

(1)

$|+| \uparrow\uparrow$

$|0 \sqrt{2}(|\downarrow\uparrow + \downarrow\uparrow|)$

1	2
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$| - | \downarrow\downarrow$

$|0 \sqrt{2}(|\uparrow\downarrow - \downarrow\uparrow|)$

1
2

$\frac{3}{2} + \frac{3}{2} \uparrow\uparrow\uparrow$

$\frac{3}{2} + \frac{1}{2} \sqrt{\frac{1}{3}}(|\uparrow\uparrow\downarrow + \uparrow\downarrow\uparrow + \downarrow\uparrow\uparrow|)$

$\frac{3}{2} - \frac{1}{2} \sqrt{\frac{1}{3}}(|\uparrow\downarrow\downarrow + \downarrow\uparrow\downarrow + \downarrow\downarrow\uparrow|)$

$\frac{3}{2} - \frac{3}{2} \downarrow\downarrow\downarrow \emptyset$

$\frac{1}{2} + \frac{1}{2} \sqrt{\frac{2}{3}}|\uparrow\downarrow\downarrow - \sqrt{\frac{1}{3}}\sqrt{\frac{2}{3}}(|\uparrow\downarrow + \downarrow\uparrow)\uparrow|$

$\frac{1}{2} - \frac{1}{2} \sqrt{\frac{2}{3}}\sqrt{\frac{2}{3}}(|\uparrow\downarrow + \downarrow\uparrow)| - \sqrt{\frac{2}{3}}\downarrow\downarrow\uparrow|$

1	2
3	

$\frac{1}{2} + \frac{1}{2} \sqrt{\frac{1}{2}}(|\uparrow\downarrow - \downarrow\uparrow)\uparrow|$

$\frac{1}{2} - \frac{1}{2} \sqrt{\frac{1}{2}}(|\uparrow\downarrow - \downarrow\uparrow)\downarrow|$

1	3
2	

$\sqrt{\frac{1}{4}}, \sqrt{\frac{2}{5}}, \sqrt{\frac{1}{10}}$

$2+2 \uparrow\uparrow\uparrow\uparrow$

$2+1 \frac{1}{2}(|\uparrow\uparrow\uparrow\downarrow + \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow|)$

$20 \sqrt{5}(|\uparrow\uparrow\downarrow\downarrow + \uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow + \uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow + \downarrow\downarrow\uparrow\uparrow|)$

$2-1 \frac{1}{2}(|\uparrow\downarrow\downarrow\downarrow + \downarrow\uparrow\downarrow\downarrow + \downarrow\downarrow\uparrow\downarrow + \downarrow\downarrow\downarrow\uparrow|)$

$2-2 \downarrow\downarrow\downarrow\downarrow$

$|+1| \frac{\sqrt{3}}{2}\uparrow\uparrow\uparrow\downarrow - \frac{1}{2}\sqrt{\frac{1}{3}}(|\uparrow\downarrow\downarrow + \downarrow\uparrow\uparrow + \downarrow\downarrow\uparrow)\uparrow|$

$|0 \sqrt{\frac{1}{2}}\sqrt{\frac{1}{3}}(|\uparrow\uparrow\downarrow + \uparrow\downarrow\uparrow + \cancel{\uparrow\uparrow\uparrow})\downarrow| + (-\frac{1}{\sqrt{2}})\sqrt{\frac{1}{3}}(|\uparrow\downarrow\downarrow + \downarrow\uparrow\downarrow + \downarrow\downarrow\uparrow)\uparrow|$

$| - 1| \frac{1}{2}\sqrt{\frac{1}{3}}(|\uparrow\downarrow\downarrow + \downarrow\uparrow\downarrow + \downarrow\downarrow\uparrow)\downarrow| - \frac{\sqrt{3}}{2}\downarrow\downarrow\downarrow\uparrow|$

1	2	3
4		

$$1+1 [\sqrt{\frac{2}{3}} \uparrow\downarrow\downarrow - \sqrt{\frac{1}{6}} (\uparrow\downarrow\uparrow + \downarrow\uparrow\downarrow)] \uparrow$$

