

Variance in Variants: Propagating Genome Sequence Uncertainty into Downstream Analyses

David Champredon*, Devan Becker*, Connor Chato, Gopi Gugan, Art Poon

*contributed equally

Abstract

Genetic sequencing is subject to many different types of errors, but most analyses treat the resultant sequences as if they are perfect. Since the process of sequencing is very difficult, modern machines rely on significantly larger numbers of reads rather than making each read significantly more accurate. Still, the coverage of such machines is imperfect and leaves uncertainty in many of the base calls. Furthermore, there are circumstances around the sequencing that can induce further problems. In this work, we demonstrate that the uncertainty in sequencing techniques will affect downstream analysis and propose a straightforward (if computationally expensive) method to propagate the uncertainty.

Our method uses a probabilistic matrix representation of individual sequences which incorporates base quality scores and makes various uncertainty propagation methods obvious and easy. With the matrix representation, resampling possible base calls according to quality scores provides a bootstrap- or prior distribution-like first step towards genetic analysis. Analyses based on these re-sampled sequences will include an honest evaluation of the error involved in such analyses.

We demonstrate our resampling method on HIV and SARS-CoV-2 data. The resampling procedure adds computational cost to the analyses, but the large impact on the variance in downstream estimates makes it clear that ignoring this uncertainty leads to invalid conclusions. For HIV data, we show that phylogenetic reconstructions are much more sensitive to sequence error uncertainty than previously believed, and for SARS-CoV-2 data we show that lineage designations via Pangolin are much less certain than the bootstrap support would imply.

TODO (with input from David/Art)

- Ensure I'm using pangolin/pangoLEARN in proper contexts
 - Right now, I'm using them as synonyms (bad?)
- Nomenclature:
 - \mathcal{S} is “nucleotide-level uncertainty sequence” or simply “uncertainty matrix”?

- * “Uncertainty matrix” is a misnomer - the entries are the probability of basis call. Is there a better term?
- * Maybe “Call Probability Matrix”?
- * I realize now that David calls it the “Probabilistic Sequence”.
- Nucleotide “position”, “location”, or “locus”?
- “sequence-level uncertainty sequence” or “genome likelihood”?
- * Genome likelihood is used in other contexts; their formulations are model-based but have the same interpretation.
- Notation:
 - I use subscript j for arbitrary locations on the genome - double check that this is consistent throughout.
- Style:
 - I’m really bad at tense.

1 Introduction

Generating a genetic sequence from a biological sample is a complex process that involves many steps. Nucleic acids must be extracted from the sample while avoiding contamination by foreign material. If working with RNA, then we must use reverse transcription to convert the RNA into DNA. For some next-generation sequencing (NGS) applications, we have to generate a sequencing library by random shearing of nucleic acids into fragments that are ligated onto special ‘adaptors’. NGS procedures such as sequencing by synthesis suffer from greater error rate relative to conventional Sanger dye-terminator sequencing, although these rates have continued to improve with new technologies [REF]. In addition, the short reads produced by NGS platforms need to be aligned — either by alignment against a reference genome, *de novo* assembly, or a combination of the two — to reconstruct the complete sequence using one or more bioinformatic programs. Errors can be introduced any one of these steps [Beerenwinkel and Zagordi, 2011, O’Rawe et al. [2015]].

In some cases, the variation induced by measurement error is directly quantified and encoded into the output. For example, ambiguous base calls from sequence chromatograms are assigned ambiguity codes (*e.g.*, Y for C or T, R for A or G) when the base calling program cannot determine which base is dominant. In 1998, Ewing and Green [1998] and Richterich [1998] both showed that estimates of the base call quality, typically quantified as Phred quality scores ($Q = -10\log_{10}P$, where P is the estimated error probability), can be an accurate estimate of the number of errors that the machines at the time would make. Even though the accuracy of Phred quality scores has been disputed and other methods for quantifying error probabilities have been proposed [Li et al., 2004, DePristo et al. [2011], Li et al. [2009]], Phred scores remain the standard means of reporting the estimated error probabilities for current sequencing platforms.

1 Generally, these scores are used to censor the base calls (*i.e.*, label them “N” rather than A, T, C or G) if the estimated
2 probability of error exceeds a predefined threshold. It is also common practice to remove the sequence from further
3 analysis if the total number of censored bases exceeds a maximum tolerance; *e.g.*, Doronina [2005], Robasky et al.
4 [2014], O’Rawe et al. [2015].

5 Furthermore, some studies have extended the concept of per-base error probabilities to calculate the joint likelihood of
6 partial or full sequences. For example, DePristo et al. [2011] and Gompert and Buerkle [2011] incorporate adjusted
7 Phred scores into a likelihood framework to generate more accurate estimates of population-level allele distributions;
8 this approach has subsequently been used to develop new estimators for population genetic diversity (Fumagalli et al.
9 [2013]). Kuo et al. [2018] use genome likelihoods to perform hypothesis tests that evaluate whether a given genome
10 sequence is consistent with a given alternative sequence after accounting for the errors. As with any parametric
11 model-based approach, genome likelihoods use assumptions about the errors in order to make conclusions about the
12 underlying patterns.

13 Few other authors have considered the uncertainty present in the sequences in downstream analyses. One notable
14 exception is O’Rawe et al. [2015], who suggest methods for propagating sequence-level uncertainty into determining
15 whether two subjects have the same alleles as well as incorporating the sequence-level uncertainty into confidence
16 intervals for allele frequency.

17 Alignment methods are heuristic methods based on similarity scores that generally do not quantify the uncertainty of
18 alignment. Methods to reconstruct phylogenies usually leave out the uncertainty complexity and settle for sequences
19 composed of the most frequent nucleotides and/or ignore ambiguity codes (with some exceptions, *e.g.*, DePristo et al.
20 [2011]). When the phylogenetic tree to infer is based on pathogen sequences infecting hosts, the potential genetic
21 diversity of the infection adds a complexity in phylogeny reconstruction. Typical examples are epidemiological studies
22 reconstructing transmission trees from viral genetic sequences (*e.g.*, HIV, HepC) sampled from infected patients.

23 In our work, we present a simple, general framework that can be incorporated into any analysis of genetic sequence
24 data. This framework involves converting the uncertainty scores into a matrix of probabilities, and repeatedly sampling
25 from this matrix and using the resultant samples in downstream analysis. Unlike likelihood-based approaches, we do
26 not make assumptions about the underlying patterns in the data. In doing so, we gain more accurate estimation of the
27 errors at the expense of computation time. Our technique is amenable to any appropriate quality score adjustments prior
28 to building the uncertainty matrix.

2 Methods

2.1 Probabilistic Representation of Sequences

Here, we describe two theoretical frameworks to model sequence uncertainty at the *nucleotide level* or at the *sequence level*. In both frameworks, the sequence of nucleotides from a biological sample is not treated as a certain observation, but rather as a collection of possible sequences.

2.1.1 Nucleotide-level uncertainty

To represent the uncertainty at each location along the genome, we introduce following matrix:

$$\mathcal{S} = \begin{matrix} & \begin{matrix} 1 & 2 & \dots & \ell \end{matrix} \\ \begin{matrix} \text{A} \\ \text{C} \\ \text{G} \\ \text{T} \\ - \end{matrix} & \begin{pmatrix} \mathcal{S}_{A,1} & \mathcal{S}_{A,2} & \dots & \mathcal{S}_{A,\ell} \\ \mathcal{S}_{C,1} & \mathcal{S}_{C,2} & \dots & \mathcal{S}_{C,\ell} \\ \mathcal{S}_{G,1} & \mathcal{S}_{G,2} & \dots & \mathcal{S}_{G,\ell} \\ \mathcal{S}_{T,1} & \mathcal{S}_{T,2} & \dots & \mathcal{S}_{T,\ell} \\ \mathcal{S}_{x,1} & \mathcal{S}_{x,2} & \dots & \mathcal{S}_{x,\ell} \end{pmatrix} \end{matrix} \quad (1)$$

Each column represents the nucleotide position, each row one of the four nucleotide **A,C,G,T** as well as an empty position “-” that symbolizes a genuine deletion (not caused by missing data). Hence, \mathcal{S} is a $5 \times \ell$ matrix. Its elements represent the probability that a nucleotide is at given position:

$$\mathcal{S}_{\mathbf{n},j} = \mathbb{P}(\text{nucleotide } \mathbf{n} \text{ is at position } j) \quad (2)$$

with the special case for a deletion:

$$\mathcal{S}_{-,j} = \mathbb{P}(\text{empty position } j) \quad (3)$$

Note that we have for all $1 \leq j \leq \ell$:

$$\sum_{n \in \{\text{A}, \text{C}, \text{G}, \text{T}, -\}} \mathcal{S}_{n,j} = 1 \quad (4)$$

Also, the sequence length is stochastic if $\mathcal{S}_{-,i} > 0$ for at least one i . The probability that the sequence has the maximum length ℓ is $\prod_{i=1}^{\ell} (1 - \mathcal{S}_{-,i})$. We call the matrix \mathcal{S} the *nucleotide-level probabilistic sequence* of a biological sample. The nucleotide (or deletion) drawn at each position is independent from all the others, so there are 5^ℓ possible different sequences for a given probabilistic nucleotide sequence, but these sequences are *not* equally probable.

