

# Faculty of Information Engineering, Informatics and Statistics Department of Computer Science

# Distributed Systems

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# Contents

1	Intr	roduction	1
	1.1	Defining a distributed system	1
	1.2	Computation	1
	1.3	Monitoring computations	3
	1.4	Vector clocks	5
	1.5	Distributed snapshots	6
2		mic transaction	7
	2.1	2 Phase commit	7
	2.2	Paxos	8
		2.2.1 Fast-Paxos	10
		2.2.2 Multi-Paxos	12
		2.2.3 Leader election	12

# 1

## Introduction

## 1.1 Defining a distributed system

We define a **distributed system** as a collection of processes  $p_1, p_2, \ldots, p_n$  that run on different computers and cooperate to solve a problem. The processes comunicate using **channels** and we assume the system is fully connected, meaning that every pair of processes can excange messages between them. The channels are reliable, in the sense that te message arrive, but may delivered messages out of order.

The simple model for a distributed system is called **asynchronous**, that have no upper bound on the speed of processes and no upper bound for the delay of a message. If these upper bounds exists the system is called **synchronous**. The second one is stronger, in the sense that we do more assumpions and this means that every program that run on a synchronous system can run on an asynchronous system (the opposite can be possible but not sure).

A distributed system can have different properties:

- Consistency: every part of the system has the same information at every time
- Avilability: the information are available at every time
- Partiotion tolerance: if one part of the system goes offline the system can continue to run

Every type of distributed system can have up to 2 of this properties.

### 1.2 Computation

We describe the execution of a program on a distributed system as a collection of processes. Every process is defined as a sequence of **events**. The events can be internal or involve comunication like the events **send(m)** and **receive(m)**.

We label an event with the notation:

 $e_i^k$ 

in which i represent the index of the process  $p_i$  and k the order of the event for that specific process.

1. Introduction 1.2. Computation

#### Local and global history

The **local history** of a process  $p_i$  is a sequence of events  $h_i = e_i^1 e_1^2 \dots$  that represent the sequencial execution of events in the process. We use  $h_i^k$  to represent the sequence of the first k events in the process  $p_i$ .

The **global history** of the computation is a set that contains all events:

$$H = h_1 \cup h_2 \cup \cdots \cup h_n$$

The global history gives us no information about the time in which these events are executed, because in an asynchronous system there is no global clock.

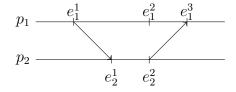
#### Relation of cause-effect

Events can be labeled based of the notion of **cause-effect**, defining a relation (with symbol  $\rightarrow$ ) between two events such that:

- $\forall e_i^k, e_i^l \in h_i \land k < l \implies e_i^k \rightarrow e_i^l$
- $e_i = \mathtt{send(m)} \wedge e_j = \mathtt{receive(m)} \implies e_i \rightarrow e_j$
- $e \to e' \land e' \to e'' \implies e \to e''$  (Transitive)

This relation mean that  $e \to e'$  if e causally precedes e', so the computation of e' is influenced by e. Two events can be unrelated, so neither  $e \to e'$  nor  $e' \to e$ . We call this pair of events as **concurrent** and write them as e||e'.

We can graphically represent a computation with a space-time diagram like this:



An arrow from  $p_1$  to  $p_2$  means that  $p_1$  sends a message to  $p_2$ .

#### Run

A **run** is a total order of all events in the global history, consistent with each local history, so the events in history  $h_i$  appear in the same order in R:

$$R = e_1^1 e_2^1 \dots$$

A single program can have many different runs because some events are unrelated.

## 1.3 Monitoring computations

#### Local and global state

We denote  $\sigma_i^k$  the **local state** of a process  $p_i$  after the event  $e_i^k$ . The **global state** of the computation is an *n*-tuple of local states:

$$\Sigma = (\sigma_1, \sigma_2, \dots, \sigma_n)$$

#### Cut

A **cut** is a collection of local histories:

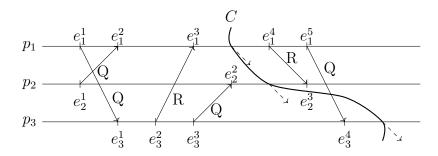
$$C = \langle h_1^{k_1}, h_2^{k_2}, \dots, h_n^{k_n} \rangle$$

To monitor the computation or to compute a global problem (for example knowing if the system is in deadlock) we add a process  $p_0$ .

The first idea is to make  $p_0$  send a message to every process to which a process  $p_i$  will respond with the current state  $\sigma_i$ . After all the response  $p_0$  can construct a global state, that defines a cut.