1	3	4
2		

1	2	4
3		

$$10 \sqrt{\frac{1}{2}} [\sqrt{\frac{2}{3}} \uparrow\downarrow\downarrow - \sqrt{\frac{1}{6}} (\uparrow\downarrow\uparrow + \downarrow\uparrow\downarrow)] \downarrow + \sqrt{\frac{1}{2}} [\sqrt{\frac{1}{6}} (\uparrow\downarrow\downarrow + \downarrow\uparrow\downarrow) - \sqrt{\frac{2}{3}} \downarrow\downarrow\uparrow\uparrow]$$

$$= \sqrt{\frac{1}{3}} \uparrow\downarrow\downarrow - \sqrt{\frac{1}{12}} (\uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\downarrow) + \sqrt{\frac{1}{12}} (\uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow) - \sqrt{\frac{1}{3}} \downarrow\downarrow\uparrow\uparrow \quad (2)$$

$$1-1 \sqrt{6} (\uparrow\downarrow\downarrow\downarrow + \downarrow\uparrow\downarrow\downarrow) - \sqrt{\frac{2}{3}} \downarrow\downarrow\uparrow\downarrow$$

1	2
3	4

$$00 \sqrt{\frac{1}{3}} \uparrow\uparrow\downarrow\downarrow - \sqrt{\frac{1}{12}} (\uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow) - \sqrt{\frac{1}{12}} (\uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow) + \sqrt{\frac{1}{3}} \downarrow\downarrow\uparrow\uparrow$$

$$1+1 \sqrt{\frac{1}{2}} (\uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow),$$

1	3	4
2		

$$10 \sqrt{\frac{1}{2}} \sqrt{\frac{1}{2}} (\uparrow\downarrow\uparrow\downarrow - \downarrow\uparrow\uparrow\downarrow) + \sqrt{\frac{1}{2}} \sqrt{\frac{1}{2}} (\uparrow\downarrow\downarrow\uparrow - \downarrow\uparrow\downarrow\uparrow),$$

$$1-1 \sqrt{\frac{1}{2}} (\uparrow\downarrow\downarrow\downarrow - \downarrow\uparrow\downarrow\downarrow)$$

1	3
2	4

$$00 \frac{1}{2} (\uparrow\downarrow\uparrow\downarrow - \downarrow\uparrow\uparrow\downarrow) - \frac{1}{2} (\uparrow\downarrow\downarrow\uparrow - \downarrow\uparrow\downarrow\uparrow)$$

$$\frac{5}{2} + \frac{5}{2} \uparrow\uparrow\uparrow\uparrow\uparrow$$

1	2	3	4	5
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$$\frac{5}{2} + \frac{3}{2} \sqrt{5} (\uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow + \uparrow\uparrow\uparrow\downarrow)$$

$$\frac{5}{2} + \frac{1}{2} \sqrt{10} (\uparrow\uparrow\downarrow\downarrow + \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow + \uparrow\uparrow\downarrow\uparrow)$$

$$\frac{5}{2} - \frac{1}{2} + \uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\downarrow\uparrow + \uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow + \downarrow\downarrow\uparrow\uparrow$$

$$\frac{5}{2} - \frac{3}{2}$$

$$\frac{5}{2} - \frac{5}{2}$$

1	2	3	4
5			

$$\frac{3}{2} + \frac{3}{2} \cancel{\frac{\sqrt{3}}{2} \uparrow\uparrow\uparrow\downarrow} - \cancel{\frac{1}{2} \sqrt{\frac{1}{3}} (\uparrow\uparrow\downarrow + \uparrow\downarrow\uparrow + \downarrow\uparrow\uparrow)}$$

$$\cancel{\frac{3}{2} + \frac{1}{2} \sqrt{\frac{4}{5}} \uparrow\uparrow\uparrow\downarrow} - \sqrt{\frac{1}{5}} \frac{1}{2} (\uparrow\uparrow\downarrow + \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \uparrow$$

$$\frac{3}{2} + \frac{1}{2} \sqrt{\frac{3}{5}} \frac{1}{2} (\uparrow\uparrow\downarrow + \uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \downarrow$$

$$- \sqrt{\frac{2}{5}} \sqrt{\frac{1}{6}} (\uparrow\uparrow\downarrow\downarrow + \uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow + \uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow + \downarrow\downarrow\uparrow\uparrow) \uparrow$$

$$\frac{3}{2} - \frac{1}{2}$$

$$\frac{3}{2} - \frac{3}{2}$$

④

1	2	3	5
4			

$$\frac{3}{2} + \frac{3}{2} \quad \frac{\sqrt{3}}{2} \uparrow \uparrow \uparrow \downarrow \uparrow - \frac{1}{2} \sqrt{\frac{1}{3}} (\uparrow \uparrow \downarrow \uparrow + \uparrow \downarrow \uparrow \uparrow + \downarrow \uparrow \uparrow \uparrow) \uparrow$$

