

# Andrea Loi: Curriculum Vitae et Studiorum.

## Personal Details

Date of birth: September 28, 1969

Place of birth: Cagliari, Italy.

address: Dipartimento di Matematica e Informatica  
Via Ospedale 72, 09124 Cagliari-Italy

email: loi@unica.it  
phone number: 39 070 6758526

## Current Position

Full Professor at University of Cagliari (Italy).

## Postgraduate studies

1998 Ph.D. in Mathematics at the University of Warwick, supervisor J. Rawnsley, dissertation titled *Quantization of Kähler manifolds and Holomorphic immersions in projective spaces*.

1994 Master in Mathematics at the University of Warwick, supervisor J. M. Micallef, dissertation titled *Deformation of complex structures : Complex Tori and K3 Surfaces*.

## Skills

- Proficient in written and spoken English; good in written and spoken French.

## Scientific travels

- Jussieu Paris (France) (22 February-24 February 2018)
- Luminy (France) (14 January–19 January 2018).
- University of Evora (Portugal) (1 September–06 September 2013).
- Visiting Professor, Institut Fourier de Mathématiques (Grenoble) (9 January - 9 February 2012).
- University of München (Germany) (18-21/12/2011).
- University of Bilbao (Spain) (06-10/10 2011).
- The thirteenth international conference on Geometry, Integrability and Quantization; Varna (Bulgaria), (with a cast grant) (03-08/06 2011).
- Workshop on Symplectic Geometry, Contact Geometry, and Interactions; Department of Mathematics, Uppsala University (with a CAST grant) (27-29/1 2011).
- University of Sofia (Bulgary) (6-8/9 2010).
- University of Veliko Tarnovo (Bulgary) (8-10/9 2010)].

- Mathematics Institute, Princeton University (invitation by G. Tian);  
Courant Institute, Department of Mathematics New York (invitation by M. Gromov) (01/04-30/04 2008)
- University of Sofia (15/7-15/9 2003).
- I.H.E.S. (invitation by J. P. Bourguignon) (one month: October 1995)
- University of Warwick, England (1993-98)
- Mathematics Institute Louis Pasteur, Strasbourg (one year: 1990-91).

**Invited speakers to the following conferences (last 15 years)**

- 2024 *Dual Kähler metrics*, Differential Geometry Workshop in Lerici, April 8-10, 2024, Lerici, Italy.
- 2023 *Rigidity properties of holomorphic isometries into homogeneous Kähler manifolds*, The 7th workshop "Complex Geometry and Lie Groups" May 22- 26, 2023, Lecce, Italy.
- 2020 *Kähler immersions into complex space forms: old and new results*, A Geometry Day in Como (on January 10th),
- 2018 *Symplectic coordinates on Kähler manifolds*, Sèminarie de Gèometrie Hamiltonienne, Jussieu Paris (France)
- 2018 *Kähler immersions of homogeneous Kähler manifolds into complex space forms*, CIRM Luminy (France), 14 January 2018.
- 2013 *The Gromov width of symmetric spaces*, XXII International fall workshop on Geometry and Physics, 2-5 September 2013, Evora (Portugal).
- 2012 *Kähler immersions of homogeneous Kähler manifolds into complex space forms*, Institut Fourier de Mathématiques (Grenoble), 24 Gennaio 2012.
- 2011 *Balanced metrics, TYZ expansion and Szegő kernel*, conference at the Mathematics Institute of the University of München, München (Germany) 20 Dicembre 2011.
- 2011 *Global Symplectic coordinates on Kähler manifolds*, EMS-RSME JOINT MATHEMATICAL WEEKEND, Bilbao, October 7-9, 2011.
- 2011 *Balanced metrics, Tian–Yau–Zelditch expansion and quantization of a Kähler manifold*, The thirteenth international international conference on Geometry, Integrability and Quantization, Varna (Bulgaria) 3-8 June 2011.
- 2011 *Metriche bilanciate, espansione di Tian–Yau–Zelditch e quantizzazione di una varietà di Kähler*, Geometry in Bicocca (Milan) 2011, 12-13 May 2011.
- 2010 *Kähler immersions of homogeneous Kähler manifolds into complex space forms* Global Analysis and PDE on Manifolds, IMI, BAS, SOFIA, 6-8 September 2010.