#### Example:

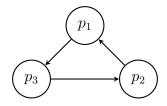
Considering the follows space-time diagram with the cut C (the dashed arrow represent when the process sends the response to  $p_0$ ):



If we use the responses to create a graph, based on the states, we can say that:

- $p_1$  is going to send a response to  $p_2$
- $p_2$  is going to send a response to  $p_3$
- $p_3$  is going to send a response to  $p_1$

So the graph generated by  $p_0$  will be:



It seems the system has a deadlock, but if we watch carefully we can see that this is not true. The problem is that the global state defined by the cut C could never happen during a computation.

#### Consistent cut

A cut is **consistent** if only if:

$$\forall e \to e' \land e' \in C \implies e \in C$$

So a cut is consistent if the global state generated by the cut could be possible during a computation.

If we use  $p_0$  only to receive messages and we make every process notify the events to  $p_0$  with a timestamp associated,  $p_0$  can reorder the events to create a run. This is true only if there is a global clock, which is not true. To overcome this problem we have to create a local clock for every process and update it in a consisten way.

#### **Clock condition**

A run is consistent if only if follows the **clock condition**:

$$\forall e \to e' \implies TS(e) < TS(e')$$

If TS(e) < TS(e') is possible but not garanteed that  $e \to e'$ .

#### Local clock

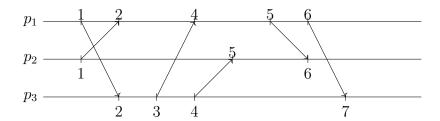
We define the **local clock** of a process as follows:

$$LC(e_i) = \begin{cases} LC + 1 & e_i \text{ is internal or send} \\ \max(LC, TS(m)) + 1 & e_i \text{ is a receive(m)} \end{cases}$$

The local clocks satisfy the clock condition.

#### Example:

In the previous example the timestamps of the local clocks will be:



1. Introduction 1.4. Vector clocks

#### 1.4 Vector clocks

We want to ensure that the process  $p_0$  sends the messages from the network level to the upper level in order, so the communication between two processes has to be FIFO (First-In First-Out). To do that in a synchronous system with a global clock and an upper bound for a message  $\Delta t$ , we can follow a simple rule fro  $p_0$ :

• On a certain time t, deliver all the message with timestamp lower than  $t - \Delta t$  in order based on the global clock.

In an asynchronous system we have to decide when to deliver a message, so we have to be sure that all the previous message are already delivered. We could wait for every other process to send to  $p_0$  every notification with local timestamp lower than the one received before, but this could stuck the system if a process doesn't have enough events to notify.

#### Strong clock condition

We expand the definition of clock condition changing the implication with a if only if:

$$e \to e' \iff TS(e) < TS(e')$$

#### History of an event

We define the **history** of an event as a set:

$$H(e) = \{e'|e' \rightarrow e\} \cup \{e\}$$

This includes all the previous events that could have changed the result of event e.

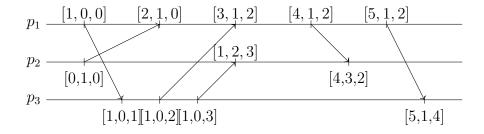
We will identify an history of a process e with a vector in which every index i represent the last event of process  $p_{i+1}$  in H(e). For example the history  $H(e_1^4) = \{e_1^1, e_1^2, e_1^3, e_1^4, e_1^1, e_1^2, e_3^1, e_3^2, e_3^3\}$  is identified by the vector [4, 1, 3]. This vector clocks are updated for a process  $p_i$  following the rule:

$$VC = \begin{cases} VC[i] = VC[i] + 1 & \text{always} \\ VC[j] = \max(VC[j], TS(m)[j]) \ \forall j \neq i \quad e_i \text{ is a recieve(m)} \end{cases}$$

These clocks respect the strong clock condition.

#### Example:

Using this new vector clocks in the previous example the result is:



To know when to deliver a notification  $p_0$  has a counter D in which D[i] contains the number of messages delivered from  $p_i$ .  $p_0$  will deliver the notification of an event  $e_i$  if:

$$VC(e_i)[i] = D[i] + 1$$
  
 $VC(e_i)[j] \le D[j] \ \forall j \ne i$ 

#### Gap detection

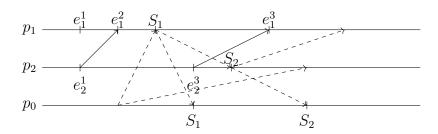
Taken two events  $e_i$ ,  $e_j$  is possible to know if exists an event between the two:

$$\exists e_k \ e_k \rightarrow e_i \land e_k \not\rightarrow e_i \iff VC(e_i)[k] > VC(e_i)[k]$$

## 1.5 Distributed snapshots

If we reuse the idea proposed in Section 1.3 where  $p_0$  sends a message to the other processes and they respond with their state, called **snapshot**. The cut generated by this idea was not surely consistent, so we apply a change.

