



中国石油大学  
CHINA UNIVERSITY OF PETROLEUM

**JET 101**

# 石油工程数值分析及数据可视化方法

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# Python科学计算

## □ 学习目标

学习目标	学习成果	效果考察	课程活动
应该掌握哪些知识？	应该能够做哪些事情？	怎么考察学生？	应该怎么学习？
<b>1. 实战非线性方程解法</b> <ul style="list-style-type: none"><li>• 数学算法回顾</li><li>• Scipy库的使用</li></ul> <b>2. 中期Project答疑</b> <b>3. 期末Project的Proposal</b>	<b>1. 能够针对数学算法自行编程求解</b> <b>2. 可以找到对应的库进行求解计算</b>	<b>1. 测试学生是否能编程二分法解非线性方程</b> <b>2. 测试学生能否寻找并使用scipy</b> <b>3. 课堂测验简单问题</b> <ul style="list-style-type: none"><li>• 期末Proposal</li></ul>	<b>1. 完成期中Project</b>



## □ 非线性方程（Root finding）解法

$$f(x) = 0$$

**PR气体状态方程**  $f(x) = Z^3 + (B - 1)Z^2 + (A - 2B - 3B^2)Z - AB + B^2 + B^3$

**Colebrook管流压耗摩阻系数**  $\frac{1}{\sqrt{f}} = -2 \log \left( \frac{\varepsilon}{3.7 D_h} + \frac{2.51}{\text{Re} \sqrt{f}} \right)$

- Bisection method（二分法）
- Fixed-Point Iteration (不动点迭代法)
- Newton-Rapson Method (牛顿迭代法)



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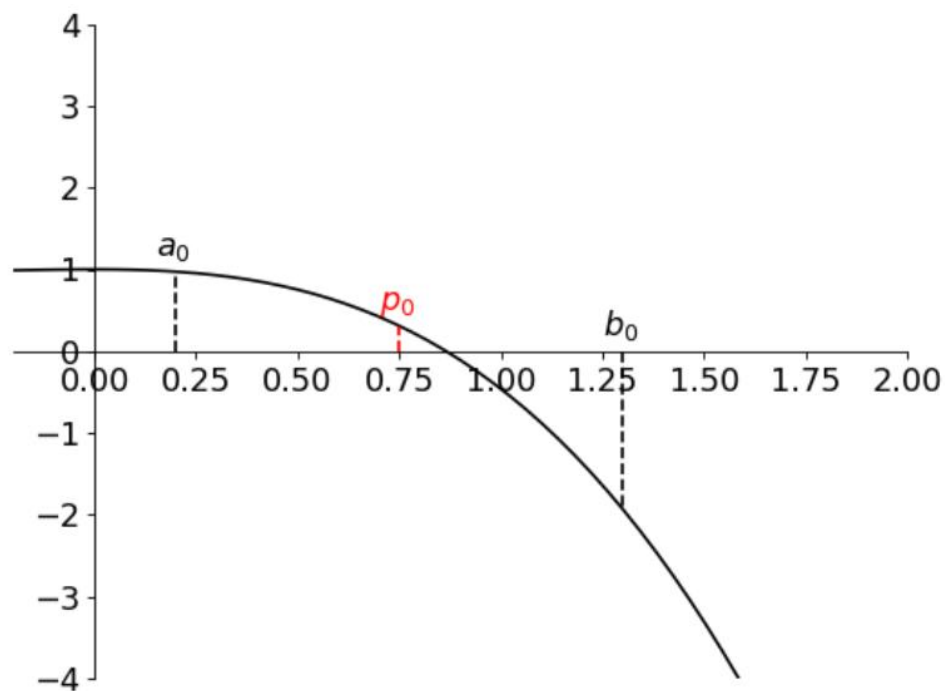


# Python科学计算

## □ 非线性方程（Root finding）解法 – 二分法

$$f(x) = \cos(x) - x^3$$

$$a_0 = 0.2, \quad b_0 = 1.3$$



INPUT endpoints  $a, b$ ; tolerance  $TOL$ ; maximum number of iterations  $N_0$ .

