C2 W4 Decision Tree with Markdown

May 24, 2023

1 Practice Lab: Decision Trees

In this exercise, you will implement a decision tree from scratch and apply it to the task of classifying whether a mushroom is edible or poisonous.

2 Outline

```
Section ??Section ??
```

• Section ??

- Section ??

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- Section ??

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• Section ??

NOTE: To prevent errors from the autograder, you are not allowed to edit or delete non-graded cells in this notebook. Please also refrain from adding any new cells. **Once you have passed this assignment** and want to experiment with any of the non-graded code, you may follow the instructions at the bottom of this notebook.

```
## 1 - Packages
```

First, let's run the cell below to import all the packages that you will need during this assignment.

- numpy is the fundamental package for working with matrices in Python. - matplotlib is a famous library to plot graphs in Python. - utils.py contains helper functions for this assignment. You do not need to modify code in this file.

```
[1]: import numpy as np
import matplotlib.pyplot as plt
from public_tests import *
from utils import *
```

%matplotlib inline

2 - Problem Statement

Suppose you are starting a company that grows and sells wild mushrooms. - Since not all mushrooms are edible, you'd like to be able to tell whether a given mushroom is edible or poisonous based on it's physical attributes - You have some existing data that you can use for this task.

Can you use the data to help you identify which mushrooms can be sold safely?

Note: The dataset used is for illustrative purposes only. It is not meant to be a guide on identifying edible mushrooms.

3 - Dataset

You will start by loading the dataset for this task. The dataset you have collected is as follows:

Cap Color	Stalk Shape	Solitary	Edible
Brown	Tapering	Yes	1
Brown	Enlarging	Yes	1
Brown	Enlarging	No	0
Brown	Enlarging	No	0
Brown	Tapering	Yes	1
Red	Tapering	Yes	0
Red	Enlarging	No	0
Brown	Enlarging	Yes	1
Red	Tapering	No	1
Brown	Enlarging	No	0

- You have 10 examples of mushrooms. For each example, you have
 - Three features
 - * Cap Color (Brown or Red),
 - * Stalk Shape (Tapering (as in \/) or Enlarging (as in /\)), and
 - * Solitary (Yes or No)
 - Label
 - * Edible (1 indicating yes or 0 indicating poisonous)

3.1 One hot encoded dataset For ease of implementation, we have one-hot encoded the features (turned them into 0 or 1 valued features)

Brown Cap	Tapering Stalk Shape	Solitary	Edible
1	1	1	1
1	0	1	1
1	0	0	0
1	0	0	0
1	1	1	1
0	1	1	0
0	0	0	0

Brown Cap	Tapering Stalk Shape	Solitary	Edible
1	0	1	1
0	1	0	1
1	0	0	0

Therefore, - X_train contains three features for each example - Brown Color (A value of 1 indicates "Brown" cap color and 0 indicates "Red" cap color) - Tapering Shape (A value of 1 indicates "Tapering Stalk Shape" and 0 indicates "Enlarging" stalk shape) - Solitary (A value of 1 indicates "Yes" and 0 indicates "No")

- y_train is whether the mushroom is edible
 - -y = 1 indicates edible
 - -y = 0 indicates poisonous

```
[2]: X_train = np.

array([[1,1,1],[1,0,1],[1,0,0],[1,0,0],[1,1,1],[0,1,1],[0,0,0],[1,0,1],[0,1,0])

y_train = np.array([1,1,0,0,1,0,0,1,1,0])
```

View the variables Let's get more familiar with your dataset.

- A good place to start is to just print out each variable and see what it contains.

The code below prints the first few elements of X_train and the type of the variable.

```
[3]: print("First few elements of X_train:\n", X_train[:5]) print("Type of X_train:",type(X_train))
```

First few elements of X_train:

[[1 1 1]

[1 0 1]

[1 0 0]

[1 0 0]

[1 1 1]]

Type of X_train: <class 'numpy.ndarray'>

Now, let's do the same for y_train

```
[4]: print("First few elements of y_train:", y_train[:5]) print("Type of y_train:",type(y_train))
```

```
First few elements of y_train: [1 1 0 0 1]
Type of y_train: <class 'numpy.ndarray'>
```

Check the dimensions of your variables Another useful way to get familiar with your data is to view its dimensions.

