

Image Processing - 67829

Exercise 4: Panorama Registration & Stitching

Due date: 05.01.2023 at 23:59

Version 1.0 - Last update 07.12.2022

1 Overview

In this exercise you will be guided through the steps discussed in class to perform automatic "Stereo Mosaicking". The input of such an algorithm is a sequence of images scanning a scene from left to right (due to camera rotation and/or translation - we assume rigid transform between images), with significant overlap in the field of view of consecutive frames. This exercise covers the following steps:

- Registration: The geometric transformation between each consecutive image pair is found by detecting *Harris feature points*, extracting their *MOPS-like descriptors*, matching these descriptors between the pair and fitting a rigid transformation that agrees with a large set of inlier matches using the *RANSAC algorithm*.
- Stitching: Combining strips from aligned images into a sequence of panoramas. Global motion will be compensated, and the residual parallax, as well as other motions will become visible.

2 Background and Dependencies

You are given an outline of the code in the *ex4-impr-supplementary material.zip* file available to you on the Moodle. There are also some videos you can use to test your code. For this assignment you will need the functions `read_image` and `build_gaussian_pyramid` from the previous exercise (and `pyramid_blending` for the bonus). Include these and all of their dependencies in a file named `sol4_utils.py`, imported from your `sol4.py`. Don't forget to add this file to your submission. Nevertheless, the implementation of

these functions will not affect your grade, as we will use our own implementation when testing your code. Be sure not to use any other functions from `sol4_utils.py` as they will not exist in our implementation.

3 Image Pair Registration

In this section we will focus on computing the geometric transformation between a pair of consecutive frames, I_i and I_{i+1} , of some image sequence. For an example of such a frame pair, have a look at the example input image sequences provided in the supplementary images (*ex4-impr-supplementary material/external*). Although the provided input sequences are of RGB images, in the current registration phase we will only require I_i and I_{i+1} to be grayscale images (load them accordingly). To dump a video into a sequence of images use *FFmpeg* (more in the [tips section](#)), a usage example is provided in *example_panoramas.py*.

3.1 Feature point detection and descriptor extraction

As discussed in class, not all points in an image are good candidates for matching. To detect points in a frame that can be localized well and that will be likely reproduced in the consecutive frame we will use the *Harris corner detector*. To do so you will implement a function `harris_corner_detector` which gets a grayscale image and returns (x, y) locations that represent corners in the image. We will not implement the Scale Invariant version of the Harris Detector.

You should implement the following algorithm:

- Get the I_x and I_y derivatives of the image using the filters $[1, 0, -1]$, $[1, 0, -1]^T$ respectively.
- Blur the images: I_x^2 , I_y^2 , $I_x I_y$. You may use `blur_spatial` function from `sol4_utils.py` with `kernel_size=3`.
- Then, for each pixel you will have the following matrix M :

$$\begin{pmatrix} I_x^2 & I_x I_y \\ I_y I_x & I_y^2 \end{pmatrix}$$

- As you learned in class, the eigenvalues of this matrix tell us about the intensity changes of a window around this pixel, in a small neighborhood of the pixel. No intensity change means a constant gray level over the entire window. A big change in one direction (one large eigenvalue) means this window

contains an edge. A big change in two directions (two large eigenvalues) means that this window contains a corner. One way to measure how big are the two eigenvalues is

$$R = \det(M) - k(\text{trace}(M))^2$$

We will use $k = 0.04$.

- Finding R for every pixel results in a response image R . The corners are the local maximum points of R . To find these points you can use the supplied `non_maximum_suppression` function, which gets a response image as an input, thresholds out areas with low response and returns a binary image contains the local maximum points.
- Return the xy coordinates of the corners.

The function should implement the following API:

```
harris_corner_detector(im)
where
im — grayscale image to find key points inside.
Returns An array with shape (N,2) of [x,y] key point locations in im.
```

Note the coordinate order is (x,y), as opposed to the order when indexing an array which is (row, column)

We would prefer though that the feature positions we locate in each image are spread-out and not concentrated in one small region of the image (a region that happens to have a lot of texture and contrast). For this purpose you are provided with the `spread_out_corners` function. Have a look at it. This function splits the input image `im` into $n \times m$ approximately equal sub-images and runs your `harris_corner_detector` on each. `spread_out_corners` should be used in your code instead of calling `harris_corner_detector` directly. You are encouraged to experiment with the values of the `n` and `m` parameters but a good starting point should be `n=7` and `m=7`. To visualize the detected corner positions, display the image and then plot the points using `plt.scatter` or `plt.plot` with `'.'` (see [tips section](#)).

