Data-Flow Analysis: Simulation and Visualisation

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Abstract

Data-flow analysis is one of the cornerstones of modern compiler optimisation. A thorough understanding of the processes involved is essential to further exploration of the subject. A tool which allows exploration of data-flow analysis in an interactive environment would prove invaluable to students encountering the topic for the first time.

This report describes the design and implementation of an interactive system to simulate and visualise forms of data-flow analysis on simple assembly-like programs. The system is evaluated by in terms of user experience and the achievement of learning outcomes, through self-assessment and by examining usage data collected during the evaluation period.

The software proved (successful/unsuccessful) in providing a tool for increasing the learning capacity of the subjects.

Acknowledgements

Acknowledgements go here.

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Introduction

This chapter gives a short introduction to the topic of data-flow analysis, describes motivations and desired outcomes for the project and provides a brief summary of contributions.

1.1 Data-Flow Analysis

Data-flow analysis is a tool for analysing the flow of data through a program at various points in its execution. Analysis is performed over a control-flow graph, computing the properties of values flowing in and out of each node. Many forms of data-flow analysis exist to compute various properties, for example liveness analysis identifies variables which will be used in future instructions and available expressions identifies those expressions whose value has been previously computed at some point in the control-flow graph.

This analysis is used to inform optimisations which can be performed on a given program. Using the example of *liveness analysis*, the values computed can be used to optimise register allocation: a variable which is not live at a given point does not need to be allocated to a register, enabling more efficient use of available resources.

Data-flow analysis is not only useful in compiler optimisation. The information gathered can be used in other ways, such as identifying unsafe operations in PHP web applications^[1] by monitoring sanitization¹ of variables which have been assigned to user input.

¹To sanitize a user input is to remove any potentially dangerous elements from said input; for example, if a user input string is to be inserted into the HTML of a webpage it could be sanitized by replacing instances of < and > with < and >, respectively. This would prevent that input being misinterpreted as HTML and thus avoid malicious scripts contained within that input from being executed.

1.2 Motivations

This project was inspired by the project's supervisor, Hugh Leather. The original concept was an online tutor for data-flow analysis which would allow users to simulate an analysis on simple programs. The user could vary parameters, such as the data-flow in question or the order in which nodes are evaluated, and examine the resulting solution.

As lecturer of the Compiler Optimisations course at the University of Edinburgh, Dr. Leather desired a system which could teach students the foundations of the course in a more interactive format than standard lectures. The system should be suitable for hosting on the course web page to make it accessible to all students.

My personal interest in this project stemmed from a desire to use my practical skills to increase my capacity for understanding theoretical content. As noted in our early discussions, many students find it difficult and time consuming to read and understand material from the course textbook. Presenting this information in such a way that it could be easily digested by even a novice to Computer Science provided an exciting challenge.

1.3 Objectives

The main aim of this project was to create an interactive system to teach students the basic principles of data-flow analysis in compilers.

This would take the form of a web application using visual components which could be combined in different ways, for example to present a series of tutorials on data-flow analysis or to provide a sandbox environment to explore. The content of the application would cover a range of topics from the basics of data-flow analysis to algorithms and frameworks for solving generic data-flow problems.

The application would be aimed at students of the Compiler Optimisations course and as such would be based on material from the course textbook *Engineering a Compiler*, 2nd ed.^[2] by Keith D. Cooper and Linda Torczon. The application could then be extended to cover the topic in more depth using content from *Compilers: Principles, Techniques and Tools, 1st ed.*^[3] by Alfred V. Aho, Ravi Sethi and Jeffery D. Ullman.

Users would be able to interact with the system by providing simple assembly-like programs, altering parameters of the analysis and stepping through a simulation. Elements of the simulation such as the current state and the control-flow graph of the program would be visualised on-screen and update as the simulation progressed. Each of these elements would be linked visually to show how the concepts relate.

The application would be tested on real users. It would be evaluated in terms of user experience by analysing interactions with the system and conducting a

user experience survey. Achievement of learning outcomes would be assessed by examining responses to questions built into the software and self-assessment by the user.

