Practical Empirical Research for Beginners and Professionals Using Gretl

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Abstract

This paper examines

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1 Introduction

Data analysis is a vital part of the economic training and of an economist's daily life. Economists are trained to be sophisticated users of data, and econometrics — the interchange of economic theory, statistics and mathematics — is a subject which usually all economics students have to attend. A typical economics degree program comprises subjects on data management, statistics, model simulation and estimation.

Typically, undergraduates studying economics are typically exposed to at least once course in econometrics, covering the practice and interpretation of least-squares regression, data management and data visualisation. Graduate students learn the advanced treatments of the subject, likely involving Maximum Likelihood estimation, simulation and so on. Professional economists — whether in public or private institutions — are likely to find themselves using, or possibly developing, econometric methods.

Gretl is a open-source and freely available statistics and econometrics software attempting to bridge the different demands for teaching and professional work. It comprises a full-featured graphical interface but also a powerful scripting language. Gretl can be seen as a domain-specific language for statistics and econometrics. It handles datasets — a matrix but with a richer structure including information on the data type, eventual calendar date and recorded data frequency — similar to Eviews but can also deal with 'pure' matrices such as Matlab, Gauss and Julia for advanced programming purposes.

In the following, we will introduce Gretl — and to some extend also Hansl — alongside a practical empirical example using time-series data. Nevertheless, it should be said that Gretl can also handle cross-sectional as well as panel data structures.

The paper is structured as follows. The next section introduces the forecasting model, estimation techniques and forecast evaluation statistics as well as tests. Section 3 discusses the model specifications and presents the time-series used. Section 4 presents the empirical results as well as some robustness exercises. Section 5 concludes.

2 Econometric Software and Gretl

2.1 The 'Market' of econometrics software

The requirements for an econometric software are a delicate issue. For teaching purpose it makes sense to have undergraduate students work with reasonably user-friendly software — in the easiest case steering the software by a graphical user interface through point-and-click using the mouse. However, it makes little sense to introduce a software to undergraduates which does not support more advanced methods and does not offer a fully-fledged scripting and programming environment — aspects which are required for an advanced treatment in graduate classes and professionals. And of course there's a premium on teaching "marketable skills" rather than dead-end expertise.

Gretl is a program which attempts to bridge these different demands. It comprises a full-featured graphical interface (the GUI): its underlying functionality (coded in C) can be driven either by hansl (Gretl's scripting language) scripting or by the apparatus of menus, dialog boxes and so on. The developers try to ensure that almost everything that can be done via hansl can also be done via the GUI, and vice versa, with only few exceptions.

Gretl's main competitors are the major proprietary econometrics packages, Stata and Eviews, and also the major open-source statistical software project, R. As in gretl datasets and series are also basic in Stata and Eviews, and econometric functionality is supported by a wide range of built-in commands. Even though both Stata and Eviews support support scripting, their respective languages are quite odd from the point of view of a programmer used to general-purpose scripting languages or Matlab-like interfaces for matrix manipulation. One cannot define a function as such in either Stata or Eviews. Gretl, however, also offers the common apparatus of fully-fledged programming languages (function-calling, function-definition, declaration of and assignment to named variables of various types) similar of what is known from Matlab. Gretl scripting language hansl will look quite familiar to anyone who has worked with Matlab or Gauss.

Another major plus of Gretl is its built-in capability to communicate with other software packages such as Stata, Python, R, Julia, Ox and Octave. The *foreign*-block is an interface

to include statements of other languages into a hansl script allowing to send and receive information (in the form of matrices) to each other. Thus, users can use functions which are, for instance, currently not available in Gretl. For details see the Appendix A.8.

2.2 Gretl and Hansl

Gretl is acronym for Gnu Regression, Econometrics and Time-series Library. The software is available for Windows, Mac OS X as well as Linux through the official Gretl homepage: http://gretl.sourceforge.net/. It is free, open-source software which may be redistributed and/or modify it under the terms of the GNU General Public License as published by the Free Software Foundation.

Gretl comprises a large shared library, a common command line (CLI) program and a GUI client, and makes use of reliable free software packages, e.g. (multi-threaded) LA-PACK/BLAS, fftw, GTK, gnuplot, etc. The first Gretl version was released in January 2000 and has been under active development, mainly using the C programming language, since then. Its user interface is available in 17 languages thanks to an active community. Gretl is shipped with a User Guide of already 380+ pages, a Command Reference of 210+ pages, and a "A Hansl Primer" tutorial to Gretl's scripting language named "hansl" among additional useful documents.