Now that we've detected feature points in two images, we would like to extract descriptors at their locations. The type of descriptor you are guided to implement here is a simplified version of the MOPS descriptor presented in class. To sample this descriptor at position $p = (x, y)$ in an image I we will first need to prepare a 3-level Gaussian pyramid $G_I[l]$ of this image, where the index l here is used to denote the level ($l = 0$ being the original image). The descriptor we will extract, denoted by d , is a 7×7 matrix

of normalized image intensities. These should be sampled in the third pyramid level image, $G_I[2]$, in a 7×7 patch centered around p_{l_3} , which is the location of the point $p = (x, y)$ in the 3rd level. In general you can transform point coordinates between any two pyramid levels l_i and l_j in the following way

$$p_{l_j} = (x_{l_j}, y_{l_j}) = 2^{l_i - l_j} p_{l_i} = 2^{l_i - l_j} (x_{l_i}, y_{l_i}) \quad (1)$$

Note that the coordinates at which we would like to sample this 7×7 patch at level 3 of the pyramid won't necessarily be integer valued. You will therefore need to sample them at these sub-pixel coordinates by interpolating within the pyramid's 3rd level image properly. To do this use `map_coordinates` from `scipy.ndimage` (see [tips section](#)). Once this 7×7 intensity matrix has been sampled we would like to normalize it so that the resulting descriptor is invariant to certain changes of lighting. Denoting by \tilde{d} the sampled descriptor matrix, the final descriptor matrix is $d = (\tilde{d} - \mu) / \|\tilde{d} - \mu\|$ where μ is the mean \tilde{d} and $\|\cdot\|$ is the euclidean norm operation (use `np.linalg.norm`) (in cases where the norm is zero you may simply return the zero descriptor).

Descriptor sampling should be implemented in the `sample_descriptor` function having the following interface

```
sample_descriptor(im, pos, desc_rad)
```

where

`im` — grayscale image to sample within.

`pos` — An array with shape (N,2) of [x,y] positions to sample descriptors in `im`.

`desc_rad` — "Radius" of descriptors to compute (see below).

Returns A 3D array with shape (N,K,K) containing the `i`th descriptor at `desc[i,:]`. The per-descriptor dimensions KxK are related to the `desc_rad` argument as follows $K = 1 + 2 * \text{desc_rad}$.

Note that `sample_descriptor` already expects the grayscale image `im` to be the 3rd level pyramid image. Note also that to obtain 7×7 descriptors, `desc_rad` should be set to 3.

The `sample_descriptor` function should be called by a wrapper function you will implement called `find_features` which has the following interface

```
find_features (pyr)
```

`pyr` — Gaussian pyramid of a grayscale image having (at least) 3 levels.

Returns a Python list containing:

- 1) An array with shape (N,2) of [x,y] feature location per row found in the image. These coordinates are provided at the pyramid level `pyr[0]`.
- 2) A feature descriptor array with shape (N,K,K).

This function is responsible for both the feature detection and the descriptor extraction. `find_features` detects feature points in the pyramid and samples their descriptors. This function should call the func-

tions `spread_out_corners` for getting the keypoints, and `sample_descriptor` for sampling a descriptor for each keypoint.

3.2 Matching descriptors

After obtaining the descriptor matrices D_i and D_{i+1} (the *desc* matrices returned by `find_features`) extracted from images I_i and I_{i+1} , we would now like to match features in one frame to the corresponding features in the other. Note that the number of features in D_i detected in frame i will in general differ from the number of features in D_{i+1} detected in frame $i+1$. We denote by $D_{i,j}$ the j th feature descriptor detected in the i th frame. The match score we choose between two descriptors will simply be their dot-product (flattened to 1D arrays). Therefore $S_{j,k} = D_{i,j} \cdot D_{i+1,k}$ would be the match score between the j th descriptor in frame i and the k th descriptor in frame $i+1$. We will say that descriptors $D_{i,j}$ and $D_{i+1,k}$ match if the following three properties hold

