

Cognitive Constraint Modeling: An Alternative to Traditional Architectures

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Outline

Overview of
Constraint
Analysis

Example #1:
Dual-tasks

How It Works

Example #2:
777 Cockpit

Example #3:
ACT-R
Critique

Summary

- 1 Overview of Constraint Analysis
- 2 Example #1: Simple Dual-tasks
- 3 How Cognitive Constraint Modeling Works
- 4 Example #2: Boeing 777/FDF Cockpit Tasks
- 5 Example #3: A Critique of a Prominent ACT-R Model
- 6 Summary

Key Claims

- ① Human Task Performance can be predicted by **formally reasoning about the implications of a theory** rather than running a simulation.
- ② A theory of cognitive architecture **explains** empirically observed asymptotic bounds on performance if there is **substantial correspondence between the asymptote and the optimal performance implied by the theory**.
- ③ The ability to automatically derive optimal predictions from cognitive theory has **significant theoretical and applied benefits**.

How Architectures Make Predictions

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**ARCHITECTURE +
KNOWLEDGE (STRATEGY)
= BEHAVIOR**

A Conundrum for Cognitive Theory

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**Complete cognitive theories must take the form
architectures that admit of arbitrary knowledge/strategic
variation**

BUT: knowledge, strategy can become theoretical degrees of freedom in modeling data

- Explanation may reside primarily in strategy, not architecture
- Strategy may have been selected to fit the data at hand

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BUT: knowledge, strategy can become theoretical degrees of freedom in modeling data

- Explanation may reside primarily in strategy, not architecture
- Strategy may have been selected to fit the data at hand
- (*But that never happens, right?*)

Two Possible Solutions

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- ① Focus on “**immediate behavior**” (Newell 1990)
 - Behavior < 1 s
 - Problem: Even < 1 s behavior shows surprising amount of strategic modulation (Meyer & Kieras, 1997)
- ② Theory of **learning/instruction taking**
 - “Close the loop”, so strategy not under theorist’s control
 - Problem: complexity; testing many aspects of theory simultaneously

Constraint Analysis Overview

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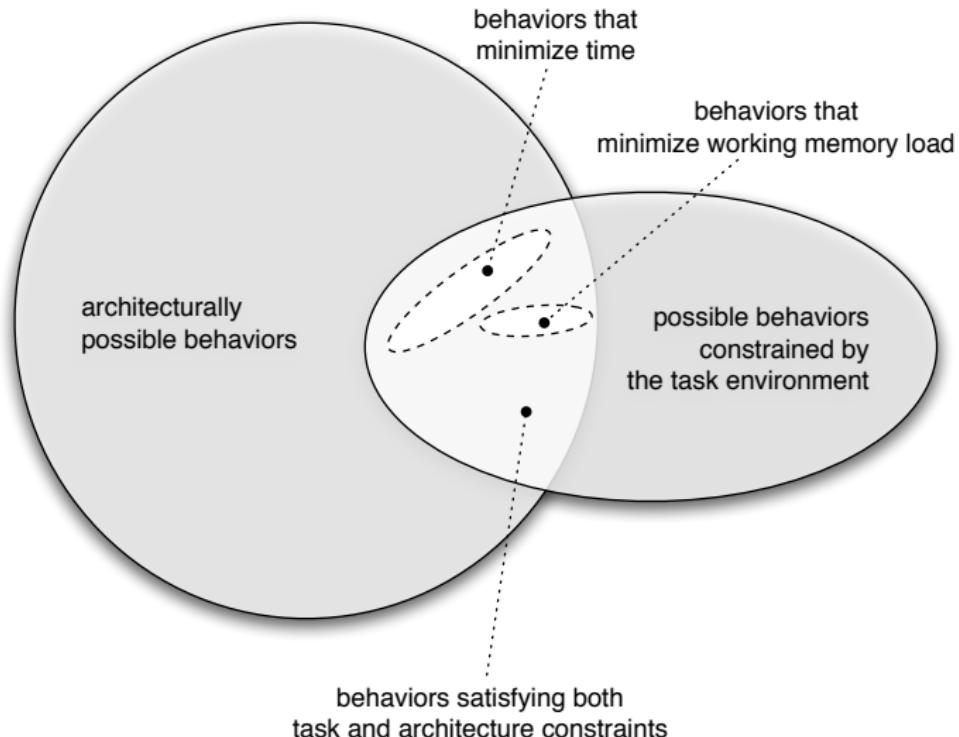
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- Adaptive behavior is bounded by **Objective + Environment + Knowledge + Architecture** (Simon 1992)
- **Constraint satisfaction techniques can be used to calculate the optimal behavior given a set of heterogeneous constraints plus an objective.**
- In short, combining **Formal Rational Analysis** with **Bounded Rationality**

Constraint Analysis Overview

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Explaining the Bounds on Adaptation

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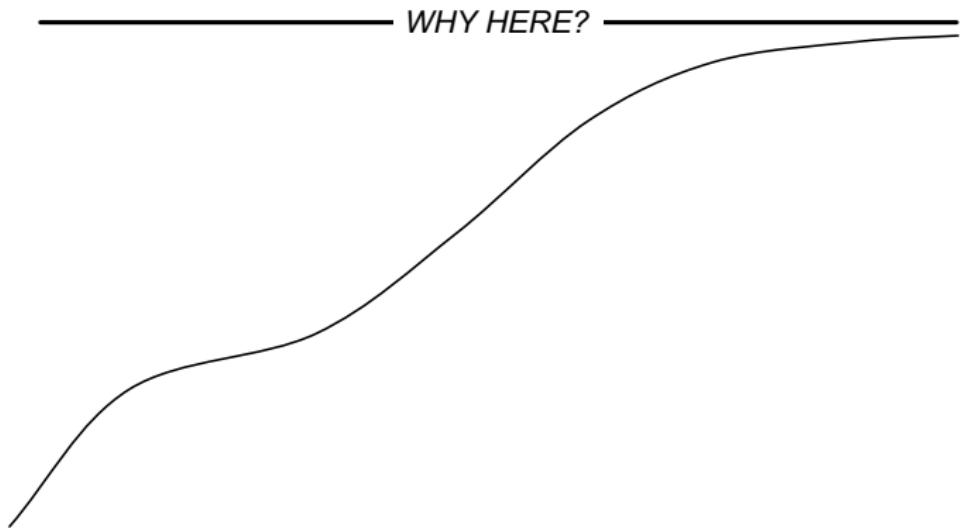
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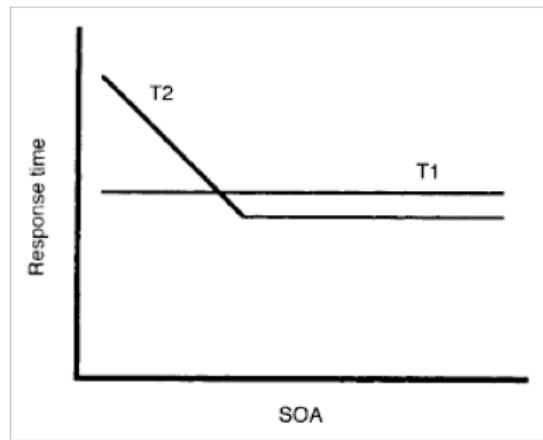
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Typical PRP (psychological refractory period) Experiment

- Choice response to a tone (T1) and a pattern (T2).
- Give priority to the tone response.
- Tone presented first, pattern stimulus is presented after an SOA.
- According to Meyer and Kieras, elevated RT2 is because participants ensure T2 response is after T1 response
- They called this *Strategic Response Deferment* (SRD).



Simple Dual-Tasking PRP Study

Ruthruff et al., 2003 report a PRP experiment with:

- Single participant.
- Unordered responses.