2.1.2 Sequence-level uncertainty

Out of the 5^ℓ possible sequences, the nucleotide uncertainty may assign a positive probability to sequences that are not biologically possible. As an alternative representation and to reduce the space of possible sequences, let's assume we have enough information (either directly observed from data or simulated) to generate a set of sequences $\mathcal{B} = (\mathcal{B}_i)_{i \in \{1 \dots m\}}$ of all m biologically possible sequences. Note that the \mathcal{B}_i do not have necessarily the same length. The observed genetic sequence, s , is a sample from a specified distribution a :

$$\mathbb{P}(s = \mathcal{B}_i) = a(i) \quad (5)$$

We call the set \mathcal{B} the *sequence-level probabilistic sequence*. Note that, because a is a distribution, we must have $\sum_{i=1}^m a(i) = 1$.

If we have the following nucleotide-level probabilistic sequence:

$$\mathcal{S} = \begin{matrix} & 1 & 2 & 3 & 4 & 5 & 6 \\ \begin{matrix} \text{A} \\ \text{C} \\ \text{G} \\ \text{T} \\ - \end{matrix} & \begin{pmatrix} 0.9 & 0.05 & 0.99 & 0 & 0 & 0.6 \\ 0 & 0.8 & 0 & 0 & 0.1 & 0.1 \\ 0.1 & 0.15 & 0 & 0.3 & 0.9 & 0 \\ 0 & 0 & 0.01 & 0.7 & 0 & 0.3 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix} \end{matrix}$$

then there are $2 \times 3 \times 2^3 \times 3 = 144$ possible sequences. The most likely is the one having the highest nucleotides probabilities: **ACATGA** with probability 0.2694 ($0.9 \times 0.8 \times 0.99 \times 0.7 \times 0.9 \times 0.6$).

If there is a positive probability of deletion for at least one position, then the sequence has a variable length. Let's take the same example as above, but adding one possible empty position:

$$\mathcal{S} = \begin{matrix} & 1 & 2 & 3 & 4 & 5 & 6 \\ \begin{matrix} \text{A} \\ \text{C} \\ \text{G} \\ \text{T} \\ - \end{matrix} & \begin{pmatrix} 0.9 & 0.05 & 0.99 & 0 & 0 & 0.6 \\ 0 & 0.8 & 0 & 0 & 0.1 & 0.1 \\ 0.1 & 0.15 & 0 & 0.2 & 0.9 & 0 \\ 0 & 0 & 0.01 & 0.7 & 0 & 0.3 \\ 0 & 0 & 0 & 0.1 & 0 & 0 \end{pmatrix} \end{matrix}$$

Like above, there is still a 0.2694 probability that the sequence is **ACATGA**, but now there is a chance that position 4 is

1 deleted. For example, with probability 0.038 the sequence is **ACA-GA**.

2 Below is an example for a sequence-level probabilistic sequence \mathcal{B} :

sequence	a
ACATGA	0.60
ACATCA	0.12
AGATCA	0.15
ACAGA	0.05
GCATGA	0.08

3 % Sampling from \mathcal{B} , we will have for example **ACATCA** 12% of the time. Large genomes, such as SARS-CoV-2, will
 4 result in vanishingly small probabilities for all sequences, and thus calculations on the log scale are often preferred.

5 2.2 Deletions and Insertions

6 By construction, the nucleotide-level probabilistic sequence must be defined with its longest possible length. Deletions
 7 are naturally modelled with our representation but insertions have to be modelled using deletion probability.

8 Consider the following nucleotide-level probabilistic sequence:

$$\mathcal{S} = \begin{matrix} & 1 & 2 & 3 & 4 & 5 & 6 \\ \begin{matrix} \text{A} \\ \text{C} \\ \text{G} \\ \text{T} \\ - \end{matrix} & \begin{pmatrix} 0 & 0 & 1 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0.99 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0.01 & 0 & 1 \\ 0 & 0.01 & 0 & 0.99 & 0 & 0 \end{pmatrix} \end{matrix} \quad (6)$$

9 The low deletion probability for position 2 is straightforward to interpret: about 1% of the time, nucleotide **G** at position
 10 2 is deleted. The high deletion probability for position 4 means there is a 1% chance of a **T** insertion at this position.
 11 Table 1 illustrates this.

Table 1: Representation of insertions and deletions from \mathcal{S} defined in (6)

sequence	frequency
CGAAT	common, 98% of the time
CAAT	rare (1% frequency) G deletion at position 2,
CGATAT	rare (1% frequency) T insertion at position 4
CATAT	very rare (0.01% frequency) deletion and insertion

12 The representation of deletions and insertions with a sequence-level probabilistic sequence (not nucleotide-level) is
 13 straightforward because in this framework the sequences are explicitly written out, so are their deletions/insertions.

2.3 Constructing The Uncertainty Matrix

Fragment sequencing error is an error that is quantified with quality (or “Phred”) score attributed to each base call from sequencing instrument. The quality score Q is directly related to the error probability: $\epsilon = 10^{-Q/10}$. Ewing and Green [1998] (where Q typically ranges between 1 and 60). The FASTQ file format is the standard representation for combining sequence and observation error. The uncertainty associated to the base call is quantified by defining the probability that the observed nucleotide is the correct one:

$$\mathbb{P}(\text{nucleotide} = X \mid \text{observed nucleotide} = X) = 1 - \epsilon \quad (7)$$

Unfortunately, for FASTQ files, this base-call probability relates to only one *focal* nucleotide and we have no information on the probability for the three other possible nucleotides. Hence, we must make a modelling choice regarding the distribution of the remaining probabilities.

2.3.1 SAM Files

Massive parallel sequencing platforms (*e.g.*, Illumina, Oxford Nanopores, etc.) provide a large number of short reads sequences of the biological sample of interest. The length of those short reads are typically much smaller than the genome sequenced, so they have to be aligned and stitch together in order to re-assemble the full genome sequence. The short reads are typically stored in FASTQ files where the observation error of each nucleotide (estimated by the sequencing platform itself) is indicated by its Phred score. The alignment and assembly of the short reads is performed by software (internal to the sequencing platform or not ([check this. Examples?](#))) and generates a SAM file ([ref](#)) that efficiently stores the alignment information. The assembly of the short reads in the SAM file can be represented in as an array where the columns are the nucleotide positions. The short reads are “stacked” vertically according to the alignment. The number of short reads stacked for a given nucleotide gives the “coverage” of that position. See Figure 1 for an illustration of this SAM file representation.

The nucleotide-level probabilistic sequence can be constructed from this alignment. The algorithm that we suggest is as follows.

We begin by initializing an empty $5 \times \ell$ matrix \mathcal{S}' . Each label in Figure 1 has an associated probability score. These labels denote a row in \mathcal{S} , and their location on the genome denotes the columns, say (A, j) . At this entry, we add the corresponding quality score to whatever was there before.