- $S_{j,k} \geq 2_{ndmax}\{S_{j,l} \mid l \in \{0..f_1 - 1\}\}$ where f_1 is the number of features in frame $i+1$. Explanation: $S_{j,k}$ is in the best 2 features that match feature j in image i , from all features in image $i+1$.
- $S_{j,k} \geq 2_{ndmax}\{S_{l,k} \mid l \in \{0..f_0 - 1\}\}$ where f_0 is the number of features in frame i . Explanation: $S_{j,k}$ is in the best 2 features that match feature k in image $i+1$, from all features in image i .
- $S_{j,k}$ is greater ($>$) than some predefined minimal score (called `min_score` in the following).

Note that these dot-products are necessarily in the range $[-1,1]$ because of the way we normalized the descriptors. You should tweak the `min_score` parameter until you find that you're obtaining good matches. A good value to start with is `min_score=0.5`. In general, reasonable values would be in the range $[0,1)$. The function `match_features` performing this matching procedure should be implemented with the following interface

```
match_features (desc1, desc2, min_score)
where
desc1 — A feature descriptor array with shape (N1,K,K).
desc2 — A feature descriptor array with shape (N2,K,K).
min_score — Minimal match score between two descriptors required to be regarded as corresponding points.
Returns a Python list containing:
    1) Array with shape (M,) and dtype int of matching indices in desc1.
    2) Array with shape (M,) and dtype int of matching indices in desc2.
```

It will match feature descriptors in desc1 and desc2.

Note:

- The descriptors of the j th match are `desc1[match_ind1[j], :, :]` in image I_i and `desc2[match_ind2[j], :, :]` in image I_{i+1} .
- The number of feature descriptors N_1 generally differs from N_2 .
- The value of M depends on the actual number of corresponding pairs your algorithm will find in the images.

3.3 Registering the transformation

We will now use the feature point matches found above to compute the most fitting homography that transforms I_i to the coordinate system of I_{i+1} . To do this we will first need to implement a function that applies a homography transformation on a set of points. This is the `apply_homography` function you are required to implement

```
apply_homography(pos1, H12)
```

where

`pos1` — An array with shape $(N,2)$ of $[x,y]$ point coordinates.

`H12` — A 3×3 homography matrix.

Returns an array with the same shape as `pos1` with $[x,y]$ point coordinates in image $i+1$ obtained from transforming `pos1` using `H12`.

As a reminder to how homographies transform points - given a point (x_1, y_1) in coordinate system 1 and a homography matrix $H_{1,2}$, then `apply_homography` will transform this point to (x_2, y_2) in coordinate system 2 in the following way

$$\begin{bmatrix} \tilde{x}_2 \\ \tilde{y}_2 \\ \tilde{z}_2 \end{bmatrix} = H_{1,2} \begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix} \quad (2)$$

$$\begin{bmatrix} x_2 \\ y_2 \end{bmatrix} = \begin{bmatrix} \tilde{x}_2 \\ \tilde{y}_2 \end{bmatrix} / \tilde{z}_2 \quad (3)$$

Note that $\tilde{z}_2 = 0$ means the point (x_1, y_1) is transformed to the infinity, it is not likely to happen with relatively small camera rotations as the ones we will have. It may occur however when applying a homography computed from incorrect point correspondences. Don't worry about how to normalize such points as they will be considered outliers by the RANSAC procedure mentioned next.

We will now use `apply_homography` in our RANSAC (Random Sample Consensus) homography fitting code. Let's first recall how RANSAC operates. Given 2 sets of N matched points P_1 and P_2 s.t. $P_{1,j}$

are the x-y coordinates of the j th match in image 1 and $P_{2,j}$ are the x-y coordinates of the j th match in image 2. **We will estimate a rigid transform = rotation and translation of image points.**

- Pick a random set of 2 point matches from the supplied N point matches. Let's denote their indices by J . We call these two sets of 2 points in the two images $P_{1,J}$ and $P_{2,J}$.
- Compute the homography $H_{1,2}$ that transforms the 2 points $P_{1,J}$ to the 2 points $P_{2,J}$. As discussed in class, there is a closed form solution for that. To simplify matters you have been provided with the `estimate_rigid_transform` function that performs this step. This function returns a 3x3 homography matrix which performs the rigid transformation.
- For a camera which is mostly translating (i.e a lot of parallax) it is sometimes better to estimate only translation with no rotation, use `translation_only = True` in that case. You will only need one pair of points in each ransac iteration if you estimate only translation.
- Use $H_{1,2}$ to transform the set of points P_1 in image 1 to the transformed set P'_2 (using the above `apply_homography`) and compute the squared euclidean distance $E_j = ||P'_{2,j} - P_{2,j}||^2$ for $j = 0..N - 1$. Mark all matches having $E_j < \text{inlier_tol}$ as inlier matches and the rest as outlier matches for some constant threshold `inlier_tol`.