1.4 Summary of Contributions

The final version of the software is capable of the following:

- Simulation of pre-defined data-flows using generic framework models. (p.)
- Simulation of user-defined programs using the ILOC^[2, appx. A] language from *Engineering a Compiler*. (p.)
- Simulation using the round-robin iterative algorithm (p.)
- User-controlled simulation allowing step-by-step, instant or automated play-back.
- Visualisation of the following simulation elements:
 - Control-flow graph (p.)
 - Simulator state incl. currently evaluated node, framework etc. (p.)
 - Table of results displaying data flowing in / out of each node.
 - Hasse diagram of meet semi-lattice (p.)
- Tutorials covering basics of the topic with interactive elements (p.)
- Interactive test to assess achievement of learning outcomes

In addition, I have produced an API to record user interaction events modeled on the Google Analytics event tracking system (p.).

Detailed explanations of the terminology mentioned above can be found in chapter 2. A quick summary of terms can be found in the glossary in appendix A.

Background

This chapter briefly covers the necessary background information required to understand this project, both to inform the reader and to demonstrate understanding of the topic.

2.1 Introduction to Data-Flow Analysis

Data-flow analysis computes information about data flowing *in* and *out* of each node in a program's control-flow graph. Many types of analysis can be performed and the information gathered can be used to inform the decisions of optimising compilers. A brief list of analyses and their purposes can be found in appendix B.

2.1.1 Control-flow Graph

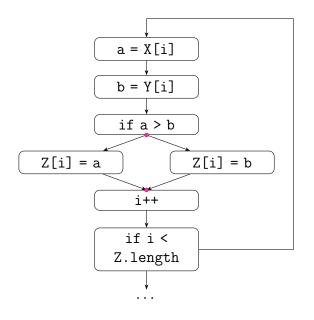


Figure 2.1: A control-flow graph.

A control-flow graph displays the possible execution paths for a given program. Each node in the graph represents an instruction or basic block, each edge represents an execution path leading from that instruction. A node can have multiple outward edges if it is a branching instruction. Branches may point backward in the control-flow. An example of a simple control-flow graph can be seen in fig. 2.1.

A point in the control-flow graph refers to some point along the edges of the graph. In data-flow analysis we usually deal with sets of values at the *in* and *out* points of each node, i.e. the point where the *in-edges* meet and the *out-edges* originate, respectively (shown in magenta on the left).

2.1.2 A Simple Example

An oft-used example of data-flow analysis is that of reaching definitions, which we will demonstrate here due to its simplicity. Reaching definitions computes the set of variable definitions which are are available at a given point. A definition is said to reach a point p if there is no intermediate assignment to the same variable along the path from the definition of the variable to the point p.

Let us take the example in fig. 2.1. The first node defines the variable a. We shall refer to this definition of a as a_1 . The definition of a reaches each point in the control-flow graph as it is never re-defined. The definition c_1 , however, does not reach the exit node as c is re-defined by c_2 . The graph in fig. 2.2 shows the set of reaching definitions at each point in the program. We have combined the in and out points to save space.

Data-flows have *direction*. Reaching definitions is a *forward flow problem*; values flow from the entry node of the control-flow graph (CFG) to the exit node.

The values at each point are determined using data-flow equations. For example, the equations for reaching definitions (defined in terms of in and out) at a given node n are:

$$In(n) = \bigcup_{p \in preds} Out(n)$$
$$Out(n) = DefGen(n) \cup (In(n) \setminus Out(n))$$

The equations for In(n) and Out(n) are often referred to as meet and transfer functions. In a forward flow problem the meet function combines the out sets of a node's predecessors to form its in set. The transfer function computes a node's out set from its in set and information obtained from the node itself, thereby transferring values through a node.

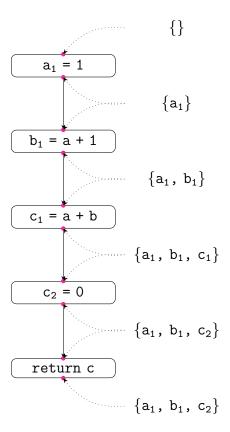


Figure 2.2: A control-flow graph.

2.1.3 Lattices

Sets in a data-flow problem have a partial order. This can be expressed using a structure known as a *meet semi-lattice*. A meet semi-lattice consists of a set of possible values L, the meet operator \wedge , and a *bottom element* \perp . The semi-lattice imposes an order on values in L such that:

$$a \ge b$$
 if and only if $a \land b = b$
 $a \ge b$ if and only if $a \land b = b$ and $a \ne b$

For the bottom element \perp , we have the following:

$$\forall a \in L, a \ge \bot$$

 $\forall a \in L, a \land \bot = \bot$

We can express the semi-lattice using a *Hasse diagram*, shown in fig. 2.3.