Gretl comprises a full featured graphical user interface for steering tasks through clicking. However, apart from the GUI, functions can also be driven either by scripting. As the unique selling point, Gretl offers a high-level matrix oriented language similar to Matlab or Gauss, and an intuitive high-level scripting language that is attuned to econometrics. This makes Gretl especially interesting for both lecturing statistics or econometrics but also serious academic research.

Hansl—"Hansl's A Neat Scripting Language"— was developed over time and has become a very advanced high-level scripting language with more than 140 commands to date. Gretl's main developers have pushed the development of Gretl mainly through Hansl in recent times. Hansly is a language specifically tailored to the domain of econometrics. Users and developers are asked to program and publish user-contributed function packages

by means of Hansl rather than the low-level language C. A great plus of Hansl-based function packages is that it comes with a handy optional GUI integration making it possible that developers add access to specific functions through the GUI rather than solely the CLI. Most important: Hansl is a very clean and intuitive scripting language with a very nice syntax as you will see below. For more technical details on Hansl, we refer to Cottrell (2017).

To date Gretl *natively* implements a variety of models, methods and functions among others such as:

- 1. Time series data: ARIMA, GARCH-type, (S) VARs and VECMs, unit root and cointegration tests, Kalman filter, Mixed time-series frequencies (MIDAS), etc.
- 2. Limited dependent variables: Logit, Probit, Tobit, Interval regression, Models for count and duration data, etc.
- 3. Panel-data: Instrumental variables, Probit and GMM-based dynamic panel models, etc.
- 4. Output models as LaTeX files, in tabular or equation format.
- 5. Using gnuplet for compiling high-quality graphs.
- 6. Support for machine learning via the LIBSVM library.

Besides gretl's core functionality, several addons (http://gretl.sourceforge.net/addons.html) and numerous contributed function packages (http://ricardo.ecn.wfu.edu/gretl/cgi-bin/gretldata.cgi?opt=SHOW_FUNCS) are hosted on the package server and are easily accessible.

3 Getting Started in Gretl

There are several ways to work in Gretl. For starters, the most intuitive way is to use the program is through its built-in graphical user interface (GUI). The GUI is shown in Figure 1 and consists of four windows. At the top of the main window (see Figure 1(a)) you find the menu bar. Here you find commands to import and manipulate data, analyze data, and

manage output. Below the menu bar, the user finds information on the loaded file and the currently set working directory. Most space is given to the variables list where each variable is associated with an ID number, the variable's name and an eventual descriptive label. Below the variables list, information on the loaded dataset is given such as the total number of observations or of the selected sub-sample, respectively. The toolbar containing a number of useful utilities can be found at the bottom of the window.

The console window, as depicted in Figure 1(b) accepts Gretl commands which can be directly executed pressing "Enter". The output will immediately appear in the console. From the command prompt, '?' you can type in commands from the gretl language and calculate something. For instance,

? eval sqrt(25)/5

The eval command evaluates expression and prints its value. The icon view window comprises small icons for so eventually generated scalar values, matrices and model objects among others. Lastly, the script editor collects several lines of programming code into a file which can be executed all at once in a script. Serious and reproducible research usually uses such scripts for recording each step of the data analysis.

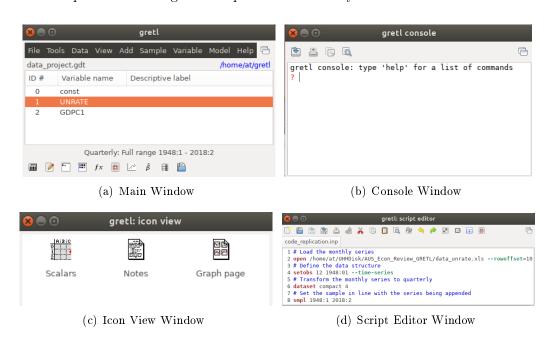


Figure 1: The Gretl Interface

Lee Adkin's (2014) terrific and freely available econometrics Ebook using Gretl for the applications provides a much deeper introduction to Gretl, and is highly recommended for learning and mastering Gretl (4th edition downloadable here: http://www.learneconometrics.com/gretl/using_gretl_for_P0E4.pdf but the 5th edition will be published very soon!).

