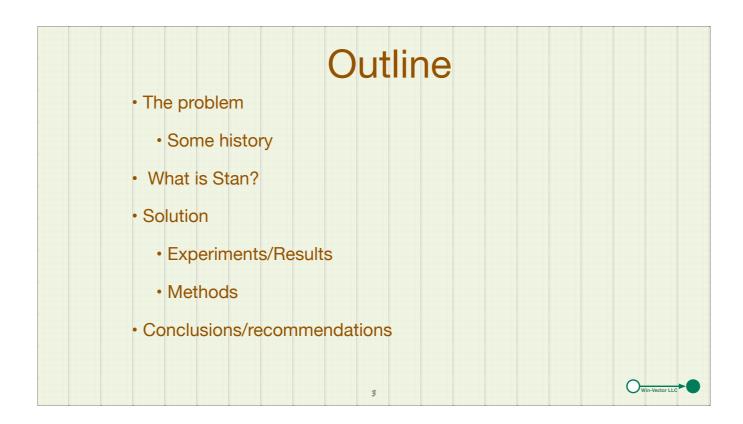


Slides, links, and code: https://github.com/WinVector/Examples/tree/main/rank Rehearsal video recording: https://www.youtube.com/watch?v=8x-RY8Ua4Go

Who I am

- John Mount, General Partner at Win Vector LLC.
 - Co-author of Practical Data Science with R, 2nd edition, Manning, 2020.
 - Co-author of the vtreat R package for re-encoding high cardinality explanatory variables.
- Win Vector LLC is a statistics, machine learning, and data science consultancy and training organization.
 - Specialize in solution design, technology evaluation, and prototyping.
 - We help greatly speed up solution and production deployment.
 - Looking for some more engagements.
 - Please contact: jmount@win-vector.com .
- Please follow us on the Win Vector blog: https://win-vector.com/blog-2/





I am going to try to outline an interesting problem, show you the basics of using Stan, and the basics of taking benefits from Stan's solution.



Example Problem

- User is shown 5 products online and clicks on one.
- User tastes 5 wines and buys at most one.
 - (repeat with 100 users thought to be in same persona)



We **wish** they would tell us a numerical valuation of each wine!



Our Goal

- Estimate the user (or user cohort) *intrinsic* preferences (independent of presentation position and other items).
 - Allows us to rate items with respect to user to retrieve, sort, estimate utilities and so on.
 - Eliminates some systems, such as xgb.XGBRanker (as it reproduces predictions over whole lists).



Formal Set Up

- Users (or user personas) have intrinsic unobserved preferences or valuations
 - •Personas are either representatives of a group of users or a label collecting together a group of users.
 - This lets us assume we can collect a lot of per-persona data.
- We (unfortunately) only observe user behaviors
 - Typical observation: we presented 5 alternatives and the user selected one.
 - Observation contaminated both by presentation position and alternative items in the presentation.
- Can we estimate persona preferences from persona behaviors?
 - Often called "learning to rank."
 - We can use estimated preferences to plan (a lot more than just predicting future list behaviors).
- Typically inferring hidden state from observations is very high value.
 - Stan can simulate inverting fairly complicated "hidden state to observations" processes.



Leaning to Rank History

- Tradition: each field develops solutions ignoring all other fields
 - BIG topic in search engines
 - · Joachims, T. (2002), "Optimizing Search Engines using Clickthrough Data", Proceedings of the ACM Conference on Knowledge Discovery and Data Mining
 - Tie-Yan Liu (2009), "Learning to Rank for Information Retrieval", Foundations and Trends in Information Retrieval, 3 (3): 225-331
- Huge survey: https://en.wikipedia.org/wiki/Learning to rank
 - Claims that logistic regression does not work
 - "Bill Cooper proposed logistic regression for the same purpose in 1992, and used it with his Berkeley research group to train a successful ranking function for TREC. Manning et al. suggest that these early works achieved limited results in their time due to little available training data and poor machine learning techniques."