Some data-flows deal with sets of pairs of values. In constant propagation, we pair a variable with one of three elements: $undef(\top)$, $nonconst(\bot)$ and const. A variable is initially paired with undef. When it is assigned a constant value, we assign it that value. If it is later assigned another value, we assign it nonconst. This can be expressed as the meet function, \land , seen in fig. 2.4.

The values form a semi-lattice, as seen in fig. 2.5.

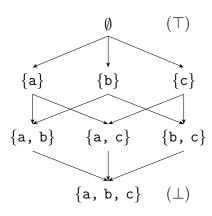


Figure 2.3: A Hasse diagram for the meet function $a \wedge b = a \cup b$.

$$nonconst \wedge c = nonconst$$
 for any constant c $c \wedge d = nonconst$ for any constants $c \neq d$ $c \wedge undef = c$ for any constant c $nonconst \wedge undef = nonconst$ for any value x

Figure 2.4: Equations describing the constant propagation meet function.

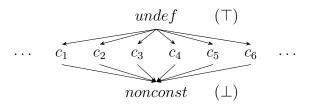


Figure 2.5: A Hasse diagram for the meet function described in fig??.

2.2 Algorithms for Analysis

There exist a number of algorithms for performing data-flow analysis. In this section, I will give a brief overview of the methods proposed in the related reading [2] [3].

2.2.1 Round-Robin Iterative Algorithm

The simplest algorithm used to solve data-flow problems is the round-robin iterative method. We consider each node of the CFG in turn, calculating the In and Out sets using our data-flow equations. This is a fixed-point computation: we iterate until our value sets stop changing between iterations. Algorithm 2.1 shows the round-robin iterative method for solving reaching definitions.

Algorithm 2.1: Iterative Round-Robin Method for Reaching Definitions

```
for each (node n in the CFG)

In (n) = \emptyset;

while (changes to any sets occur)

for each (node n in the CFG)

In (n) = \cup_{\text{predecessors } p \text{ of } n} \text{Out}(p);

Out (n) = \text{DefGen}(n) \cup (\text{In}(n) \setminus \text{DefKill}(n));

end

end
```

2.2.2 Worklist Algorithm

The above solution holds value in its simplicity, but it is trivial to find a more efficient solution. A node's sets will only change if the Out sets of its predecessors change. Thus, we may use a worklist: starting with the initial node, we calculate the Out set for that node; if it changes we add the node's successors to the list. We continue this process until the worklist is empty. Algorithm 2.2 shows the worklist method for solving reaching definitions.

Algorithm 2.2: Worklist Method for Reaching Definitions

```
worklist = [ n_0 ];

while (worklist is not empty)

n = pop(worklist);

In(n) = \cup_{\text{predecessors } p \text{ of } n} \text{Out}(p);

Out(n) = DefGen(n) \cup (In(n) \ DefKill(n));

if (Out(n) has changed) append n to worklist;

end
```

2.2.3 Structural Algorithm

A third algorithm takes an entirely different approach. Instead of iterating over each node, we perform a number of simple transformations on the graph in order to reduce it to a single region. We then expand each node, calculating the In and Out sets of our reduced nodes as we expand them. A more detailed explanation of this concept may be found in the $Dragon\ Book^{[3,\ p.\ 673]}$.

2.3 Data-Flow Frameworks

It is possible to model data-flow problems using a generic framework. This allows us to use the same algorithm for multiple problems by specifying the following constraints [3, p. 680]:

- The *domain* of values on which to operate;
- The *direction* in which data flows;
- A set of data-flow equations including the meet operator \wedge and the set of transfer functions F^1 ;
- The boundary value $v_{BOUNDARY}$ specifying the value at the entry or exit to the CFG; and
- The *initial value*, \top , at each point in the graph.

2.3.1 Algorithm for General Frameworks

Algorithm 2.3, adapted from the one in the $Dragon\ Book^{[3, p. 691]}$, computes the value sets at each node using the elements of our general framework.

Instead of referring to the value sets as In and Out as the *Dragon Book* does, we may call them Meet and Transfer. This allows us to generalise our algorithm to

Algorithm 2.3: Data-Flow Analysis of General Frameworks

```
1 Transfer BOUNDARY = VBOUNDARY;

2
3 for \ each \ (block \ B \ in \ the \ CFG)

4 Transfer B = T;

5 end

6
7 while \ (changes \ to \ any \ Transfer \ occur)

8 for \ each \ (block \ B \ in \ the \ CFG)

9 Meet_B = \wedge_{priors \ P \ of \ B} \ Transfer_P;

10 Transfer_B = F_B(In_B);

11 end

12 end
```

Figure 2.6: Algorithm for Data-Flow Analysis of General Frameworks

¹The function corresponding to a particular node/block B is denoted F_B

both forward and backward analyses; in the forward direction Meet is In whereas in the backward direction it is Out (and vice-versa for Transfer).