When a process recieve the message "take snapshot" from  $p_0$ , it broadcast his state to the other processes. If another process recieve the state of a process it will also broadcast his state. A process will send his state only one time during the protocol, so if he already sent his state to  $p_0$  he will not send it again even if he recieves the state of another process. Every process knows the protocol ended when he receives the state of all the other processes. This protocol, called **Chandy-Lampart Protocol** generates a consistent cut if the channels are FIFO.



# 2

## Atomic transaction

#### Atomic commit

An atomic commit is the problem that occurs when there is a transaction T that involves multiple sistes in a distibuted system. So all the sites do the transaction, or no one does.

We can explain an atomic commit as if every process involved in the transaction votes yes or no to committing the transaction. The system after the votes decide to commit or abort. An atomic commit has different properties:

- If a process reach a decision, it must be the same.
- If a process reaches a decision, it cannot change that.
- Decision is to commit only if every process votes yes.
- If there are not failures and all votes are yes the decision must be commit.
- If all failures ar fixed then the protocol should terminate.

### 2.1 2 Phase commit

One simple protocol to execute an atomic commit is the **2 Phase commit**, in which there is a coordinator process and there other processes are participants.

The protocol follows 4 phases:

- 1. The coordinator sends a vote request to every participants.
- 2. Each participant votes yes or no. If the vote is no the participant can already abort.
- 3. The coordinator controls the votes and if they are all yes sends a commit message to every participant. Else it sends an abort message.
- 4. The partecipants execute the decision recieved.

The main problems that can occur during this protocol are message not delivered or process that fail during the execution.

To resolve the message failure a timestamp can be used. At every phase the timeout is used in a different way:

1. The participant is waiting for the vote request and reaches the timeout, so it votes no and abort.

- 2. The coordinator is waiting for the votes and reaches the timeout, so it sends and abort message.
- 3. The participant is waiting for the decision and reaches the timeout, so it asks other processes for their decision. If they have a decision, it execute the same, if every process is waiting they have to continue waiting.

To resolve the sites failure the processes log during the protocol. Also in this case every phase has a different method to log:

1. The coordinator log the start of the transaction:

$$START2PC \rightarrow DTlog$$

Is better to log and then send the messages because in the case of a crash in between the two:

- If the log is empty: nothing has been sent, so a transaction can start safely.
- If the log is full: is safe to resend the request.
- 2. The participant logs its vote:

$$yes/no \rightarrow DTlog$$

Also in this case is better to log and then send the message because in the case of a crash in between the two:

- If the log is empty: nothing has been sent, so is safe to abort.
- If the log is full: is safe to resend the request.
- 3. The coordinator logs the votes received and ater it sends the decision.
- 4. The participant logs the decision before executing it.

In some distributed systems with a lot of servers with the same data, this protocol is not the best, because if even one server fails the transaction is aborted.

#### 2.2 Paxos

The **Paxos** protocol has the goal to make a system work even in presence of failures. The servers are divided in three categories:

- **Proposer**: start the transaction and propose the value to vote.
- Acceptors: vote the value.
- Learners: keep track of the decision made by the Acceptors.

The protocol has two additional rules:

- All the servers need to choose the same value at the end of the protocol.
- The value chosen must be suggested from outside.

The protocol work with minimum one Proposer and one Learner. For the Acceptors the majority is needed so the maximum number of failures tollerated is with n Acceptors:

$$f = \left\lfloor \frac{n-1}{2} \right\rfloor$$

And the size of the quorum will be:

$$|Q| = n - f$$

The protocol works in **rounds** and every round is associated with only one transaction. A round work in this way:

1. Proposer sends a message to all the Acceptors:

$$P \to A$$
 prepare(curr-round)

2. Acceptors respond to the Proposer:

$$A \rightarrow P$$
 promise(curr-round, last-round, last-value)

In which they promise to participate in the current round and to not participate to any round lower than that. In addition it also sends the last round in which it has voted and the last value voted.

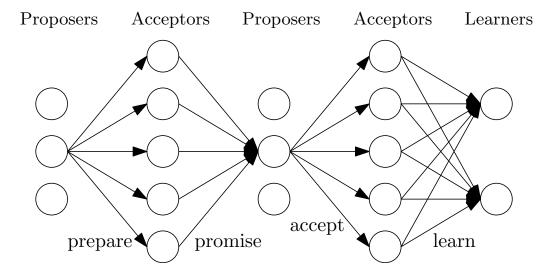
- 3. Proposer waits for a quorum of promises and after sends to every Acceptor a message with the value proposed x, that is chosen in this way:
  - If no Acceptor has ever voted the value x can be chosen at random (value that comes from the client).
  - Else the value x is the last value voted associated with the largest value of last-round in the promises.

$$P \to A$$
 accept(curr-round,  $x$ )

4. Acceptors sends their vote to the Learners:

$$A \to L$$
 learn(curr-round,  $x$ )

5. Learners control the votes and if a quorum voted the same value in the same round the value is chosen. If there is no quorum after a timeout the Proposer will asks the Learners for a decision, if there is no decision there will be another round.



