

TDT4120

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1 Algorithm Design

1.1 Divide and Conquer

Divide and Conquer is an Algorithm design paradigm based on multi-branch recursion. A divide and conquer algorithm works by recursively breaking down a problem into two or more sub-problems of the same or related type, until these become simple enough to be solved directly. The solutions to the sub-problems are then combined to give a solution to the original problem.

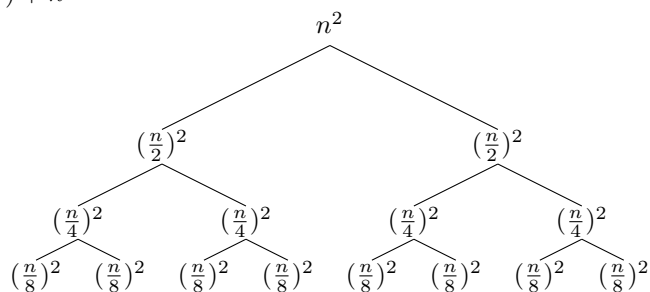
2 Loose Recurrences

2.1 The Master-Theorem

Generic form $T(n) = aT(\frac{n}{b}) + f(n)$

2.2 Recursion Trees

$$T(n) = 4T\left(\frac{n}{2}\right) + n^2$$



This is supposed to be a tree...

```

n^2
--(n/2)^2
---(n/4)^2
---(n/4)^2
---(n/4)^2
---(n/4)^2
---(n/2)^2
---(n/4)^2
---(n/4)^2
---(n/4)^2
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---(n/2)^2
---(n/4)^2
---(n/4)^2
---(n/4)^2
  
```

2.3 Variable-switching

$$T(n) = 2T(\sqrt{n}) + \log n$$

3 Sorting Algorithms

3.1 Mergesort

$$\theta(n \log n)$$

3.2 Quicksort

Howto:

Listing 1: Julia example

```
function traverse_recursive_max(node, start_value)
    highest_value = start_value
    if (node.value > highest_value)
        highest_value = node.value
    end
    if node.next == nothing
        return highest_value
    end
    traverse_recursive_max(node.next, highest_value)
end

traversemax(node) = traverse_recursive_max(node, node.value)
```

4 Code example overview

Listings

1	Julia example	4
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