Please print the shape of X_train and y_train and see how many training examples you have in your dataset.

```
[5]: print ('The shape of X_train is:', X_train.shape)
print ('The shape of y_train is: ', y_train.shape)
print ('Number of training examples (m):', len(X_train))
```

```
The shape of X_train is: (10, 3)
The shape of y_train is: (10,)
Number of training examples (m): 10
```

4 - Decision Tree Refresher

In this practice lab, you will build a decision tree based on the dataset provided.

- Recall that the steps for building a decision tree are as follows:
 - Start with all examples at the root node
 - Calculate information gain for splitting on all possible features, and pick the one with the highest information gain
 - Split dataset according to the selected feature, and create left and right branches of the tree
 - Keep repeating splitting process until stopping criteria is met
- In this lab, you'll implement the following functions, which will let you split a node into left and right branches using the feature with the highest information gain
 - Calculate the entropy at a node
 - Split the dataset at a node into left and right branches based on a given feature
 - Calculate the information gain from splitting on a given feature
 - Choose the feature that maximizes information gain
- We'll then use the helper functions you've implemented to build a decision tree by repeating the splitting process until the stopping criteria is met
 - For this lab, the stopping criteria we've chosen is setting a maximum depth of 2

4.1 Calculate entropy

First, you'll write a helper function called <code>compute_entropy</code> that computes the entropy (measure of impurity) at a node. - The function takes in a numpy array (y) that indicates whether the examples in that node are edible (1) or poisonous(0)

Complete the compute_entropy() function below to: * Compute p_1 , which is the fraction of examples that are edible (i.e. have value = 1 in y) * The entropy is then calculated as

$$H(p_1) = -p_1 \log_2(p_1) - (1 - p_1) \log_2(1 - p_1)$$

* Note * The log is calculated with base 2 * For implementation purposes, $0\log_2(0) = 0$. That is, if $p_1 = 0$ or $p_1 = 1$, set the entropy to 0 * Make sure to check that the data at a node is not empty (i.e. len(y) != 0). Return 0 if it is

Exercise 1

Please complete the compute_entropy() function using the previous instructions.

If you get stuck, you can check out the hints presented after the cell below to help you with the implementation.

```
[8]: # UNQ_C1
     # GRADED FUNCTION: compute_entropy
     from math import log2
     def compute_entropy(y):
         11 11 11
         Computes the entropy for
         Args:
            y (ndarray): Numpy array indicating whether each example at a node is
                edible (`1`) or poisonous (`0`)
         Returns:
             entropy (float): Entropy at that node
         11 11 11
         # You need to return the following variables correctly
         entropy = 0.
         ### START CODE HERE ###
         # Count the number of examples
         total_examples = len(y)
         # Count the number of edible and poisonous mushrooms
         count_edible = np.sum(y)
         count_poisonous = total_examples - count_edible
         # Calculate the proportions
         p_edible = count_edible / total_examples
         p_poisonous = count_poisonous / total_examples
         # Calculate entropy
         if p_edible != 0 and p_poisonous != 0:
             entropy = - p_edible * log2(p_edible) - p_poisonous * log2(p_poisonous)
         ### END CODE HERE ###
         return entropy
```

- To calculate p1 * You can get the subset of examples in y that have the value 1 as y[y == 1] * You can use len(y) to get the number of examples in y
 - To calculate entropy

- * np.log2 let's you calculate the logarithm to base 2 for a numpy array
- * If the value of p1 is 0 or 1, make sure to set the entropy to 0

Click for more hints

 $-\,$ Here's how you can structure the overall implementation for this function

```
def compute_entropy(y):
```

```
# You need to return the following variables correctly
entropy = 0.

### START CODE HERE ###

if len(y) != 0:
    # Your code here to calculate the fraction of edible examples (i.e with value = p1 =

# For p1 = 0 and 1, set the entropy to 0 (to handle OlogO)

if p1 != 0 and p1 != 1:
    # Your code here to calculate the entropy using the formula provided above entropy =
    else:
        entropy = 0.

### END CODE HERE ###
```

return entropy

If you're still stuck, you can check the hints presented below to figure out how to calculate p1 and entropy.

```
Hint to calculate p1 You can compute p1 as p1 = len(y[y == 1]) / len(y)

Hint to calculate entropy (1 - p1) * np.log2(1 - p1) You can compute entropy as entropy = -p1 * np.log2(p1) -
```

