- 1) Design a suitable data structure for storing Context Free Grammars. Use this data structure in the following problems.
- 2) Consider the following grammar:

G[S]:
$$S \rightarrow aSbS \mid bSaS \mid$$

Show that the grammar is ambiguous by constructing two different leftmost derivations for abab. Write a recursive descent parser with backtracking for this grammar.

3) Consider the following grammar for logical expressions:

G[E]:
$$E \rightarrow E$$
 or $T \mid T$
 $T \rightarrow T$ and $F \mid F$
 $F \rightarrow \text{not } F \mid (E) \mid \text{true } \mid \text{false}$

Here or, and, and not are logical operators; and true and false are logical constants. Make this grammar suitable for top-down parsing by removing left recursion from this grammar. Then write a recursive descent parser with backtracking for this grammar.

4) The grammar

G[S]:
$$S \rightarrow aSa \mid aa$$

generates all even length strings of a's except for the empty string. Construct a recursive descent parser with backtracking for the grammar that tries the alternate aSa before aa. Show parsing of various strings of a's and determine whether the parser succeeds on 2, 4, 6, and 8 a's.

5) Try constructing a recursive descent parser with exhaustive backtracking for the grammar of problem 5 and show parsing of above strings. Determine if it is able to accept string of 6 a's.