By this construction, the sum of each column represents the coverage at that location. Dividing each entry of \mathcal{S}' by the sum of that column results in \mathcal{S} . For our proposed propagation methods, it is convenient to work with \mathcal{S}' until

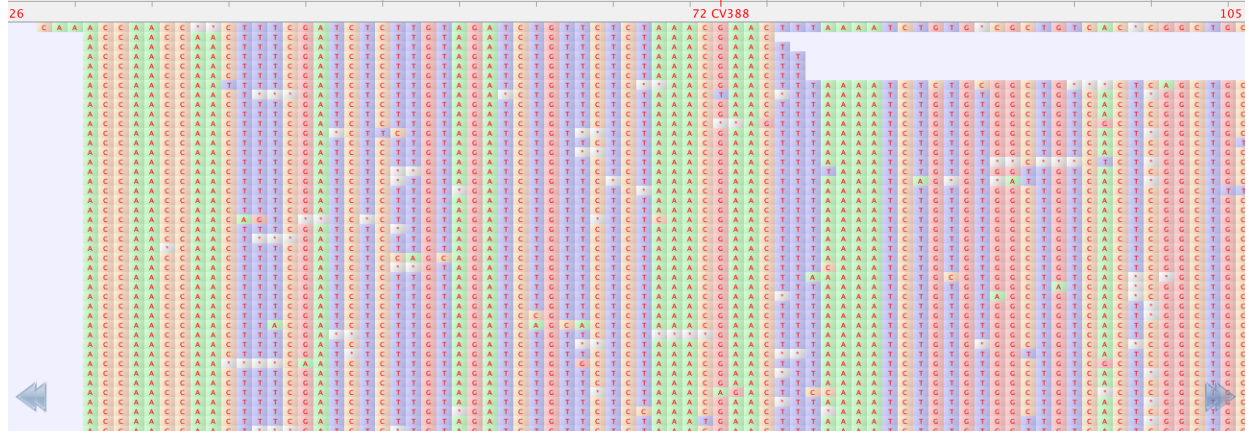


Figure 1: **SAM file graphical representation.** The software Tablet ([ref](#)) was used. Each base call is colour coded so that base calls that disagree with the consensus are obvious. The 72th nucleotide in this alignment has a coverage of 388 reads.

probabilities are necessary.

It is important to note that many NGS platforms use paired reads where the same genome is read in both directions. In these situations, the two reads are not independent and should not be treated as such. Our implementation involves taking the average of the quality scores. If the quality scores were 90% A for one read and 95% A in the second read, then 0.925 is added to the A row in \mathcal{S}' . If the two reads were 60% A and 55% C in the two reads, then the average of 0.6 and $(1-0.55)/3$ would be added to the A row, the average of $(1-0.55)/6$ and 0.55 would be added to the C row, and the average of $(1-0.55)/3$ and $(1-0.6)/3$ would be added to the other rows. This is equivalent to simply determining which reads are paired and dividing all values in their column by two before adding it to \mathcal{S}' . This is advantageous as it allows us to parallelize the reading of SAM files without needing to know which read it is paired with.

2.3.2 Consensus sequence FASTQ files

For most published genome sequences, the short read files are not available. It is common to find the so-called consensus sequence, which is the sequence that represents the most commonly called base at each location, along with a single quality score for each location. The methods for obtaining Phred scores when converting a SAM file to a consensus FASTQ differ by software [Li et al., 2004, Keith et al. [2002], Li et al. [2008]], but generally involve a computation that includes all of the Phred scores of the bases that agree with the consensus (*e.g.*, if the short reads have A with Phred of 30, A with a Phred of 31, and C with phred of 15, then the Phred scores of 30 and 31 are combined in software-defined way, usually incorporating extra information on top of the Phred score).

As a first simplifying step, we ignore insertions and deletions. Given a base call and its associated quality score at each position, we can assume that the other bases are all equally likely with probability $\epsilon/3$. For example, let's assume the

1 output sequence after fragment sequencing and alignment is **ACATG** and its associated quality scores are respectively
 2 $Q = 60, 30, 50, 10, 40$. The probabilistic sequence is:

$$S = \begin{pmatrix} 1 - 10^{-6} & 10^{-3}/3 & 1 - 10^{-5} & 10^{-1}/3 & 10^{-4}/3 \\ 10^{-6}/3 & 1 - 10^{-3} & 10^{-5}/3 & 10^{-1}/3 & 10^{-4}/3 \\ 10^{-6}/3 & 10^{-3}/3 & 10^{-5}/3 & 10^{-1}/3 & 1 - 10^{-4} \\ 10^{-6}/3 & 10^{-3}/3 & 10^{-5}/3 & 1 - 10^{-1} & 10^{-4}/3 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix} \quad (8)$$

3 Usually, the genetic sequence **ACATG** would be considered as certain and quality scores discarded. In con-
 4 trast, within the probabilistic sequence framework the probability the sequence is **ACATG** is only 0.899
 5 $(= (1 - 10^{-6}) \times (1 - 10^{-3}) \times (1 - 10^{-5}) \times (1 - 10^{-1}) \times (1 - 10^{-4}))$.

6 Insertions and deletions (“indels”) can be included in the uniform framework. Here, we propose that the nucleotides
 7 probabilities are defined conditional on an indel but other models are possible. For a given position, the error probability
 8 is $\varepsilon = 10^{-Q/10}$ (Q is the quality score) and we assume the probability a deletion happens at this position is d . Conditional
 9 on not being deleted, the probability to have the base called is $(1 - d)(1 - \varepsilon)$ and the other three nucleotides can occur
 10 with probability $(1 - d)\varepsilon/3$. Hence, if we assume the base call is **A**, the column of the nucleotide-level probabilistic
 11 sequence for that position is

$$\begin{pmatrix} (1 - d)(1 - \varepsilon) \\ (1 - d)\varepsilon/3 \\ (1 - d)\varepsilon/3 \\ (1 - d)\varepsilon/3 \\ d \end{pmatrix} \quad (9)$$

12 2.3.3 Consensus sequence FASTA files

- 13 • Analysis will not draw any firm conclusions, but...
 - 14 – stress testing for your analysis, *e.g.*, could resample genomes at different overall error rates, then simulate
 - 15 error rates from overall rate at each location, then see how much it F’s up your analysis.

16 In the absense of any measured uncertainty we are constrained with what we can do. Any uncertainty that we impose
 17 upon the data will be a principled assumption. However, imposing our assumptions can still be very useful as a “stress
 18 test” of our analysis; we can assume different levels/types of uncertainty and quantify the stability of our results.

19 The error probability at any given nucleotide location can be simulated as a beta distribution, *i.e.*,

$$\varepsilon_j \sim \text{Beta}(\alpha, \beta)$$

1 The called base at position j will be assigned $1 - \varepsilon$ as the probability, then the remaining bases (not including a gap)
 2 will be assigned $\varepsilon_j/3$. To incorporate gaps, another probability d can be generated as the “gap probability”. With these
 3 defiend, the nucleotide-level uncertainty sequence at the j th column (supposing the base call at location j was **A**) can be
 4 generated as:

$$\mathcal{S} = \begin{matrix} & j \\ \text{A} & (1 - d/4)(1 - \varepsilon_j) \\ \text{C} & (1 - d/4)\varepsilon_j/3 \\ \text{G} & (1 - d/4)\varepsilon_j/3 \\ \text{T} & (1 - d/4)\varepsilon_j/3 \\ - & d \end{matrix}$$

5 This uncertainty sequence is completely fabricated, but downstream analyses can be evaluated by choosing values of α ,
 6 β , and d based on previous studies and propagating these uncertainties into downstream analysis.

7 **2.4 Propagation of uncertainty via resampling**

8 The most general way to propagate uncertainty is through resampling. Given \mathcal{S} and assuming that locations are
 9 independent (or pre-defining biologically-reasonable sequences and calculating their probabilities), uncertainty can
 10 be propagated by re-sampling the sequences according to their probability and re-running the analysis on each set of
 11 sampled sequences (I don’t have a citation for this, but I believe Peter Piper sampled a set of sampled sequences).

12 Re-sampling can either be done simply based on the nucleotide-level uncertainty as a multinomial distribution. If the
 13 j th column of \mathcal{S} is (0.5, 0.2, 0.2, 0.09, 0.01), then we could sample **A** with 50% probability, **C** with 20%, etc. However,
 14 this disregards the coverage at each location, thereby disregarding the variance of the error probabilities.

15 To incorporate the variance of the errors, a Dirichlet-Multinomial sampling scheme can be derived by assuming that the
 16 error probabilities follow a Dirichlet prior and the bases follow a multinomial likelihood. For each base at each location,
 17 the entry for \mathcal{S}' is defined as the sum of the probabilities (one minus the error probabilities). These values can be used
 18 as the parameters in the Dirichlet prior, from which base probabilities can be sampled.

