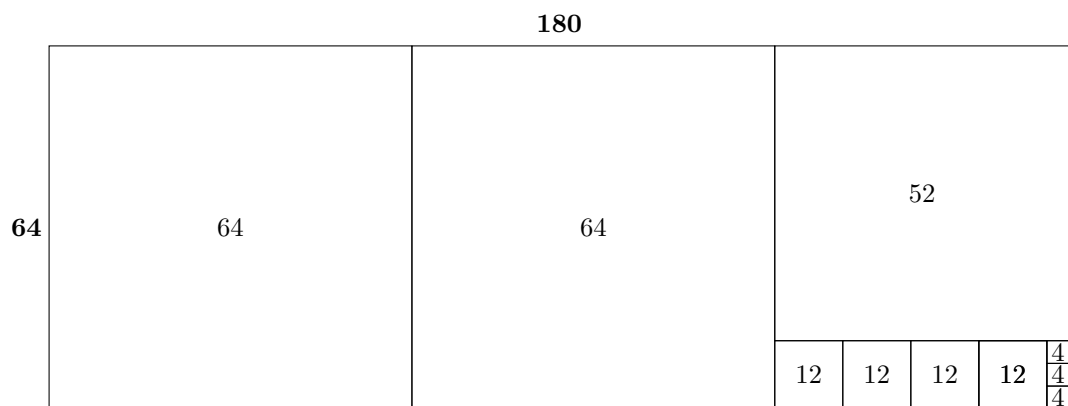


NOTES ON CONTINUED FRACTIONS

ERIC MARTIN

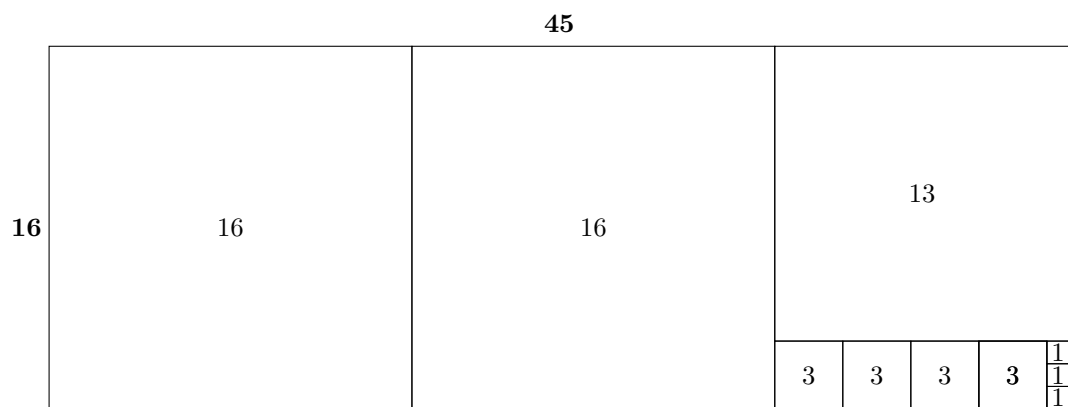
Applying Euclid's algorithm to determine that $\gcd(180, 64) = 4$:

$$\begin{array}{rclclcl}
 180 & = & 180 // 64 * 64 + 180 \% 64 & = & 2 * 64 + 52 \\
 64 & = & 64 // 52 * 52 + 64 \% 52 & = & 1 * 52 + 12 \\
 52 & = & 52 // 12 * 12 + 52 \% 12 & = & 4 * 12 + 4 \\
 12 & = & 12 // 4 * 4 + 12 \% 4 & = & 3 * 12 + 0
 \end{array}$$



Irreducible fractions have a gcd equal to 1:

$$\begin{array}{rclclcl}
 45 & = & 45 // 16 * 16 + 45 \% 16 & = & 2 * 16 + 13 \\
 16 & = & 16 // 13 * 13 + 16 \% 13 & = & 1 * 13 + 3 \\
 13 & = & 13 // 3 * 3 + 13 \% 3 & = & 4 * 3 + 1 \\
 3 & = & 3 // 1 * 3 + 3 \% 1 & = & 3 * 1 + 0
 \end{array}$$



$$\frac{45}{16} = 2 + \frac{1}{1 + \frac{1}{4 + \frac{1}{3}}}$$