OUTPUT approximate solution  $p$  or message of failure.

Step 1 Set  $i = 1$ ;  
 $FA = f(a)$ .

Step 2 While  $i \leq N_0$  do Steps 3–6.

Step 3 Set  $p = a + (b - a)/2$ ; (Compute  $p_i$ .)  
 $FP = f(p)$ .

Step 4 If  $FP = 0$  or  $(b - a)/2 < TOL$  then  
OUTPUT ( $p$ ); (Procedure completed successfully.)  
STOP.

Step 5 Set  $i = i + 1$ .

Step 6 If  $FA \cdot FP > 0$  then set  $a = p$ ; (Compute  $a_i, b_i$ .)  
 $FA = FP$   
else set  $b = p$ .

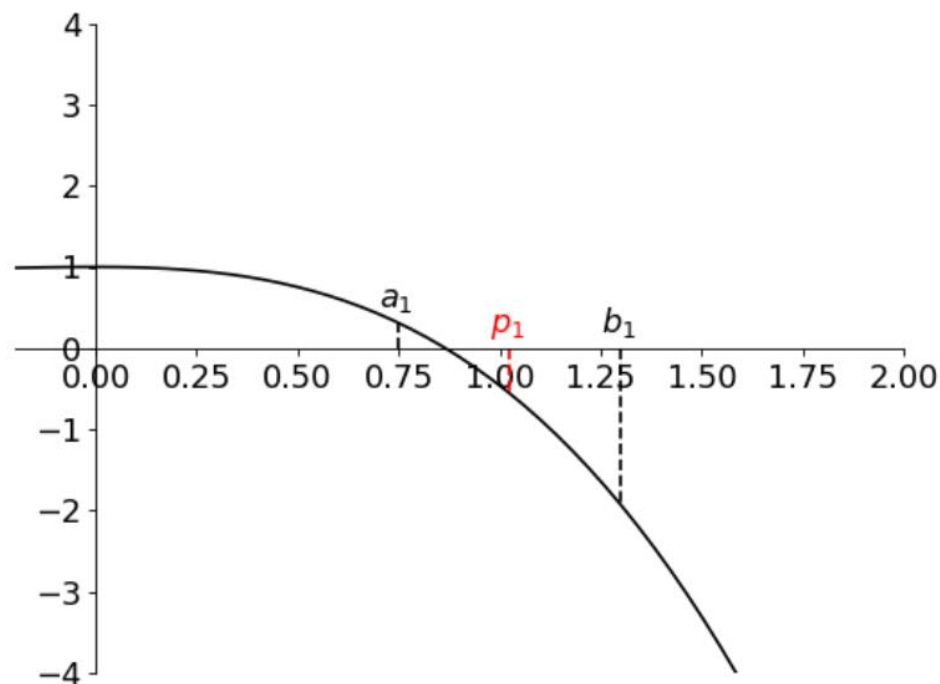
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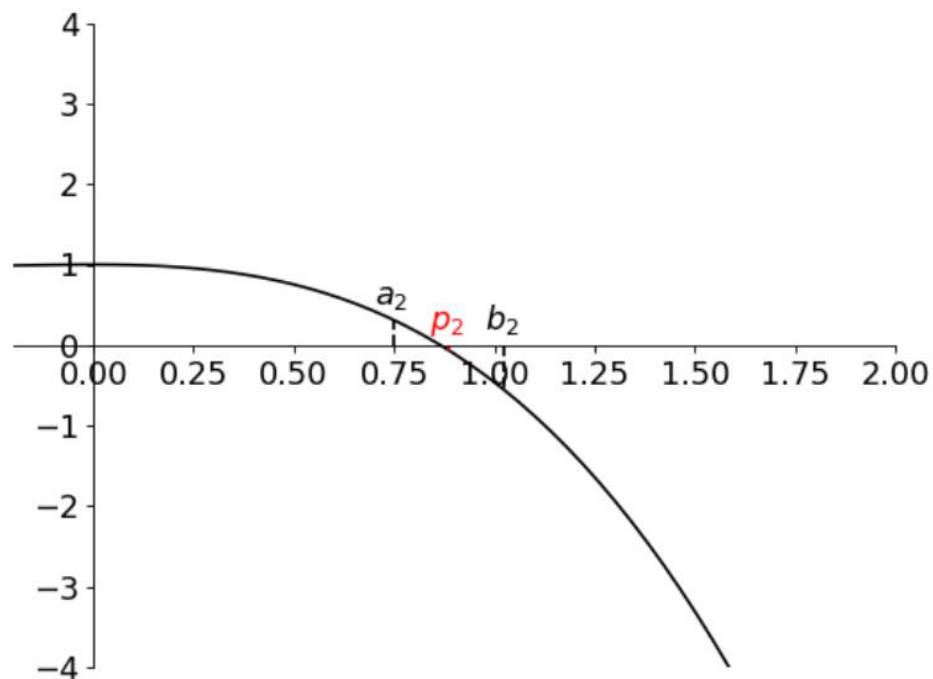
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i	a	b	p
1	0.2	1.3	0.75
2	0.75	1.3	1.025
3	0.75	1.025	0.8875
..	..	..	
10	0.8649	0.8660	0.8654

