit(int n, int digit)`

Hint: Use modulo base 10 and integer arithmetic to isolate the digits of the number.

2. A *Bunker array* is defined to be an array in which **at least one** odd number is immediately followed by a prime number. So {4, 9, 6, 7, 3} is a Bunkerarray because the odd number 7 is immediately followed by the prime number 3. But {4, 9, 6, 15, 21} is not a Bunker array because none of the oddnumbers are immediately followed by a prime number.

Write a function named **isBunkerArray** that returns 1 if its array argument is a Bunker array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isBunkerArray(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBunkerArray(int a[ ], int len) where len is the number of elements in the array.
```

You may assume that there exists a function isPrime that returns 1 if it argument is a prime, otherwise it returns 0. **You do not have to write this function.**

3. A *Meera array* is defined to be an array such that for all values n in the array, the value $2*n$ is not in the array. So {3, 5, -2} is a Meera array because $3*2$, $5*2$ and $-2*2$ are not in the array. But {8, 3, 4} is not a Meera array because for $n=4$, $2*n=8$ is in the array.

Write a function named **isMeera** that returns 1 if its array argument is a Meera array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isMeera(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isMeera(int a[ ], int len) where len is the number of elements in the array.
```

April 23rd 2016

There are three questions on this test. Please do your own work. All you need to write is three functions. Please do not use any String functions. No sorting allowed. No additional arrays or data structures allowed. Try to write a simple, elegant and correct code. If you are not a Java or C# programmer, you can assume one more argument int len, to pass the length of the array.

Question 1. Write a function fill with signature

```
int[] fill(int[] arr, int k, int n)
```

which does the following: It returns an integer array arr2 of length n whose first k elements are the same as the first k elements of arr, and whose remaining elements consist of repeating blocks of the

first k elements. You can assume array arr has at least k elements. The function should return null if either k or n is not positive.

Examples: fill({1,2,3,5, 9, 12,-2,-1}, 3, 10) returns {1,2,3,1,2,3,1,2,3,1}. Fill({4, 2, -3, 12}, 1, 5) returns {4, 4, 4, 4, 4}. fill({2, 6, 9, 0, -3}, 0, 4) returns null.

Question 2. Write a function sumIsPower with signature

boolean sumIsPower(int[] arr)

which outputs true if the sum of the elements in the input array arr is a power of 2, false otherwise. Recall that the powers of 2 are 1, 2, 4, 8, 16, and so on. In general a number is a power of 2 if and only if it is of the form 2^n for some nonnegative integer n. You may assume (without verifying in your code) that all elements in the array are positive integers. If the input array arr is null, the return value should be false.

Examples: sumIsPower({8,8,8,8}) is true since $8 + 8 + 8 + 8 = 32 = 2^5$. sumIsPower({8,8,8}) is false, since $8 + 8 + 8 = 24$, not a power of 2.

Question 3. An array is said to be hollow if it contains 3 or more zeros in the middle that are preceded and followed by the same number of non-zero elements. Write a function named isHollow that accepts an integer array and returns 1 if it is a hollow array, otherwise it returns 0. The function signature is

int isHollow(int[] a).

Examples: isHollow({1,2,4,0,0,0,3,4,5}) returns true. isHollow ({1,2,0,0,0,3,4,5}) returns false. : isHollow ({1,2,4,9, 0,0,0,3,4, 5}) returns false. isHollow ({1,2, 0,0, 3,4}) returns false.

May 7 2016

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. Write a function named **factorTwoCount** that returns the number of times that 2 divides the argument.

For example, `factorTwoCount(48)` returns 4 because

$$48/2 = 24$$

$$24/2 = 12$$

$$12/2 = 6$$

$$6/2 = 3$$

2 does not divide 3 evenly.

Another example: `factorTwoCount(27)` returns 0 because 2 does not divide 27.

The function signature is

```
int factorTwoCount(int n);
```

2. A **Meera array** is defined to be an array that contains at least one odd number and begins and ends with the same number of even numbers.

So **{4, 8, 6, 3, 2, 9, 8, 11, 8, 13, 12, 12, 6}** is a Meera array because it begins with three even numbers and ends with three even numbers and it contains at least one odd number

The array **{2, 4, 6, 8, 6}** is not a Meera array because it does not contain an odd number.

The array **{2, 8, 7, 10, -4, 6}** is not a Meera array because it begins with two even numbers but ends with three even numbers.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array. Otherwise, it returns 0.

If you are writing in Java or C#, the function signature is

```
int isMeera (int[ ] a)
```

If you are writing in C or C++, the function signature is

```
int isMeera (int a[ ], int len) where len is the number of elements in the array.
```

3. Write a function called **goodSpread** that returns 1 if no value in its array argument occurs more than 3 times in the array.

For example, `goodSpread(new int[] {2, 1, 2, 5, 2, 1, 5, 9})` returns 1 because no value occurs more than three times.

But `goodSpread(new int[] {3, 1, 3, 1, 3, 5, 5, 3})` returns 0 because the value 3 occurs four times.

If you are writing in Java or C#, the function signature is

```
int goodSpread (int[ ] a)
```

If you are writing in C or C++, the function signature is

```
int goodSpread (int a[ ], int len) where len is the number of elements in the array.
```

May 21, 2016

This exam is two hours long and contains three questions. Please indent your code so it is easy for the grader to read it.

1. Write a method named **getExponent(n, p)** that returns the largest exponent x such that p^x evenly divides n. If p is ≤ 1 the method should return -1.

For example, `getExponent(162, 3)` returns 4 because $162 = 2^1 * 3^4$, therefore the value of x here is 4.

The method signature is

`int getExponent(int n, int p)`

Examples:

if n is and p is return because

27	3	3	3^3 divides 27 evenly but 3^4 does not.
28	3	0	3^0 divides 28 evenly but 3^1 does not.
280	7	1	7^1 divides 280 evenly but 7^2 does not.
-250	5	3	5^3 divides -250 evenly but 5^4 does not.
18	1	-1	if $p \leq 1$ the function returns -1.
128	4	3	4^3 divides 128 evenly but 4^4 does not.

2. Define an array to be a 121 array if all its elements are either 1 or 2 and it begins with one or more 1s followed by a one or more 2s and then ends with the same number of 1s that it begins with. Write a method named **is121Array** that returns 1 if its array argument is a 121 array, otherwise, it returns 0.

If you are programming in Java or C#, the function signature is

`int is121Array(int[] a)`

If you are programming in C or C++, the function signature is

`int is121Array(int a[], int len)` where len is the number of elements in the array a.

Examples

a is	then function returns	reason
------	--------------------------	--------

{1, 2, 1}	1	because the same number of 1s are at the beginning and end of the array and there is at least one 2 in between them.
{1, 1, 2, 2, 2, 1, 1}	1	because the same number of 1s are at the beginning and end of the array and there is at least one 2 in between them.
{1, 1, 2, 2, 2, 1, 1, 1}	0	Because the number of 1s at the end does not equal the number of 1s at the beginning.
{1, 1, 2, 1, 2, 1, 1}	0	Because the middle does not contain only 2s.
{1, 1, 1, 2, 2, 2, 1, 1, 1, 3}	0	Because the array contains a number other than 1 and 2.
{1, 1, 1, 1, 1, 1}	0	Because the array does not contain any 2s
{2, 2, 2, 1, 1, 1, 2, 2, 2, 1, 1}	0	Because the first element of the array is not a 1.
{1, 1, 1, 2, 2, 2, 1, 1, 2, 2}	0	Because the last element of the array is not a 1.
{2, 2, 2}	0	Because there are no 1s in the array.

3. An array is defined to be **maxmin equal** if it contains at least two **different** elements and the number of times the maximum value occur is the same as the number of times the minimum value occur. So {11, 4, 9, 11, 8, 5, 4, 10} is **maxmin equal**, because the max value 11 and min value 4 both appear two times in the array.

