

1.

DATE
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① Algorithm $\text{inPlacePartition}(\text{arr}, s, e)$

```

pivot ← arr[e]
pos ← s
for i = s → e-1 do
    if arr[i] < pivot then
        if (i != pos) then
            temp ← arr[i]
            arr[i] ← arr[pos]
            arr[pos] ← temp
        pos++
temp ← arr[pos]
arr[pos] ← pivot
arr[e] ← temp
return pos
        
```

$\text{IP} = [1, 6, 2, 4, 3, 5]$
 $[5, 6, 2, 4, 3, 1], 0, 5$
 $[1, 6, 2, 4, 3, 5]$

$[1, 5, 2, 4, 3, 6]$ $[3]$
 $[1, 3, 2, 4, 5, 6]$ $[4]$
 $[1, 4, 2, 3, 5, 6]$ $[3]$
 $[1, 2, 4, 3, 5, 6]$
 $[1, 2, 3, 4, 5, 6]$
 $[1, 2, 3, 4, 5, 6]$ $[3]$
 base condition base worst condition

input = $[1, 6, 2, 4, 3, 5]$
 $[5, 6, 2, 4, 3, 1]$
 $[1, 6, 2, 4, 3, 5]$

$[1, 2, 3, 4, 5, 6]$

2.

2.
(a)

[5, 1, 4, 3, 6, 2, 7, 1, 3] (n=9)

of elements $\leq \frac{3 \times 9}{4} \approx 7.5 = 7$
 # of elements $< 5 = 6$

Pivot = 5 Pivot = 1
 $> 5 = 2 \checkmark$ $> 1 = 7 \checkmark$
 $< 5 = 6$ $< 1 = 0$

Pivot = 4 } $> 4 = 3 \checkmark$ Pivot = 3 } $> 3 = 4 \checkmark$ Pivot = 6 } $> 6 = 1 \checkmark$ Pivot = 2 } $> 2 = 6 \checkmark$
 $< 4 = 5$ $< 3 = 3$ $< 6 = 7$ $< 2 = 3$

Pivot = 7 } $> 7 = 0 \checkmark$ Pivot = 1 } $> 1 = 7 \checkmark$ Pivot = 3 } $> 3 = 4 \checkmark$
 $< 7 = 8$ $< 1 = 0$ $< 3 = 3$

total Pivots = 9

Pivots with right and left elements $< 7 = 5$

Good Pivot = $\frac{5}{9} \approx 5/9 \approx 7/9$

Yes, At least half of 4 are good pivots.

3.

3

Good cases when pivot divides the array into reasonably balanced ~~arrays~~ halves.

Best case is when pivot divides the array into two equal halves.

Good case is not the base case in Quicksort but they do have similar Time Complexity.

lets take an Array with n elements and
Suppose ~~to~~ the pivot divides the Array into equal halves in every levels.

work = partition = n

work = $n/2 + n/2 = n$

work = $n/4 + n/4 + n/4 + n/4 = n$

work = $1 + 1 + 1 + \dots + 1 = n$

Time Complexity = # of levels * work
 $= (\log_2 n) * O(n)$
 $= O(n \log_2 n)$

4.

```

class Solution {
    public static int quickSortedIndex(int[] arr, int s, int e){
        int pivot = arr[e];
        int pos = s;
        for(int i=s;i<e;i++){
            if(arr[i] < pivot){
                if(pos != i){
                    int temp = arr[pos];
                    arr[pos] = arr[i];
                    arr[i] = temp;
                }
                pos++;
            }
        }
        arr[e] = arr[pos];
        arr[pos] = pivot;
        return pos;
    }

    public int findKthLargest(int[] nums, int k) {
        int position = nums.length - k;
        int start = 0;
        int end = nums.length - 1;
        while(start < end){ // element in position or index is the of the correct order
            int cursor = quickSortedIndex(nums,start,end);
            if(cursor==position){
                break;
            }
            if(position < cursor){
                end = cursor - 1;
            }else{
                start = cursor + 1;
            }
        }
        return nums[position];
    }
}

```