Maybe Things Can Be Easy?

- If:
 - Most of the unobserved activation lists have two alternatives?
- Then:
 - This looks like the question structure from conjoint analysis
 - •Most of the unobserved activation lists are then identical to the observed selection lists.
 - Problem is solvable by direct item-wise logistic regression.



Maybe Things are Difficult?

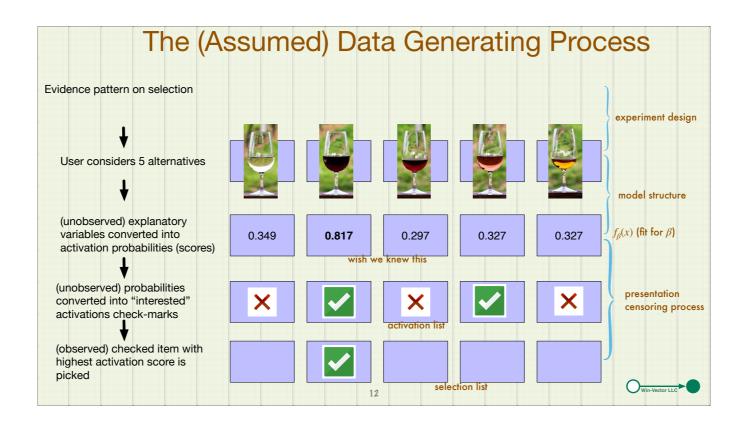
- Presentation position may be a strong influence
 - Users may be biased to pick earlier presentation positions, forget earlier positions, or even not even try/ look-at later positions!
 - Item quality may correlate with presentation position.
 - · What other items are in the list or panel having an effect (such as high priced irrelevant alternatives).
- · Data is low fidelity or censored
 - Selecting 1 out of 5 positions is only 2.3 bits of information
- · No-select lists may be coming from an unknown mixture of two sources
 - · Motivated Shoppers (with intent to buy, so non-buying strong evidence against all presented wines).

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- Idle Browsers (with no intent to buy, so non-buying against any wine).
- These are not the same persona! Would need per-user variables to sort these users out.
- Punishes highly desirable selections more than less desirable selections.

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O	ur	"V	Vin	e" E	X	am	np	le		
Artificial Problem		group	position	example_index	x 1	x2	хЗ	score	hidden_activation	selected
Artificial Froblem	0	0	0	7	0.00	1.00	1.00	0.295	False	False
Know answer	1	0	1	2	0.00	0.00	0.10	0.257	False	False
	2	0	2	3	0.00	1.00	1.00	0.304	False	False
3 explanatory variables: x1, x2, x3	3	0	3	8	0.00	1.00	1.00	0.288	False	False
	4	0	4	10	0.00	1.00	1.00	0.348	False	False
· Visible Data	5	1	0	1	1.00	6.00	0.00	0.546	True	False
	6	1	1	0	12.00	1.00	0.00	0.796	True	True
 Panels of 5 wines tasted in one sitt 	ing 7	1	2	3	0.00	1.00	1.00	0.326	True	False
	8	1	3	7	0.00	1.00	1.00	0.309	False	False
explanatory variables	9	1	4	2	0.00	0.00	0.10	0.210	True	False
	10	2	0	6	0.00	1.00	1.00	0.349	False	False
selected (if any) wine	11	2	1	0	12.00	1.00	0.00	0.817	True	True
	12	2	2	5	0.00	1.00	1.00	0.297	False	False
Many repetitions over many customers	13	2	3	10	0.00	1.00	1.00	0.327	True	False
thought to be in the same persona cluste	r. 14	2	4	8	0.00	1.00	1.00	0.327	False	False
				11				ur	nobserved	Vector LLC