3.1 Loading and Appending Data

Gretl can import data from a variety of formats. In the GUI program this can be done via the "File, Open Data, User file" menu. In script mode, simply use the open command. The supported import formats include (i) plain text files (typically comma-separated or "CSV"), (ii) spreadsheet formats as MS Excel, Gnumeric and Open Document (ODS), (iii) Stata data files (.dta), (iv) SPSS data files (.sav), (v) Eviews workfiles (.wf1) among some others.

The following conditions must be satisfied to make sure Gretl reads data successfully:

- 1. The first row must contain valid variable names, otherwise the program will automatically add names, v1, v2 and so on.
- 2. Data values should constitute a rectangular block, with one variable per column (and one observation per row).
- 3. Numeric data are expected, but in the case of importing from plain text, the program offers handling of character (string) data.
- 4. Optionally, the first column may contain strings such as dates, or labels for cross-sectional observations

One can append additional data either by the append command or via the "File, Append data" menu items: gretl will check the new data for conformability with the existing dataset and, if everything seems OK, will merge the data. For more complex tasks, there exists the powerful join command.

Once data is read-in by Gretl, it may be necessary to supply some information on the type of the dataset. The three types that can be distinguished are cross section, time series

and panel data. The primary tool for doing this is the "Data, Dataset structure" menu entry in the GUI, or the setobs command when using scripts or the console.

In our real-world example, we deal with two macroeconomic time-series downloaded from the St, Louis Federal Reserve Bank database called FRED (https://fred.stlouisfed.org/). The first series is real GDP of the U.S. economy for which data values are collected at a quarterly frequency since 1947 (https://fred.stlouisfed.org/series/GDPC). The second series refers to the civilian unemployment rate observed at monthly frequency since 1948 (https://fred.stlouisfed.org/series/UNRATE).

The two separate spreadsheets look as depicted in Figure 2 with basic information on data characteristics reported in Table 1.

	A	В		A	В
	FRED Graph Observation	s	1	FRED Graph Observation	is
2	Federal Reserve Econom		2	Federal Reserve Econom	iic Data
3	Link: https://fred.stlouisfe		3	Link: https://fred.stlouisfe	ed_org
4	Help: https://fred.stlouisf		4	Help: https://fred.stlouisf	ed_org/help-faq
5	Economic Research Divi	sion	5	Economic Research Divis	sion
6	Federal Reserve Bank of	St. Louis	6	Federal Reserve Bank of	St. Louis
7			7		
8	GDPC1	Real Gross Domestic Prod	luct, 8	UNRATE	Civilian Unemployment Rate,
9			9	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	
10	Frequency: Quarterly		10	Frequency: Monthly	
11	observation date	GDPC1	11	observation_date	UNRATE
12	1948-01-01	2086.017	12	1948-01-01	3.4
13	1948-04-01	2120.450	13	1948-02-01	3.8
14	1948-07-01	2132.598	14	1948-03-01	4.0
15	1948-10-01	2134.981	15	1948-04-01	3.9
16	1949-01-01	2105.562	16	1948-05-01	3.5
17	1949-04-01	2098.380	17	1948-06-01	3.6
18	1949-07-01	2120.044	18	1948-07-01	3.6

Figure 2: Raw Data of Real GDP and Unemployment Rate for the U.S., Spreadsheet

Series	Frequency	Starting Date	Ending Date
GDPC1	quarterly	1948Q1	2018Q2
UNRATE	$\operatorname{monthly}$	$1948\mathrm{M}1$	$2018\mathrm{M}7$

Table 1: Data Information of Raw Data

Working with these two series involves three problems. First, the frequency among the variables differs which requires some method to equalize it. Second, the starting date of the series is different and also needs being adjusted. Third, both series are stored in separate Excel files and need being joined. All three tasks can easily be done using Gretl.

First, we load the monthly UNRATE series via the "File, Open data, User file" menu items which opens the "spreadsheed import" window (see Figure 3). As the name of the first variable ('observation_date') has its entry in the spreadsheet in column A and row 11 we start the data import of the rectangular block at this position as depicted in Figure 3.



Figure 3:

In case Gretl has not successfully recognized the time-series structure given some observation column (here 'observation_date'), the user can manually determine the frequency and starting by the menus automatically showing up in the process. Alternative we can set the data structure by the following setobs command

setobs 12 1948:1 --time-series

where '12' refers to the number of observations per year ('12' for monthly data) followed by the initial observation date and an option saying that the data has a time series structure. The series which appear in the main window are of the so called 'series' type.