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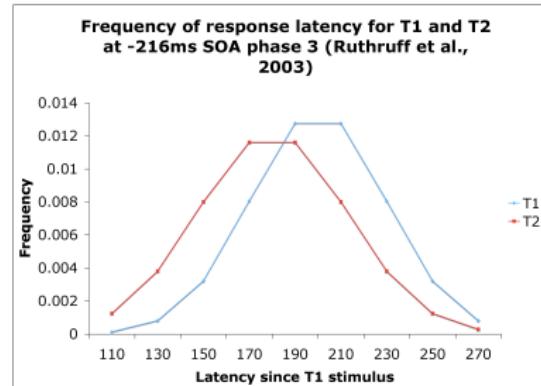
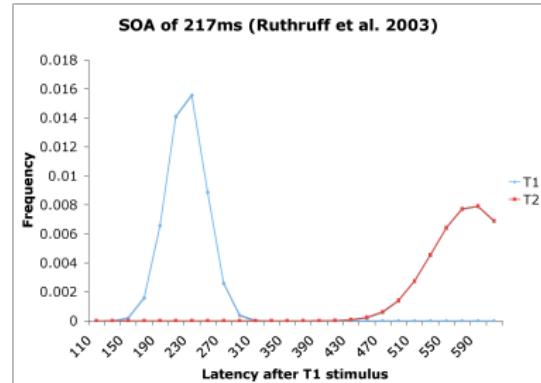
Summary

Ruthruff et al., 2003 report a PRP experiment with:

- Single participant.
- Unordered responses.

Now imagine if subject must produce **ordered** responses:

- At long SOAs no SRD is required to avoid response reversal.
- At short SOAs more than 50% response reversal when objective not sensitive to reversal.



A Very Simple Constraint Model

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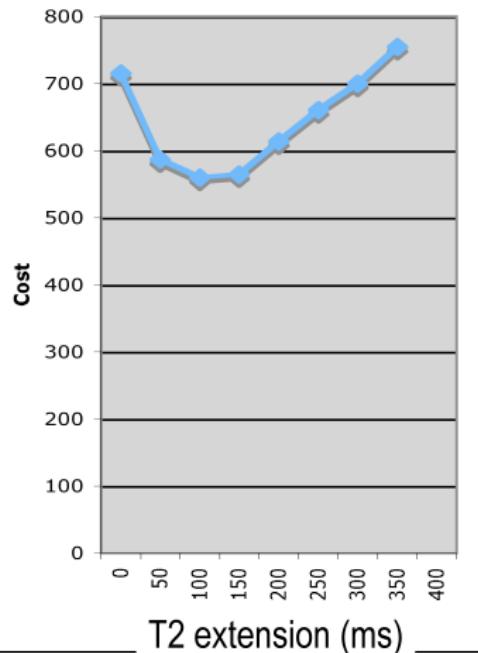
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Summary

- Constraints consist of the mean overall RTs and SDs.
- Space of strategies defined by a single variable: Extension of T2 response (E).
 - A simple form of Meyer and Kieras' SRD
- Objective is to minimize duration and response reversals.
 - Note the **trade-off**: Reduced reversals vs. total duration.

Combining Task + Architecture to Compute Optimal Behavior

- Now we can compute cost function from Monte-carlo simulations given this subject's standard deviation of RTs.
- Note that this combines two features:
 - Constraints on the **TASK** (ordering and speed constraints, as expressed through explicit payoff).
 - Constraints on the **ARCHITECTURE** (noise in the performance system).



Simple Ordered Responses

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New experiments (Kopecky):

- ① Visual cue appears.
- ② Subject must quickly press two keys in order:
 - Left index, right middle.
 - Left middle, left index.
 - Right ring, left middle.
 - etc.
- ③ Subject rewarded for speed and accuracy.

SIMPLE MODEL

- Subjects defer R2 for IRI milliseconds after R1, where IRI maximizes payoff given their indiosyncratic variance.

Explicit Payoff Schemes

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Subjects were rewarded with CASH with explicit payoff schemes. Example:

- If correct and Total RT $< 500ms$, then award $100 - RT/5$ points.
- If correct and Total RT $\geq 500ms$, then award zero points.
- If incorrect, then lose 100 points.

Sample Payoff Curves at 4 Different Standard Deviations (SD) of IRI

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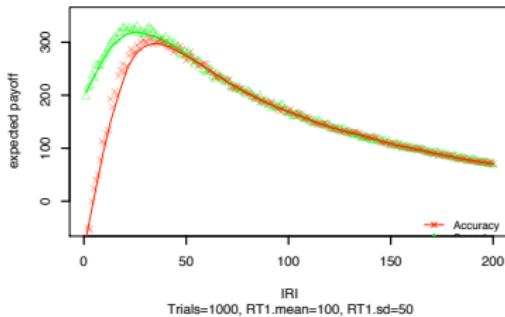
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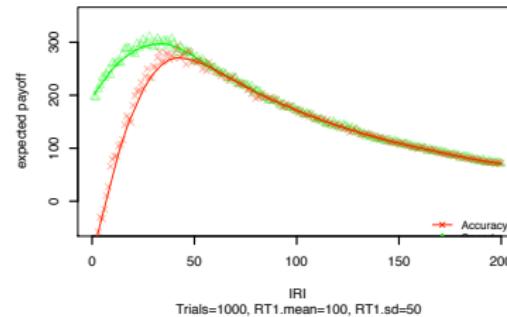
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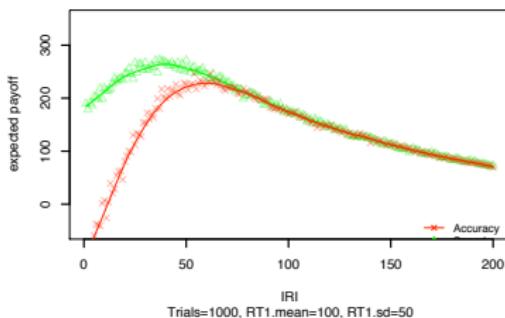
Expected payoff as function of IRI at SD=16



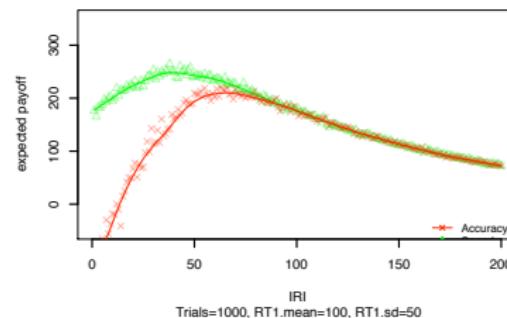
Expected payoff as function of IRI at SD=21