$$\begin{aligned} \frac{3}{2} + \frac{1}{2} \quad & \sqrt{\frac{1}{3}} \left(\frac{\sqrt{3}}{2} \uparrow \uparrow \uparrow \downarrow - \frac{1}{2} \sqrt{\frac{1}{3}} \uparrow \uparrow \downarrow \uparrow + \uparrow \downarrow \uparrow \uparrow + \downarrow \uparrow \uparrow \uparrow \right) \downarrow \\ & + \sqrt{\frac{2}{3}} \sqrt{\frac{1}{6}} (\uparrow \uparrow \downarrow \downarrow + \uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \uparrow \downarrow - \uparrow \downarrow \uparrow \downarrow - \downarrow \uparrow \downarrow \uparrow \downarrow \downarrow \uparrow \uparrow) \uparrow \end{aligned}$$

$$\frac{3}{2} - \frac{1}{2}$$

$$\frac{3}{2} - \frac{3}{2}$$

1	2	3
4	5	

$$\begin{aligned} \frac{1}{2} + \frac{1}{2} \quad & \sqrt{\frac{2}{3}} \frac{\sqrt{3}}{2} \uparrow \uparrow \uparrow \downarrow - \sqrt{\frac{2}{3}} \frac{1}{2} \sqrt{\frac{1}{3}} (\uparrow \uparrow \downarrow \uparrow + \uparrow \downarrow \uparrow \uparrow + \downarrow \uparrow \uparrow \uparrow) \downarrow \\ & + \cancel{\frac{1}{2}} - \sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}} (\uparrow \uparrow \downarrow \downarrow + \uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \downarrow \downarrow) \uparrow + \sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}} (\uparrow \downarrow \uparrow \uparrow + \downarrow \uparrow \uparrow \uparrow + \downarrow \uparrow \uparrow \uparrow) \uparrow \end{aligned}$$

$$\begin{aligned} \cancel{\frac{1}{2}} - \frac{1}{2} \quad & - \sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}} (\uparrow \uparrow \downarrow \downarrow + \uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \downarrow \downarrow) \uparrow - \sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}} (\cancel{\uparrow \downarrow \uparrow \uparrow} + \cancel{\downarrow \uparrow \uparrow \uparrow} + \cancel{\downarrow \uparrow \uparrow \uparrow}) \uparrow \end{aligned}$$

$$\begin{aligned} \frac{1}{2} - \frac{1}{2} \quad & \sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}} (\uparrow \uparrow \downarrow \downarrow + \uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \downarrow \downarrow) \downarrow - \sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}} (\cancel{\uparrow \downarrow \uparrow \uparrow} + \cancel{\downarrow \uparrow \uparrow \uparrow} + \cancel{\downarrow \uparrow \uparrow \uparrow}) \uparrow \\ & - \sqrt{\frac{2}{3}} \frac{1}{2} \sqrt{\frac{1}{3}} (\uparrow \downarrow \downarrow \downarrow + \downarrow \uparrow \downarrow \downarrow + \downarrow \downarrow \uparrow \downarrow) \uparrow - \sqrt{\frac{2}{3}} \left(\frac{-\sqrt{3}}{2} \right) \downarrow \downarrow \uparrow \uparrow \end{aligned}$$

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1	2	4	5
3			

$$\frac{3}{2} + \frac{3}{2} \quad \sqrt{\frac{2}{3}} \uparrow \downarrow \uparrow \downarrow - \sqrt{\frac{1}{6}} (\uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \downarrow \uparrow)$$

$$\frac{3}{2} + \frac{1}{2} \quad \sqrt{\frac{2}{3}} \cancel{\left[\sqrt{\frac{2}{3}} \sqrt{\frac{2}{3}} \uparrow \downarrow \uparrow \downarrow - \sqrt{\frac{1}{2}} \sqrt{\frac{1}{6}} (\uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \downarrow \uparrow) \right]} \downarrow$$

$$\begin{aligned} & \sqrt{\frac{2}{3}} \cancel{\left[\sqrt{\frac{2}{3}} \uparrow \downarrow \uparrow \downarrow - \sqrt{\frac{1}{12}} (\uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \downarrow \uparrow) + \sqrt{\frac{1}{12}} (\uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \downarrow \uparrow) \right]} \uparrow \\ & + \sqrt{\frac{2}{3}} \sqrt{\frac{1}{3}} (\sqrt{\frac{2}{3}} \uparrow \downarrow \uparrow \downarrow - \sqrt{\frac{1}{6}} \uparrow \downarrow \uparrow \downarrow - \sqrt{\frac{1}{6}} \downarrow \uparrow \uparrow \uparrow) \downarrow \end{aligned}$$