INPUT endpoints  $a, b$ ; tolerance  $TOL$ ; maximum number of iterations  $N_0$ .

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## □ 非线性方程（Root finding）解法 – 作业

The Peng-Robinson Equation of State

$$P = \frac{RT}{V_m - b} - \frac{a\alpha}{V_m^2 + 2bV_m - b^2}$$

$$a = \frac{0.45724R^2T_c^2}{P_c}$$

$$b = \frac{0.07780RT_c}{P_c}$$

$$\alpha = \left(1 + \left(0.37464 + 1.54226\omega - 0.26992\omega^2\right) \left(1 - T_r^{0.5}\right)\right)^2$$

$$T_r = \frac{T}{T_c}$$

Where  $\omega$  is the acentric factor for the species,  
 $P_c$  is critical pressure,  
 $T_c$  is critical temperature.

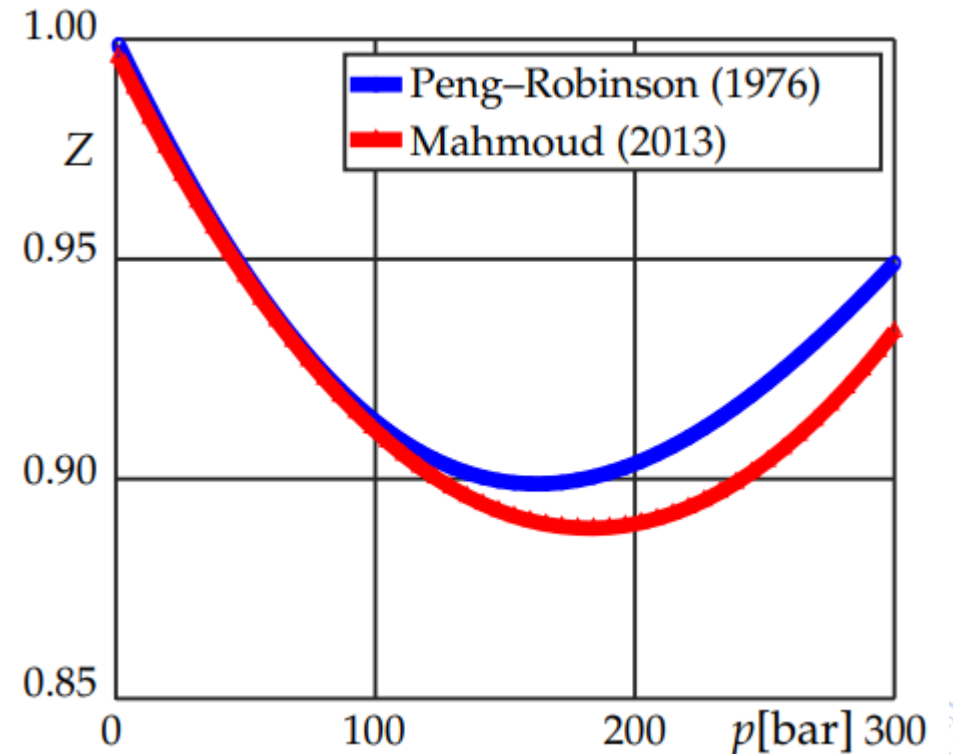
Values applied for 100% methane ( $\text{CH}_4$ ):