- 2010 *Kähler immersions of homogeneous Kähler manifolds into complex space forms*  
ICDG (International Congress in Differential Geometry 2010, Veliko Tarnovo 8-10 September 2010).
- 2008 *Holomorphic immersions of Kähler-Einstein manifolds into complex space forms*  
(School and Conference on Differential Geometry, ICTP, Trieste, 2 June - 20 June 2008)
- 2008 *Symplectic duality between complex domains* (Extremal Kaehler metrics and Kaehler-Ricci flow, Centro De Giorgi, Pisa, 2 March - 29 March 2008).

### Research interests

1. Induction of geometric structures (Kähler form, symplectic forms, Riemannian metrics, connections, Kähler-Ricci solitons);
2. analytic and geometric methods for the quantization (geometric and by deformation) of a Kähler manifold;
3. balanced metrics and the TYZ (Tian–Yau–Zelditch) expansion.

### Organization of events

1. *Odysseus 2018*, Cagliari, 3-8 June 2018.
2. *Indam-Day*, Cagliari, 1 June 2018.
3. *Two days of Geometry in honor of Giusi D'Ambra*, Cagliari, 16-17 February 2018.
4. *Complex and Riemannian Geometry days*, Cagliari, 8-9 September 2016.
5. *New Trends in Differential Geometry*, Villasimius, 18-20 September 2014.

## Research publications

### Complex, Kähler, Symplectic Geometry and Topology

1. (joint with Giovanni Placini) *Any Sasakian structure is approximated by embeddings into spheres*, to appear in FORUM.
2. (joint with Giovanni Placini e Michela Zedda) *Immersiones into Sasakian Space Forms* to appear in MZ.
3. (joint with Stefano Bonzio) *Embeddings of metric Boolean Algebras in  $\mathbb{R}^N$* , to appear in Topology and its Applications.
4. (joint with Claudio and Chao) *Gromov-Hausdorff limits and holomorphic isometries* to appear in MRL.
5. (joint with Robi) *Rigidity of holomorphic isometries into homogeneous Kähler manifolds* to appear in Proc. Amer. Math. Soc.
6. (joint with F. Zuddas) *Some characterizations of the complex projective space via Ehrhart polynomials*, to appear in International Journal of Mathematics.
7. (joint F. Zuddas e Filippo) *On canonical radial Kähler metrics*, Osaka J. Math. 60 (2023), no. 3, 545-554.
8. (joint with Roberto Mossa) *On holomorphic isometries into blow-ups of  $\mathbb{C}^\times$* , Mediterr. J. Math. 20 (2023), no. 4, 230.
9. (joint with Stefano Matta) *Robustness of induced statistical structures*, Topology Appl. 327 (2023), Paper No. 108438, 8 pp.
10. (joint with Roberto Mossa) *Holomorphic isometries into bounded homogeneous domains*, Proc. Amer. Math. Soc. 151 (2023), no. 9, 3975-3984.
11. (joint F. Zuddas e Filippo) *Kähler-Ricci solitons induced by infinite dimensional complex space forms*, Pacific Journal of Mathematics 316 (2022), 183-205.
12. (joint with R. Mossa) *KRS into definite or indefinite complex space forms* Proc. Amer. Math. Soc. 149 (2021), no. 11, 4931-4941.
13. (joint F. Salis e F. Zuddas) *Extremal Kähler metrics induced by finite or infinite dimensional complex space forms*, J. Geom. Anal. 31 (2021), no. 8, 7842-7865.
14. (joint with M. Zedda and F. Zuddas) *Ricci flat Calabi's metric is not projectively induced* Tohoku Math. J. 73 (2021), 29-37.
15. (joint with F. Zuddas) *Partially regular and cscK metrics*, Internat. J. Math. 31 (2020), no. 10, 2050079, 8 pp.
16. (joint with F. Salis and F. Zuddas) *Characterization of complex space forms through Laplacians*, Abh. Math. Semin. Univ. Hambg. 90 (2020), no. 1, 99-109.