19 For example, if the j th column of \mathcal{S}' is (1200.45, 200.09, 100.74, 121.11, 0), then possible base probabilities could be
 20 (0.743, 0.126, 0.062, 0.070, 0), (0.739, 0.121, 0.066, 0.074, 0), or (0.744, 0.128, 0.056, 0.071, 0). In contrast, if the j th

column of \mathcal{S}' were (12.4, 1.2, 0.4, 1.7, 0), then some samples from the Dirichlet distribution might be (0.759, 0.059, 0.029, 0.153, 0), (0.916, 0.065, 0.009, 0.009, 0), or (0.779, 0.117, 0, 0.104, 0). The lower coverage is incorporated into the analysis by the increase in the variance of the Dirichlet distribution.

In a maximum likelihood framework, this is similar to bootstrapping. In fact, the ultimate effect of this would be to decrease the bootstrap confidence to a level that is more in line with the actual uncertainty in the data.

In a Bayesian framework, this could be incorporated as prior distribution on each nucleotide. For large collections of large sequences, this increases the dimensionality dramatically. In the next section, we provide a proposal for reducing the number of sequences that must be sampled.

2.5 Reducing computational burden with sequence-level uncertainty

Suppose we wish to use a single sequence to estimate some parameter θ (for instance, the p-value for whether a sequence is a particular variant or the lineage assignment for grafting to a pre-computed tree) and we are interested in the effect that uncertainty has on this estimate. Computational burden can be partially alleviated by incorporating sequence-level uncertainty.

To start with, the most likely sequences must be calculated. This could be done by calculating all of the sequences, comparing their likelihoods (labelled a_i), and putting them in order ($a_{(i)}$), but this is not necessary. Instead, the most likely sequence is already known (the consensus sequence). The second most likely sequence can be found by substituting the base call that was least likely (but still called) with the second most likely base call.

The calculation of the likelihood will be identical in these two cases except for the one substitution. Instead of calculating the entire likelihood (which can be numerically unstable since there are nearly 30,000 base pairs), the difference in the likelihood can be calculated.

Consider the two vectors M and m , where M_j represents the largest value in the j th column of \mathcal{S} and m_j represents the second largest value. The likelihood of the consensus sequence is $a_{(0)} = \prod_{j=1}^N M_j$. Let k be the index of the smallest value in M , then the second most likely sequence has likelihood $a_{(1)} = \prod_{j \neq k} M_j m_k$. The change in likelihood is $a_{(0)}/a_{(1)} = M_k/m_k$, which implies that $a_{(1)} = a_{(0)}m_k/M_k$.

This process does not necessarily continue in a straightforward manner. At some point, it will be uncertain whether making a different substitution will have a larger effect on the likelihood than adding a substitution than one made in another sequence. The differences in likelihood derived above provide a very fast comparison of likelihoods, though, so it is not expensive to calculate both possible situations. Because of this speed-up, it is computationally feasible to simply calculate the likelihood for all substitutions involving the d least likely base calls that made it into the conseq

and then sort them out later. There are 2^d possible combinations of substitutions for d bases, which means that $d = 12$ will provide the 4,096 most likely sequences.

For an arbitrary set of substitutions \mathcal{J} relative to the conseq, the likelihood can be calculated as $a_{(0)} \prod_{j \in \mathcal{J}} m_j / M_k$. To greatly simplify the calculation of the likelihood, only the d locations need to be considered.

Suppose we are using these sequences to estimate some parameter θ . The sequences can be ordered according to their uncertainty, with the most likely sequence having uncertainty $a_{(1)}$, the second-most likely sequence $a_{(i)}$, etc. The analysis can be performed using the most likely sequence, resulting in an estimate $\theta_{(0)}$. The analysis can be re-run with the second-most likely sequence, $\theta_{(1)}$. Given just these two estimates, a weighted estimate of θ given the 2 most likely sequences could be found as:

DEVAN! BAD! $a_{(0)}$ has already been used! Maybe use primes?

$$\hat{\theta}_{(1)} \approx \theta_{(0)} \tilde{a}_{(0)} + \theta_{(1)} \tilde{a}_{(1)}, \text{ where } \tilde{a}_{(j)} = a_{(j)} / \sum_{i=1}^2 a_{(i)}$$

The third-most likely sequence can be analysed, resulting in $\hat{\theta}_{(2)}$. This process can be repeated until new estimates do not have any impact on the results (convergence criteria could be set, but a graphical representation of $\theta_{(i)}$ would be more informative). If convergence is not clearly met, the d can be increased until enough sequences are obtained.

With this algorithm, the computational burden is separated into calculating the sequence likelihood for the most likely sequences and running the analysis enough times to be confident convergence is achieved.

For analyses that require a set of sequences, the likelihoods for the set of sequences can be calculated as the product of the likelihoods (or, for computational stability, the sum of the log-likelihoods) of the individual sequences. The algorithm above can be adjusted accordingly.

3 Applications

3.1 Generated Uncertainty as Evaluation

If only FASTA files are available, then it's unclear how much variation there is. FASTQ files have a measure of uncertainty at each position, but this does not tell us whether the added uncertainty has a large or a small effect on the results. In this analysis, we generate a phylogeny so we know exactly what the truth is. From this phylogeny, we simulate uncertainty (FASTQ-style) at four different parameter combinations, based on those found in ?. These parameter combinations represent increasing levels of entropy. With this uncertainty, we re-sample our sequences and attempt to reconstruct the phylogeny. From these re-sampled phylogenies, we calculate the distance between each new

tree and the original perfectly known tree. The results demonstrate the additional variance that can be added to a tree on top of the variance that other analysis will consider. In a study of real sequences, the entropy can be calculated from the FASTQ file then compared to a similar entropy level for simulated data. The variation in tree distance for that level of entropy can be seen as a measure of the un-accounted-for variance in the results.

Our simulation was set up as follows. The 300 nucleotide long base sequence and its evolutionary tree with 20 terminal nodes were simulated using the functions in the PhyloSim R package. Error probabilities were introduced based on random draws from a beta distribution. The mean values of this beta distribution were chosen to represent reasonable amounts of error, then the standard deviations were chosen based on the order of magnitude of the mean, then the corresponding shape parameters were found (see Figure ??). New sequences were simulated from this uncertainty based on sampling from the uncertainty matrix defined by these error probabilities, with the remaining probability distributed uniformly across the other bases (see Section ??). We also set the probability of deletion based on a beta distribution with shape parameters 1 and 6, but only for nucleotide positions 5 to 15 and 200 to 250. The sequence uncertainty generation process was repeated 300 times for each parameter set (the original sequence and evolutionary tree were the same for all simulations).

To summarise the results of this simulation, we looked at the distance between the trees as well as the distance between nodes within each tree. We looked at the Robinson-Foulds distance [?], Kuhner-Felsenstein distance [?], and a distance based on shared ancestry. The shared ancestry distance has calculated by calculating the set of ancestors at each node (both internal and terminal), recording the set of all ancestry sets for each tree, then enumerating the number of ancestry sets that two trees share. This definition of distance works especially well for our application since the nodes in each tree are all deviations from the same initial set of nodes, and thus would have exactly the same ancestry were it not for our generated uncertainty. The distance within a tree is calculated as the mean of the TN93 distance between nodes.

- Parameter settings for the most recent run (I will try to define them, but my ignorance will shine through).

- 300: Length of the ‘true’ root sequence
- 0.75: Proportion of invariant positions in the root sequence
- 1: Generate the root sequence randomly?
- 20: Number of tips in the ‘true’ simulated phylogeny
- 1: Evolution rate (in tree time unit)
- 29: Beta shape prm_1 (alpha) for base call probability
- 0.05: Beta shape prm_2 (beta) for base call probability
- 500: Monte Carlo iterations for sampling tip probabilistic sequences
- TN93: Distance (nucleotide)
- Tree distances: ~~Kernel~~, Robinson-Foulds, Kuhner-Felsenstein, shared?

1 * Shared: proportion of nodes in a tree that DO NOT have the same descendance as a reference tree. To
 2 calculate, the ancestors of every node (tip and internal) are stored in a list. This list is compared to
 3 the ancestor list for the reference tree (*i.e.*, the tree calculated prior to gen-uncertain). The distance is
 4 measured as 1 minus the proportion of ancestors that are shared.

5 * I need a reference for this.