As real GDP is only quarterly observed, we need to transform the monthly UNRATE series to quarterly observations. A standard way to do this is to compute the average of three consecutive months of a specific quarter. This is easily done via the "Data, Compact data" menu or the command

dataset compact 4

telling Gretl to transform the dataset from a monthly to a quarterly frequency which ranges from 1948Q1 to 2018Q2.

The next step involves appending the real GDP series from another source to the existing dataset. However, we need to make sure that the currently active dataset covers the same time span as the one wished to append. Thus, to avoid error, we restrict the currently selected sample for the period between 1948Q1 to 2018Q2 by the command smpl 1948:1

2018:2. Appending a file can be done by using the "File, Append data" menu items followed by the same request of the 'spreadsheet import' window as already shown in Figure 3. Gretl automatically recognizes that the appended dataset has the same length as the active one and will add the real GDP series to the dataset. This will finally result in Figure 4.

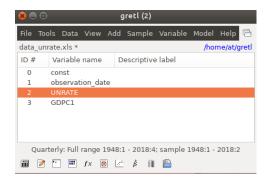


Figure 4:

Instead of using the GUI, these steps can be done using a collection of Gretl commands as shown in the Appendix A.2.

It should be said, that Gretl natively includes many example datasets, some of them taken from popular econometrics textbooks. These can be accessed through the "File, Open data, Sample file" menus. Additionally, since the latest stable Gretl version (2018b) available, users can easily download data from the DB.NOMICS database (https://next.nomics.world/). See for a how-to the following video on youtube: https://youtu.be/B2KmX9A6ICg. Also there exist user-written packages for downloading data from the quandl.com (see the getQuandl package), and yahoo.com (see the yahoo_get package) databases.

3.2 Basic Commands

The purpose of this section is to introduce some basic commands which are frequently executed when doing data analysis. In the following, we proceed with the dataset compiled in the previous step. Once the data is loaded, one should check it for validity. Initially, we will generate a so called list which can (and should!) be used to make command scripts less verbose and repetitious, and more easily modifiable. In the following, a list named L should include both variables of interest namely UNRATE and GDPC1:

list L = UNRATE GDPC1

For printing the values for each variable in a list by their respective observations, we use the print command with the --byobs option:

print L --byobs

summary L

The corresponding output for the first five observations looks like:

UNRATE	GDPC1
3.73333	2086.02
3.66667	2120.45
3.76667	2132.60
3.83333	2134.98
4.66667	2105.56
	3.73333 3.66667 3.76667 3.83333

One can easily compute basic descriptive statistics for elements in a list by means of the summary (execute help summary in the console for obtaining additional options) command

which returns various statistics as well as information on eventual missing values:

UNRATE GDPC1	Mean 5.7771 8557.0	Median 5.5667 7013.6	Minimum 2.5667 2086.0	Maximum 10.667 18507
UNRATE GDPC1	Std. Dev. 1.6318 4956.1	C.V. 0.28245 0.57919	Skewness 0.62860 0.44045	Ex. kurtosis 0.096705 -1.1495
UNRATE GDPC1	5% perc. 3.5050 2465.1	95% perc. 9.0617 17234	IQ range 2.2083 9046.0	Missing obs. 0 0

In case one wants to compute these descriptive statistics using only for data between 1980Q1 and 2007Q4 one simply needs to restrict the sample accordingly before calling the summary command by smpl 1980:1 2007:4.

The user also has options to restrict the underlying sample in a more complicated way, for instance by running the command

smpl UNRATE>4 && UNRATE <= 9.6 --restrict --replace

which would restrict the selected dataset to observations which fulfil the criteria that UNRATE is greater 4 but less or equal to 9.6, and replace any eventual previous restrictions imposed by the --replace option.¹

Gretl will inform the user that the currently selected sample includes only 237 out of all 282 observations as depicted in Figure 5. The information that the currently selected sample is "undated" informs that due to the restrictions imposed, the time-series structure of consecutive observations has been broken. The original full sample with a time-series structure can be restored by the smpl full command.