RANSAC performs several iterations (later denoted `num_iters`) of these 3 steps, keeping a record of the largest set of inliers J_{in} it has come upon. Once these iterations are complete the homography is recomputed over the matches J_{in} . To do this you will simply need to rerun `estimate_rigid_transform` on these inlier point matches $P_{1,J_{in}}$ and $P_{2,J_{in}}$ and obtain the final least squares fit of the homography over the largest inlier set. Your RANSAC implementation should have the following interface

```
ransac_homography(pos1, pos2, num_iters, inlier_tol, translation_only=False)
```

where

`pos1, pos2` — Two Arrays, each with shape (N,2) containing N rows of [x,y] coordinates of matched points.

`num_iters` — Number of RANSAC iterations to perform.

`inlier_tol` — inlier tolerance threshold.

`translation_only` — whether to compute translation only. False (**default**) to compute rotation as well.

Returns a Python list containing:

1) A 3x3 normalized homography matrix.

2) An Array with shape (S,) where S is the number of inliers, containing the indices in `pos1/pos2` of the maximal set of inlier matches found.

To visualize the full set of point matches and the inlier matches detected by RANSAC implement the following display function

```
display_matches(im1, im2, pos1, pos2, inliers)
```

`im1, im2` — two grayscale images

`pos1, pos2` — Two arrays with shape (N,2) each, containing N rows of [x,y] coordinates of matched points in `im1` and `im2` (i.e. the match of the *i*th coordinate is `pos1[i,:]` in `im1` and `pos2[i,:]` in `im2`).

`inliers` — An array with shape (S,) of inlier matches (e.g. see output of `ransac_homography`)

This function should display a horizontally concatenated image (use `np.hstack` of an image pair `im1` and `im2`, with the matched points provided in `pos1` and `pos2` overlaid correspondingly as red dots. Each outlier match, say at index *j*, is denoted by plotting a blue line between `pos1[j,:]` and the horizontally shifted `pos2[j,:]`. Similarly, inlier matches are denoted by plotting a yellow line between the matched points (see section [tips section](#) for tips). As an example of how the output should look like, below is the figure resulting from running `display_matches` on an image pair on one of the provided example sequences together with its point matches `pos1, pos2` (obtained from `find_features + match_features`) and inlier index set `inliers` obtained from `ransac_homography`.



This figure shows the large number of outlier matches the RANSAC algorithm had to deal with. As opposed to the set of outliers (shown in blue) the inlier set (shown in yellow) shows a more consistent motion. Also note that although many features detected in the cloud texture were probably matched correctly, these were marked as outliers. This is probably due to the fact that the clouds had enough time to move between these two shots, and due to the value of `inlier_tol`. Your results will differ from the above example due to the random nature of RANSAC.

Our efforts so far eventually provided us with the set of registered homographies $H_{i,i+1}$, for $i = 0..M - 2$, between consecutive frames in a given image sequence of M frames I_i . We would now like to use these homographies to align the M frames to a common coordinate system.

3.4 Transforming to a common coordinate system

The first stage in doing this is to pick a coordinate system in which we would like the panorama to be rendered. We will (somewhat arbitrarily) choose this coordinate system to be the coordinate system of the middle frame I_m in our image sequence, where $m = (M-1)//2$. What we mean by this is that the resulting panorama image will be composed of frame I_m with all the other frames back-warped so that they properly align with it. To achieve this we will need to translate the set of homographies $H_{i,i+1}$ that transform image coordinates in frame I_i to frame I_{i+1} into a different set of homographies $\bar{H}_{i,m}$ that transform image coordinates in frame I_i to this middle frame I_m .