Write a function called *isMaxMinEqual* that accepts an integer array and returns 1 if the array is **maxmin equal**; otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isMaxMinEqual(int[] a)
```

If you are programming in C or C++, the function signature is

```
int isMaxMinEqual(int a[], int len) where len is the number of elements in the array
```

Some other examples:

if the input array is	<i>isMaxMinEqual</i> should return
{}	0 (array must have at least two <i>different</i> elements)
{2}	0 (array must have at least two <i>different</i> elements)
{1, 1, 1, 1, 1, 1}	0 (array must have at least two <i>different</i> elements)
{2, 4, 6, 8, 11}	1 (Both max value (11) and min value 2 appear exactly one time)
{-2, -4, -6, -8, -11}	1 (Both max value (-2) and min value -11 appear exactly one time)

June 4th 2016

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. An integer is defined to be an **even subset** of another integer n if every even factor of m is also a factor of n . For example 18 is an even subset of 12 because the even factors of 18 are 2 and 6 and these are both factors of 12. But 18 is not an even subset of 32 because 6 is not a factor of 32.

Write a function with signature **int isEvenSubset(int m, int n)** that returns 1 if m is an even subset of n , otherwise it returns 0.

2. A **twinoid** is defined to be an array that has exactly two even values that are adjacent to one another. For example {3, 3, 2, 6, 7} is a twinoid array because it has exactly two even values (2 and 6) and they are adjacent to one another. The following arrays are not twinoid arrays.

{3, 3, 2, 6, 6, 7} because it has three even values.

{3, 3, 2, 7, 6, 7} because the even values are not adjacent to one another

{3, 8, 5, 7, 3} because it has only one even value.

Write a function named **isTwinoid** that returns 1 if its array argument is a twinoid array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isTwinoid (int [] a);

If you are programming in C or C++, the function signature is

int isTwinoid(int a[], int len) where len is the number of elements in the array.

3. A **balanced** array is defined to be an array where for every value n in the array, $-n$ also is in the array. For example {-2, 3, 2, -3} is a balanced array. So is {-2, 2, 2, 2}. But {-5, 2, -2} is not because 5 is not in the array.

Write a function named isBalanced that returns 1 if its array argument is a balanced array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

`int isBalanced (int [] a);`

If you are programming in C or C++, the function signature is

`int isBalanced(int a[], int len)` where len is the number of elements in the array.

18th of June 2016

rk. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. **Mode** is the most frequently appearing value. Write a function named *hasSingleMode* that takes an array argument and returns 1 if the mode value in its array argument occurs exactly once in the array, otherwise it returns 0. If you are writing in Java or C#, the function signature is

int hasSingleMode(int[]).

If you are writing in C or C++, the function signature is

int hasSingleMode(int a[], int len)

where len is the length of a.

Examples

Array elements	Mode values	Value returned	Comments
1, -29, 8, 5, -29, 6	-29	1	single mode

1, 2, 3, 4, 2, 4, 7	2, 4	0	no single mode
1, 2, 3, 4, 6	1, 2, 3, 4, 6	0	no single mode
7, 1, 2, 1, 7, 4, 2, 7,	7	1	single mode

2. A **Meera array** is an array that contains the value 0 if and only if it contains a prime number. The array {7, 6, 0, 10, 1} is a Meera array because it contains a primenumber (7) and also contains a 0. The array {6, 10, 1} is a Meera array because it contains no prime number and also contains no 0.

The array {7, 6, 10} is **not** a Meera array because it contains a prime number (7) but does not contain a 0. The array {6, 10, 0} is **not** a Meera array because it contains a 0 but does not contain a prime number.

It is okay if a Meera array contains more than one value 0 and more than one prime, so the array {3, 7, 0, 8, 0, 5} is a Meera array (3, 5 and 7 are the primes and there are two zeros.).

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write isPrime, you can just call it.

If you are programming in Java or C#, the function signature is

int isMeera(int [] a)

If you are are programming in C or C++, the function signature is

int isMeera(int a[], int len) where *len* is the number of elements in the array.

3. A **Bean array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Bean array because

$$2 = 3-1$$

$$10 = 9+1$$

$$3 = 2 + 1$$

$$9 = 10 -1$$

Other Bean arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Bean array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isBean* that returns 1 if its array argument is a *Bean* array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

int isBean(int[] a)

If you are programming in C or C++, the function signature is

int isBean(int a[], int len) where *len* is the number of elements in the array.

July 2nd 2016

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

QUESTION 1. An array *a* is called ***paired*** if its even numbered elements (*a*[0], *a*[2], etc.) are odd and its odd numbered elements (*a*[1], *a*[3], etc.) are even. Write a function named *isPaired* that accepts an array of integers and returns 1 if the array is paired, otherwise it returns 0. Examples: {7, 2, 3, 6, 7} is paired since *a*[0], *a*[2] and *a*[4] are odd, *a*[1] and *a*[3] are even. {7, 15, 9, 2, 3} is not paired since *a*[1] is odd. {17, 6, 2, 4} is not paired since *a*[2] is even.

If you are programming in Java or C#, the function signature is

int isPaired(int[] a)

If you are programming in C or C++, the function signature is

int isPaired(int a[], int len)

where *len* is the number of elements in the array.

QUESTION 2. An array is defined to be ***odd-heavy*** if it contains at least one odd element and every odd element is greater than every even element. So {11, 4, 9, 2, 8} is odd-heavy because the two odd elements (11 and 9) are greater than all the even elements. And {11, 4, 9, 2, 3, 10} is not odd-heavy because the even element 10 is greater than the odd element 9. Write a function called *isOddHeavy* that accepts an integer array and returns 1 if the array is odd-heavy; otherwise it returns 0. Some other examples: {1} is odd-heavy, {2} is not odd-heavy, {1, 1, 1, 1} is odd-heavy, {2, 4, 6, 8, 11} is odd-heavy, {-2, -4, -6, -8, -11} is not odd-heavy.

If you are programming in Java or C#, the function signature is

int isOddHeavy(int[] a)

If you are programming in C or C++, the function signature is

int isOddHeavy(int a[], int len)

where *len* is the number of elements in the array.

QUESTION 3. Write a function named `maxDistance` that returns the largest distance between two non-trivial factors of a number. For example, consider $1001 = 7 * 11 * 13$. Its non-trivial factors are 7, 11, 13, 77, 91, 143. Note that 1 and 1001 are trivial factors. `maxDistance(1001)` would return 136 because the largest distance between any two non-trivial factors is 136 ($143 - 7 = 136$). As another example, `maxDistance(8)` would return 2 because the non-trivial factors of 8 are 2 and 4 and the largest distance between any two non-trivial factors is 2 ($4 - 2 = 2$). Also, `maxDistance(7)` would return -1 since 7 has no non-trivial factors. Further, `maxDistance(49)` would return 0 since 49 has only one nontrivial factor 7. Hence `maxDistance(49)` is 0 ($7 - 7 = 0$).

The function signature is

```
int maxDistance(int n)
```

July 16, 2016

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. A **Meera number** is a number such that the number of nontrivial factors is a factor of the number. For example, 6 is a Meera number because 6 has two nontrivial factors : 2 and 3. (A nontrivial factor is a factor other than 1 and the number). Thus 6 has two nontrivial factors. Now, 2 is a factor of 6. Thus the number of nontrivial factors is a factor of 6. Hence 6 is a Meera number. Another Meera number is 30 because 30 has 2, 3, 5, 6, 10, 15 as nontrivial factors. Thus 30 has 6 nontrivial factors. Note that 6 is a factor of 30. So 30 is a Meera Number. However 21 is **not** a Meera number. The nontrivial factors of 21 are 3 and 7. Thus the number of nontrivial factors is 2. Note that 2 is not a factor of 21. Therefore, 21 is not a Meera number.

Write a function named *isMeera* that returns 1 if its integer argument is a Meera number, otherwise it returns 0.

The signature of the function is