6 – InDels: 5:15, 200:250; TODO: find the mean/sd of the error probability

7 The results are displayed as some sort of graph. Distance between true tree and sampled ones versus entropy is a nice.

8 Average/sd of within-tree TN93 is interesting as well. Clusters are all 1, for some reason.

9 • TODO:

10 – Import analysis visualization code

11 * DONE: Beta distribution shapes

12 * TODO: Hist of dist to certain tree

13 * TODO: Hist of within-tree TN93, with certaintree highlighted

14 · Also, a description of this

15 – Calculate important/interesting statistics

16 * Mean/sd distance to certain tree

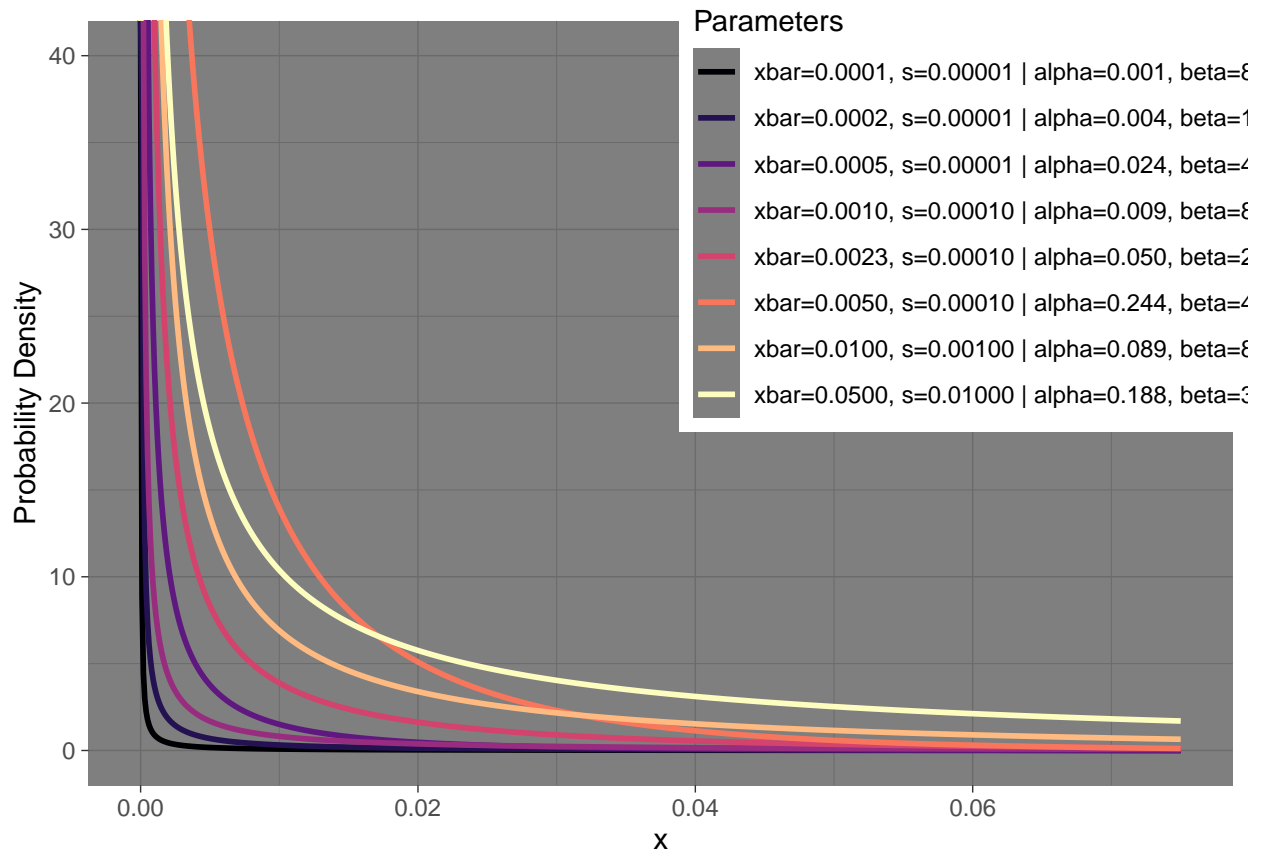
17 *

18 – Describe the beta parameters

19 * DONE: Re-run with a finer scale but fewer iterations

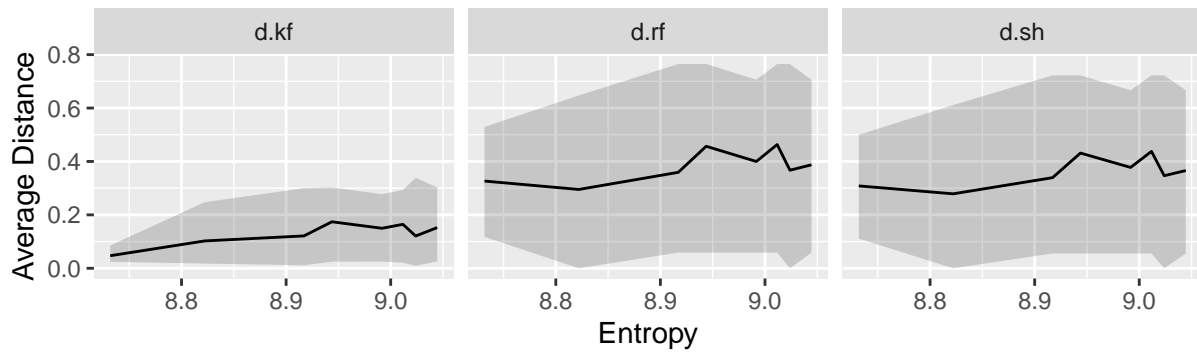
20 * TODO: Explain them

	prmset	s1	s2	entropy	mean	var
	1	0.0008999	8.99810	9.023867	0.0001	1e-05
	2	0.0037992	18.99220	8.917083	0.0002	1e-05
	3	0.0244875	48.95051	9.011684	0.0005	1e-05
	4	0.0089900	8.98101	8.943781	0.0010	1e-04
	5	0.0504783	21.89662	9.044467	0.0023	1e-04
	6	0.2437500	48.50625	8.991713	0.0050	1e-04
	7	0.0890000	8.81100	8.822024	0.0100	1e-03
	8	0.1875000	3.56250	8.731836	0.0500	1e-02

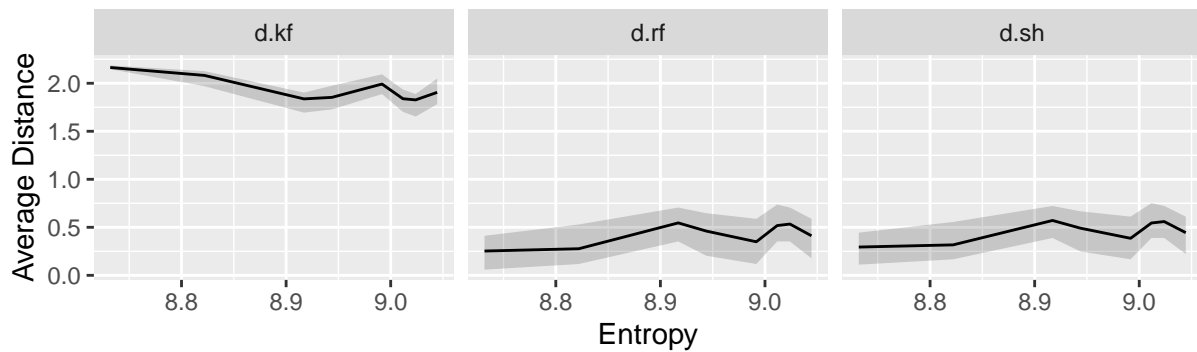


1

Average distance between inferred trees



Average distance from inferred trees to certain tree



2

3.2 SARS-CoV-2

In this section, we demonstrate the re-sampling method on lineage assignment of SARS-CoV-2. Sequences are sampled from \mathcal{S}^I and then assigned a lineage based on the current state-of-the-art in phylogenetic analysis.

We use the lineage designations described in Rambaut et al. [2020] and assign our sequences to lineages using the pangoLEARN tool (pangolin version 2.3.2, pangoLEARN version 2021-02-21) that the authors have made available (github.com/cov-lineages/pangolin). This tool uses a decision tree model to determine which lineage a given sequence is most likely to belong to. The tool also reports a bootstrap support probability as a measurement of the tool's confidence in its assignment. We demonstrate that even the best available tools are underestimating the variance and therefore producing overconfident conclusions.

3.2.1 Data

The data for this application were downloaded from NCBI's SRA web interface (<https://www.ncbi.nlm.nih.gov/sra/?term=txid2697049>). Search results were filtered to only include runs that had SAM files. To select which runs to download, a selection of 5-10 files from each of 20 non-sequential results pages were chosen. Once collecting the run accession numbers from the search results, an R script was run to download the relevant files and check that all information was complete. 23 out of 300 files were labelled incomplete due to having too few reads (possibly because the download timed out) or not containing a CIGAR string. The GISAID accession numbers for the sequences we used are provided in the appendix.