$\omega = 0.0115$

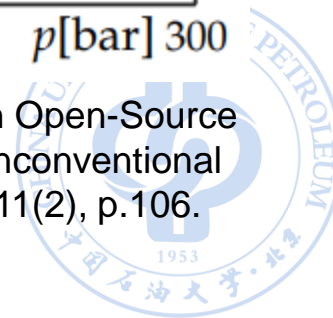
$T_c = 191.15 \text{ K}$

$P_c = 4.641 \text{ MPa}$

The ideal gas constant  $R = 8.314413 \text{ J/mol-K}$



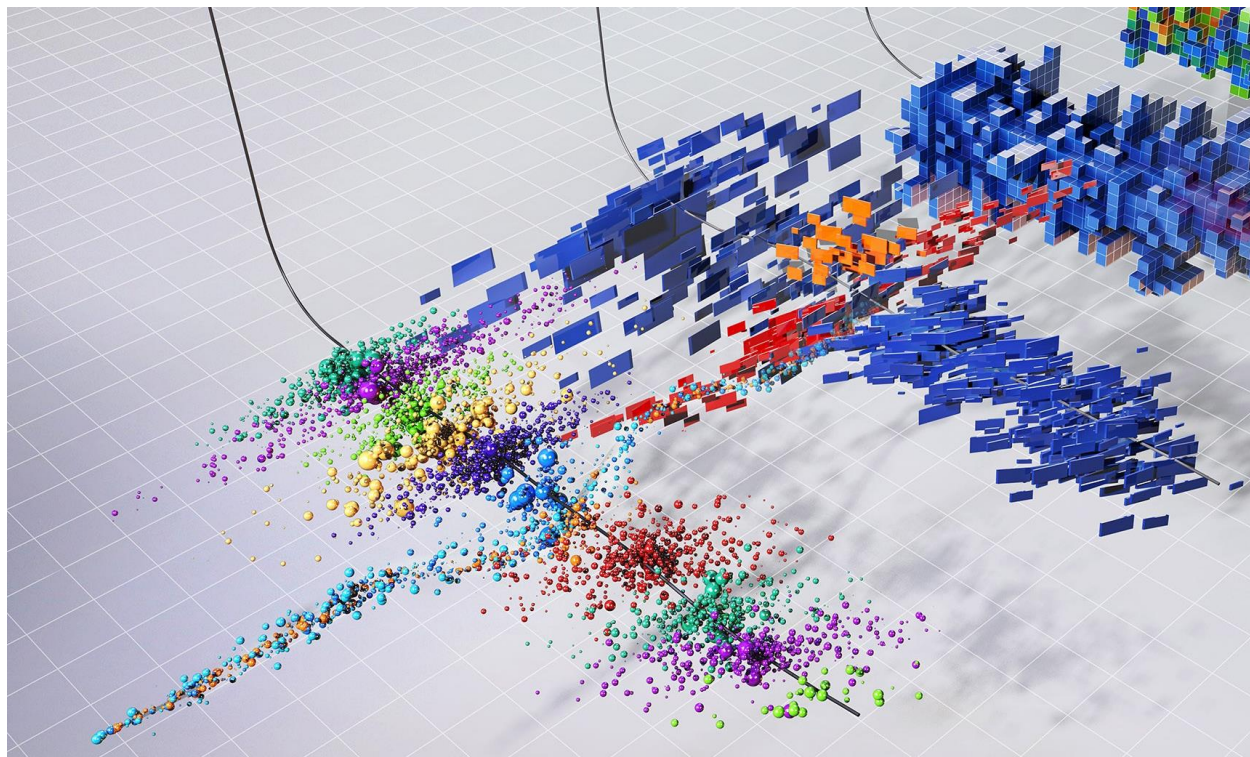
**Wang, B.** and Fidelibus, C., 2021. An Open-Source Code for Fluid Flow Simulations in Unconventional Fractured Reservoirs. *Geosciences*, 11(2), p.106.