Expected payoff as function of IRI at SD=31

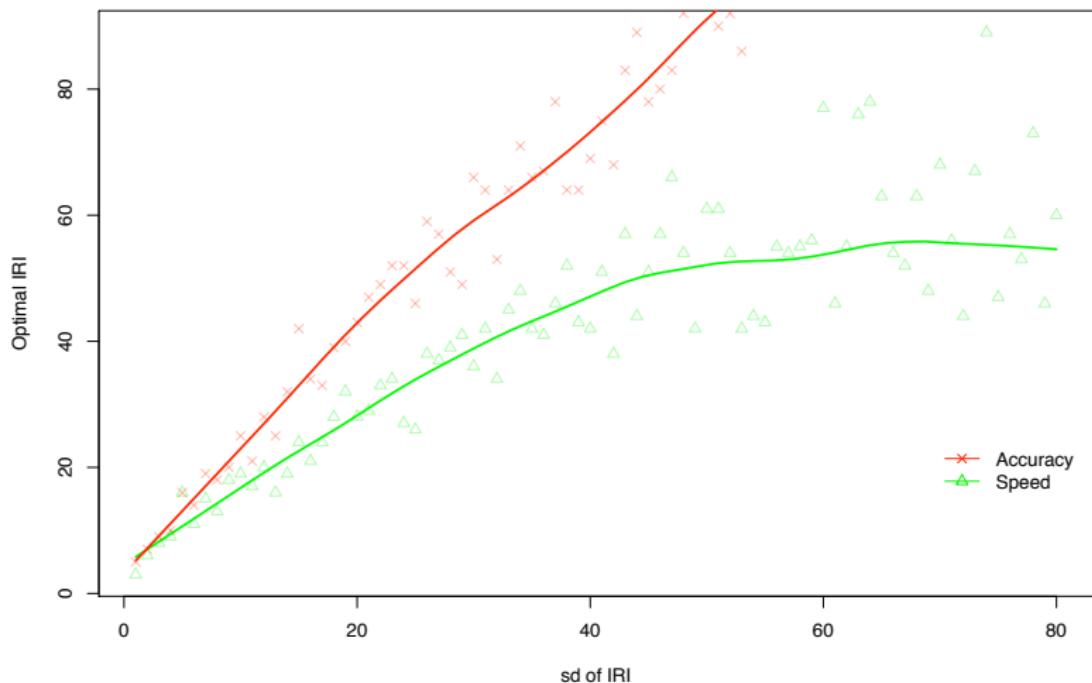


Expected payoff as function of IRI at SD=36



Predicted optimal IRI as function of SD of IRI

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A Good Subject

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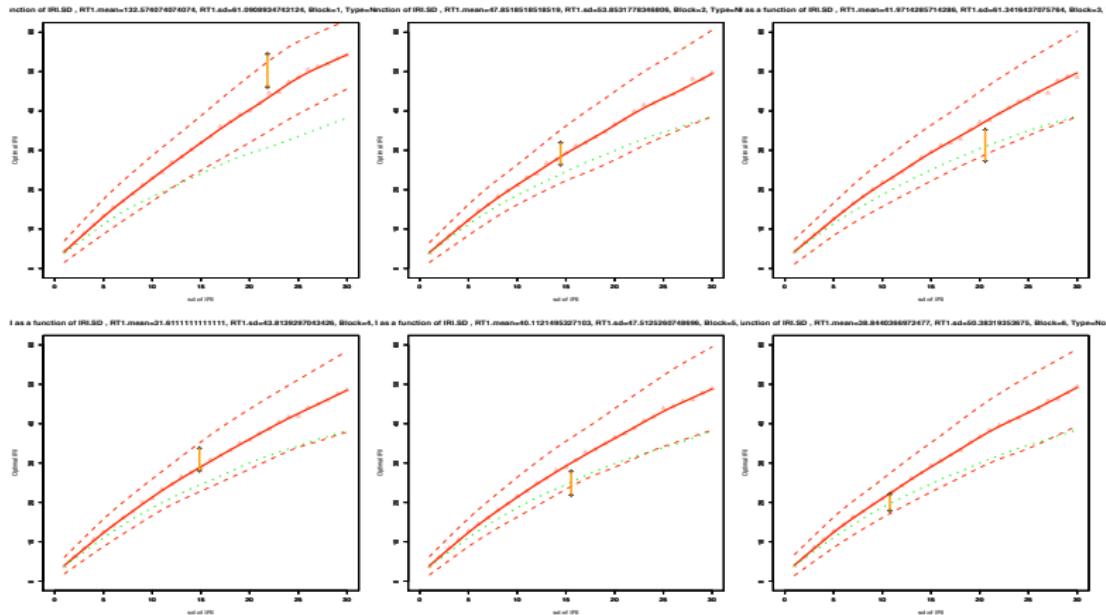
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Another Good Subject

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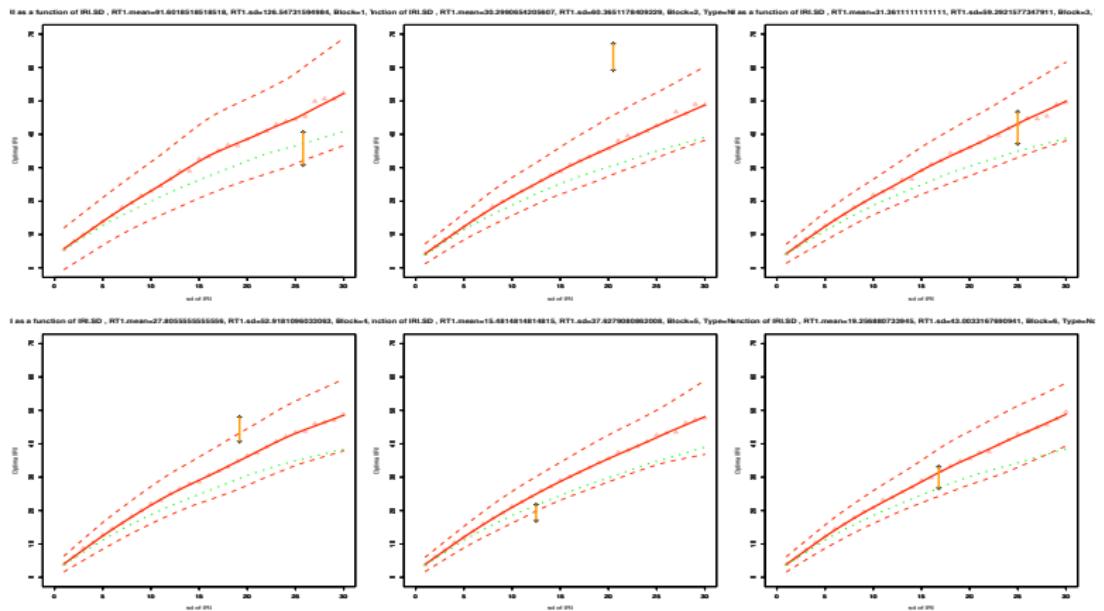
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A So-So Subject

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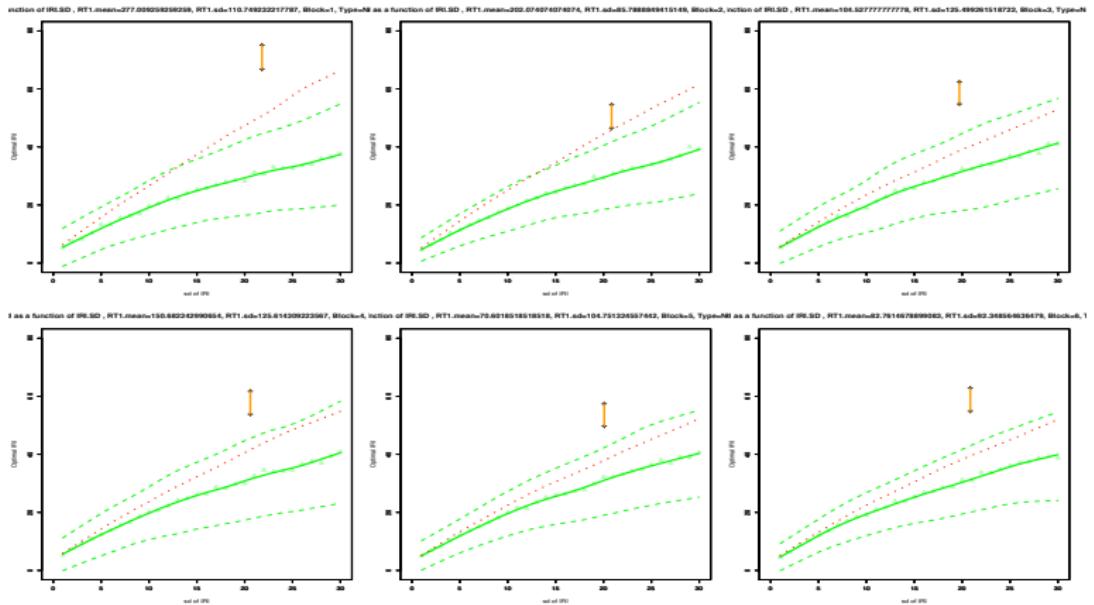
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All Subjects, all Finger-Pairs: Actual vs. Predicted Optimal Points