17. (joint with B. Cappelletti Montano and G. Bande)  *$\eta$ -Einstein Sasakian immersions in non-compact Sasakian space forms*, Ann. Mat. Pura Appl. (4) 199 (2020), no. 6, 2117-2124.
18. (joint with R. Mossa and F. Zuddas) *Finite TYCZ expansions and cscK metrics* J. Math. Anal. Appl. 484 (2020).
19. (joint with B. Cappelletti Montano) *Einstein and  $\eta$ -Einstein Sasakian submanifolds in spheres* Ann. Mat. Pura Appl. (4) 198 (2019), no. 6, 2195-2205.
20. (joint F. Cannas Aghedu) *The Simanca metric admits a regular quantization* Ann. Global Anal. Geom. 56 (2019), no. 3, 583-596.
21. (joint with R. Mossa and F. Zuddas) *Bochner coordinates on flag manifolds*, Bull. Braz. Math. Soc, New Series, 50 497-514 (2019).
22. (joint with F. Salis and F. Zuddas) *On the third coefficient of TYZ expansion for radial scalar flat metrics*, Journal of Geometry and Physics 133, 210-218 (2018).
23. (joint with F. Salis and F. Zuddas) *Two conjectures on Ricci flat metrics*, Math. Z. (2018) 290, 599–613.
24. (joint with B. Cappelletti Montano and D. Zuddas) *On codimension one submanifolds of the real and complex projective space*, Topology Appl. 232 (2017), 237-241.
25. (joint with F. Zuddas) *Explicit symplectic coordinates on Kähler manifolds*, Special metrics and group actions in geometry, 215-239, Springer INdAM Ser., 23, Springer, Cham, 2017
26. (joint with R. Mossa and F. Zuddas) *The log-term of the disc bundle over a homogeneous Hodge manifold*, Ann. Global Anal. Geom. 51 (2017), no. 1, 35-51.
27. (joint with M. Zedda) *The diastasis function of the Cigar metric*, Journal of Geometry and Physics 110, 269-276 (2016).
28. (joint with F. Zuddas) *On the Gromov width of Homogeneous Kähler manifolds*, Diff. Geom. Appl. 47, 130-132 (2016).
29. (joint with C. Arezzo and F. Zuddas) *Some remarks on the symplectic and Kähler geometry of toric varieties*, Annali di Matematica Pura e Applicata 4, 1287-1304 (2016).
30. (joint with R. Mossa and F. Zuddas) *Symplectic capacities of Hermitian symmetric spaces of compact and non compact type*, Journal of Symplectic Geometry Volume 13, Number 4, 1049-1073 (2015).
31. (joint with R. Mossa) *Some remarks on Homogeneous Kähler manifolds*, Geometriae Dedicata Volume 179 (2015), 1-7.
32. (joint with M. Zedda) *On the coefficients of TYZ expansion of locally Hermitian symmetric spaces*, Manuscripta Mathematica (2015), Vol. 148, 303-315.