There was no particular reason for choosing any given file, but the resulting data should not be viewed as a random sample. Each result page likely includes several runs from the same study, and runs were chosen arbitrarily within each result page. We were not attempting a completely random sampling strategy, we simply wanted a collection of runs on which to demonstrate our methods.

3.2.2 Re-sampling the call probability matrix

Since pangoLEARN is a pre-trained model, the analysis is not computationally burdensome. Sampling 10,000 different sequences from a call probability matrix is reasonable, even on a mid-range consumer laptop.

For this analysis we use the most basic resampling strategy. We simply draw probabilities from the Dirichlet distribution with parameters defined by \mathcal{S}^I , sample base calls from the multinomial distribution, then use pangoLEARN to determine the lineage assignment.

In ??, each row represents resamples from one SAM file. Each bar represents one lineage assignment from pangolin. The width of the bars represents the sum of the weights (genome likelihoods) of sampled sequences. Bars are subdivided

Initial analyses used pangolin version 2.0.8, which used multinomial logistic regression, rather than decision trees, to assign lineages. This procedure resulted in bootstrap support values that varied from 0.6 to 1. After upgrading to pangolin version 2.3.2, which uses a decision tree model, all bootstrap probabilities are reported as 1.

Wishlist:

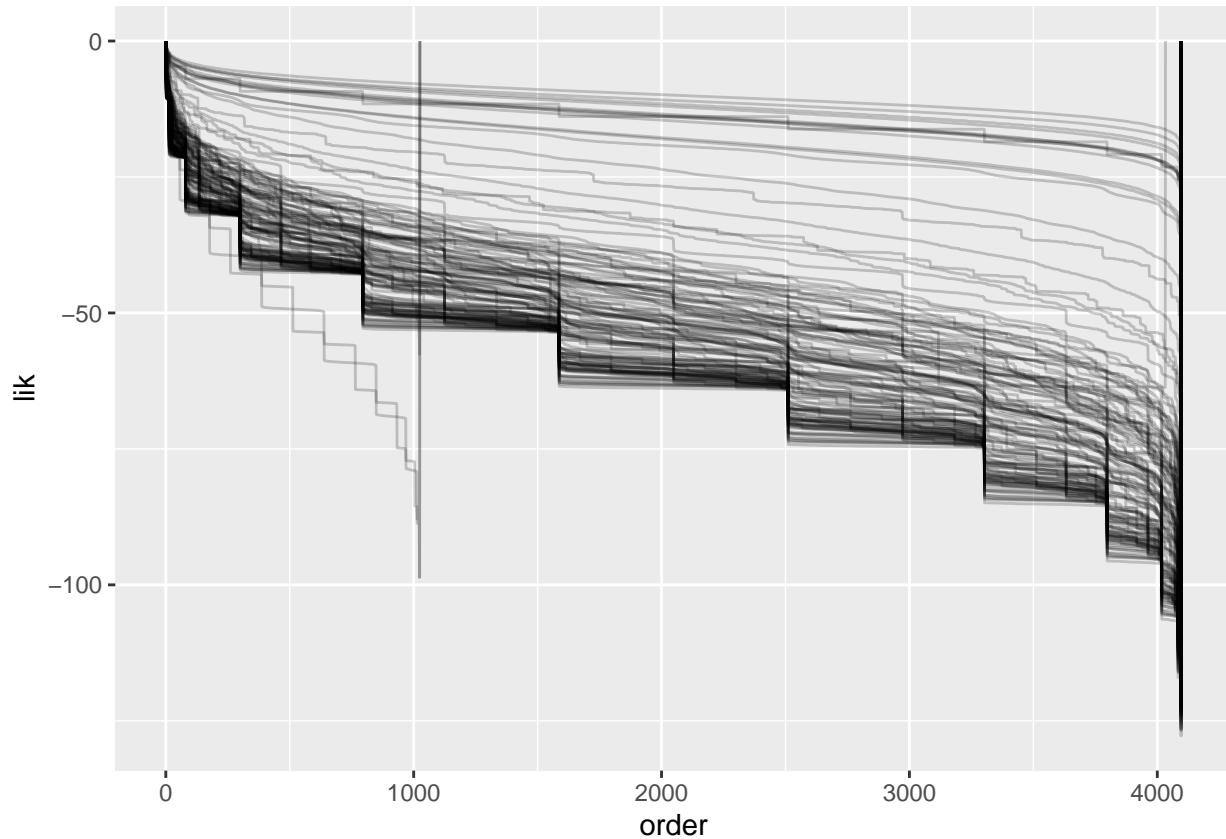
- Average Mode/#
 - Histogram to show distribution? Maybe with a transparent Runner-Up distribution?

3.2.3 Sequential re-analysis with genome likelihoods

TODO (Analysis has been run on a single accession number; not sure how this will compare to resampling in all accessions.)

Wishlist

- Scatterplot: #/N on the y axis, total weight from the sequences agreeing with the conseq divided by total weights of all sequences on the x axis.
- Average number of substitutions (or average likelihood difference) before the called lineage changes
- Set difference of lineages with ordered likelihoods versus re-sampling (*i.e.*, which lineage assignments were unique to each method).
- Overarching conclusion



4 Conclusions

The short run files produced by next generation sequencing platforms include valuable information about the quality of base calls which can easily be propagated into analyses. Re-sampling allows a more honest appraisal of the variance in the estimates (or provides a reasonable prior distribution in a Bayesian setting), while comparing results for the most likely sequences provide a measure of robustness to sequence uncertainty.

Our proposed methods can result in a drastic increase in computational expense. Even the method base on ordering the sequences by likelihood can result in re-running the analysis numerous times. However, we have demonstrated that the uncertainty in the sequences themselves can lead to major changes to the interpretations of the results. The so-called “consensus sequence” is simply the most likely sequence, and the reported uncertainty is not merely an academic curiosity.

Our analysis focused on phylogenetic trees based on HIV sequences as well as designation of lineages according to the Pangolin model. The importance of incorporating sequence uncertainty is not confined to these applications; any analysis involving sequenced genomes would benefit from some method of incorporating the uncertainty or including some measure of robustness. For example, the estimated frequency of alleles in the population could be used as the

probability sequence, then propagated into further analysis.

Our method does not preclude tertiary analyses to test for systematic errors or deviations from a Mendelian inheritance pattern assumption. We cannot account for systematic errors, such as those present due to human errors (*e.g.*, mis-calibrated machines or that one lab in ? that kept giving the same mutations). Our method allows for adjustments of the base call quality score (such as those in ?), as well as more sophisticated definitions genome likelihoods (such as those in ?).

This study should not be taken in any way as a criticism of the pangolin lineage assignment procedure. Rather, pangolin was chosen as it is a state-of-the art tool based on the best available algorithms for phylogeny reconstruction. The phylogeny created by this team has been a vital resource for researchers and for public health professionals. In particular, their label for the current Variants of Concern (VOCs), especially B.1.1.7, are the labels being used worldwide by news organizations.

- Other things that could be added here:
 - Resample to get variance around representative sequence for a given lineage (*e.g.*, HIV)
 - * Can be done with just FASTQ files (less accurate)
 - Given a canonical reference sequence for a lineage, find level of entropy that makes it a different sequence

5 Appendix: Results for all lineages

Accession	Conseq	Mode	Mode #	Mode #/N	Runner-Up	RU #	Unique	Atoms
SRR12762573	A	A	3532	70.68	B	1028	17	4
SRR13092002	A.1	A.1	4922	98.50	B.40	37	17	7
SRR13020990	A.2.2	A.2.2	2892	57.87	A.2	737	107	48
ERR4891988	B	B	3914	78.33	B.23	296	55	24
ERR4999282	B	B	4041	80.87	B.54	246	53	11
ERR4891715	B	B	4521	90.47	B.23	123	28	6
SRR13020989	B.1.1.273	B.1	1338	26.87	B	302	425	132
ERR4440194	B.1	B.1	2575	51.53	B.1.98	2254	18	4
ERR4891841	B.1	B.1	3785	75.75	B.1.243	38	219	52
ERR4890354	B.1	B.1	4326	86.57	B.1.243	25	179	48
ERR4893013	B.1	B.1	4444	88.93	B.1.88	124	49	17
ERR4692364	B.1	B.1	4524	90.53	B.1.400	170	58	25
ERR4440731	B.1	B.1	4666	93.38	B.1.391	50	54	19
ERR5069624	B.1	B.1	4821	96.48	B.1.247	83	42	18
ERR4694556	B.1.1.15	B.1.1.15	4772	95.50	B.1.1.107	19	57	17
ERR4892293	B.1.1.162	B.1.1.162	3145	62.94	B.1.1.197	93	190	48
ERR4440219	B.1.1.164	B.1.1.164	4682	93.70	B.1.1	32	70	23
ERR4891863	B.1.1.216	B.1.1.216	4201	84.07	B.1	119	127	48
ERR4893186	B.1.1.216	B.1.1.216	4432	88.69	B.1	44	86	24