First we note that given 2 homography matrices $H_{a,b}$ and $H_{b,c}$ and a point p_a in coordinate system a , we can transform the point to coordinate system c by first operating with homography $H_{a,b}$ to obtain an intermediate point p_b in system b and then by operating with homography $H_{b,c}$ to obtain p_c in system c . Each time we operate with a homography H on a point $p = (x, y)$ we do two things: first we multiply the homogeneous column 3-vector $\tilde{p} = (x, y, 1)^T$ from the left by H and then we re-normalize to keep the 3rd element equal to 1. When we operated on p_a first with $H_{a,b}$ and then with $H_{b,c}$ we could have equally well multiplied the homogeneous vector \tilde{p}_a once from the left by the matrix $H_{b,c}H_{a,b}$ and then normalized only once at the very end. We see then that multiplying the homography matrices $H_{a,b}$ and $H_{b,c}$ has produced a new homography matrix $H_{a,c} = H_{b,c}H_{a,b}$ that now transforms points from coordinate system a directly to c .

We may now use this property of homographies to obtain $\bar{H}_{i,m}$ from $\{H_{i,i+1} : i = 0..M-1\}$. We do this as follows

- For $i < m$ we set $\bar{H}_{i,m} = H_{m-1,m} * \dots * H_{i+1,i+2} * H_{i,i+1}$
- For $i > m$ we set $\bar{H}_{i,m} = H_{m,m+1}^{-1} * \dots * H_{i-2,i-1}^{-1} * H_{i-1,i}^{-1}$
- For $i = m$ we set $\bar{H}_{i,m}$ to the 3×3 identity matrix $I = \text{np.eye}(3)$

This procedure should be implemented in the following function

```
accumulate_homographies(H_successive, m)
```

where

$H_{\text{successive}}$ — A list of $M-1$ 3×3 homography matrices where $H_{\text{successive}}[i]$ is a homography that transforms points from coordinate system i to coordinate system $i+1$.

m — Index of the coordinate system we would like to accumulate the given homographies towards.

Returns A list of M 3×3 homography matrices, where $H2m[i]$ transforms points from coordinate system i to coordinate system m .

Note: In this exercise homography matrices should always maintain the property that $H[2,2]=1$. This should be done by normalizing them as follows before using them to perform transformations $H \leftarrow H[2,2]$. In this function's interface the list of homographies `H_successive` corresponds in the above discussion to the set of homographies $H_{i,i+1}$ and the returned list corresponds to the set $\bar{H}_{i,m}$.