33. (joint with D. Uccheddu and M. Zedda) *On the Szegő kernel of Cartan–Hartogs domains*, Arxiv for Matematik, Vol. 54 Issue 2 (2015), 473-484.
34. (joint with L. Cadeddu and S. Gallot) *Maximizing mean exit-time of the Brownian motion on Riemannian manifolds*, Monatsh. Math. Vol. 176, Issue 4 (2015), 551-570.
35. (joint with R. Mossa and F. Zuddas) *Some remarks on the Gromov width of homogeneous Hodge manifolds*, Int. J. Geom. Methods Mod. Phys. Vol. 11, No. 2 (2014).
36. (joint with C. Arezzo and F. Zuddas) *Szego Kernel, regular quantizations and spherical CR-structures*, Math. Z. (2013) 275, 1207-1216.
37. (joint with M. Zedda) *Global symplectic coordinates on gradient Kähler–Ricci solitons*, Monatsh. Math. (2013) 171:415-423.
38. (joint with C. Arezzo and F. Zuddas) *On homothetic balanced metrics*, Ann. Global Anal. Geom. 41, n. 4 (2012), 473-491.
39. (joint with M. Zedda and F. Zuddas) *Some remarks on the Kähler geometry of the Taub–NUT metrics*, Ann. Global Anal. Geom. 41, n. 4 (2012), 515-533.
40. (joint with A. J. Di Scala and H. Hishi) *Kähler immersions of homogeneous Kähler manifolds into complex space forms*, Asian Journal of Mathematics Vol. 16 No. 3 (2012), 479-488.
41. (joint with R. Mossa) *Berezin quantization of homogeneous bounded domains*, Geom. Dedicata 161 (2012) 119-128.
42. (joint with M. Zedda) *Calabi’s inhomogeneous Einstein manifold is globally symplectomorphic to  $\mathbb{R}^{2n}$* , Diff. Geom. Appl. (30) 2 (2012), 145-147.
43. (joint with M. Zedda) *Balanced metrics on Cartan and Cartan-Hartogs domains* Math. Z. 270 (2012), no. 3-4, 1077-1087.
44. (joint with M. Zedda), *Kähler-Einstein submanifolds of the infinite dimensional projective space*, Math. Ann. 350 (2011), 145-154.
45. (joint with Roberto Mossa), *The diastatic exponential of a symmetric space*, Math. Z. 268 (2011), no. 3-4, 1057-1068.
46. (joint with G. D’Ambra and R. Deleo) *Partially isometric immersions and free maps* Geom. Dedicata 151 (2011), 79-95.
47. (joint with R. Mossa) *Uniqueness of balanced metrics on complex vector bundles*, J. Geom. Phys. 61 (2011) , 312-316.
48. (joint with M. Zedda) *Balanced metrics on Hartogs domains* Abh. Math. Semin. Univ. Hambg. 81 (2011), no. 1, 69-77.
49. (joint with T. Gramchev) *TYZ expansion for some rotation invariant Kähler metrics*, Proceedings of the 2nd International Colloquium on Differential Geometry and Its Related Fields, World Sci., (2011), 91-108.