Figure 5: Sample Selection Information After Imposed Restriction

Sometimes one has to manipulate data entries due to wrong or missing values recorded. Let us assume that variable UNRATE includes a missing value for observation 1981Q2 but you know that the U.S. unemployment rate has been 7.4 % for this observation. Replacing a valid value or a missing value for a specific observation can be simply done by

UNRATE[1981:2] = 7.4

A basic statistics for a bivariate analysis is the correlation coefficient. The correlation coefficient can be easily computed for all pairs of variables in a list by means of the command corr L

which computes Pearson's product-moment correlation. Other types of correlation such as Spearman's rho (using the option --spearman) and Kendall's tau (using --kendall) are also available. The correlation between $UNRATE_t$ and $GDPC1_t$ where t is a subscript referring to the t-th observation for t = 1, ..., T is not significantly different from zero in this example:

```
corr(UNRATE, GDPC1) = -0.01416004
Under the null hypothesis of no correlation:
t(280) = -0.236967, with two-tailed p-value 0.8129
```

An overview about some available descriptive statistics are listed in Table 2.

¹An overview about logical operators can be found in Table A1 in the Appendix.

Command	Description
summary	Prints summary statistics of the series
xtab	Displays a contingency table or cross-tabulation for series
freq	Prints/ Plots the frequency distribution of the series
corr	Prints the pairwise correlation coefficients for series
xcorrgm	Prints and graphs the cross-correlogram between two series
pergm	Computes and displays the spectrum of the series

Table 2: Examples of Descriptive Statistics in Gretl

3.3 Plotting

Visualising data marks an important step in empirical work. Gretl generates graphs by means of the reliable open-source tool gnuplot which is available for many platforms. Gnuplot is a very full-featured graphing program with myriad options (for details see ch. 6 in the gretl manual). Gretl gives you direct access, via a graphical interface, to a subset of gnuplot's options and it tries to choose sensible values for you; it also allows you to take complete control over graph details if you wish.

In a time-series context, an obvious informative graph is the time-series plot which depicts data over time. This is easily done in Gretl by (the backslash allows for line breaks) gnuplot L --with-lines=GDPC1 --with-impulses=UNRATE \
--time-series --output=display

and the graph can be seen in Figure 6(a). We ask gnuplot to plot the variables in list L over time using the --time-series option. Furthermore, we want series GDPC1 being drawn as a line but UNRATE as impulses in this example. The option --output=display returns an immediate plot onto the screen.

Also scatter-plots serve as standard tools for visualising relationships between two variables. A simple scatter-plot with a linear OLS-based regression fit is called by (see Figure 6(b)):

gnuplot L --fit=linear --output=display

The option -output=filename controls the filename used, and at the same time allows you to specify a particular output format. Supported output formats are .eps (Encapsulated PostScript), .pdf PDF and .png PNG among others. For instance, for storing the figure as png-file in a specific directory just write --output="C:\Project\Figures\Fig1.png".

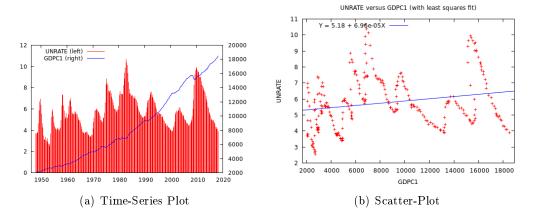


Figure 6: Time-Series and Scatter-Plot using Gretl

Another useful type of plot is the Boxplot which comprises a number of useful descriptive information for the researcher. The boxplot command produces these type of graphs easily in Gretl. Before showing an example, however, let's generate a new series named GreatModeration which shall be a binary dummy variable taking the value of one for observations between 1985Q1 and 2007Q4, and otherwise zero:

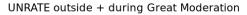
```
series GreatModeration = (obs>="1985:1" && obs<="2007:4")
```

The ones indicate the well-known Great Moderation period during which business cycle indicators such as GDP growth and price inflation rates followed a rather stable path associated with only small variance round some mean value.

Next, we draw the boxplot of the UNRATE series and examine its distribution conditional on the value of the dummy variable GreatModeration:

```
boxplot UNRATE GreatModeration --factorized --output=display \
{ set title 'Distribution of UNRATE outside and during Great Moderation'; }
```

The graph is depicted in Figure 7 showing that the variance of the unemployment rate has indeed been smaller during the Great Moderation in the U.S. Also, note that we added a self-explanatory title to the graph.



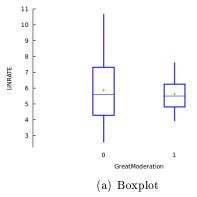


Figure 7: Factorized Boxplot using Gretl

4 Let's estimate a dynamic time-series model

In this section we want to illustrate how to estimate a dynamic single-equation time-series model. We want to examine the dynamic relationship between the change in the unemployment rate and growth in output (as proxied by the Gross Domestic Product). This relationship is known as 'Okun's Law' named after the famous macroeconomist Arthur Melvin Okun who formulated a negative relationship between these two variables.