Accession	Conseq	Mode	Mode #	Mode #/N	Runner-Up	RU #	Unique	Atoms
ERR4892203	B.1.1.216	B.1.1.216	4495	89.95	B.1.1.208	64	90	24
ERR5080893	B.1.1.251	B.1.1.251	2943	58.90	B.1	185	149	27
ERR4664555	B.1.1.253	B.1.1.253	4813	96.32	B.1	49	23	4
ERR4307842	B.1.1.289	B.1.1.289	4745	94.96	B.1	56	29	11
ERR4759453	B.1.1.29	B.1.1.29	977	19.55	B.1.1.208	244	207	47
ERR4440425	B.1.1.29	B.1.1.29	1076	21.53	B.1	129	260	24
ERR4892066	B.1.1.29	B.1.1.29	1297	25.96	B.1.1.59	343	231	56
ERR4890228	B.1.1.29	B.1.1.29	1982	39.66	B.1.1.273	133	232	58
ERR4893037	B.1.1.29	B.1.1.29	2495	49.93	B.1	90	223	28
ERR4890294	B.1.1.29	B.1.1.29	2710	54.23	B.1.1.37	521	189	41
ERR4440247	B.1.1.29	B.1.1.29	3155	63.14	B.1	229	227	38
ERR4694571	B.1.1.29	B.1.1.29	3176	63.56	B.1.1.44	131	213	42
ERR4440354	B.1.1.29	B.1.1.29	3323	66.50	B.1.1.132	65	211	33
ERR4440402	B.1.1.29	B.1.1.29	3490	69.84	B.1	168	215	45
ERR4364007	B.1.1.29	B.1.1.29	4271	85.47	B.1.1	56	89	29
ERR4694617	B.1.1.304	B.1.1.304	4711	94.28	B.1.1.10	66	28	3
ERR4891898	B.1.1.304	B.1.1.304	4831	96.68	B.1.1.4	18	29	7
ERR4893033	B.1.1.307	B.1.1.307	4870	97.46	B.1	63	34	22
ERR5062514	B.1.1.307	B.1.1.307	4943	98.92	B.1.1.311	18	17	10
ERR4892048	B.1.1.307	B.1.1.307	4966	99.38	B.1.1.311	16	8	5
ERR4893353	B.1.1.307	B.1.1.307	4973	99.52	B.1	13	7	3
ERR4890271	B.1.1.307	B.1.1.307	4978	99.62	B.1	7	8	3
ERR4693079	B.1.1.310	B.1.1.310	4376	87.57	B.1.1.29	231	107	50
ERR4693034	B.1.1.310	B.1.1.310	4399	88.03	B.1.1.59	57	89	44
ERR5080913	B.1.1.311	B.1.1.311	4861	97.28	B.1.1.281	47	16	8
ERR5082696	B.1.1.315	B.1.1.315	4575	91.55	B.1	147	43	20
ERR5082664	B.1.1.315	B.1.1.315	4866	97.38	B.1	60	13	4
ERR4667618	B.1.1.315	B.1.1.315	4933	98.72	B.1	30	11	3
ERR4869497	B.1.1.315	B.1.1.315	4944	98.94	B.1	15	11	4
ERR5062388	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5062935	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5063143	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5063807	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5064346	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5064811	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5069584	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5069616	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5069871	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5070294	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5077411	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5077618	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5082610	B.1.1.7	B.1.1.7	4997	100.00	NA	NA	1	0
ERR5074314	B.1.160	B.1.160	4833	96.72	B.1.160.8	95	18	10
ERR5082569	B.1.160	B.1.160	4845	96.96	B.1.160.5	68	23	10
ERR4869446	B.1.160.7	B.1.160.7	4947	99.00	B.1.160	42	5	0
ERR5082711	B.1.177	B.1.177	3683	73.70	B.1.177.22	749	29	11
ERR5082645	B.1.177	B.1.177	3805	76.15	B.1.177.22	517	22	7

Accession	Conseq	Mode	Mode #	Mode #/N	Runner-Up	RU #	Unique	Atoms
ERR4893031	B.1.177	B.1.177	3812	76.29	B.1.177.7	1003	19	7
ERR4892152	B.1.177	B.1.177	4260	85.25	B.1.177.7	498	14	3
ERR5082561	B.1.177	B.1.177	4313	86.31	B.1.177.22	447	22	5
ERR5062062	B.1.177	B.1.177	4326	86.57	B.1.177.8	381	16	2
ERR5082695	B.1.177	B.1.177	4483	89.71	B.1.177.22	297	19	4
ERR4869480	B.1.177	B.1.177	4511	90.27	B.1.177.22	252	22	5
ERR4893242	B.1.177	B.1.177	4561	91.27	B.1.177.6	164	15	3
ERR4892339	B.1.177	B.1.177	4566	91.37	B.1.177.23	131	19	1
ERR5082576	B.1.177	B.1.177	4567	91.39	B.1.177.22	237	20	1
ERR5064294	B.1.177	B.1.177	4576	91.57	B.1.177.27	272	14	2
ERR5082580	B.1.177	B.1.177	4601	92.08	B.1.177.22	242	20	1
ERR5081301	B.1.177	B.1.177	4638	92.82	B.1.177.22	195	21	4
ERR4869458	B.1.177	B.1.177	4648	93.02	B.1.177.22	198	19	3
ERR4869487	B.1.177	B.1.177	4702	94.10	B.1.177.22	147	17	1
ERR5080918	B.1.177	B.1.177	4723	94.52	B.1.177.22	150	19	4
ERR5064166	B.1.177	B.1.177	4731	94.68	B.1.177.22	149	16	1
ERR5062729	B.1.177	B.1.177	4760	95.26	B.1.177.22	116	14	1
ERR4893080	B.1.177	B.1.177	4767	95.40	B.1.177.22	118	14	5
ERR5063922	B.1.177	B.1.177	4769	95.44	B.1.177.22	148	16	1
ERR4892392	B.1.177	B.1.177	4770	95.46	B.1.177.22	95	18	5
ERR5063539	B.1.177	B.1.177	4774	95.54	B.1.177.22	121	20	4
ERR4893197	B.1.177	B.1.177	4779	95.64	B.1.177.23	105	18	5
ERR5077151	B.1.177	B.1.177	4785	95.76	B.1.177.22	114	20	2
ERR5062571	B.1.177	B.1.177	4800	96.06	B.1.177.22	98	21	3
ERR5060778	B.1.177	B.1.177	4827	96.60	B.1.177.22	115	15	5
ERR4890403	B.1.177	B.1.177	4831	96.68	B.1.177.22	82	18	5
ERR5070060	B.1.177	B.1.177	4854	97.14	B.1.177.22	69	14	2
ERR5081316	B.1.177.15	B.1.177.15	4799	96.04	B.1.177	131	16	6
ERR4893138	B.1.177.16	B.1.177.16	4954	99.14	B.1.177	30	7	3
ERR4892200	B.1.177.17	B.1.177.17	4956	99.18	B.1.177	39	4	2
ERR5064787	B.1.177.17	B.1.177.17	4958	99.22	B.1.177	23	5	2
ERR4890386	B.1.177.18	B.1.177.18	4969	99.44	B.1.177.13	15	6	2
ERR5076163	B.1.177.19	B.1.177.19	4856	97.18	B.1.177	99	11	1
ERR5076748	B.1.177.19	B.1.177.19	4892	97.90	B.1.177	67	12	5
ERR5063165	B.1.177.19	B.1.177.19	4905	98.16	B.1.177	67	8	2
ERR5063813	B.1.177.19	B.1.177.19	4932	98.70	B.1.177	47	9	3
ERR4693605	B.1.177.3	B.1.177.3	4825	96.56	B.1.177	68	17	2
ERR5081304	B.1.177.4	B.1.177.4	4954	99.14	B.1.177.2	21	17	10
ERR5082590	B.1.177.4	B.1.177.4	4971	99.48	B.1.177.2	13	11	7
ERR5062648	B.1.177.4	B.1.177.4	4988	99.82	B.1.177	4	6	3
ERR5082674	B.1.177.6	B.1.177.6	4858	97.22	B.1.177	79	13	4
ERR4891805	B.1.177.6	B.1.177.6	4939	98.84	B.1.177	24	8	0
ERR5082712	B.1.177.7	B.1.177.7	3334	66.72	B.1.177	1612	15	5
ERR5082556	B.1.177.7	B.1.177.7	3766	75.37	B.1.177	1195	11	2
ERR5082630	B.1.177.7	B.1.177.7	4833	96.72	B.1.177	128	13	6
ERR4693537	B.1.177.7	B.1.177.7	4849	97.04	B.1.177	126	13	6
ERR4363387	B.1.222	B.1.222	4761	95.28	B.1	96	27	14