$$\frac{3}{2} - \frac{1}{2}$$

$$\frac{3}{2} - \frac{3}{2}$$

1	2	4
3	5	

$$-\sqrt{\frac{1}{6}}$$

$$\frac{1}{2} + \frac{1}{2} \quad \sqrt{\frac{2}{3}} (\sqrt{\frac{2}{3}} \uparrow \downarrow \uparrow \downarrow - \sqrt{\frac{1}{6}} \uparrow \downarrow \uparrow \downarrow \oplus \downarrow \uparrow \uparrow \uparrow) \downarrow$$

$$\begin{aligned} & - \sqrt{\frac{1}{3}} \left[\sqrt{\frac{2}{3}} \uparrow \downarrow \uparrow \downarrow - \sqrt{\frac{1}{12}} (\uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \downarrow \uparrow) + \sqrt{\frac{1}{12}} (\oplus \uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \downarrow \uparrow) \right. \\ & \left. - \sqrt{\frac{1}{3}} \downarrow \uparrow \uparrow \uparrow \right] \uparrow \end{aligned}$$

$$\begin{aligned} \frac{1}{2} - \frac{1}{2} \quad & \sqrt{\frac{1}{3}} \left[\sqrt{\frac{2}{3}} \uparrow \downarrow \uparrow \downarrow - \sqrt{\frac{1}{12}} (\uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \oplus \downarrow) + \sqrt{\frac{1}{12}} (\uparrow \downarrow \uparrow \downarrow \right. \\ & \left. + \downarrow \uparrow \downarrow \downarrow) - \sqrt{\frac{1}{3}} \downarrow \uparrow \uparrow \right] \downarrow \end{aligned}$$

$$- \sqrt{\frac{2}{3}} \left[\frac{1}{6} (\uparrow \downarrow \downarrow \downarrow + \downarrow \uparrow \downarrow \downarrow) - \sqrt{\frac{2}{3}} \downarrow \uparrow \downarrow \downarrow \right] \uparrow$$

⑥

1	2	3
3	4	

$$\frac{1}{2} + \frac{1}{2}\sqrt{3} \uparrow\downarrow\downarrow\uparrow - \sqrt{\frac{1}{2}}(\uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow) \uparrow - \sqrt{\frac{1}{2}}(\uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow) \uparrow \\ + \sqrt{3}\downarrow\downarrow\uparrow\uparrow\uparrow$$

$$\frac{1}{2} - \frac{1}{2} \sqrt{3} \downarrow\downarrow\downarrow - \sqrt{\frac{1}{2}}(\uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow) \downarrow - \sqrt{\frac{1}{2}}(\uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow) \downarrow \\ + \sqrt{3}\downarrow\downarrow\uparrow\uparrow\downarrow$$

1	3	4	5
2			

$$\frac{3}{2} + \frac{3}{2}\sqrt{\frac{1}{2}}(\uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow) \uparrow \\ \frac{3}{2} + \frac{1}{2}\sqrt{3}\sqrt{\frac{1}{2}}(\uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow) \downarrow + \sqrt{\frac{2}{3}}\frac{1}{2}(\uparrow\downarrow\uparrow\downarrow - \downarrow\uparrow\uparrow\downarrow + \uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow) \uparrow$$

$$\frac{3}{2} - \frac{1}{2}$$

$$\frac{3}{2} - \frac{1}{2}$$

1	3	4
2	5	

$$\frac{1}{2} + \frac{1}{2}\sqrt{\frac{2}{3}}\sqrt{\frac{1}{2}}(\uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow) \downarrow - \sqrt{\frac{1}{3}}\frac{1}{2}(\uparrow\downarrow\uparrow\downarrow - \downarrow\uparrow\uparrow\downarrow + \uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow) \uparrow$$

$$\frac{1}{2} - \frac{1}{2}\sqrt{3}\sqrt{\frac{1}{2}}(\uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow) \downarrow - \sqrt{\frac{1}{3}}\frac{1}{2}(\uparrow\downarrow\uparrow\downarrow - \downarrow\uparrow\uparrow\downarrow + \uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow) \downarrow$$

$$- \sqrt{\frac{2}{3}}\frac{1}{2}(\uparrow\downarrow\downarrow\downarrow - \downarrow\uparrow\downarrow\downarrow) \uparrow$$