Before starting estimating a regression model, one needs to generate the two variables of interest. The following two lines generate two new series objects where dU refers to the period-change in the unemployment rate, $dU_t = U_t - U_t$, and gY refers to the (exact) period-growth rate of real GDP (in percent), $gY_t = 100 \times \left(\frac{Y_t - Y_{t-1}}{Y_{t-1}}\right) = 100 \times \left(\frac{Y_t}{Y_{t-1}} - 1\right)$:

As can be seen, in a time-series (but also panel) context, Gretl easily handles lags and leads by using an expression such as $\mathbf{x}(\mathbf{p})$ where p generates the p-th lag if it takes a negative and the p-th lead if it takes a positive integer value.

For illustration purpose we want to estimate the following linear autoregressive distributed lag (ARDL(p,q)) model

$$dU_t = \beta_0 + \sum_{i=1}^p \beta_i dU_{t-i} + \sum_{j=0}^q \theta_j g Y_{t-j} + u_t, t = 1, \dots, T$$
 (1)

where dU_t is a function of its own p lagged values, and the contemporary as well as lagged values up to order q of growth of output, gY_t . The error-term u_t follows a white-noise zero mean process with constant variance $u_t \sim WN(u, \sigma_u^2)$.

The objective is to estimate the unknown β and θ parameters. Assuming, that gY_t is indeed exogenous w.r.t. dU_t meaning that gY_t causes contemporarily dU_t but not vice versa, we can estimate eq. (1) by simple OLS.

For illustration we will base the estimation on a specific sub-sample ranging from 1985Q1 to 2007Q4 comprising in total T=92 valid observations as this sample is associated with parameter stability. As a consequence of two oil crises in the mid and late 1970s as well as the recent Great Financial Crisis, Okun's Law has been associated with changed model coefficients and heteroskedasticity — so called structural breaks which violate some of the standard Gauss Markov assumptions required for an unbiased and efficient OLS estimator. The sample restriction is called by the command:

smpl 1985:1 2007:4

For simplification, we restrict the lag-orders p and q to be equal which of course doesn't actually have to be but simplifies things. The unknown optimal finite lag-order is usually determined by means of information criteria add REF. We use Gretl's built-in var command with the option --lagselect to determine the optimal lag order by setting the maximum lag order twice the data frequency (=8 for quarterly data). The command and the corresponding output are

var 8 dU gY --lagselect

lags	loglik	p(LR)	AIC	BIC	HQC
1 2 3 4 5 6 7 8	-7.70739 -0.56199 1.35475 3.11277 4.19395 6.09821 8.02423 14.89473	0.00642 0.42901 0.47544 0.70592 0.43254 0.42640 0.00817	0.297987 0.229608* 0.274897 0.323635 0.387088 0.432648 0.477734 0.415332	0.462451* 0.503716 0.658647 0.817029 0.990124 1.145327 1.300056	0.364366 0.340241* 0.429782 0.522773 0.630479 0.720291 0.809630 0.791481

While the Akaike (AIC) and Hannan–Quinn (HQC) information criteria select the optimal lag-order to be $p^* = q^* = 2$ — resulting in a ARDL(2,2) model — the Schwarz (BIC) criteria

selects a parsimonious ARDL(1,1) model. We stick to the ARDL(2,2) in the following example but the reader is invited to re-run the analysis for a ARDL(1,1) model.

Estimating the ARDL(2,2) model by means of OLS can be done by

```
Model <- ols dU const dU(-1 to -2) gY(0 to -2)  \# \ \ \text{equal to: ols dU const dU(-1) dU(-2) gY gY(-1) gY(-2)}
```

which illustrates the ease of handling leads and lags in Gretl. The ols command is followed by the name of the endogenous variable and a set (or list) of exogenous series. The intercept is not included per default but can be added by the const series (the built-in identifier for a constant or y-intercept). Furthermore, note the expression Model <- preceding the actual ols command. This expression generates a so called model object (here named "Model") which instantly appears in the icon view. A double-click on the "Model"-icon opens the "models"-window (see Figure 8) where the user can proceed with a GUI for calling various tests and inference, change the model specification, plot several estimation-related graphs such as residuals and fitted values etc. This shows the nice implementation of graphical objects which are especially useful for beginners and teaching.