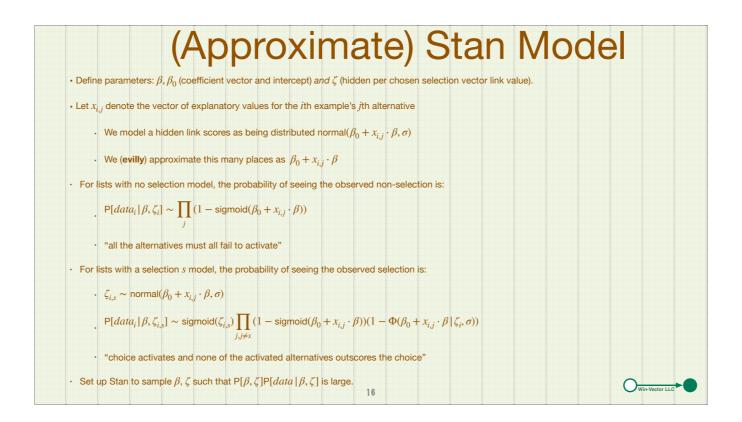


Stan

- A Markov Chain Monte Carlo sampler
- · Can be used for complicated Bayesian inference
 - Guesses likely values of parameters, and nuisance variables, and unobserved intermediate state conditioned on observed data.
 - Returns distributional answers.
- Fairly high dependency (requires C++ compiler and linker)
 - May eventually see competition from Torch based alternatives



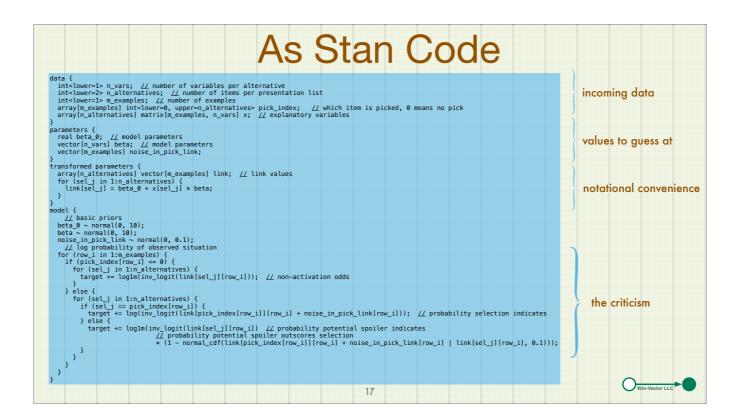




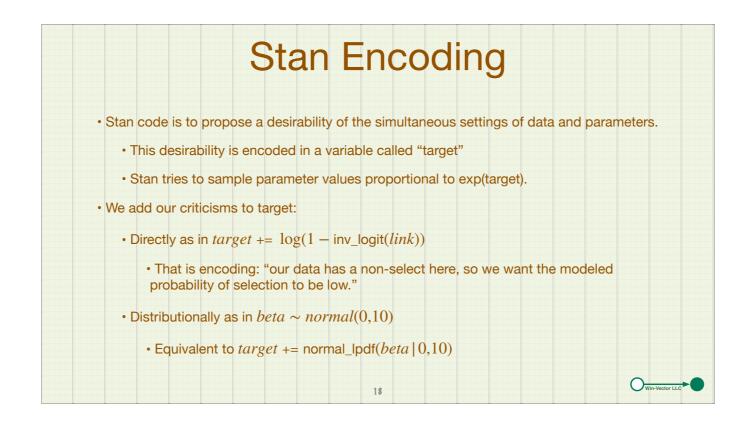
The usual "double negative world" of encoding statistical properties.

No selection arrises from failing to select any of the alternatives.

For a selection to prevail it must be activated, and none of the alternative must simultaneously activate and exceed the selection's score. We condition on an explicit link score to make the terms conditionally independent and justify multiplying probabilities.



Setting up the blocks is the trick. The main section is the model block, all other blocks are in service of the model block. We prefer vectorized operations and no control structures such as "for" or "if". In our case we have them, but notice all control structures are conditional on data and not on inferred parameters. This means the scoring process is the same for all parameter values, and we are well within the design regime of Stan. Stan maximizes the hidden variable "target".