1	3	5
2	4	

$$\frac{1}{2} + \frac{1}{2} [\frac{1}{2}(\uparrow\downarrow\uparrow\downarrow - \downarrow\uparrow\uparrow\downarrow) - \frac{1}{2}(\uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow)] \uparrow$$

$$\frac{1}{2} - \frac{1}{2} [\frac{1}{2}(\uparrow\downarrow\uparrow\downarrow - \downarrow\uparrow\uparrow\downarrow) - \frac{1}{2}(\uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow)] \downarrow.$$

⑦

1	2	3	4	5	6
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$$3+3 \uparrow\uparrow\uparrow\uparrow\uparrow\uparrow$$

1	2	3	4	5
6				

$$2+2. \sqrt{\frac{5}{6}} \uparrow\uparrow\uparrow\uparrow\uparrow\downarrow$$

$$-\sqrt{\frac{5}{6}} \sqrt{\frac{1}{5}} (\uparrow\uparrow\uparrow\downarrow\uparrow + \uparrow\uparrow\downarrow\uparrow\uparrow + \uparrow\downarrow\uparrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow\uparrow + \uparrow\uparrow\uparrow\downarrow) \uparrow$$

1	2	3	4	6
5				

$$2+2 \sqrt{\frac{4}{5}} \uparrow\uparrow\uparrow\uparrow\downarrow\uparrow$$

$$-\frac{1}{2} \sqrt{\frac{1}{5}} (\uparrow\uparrow\uparrow\downarrow + \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \uparrow\uparrow$$

1	2	3	4
5	6		

$$1+1 \sqrt{\frac{3}{4}} [\sqrt{\frac{4}{5}} \uparrow\uparrow\uparrow\uparrow\downarrow - \frac{1}{2} \sqrt{\frac{1}{5}} (\uparrow\uparrow\uparrow\downarrow + \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \uparrow] \downarrow$$

$$-\frac{1}{2} [\frac{1}{2} \sqrt{\frac{3}{5}} (\uparrow\uparrow\uparrow\downarrow + \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \downarrow$$

$$(-\sqrt{\frac{2}{5}} \sqrt{\frac{1}{6}}) (\uparrow\uparrow\downarrow\downarrow + \uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\downarrow\downarrow + \uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow + \downarrow\downarrow\uparrow\uparrow)$$

$\uparrow\uparrow\uparrow\uparrow$

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1	2	3	4
5	6		

$$1+1 \cdot \sqrt{\frac{3}{4}} \left[\sqrt{\frac{4}{5}} \uparrow\uparrow\uparrow\downarrow - \frac{1}{2} \sqrt{\frac{1}{5}} (\uparrow\uparrow\uparrow\downarrow + \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \right] \downarrow$$

$$- \sqrt{\frac{1}{4}} \frac{1}{2} \sqrt{\frac{3}{5}} (\uparrow\uparrow\uparrow\downarrow + \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \downarrow \uparrow$$

$$\left[-\sqrt{\frac{1}{4}} \left(-\sqrt{\frac{2}{5}} \sqrt{\frac{1}{6}} \right) (\uparrow\uparrow\downarrow\downarrow + \uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow + \uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow + \downarrow\downarrow\uparrow\uparrow) \right. \\ \left. + \downarrow\downarrow\uparrow\uparrow \right] \uparrow\uparrow$$

1	2	3	5	6
4				

$$2+2 \cdot \frac{\sqrt{3}}{2} \uparrow\uparrow\uparrow\downarrow\uparrow\uparrow - \frac{1}{2} \sqrt{\frac{1}{3}} (\uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \uparrow\uparrow.$$

1	2	3	5
4	6		

$$1+1 \frac{\sqrt{3}}{2} \left(\frac{\sqrt{3}}{2} \uparrow\uparrow\uparrow\downarrow\uparrow\downarrow - \frac{1}{2} \sqrt{\frac{1}{3}} (\uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \uparrow\downarrow \right)$$

$$- \frac{1}{2} \sqrt{\frac{1}{3}} \left(\frac{\sqrt{3}}{2} \uparrow\uparrow\uparrow\downarrow - \frac{1}{2} \sqrt{\frac{1}{3}} (\uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \downarrow\uparrow \right)$$

$$- \frac{1}{2} \sqrt{\frac{2}{3}} \sqrt{\frac{1}{6}} (\uparrow\uparrow\downarrow\downarrow + \uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow - \uparrow\downarrow\downarrow\uparrow - \downarrow\uparrow\downarrow\uparrow - \downarrow\downarrow\uparrow\uparrow) \uparrow\uparrow.$$