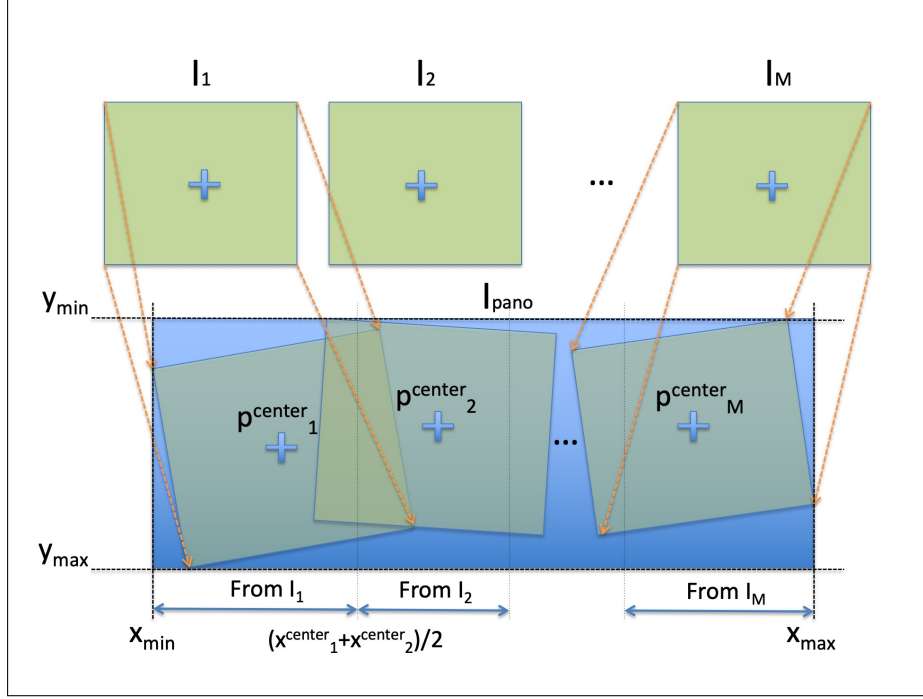
4 Stitching

4.1 Rendering the panoramas

Now that we have the set of M homographies $\bar{H}_{i,m}$ transforming pixel coordinates in frame I_i to the panorama coordinate system (all panoramas share the same coordinate system). We now proceed to describing the way in which a panorama frame I_{pano} is rendered. First we will need to define where we want I_{pano} to be rendered. We would like this region to be large enough to include all pixels from all frames I_i . To do so we compute where the 4 corner pixel coordinates (top-left, top-right, bottom-right, bottom-left) of each frame I_i get mapped to by $\bar{H}_{i,m}$, denoting these positions in the panorama coordinate system by $p_i^{corner_k}$ where $k = 1..4$. The coordinates of a rectangle bounding the set of $4 * M$ corners $p_i^{corner_k}$ denoted $x_{max}, x_{min}, y_{max}, y_{min}$, will then define the region in which the panorama image I_{pano} should be rendered. For that, you will implement the following function:

```
compute_bounding_box (homography, w, h)
where
homography — A 3x3 homography matrix transforming an image to common coordinate system.
w,h — width and height of the image.
Returns a 2x2 array of type np.int, where the first row is [x,y] of the top left corner, and the second row is the [x,y] of the
bottom right corner.
```

We will now define what parts of I_{pano} should be obtained from which frame I_i . We divide the panorama to M vertical strips, each covering a portion of the full lateral range $[x_{min}, x_{max}]$. The boundaries between these strips are taken to be the following $M - 1$ x -coordinates: $(x_i^{center} + x_{i+1}^{center})/2$ for all $i = 0..M - 2$, where we denote by x_i^{center} the x -coordinate of the center of the i th image strip p_i^{center} in the panorama coordinate system (obtained again using $\bar{H}_{i,m}$). This division of the panorama to vertical strips is shown in the following figure. Every panorama I_{pano} is constructed by combining strips taken around different x values. For example if the image size is $640x480$ and we would like to create a sequence of 9 panoramas, we will take strips around (64, 128, 192, ..., 576)



Back-warping of the strips should then be performed as follows. Initially, for an input image prepare coordinate strips X_{coord} and Y_{coord} using the function `np.meshgrid` to hold the x and y coordinates of each of the warped image. Recall that these should be in the bounding box calculated by `compute_bounding_box`.

Now, the coordinate mesh created for this image, denoted X^i and Y^i should be transformed by the **inverse** homography $\bar{H}_{i,m}^{-1}$ using `apply_homography back` to the coordinate system of frame i . We call these X^{ri} and Y^{ri} . These back-warped coordinates can now be used to interpolate the image with `map_coordinates`. The interpolated pixel values for the three channels are combined to an RGB image by `warp_image`. You are required to implement

```
warp_channel (image, homography)
where
image — a 2D image.
param homography: homography with which to warp the image.
Returns A 2d warped image.
```

4.2 Stitching

The method `generate_panoramic_images` uses the warped images to populate the panoramas. It places strips from images according to their relative location calculated from their bounding boxes.

4.3 Crop

We don't want to use strips with less than *The number_of_panoramas* different views. Therefore we crop the panoramas such that the first and last frames are entirely cropped out. It ensures the leftmost strip of the panorama is taken from the rightmost strip of some input image, and vice versa for the other side.

5 Tying it all Together

To ease the development burden, the main class, `PanoramicVideoGenerator` responsible for all the house-keeping has been provided. Its two main functions are `align_images` and `generate_panoramic_images`. `align_images` essentially goes through the following steps:

- Find feature points and sample their descriptors (using your `gaussian_pyramid` and `find_features`).
- Match feature points (using your `match_features`).
- Register rigid transform between pairs of images (using your `ransac_homography`).
- Display inlier and outlier matches for the result of `ransac_homography` function (using your `display_matches`). Uncomment for debugging.
- Transform the homographies (using your `accumulate_homographies`).
- Discard images where the motion is too small.

Have a look at `generate_panoramic_images`'s code so that you understand its flow. Once your implementation is complete you can also execute the provided `example_panoramas.py`. This script generates two stereo panoramas, one with translation and rotation, and one with translation only. Check the output videos to verify your results.