Have to get comfortable with mixing probabilities and densities. Easiest to thin of the Stan code as a grouped criticism, and not worry over much what is prior and posterior conditioning.

The math from 3 slides ago is only these few lines.

Calling Stan from R or Python library(rstan) library(jsonlite) data <- fromJSON("rank_src_censored_picks.stan")</pre> sample <- stan(</pre> data = data, # Stan program data = data, # named list of data chains = 4, # number of Markov chains cores = 4, # number of cores (could use one per chain) refresh = 0, pars=c("lp__", "beta_0", "beta") # no progress shown # parameters to bring back draws <- as.data.frame(sample)</pre> from cmdstanpy import CmdStanModel logger = logging.getLogger("cmdstanpy") logger.addHandler(logging.NullHandler()) # instantiate the model object model_comp = CmdStanModel(stan_file="rank_src_censored_picks.stan") # sample high probability parameter settings sample_Stan = model_comp.sample(data="rank_src_censored_picks.stan", show_progress=True, show_console=False, draws = sample_Stan.draws_pd(vars=['lp__', 'beta_0', 'beta']) 20

Why That Works

- We want to maximize plausibility of parameters given data: $P[\beta_0, \beta, \zeta \mid data]$.
- By Bayes' Law $P[\beta_0, \beta, \zeta \mid data] = P[\beta_0, \beta, \zeta]P[data \mid \beta_0, \beta, \zeta]/P[data].$
 - Can ignore P[data] as it is free of our parameter estimates.
 - So picking β, ζ such that $P[\beta_0, \beta, \zeta]P[data \,|\, \beta_0, \beta, \zeta]$ is large is the same as picking such that $P[\beta_0, \beta, \zeta \,|\, data]$ is large.
- Can invoke ideas such as the Bernstein-von Mises theorem to argue "large" is going to concentrate samples near the (unknown) true parameter value as we add more data.
 - (Technically better to argue that for a model with no data size dependent variables ζ .)
 - With enough data and flat enough ${\sf P}[\beta_0,\beta,\zeta]$, we can even omit the ${\sf P}[\beta_0,\beta,\zeta]$ term.
 - Structural mis-specification more risky than "wrong priors."

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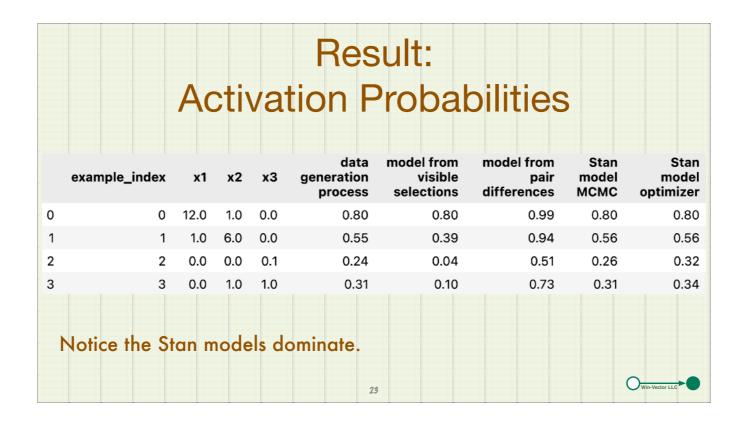
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draws |>
 head() |>
 knitr::kable()

lp	beta_0	beta[1]	beta[2]	beta[3]
-1251.130	-1.520818	0.2282623	0.2879370	0.3201965
-1250.358	-1.506511	0.2233696	0.2475490	0.1977965
-1251.936	-1.552996	0.1998336	0.2522806	0.3323120
-1249.657	-1.533951	0.2080136	0.2574112	0.3573067
-1248.750	-1.493253	0.2228508	0.2416577	0.3151417
-1248.531	-1.221375	0.2030706	0.2373745	0.0258106

nrow(draws)

[1] 4000



In this table we have 4 types of examples, one in each row. The numbers to the right of the 'x' columns are the probability the item is selected. So, good models should return numbers near the data generation process column. The models evaluated are listed in the next slide.

