# How coexistence mechanisms mediate temporal stability

- <sup>2</sup> Andrew T. Tredennick, Peter B. Adler, and Frederick R. Adler
- 3 Andrew T. Tredennick (atredenn@gmail.com), Department of Wildland Resources and the
- <sup>4</sup> Ecology Center, Utah State University, Logan, UT
- 5 Peter B. Adler, Department of Wildland Resources and the Ecology Center, Utah State
- 6 University, Logan, UT
- 7 Frederick R. Adler, Departments of Biology and Mathematics, University of Utah, Salt Lake
- 8 City, UT

## 9 Introduction

- 10 Species richness tends to confer temporal stability of biomass production in competitive
- plant communities via compensatory dynamics among species. Two classes of mechanisms
- can produce copmensatory dynamics: (1) temporal complementarity among species and
- 13 (2) functional complementarity among species. Temporal complementarity results in asyn-
- chronous population fluctations that, when aggregated over all populations in a community,
- dampens variability at the community or ecosystem level. Such asynchonry in population
- dynamics through time is driven by either species-specific responses to variable environmental
- 17 conditions or differences in the rate at which species respond to disturbance.
- 18 In contrast to temporal complementarity, functional complementarity increases community
- stability by reducing the strength of interspecific competition. Once thought to be stabilizing
- 20 at the community level, recent work suggests interspecific competition is actually destabilizing.
- 21 This is because functional complementarity and competition are negatively correlated, and
- <sup>22</sup> functional complementarity among species (i.e., non-temporal niche differences) generally
- 23 results in the productivity of speecies in mixture being greater than expected from monocul-

- tures. So called overyielding increases mean productivity more than its variance, leading to
- <sub>25</sub> greater temporal stability.
- 26 This implies a strong role for the mode and stability of species coexistence. Yet, theoretical
- 27 work aimed toward identifying the mechanisms by which species richness promotes temporal
- 28 stability has treated species coexistence as a foregone conclusion. Most studies either assume
- 29 coexistence a priori or ensure coexistence by non-temporal forms of niche differentiation. In so
- doing, that large body of work implicitly assumes that the interaction between environmental
- variability and the mechanism(s) by which species coexist is trivial.
- To that end, we will analyze a general consumer-resource model under different coexistence
- assemptions. Our starting point is a model of two plant consumers and one resource (e.g., soil
- moisture or nitrogen). We will focus on three cases of species coexistence:
- 1. Relative nonlinearty
- 2. Temporal storage effect
- 3. A combination of both mechanisms
- Each scenario requires different model assumptions and structure, so we will describe each
- in turn. Although the structure may change slightly to incorporate different coexistence
- 40 mechanisms, the strength of our approach lies in the similarities among the models since we
- work under a unified consumer-resource framework.

# 42 Model description and analysis

## 43 A general consumer-resource model

- 44 We start with a general consumer-resource model where the consumer can be in one of
- two-states: a dormant state D and a live state N (Figure  $\sim$ ??). Transitions between N and

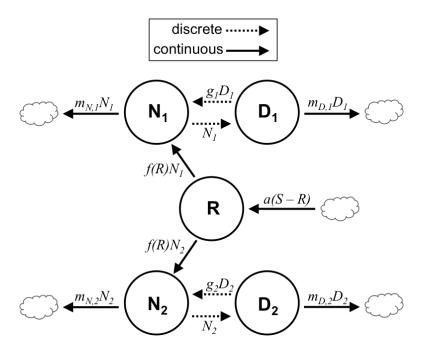


Figure 1: Diagram of our semi-discrete consumer-resource model. Solid lines show continuous dynamics while dashed lines show the discrete transitions.

 $^{46}$  D occur at discrete intervals T, so our model is formulated as "pulsed differential equations" (Pachepsky et al. 2008, Mailleret and Lemesle 2009). For clarity we refer to T as years and the growing time between years,  $\tau$ , as seasons. Seasonal (within-year) dynamics are modeled as three differential equations:

$$\frac{\mathrm{d}D_i}{\mathrm{d}\tau} = -(m_{D,i}D_i)\tag{1}$$

$$\frac{\mathrm{d}N_i}{\mathrm{d}\tau} = f_i(R)N_i - m_{N,i}N_i \tag{2}$$

$$\frac{\mathrm{d}R_i}{\mathrm{d}\tau} = a(S - R) - \sum_{i=1,2} f_i(R)N_i \tag{3}$$

where i denotes species, D is the dormant (long-lived) biomass state, N is the living biomass (fast-growing, shorter-lived) state, and ms are biomass loss rates. The growth rate of living biomass is a resource-dependent function,  $f_i(R) = r_i e^{-\alpha_i e^{-\beta_i R}}$ . For the resource dynamics, whose state is denoted by R, we use a linear resource renewal equation where a scales resource turnover rate and S is the resource equilibrium when consumers are absent, and an offtake of the resource equal to the sum of each species' consumption,  $\sum_{i=1,2} f(R)N_i$ . Note that since transitions between N and D are pulsed, only biomass loss occurs throughout the season for D.