There are some problems with transaction that could start in the same time. If the prepare message of a transaction with a lower round arrives after one with an higher round the first transaction will never be done. On the other hand if the prepare message of a transaction with an higher round arrives before the vote of a transaction with a lower round this transaction will be stopped after the acceptors promise with the higher round. This is the reason Paxos is not **live**, in the sense that if this continue to occur the protocol doesn't do nothing.

This protocol is **safe**, means that doesn't do anything wrong even in presence of more then f failures.

#### Safety condition

For Paxos the safety condition is:

Is an acceptor  $A_k$  votes for a value x in round i, no value different from x can be chosen by learners in a previous round.

#### **Demonstration:**

The demonstration can be done by induction:

- 1. Base case: round 1 doesn't have previous rounds so the property is valid.
- 2. Induction ipothesis: for every round i, the value to vote is equal to the value x associated with the max last round j in the promises. If for j is valid the property, also is valid for i.
- 3. Induction step: the value voted in round i must be voted by some acceptors in round j, so in round j is impossible to have a quorum on a value different that x. All the acceptors that sent promises in round i don't vote in rounds between j and i so any of this rounds can have a quorum of votes.

#### 2.2.1 Fast-Paxos

The **Fast-Paxos** protocol is a different version of Paxos, in which there is a Coordinator in the Proposers that prepare the first round before the value to vote arrives. A round works like this:

1. Coordinator sends a message to all the Acceptors:

$$C \to A$$
 prepare(curr-round)

2. Acceptors respond to the Coordinator:

$$A \to C$$
 promise(curr-round, last-round, last-value)

In which they promise to participate in the current round and to not participate to any round lower than that. In addition it also sends the last round in which it has voted and the last value voted.

- 3. Coordinator waits for a quorum of promises and after sends to every Acceptor a message that depends on the promises:
  - If no Acceptor has ever voted the Coordinator sends an acceptany message to tell the Acceptors to accept values from any Proposer.

$$C \to A$$
 acceptany(curr-round)

• Else the value x is the most voted value in the max last round.

$$P \to A$$
 accept(curr-round,  $x$ )

4. When a value arrives to the Proposers they send an accept message to the Acceptors with the value x.

$$P \to A$$
 accept(curr-round,  $x$ )

5. Acceptors sends their vote to the Learners:

$$A \to L$$
 learn(curr-round, x)

6. Learners control the votes and if a quorum voted the same value in the same round the value is chosen. If there is no quorum after a timeout the Coordinator will start another round.

In a round there could be different values voted, to overcome this problem the quorum is modified to be equal to  $\frac{2}{3} + 1$ . So, the maximum number of failures tolerated decrease to:

$$f = \left\lfloor \frac{n-1}{3} \right\rfloor$$

The protocol Fast-Paxos is safe.

#### **Demonstration:**

The demonstration can be done by induction:

- 1. Base case: round 1 doesn't have previous rounds so the property is valid.
- 2. Induction ipothesis: for every round i, the value to vote is equal to the value x most common in the max last round j in the promises. If for j is valid the property, also is valid for i.
- 3. Induction step: the value voted in round i is the most common value voted in round j, and is the only value that can reach a quorum in round j, because only 1 value every round has the possibility to have a quorum of votes. This is because with a quorum of  $\frac{2}{3}$  only 1 value can have more than  $\frac{1}{3}$  votes in the promises that could result in a quorum if the  $\frac{1}{3}$  outside the quorum all voted for that value. All the acceptors that sent promises in round i don't vote in rounds between j and i so any of this rounds can have a quorum of votes.

#### 2.2.2 Multi-Paxos

Normally the problem is not only to agree on a single value, but on a series of values and on their order. This can be done with the protocol **Multi-Paxos** in which a lot of istances of Paxos (or Fast-Paxos) are run at the same time. Every istance agree on a value and the order in which the transactions are executed is the order of the istances.

The prepare message now contains also the istance of Paxos and multiple istances can be prepared at the same time, for example for n istances:

$$C \to A$$
 prepare(1-n, curr-round)

Also Acceptors can promise to multiple istances:

$$A \to C$$
 promise(1-n, curr-round, last-round, last-value)

And the acceptany message can be sent for multiple istances:

$$C \to A$$
 acceptany  $(1-n, curr-round)$ 

The accept messages have to be sent for every istance singularly and the istance to send a particul value is chosen by the Proposers. If the Prosopers are also Learners they know which istances have aleady chosen a value and can send the new values to other istances.

#### 2.2.3 Leader election

In the previous protocols a coordinator must be chosen, but this can't be done. If could be done Paxos would be live.