Models Compared

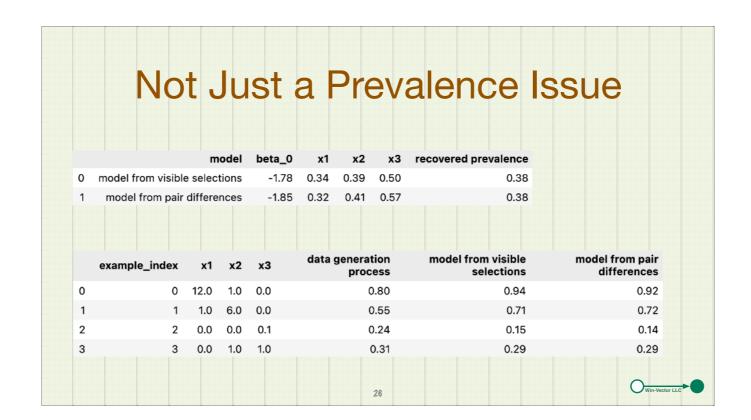
- Model from visible selections: treat each item selection or non-selection as a positive or negative example. Also called "item-wise" ranking. A nice logistic regression solution for comparison.
- Model from pair differences: encode each pair in a list where one wine is picked and one is not as an example. A common "let's be clever trick."
- Stan Model MCMC: encode an entire probability model (including guessing unseen quantities) and then use a Markov chain to sample high likelihood values. The big dog.
- Stan Model Optimizer: use the above encoding as a "loss", and hope something as simple as standard optimizer can find a high likelihood solution. "Cheap Stan" (could use other numeric platforms like PyTorch for this).

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Our Results: Model Coefficients

	model	beta_0	x1	x2	х3
0	data generation process	-1.20	0.20	0.20	0.20
1	model from visible selections	-3.13	0.34	0.39	0.50
2	model from pair differences	0.00	0.32	0.41	0.57
3	Stan model MCMC	-1.05	0.19	0.18	0.05
4	Stan model optimizer	-0.73	0.16	0.13	-0.06

	example_index	x1	x2	хЗ	data generation process	model from visible selections	model from pair differences	Stan model MCMC	Stan model optimizer
0	0	12.0	1.0	0.0	0.80	0.80	0.99	0.80	0.80
1	1	1.0	6.0	0.0	0.55	0.39	0.94	0.56	0.56
2	2	0.0	0.0	0.1	0.24	0.04	0.51	0.26	0.32
3	3	0.0	1.0	1.0	0.31	0.10	0.73	0.31	0.34
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This slide is what happens if we statistically adjust (or correct) the simple models to reproduce the correct prevalence. What happens is: not too much improvement, and the difference between the simple logistic model and difference model goes away.

Conclusions

- There are examples where easy inference of preference doesn't work.
- Stan was powerful to let us pick our assumed presentation censoring process.
 - The other systems impose a presentation behavior.
- Stan is great for prototyping solution methods and experimenting with how much model structure and presentation hygiene you wish to capture.
 - Can export inferred parameters and use them elsewhere.



Tools Used

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- · Stan, R, and Python
- All code and data shared here:

https://github.com/WinVector/Examples/tree/main/rank

rstan.md

rstan.Rmd

rank_src_censored_picks_reified_noise.stan

rank_src_censored_picks.stan

generate_example.ipynb

rank_data_censored_picks.json

LearningToRank.pdf



Our Using Stan to Solve Problems Training Offering

- The series currently includes:
 - Dealing with range censored data, or tobit style regression.
 - Learning rank preferences from observed actions.
 - Time series with external explanatory variables.
- Contact <u>imount@win-vector.com</u> for custom training and consulting.



Thank you

Slides, links, and code: https://github.com/WinVector/Examples/tree/main/rank Rehearsal video recording: https://www.youtube.com/watch?v=8x-RY8Ua4Go

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