```
int isMeera(int n)
```

2. A **Bunker array** is an array that contains the value 1 if and only if it contains a prime number. The array {7, 6, 10, 1} is a Bunker array because it contains a prime number (7) and also contains a 1. The array {7, 6, 10} is **not** a Bunker array because it contains a prime number (7) but does not contain a 1. The array {6, 10, 1} is **not** a Bunker array because it contains a 1 but does not contain a prime number.

It is okay if a Bunker array contains more than one value 1 and more than one prime, so the array {3, 7, 1, 8, 1} is a Bunker array (3 and 7 are the primes).

Write a function named *isBunker* that returns 1 if its array argument is a Bunker array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

```
int isBunker(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBunker(int a[ ], int len) where len is the number of elements in the array.
```

3. A **Nice array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Nice array because

$$2 = 3 - 1$$

$$10 = 9 + 1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Nice arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Nice array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isNice* that returns 1 if its array argument is a Nice array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

```
int isNice(int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isNice(int a[ ], int len) where len is the number of elements in the array.
```

July 30 2016

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. Write a function named **maxOccurDigit** that returns the digit that occur the most. If there is no such digit, it will return -1. For example **maxOccurDigit**(327277) would return 7 because 7 occurs three times in the number and all other digits occur less than three times. Other examples:

maxOccurDigit(33331) returns 3

maxOccurDigit(3232, 6) returns -1

maxOccurDigit(5) returns 5

maxOccurDigit(-9895) returns 9

The function signature is

maxOccurDigit(int n)

2. A *Bunker array* is defined to be an array in which **at least one** odd number is immediately followed by its square. So {4, 9, 6, 7, 49} is a Bunker array because the odd number 7 is immediately followed by 49. But {2, 4, 9, 3, 15, 21} is not a Bunker array because none of the odd numbers are immediately followed by its square.

Write a function named **isBunkerArray** that returns 1 if its array argument is a Bunker array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isBunkerArray(int [] a)

If you are programming in C or C++, the function signature is

int isBunkerArray(int a[], int len) where len is the number of elements in the array.

3. A *Meera array* is defined to be an array such that for all values n in the array, the value $-n$ is not in the array. So $\{3, 5, -2\}$ is a Meera array. But $\{8, 3, -8\}$ is not a Meera array because for $n=8$, $-n = -8$ is in the array.

Write a function named **isMeera** that returns 1 if its array argument is a Meera array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

`int isMeera(int [] a)`

If you are programming in C or C++, the function signature is

`int isMeera(int a[], int len)` where *len* is the number of elements in the array.

Aug 20, 2016

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. An integer array is said to be *evenSpaced*, if the difference between the largest value and the smallest value is an even number. Write a function *isEvenSpaced(int[] a)* that will return 1 if it is *evenSpaced* and 0 otherwise. If array has less than two elements, function will return 0. If you are programming in C or C++, the function signature is:

`int isEvenSpaced (int a[], int len)` where *len* is the number of elements in the array.

Examples

Array	Largest value	Smallest value	Difference	Return value
{100, 19, 131, 140}	140	19	$140 - 19 = 121$	0
{200, 1, 151, 160}	200	1	$200 - 1 = 199$	0
{200, 10, 151, 160}	200	10	$200 - 10 = 190$	1
{100, 19, -131, -140}	100	-140	$100 - (-140) = 240$	1
{80, -56, 11, -81}	80	-81	$-80 - 80 = -161$	0

2. An *Sub array* is defined to be an array in which each element is greater than sum of all elements **after** that. See examples below:

{13, 6, 3, 2} is a *Sub array*. Note that $13 > 2 + 3 + 6$, $6 > 3 + 2$, $3 > 2$.

{11, 5, 3, 2} is a NOT a *Sub array*. Note that 5 is not greater than $3 + 2$.

Write a function named *isSub* that returns 1 if its array argument is a *Sub array*, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

`int isSub (int [] a)`

If you are programming in C or C++, the function signature is:

`int isSub (int a[], int len)` where *len* is the number of elements in the array.

3. An *isSym* (even/odd Symmetric) *array* is defined to be an array in which even numbers and odd numbers appear in the same order from “*both directions*”. You can assume array has at least one element. See examples below:

{2, 7, 9, 10, 11, 5, 8} is a *isSym* array.

Note that from left to right or right to left we have even, odd, odd, even, odd, odd, even.

{9, 8, 7, 13, 14, 17} is a *isSym* array.

Note that from left to right or right to left we have {odd, even, odd, odd, even, odd}.

However, {2, 7, 8, 9, 11, 13, 10} is not a *isSym* array.

From left to right we have {even, odd, even, odd, odd, odd, even}.

From right to left we have {even, odd, odd, odd, even, odd, even},

which is not the same.

Write a function named *isSym* that returns 1 if its array argument is a *isSym* array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

int *isSym* (int [] a)

If you are programming in C or C++, the function signature is:

int *isSym* (int a[], int len) where *len* is the number of elements in the array.

Sept 3rd 2016

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures

including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. Write a function named **factorTwoCount** that returns the number of times that 2 divides the argument.

For example, `factorTwoCount(48)` returns 4 because

$$48/2 = 24$$

$$24/2 = 12$$

$$12/2 = 6$$

$$6/2 = 3$$

2 does not divide 3 evenly.

Another example: `factorTwoCount(27)` returns 0 because 2 does not divide 27.

The function signature is

```
int factorTwoCount(int n);
```

2. A **Meera array** is defined to be an array that contains at least one odd number and begins and ends with the same number of even numbers.

So {**4, 8, 6**, 3, 2, 9, 8, 11, 8, 13, **12, 12, 6**} is a Meera array because it begins with three even numbers and ends with three even numbers and it contains at least one odd number

The array {2, 4, 6, 8, 6} is not a Meera array because it does not contain an odd number.

The array {**2**, **8**, 7, **10**, **-4**, **6**} is not a Meera array because it begins with two even numbers but ends with three even numbers.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array. Otherwise, it returns 0.

If you are writing in Java or C#, the function signature is

```
int isMeera (int[ ] a)
```

If you are writing in C or C++, the function signature is

```
int isMeera (int a[ ], int len) where len is the number of elements in the array.
```

3. Write a function called **goodSpread** that returns 1 if no value in its array argument occurs more than 3 times in the array.

For example, `goodSpread(new int[] {2, 1, 2, 5, 2, 1, 5, 9})` returns 1 because no value occurs more than three times.

But `goodSpread(new int[] {3, 1, 3, 1, 3, 5, 5, 3})` returns 0 because the value 3 occurs four times.

If you are writing in Java or C#, the function signature is

```
int goodSpread (int[ ] a)
```

If you are writing in C or C++, the function signature is