50. (joint with M. Zedda), *A note on the  $l^2$ -norm of the second fundamental form of algebraic manifolds*, Serdica Math. J. 36 (2010), 67-74.
51. (joint with A. J. Di Scala), *Kähler manifolds and their relatives*, Ann. Scuola Norm. Sup. Pisa Cl. Sci. (5) Vol. IX (2010), 495-501.
52. (joint with A. J. Di Scala and F. Zuddas), *Symplectic duality between complex domains* Monatsh. Math. 160 (2010) 403-428.
53. (joint with F. Zuddas), *Canonical metrics on Hartogs domains*, Osaka J. Math. Vol. 47, No.2 (2010), 507-521.
54. (joint with A. Greco), *Radial balanced metrics on the unit disk*, J. Geom. Phys. 60 (2010), 53-59.
55. (joint with F. Zuddas), *Engliš expansion for Hartogs domains*, Int. J. Geom. Methods Mod. Phys. Vol. 6, No. 2 (2009), 233-240.
56. (joint with A. J. Di Scala and F. Zuddas), *Riemannian geometry of Hartogs domains*, International Journal of Mathematics Vol. 20, Number 2 (2009), 139-149.
57. (joint with T. Gramchev), *TYZ expansion for the Kepler manifold*, Comm. Math. Phys. 289, (2009), 825-840.
58. (joint with M. Zedda), *Cartan domains and indefinite Euclidean spaces*, Extracta Math. 23 no. 3 (2008), 255-263.
59. (joint with A. J. Di Scala and Guy Roos), *The bisymplectomorphism group of a bounded symmetric domain*, Transformation Groups Vol. 13, Number 2 (2008), 283-304.
60. (joint with A. J. Di Scala) *Symplectic duality of symmetric spaces*, Adv. Math. 217 (2008), 2336-2352.
61. (joint with F. Zuddas), *Symplectic maps of complex domains into complex space forms*, J. Geom. Phys. 58 (2008), 888-899.
62. (joint with C. Arezzo and A. Ghigi) *Stable bundles and the first eigenvalue of the Laplacian*, J. Geom. Anal. Vol. 17, N. 3 (2007), 401-412.
63. (joint with F. Cuccu) *Balanced metrics on  $\mathbb{C}^n$* , J. Geom. Phys. 57 (2007), 1115-1123.
64. (joint with G. D'Ambra) *Non-free isometric immersions of Riemannian manifolds*, Geom. Dedicata 127 (2007), 151-158.
65. (joint with A.J. Di Scala) *Kähler maps of Hermitian symmetric spaces into complex space forms*, Geom. Dedicata 25 (2007), 103-113.
66. *Regular quantizations and covering maps*, Geom. Dedicata 123 (2006), 73-78.
67. *Calabi's diastasis function for Hermitian symmetric spaces*, Differential Geom. Appl. 24 (2006), 311-319.

68. (joint with F. Cuccu) *Global symplectic coordinates on complex domains*, J. Geom. Phys. 56 (2006), 247-259.
69. *A Laplace integral on a Kähler manifold and Calabi's diastasis function*, Differential Geom. Appl. 23 (2005), 55-66.
70. *Bergman and balanced metrics on complex manifolds*, Int. J. Geom. Methods Mod. Phys. 2 (2005), 553-561.
71. *A Laplace integral, the T-Y-Z expansion and Berezin's transform on a Kaehler manifold* Int. J. Geom. Methods Mod. Phys. 2 (2005), 359-371.
72. *Regular quantizations of Kähler manifolds and constant scalar curvature metrics*, J. Geom. Phys. 53 (2005), 354-364.
73. (joint with C. Arezzo) *A note on Kähler-Einstein metrics and Bochner's coordinates*, Abh. Math. Sem. Univ. Hamburg 74 (2004), 49-55.
74. (joint with C. Arezzo) *Moment maps, scalar curvature and quantization of Kähler manifolds*, Comm. Math. Phys. 243 (2004), 543-559.
75. *The Tian-Yau-Zelditch asymptotic expansion for real analytic Kähler metrics*, Int. J. Geom. Methods Mod. Phys. v. 1 No 3 (2004), 253-263.
76. (joint with G. D'Ambra) *Inducing connections on  $SU(2)$ -bundles*, JP J. Geom. Topol. 3 (1) (2003), 65-88.
77. (joint with C. Arezzo) *Quantization of Kähler manifolds and the asymptotic expansion of Tian-Yau-Zelditch*, J. Geom. Phys. 867 (2003), 1-13.
78. (joint with G. D'Ambra) *A symplectic version of Nash  $C^1$ -isometric embedding theorem*, Differential Geom. Appl. 16, no. 2 (2002), 167-179.
79. *Holomorphic maps of Hartogs domains in Complex Space forms*, Riv. Mat. Univ. Parma (7), vol. 1 (2002), 103-113.
80. (joint with R. Piergallini) *Compact Stein surfaces with boundary as branched covers of  $B^4$* , Invent. Math. 143 (2001), 325-348.
81. (joint with D. Zuddas) *Some remarks on Bergmann metrics*, Riv. Mat. Univ. Parma 6, no. 4 (2001), 71-86.
82. *The function epsilon for complex Tori and Riemann surfaces*, Bull. Belg. Math. Soc. Simon Stevin 7, no. 2 (2000), 229-236.
83. (joint with P. Sitzia) *Explicit formulas for geodesics of homogeneous  $SO(2)$ -isotropic three dimensional manifolds*, Adv. Math. 156 (2000), 1-22.
84. *Quantization of bounded domains*, J. Geom. Phys. 29 (1999), 1-4.