1	2	3	6
4	5		

$$1+1 \cdot \sqrt{\frac{2}{3}} \frac{\sqrt{3}}{2} \uparrow\uparrow\uparrow\downarrow\downarrow\uparrow - \sqrt{\frac{2}{3}} \frac{1}{2} \sqrt{\frac{1}{3}} (\uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \downarrow\uparrow.$$

$$- \sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}} (\uparrow\uparrow\downarrow\downarrow + \uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow) \uparrow\uparrow.$$

$$+ \sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}} (\uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow + \downarrow\downarrow\uparrow\uparrow) \uparrow\uparrow.$$

1	2	3
4	5	6

⑨

$$\sqrt{\frac{1}{2}}$$

$$0 \quad 0 \quad \sqrt{\frac{1}{2}} \sqrt{\frac{2}{3}} \frac{\sqrt{3}}{2} \uparrow \uparrow \uparrow \downarrow \downarrow \downarrow - \sqrt{\frac{2}{3}} \frac{1}{2} \sqrt{\frac{1}{3}} (\uparrow \uparrow \downarrow \uparrow + \uparrow \downarrow \uparrow \uparrow + \downarrow \uparrow \uparrow \uparrow) \downarrow \downarrow$$

$$\sqrt{\frac{1}{2}} (-\sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}}) (\uparrow \uparrow \downarrow \downarrow + \uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \downarrow \downarrow) \uparrow \downarrow$$

$$\sqrt{\frac{1}{2}} \sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}} (\uparrow \downarrow \downarrow \uparrow + \downarrow \uparrow \downarrow \uparrow + \downarrow \downarrow \uparrow \uparrow) \uparrow \downarrow .$$

$$(-\sqrt{\frac{1}{2}}) \sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}} (\uparrow \uparrow \downarrow \downarrow + \uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \uparrow \downarrow) \downarrow \uparrow$$

$$(-\sqrt{\frac{1}{2}}) (-\sqrt{\frac{1}{3}} \sqrt{\frac{1}{6}}) (\uparrow \downarrow \downarrow \uparrow + \downarrow \uparrow \downarrow \uparrow + \downarrow \downarrow \uparrow \uparrow) \downarrow \uparrow .$$

$$(-\sqrt{\frac{1}{2}}) (-\sqrt{\frac{1}{3}} \frac{1}{2} \sqrt{\frac{1}{3}}) (\uparrow \downarrow \downarrow \downarrow + \downarrow \uparrow \downarrow \downarrow + \downarrow \downarrow \uparrow \downarrow) \uparrow \uparrow .$$

$$(-\sqrt{\frac{1}{2}}) (-\sqrt{\frac{1}{3}} - \frac{\sqrt{3}}{2}) \downarrow \downarrow \downarrow \uparrow \uparrow \uparrow .$$

1	2	4	5	6
3				

$$2+2 \quad \sqrt{\frac{3}{2}} \uparrow \uparrow \downarrow \uparrow \uparrow \uparrow - \sqrt{\frac{1}{6}} (\uparrow \downarrow \uparrow \uparrow \uparrow \uparrow + \downarrow \uparrow \uparrow \uparrow \uparrow) \uparrow$$

1	2	4	5
3	6		

$$1+1. \sqrt{\frac{3}{4}} [\sqrt{\frac{2}{3}} \uparrow \uparrow \downarrow \uparrow \uparrow - \sqrt{\frac{1}{6}} (\uparrow \downarrow \uparrow \uparrow \uparrow + \downarrow \uparrow \uparrow \uparrow \uparrow)] \downarrow$$

$$-\frac{1}{2} \sqrt{\frac{2}{3}} [\sqrt{\frac{2}{3}} \uparrow \uparrow \downarrow \downarrow - \sqrt{\frac{1}{12}} (\uparrow \downarrow \uparrow \downarrow + \downarrow \uparrow \downarrow \downarrow) + \sqrt{\frac{1}{12}} (\uparrow \downarrow \downarrow \uparrow + \downarrow \uparrow \downarrow \uparrow)]$$

$$-\sqrt{\frac{1}{3}} \downarrow \uparrow \uparrow \uparrow \uparrow \uparrow$$

$$-\frac{1}{2} \sqrt{\frac{1}{3}} (\sqrt{\frac{2}{3}} \uparrow \uparrow \downarrow \uparrow - \sqrt{\frac{1}{6}} \uparrow \downarrow \uparrow \uparrow - \sqrt{\frac{1}{6}} \downarrow \uparrow \uparrow \uparrow) \downarrow \uparrow$$