```
int goodSpread (int a[ ], int len) where len is the number of elements in the array.
```

September 17, 2016

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. A **Fibonacci number** is a number in the sequence 1, 1, 2, 3, 5, 8, 13, 21,.... Note that first two Fibonacci numbers are 1 and any Fibonacci number other than the first two is the sum of the previous two Fibonacci numbers. For example, $2 = 1 + 1$, $3 = 2 + 1$, $5 = 3 + 2$ and so on.

Write a function named *isFibonacci* that returns 1 if its integer argument is a Fibonacci number, otherwise it returns 0.

The signature of the function is

int isFibonacci (int n)

2. A **Meera array** is an array that contains the value 0 if and only if it contains a prime number. The array {7, 6, 0, 10, 1} is a Meera array because it contains a prime number (7) and also contains a 0. The array {6, 10, 1} is a Meera array because it contains no prime number and also contains no 0.

The array {7, 6, 10} is **not** a Meera array because it contains a prime number (7) but does not contain a 0. The array {6, 10, 0} is **not** a Meera array because it contains a 0 but does not contain a prime number.

It is okay if a Meera array contains more than one value 0 and more than one prime, so the array {3, 7, 0, 8, 0, 5} is a Meera array (3, 5 and 7 are the primes and there are two zeros.).

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

int isMeera(int [] a)

If you are programming in C or C++, the function signature is

int isMeera(int a[], int len) where *len* is the number of elements in the array.

3. A **Bean array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Bean array because

$$2 = 3-1$$

$$10 = 9+1$$

$$3 = 2 + 1$$

$$9 = 10 -1$$

Other Bean arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Bean array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isBean* that returns 1 if its array argument is a *Bean* array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

int isBean(int[] a)

If you are programming in C or C++, the function signature is

int isBean(int a[], int len) where *len* is the number of elements in the array.

October 1st, 2016

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not write main method. If you write, you are just wasting your time! Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. A **fancy number** is a number in the sequence 1, 1, 5, 17, 61,Note that first two fancy numbers are 1 and any fancy number other than the first two is sum of the three times previous one and two times the one before that. See below:

1,

1,

$$3*1 + 2*1 = 5$$

$$3*5 + 2*1 = 17$$

$$3*17 + 2*5 = 61$$

Write a function named *isFancy* that returns 1 if its integer argument is a Fancy number, otherwise it returns 0.

The signature of the function is

int isFancy(int n)

2. A **Meera array** is an array that contains the value 1 if and only if it contains 9. The array {7, 9, 0, 10, 1} is a Meera array because it contains 1 and 9. The array {6, 10, 8} is a Meera array because it contains no 1 and also contains no 9.

The array {7, 6, 1} is **not** a Meera array because it contains 1 but does not contain a 9. The array {9, 10, 0} is **not** a Meera array because it contains a 9 but does not contain 1.

It is okay if a Meera array contains more than one value 1 and more than one 9, so the array {1, 1, 0, 8, 0, 9, 9, 1} is a Meera array.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array and returns 0 otherwise.

If you are programming in Java or C#, the function signature is

int isMeera(int [] a)

If you are programming in C or C++, the function signature is

int isMeera(int a[], int len) where *len* is the number of elements in the array.

3. A **Bean array** is defined to be an integer array where for every value n in the array, there is also an element $2n$, $2n+1$ or $n/2$ in the array.

For example, {4, 9, 8} is a Bean array because

For 4, 8 is present; for 9, 4 is present; for 8, 4 is present.

Other Bean arrays include {2, 2, 5, 11, 23}, {7, 7, 3, 6} and {0}.

The array {3, 8, 4} is **not** a Bean array because of the value 3 which requires that the array contains either the value 6, 7 or 1 and none of these values are in the array.

Write a function named *isBean* that returns 1 if its array argument is a *Bean* array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

int isBean(int[] a)

If you are programming in C or C++, the function signature is

int isBean(int a[], int len) where *len* is the number of elements in the array.

October 29th, 2016

There are three questions on this test. Please do your own work. All you need to write is three functions. Please do not use any String functions. No sorting allowed. No additional arrays or data structures allowed. Try to write a simple, elegant and correct code. If you are not a Java or C# programmer, you can assume one more argument *int len*, to pass the length of the array.

Question 1. Write a function *fill* with signature

`int[] fill(int[] arr, int k, int n)`

which does the following: It returns an integer array *arr2* of length *n* whose first *k* elements are the same as the first *k* elements of *arr*, and whose remaining elements consist of repeating blocks of the first *k* elements. You can assume array *arr* has at least *k* elements. The function should return null if either *k* or *n* is not positive.

Examples: `fill({1,2,3,5, 9, 12,-2,-1}, 3, 10)` returns `{1,2,3,1,2,3,1,2,3,1}`. `fill({4, 2, -3, 12}, 1, 5)` returns `{4, 4, 4, 4, 4}`. `fill({2, 6, 9, 0, -3}, 0, 4)` returns null.

Question 2. An *Super array* is defined to be an array in which each element is greater than sum of all elements before that. See examples below:

`{2, 3, 6, 13}` is a *Super array*. Note that $2 < 3$, $2+3 < 6$, $2 + 3 + 6 < 13$.

`{2, 3, 5, 11}` is a NOT a *Super array*. Note that $2 + 3$ not less than 5.

Write a function named *isSuper* that returns 1 if its array argument is a *isSuper* array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

`int isSuper (int [] a)`

If you are programming in C or C++, the function signature is:

`int isSuper (int a[], int len)` where *len* is the number of elements in the array.

Question 3. An array is said to be hollow if it contains 3 or more zeros in the middle that are preceded and followed by the same number of non-zero elements. Write a function named `isHollow` that accepts an integer array and returns 1 if it is a hollow array, otherwise it returns 0. The function signature is

`int isHollow(int[] a).`

Examples: `isHollow({ 1,2,4,0,0,3,4,5})` returns true. `isHollow ({ 1,2,0,0,0,3,4,5})` returns false. : `isHollow ({ 1,2,4,9, 0,0,0,3,4, 5})` returns false. `isHollow ({ 1,2, 0,0, 3,4})` returns false.

Nov 26th

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. An integer is defined to be an **even subset** of another integer n if every even factor of m is also a factor of n . For example 18 is an even subset of 12 because the even factors of 18 are 2 and 6 and these are both factors of 12. But 18 is not an even subset of 32 because 6 is not a factor of 32.

Write a function with signature **`int isEvenSubset(int m, int n)`** that returns 1 if m is an even subset of n , otherwise it returns 0.

2. A **twinoid** is defined to be an array that has exactly two even values that are adjacent to one another. For example `{ 3, 3, 2, 6, 7 }` is a twinoid array because it has exactly two even values (2 and 6) and they are adjacent to one another. The following arrays are not twinoid arrays.

`{ 3, 3, 2, 6, 6, 7 }` because it has three even values.

{3, 3, 2, 7, 6, 7} because the even values are not adjacent to one another

{3, 8, 5, 7, 3} because it has only one even value.

Write a function named **isTwinoid** that returns 1 if its array argument is a twinoid array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isTwinoid (int [] a);

If you are programming in C or C++, the function signature is

int isTwinoid(int a[], int len) where len is the number of elements in the array.

3. A **balanced** array is defined to be an array where for every value n in the array, -n also is in the array. For example {-2, 3, 2, -3} is a balanced array. So is {-2, 2, 2, 2}. But {-5, 2, -2} is not because 5 is not in the array.

Write a function named isBalanced that returns 1 if its array argument is a balanced array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isBalanced (int [] a);

If you are programming in C or C++, the function signature is

int isBalanced(int a[], int len) where len is the number of elements in the array.

Dec 10th 2016

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. Write a function named **countDigit** that returns the number of times that a given digit appears in a positive number. For example countDigit(32121, 1) would return 2 because there are two 1s in 32121. Other examples:

countDigit(33331, 3) returns 4

countDigit(33331, 6) returns 0

countDigit(3, 3) returns 1

The function should return -1 if either argument is negative, so

countDigit(-543, 3) returns -1.

The function signature is

```
int countDigit(int n, int digit)
```

Hint: Use modulo base 10 and integer arithmetic to isolate the digits of the number.

2. A *Bunker array* is defined to be an array in which **at least one** odd number is immediately followed by a prime number. So {4, 9, 6, 7, 3} is a Bunker array because the odd number 7 is immediately followed by the prime number 3. But {4, 9, 6, 15, 21} is not a Bunker array because none of the odd numbers are immediately followed by a prime number.

Write a function named **isBunkerArray** that returns 1 if its array argument is a Bunker array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isBunkerArray(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBunkerArray(int a[ ], int len) where len is the number of elements in the array.
```

You may assume that there exists a function isPrime that returns 1 if its argument is a prime, otherwise it returns 0. **You do not have to write this function.**

3. A *Meera array* is defined to be an array such that for all values n in the array, the value $2*n$ is not in the array. So {3, 5, -2} is a Meera array because $3*2$, $5*2$ and $-2*2$ are not in the array. But {8, 3, 4} is not a Meera array because for $n=4$, $2*n=8$ is in the array.