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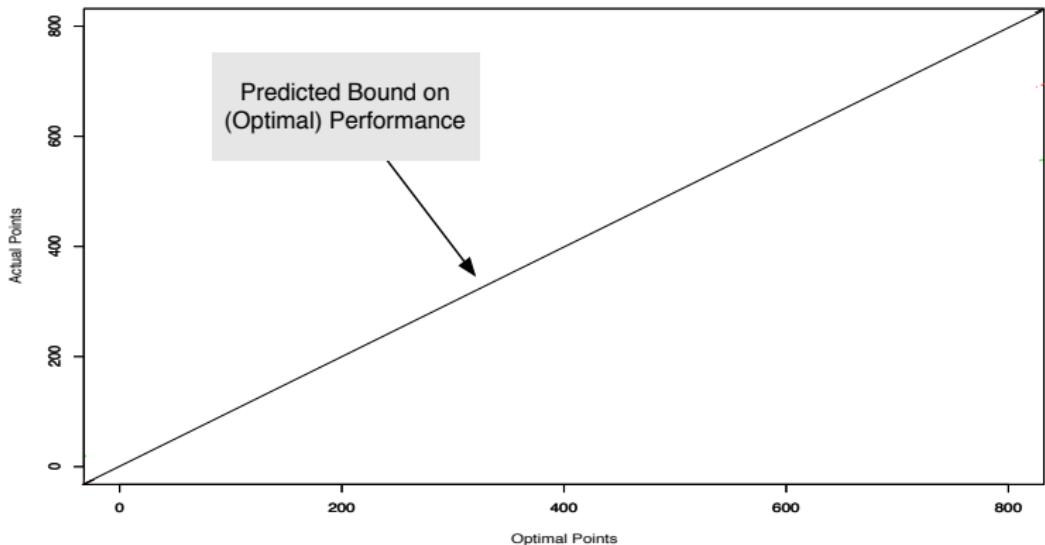
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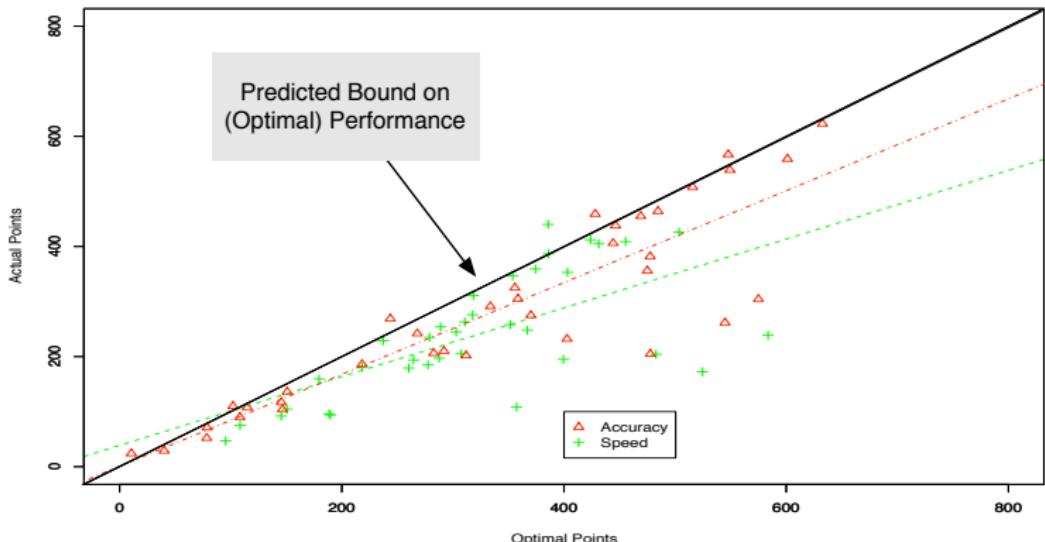
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This was a simple task where the strategy space = single quantitative variable.

Analysis of more sophisticated strategies needs a more general solution... .

Cognitive Constraint Modeling

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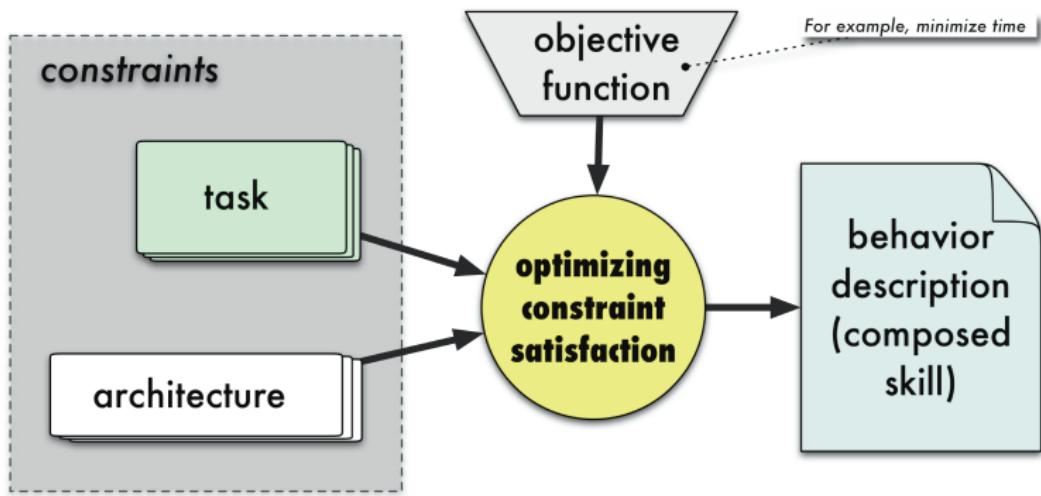
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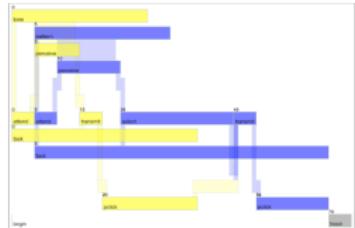


Cognitive Constraint Modeling

The tool is called CORE: Constraint-based Optimizing Reasoning Engine

$$\begin{aligned} \forall P_j: & \{ (\text{isa}, \text{process}) (\text{name}, \text{initclick}) \\ & (\text{start}, S_j) (\text{duration}, D_j) \} \subseteq P_j \\ \rightarrow & \exists P_i: \{ (\text{isa}, \text{process}) (\text{name}, \text{click}) (\text{start}, S_i) \} \subseteq P_i \\ & \wedge S_j + D_j \leq S_i \\ & \wedge S_i - (S_j + D_j) \leq 300 \end{aligned} \quad (3)$$

Constraint Satisfaction



Constraints are logical relations between variables. They may specify partial values (e.g., duration, $D_i > 24$ ms), are non-directional (E.g. $S_j \leq E_i + 300$ ms), and declarative.

Behavior Graphs

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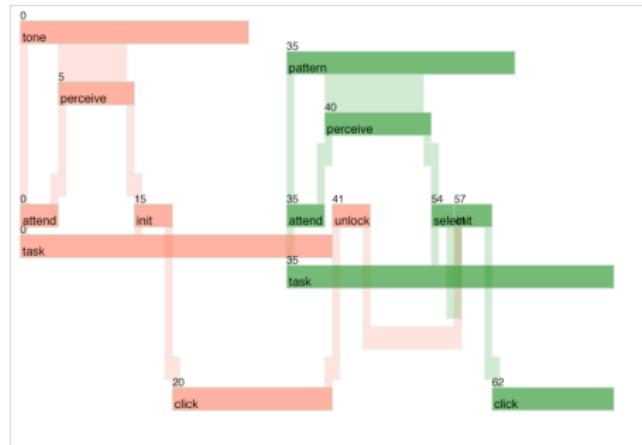
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- Boxes represent **cascaded processes**.
- Rows of processes represent **resources** (cognition, perceptual, motor) and **world events**.
- Time is represented from left to right.
- Horizontal position represents onset.
- Spatial extent represents duration.