Accession	Conseq	Mode	Mode #	Mode #/N	Runner-Up	RU #	Unique	Atoms
ERR5081322	B.1.235	B.1.235	4743	94.92	B.1	128	21	8
ERR4893184	B.1.258	B.1.258	4099	82.03	B.1.258.17	435	35	15
ERR5062004	B.1.258	B.1.258	4563	91.31	B.1	80	35	7
ERR4891711	B.1.36	B.1.36	4770	95.46	B.1.36.9	81	27	8
ERR4890371	B.1.36.17	B.1.36.17	4177	83.59	B.1	491	45	17
ERR5080897	B.1.36.17	B.1.36.17	4763	95.32	B.1	132	24	13
ERR4890352	B.1.36.17	B.1.36.17	4938	98.82	B.1	20	16	10
ERR4890337	B.1.36.17	B.1.36.17	4951	99.08	B.1	20	9	3
ERR4892423	B.1.523	B.1.523	4493	89.91	B.1	128	31	9
ERR4893393	B.1.523	B.1.523	4658	93.22	B.1	153	36	15
ERR4890285	B.1.523	B.1.523	4892	97.90	B.1	50	23	9
ERR4891889	B.1.98	B.1.98	4166	83.37	B.1	311	70	42
ERR4693061	B.23	B.23	4734	94.74	B.48	113	19	5
ERR4694400	B.3	B.3	4903	98.12	B.3.1	42	13	3
ERR4305816	B.3.1	B.3.1	4788	95.82	B.3	147	15	3
ERR4892112	B.39	B.39	4733	94.72	B.3	85	31	13
ERR4890427	B.39	B.39	4757	95.20	A.16	96	20	4
ERR4440332	B.40	B.40	4917	98.40	B.1	41	8	2
ERR4892386	B.40	B.40	4967	99.40	B.1	10	8	2
ERR4440373	B.40	B.40	4972	99.50	B	10	9	5
ERR4891916	None	None	4993	99.96	B.1	2	2	0
ERR4999251	None	None	4997	100.00	NA	NA	1	0
ERR4999255	None	None	4997	100.00	NA	NA	1	0
ERR4999275	None	None	4997	100.00	NA	NA	1	0
SRR12639958	None	None	4997	100.00	NA	NA	1	0

Bibliography

- Niko Beerenwinkel and Osvaldo Zagordi. Ultra-deep sequencing for the analysis of viral populations. *Current Opinion in Virology*, 1(5):413–418, November 2011. ISSN 1879-6257. doi: 10.1016/j.coviro.2011.07.008.
- Mark A DePristo, Eric Banks, Ryan Poplin, Kiran V Garimella, Jared R Maguire, Christopher Hartl, Anthony A Philippakis, Guillermo del Angel, Manuel A Rivas, Matt Hanna, Aaron McKenna, Tim J Fennell, Andrew M Kernysky, Andrey Y Sivachenko, Kristian Cibulskis, Stacey B Gabriel, David Altshuler, and Mark J Daly. A framework for variation discovery and genotyping using next-generation DNA sequencing data. *Nature Genetics*, 43(5):491–498, May 2011. ISSN 1061-4036, 1546-1718. doi: 10.1038/ng.806.
- N. V. Doronina. Phylogenetic position and emended description of the genus *Methylovorus*. *INTERNATIONAL JOURNAL OF SYSTEMATIC AND EVOLUTIONARY MICROBIOLOGY*, 55(2):903–906, March 2005. ISSN 1466-5026, 1466-5034. doi: 10.1099/ij.s.0.63111-0.

1 Brent Ewing and Phil Green. Base-Calling of Automated Sequencer Traces Using *Phred*. II. Error Probabilities.
2 *Genome Research*, 8(3):186–194, March 1998. ISSN 1088-9051, 1549-5469. doi: 10.1101/gr.8.3.186.

3 Matteo Fumagalli, Filipe G Vieira, Thorfinn Sand Korneliussen, Tyler Linderoth, Emilia Huerta-Sánchez, Anders
4 Albrechtsen, and Rasmus Nielsen. Quantifying Population Genetic Differentiation from Next-Generation Sequencing
5 Data. *Genetics*, 195(3):979–992, November 2013. ISSN 1943-2631. doi: 10.1534/genetics.113.154740.

6 Zachariah Gompert and C. Alex Buerkle. A Hierarchical Bayesian Model for Next-Generation Population Genomics.
7 *Genetics*, 187(3):903–917, March 2011. ISSN 0016-6731, 1943-2631. doi: 10.1534/genetics.110.124693.

8 Jonathan M. Keith, Peter Adams, Darryn Bryant, Dirk P. Kroese, Keith R. Mitchelson, Duncan A. E. Coachran, and
9 Gita H. Lala. A simulated annealing algorithm for finding consensus sequences. *Bioinformatics*, 18(11):1494–1499,
10 November 2002. ISSN 1367-4803. doi: 10.1093/bioinformatics/18.11.1494.

11 Tony Kuo, Martin C. Frith, Jun Sese, and Paul Horton. EAGLE: Explicit Alternative Genome Likelihood Evaluator.
12 *BMC Medical Genomics*, 11(2):28, April 2018. ISSN 1755-8794. doi: 10.1186/s12920-018-0342-1.

13 Heng Li, Jue Ruan, and Richard Durbin. Mapping short DNA sequencing reads and calling variants using mapping
14 quality scores. *Genome Research*, 18(11):1851–1858, January 2008. ISSN 1088-9051, 1549-5469. doi: 10.1101/gr.0
15 78212.108.

16 Ming Li, Magnus Nordborg, and Lei M. Li. Adjust quality scores from alignment and improve sequencing accuracy.
17 *Nucleic Acids Research*, 32(17):5183–5191, 2004. ISSN 0305-1048. doi: 10.1093/nar/gkh850.

18 Ruiqiang Li, Yingrui Li, Xiaodong Fang, Huanming Yang, Jian Wang, Karsten Kristiansen, and Jun Wang. SNP
19 detection for massively parallel whole-genome resequencing. *Genome Research*, 19(6):1124–1132, January 2009.
20 ISSN 1088-9051, 1549-5469. doi: 10.1101/gr.088013.108.

21 Jason A. O’Rawe, Scott Ferson, and Gholson J. Lyon. Accounting for uncertainty in DNA sequencing data. *Trends in*
22 *Genetics*, 31(2):61–66, February 2015. ISSN 0168-9525. doi: 10.1016/j.tig.2014.12.002.

23 Andrew Rambaut, Edward C. Holmes, Áine O’Toole, Verity Hill, John T. McCrone, Christopher Ruis, Louis du Plessis,
24 and Oliver G. Pybus. A dynamic nomenclature proposal for SARS-CoV-2 lineages to assist genomic epidemiology.
25 *Nature Microbiology*, July 2020. ISSN 2058-5276. doi: 10.1038/s41564-020-0770-5.

26 Peter Richterich. Estimation of Errors in “Raw” DNA Sequences: A Validation Study. *Genome Research*, 8(3):251–259,
27 January 1998. ISSN 1088-9051, 1549-5469. doi: 10.1101/gr.8.3.251.

28 Kimberly Robasky, Nathan E. Lewis, and George M. Church. The role of replicates for error mitigation in next-

1 generation sequencing. *Nature Reviews Genetics*, 15(1):56–62, January 2014. ISSN 1471-0064. doi: 10.1038/nrg3
2 655.