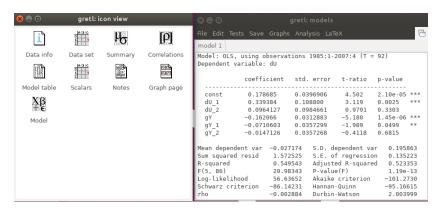


Figure 8: Model Window

The well-formatted estimation output covers standard model information:

Model 1: OLS, using observations 1985:1-2007:4 (T = 92) Dependent variable: dU

	coefficient	std. error	t-ratio	p-value	
const dU_1 dU_2	0.178685 0.339384 0.0964127	0.0396906 0.108800 0.0984661	4.502 3.119 0.9791	2.10e-05 0.0025 0.3303	*** ***

```
-5.180
                                                  1.45e-06 ***
           -0.162066
                          0.0312883
ğY_1
                          0.0357299
                                       -1.989
                                                  0.0499
           -0.0710603
                                                           **
           -0.0147126
                          0.0357268
                                        -0.4118
                                                  0.6815
                     -0.027174
Mean dependent var
                                 S.D. dependent var
                                                       0.195863
Sum squared resid
                      1.572525
                                 S.E. of regression
                                                       0.135223
                      0.549543
                                 Adjusted R-squared
R-squared
                                                       0.523353
F(5, 86)
                      20.98343
                                 P-value(F)
                                                       1.19e-13
Log-likelihood
                      56.63652
                                                      -101.2730
                                 Akaike criterion
Schwarz criterion
                     -86.14231
                                 Hannan-Quinn
                                                      -95.16615
                     -0.002884
                                 Durbin-Watson
                                                       2.003999
```

Excluding the constant, p-value was highest for variable 9 (gY_2)

Before proceeding with the model interpretation, one needs to run specification tests to check whether the Gauss-Markov criteria are fulfilled by the estimated models. Using commands instead of the GUI, the estimated residuals are depicted in Figure 9(a) and can be directly accessed after having executed the ols command by the \$uhat accessor (for a list of available accessors, click the menu "Help, function reference"):

```
series resid = $uhat  # store residuals as series object
gnuplot resid --with-lines --time-series --output=display
```

The following four lines run a battery of specification tests. The modtest command calls various built-in specification tests such as tests on remaining serial correlation of order k in the residuals (using k --autocorr), the White's test on homoskedasticity (--white) and more (see help modtest for details). The command reset calls Ramsey's RESET test on the correct functional form while qlrtest performs the Quandt likelihood ratio test for a structural break at an unknown point in time. Many more standard tests are easily accessible for cross-sectional, time-series and panel-data models. The --quiet option suppresses auxiliary regressions which may be deactivated if one wants to understand how the respective tests are actually performed.

The output indicates that the model does not seem to suffer from any misspecification issues and also there is no hint on parameter breaks at any point in time (see Figure 9(b)):

```
Breusch-Godfrey test for first-order autocorrelation Test statistic: LMF = 0.030358,
```

```
with p-value = P(F(1,85) > 0.0303584) = 0.862

White's test for heteroskedasticity

Test statistic: TR^2 = 12.437424,

with p-value = P(Chi\text{-square}(20) > 12.437424) = 0.900198

RESET test for specification (squares and cubes)

Test statistic: F = 2.831376,

with p-value = P(F(2,84) > 2.83138) = 0.0646

Quandt likelihood ratio test for structural break at an unknown point,

with 15 percent trimming:

The maximum F(6, 80) = 1.38908 occurs at observation 2000:3

Asymptotic p-value = 0.870269 for chi-square(6) = 8.33445
```

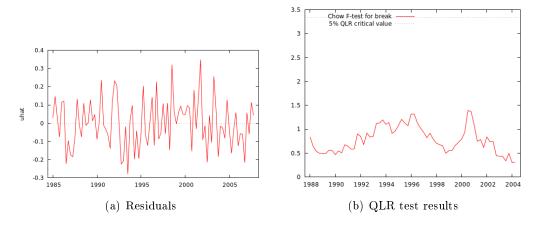


Figure 9: Estimated residuals, \hat{u}_t and Quandt likelihood ratio test results on parameter stability