# 课程大作业

## □ 期中大作业

- 组队或者单人（不超过3人）
- OnePetro阅读文献，从一个角度
- xlwings读单井数据Excel
- Matplotlib画2D井眼轨迹
- Matplotlib微地震散点图
- PyVista三维画图（奖励任务）

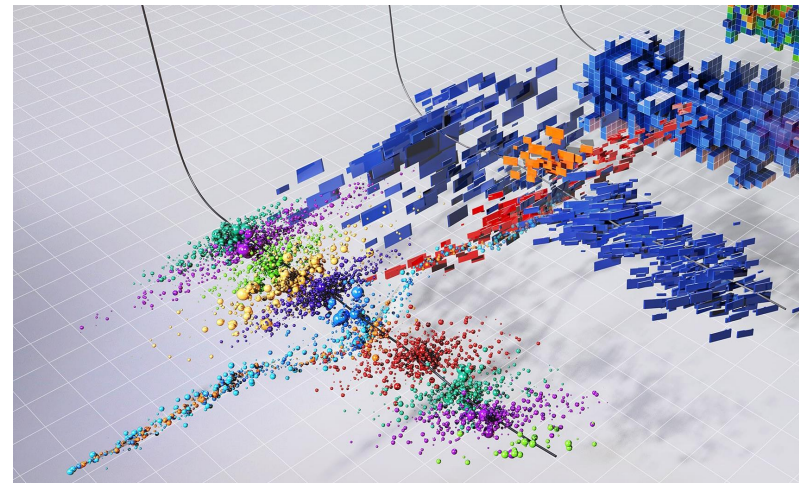
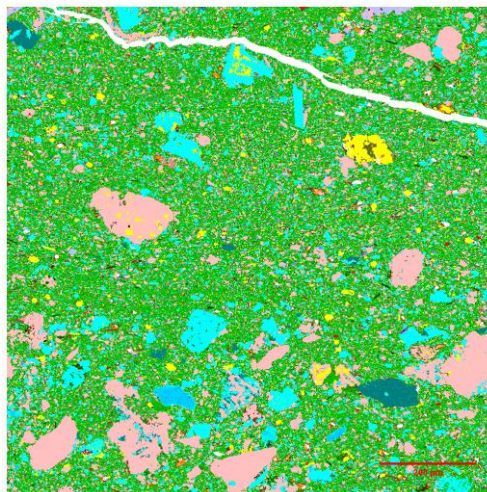
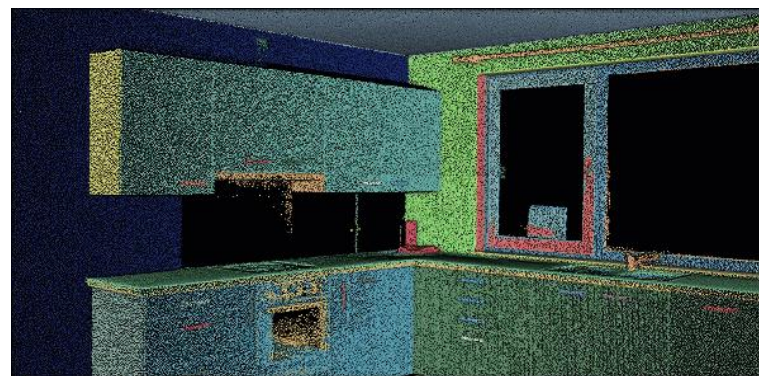




# 课程大作业

## □ 期末大作业选题

- QEMSCAN数字岩心矿物分割与分析
- 3D裂缝地层COMSOL网格转换
- 3D井眼轨迹与微地震数据可视化
- 3D微地震点云裂缝网重构\*
- 超临界CO<sub>2</sub>状态SW方程求解
- .....



\*<https://www.freehowtos.com/how-to-automate-3d-point-cloud-segmentation-and-clustering-with-python/>

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