Dual-task (PRP) with simple set of process & information-flow constraints (50ms SOA)

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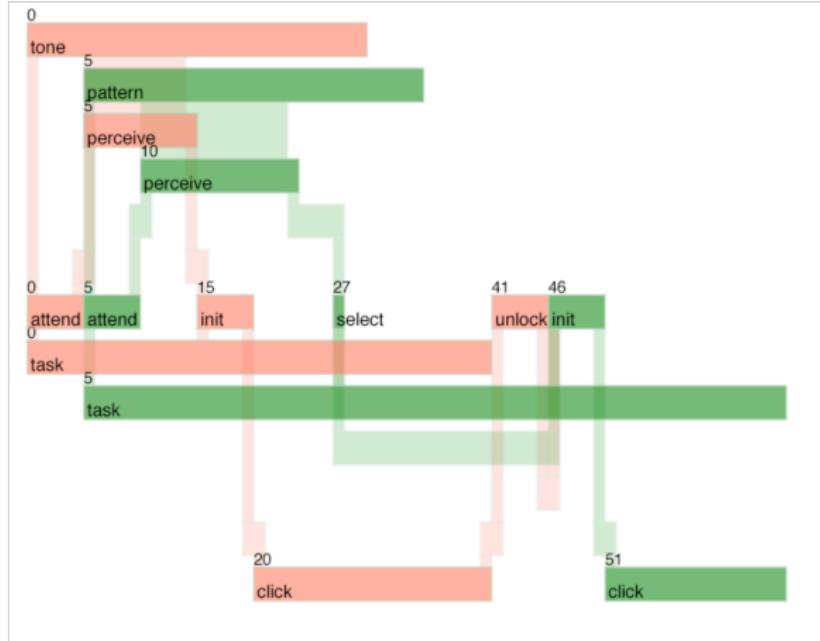
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**But does the approach scale to more
complex tasks?**

Comparing two cockpit designs

777



FDF



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Goals:

- New design should reduce errors
- New design should be no slower than old

777 Interface: Task 1



"You are following the altitude restrictions of the Moorpark 3 arrival; your last altitude clearance was 1-7 thousand. Descend via the Moorpark 3 arrival; maintain 1-2 thousand"

1. Verify current vertical mode
2. Dial Altitude Selector down to 12,000
3. Hit Altitude Selector
4. Verify new altitude
5. Verify new vertical mode

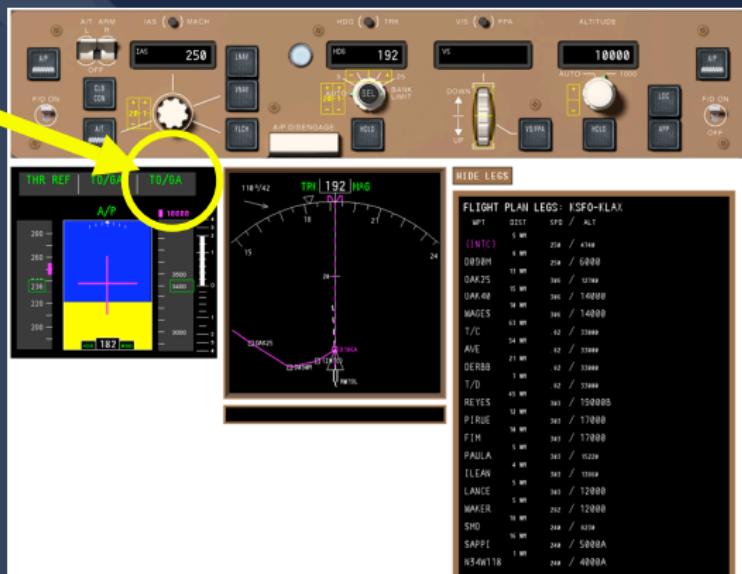


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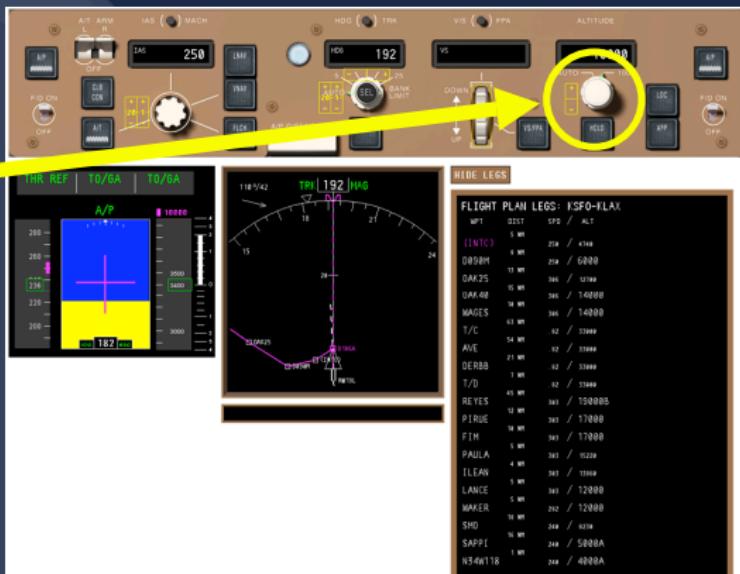


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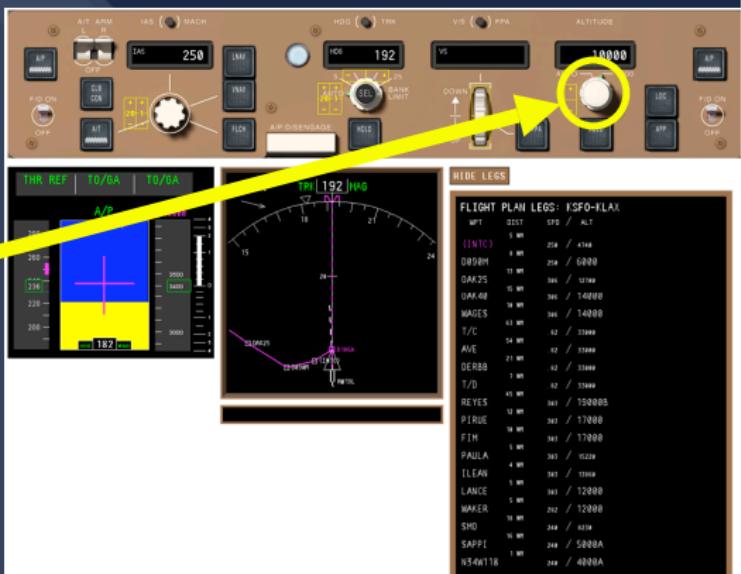


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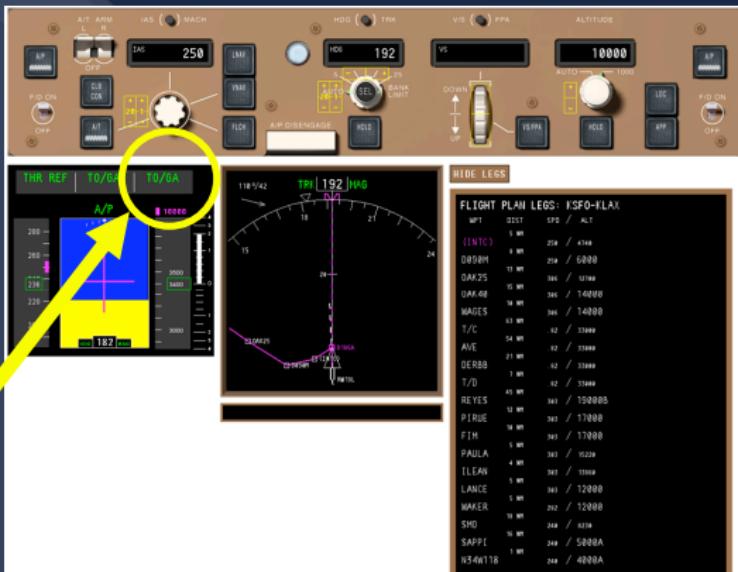


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The Demands of Applied Modeling

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- Not just interested in *time*, but **memory load** and **ability to handle interruption**
- Tracking memory load requires specifying what must be held in memory and when
- Our task specification language and models capture this in the form of **information flow constraints**...