We first initialise the Transfer set using the boundary condition, then initialise each node's transfer set to our initial value \top .

Next, we perform a fixed-point computation on the CFG, evaluating each node's Meet and Transfer sets using our data-flow equations until the sets stop changing.

The meet is taken over a node's *priors*: in the forward direction, the node's predecessors; in the backward direction, the node's successors.

This algorithm can be applied to any framework. In fact, all of the data-flow problems in appendix B may be solved using this process.

2.3.2 Conditions for Termination

We must be careful when constructing our general frameworks. If our value sets continuously change we may never reach a fixed-point and thus our computation will never halt.

To avoid this, our frameworks must satisfy the following conditions [3, p. 684]:

- The set of transfer functions, F, contains the identity function²;
- F is closed under composition: that is, for any two functions f and g, f(g(x)) is also in F;
- \bullet F is monotone; and
- The domain and the meet operator, \wedge , must form a meet semi-lattice.

These conditions ensure that during every iteration of the algorithm the values at each point will either become smaller (with respect to the partial ordering) or stay the same. Since F is monotone, all of the sets must eventually stop changing **or** reach the bottom element of the lattice, \bot , at which point they cannot change any further.

²The identity function maps its input to its output, i.e. F(x) = x

Related Work

In this chapter I will discuss the merits and drawbacks of related work and identify aspects of said work which may be applied to this project.

3.1 Introduction

Although there exists a wide range of literature dealing with data-flow analysis in compilers *independent* of interactive tutoring and vice-versa, I believe that the combination of the two has yet to be explored. Therefore, I have widened my research to two main areas: the topic of data-flow analysis, and advancements in interactive tutoring software.

Chapter 2 provides a brief introduction to data-flow analysis with reference to two major textbooks; the first, Engineering a Compiler, 2nd ed. [2] by Keith D. Cooper and Linda Torczon, serves as an excellent introduction to the topic and a brief overview of some of the more complex elements. The second, Compilers: Principles, Techniques and Tools, 1st ed. [3] (often referred to as the Dragon Book) provides a more theoretical discussion of the material.

This chapter discusses the second area of research, advancements in interactive tutoring software.

3.2 Simulators as an Interactive Teaching Tool

In his article Evaluating A System Simulator For Computer Architecture Teaching And Learning Support^[4], Mustafa discusses the design & implementation of a system which integrates the simulation of a compiler, CPU and operating system to aid in the teaching of undergraduate computer architecture and operating systems modules.

Although brief, the article provides valuable insight into the design and evaluation of such teaching software. The primary source of feedback came from an opinion survey using a 5-point Likert scale for quantitative analysis and openended questions for qualitative feedback. In addition, students were administered a test to assess their knowledge pre- and post- use of the system.

The evaluation results highlight an important point to consider when designing teaching software; over 20% of respondents indicated that they spent more time learning how to use the software than they did completing the given exercises. An equal number of students reported that the simulator left them *more confused* than before. In addition, 7.1% of respondents said that the simulator was too complicated to use effectively in their tutorials.

However, the converse of these results gives a positive outlook for this project: 72.4% of respondents disagreed with the above statements and 79.3% believed that the system did improve their understanding of the topics covered in lectures. Over 95% of responents agreed that the simulator was a useful tool in understanding the material. Perhaps there is potential to achieve similar results when extending the concept to data-flow analysis.

3.3 Learning and Teaching Styles

A 1988 report by Richard M. Felder and Linda K. Silverman, entitled "Learning and Teaching Styles in Engineering Education"^[5], categorizes students' learning methods and describes ways in which professors may target specific categories in their teaching strategy.

Felder refers to the *learning modalities* (or VAK) model proposed by Walter Burke Barbe, which defines three *modalities*:

- visual those who learn best by viewing images and diagrams;
- auditory those who learn best by listening or speaking aloud; and
- **kinaesthetic** those who learn best by actively experiencing things, learning by doing.

The report claims that most people of college age and above, our intended audience, identify as *visual* learners – those who benefit from charts, diagrams and such – whereas the presentation of content in university courses is primarily *auditory* (via lectures) or a visual representation of auditory information (i.e. words or mathematical formulae).