You can check if your implementation was correct by running the following test code:

```
[9]: # Compute entropy at the root node (i.e. with all examples)
# Since we have 5 edible and 5 non-edible mushrooms, the entropy should be 1"

print("Entropy at root node: ", compute_entropy(y_train))

# UNIT TESTS
compute_entropy_test(compute_entropy)
```

```
Entropy at root node: 1.0 All tests passed.
```

Expected Output:

Entropy at root node: 1.0

4.2 Split dataset

Next, you'll write a helper function called split_dataset that takes in the data at a node and a feature to split on and splits it into left and right branches. Later in the lab, you'll implement code to calculate how good the split is.

- The function takes in the training data, the list of indices of data points at that node, along with the feature to split on.
- It splits the data and returns the subset of indices at the left and the right branch.
- For example, say we're starting at the root node (so node_indices = [0,1,2,3,4,5,6,7,8,9]), and we chose to split on feature 0, which is whether or not the example has a brown cap.
 - The output of the function is then, left_indices = [0,1,2,3,4,7,9] (data points with brown cap) and right_indices = [5,6,8] (data points without a brown cap)

	Brown Cap	Tapering Stalk Shape	Solitary	Edible
0	1	1	1	1
1	1	0	1	1
2	1	0	0	0
3	1	0	0	0
4	1	1	1	1
5	0	1	1	0
6	0	0	0	0
7	1	0	1	1
8	0	1	0	1
9	1	0	0	0

Exercise 2

Please complete the split_dataset() function shown below

- For each index in node_indices
 - If the value of X at that index for that feature is 1, add the index to left_indices
 - If the value of X at that index for that feature is 0, add the index to right_indices

If you get stuck, you can check out the hints presented after the cell below to help you with the implementation.

```
feature (int):
                             Index of feature to split on
Returns:
    left_indices (list): Indices with feature value == 1
    right_indices (list): Indices with feature value == 0
# You need to return the following variables correctly
left indices = []
right_indices = []
### START CODE HERE ###
if isinstance(node indices, int):
    node_indices = [node_indices] # Convert to a list if it is an integer
for index in node_indices:
    if X[index][feature] == 1:
        left_indices.append(index)
    else:
        right_indices.append(index)
### END CODE HERE ###
return left_indices, right_indices
```

• Here's how you can structure the overall implementation for this function "'python def split_dataset(X, node_indices, feature):

```
# You need to return the following variables correctly
left_indices = []
right_indices = []

### START CODE HERE ###

# Go through the indices of examples at that node
for i in node_indices:
    if # Your code here to check if the value of X at that index for the feature is 1
        left_indices.append(i)
    else:
        right_indices.append(i)

### END CODE HERE ###

return left_indices, right_indices "'
Click for more hints

The condition is if X[i][feature] == 1:.
```

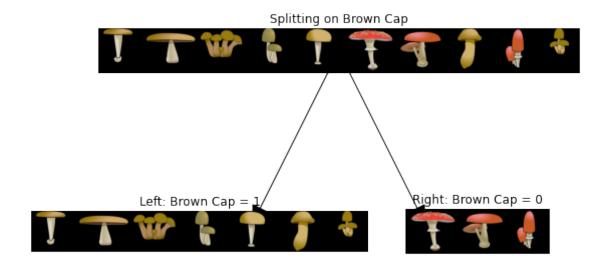
Now, let's check your implementation using the code blocks below. Let's try splitting the dataset at the root node, which contains all examples at feature 0 (Brown Cap) as we'd discussed above. We've also provided a helper function to visualize the output of the split.

```
[48]: # Case 1
      root_indices = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
      # Feel free to play around with these variables
      # The dataset only has three features, so this value can be 0 (Brown Cap), 1_{\sqcup}
      → (Tapering Stalk Shape) or 2 (Solitary)
      feature = 0
      left_indices, right_indices = split_dataset(X_train, root_indices, feature)
      print("CASE 1:")
      print("Left indices: ", left_indices)
      print("Right indices: ", right_indices)
      # Visualize the split
      generate_split_viz(root_indices, left_indices, right_indices, feature)
      print()
      # Case 2
      root_indices_subset = [0, 2, 4, 6, 8]
      left_indices, right_indices = split_dataset(X_train, root_indices_subset,__
       →feature)
      print("CASE 2:")
      print("Left indices: ", left_indices)
      print("Right indices: ", right_indices)
      # Visualize the split
      generate_split_viz(root_indices_subset, left_indices, right_indices, feature)
      # UNIT TESTS
      split_dataset_test(split_dataset)
```