Write a function named **isMeera** that returns 1 if its array argument is a Meera array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isMeera(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isMeera(int a[ ], int len) where len is the number of elements in the array.
```

Jan 7th 2017

There are 3 questions on this test. You have 2 hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string functions. No sorting allowed. No additional arrays allowed. Try to write a simple, elegant and correct code.

1. Write a function named **minPrimeDistance** that returns the smallest distance between two prime factors of a number. For example, consider 13013. Its prime factors are 1, 7, 11, 13 and 13013. **minPrimeDistance**(13013) would return 2 because the smallest distance between any two prime factors is 2 ($13 - 11 = 2$). As another example, **minPrimeDistance**(8) would return 1 because the prime factors of 8 are 1, 2 and the smallest distance between any two factors is 1 ($2 - 1 = 1$). Note: Consider 1 as a prime number.

The function signature is

int **minPrimeDistance**(int n)

2. A **wave array** is defined to an array which does **not** contain two even numbers or two odd numbers in adjacent locations. So {7, 2, 9, 10, 5}, {4, 11, 12, 1, 6}, {1, 0, 5} and {2} are all **wave arrays**. But {2, 6, 3, 4} is not a wave array because the even numbers 2 and 6 are adjacent to each other.

Write a function named *isWave* that returns 1 if its array argument is a Wave array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

int isWave (int [] a)

If you are programming in C or C++, the function signature is

int isWave (int a[], int len) where len is the number of elements in the array.

3. An array is defined to be a **Bean array** if it meets the following conditions

- a. If it contains a 9 then it also contains a 13.
- b. If it contains a 7 then it does **not** contain a 16.

So {1, 2, 3, **9**, 6, **13**} and {3, 4, 6, **7**, 13, 15}, {1, 2, 3, 4, 10, 11, 12} and {3, 6, 9, 5, 7, 13, 6, 17} are Beanarrays. The following arrays are **not** Bean arrays:

- a. { 9, 6, 18} (contains a 9 but no 13)
- b. {4, 7, 16} (contains both a 7 and a 16)

Write a function named *isBean* that returns 1 if its array argument is a Bean array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isBean (int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBean (int a[ ], int len) where len is the number of elements in the array.
```

Jan 28th, 2017

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. A **Meera number** is a number such that the number of nontrivial factors is a factor of the number. For example, 6 is a Meera number because 6 has two nontrivial factors : 2 and 3. (A nontrivial factor is a factor other than 1 and the number). Thus 6 has two nontrivial factors. Now, 2 is a factor of 6. Thus the number of nontrivial factors is a factor of 6. Hence 6 is a Meera number. Another Meera number is 30 because 30 has 2, 3, 5, 6, 10, 15 as nontrivial factors. Thus 30 has 6 nontrivial factors. Note that 6 is a factor of 30. So 30 is a Meera Number. However 21 is **not** a Meera number. The nontrivial factors of 21 are 3 and 7. Thus the number of nontrivial factors is 2. Note that 2 is not a factor of 21. Therefore, 21 is not a Meera number.

Write a function named *isMeera* that returns 1 if its integer argument is a Meera number, otherwise it returns 0.

The signature of the function is

```
int isMeera(int n)
```

2. A **Bunker array** is an array that contains the value 1 if and only if it contains a prime number. The array {7, 6, 10, 1} is a Bunker array because it contains a prime number (7) and also contains a 1. The array {7, 6, 10} is **not** a Bunker array because it contains a prime number (7) but does not contain a 1. The array {6, 10, 1} is **not** a Bunker array because it contains a 1 but does not contain a prime number.

It is okay if a Bunker array contains more than one value 1 and more than one prime, so the array {3, 7, 1, 8, 1} is a Bunker array (3 and 7 are the primes).

Write a function named *isBunker* that returns 1 if its array argument is a Bunker array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

```
int isBunker(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBunker(int a[ ], int len) where len is the number of elements in the array.
```

3. A **Nice array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Nice array because

$$2 = 3 - 1$$

$$10 = 9 + 1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Nice arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Nice array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isNice* that returns 1 if its array argument is a Nice array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

```
int isNice(int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isNice(int a[ ], int len) where len is the number of elements in the array.
```

25th Feb 2017

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. Given a positive integer k , another positive integer n is said to have k -small factors if n can be written as a product $u \cdot v$ where u and v are both less than k . For instance, 20 has 10-small factors since both 4 and 5 are less than 10 and $4 \cdot 5 = 20$. (For the same reason, it is also true to say that 20 has 6-small factors, 7-small factors, 8-small factors, etc). However, 22 does not have 10-small factors since the only way to factor 22 is as $22 = 2 \cdot 11$, and 11 is not less than 10.

Write a function *hasKSmallFactors* with signature

boolean hasKSmallFactors(int k, int n)

which returns true if n has k -small factors. The function should return false if either k or n is not positive.

Examples:

hasKSmallFactors(7, 30) is true (since $5 \cdot 6 = 30$ and $5 < 7$, $6 < 7$).

hasKSmallFactors(6, 14) is false (since the only way to factor 14 is $2 \cdot 7 = 14$ and 7 not less than 6)

hasKSmallFactors(6, 30) is false (since $5 \cdot 6 = 30$, 6 not less than 6; $3 \cdot 10 = 30$, 10 not less than 6; $2 \cdot 15 = 30$, 15 not less than 6)

2. Write a function *fill* with signature

int[] fill(int[] arr, int k, int n)

which does the following: It returns an integer array *arr2* of length n whose first k elements are the same as the first k elements of *arr*, and whose remaining elements consist of repeating blocks of the first k elements. You can assume array *arr* has at least k elements. The function should return null if either k or n is not positive.

Examples:

`fill({1,2,3,5, 9, 12,-2,-1}, 3, 10)` returns `{1,2,3,1,2,3,1,2,3,1}`.

`fill({4, 2, -3, 12}, 1, 5)` returns `{4, 4, 4, 4, 4}`.

`fill({2, 6, 9, 0, -3}, 0, 4)` returns `null`.

3. An array is said to be **hollow** if it contains 3 or more zeroes in the middle that are preceded and followed by the same number of non-zero elements. Write a function named *isHollow* that accepts an integer array and returns 1 if it is a hollow array, otherwise it returns 0

Examples: `isHollow({1,2,4,0,0,0,3,4,5})` returns 1. `isHollow ({1,2,0,0,0,3,4,5})` returns 0. `isHollow ({1,2,4,9, 0,0,0,3,4, 5})` returns 0. `isHollow ({1,2, 0,0, 3,4})` returns 0.

If you are programming in Java or C#, the function signature is

int isHollow(int[] a).

If you are C or C++ programmer

int isHollow(int[] a, int len)

where *len* is the number of elements in the array.

March 25th 2017

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa. You are not allowed to use any additional data structures.

1. A **Meera number** is a number such that the number of nontrivial factors is a factor of the number. For example, 6 is a Meera number because 6 has two nontrivial factors : 2 and 3. (A nontrivial factor is a factor other than 1 and the number). Thus 6 has two nontrivial factors. Now, 2 is a factor of 6. Thus the number of nontrivial factors is a factor of 6. Hence 6 is a Meera number. Another Meera number is 30 because 30 has 2, 3, 5, 6, 10, 15 as nontrivial factors. Thus 30 has 6 nontrivial factors. Note that 6 is a factor of 30. So 30 is a Meera Number. However 21 is **not** a Meera number. The nontrivial factors of 21 are 3 and 7. Thus the number of nontrivial factors is 2. Note that 2 is not a factor of 21. Therefore, 21 is not a Meera number.

Write a function named *isMeera* that returns 1 if its integer argument is a Meera number, otherwise it returns 0.

The signature of the function is

```
int isMeera(int n)
```

2. A **Bunker array** is an array that contains the value 1 if and only if it contains a prime number. The array {7, 6, 10, 1} is a Bunker array because it contains a prime number (7) and also contains a 1. The array {7, 6, 10} is **not** a Bunker array because it contains a prime number (7) but does not contain a 1. The array {6, 10, 1} is **not** a Bunker array because it contains a 1 but does not contain a prime number.

