

# Graph

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# ANARC08G - Think I will Buy Me a Football Team

## Graph Definition

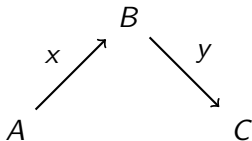
- Each bank is represented as a node.
- Each debt is represented as an arc between two nodes labeled with the debt amount.

## Questions

- How can you compute the total amount of money needed to settle all debts between the banks?
- How can you reduce this total amount?

# ANARC08G - Transitivity Reduction Rule

## Transitivity Reduction Rule



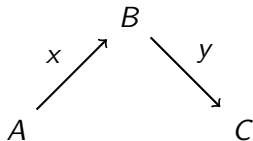
## Question

The current flow is  $x + y$ .

**How can you reduce the flow?**

# ANARC08G - Transitivity Reduction Rule

## Transitivity Reduction Rule



### Question

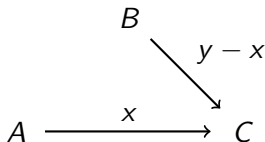
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**How can you reduce the flow?**

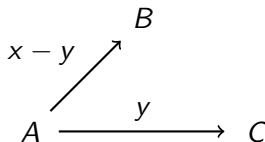
### Answer

The flow is reduced to  $\max(x, y)$ .

$$y \geq x$$



$$y \leq x$$



# ANARC08G - Fixpoint algorithm

## Fixpoint Algorithm

Apply repeatedly the transitivity reduction rule on the graph until it is not possible.

## Questions

- What is the complexity of the fixpoint algorithm?
- Which properties are satisfied by the graph when the fixpoint has been reached?
- Is the resulting graph unique?
- Can you propose better algorithm that solves the problem? What is its complexity?