CASE 1:

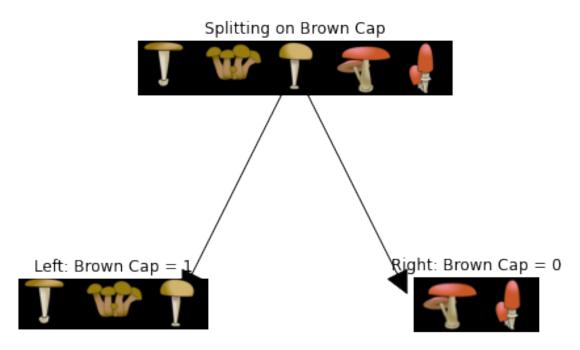
Left indices: [0, 1, 2, 3, 4, 7, 9]

Right indices: [5, 6, 8]



CASE 2:

Left indices: [0, 2, 4] Right indices: [6, 8]



All tests passed.

Expected Output:

CASE 1:

```
Left indices: [0, 1, 2, 3, 4, 7, 9]
Right indices: [5, 6, 8]

CASE 2:
Left indices: [0, 2, 4]
Right indices: [6, 8]
```

4.3 Calculate information gain

Next, you'll write a function called information_gain that takes in the training data, the indices at a node and a feature to split on and returns the information gain from the split.

```
### Exercise 3
```

Please complete the compute_information_gain() function shown below to compute

```
Information Gain = H(p_1^{\text{node}}) - (w^{\text{left}}H(p_1^{\text{left}}) + w^{\text{right}}H(p_1^{\text{right}}))
```

where - $H(p_1^{\text{node}})$ is entropy at the node - $H(p_1^{\text{left}})$ and $H(p_1^{\text{right}})$ are the entropies at the left and the right branches resulting from the split - w^{left} and w^{right} are the proportion of examples at the left and right branch, respectively

Note: - You can use the compute_entropy() function that you implemented above to calculate the entropy - We've provided some starter code that uses the split_dataset() function you implemented above to split the dataset

If you get stuck, you can check out the hints presented after the cell below to help you with the implementation.

```
[49]: # UNQ_C3
      # GRADED FUNCTION: compute_information_gain
      def compute_information_gain(X, y, node_indices, feature):
          Compute the information of splitting the node on a given feature
          Args:
                                       Data matrix of shape(n_samples, n_features)
              X (ndarray):
                                       list or ndarray with n samples containing the
              y (array like):
       \hookrightarrow target variable
              node_indices (ndarray): List containing the active indices. I.e, the \Box
       ⇒samples being considered in this step.
          Returns:
              cost (float): Cost computed
          11 11 11
          # Split dataset
          left_indices, right_indices = split_dataset(X, node_indices, feature)
```

```
# Some useful variables
  X_node, y_node = X[node_indices], y[node_indices]
  X_left, y_left = X[left_indices], y[left_indices]
  X_right, y_right = X[right_indices], y[right_indices]
   # You need to return the following variables correctly
  information_gain = 0
   ### START CODE HERE ###
   # Compute entropy of the current node
  entropy_node = compute_entropy(y_node)
   # Compute entropy of the left child node
  entropy_left = compute_entropy(y_left)
   # Compute entropy of the right child node
  entropy_right = compute_entropy(y_right)
   # Calculate the proportion of samples in the left and right child nodes
  p_left = len(left_indices) / len(node_indices)
  p_right = len(right_indices) / len(node_indices)
   # Calculate information gain
   information_gain = entropy_node - (p_left * entropy_left) - (p_right *_u
→entropy_right)
   # Handle the case when information gain is NaN
  if np.isnan(information_gain):
       information_gain = 0.0
  ### END CODE HERE ###
  return information_gain
```