A Natural Task Specification

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Captures the task's **information flow** rather than a fixed sequence of steps.

boeing FDF ttl

→

```
comprehend situation           : FLIGHT_PLAN LAST_CLEARANCE,  
comprehend clearance          : INSTRUCTION ALTITUDE,  
get vertical_mode after INSTRUCTION ALTITUDE    : VMODE,  
set altitude to ALTITUDE given INSTRUCTION VMODE   : DIALED PUSHED,  
check limit against ALTITUDE after DIALED PUSHED : LMT_CHECKED,  
check ap_status against INSTRUCTION after LMT_CHECKED : AP_CHECKED.
```

Emergent Strategies

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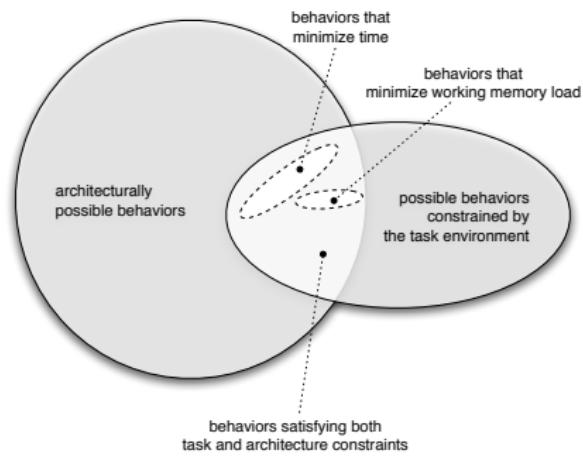
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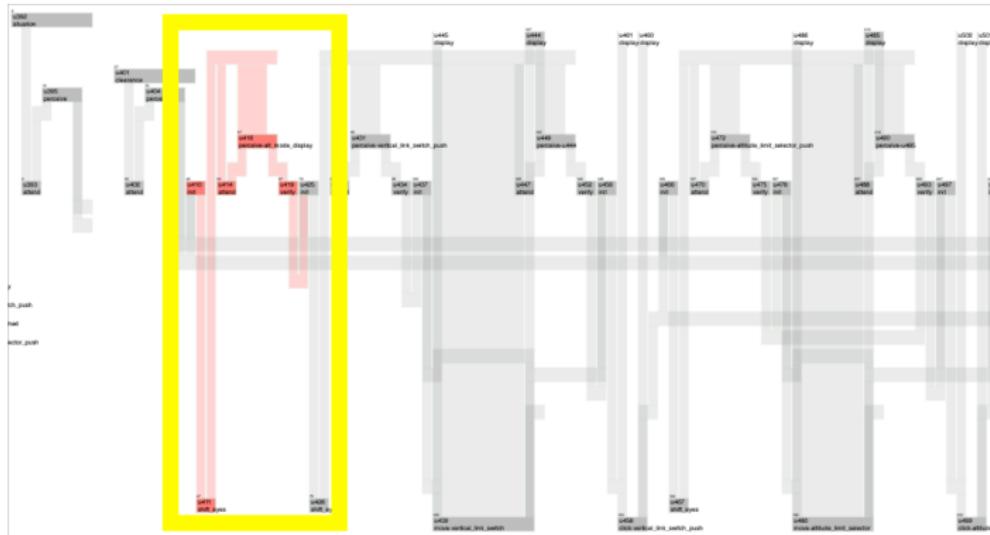
Summary

- Fully specified task constraints may still leave many details of behavior unspecified
- These details are automatically worked out by CORE to satisfy the architectural constraints
- *Example:* Precise timing of the perception of the mode information



Emergent Strategies

Early look to the mode display, in series with the rest of the task:



Emergent Strategies

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Later look to the mode display, in parallel with dialing the altitude:



A PRP Emergency!!

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WHAT IF . . . the pilot had to handle an auditory interruption that required a manual button press response?

boeing FDF ttl



`comprehend situation`
`comprehend clearance`
`get vertical_mode`
`set altitude`
`check limit`
`check ap_status`

auditory interruption



`auditory tone,`
`attend auditory`
`perceive auditory tone,`
`choose_response`
`press key.`

A PRP Emergency!!

WHAT IF . . . the pilot had to handle an auditory interruption that required a manual button press response?

task



**auditory interruption,
boeing FDF ttl.**

Auditory Interruption

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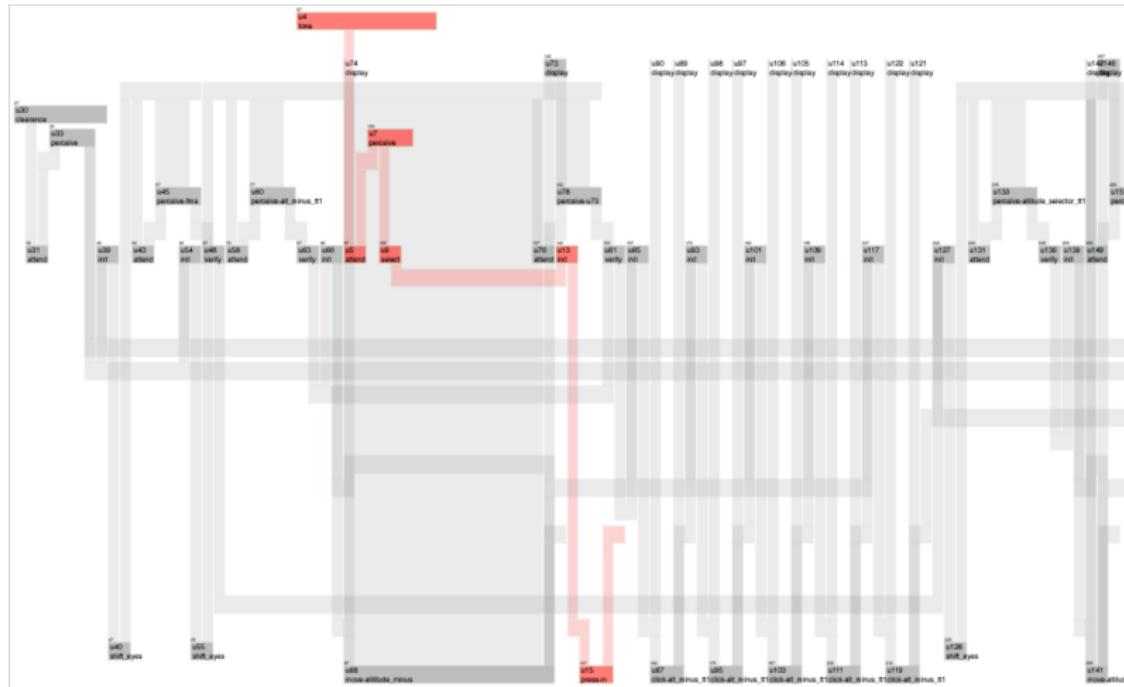
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Visual Interruption