### Mathematical Economics

85. (joint with Stefano Matta) *Endowments, patience types, and uniqueness in two-good HARA utility economies* to appear to Economic Theory Bulletin.



86. (joint with Daria Uccheddu e Stefano Matta) *Equilibrium selections: A geometric approach*. to appear in J. Math. Econom.
87. (joint with Stefano Matta) *Risk aversion and uniqueness of equilibrium in economies with two goods and arbitrary endowments*, B. E. J. Theor. Econ. 23 (2023), no. 2, 679-696.
88. (joint with Stefano Matta) *Minimal entropy and uniqueness of price equilibria in a pure exchange economy*, J. Math. Econom. 97 (2021), Paper No. 102555, 6 pp.
89. (joint with S. Matta) *Curvature and uniqueness of equilibrium*, J. Math. Econom. 74 (2018), 62-67.
90. (joint with S. Matta) *On the topology of the set of critical equilibria*. Int. J. Econ. Theory 12 (2016), no. 2, 107-126.
91. (joint with S. Matta) *Increasing complexity in structurally stable models*, J. Math. Econom. 57 (2015), 20-24.
92. (joint with S. Matta) *Structural stability and catastrophes*, Economics Bulletin (2012) Vol. 32 No. 4, 3378-3385
93. (joint with S. Matta) *Measures of economies with an arbitrarily large number of equilibria*, Int. J. Econ. Theory (2012) Vol.8, No.4, 337-343.
94. (joint with S. Matta) *Catastrophes minimization on the equilibrium manifold*, J. Math. Econom. 47 (2011), 617-620.
95. (joint with S. Matta) *A note on the structural stability of the equilibrium manifold* J. Math. Econom. 46 (2010) n.4, 591-594.
96. (joint with S. Matta), *Evolution paths on the Equilibrium Manifold*, J. Math. Econom. 45 (2009), 846-851.
97. (joint with S. Matta), *Geodesics on the equilibrium manifold*, J. Math. Econom. 44 (2008), no. 12, 1379-1384.
98. (joint with S. Matta) *A Riemannian metric on the Equilibrium Manifold: the smooth case*, Economics bulletin 30 (2006), 1-9.

### Mathematical Logic

99. (joint with Stefano Bonzio) *Probability over Plonka sums of Boolean algebras: states, metrics and topology*, Internat. J. Approx. Reason. 136 (2021), 14-35.
100. (joint with S. Bonzio) *The Plonka product of topological spaces*, Algebra Universalis 80 (2019), no. 3, 1-29.
101. (joint with S. Bonzio e L. Peruzzi) *A duality for involutive bisemilattices*, Studia Logica (2019) 107, 423-444.

### Games and Puzzle

102. (joint with S. Bonzio and L. Peruzzi) *On the  $n \times n \times n$  Rubik's Cube*, Math. Slovaca. 68 (2018), No. 5, 957-974.

103. (joint with S. Bonzio and L. Peruzzi) *On the first law of cubology for the Rubik's Revenge*. Math. Slovaca 67 (2017), No. 3, 561-572.

#### **Networks**

104. (joint F. Lilliu, D. Reforgiato Recupero, M. Sissini) *An uncertainty-aware optimization approach for flexible loads of smart grid prosumers: A use case on the Cardiff energy grid* Sustainable Energy, Grids and Networks, 20 (2019) 100272.

#### **Books**

1. *Introduzione alla Topologia Generale*, Aracne Editrice (2013).
2. (joint with M. Zedda) *Kähler immersions of Kähler manifolds into complex space forms*, Lectures Notes of the Unione Matematica Italiana, Springer (2018).