It is okay if a Bunker array contains more than one value 1 and more than one prime, so the array {3, 7, 1, 8, 1} is a Bunker array (3 and 7 are the primes).

Write a function named *isBunker* that returns 1 if its array argument is a Bunker array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

```
int isBunker(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBunker(int a[ ], int len) where len is the number of elements in the array.
```

3. A **Nice array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Nice array because

$$2 = 3 - 1$$

$$10 = 9 + 1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Nice arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Nice array because of the value 7 which requires that the array contains either the value 6 ($7-1$) or 8 ($7+1$) but neither of these values are in the array.

Write a function named *isNice* that returns 1 if its array argument is a Nice array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

```
int isNice(int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isNice(int a[ ], int len) where len is the number of elements in the array.
```

April 29, 2017

There are 3 questions on this test. Please do your own work. All you need to write is three functions. Please do not use any String functions. No sorting allowed. No additional arrays or data structures allowed. Try to write a simple, elegant and correct code.

1. Write a function named **minDistance** that returns the smallest distance between two factors of a number. For example, consider $1001 = 1 \cdot 7 \cdot 11 \cdot 13$. Its factors are 1, 7, 11, 13, 77, 91, 143 and 1001. **minDistance**(1001) would return 2 because the smallest distance between any two factors is 2 ($13 - 11 = 2$). As another example, **minDistance**(8) would return 1 because the factors of 8 are 1, 2, 4, 8 and the smallest distance between any two factors is 1 ($2 - 1 = 1$). Also, **minDistance**(15) would return 2 since the factors of 15 are 1, 3, 5, 15 and the smallest distance between any two factors is 2 ($5 - 3 = 2$).

The function signature is

```
int minDistance(int n)
```

2. A **wave array** is defined to an array which does **not** contain two even numbers or two odd numbers in adjacent locations. So {7, 2, 9, 10, 5}, {4, 11, 12, 1, 6}, {1, 0, 5} and {2} are all **wave arrays**. But {2, 6, 3, 4} is not a wave array because the even numbers 2 and 6 are adjacent to each other. Also {3, 4, 9, 11, 8} is not a wave array because the odd numbers 9 and 11 are adjacent to each other. You can assume array has at least one element.

Write a function named *isWave* that returns 1 if its array argument is a Wave array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isWave (int [ ] a)
```

If you are programming in C or C++, the function signature is

`int isWave (int a[], int len)` where len is the number of elements in the array.

3. An array is defined to be a **Bean array** if it meets the following conditions

- a. If it contains a 9 then it also contains a 13.
- b. If it contains a 7 then it does **not** contain a 16.

`{1, 2, 3, 9, 6, 13}` // 9, 13 present. 7 not present. So 16 may or may not appear. Bean array.

`{3, 4, 6, 7, 13, 15}` // 9 not present. So 13 may or may not appear. 7 present, 16 not present. Bean array.

`{1, 2, 3, 4, 10, 11, 12}` // 9 not present. So 13 may or may not appear. 7 not present. So 16 may or may not appear. Bean array.

`{3, 6, 5, 16, 13, 6, 17}` // 9 not present. So 13 may or may not appear. 7 not present. So 16 may or may not appear. Bean array.

`{ 9, 6, 18}` // contains a 9 but no 13. Not a Bean array.

`{4, 7, 16}` // contains both a 7 and a 16. Not a Bean array.

Write a function named `isBean` that returns 1 if its array argument is a Bean array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

`int isBean (int[] a)`

If you are programming in C or C++, the function signature is

`int isBean (int a[], int len)` where len is the number of elements in the array.

May 27th 2017

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. An integer array is said to be *evenSpaced*, if the difference between the largest value and the smallest value is an even number. Write a function *isEvenSpaced(int[] a)* that will return 1 if it is *evenSpaced* and 0 otherwise. If array has less than two elements, function will return 0. If you are programming in C or C++, the function signature is:

int *isEvenSpaced* (int a[], int len) where *len* is the number of elements in the array.

Examples

Array	Largest value	Smallest value	Difference	Return value
{100, 19, 131, 140}	140	19	$140 - 19 = 121$	0
{200, 1, 151, 160}	200	1	$200 - 1 = 199$	0
{200, 10, 151, 160}	200	10	$200 - 10 = 190$	1
{100, 19, -131, -140}	100	-140	$100 - (-140) = 240$	1
{80, -56, 11, -81}	80	-81	$-80 - 80 = -161$	0

2. An *Sub array* is defined to be an array in which each element is greater than sum of all elements **after** that. See examples below:

{13, 6, 3, 2} is a *Sub array*. Note that $13 > 2 + 3 + 6$, $6 > 3 + 2$, $3 > 2$.

{11, 5, 3, 2} is a NOT a *Sub array*. Note that 5 is not greater than $3 + 2$.

Write a function named *isSub* that returns 1 if its array argument is a *Sub* array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

int *isSub* (int [] a)

If you are programming in C or C++, the function signature is:

int *isSub* (int a[], int len) where *len* is the number of elements in the array.

3. An *isSym* (even/odd Symmetric) *array* is defined to be an array in which even numbers and odd numbers appear in the same order from “*both directions*”. You can assume array has at least one element. See examples below:

{2, 7, 9, 10, 11, 5, 8} is a *isSym* array.

Note that from left to right or right to left we have even, odd, odd, even, odd, odd, even.

{9, 8, 7, 13, 14, 17} is a *isSym* array.

Note that from left to right or right to left we have {odd, even, odd, odd, even, odd}.

However, {2, 7, 8, 9, 11, 13, 10} is not a *isSym* array.

From left to right we have {even, odd, even, odd, odd, odd, even}.

From right to left we have {even, odd, odd, odd, even, odd, even},

which is not the same.

Write a function named *isSym* that returns 1 if its array argument is a *isSym* array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

```
int isSym (int [ ] a)
```

If you are programming in C or C++, the function signature is:

```
int isSym (int a[ ], int len) where len is the number of elements in the array.
```

June 24 2017

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. A **Meera number** is a number such that the number of nontrivial factors is a factor of the number. For example, 6 is a Meera number because 6 has two nontrivial factors : 2 and 3. (A nontrivial factor is a factor other than 1 and the number). Thus 6 has two nontrivial factors. Now, 2 is a factor of 6. Thus the number of nontrivial factors is a factor of 6. Hence 6 is a Meera number. Another Meera number is 30 because 30 has 2, 3, 5, 6, 10, 15 as nontrivial factors. Thus 30 has 6 nontrivial factors. Note that 6 is a factor of 30. So 30 is a Meera Number. However 21 is **not** a Meera number. The nontrivial factors of 21 are 3 and 7. Thus the number of nontrivial factors is 2. Note that 2 is not a factor of 21. Therefore, 21 is not a Meera number.

Write a function named *isMeera* that returns 1 if its integer argument is a Meera number, otherwise it returns 0.

The signature of the function is

```
int isMeera(int n)
```

2. A **Bunker array** is an array that contains the value 1 if and only if it contains a prime number. The array {7, 6, 10, 1} is a Bunker array because it contains a prime number (7) and also contains a 1. The array {7, 6, 10} is **not** a Bunker array because it contains a prime number (7) but does not contain a 1. The array {6, 10, 1} is **not** a Bunker array because it contains a 1 but does not contain a prime number.

It is okay if a Bunker array contains more than one value 1 and more than one prime, so the array {3, 7, 1, 8, 1} is a Bunker array (3 and 7 are the primes).

Write a function named *isBunker* that returns 1 if its array argument is a Bunker array and returns 0 otherwise.

You may assume the existence of a function named *isPrime* that returns 1 if its argument is a prime and returns 0 otherwise. You do not have to write *isPrime*, you can just call it.

If you are programming in Java or C#, the function signature is