You are allowed to alter the given functions as long as they still function as described in this definition to generate panoramas. More specifically you may choose to alter any predefined values for the constants used throughout this exercise, which you are encouraged to change to suite your needs.

6 Your Panorama

You should submit with your exercise one video in the folder *videos*. This video should be taken from a mostly rotating camera, or from a camera moving to the right, while not rotating. This video should be less than 500 frames, and its resolution should not be larger than HD. We suggest use smaller resolution

for your experiments. When you start recording, the region of interest should be just a little to the right of the camera's field of view. Move or rotate to right, until the region of interest is completely out to the left side of the field of view. Also submit a script called `my_panorama.py` which operates in a similar manner to `example_panoramas.py` and that produces a panoramic video out of your input video. It should not plot any figures. Don't include the videos we provided in your submission.

7 Bonus - 10 points

Use your `pyramid_blending` function from ex3, for blending panoramas. We want you to think how you can do that given the image strips from the input images. In particular think what should be the relation between the width of the overlap between input images and the size of the kernel used in `pyramid_blending`.

Place the code for the bonus in the function `generate_panoramic_images_bonus` (you can copy and change whatever code you need from `generate_panoramic_images_normal`).

You should also add an additional input video of your own for the bonus section. Make sure that the names of the files include the word 'bonus', e.g. - 'my_bonus_panorama.mp4'.

Last, describe your solution in a file named `bonus.txt`.

Important! A very slow solution will not get points for the bonus.

Important! The bonus videos will also only be shown to the graders if both the `bonus.txt` file exists and some videos have 'bonus' in their name.

8 Tips & Guidelines

- Start early. This is the largest exercise and it will also be weighted accordingly in the final grade.
- FFmpeg is a CLI based open-source project consisting of a large suite of libraries and programs for handling video, audio, and other multimedia files and streams. In this exercise you will use it to dump a video into a sequence of images use, a usage example is provided in `example_panoramas.py`. To install FFmpeg please refer to <https://ffmpeg.org/download.html>.
- **Write efficient code.** Slow code is very hard to debug. the sequences contain tens to hundreds of images, if it takes your code more than about a second per frame it will be hard to detect mistakes. However, We will not reduce points unless it's extremely slow.

- If your code is slow use timers (e.g PyCharm Profiler) to analyze it and identify the bottleneck. Avoid unnecessary loops, and use vectorized operations wherever you can.
- Try to debug each function you implement first separately from the whole program.
- After rendering an image using e.g. `plt.imshow` you can use `plt.plot` to overlay points and lines on the image.
- You can control the parameters of the plotted points or lines through keyword arguments. E.g. `plt.plot(x, y, color='green', linestyle='dashed', marker='o', markerfacecolor='blue', markersize=12, lw=.5)`. see http://matplotlib.org/api/lines_api.html#matplotlib.lines.Line2D for many more options.
- To use the function `plt.plot` to draw a single thin blue line between two wide red points (`x[0],y[0]`) and (`x[1],y[1]`), you can execute `plt.plot(x, y, mfc='r', c='b', lw=.4, ms=10, marker='o')`.
- The functions we've provided are located in *ex4-impr-supplementary material/sol4.py*, use it as your initial code. You may make changes to the given code, as long as you don't alter the functions' signatures.
- Read carefully the code given in the class *PanoramicVideoGenerator*, make sure you understand what's going on, it will guide you when implementing the functions which are called by methods of this class.
- In *ransac_homography* you may find the package `np.random` useful, especially `np.random.permutation` or `np.random.choice`.
- Use `map_coordinates` with `order=1` and `prefilter=False` for linear interpolation.
- The sizes of the supplied images are not powers of 2, if it causes you a problem when reconstructing images from laplacian pyramids (should occur only in stitching) you may crop the images or use less pyramid levels.
- There might be a slight difference in your results between different runs due to the randomness of the RANSAC process. If you feel that is the case, use more iterations to ensure it converges to homographies which are good enough.
- The presubmit script is given in *ex4-impr-supplementary material.zip*, to use it locally you should place your files in a folder named `ex4` and tar your submission (`tar cvf sol4.tar ex4`). Then run `test sol4.tar`.

Good luck and enjoy!