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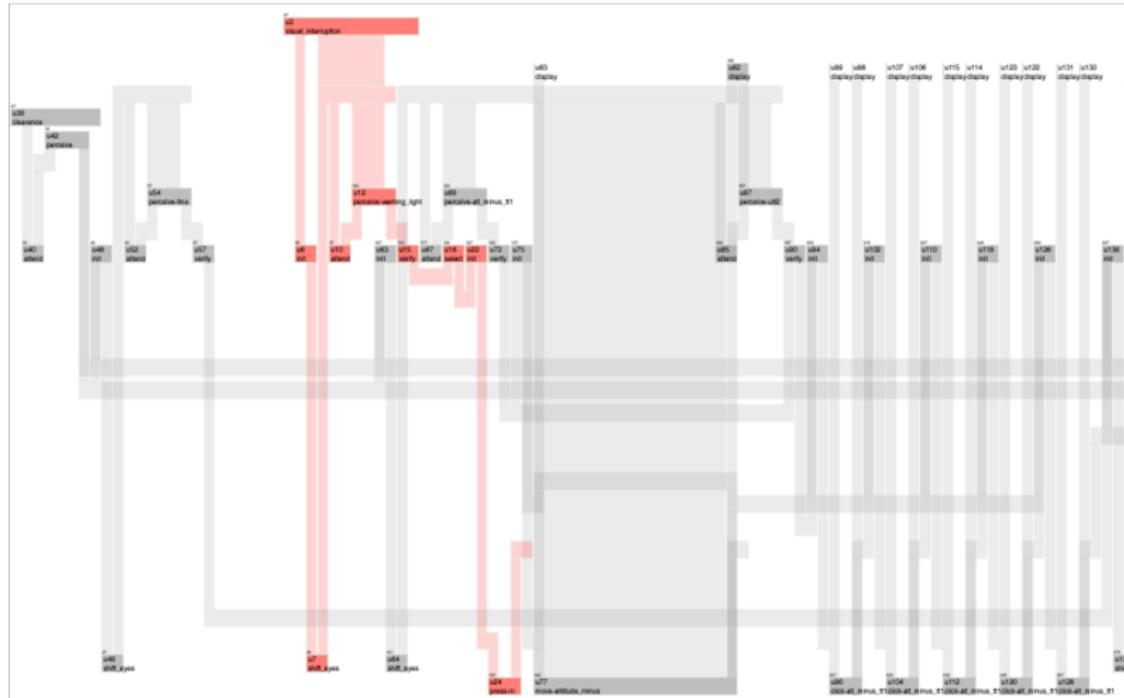
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Visual Interruption

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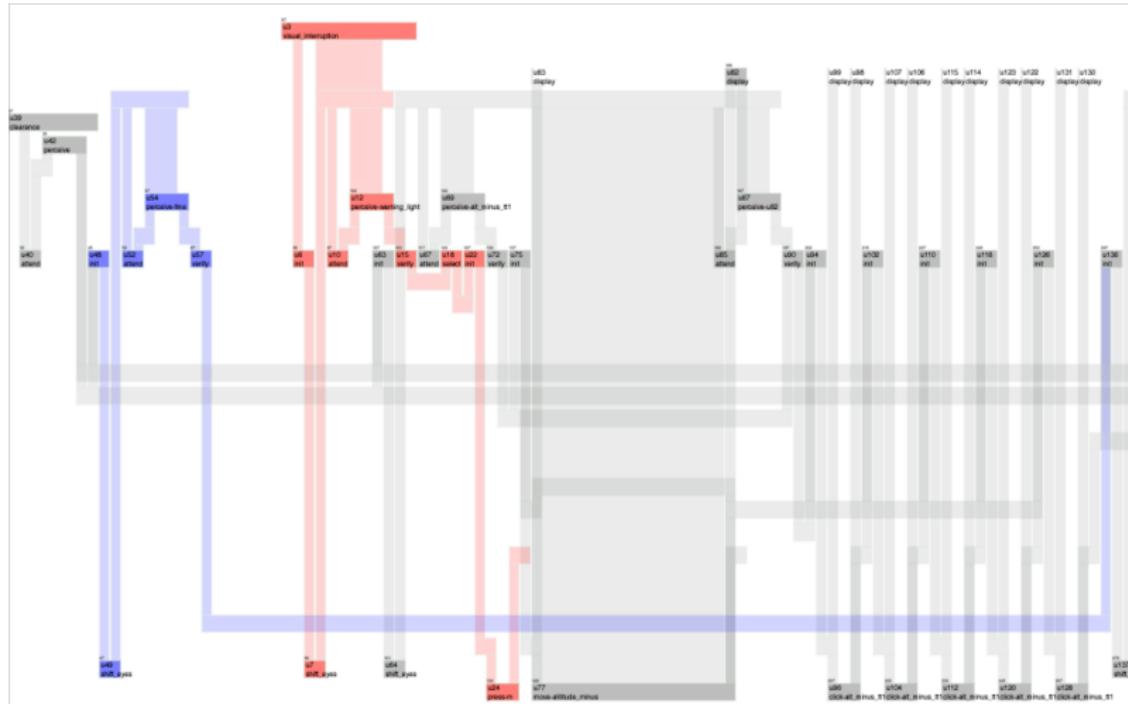
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Same Task Spec, Different Objective: Reduce Memory Load

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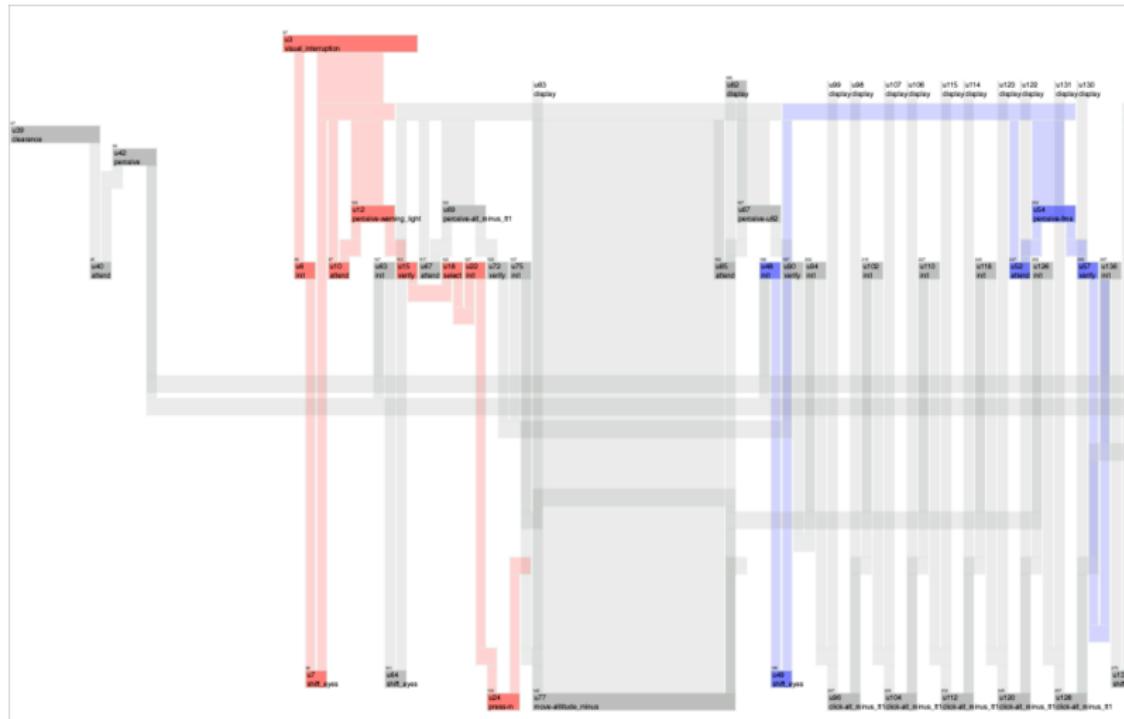
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24 Models

Alina Chu (UM) and Katherine Eng (NASA)

2 interfaces {FDF, 777} × 2 tasks × 3 interruption conditions × 2 optimizations {time, WM}

Interesting predictions:

- ① FDF faster than 777
- ② Little difference in WM load
- ③ Simple auditory interruption slightly increases time and WM load
- ④ Simple visual interruption increases time more, and effect is greater for 777

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**But is this just a different way to do
architectural modeling, or does it really
change the way we should build and test
cognitive models?**

ACT-R vs. EPIC, in Psych Review (2001)