After having checked that the OLS estimates are unbiased and efficient as the specifications seems appropriate, we compute the dynamic multipliers using the ARDL(2,2) coefficient estimates. The so called impact multiplier is refers to the immediate change in the endogenous, dU_t after a unit-change in gY_t : $\frac{\partial dU_t}{\partial gY_t} = \hat{\theta}_0 = -0.162$. A percentage point increase in growth of real GDP leads to a reduction of the change in the unemployment rate by about 0.162 percentage points in the same quarter. The long-run multiplier, $\hat{\theta}^{lr}$, is a non-linear expression computed as $\hat{\theta}^{lr} = \frac{\sum_{j=0}^2 \hat{\theta}_j}{1-\sum_{i=1}^2 \hat{\beta}_i} = -0.439$. Using Gretl we can directly compute these two multiplier values by grabbing the OLS coefficient estimates using the

```
printf "Impact multiplier = %g\n", $coeff(gY) scalar lr\_theta = ($coeff(gY)+$coeff(gY_1)+$coeff(gY_2)) / (1-$coeff(dU_1)-$coeff(dU_2)) printf "Long-run multiplier = %g\n", lr\_theta
```

\$coeff accessor as follows:

```
yielding the following values

Impact multiplier = -0.162066

Long-run multiplier = -0.439273
```

5 Working with matrices

Gretl uses the fully-fledged linear algebra library lapack. Gretl's matrix language has similarity to the syntax of widespread commercial software packages MATLAB and GAUSS. The Gretl project allows an easy transfer of series objects to the matrix-world, and vice versa. For details on matrix manipulations, matrix algebra, statistics and transformations read ch. 16 in the Gretl manual.

The following example shows how we could have estimated the ARDL(2,2) model easily by means of standard linear algebra using the solution to the minimization problem underlying standard OLS which is the famous equation $(X'X)^{-1}X'y$ where y is the $T \times 1$ vector of the endogenous and X is the $T \times k$ matrix of regressors.

```
matrix y = {dU}  # takes restricted sample into account list xlist = const dU(-1 to -2) gY(0 to -2) matrix X = {xlist} bhat = inv(X'X)*X'y printf "%12.6g\n", bhat'
```

We declare the two matrix objects y and X by directly transforming either a series or a list of series to a vector and matrix, respectively. The vector with the solution, bhat, is easily computed by using the inv() function for computing the inverse of a matrix, and ' is a shortcut for the transpose of a matrix (equal to the transp() function). The printf command prints the result

```
0.178685 0.339384 0.0964127 -0.162066 -0.0710603 -0.0147126 which is exactly the coefficient vector we have obtained before by the ols command.
```

6 Summary

References

Adkins, L. C. (2014). Using grett for Principles of Econometrics, 4th Edition. Number 1412.

Cottrell, A. (2017). Hansl: A dsl for econometrics. In *Proceedings of the 2Nd International Workshop on Real World Domain Specific Languages*, RWDSL17, pages 1:1–1:10, New York, NY, USA. ACM.

A Appendix

A.1 Further Resources

Lee Adkins youtube

A.2 Data Preparation and Cleaning Process

Below is a script for loading, defining, transforming, appending and storing the dataset used in Section 3.1. The script replicates all steps which were done using the GUI elements in Section 3.1 before.

```
# Load the monthly series
open /home/at/UHHĎisk/AUS_Econ_Review_GRETL/data_unrate.xls --rowoffset=10
# Define the data structure
setobs 12 1948:01 --time-series
# Transform the monthly series to quarterly
dataset compact 4
# Set the sample in line with the series being appended
smpl 1948:1 2018:2
# Append the real GDP series
append /home/at/UHHDisk/AUS_Econ_Review_GRETL/data_gdp.xls --rowoffset=10
# Drop the series 'observation_date'
delete observation_date
# Store the two time-series in native Gretl data format (*.gdt)
store "data_project.gdt"
                              # alternatively one can use "*.csv"
# Open the clean project file
open "data_project.gdt"
```

A.3 Econometric Models

A.4 Logical Operators

?? The following logical operators are supported in Gretl.

Logical symbol	Meaning
==	Is equal to
!=	Is not equal to
&&	And
	Or
>	Greater than
>=	Greater than or equal to
<	Less than
<=	Less than or equal to

Table A1: Logical Operators

A.5 *if*-conditions

A.6 Loops

A.7 Functions

A.8 Communication with other software packages

Gretl support the communication with other popular software packages. Through the so called "foreign mechanism" the user can interpolate into a hansl script a set of statements to be executed by another program, with apparatus available to ferry data between the programs. This facility is supported for Octave, R, Python, Ox, Stata and Julia. This is especially useful to exploit functionality in the "foreign" program that is not currently available in Gretl. For details see ch. 39 to 44 in the Gretl manual.