At the beginning of each season we start with initial conditions defined as  $V_t$ ,  $W_t$ , and  $Z_t$  for the dormant state, the live state, and the resource, respectively. So for each season, Eqs. 1-3 are solved given the initial conditions:

$$D_i(0) = V_{i,t} \tag{4}$$

$$N_i(0) = W_{i,t} \tag{5}$$

$$R(0) = Z_t \tag{6}$$

Table 1: Definition of model parameters.

	Table 1. Benintion of model parameters.
Parameter	Definition
$m_D$	dormant state mortality rate
r	live state maximum resource uptake rate
K	live state half-saturation constant for resource uptake rate
$m_N$	live state mortality rate
a	resource turnover rate
S	resource supply rate
g	dormant-to-live biomass transition fraction

- The consumers transition between N and D instantaneously between years. We assume
- resource density does not change between years. So, at the yearly transition:

$$V_{i,t+1} = [N_i(T^-) + D_i(T^-)](1 - g_t)$$
(7)

$$W_{i,t+1} = [N_i(T^-) + D_i(T^-)]g_t$$
(8)

$$Z_{t+1} = R(T^{-}) (9)$$

where  $D(T^-)$ ,  $N(T^-)$ , and  $R(T^-)$  are the densities of each state at the end of the year and g is a time-fluctuating activation rate that regulates how much dormant biomass is converted to growing-season live biomass each year. Our formulation assumes that at the end of each season all accumulated living biomass  $[N(T^-)]$  is converted to dormant biomass.

## 67

#### 68 Implementing the storage effect

To make this a "storage-effect" model, we need to satisfy three conditions: (1) the organisms must have a mechanism for persistence under unfavorable conditions, (2) species must respond differently to environmental conditions, and (3) the effects of competition on a species must be more strongly negative in good years relative to unfavorable years. Our model meets

condition 1 because we include a dormant stage with very low death rates. We satisfy condition 2 with our model whenever g is not perfectly correlated between species. Lastly, our model meets condition 3 because condition 2 partitions intraspecific and interspecific competition into different years. Thus, during a high g year for one species, resource uptake is also inherently high for that species, which increases intraspecific competition relative to interspecific competition. So, given adequate variability in g, the inferior competitor (species with lower r) can persist.

Following Adler and Drake (2008), we generated sequences of (un)correlated dormant-to-live state transition rates (g) for each species by drawing from multivariate normal distributions with mean 0 and a variance-covariance matrix of

$$\begin{bmatrix} \sigma_E^2 & \rho \sigma_E^2 \\ \rho \sigma_E^2 & \sigma_E^2 \end{bmatrix} \tag{10}$$

where  $\sigma_E^2$  is the variance and  $\rho$  is the correlation between between the two species' transition rates. For environmental variability, here induced as variability in g, to promote coexistence via the storage effect,  $\rho$  must be less than 1. The inferior competitor has the strongest potential to persist when  $\rho = -1$  (perfectly uncorrelated transition rates).

#### 87 Implementing relative nonlinearity

When considering consumer-resource dynamics, species coexistence by relative nonlinearity requires that each species has different nonlinear responses to resource availability, and resource availability must fluctuate through time. In a constant resource environment, the species with the lowest R\* will always exclude the other species. So we can compare this model to the storage effect model, we still allow the germination rate g to vary, but both species are perfectly correlate – that is,  $\rho = 1$ .

## 94 Results

## 95 Storage effect model

- Some preliminary results from running simulations of the storage effect version of the model
- <sup>97</sup> at different levels of environmental cue variability  $(\sigma_E)$  and resource supply variability  $(\sigma_S)$ .
- I ran 20 simulations at each combination of  $\sigma_E$  and  $\sigma_S$  shown in Figure~?? (the points are
- the means across the 20 simulations, each run for 2,000 time-steps, with the initial 1,000
- time-steps discarded before calculating anything). There is a weak trend of community CV
- to saturate at high levels of resource supply variability (Figure~??, top panel).
- One of the things we are interested in is how well the community buffers itself against resource
- variability. Really I should calculate some kind of asynchrony metric, but for now I just
- looked at the ratio of the resource CV to the community CV (Figure~??, bottom panel).
- 105 Kind of difficult to interpret, but it is interesting that at high levels of variability in the
- environmental cue that drives the storage effect, the ratio decreases with resource supply
- variability. The opposite occurs at lower levels of variability in the environmental cue.

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