```
int isBunker(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBunker(int a[ ], int len) where len is the number of elements in the array.
```

3. A **Nice array** is defined to be an array where for every value n in the array, there is also an element $n-1$ or $n+1$ in the array.

For example, {2, 10, 9, 3} is a Nice array because

$$2 = 3 - 1$$

$$10 = 9 + 1$$

$$3 = 2 + 1$$

$$9 = 10 - 1$$

Other Nice arrays include {2, 2, 3, 3, 3}, {1, 1, 1, 2, 1, 1} and {0, -1, 1}.

The array {3, 4, 5, 7} is **not** a Nice array because of the value 7 which requires that the array contains either the value 6 (7-1) or 8 (7+1) but neither of these values are in the array.

Write a function named *isNice* that returns 1 if its array argument is a Nice array. Otherwise it returns a 0.

If you are programming in Java or C#, the function signature is

```
int isNice(int[ ] a)
```

If you are programming in C or C++, the function signature is

```
int isNice(int a[ ], int len) where len is the number of elements in the array.
```

29th July 2017

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. Write a function named **factorTwoCount** that returns the number of times that 2 divides the argument.

For example, `factorTwoCount(48)` returns 4 because

$$48/2 = 24$$

$$24/2 = 12$$

$$12/2 = 6$$

$$6/2 = 3$$

2 does not divide 3 evenly.

Another example: `factorTwoCount(27)` returns 0 because 2 does not divide 27.

The function signature is

```
int factorTwoCount(int n);
```

2. A **Meera array** is defined to be an array that contains at least one odd number and begins and ends with the same number of even numbers.

So **{4, 8, 6, 3, 2, 9, 8, 11, 8, 13, 12, 12, 6}** is a Meera array because it begins with three even numbers and ends with three even numbers and it contains at least one odd number

The array **{2, 4, 6, 8, 6}** is not a Meera array because it does not contain an odd number.

The array **{2, 8, 7, 10, -4, 6}** is not a Meera array because it begins with two even numbers but ends with three even numbers.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array. Otherwise, it returns 0.

If you are writing in Java or C#, the function signature is

```
int isMeera (int[ ] a)
```

If you are writing in C or C++, the function signature is

```
int isMeera (int a[ ], int len) where len is the number of elements in the array.
```

3. Write a function called **goodSpread** that returns 1 if no value in its array argument occurs more than 3 times in the array.

For example, `goodSpread(new int[] {2, 1, 2, 5, 2, 1, 5, 9})` returns 1 because no value occurs more than three times.

But `goodSpread(new int[] {3, 1, 3, 1, 3, 5, 5, 3})` returns 0 because the value 3 occurs four times.

If you are writing in Java or C#, the function signature is

```
int goodSpread (int[ ] a)
```

If you are writing in C or C++, the function signature is

```
int goodSpread (int a[ ], int len) where len is the number of elements in the array.
```

26th August 2017

There are three questions on this test. Please do your own work. All you need to write is three functions. Please do not use any String functions. No sorting allowed. No additional arrays or data structures allowed. Try to write a simple, elegant and correct code. If you are not a Java or C# programmer, you can assume one more argument *int len*, to pass the length of the array.

Question 1. Write a function fill with signature

`int[] fill(int[] arr, int k, int n)`

which does the following: It returns an integer array arr2 of length n whose first k elements are the same as the first k elements of arr, and whose remaining elements consist of repeating blocks of the first k elements. You can assume array arr has at least k elements. The function should return null if either k or n is not positive.

Examples: `fill({1,2,3,5, 9, 12,-2,-1}, 3, 10)` returns `{1,2,3,1,2,3,1,2,3,1}`. `fill({4, 2, -3, 12}, 1, 5)` returns `{4, 4, 4, 4, 4}`. `fill({2, 6, 9, 0, -3}, 0, 4)` returns null.

Question 2. Write a function sumIsPower with signature

`boolean sumIsPower(int[] arr)`

which outputs true if the sum of the elements in the input array arr is a power of 2, false otherwise. Recall that the powers of 2 are 1, 2, 4, 8, 16, and so on. In general a number is a power of 2 if and only if it is of the form 2^n for some nonnegative integer n. You may assume (without verifying in your code) that all elements in the array are positive integers. If the input array arr is null, the return value should be false.

Examples: `sumIsPower({8,8,8,8})` is true since $8 + 8 + 8 + 8 = 32 = 2^5$. `sumIsPower({8,8,8})` is false, since $8 + 8 + 8 = 24$, not a power of 2.

Question 3. An array is said to be hollow if it contains 3 or more zeros in the middle that are preceded and followed by the same number of non-zero elements. Write a function named `isHollow` that accepts an integer array and returns 1 if it is a hollow array, otherwise it returns 0. The function signature is

`int isHollow(int[] a).`

Examples: `isHollow({1,2,4,0,0,0,3,4,5})` returns true. `isHollow ({1,2,0,0,0,3,4,5})` returns false. : `isHollow ({1,2,4,9, 0,0,0,3,4, 5})` returns false. `isHollow ({1,2, 0,0, 3,4})` returns false.

October 18, 2017

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. Write a function named **factorTwoCount** that returns the number of times that 2 divides the argument.

For example, factorTwoCount(48) returns 4 because

$$48/2 = 24$$

$$24/2 = 12$$

$$12/2 = 6$$

$$6/2 = 3$$

2 does not divide 3 evenly.

Another example: factorTwoCount(27) returns 0 because 2 does not divide 27.

The function signature is

```
int factorTwoCount(int n);
```

2. A **Meera array** is defined to be an array that contains at least one odd number and begins and ends with the same number of even numbers.

So {4, 8, 6, 3, 2, 9, 8, 11, 8, 13, 12, 12, 6} is a Meera array because it begins with three even numbers and ends with three even numbers and it contains at least one odd number

The array {2, 4, 6, 8, 6} is not a Meera array because it does not contain an odd number.

The array {2, 8, 7, 10, -4, 6} is not a Meera array because it begins with two even numbers but ends with three even numbers.

Write a function named *isMeera* that returns 1 if its array argument is a Meera array. Otherwise, it returns 0.

If you are writing in Java or C#, the function signature is

```
int isMeera (int[ ] a)
```

If you are writing in C or C++, the function signature is

```
int isMeera (int a[ ], int len) where len is the number of elements in the array.
```

3. Write a function called **goodSpread** that returns 1 if no value in its array argument occurs more than 3 times in the array.

For example, `goodSpread(new int[] {2, 1, 2, 5, 2, 1, 5, 9})` returns 1 because no value occurs more than three times.

But `goodSpread(new int[] {3, 1, 3, 1, 3, 5, 5, 3})` returns 0 because the value 3 occurs four times.

If you are writing in Java or C#, the function signature is

```
int goodSpread (int[ ] a)
```

If you are writing in C or C++, the function signature is

`int goodSpread (int a[], int len)` where `len` is the number of elements in the array.

Nov 11, 2017 First Group

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. Write a function named **countDigit** that returns the number of times that a given digit appears in a positive number. For example `countDigit(32121, 1)` would return 2 because there are two 1s in 32121. Other examples:

`countDigit(33331, 3)` returns 4

`countDigit(33331, 6)` returns 0

`countDigit(3, 3)` returns 1

The function should return -1 if either argument is negative, so

`countDigit(-543, 3)` returns -1.

The function signature is

`int countDigit(int n, int digit)`

Hint: Use modulo base 10 and integer arithmetic to isolate the digits of the number.

2. A *Bunker array* is defined to be an array in which **at least one** odd number is immediately followed by a prime number. So {4, 9, 6, 7, 3} is a Bunker array because the odd number 7 is immediately followed by the prime number 3. But {4, 9, 6, 15, 21} is not a Bunker array because none of the odd numbers are immediately followed by a prime number.

Write a function named **isBunkerArray** that returns 1 if its array argument is a Bunker array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isBunkerArray(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isBunkerArray(int a[ ], int len) where len is the number of elements in the array.
```

You may assume that there exists a function `isPrime` that returns 1 if its argument is a prime, otherwise it returns 0. **You do not have to write this function.**

3. A *Meera array* is defined to be an array such that for all values n in the array, the value $2*n$ is not in the array. So {3, 5, -2} is a Meera array because $3*2$, $5*2$ and $-2*2$ are not in the array. But {8, 3, 4} is not a Meera array because for $n=4$, $2*n=8$ is in the array.