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1	2	4	6
3	5		

$$1 + 1 \cdot \sqrt{\frac{2}{3}} \left(\sqrt{\frac{2}{3}} \uparrow\downarrow \downarrow\uparrow - \sqrt{\frac{1}{6}} \uparrow\downarrow \uparrow\uparrow - \sqrt{\frac{1}{6}} \downarrow\uparrow \uparrow\uparrow \right) \downarrow\uparrow$$

$$- \sqrt{\frac{1}{3}} \left[\sqrt{\frac{1}{3}} \uparrow\uparrow \downarrow\downarrow - \sqrt{\frac{1}{12}} \left(\uparrow\downarrow \uparrow\downarrow + \downarrow\uparrow \uparrow\downarrow \right) + \sqrt{\frac{1}{12}} \left(\uparrow\downarrow \downarrow\uparrow + \downarrow\uparrow \downarrow\uparrow \right) \right.$$

$$\left. - \sqrt{\frac{1}{3}} \downarrow\downarrow \uparrow\uparrow \right] \uparrow\uparrow$$

1	2	4
3	5	6

$$0 + 0 \cdot \sqrt{\frac{1}{2}} \left[\sqrt{\frac{2}{3}} \left(\sqrt{\frac{2}{3}} \uparrow\downarrow \downarrow\uparrow - \sqrt{\frac{1}{6}} \uparrow\downarrow \uparrow\uparrow - \sqrt{\frac{1}{6}} \downarrow\uparrow \uparrow\uparrow \right) \downarrow \right] \downarrow$$

$$\left(\sqrt{\frac{1}{2}} \oplus (-\sqrt{\frac{1}{3}}) \right) \left[\sqrt{\frac{2}{3}} \uparrow\uparrow \downarrow\downarrow - \sqrt{\frac{1}{12}} \left(\uparrow\downarrow \uparrow\downarrow + \downarrow\uparrow \uparrow\downarrow \right) \right.$$

$$\left. + \sqrt{\frac{1}{12}} \left(\uparrow\downarrow \downarrow\uparrow + \downarrow\uparrow \downarrow\uparrow \right) - \sqrt{\frac{1}{3}} \downarrow\downarrow \uparrow\uparrow \right] \uparrow\downarrow$$

$$\left(-\sqrt{\frac{1}{2}}, \sqrt{\frac{1}{3}} \right) \left[\sqrt{\frac{2}{3}} \uparrow\uparrow \downarrow\downarrow - \sqrt{\frac{1}{12}} \left(\uparrow\downarrow \uparrow\downarrow + \downarrow\uparrow \uparrow\downarrow \right) \right.$$

$$\left. + \sqrt{\frac{1}{12}} \left(\uparrow\downarrow \downarrow\uparrow + \downarrow\uparrow \downarrow\uparrow \right) - \sqrt{\frac{1}{3}} \downarrow\downarrow \uparrow\uparrow \right] \downarrow\uparrow$$

$$\left(-\sqrt{\frac{1}{2}}, -\sqrt{\frac{1}{3}} \right) \left[\sqrt{\frac{2}{3}} \left(\uparrow\downarrow \downarrow\downarrow + \downarrow\uparrow \downarrow\downarrow \right) - \sqrt{\frac{2}{3}} \downarrow\downarrow \uparrow\downarrow \right] \uparrow\uparrow$$

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1	2	5	6
3	4		

$$|+1, \sqrt{\frac{1}{3}}\uparrow\downarrow\downarrow\uparrow\uparrow - \sqrt{\frac{1}{12}}(\uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow)\uparrow\uparrow \\ - \sqrt{\frac{1}{12}}(\uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow)\uparrow\uparrow + \sqrt{\frac{1}{3}}\downarrow\downarrow\uparrow\uparrow\uparrow\uparrow$$

