

# Sort

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# Popular sorting algorithm

- **Insertion sort**
- Selection sort
- Bubble sort
- **Merge sort**
- Quicksort

# Insertion sort

Using arrays

1	5	3	6	4
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# Insertion sort

Using arrays

1	3	5	6	4
---	---	---	---	---

# Insertion sort

Using arrays

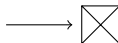
1	3	4	5	6
---	---	---	---	---

# Insertion sort

Using arrays

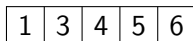
1	3	4	5	6
---	---	---	---	---

Using linked lists

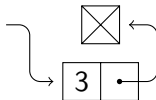


# Insertion sort

## Using arrays

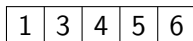


## Using linked lists

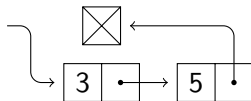


# Insertion sort

## Using arrays



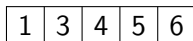
## Using linked lists



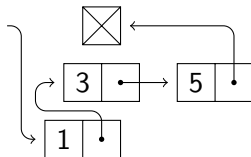


# Insertion sort

## Using arrays

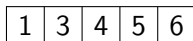


## Using linked lists

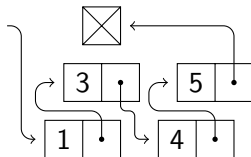


# Insertion sort

## Using arrays



## Using linked lists



# Merge sort

Merging two sorted arrays

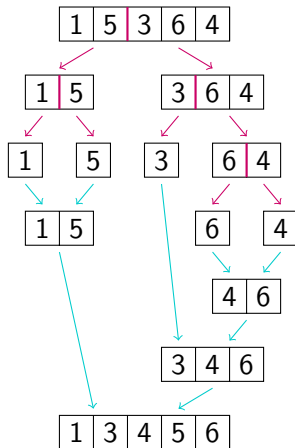
1	3	5
---	---	---

2	7	9
---	---	---

1	2	3	5	7	9
---	---	---	---	---	---

# Merge sort

## Dichotomic sort



## Exercise 1: Candy Distribution

### Statement

Given  $N$  integers indicating the number of students in each of Alice's classes, and  $N$  integers corresponding to the price of a type of candy. Knowing that all students in the same class will receive the same kind of candy, compute the least amount of money Alice must spend to give a candy to each of her students.

### Example

Input:

```
5
10 80 37 22 109
6 8 8 20 15
```

Output:

```
2120
```

## Exercise 1: Candy Distribution

### Statement

Given  $N$  integers indicating the number of students in each of Alice's classes, and  $N$  integers corresponding to the price of a type of candy. Knowing that all students in the same class will receive the same kind of candy, compute the least amount of money Alice must spend to give a candy to each of her students.

### What problems can arise?

- What do we know of  $N$ ?
- Of the number of students?
- Of the price of the candies?
- How great can the solution be?  
     $\implies$  Are integers big enough for the solution?

## Exercise 1: Candy Distribution

### Solution 1: Homemade

Using two lists or arrays with insertion sort

### Solution 2: Integrated

Using two arrays and the sort procedure in your preferred language

## Exercise 1: Candy Distribution

More test cases

Input:

4

1 10 2 1

1 2 4 2

5

10 80 37 22 89

6 8 8 20 15

0

Output:

20

2000



## Exercise 2: Inversion Count

### Statement

Given an array  $A$  of integers. If  $i < j$  and  $A[i] > A[j]$  then the pair  $(i, j)$  is called an inversion of  $A$ . Count the number of inversions of  $A$

### Example

Input:

2 3 8 6 1

Output:

5

## Exercise 2: Inversion Count

### Statement

Given an array  $A$  of integers. If  $i < j$  and  $A[i] > A[j]$  then the pair  $(i, j)$  is called an inversion of  $A$ . Count the number of inversions of  $A$

### What problems can arise?

- How great can the array be?
- How great can the values in the array be?
- How great can the solution be?  
     $\implies$  Are integers big enough for the solution?

## Exercise 2: Inversion Count

### Solution 1: Brut Force

```
read  $n$  on standard input
read the array  $A$  on standard input

result  $\leftarrow 0$ 

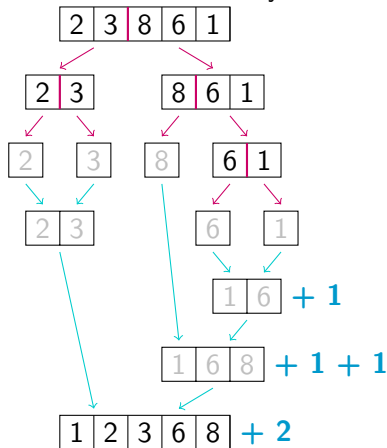
for  $i$  from 0 to  $n-2$ 
  for  $j$  from  $i+1$  to  $n-1$ 
    if  $A[i] > A[j]$  then
      result  $\leftarrow$  result + 1

print result
```

## Exercise 2: Inversion Count

### Solution 2: Using Merge sort

Key idea: if there are no inversions, then during the merge, all the elements of the left array should be added before any element of the right array



## Exercise 2: Inversion Count

More test cases

Input:

3

6

1 2 3 4 5 6

8

5 1 4 2 6 2 6 2

1

1

Output:

0

11

0

## Exercise 3: It's a Murder

### Statement

Given an array of integers, for each number sum the previous strictly smaller number

### Example

Input:                      Output:

1                              15

5

1 5 3 6 4

### Solution: Elegant

Using Merge sort

## Exercise 4: Yodaness Level

### Statement

Given a statement as Yoda says it and the same statement as it should be said normally count the number of pairs of words that changed their order

### Example

Input:

1

6

much to learn you still have

you still have much to learn

Output:

9

### Solution: Elegant

Using Merge sort