Write a function named **isMeera** that returns 1 if its array argument is a Meera array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isMeera(int [ ] a)
```

If you are programming in C or C++, the function signature is

```
int isMeera(int a[ ], int len) where len is the number of elements in the array.
```

Do not use any string methods or string operations. No String properties if your program is in C#. No sorting allowed. No additional data structures including arrays allowed. Try to write simple, elegant and correct code. You will be graded both on correctness and efficiency.

1. An integer array is said to be *evenSpaced*, if the difference between the largest value and the smallest value is an even number. Write a function *isEvenSpaced(int[] a)* that will return 1 if it is *evenSpaced* and 0 otherwise. If array has less than two elements, function will return 0. If you are programming in C or C++, the function signature is:

`int isEvenSpaced (int a[], int len)` where *len* is the number of elements in the array.

Examples

Array	Largest value	Smallest value	Difference	Return value
{100, 19, 131, 140}	140	19	$140 - 19 = 121$	0
{200, 1, 151, 160}	200	1	$200 - 1 = 199$	0
{200, 10, 151, 160}	200	10	$200 - 10 = 190$	1
{100, 19, -131, -140}	100	-140	$100 - (-140) = 240$	1
{80, -56, 11, -81}	80	-81	$-80 - 80 = -161$	0

2. A *Sub array* is defined to be an array in which each element is greater than sum of all elements **after** that. See examples below:

{13, 6, 3, 2} is a *Sub array*. Note that $13 > 2 + 3 + 6$, $6 > 3 + 2$, $3 > 2$.

{11, 5, 3, 2} is a NOT a *Sub array*. Note that 5 is not greater than $3 + 2$.

Write a function named *isSub* that returns 1 if its array argument is a *Sub array*, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

```
int isSub (int [ ] a)
```

If you are programming in C or C++, the function signature is:

```
int isSub (int a[ ], int len) where len is the number of elements in the array.
```

3. An *isSym* (even/odd Symmetric) *array* is defined to be an array in which even numbers and odd numbers appear in the same order from “*both directions*”. You can assume array has at least one element. See examples below:

{2, 7, 9, 10, 11, 5, 8} is a *isSym* array.

Note that from left to right or right to left we have even, odd, odd, even, odd, odd, even.

{9, 8, 7, 13, 14, 17} is a *isSym* array.

Note that from left to right or right to left we have {odd, even, odd, odd, even, odd}.

However, {2, 7, 8, 9, 11, 13, 10} is not a *isSym* array.

From left to right we have {even, odd, even, odd, odd, odd, even}.

From right to left we have {even, odd, odd, odd, even, odd, even},

which is not the same.

Write a function named *isSym* that returns 1 if its array argument is a *isSym* array, otherwise it returns 0.

If you are programming in Java or C#, the function signature is:

```
int isSym (int [ ] a)
```

If you are programming in C or C++, the function signature is:

```
int isSym (int a[ ], int len) where len is the number of elements in the array.
```

December 2, 2017

There are three questions on this test. You have two hours to complete it. Please do your own work. You are not allowed to use any methods or functions provided by the system unless explicitly stated in the question. In particular, you are not allowed to convert int to a String or vice-versa.

1. Given a positive integer k , another positive integer n is said to have k -small factors if n can be written as a product $u \cdot v$ where u and v are both less than k . For instance, 20 has 10-small factors since both 4 and 5 are less than 10 and $4 \cdot 5 = 20$. (For the same reason, it is also true to say that 20 has 6-small factors, 7-small factors, 8-small factors, etc). However, 22 does not have 10-small factors since the only way to factor 22 is as $22 = 2 \cdot 11$, and 11 is not less than 10.

Write a function *hasKSmallFactors* with signature

```
boolean hasKSmallFactors(int k, int n)
```

which returns true if n has k -small factors. The function should return false if either k or n is not positive.

Examples:

hasKSmallFactors(7, 30) is true (since $5 \cdot 6 = 30$ and $5 < 7, 6 < 7$).

hasKSmallFactors(6, 14) is false (since the only way to factor 14 is $2 \cdot 7 = 14$ and 7 not less than 6)

hasKSmallFactors(6, 30) is false (since $5 \cdot 6 = 30$, 6 not less than 6; $3 \cdot 10 = 30$, 10 not less than 6; $2 \cdot 15 = 30$, 15 not less than 6)

2. Write a function *fill* with signature

int[] fill(int[] arr, int k, int n)

which does the following: It returns an integer array arr2 of length n whose first k elements are the same as the first k elements of arr, and whose remaining elements consist of repeating blocks of the first k elements. You can assume array arr has at least k elements. The function should return null if either k or n is not positive.

Examples:

fill({1,2,3,5, 9, 12,-2,-1}, 3, 10) returns {1,2,3,1,2,3,1,2,3,1}.

fill({4, 2, -3, 12}, 1, 5) returns {4, 4, 4, 4, 4}.

fill({2, 6, 9, 0, -3}, 0, 4) returns null.

3. An array is said to be **hollow** if it contains 3 or more zeroes in the middle that are preceded and followed by the same number of non-zero elements. Write a function named *isHollow* that accepts an integer array and returns 1 if it is a hollow array, otherwise it returns 0

Examples: isHollow({1,2,4,0,0,0,3,4,5}) returns 1. isHollow ({1,2,0,0,0,3,4,5}) returns 0. isHollow ({1,2,4,9, 0,0,0,3,4, 5}) returns 0. isHollow ({1,2, 0,0, 3,4}) returns 0.

If you are programming in Java or C#, the function signature is

int isHollow(int[] a).

If you are C or C++ programmer

int isHollow(int[] a, int len)

where *len* is the number of elements in the array.

Jan 27, 2018

There are 3 questions on this test. You have two hours to finish it. Please do your own work. All you need to write is three functions. Please do not use any string methods. No sorting allowed. No additional data structures including arrays allowed. Try to write a simple, elegant and correct code.

1. An integer is defined to be an **even subset** of another integer n if every even factor of m is also a factor of n . For example 18 is an even subset of 12 because the even factors of 18 are 2 and 6 and these are both factors of 12. But 18 is not an even subset of 32 because 6 is not a factor of 32.

Write a function with signature **int isEvenSubset(int m, int n)** that returns 1 if m is an even subset of n , otherwise it returns 0.

2. A **twinoid** is defined to be an array that has exactly two even values that are adjacent to one another. For example {3, 3, 2, 6, 7} is a twinoid array because it has exactly two even values (2 and 6) and they are adjacent to one another. The following arrays are not twinoid arrays.

{3, 3, 2, 6, 6, 7} because it has three even values.

{3, 3, 2, 7, 6, 7} because the even values are not adjacent to one another

{3, 8, 5, 7, 3} because it has only one even value.

Write a function named **isTwinoid** that returns 1 if its array argument is a twinoid array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

`int isTwinoid (int [] a);`

If you are programming in C or C++, the function signature is

`int isTwinoid(int a[], int len)` where *len* is the number of elements in the array.

3. A **balanced** array is defined to be an array where for every value n in the array, $-n$ also is in the array. For example $\{-2, 3, 2, -3\}$ is a balanced array. So is $\{-2, 2, 2, 2\}$. But $\{-5, 2, -2\}$ is not because 5 is not in the array.

Write a function named `isBalanced` that returns 1 if its array argument is a balanced array. Otherwise it returns 0.

If you are programming in Java or C#, the function signature is

```
int isBalanced (int [ ] a);
```

If you are programming in C or C++, the function signature is

```
int isBalanced(int a[ ], int len) where len is the number of elements in the array.
```