The survey results from Mustafa^[4, p. 103] support this observation: although only a small sample (N=54) responded, 31% of respondents identified as visual learners, while a mere 6% identified as auditory learners. The majority of students (52%) identified as kinaesthetic learners, indicating that taking a hands-on approach is a valuable tool for learning.

It should be noted that Felder discounts kinaesthetic learning from his report as he considers the *learning by doing* to be a separate category, perceiving the remaining attributes of kinaesthetic learning (taste, smell, touch) to have little value in engineering. A later observation by Felder agrees with Mustafa, stating that engineers are "more likely to be active than reflective learners" [5, p. 678].

3.3.1 Ability to Identify Own Learning Style

In her PhD dissertation "Individual Differences in Learning: Predicting One's More Effective Learning Modality" [6], Beatrice J. Farr claims that students are able to accurately predict the learning style in which they perform best:

"An experiment with 72 college students confirmed that individuals could accurately predict the modality in which they could demonstrate superior learning performance. The data also revealed that it is advantageous to learn and be tested in the same modality and that such an advantage is reduced when learning and testing are both conducted in an individual's preferred modality." [7, p. 242]

Coffield^[8, p. 120] disagrees with this, based on an observation by Merrill^[9] that "most students are unaware of their learning styles and so, if they are left to their own devices, they are most unlikely to start learning in new ways". This would indicate that basing teaching methods on a student's preferences is damaging to their education. This is, however, a misinterpretation; the actual text of Merrill reads:

"... a student must engage in those activities ... that are required for them to acquire a particular kind of knowledge or skill ... Most students are unaware of these fundamental instructional (learning) strategies and hence left to their own are unlikely to engage in learning activities most appropriate for acquiring a particular kind of knowledge or skill." [9, p. 4]

Merrill later argues that the optimal strategy for teaching is primarily decided by the content being taught, and secondarily by the learner's preferred style [9, p. 4]. By not knowing the most effective strategy for learning the content they are studying, a student limits his or her potential. However, the appropriate strategy should in fact be tailored to the student's preferred learning style to obtain the best results.

3.3.2 Criticism of Matching

Some of the criticism levied at the concept of learning styles is that the idea of matching – exclusively teaching a student based on his or her preferred learning style – is harmful to a student's education. Although Coffield's [8, p. 120] reasoning is flawed, the conclusion drawn by him and Merrill [9, p. 4] is sound: by allowing

students to exclusively use their preferred way of learning, we risk them missing out on more effective methods of study.

Returning to the report by Felder, the following quote:

"... a study carried out by the Socony-Vacuum Oil Company that concludes that students retain 10 percent of what they read, 26 percent of what they hear, 30 percent of what they see, 50 percent of what they see and hear, 70 percent of what they say, and 90 percent of what they say as they do something." [5, p. 677]

indicates that by relying solely upon auditory methods, professors can only hope to convey as little as 26% of the desired material to their students.

Felder advocates using a mixture of teaching methods in order to appeal to all students' preferred learning styles.

3.4 Summary

While there may be some disagreement over the validity of learning styles or modalities, even its critics seem to agree that there is value in varying the methods of teaching in use. At present, the only available resources for learning data-flow analysis are lecture slides, videos and textbooks. These are primarily auditory and sometimes visual methods of teaching, with little kinaesthetic learning involved. There is a clear need for interactivity; although 52% of students identified as learning best through activity [4, p. 103], there is almost no support for this method of study.

Given the relative success of the examples discussed in this chapter and the apparent lack of any such resources for data-flow analysis, I believe there is a strong precedent for this project and as such intend to develop a system to fulfil this role.

However, it is important to note the mistakes made by the examples discussed here. The simulator designed by Mustafa was deemed too complex^[4, p. 103] by over 20% of respondents. This must be avoided if I am to create an effective learning resource.

In order to evaluate the success of my system I will build upon the methods presented by Mustafa, aggregating opinion using a Likert scale and using this data to judge overall satisfaction with the software and identify specific areas for improvement.