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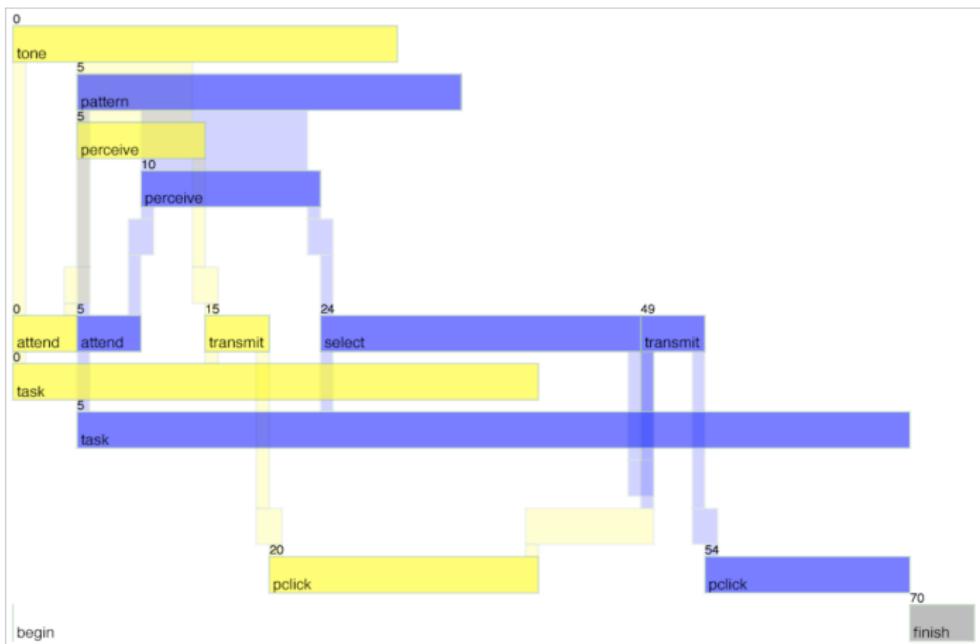
Summary

- In a prominent article promoting **an ACT-R account of PRP effects**, Byrne & Anderson (2001) created models that exhibited a *dual-task interference effect* based on ACT-R's theory of memory activation.
 - In ACT-R, retrieval time from memory is sensitive to a limit on total source activation.
 - The more retrieval features on the goal, the less activation each features receives.
- The models exhibited a dual-task interference effect because the source activation was less when tasks overlapped and the goal contained features from both tasks.

We can model this as a constraint.

An ACT-R model of the PRP task

Our reconstruction of one of the models in Byrne & Anderson (2001), *Psychological Review*:



What did the original ACT-R model explain?

Outline

Overview of
Constraint
Analysis

Example #1:
Dual-tasks

How It Works

Example #2:
777 Cockpit

Example #3:
ACT-R
Critique

Summary

- Byrne and Anderson created several ACT-R models (based on particular strategies) that fit the data.
- **But if a better strategy is available, given ACT-R's constraints, has skilled PRP performance been explained?**

ACT-R model (optimal)

Outline

Overview of
Constraint
Analysis

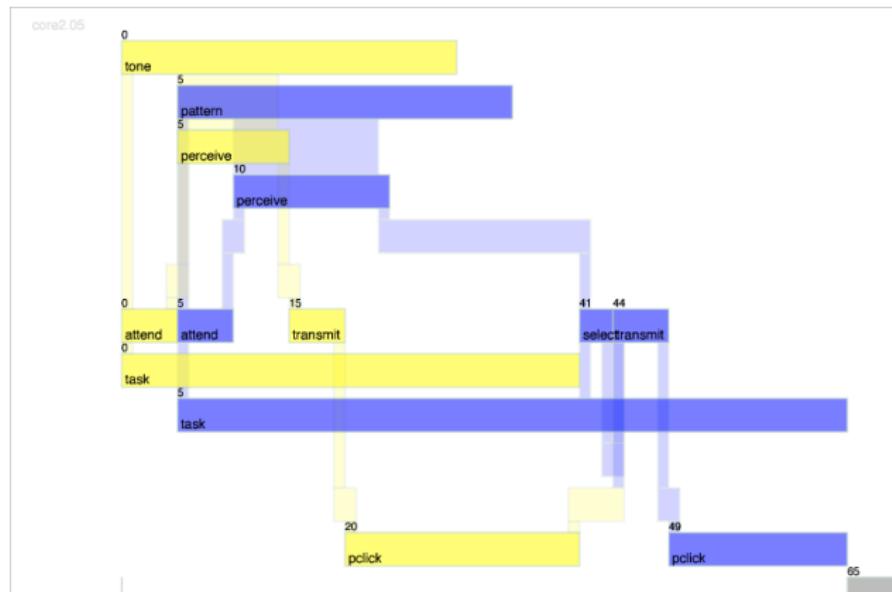
Example #1:
Dual-tasks

How It Works

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777 Cockpit

Example #3:
ACT-R
Critique

Summary



The optimal model not only deferred response, **but deferred retrieval too**. Byrne and Anderson didn't think of this—and neither did we.

An Astonishing Result

Outline

Overview of
Constraint
Analysis

Example #1:
Dual-tasks

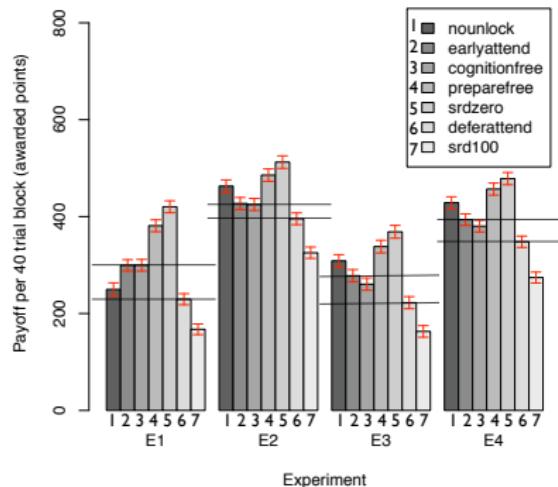
How It Works

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777 Cockpit

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Critique

Summary

Using CORE, we performed a systematic analysis of possible strategies for ACT-R models on all four PRP experiments modeled in Byrne & Anderson (2001), computing the expected payoff based on 40,000 runs.



An Astonishing Result

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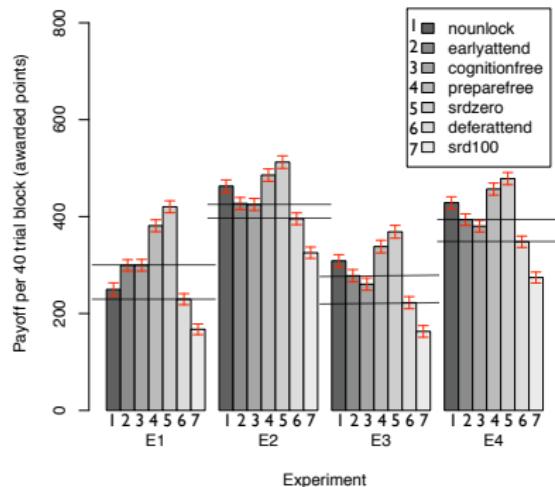
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Summary

Using CORE, we performed a systematic analysis of possible strategies for ACT-R models on all four PRP experiments modeled in Byrne & Anderson (2001), computing the expected payoff based on 40,000 runs.



In each experiment, the Byrne & Anderson models consistently underperform—sometimes by substantial amounts—the best strategy.

Summary/Nuggets de Oro

- ① Adaptation is bounded by the task environment and architecture.
- ② An architectural theory explains behavior, with no further assumptions, if the optimal performance predicted by the theory corresponds to the observed asymptotic bound.
- ③ **Constraint satisfaction can be used to predict the asymptotic bound on adaptation, formally deriving the predictions of an architectural theory while minimizing assumptions about strategy.**
- ④ **Significant theoretical and applied benefits may accrue from this approach and its associated tools.**

Nuggets de Carbón

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Summary

- ① **Efficiency.** Some models take 2 seconds, some take 24 hours, some never return.
- ② **Interaction with task simulation.** Presently, can't be done.
- ③ **Difficulty formalizing learning constraints.** Presently, can't be done (though we haven't really tried).

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