• Here's how you can structure the overall implementation for this function "'python def compute_information_gain(X, y, node_indices, feature): # Split dataset left_indices, right_indices = split_dataset(X, node_indices, feature)

```
# Some useful variables
X_node, y_node = X[node_indices], y[node_indices]
X_left, y_left = X[left_indices], y[left_indices]
X_right, y_right = X[right_indices], y[right_indices]
```

```
# You need to return the following variables correctly
           information_gain = 0
           ### START CODE HERE ###
           # Your code here to compute the entropy at the node using compute entropy()
           node entropy =
           # Your code here to compute the entropy at the left branch
           left entropy =
           # Your code here to compute the entropy at the right branch
           right_entropy =
           # Your code here to compute the proportion of examples at the left branch
           w left =
           # Your code here to compute the proportion of examples at the right branch
           w_right =
           # Your code here to compute weighted entropy from the split using
           # w_left, w_right, left_entropy and right_entropy
           weighted entropy =
           # Your code here to compute the information gain as the entropy at the node
           # minus the weighted entropy
           information_gain =
           ### END CODE HERE ###
           return information_gain
          "' If you're still stuck, check out the hints below.
          Hint to calculate the entropies
          node entropy = compute entropy(y node) left entropy = compute entropy(y left)
          right entropy = compute entropy(y right)
          Hint to calculate w_left and w_right w_left = len(X_left) / len(X_node) w_right =
          len(X right) / len(X node)
          Hint to calculate weighted_entropy weighted_entropy = w_left * left_entropy + w_right *
          right_entropy
          Hint to calculate information_gain information_gain = node_entropy - weighted_entropy
     You can now check your implementation using the cell below and calculate what the information
     gain would be from splitting on each of the featues
[50]: info_gain0 = compute_information_gain(X_train, y_train, root_indices, feature=0)
      print("Information Gain from splitting the root on brown cap: ", info_gain0)
```

info_gain1 = compute_information_gain(X_train, y_train, root_indices, feature=1)

Information Gain from splitting the root on brown cap: 0.03485155455967709 Information Gain from splitting the root on tapering stalk shape: 0.12451124978365324 Information Gain from splitting the root on solitary: 0.2780719051126377 All tests passed.

Expected Output:

Information Gain from splitting the root on brown cap: 0.034851554559677034

Information Gain from splitting the root on tapering stalk shape: 0.12451124978365313

Information Gain from splitting the root on solitary: 0.2780719051126377

Splitting on "Solitary" (feature = 2) at the root node gives the maximum information gain. Therefore, it's the best feature to split on at the root node.

4.4 Get best split Now let's write a function to get the best feature to split on by computing the information gain from each feature as we did above and returning the feature that gives the maximum information gain

Exercise 4 Please complete the get_best_split() function shown below. - The function takes in the training data, along with the indices of datapoint at that node - The output of the function is the feature that gives the maximum information gain - You can use the compute_information_gain() function to iterate through the features and calculate the information for each feature If you get stuck, you can check out the hints presented after the cell below to help you with the implementation.

```
[51]: # UNQ_C4
# GRADED FUNCTION: get_best_split

def get_best_split(X, y, node_indices):
    """

    Returns the optimal feature and threshold value
    to split the node data

Args:
    X (ndarray): Data matrix of shape(n_samples, n_features)
    y (array like): list or ndarray with n_samples containing the_□
    →target variable
    node_indices (ndarray): List containing the active indices. I.e, the_□
    →samples being considered in this step.
```

```
Returns:
   best_feature (int):
                            The index of the best feature to split
# Some useful variables
num_features = X.shape[1]
# You need to return the following variables correctly
best feature = -1
### START CODE HERE ###
# Iterate over each feature
max_info_gain = 0
# Iterate through all features
for feature in range(num_features):
    # Compute the information gain from splitting on this feature
    info_gain = compute_information_gain(X, y, node_indices, feature)
    # If the information gain is larger than the max seen so far
    if info_gain > max_info_gain:
        # Update the max_info_gain and best_feature
        max_info_gain = info_gain
        best_feature = feature
### END CODE HERE ##
return best_feature
```

 $\bullet~$ Here's how you can structure the overall implementation for this function

def get_best_split(X, y, node_indices):

```
# Some useful variables
num_features = X.shape[1]

# You need to return the following variables correctly
best_feature = -1

### START CODE HERE ###
max_info_gain = 0

# Iterate through all features
```

for feature in range(num_features):

return best_feature

If you're still stuck, check out the hints below.