1	2	5
3	4	6

$$0 + 0 \sqrt{\frac{1}{2}} \left[\sqrt{\frac{1}{3}} \uparrow\downarrow\downarrow\uparrow - \sqrt{\frac{1}{2}} (\uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow) \uparrow - \sqrt{\frac{1}{2}} (\uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow) \uparrow \right. \\ \left. + \sqrt{\frac{1}{3}} \downarrow\uparrow\uparrow\uparrow \right] \downarrow - \sqrt{\frac{1}{2}} \left[\sqrt{\frac{1}{3}} \uparrow\downarrow\downarrow\downarrow - \sqrt{\frac{1}{2}} (\uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow) \downarrow - \sqrt{\frac{1}{2}} (\uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow) \downarrow \right. \\ \left. + \sqrt{\frac{1}{3}} \downarrow\downarrow\uparrow\downarrow \right] \uparrow$$

1	3	4	5	6
2				

$$2+2 \sqrt{\frac{1}{2}}(↑↓↑↑-↓↑↑↑)↑↑$$

1	3	4	5
2	6		

$$1 + \frac{1}{\sqrt{4}} \sqrt{\frac{1}{2}} (\uparrow \downarrow \uparrow \uparrow - \downarrow \uparrow \uparrow \uparrow) \uparrow \downarrow$$

$$- \sqrt{\frac{1}{4}} \left[\sqrt{\frac{1}{6}} (\uparrow \downarrow \uparrow \uparrow - \downarrow \uparrow \uparrow \uparrow) \downarrow + \sqrt{6} (\uparrow \downarrow \uparrow \downarrow - \downarrow \uparrow \uparrow \downarrow + \uparrow \downarrow \uparrow \uparrow - \downarrow \uparrow \downarrow \uparrow) \right]$$

$\uparrow \downarrow \uparrow$

(12)

1	3	4	6
2	5		

$$1 + 1 \sqrt{\frac{1}{3}} (\uparrow \downarrow \uparrow \uparrow - \downarrow \uparrow \uparrow \uparrow) \downarrow \uparrow$$

$$- \sqrt{\frac{1}{12}} (\uparrow \downarrow \uparrow \downarrow - \downarrow \uparrow \uparrow \downarrow + \uparrow \downarrow \downarrow \uparrow - \downarrow \uparrow \downarrow \uparrow) \uparrow \uparrow$$

1	3	4
2	5	6

$$0 + 0 \sqrt{\frac{1}{2}} \sqrt{\frac{1}{3}} (\uparrow \downarrow \uparrow \uparrow - \downarrow \uparrow \uparrow \uparrow) \downarrow \downarrow$$

$$\sqrt{\frac{1}{2}} (-\sqrt{\frac{1}{12}}) (\uparrow \downarrow \uparrow \downarrow - \downarrow \uparrow \uparrow \downarrow + \uparrow \downarrow \downarrow \uparrow - \downarrow \uparrow \downarrow \uparrow) \uparrow \downarrow$$

$$(-\sqrt{\frac{1}{2}}) (\sqrt{\frac{1}{12}}) (\uparrow \downarrow \uparrow \downarrow - \downarrow \uparrow \uparrow \downarrow + \uparrow \downarrow \downarrow \uparrow - \downarrow \uparrow \downarrow \uparrow) \downarrow \uparrow$$

$$(-\sqrt{\frac{1}{2}}) (-\sqrt{\frac{1}{3}}) (\uparrow \downarrow \downarrow \downarrow - \downarrow \uparrow \downarrow \downarrow) \uparrow \uparrow.$$

1	3	5	6
2	4		

$$1 + 1 [\frac{1}{2} (\uparrow \downarrow \uparrow \downarrow - \downarrow \uparrow \uparrow \downarrow) - \frac{1}{2} (\uparrow \downarrow \downarrow \uparrow - \downarrow \uparrow \downarrow \uparrow) \uparrow \uparrow]$$

1	3	5
2	4	6

$$0 \ 0 \sqrt{\frac{1}{2}} [\frac{1}{2} (\uparrow \downarrow \uparrow \downarrow - \downarrow \uparrow \downarrow) - \frac{1}{2} (\uparrow \downarrow \downarrow \uparrow - \downarrow \uparrow \downarrow \uparrow) \uparrow \downarrow]$$

$$- \sqrt{\frac{1}{2}} [\frac{1}{2} (\uparrow \downarrow \uparrow \downarrow - \downarrow \uparrow \downarrow) - \frac{1}{2} (\uparrow \downarrow \downarrow \uparrow - \downarrow \uparrow \downarrow \uparrow) \downarrow \uparrow]$$