

Mixture Models for Community Detection

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Quelques remarques:

- hésitez pas à utiliser Zotero pour exporter d'éventuelles références bibliographiques, histoire d'avoir un remplissage uniforme et de gagner du temps
- Une fois une abbréviation introduite (ex: SBM), si possible toujours utiliser l'abbréviation et ne pas ré-écrire l'expression entière
- Je propose de préférer le terme de "cluster" à "community". (Il faudra que je change ce que j'ai écrit du coup)

Contribution Statement

TODO

1. Introduction

Community detection is the problem of revealing communities within a graph, also referred to as “graph clustering” [3], where a community within a graph is often defined as a set of nodes that are more densely connected between them than with the rest of the network. Among existing methods to tackle this problem, model-based methods fit a mathematical model capable of explaining the observed connectivity, and from which descriptive properties of a graph maybe extracted or computed. The Stochastic Block Model (SBM) is a renowned example of graph modelling. In [2], J.-J. Daudin *et al.* explore this model from a frequentist point of view and propose a variational EM algorithm to fit this model. In this report, we quickly review some literature on community detection in Section 2. In Section 3, we detail the method introduced in [2] as well as a variant from the literature and discuss the problem of overlapping communities. In Sections 4 and 5, our experiments are presented and discussed. Lastly, we conclude in Section 6.

2. Context and Related Work

2.1 What is Community Detection?

Community Detection has tremendous applications in the study of real networks such as social [1] or biological [4] networks. This problem is of importance to perform a mesoscopic study of graphs, where communities can be interpreted as meta-nodes that reveal new interactions associated to possibly interpretable functions within a complex system represented as a graph.

Although the definition of a “community” remains somewhat sloppy in the literature, a common definition describes it as a group of nodes with an internal density (defined as

the ratio of edges between nodes of the group that are actually present over the number of such possible edges) that is larger than its inter-community density (similarly defined, but between nodes of the group and nodes outside the group). This definition is actually specific to homophilious communities, which we will focus on, while heterophily would take an opposite definition.

2.2 Common community detection approaches

Community detection is an NP-hard problem, as testing all possible partitions of a graph has complexity $\mathcal{O}(2^n)$ with n the number of nodes. Instead, common approaches [...]

[Mention types of methods, but focus on model-based approaches]

2.3 A word on overlapping community detection approaches

3. Proposed method

[2]

3.1 A mixture model for random graphs

[Introduire le modèle]

3.2 Variational Expectation-Maximization algorithm

[Présenter le VEM avec la méthode de point fixe]

3.3 A variant

[Sofiane: présenter la variante]

3.4 Addressing overlapping clusters

4. Experiments

4.1 Implementation

4.2 Testing on SBM datasets

4.2.1 FITTING A MODEL

4.2.2 INITIALIZATION SENSITIVITY

4.3 Comparison to variants

4.3.1 DATASETS

4.3.2 EVALUATION METRICS

4.3.3 RESULTS

5. Analysis and discussion

TODO

6. Conclusion

TODO

Acknowledgments

Est-ce qu'on en met ?

Appendix A. plots

[...]

References

- [1] P. Chunaev. Community detection in node-attributed social networks: A survey. *Computer Science Review*, 37:100286, Aug. 2020.
- [2] J.-J. Daudin, F. Picard, and S. Robin. A mixture model for random graphs. *Statistics and Computing*, 18(2):173–183, June 2008.
- [3] S. Fortunato. Community detection in graphs. *Physics Reports*, 486(3-5):75–174, Feb. 2010.
- [4] P. Sah, L. O. Singh, A. Clauset, and S. Bansal. Exploring community structure in biological networks with random graphs. *BMC Bioinformatics*, 15(1):220, June 2014.