Data-Flow Analysis Simulation

Blah Blah

4.1 Data-Flow Framework

Blah Blah

4.2 Algorithms for Analysis

Blah Blah

4.2.1 Iterative Algorithm

Blah Blah

4.3 Intermediate Language for Optimising Compilers

Blah Blah

4.3.1 Parsing Expression Grammar

4.3.2 Control-Flow Graphs

Data-Flow Analysis Visualisation

Blah Blah

5.1 Data-Flow Framework

Blah Blah

5.2 Simulator

Blah Blah

5.3 Control-Flow Graph

Blah Blah

5.4 Lattice

Interactive Learning

6.1 User-defined Programs

Blah Blah

6.2 Interactive Tutorials

Blah Blah

6.3 Experimental Sandbox

Evaluation

Appendix A

Terminology

A.1 Glossary

- available expression An expression is available if it has been computed along all paths leading to the current node. 1, 25
- **boundary** The initial value at the starting point of an analysis, i.e. In(ENTRY) or Out(EXIT). 9
- control-flow graph A graph representing the possible execution paths in a program. Nodes represent instructions, edges represent possible jumps between said instructions. 1–3, 5, 6, 23
- data-flow A system of equations and conditions which constitute a data-flow problem, that is, a problem which may be solved through data-flow analysis. 2, 3, 6, 8–10, 23
- data-flow analysis A technique for gathering information at various points in a control-flow graph. i, 1, 2, 5, 6, 8, 11, 12, 14
- data-flow equations A system of equations which determine how data flows through a CFG. 8–10
- direction The direction in which data flows in a data-flow problem. Either forward (from the entry point of the CFG to the exit point) or backward (the opposite). 9
- **domain** The domain of values considered in a data-flow problem, e.g. definitions or expressions. 9, 10
- **dominate** In a CFG a node n_i is said to dominate a node n_j if every path from n_0 (the entry node) to n_j must go through $n_i^{[2, p. 478]}$. 24, 25
- **fixed-point** A computation in which the required process is repeated until the state stops changing. 8, 10

24 Acronyms

Hasse diagram A diagram used to represent partially ordered sets. Nodes represent elements of the sets, edges represent an ordering between a pair of elements. 3, 7

- Likert scale A method of gauging opinion on a topic, consisting of a collection of Likert items. Each Likert item contains a statement followed by an odd number of responses, containing an equal number of positive and negative responses balanced such that the difference between responses is uniform. An example Likert item is the oft-used Strongly Agree / Strongly Disagree scale, which may be weighted from from 1-5. The Likert scale is the sum of weights of responses to Likert items. 12, 14
- liveness analysis A variable is *live* if its current value will be used later in the program's execution. 1, 25
- meet An equation (or set of equations) which determines how data flows between nodes in a CFG. 6, 9, 10
- **meet operator** An operator which defines how the meet of two sets is obtained, such as \cup , \cap or another operator entirely. 9, 10
- meet semi-lattice A partially ordered set in which there exists a greatest lower bound (or meet) for any non-empty, finite subset. 3, 6, 10
- reaching definition A definition of a variable reaches a block if there exists at least one path from its definition to the block along which it is not overwritten. 6, 8, 25
- **region** A set of nodes in a graph which includes a *header* node which dominates all other nodes in the region^[3, p. 669]. 9
- **transfer** An equation (or set of equations) which determines how data flows through a node in a CFG. 6, 9, 10

A.2 Acronyms

CFG control-flow graph. 6, 8–10, 23, 24

Appendix B

Types of Data-Flow Analysis

Data-Flow	Purpose	Applications
Dominators	Computes the set of nodes	Computing SSA form.
	which dominate the current	
	node.	
Reaching definitions	Computes the set of vari-	Generating def-use chains
	able definitions which are	for other analyses.
	available at points in the	
	CFG.	
Liveness analysis	Computes the set of vari-	Register allocation. Iden-
	ables whose current value	tifying useless store oper-
	will be used at a later point	ations. Identifying unini-
	in the control flow graph.	tialised variables.
Available expressions	Identifies expressions which	Code motion.
	been computed at a previ-	
	ous point in the CFG.	
Anticipable Expressions	Computes expressions	Code motion.
	which will be computed	
	along all paths leading from	
	the current point.	
Constant Propagation	Computes the set of vari-	Constant propagation.
	ables which have a constant	Dead code elimination.
	value based on previous as-	
	signments.	
Copy Propagation	Computes the set of vari-	Dead code elimination.
	ables whose values have	Code motion.
	been copied from another	
	variable.	
Tainted Flow Analysis ^[1]	Identifies unsafe operations	Preventing security vulner-
	which have been passed un-	abilities such as SQL injec-
	sanitized (tainted) input as	tion and XSS attacks.
	a parameter.	

Table B.1: Types of data-flow analysis.

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