Hint to calculate info_gain

info_gain = compute_information_gain(X, y, node_indices, feature)

Hint to update the max_info_gain and best_feature max_info_gain = info_gain best feature = feature

Now, let's check the implementation of your function using the cell below.

```
[52]: best_feature = get_best_split(X_train, y_train, root_indices)
print("Best feature to split on: %d" % best_feature)

# UNIT TESTS
get_best_split_test(get_best_split)
```

```
Best feature to split on: 2 All tests passed.
```

As we saw above, the function returns that the best feature to split on at the root node is feature 2 ("Solitary")

```
## 5 - Building the tree
```

In this section, we use the functions you implemented above to generate a decision tree by successively picking the best feature to split on until we reach the stopping criteria (maximum depth is 2).

You do not need to implement anything for this part.

```
Build a tree using the recursive algorithm that split the dataset into 2 \sqcup
       \hookrightarrow subgroups at each node.
          This function just prints the tree.
          Args:
              X (ndarray):
                                      Data matrix of shape(n samples, n features)
                                     list or ndarray with n_samples containing the
              y (array like):
       \hookrightarrow target variable
              node\_indices (ndarray): List containing the active indices. I.e, the
       ⇒samples being considered in this step.
              branch_name (string): Name of the branch. ['Root', 'Left', 'Right']
              max_depth (int): Max depth of the resulting tree.
              current_depth (int): Current depth. Parameter used during recursive⊔
       \hookrightarrow call.
          11 11 11
          # Maximum depth reached - stop splitting
          if current_depth == max_depth:
              formatting = " "*current depth + "-"*current depth
              print(formatting, "%s leaf node with indices" % branch_name, __
       →node_indices)
              return
          # Otherwise, get best split and split the data
          # Get the best feature and threshold at this node
          best_feature = get_best_split(X, y, node_indices)
          formatting = "-"*current_depth
          print("%s Depth %d, %s: Split on feature: %d" % (formatting, current_depth, __
       →branch_name, best_feature))
          # Split the dataset at the best feature
          left_indices, right_indices = split_dataset(X, node_indices, best_feature)
          tree.append((left_indices, right_indices, best_feature))
          # continue splitting the left and the right child. Increment current depth
          build_tree_recursive(X, y, left_indices, "Left", max_depth, current_depth+1)
          build_tree_recursive(X, y, right_indices, "Right", max_depth, __
       [29]: build_tree_recursive(X_train, y_train, root_indices, "Root", max_depth=2,__
      generate_tree_viz(root_indices, y_train, tree)
      Depth O, Root: Split on feature: 2
```

- Depth 1, Left: Split on feature: 2

```
-- Left leaf node with indices [0, 1, 4, 5, 7]
 -- Right leaf node with indices []
- Depth 1, Right: Split on feature: 2
 -- Left leaf node with indices []
 -- Right leaf node with indices [2, 3, 6, 8, 9]
       ValueError
                                                  Traceback (most recent call_
→last)
        <ipython-input-29-a0c8eafbc9f8> in <module>
          1 build_tree_recursive(X_train, y_train, root_indices, "Root", __
→max_depth=2, current_depth=0)
   ---> 2 generate_tree_viz(root_indices, y_train, tree)
        ~/work/utils.py in generate_tree_viz(root_indices, y, tree)
                    indices_list = level[:2]
                    for indices in indices list:
        82
   ---> 83
                        G.add_node(idx,image= generate_node_image(indices))
                        G.add edge(root, idx)
         84
        85
        ~/work/utils.py in generate_node_image(node_indices)
                image_paths = ["images/%d.png" % idx for idx in node_indices]
         8
                images = [Image.open(x) for x in image_paths]
   ---> 9
               widths, heights = zip(*(i.size for i in images))
         10
         11
               total_width = sum(widths)
       ValueError: not enough values to unpack (expected 2, got 0)
```

Please click here if you want to experiment with any of the non-graded code.

Important Note: Please only do this when you've already passed the assignment to avoid problems with the autograder.

On the notebook's menu, click "View" > "Cell Toolbar" > "Edit Metadata"

Hit the "Edit Metadata" button next to the code cell which you want to lock/unlock

Set the attribute value for "editable" to:

[&]quot;true" if you want to unlock it