

# Asymptotic Notation Simplified

For two functions,  $f$  and  $g$ , ...

$$f = O(g) \iff "f \leq g"$$

..." $f$  is 'big oh' of  $g$ " means the growth rate of  $f$  is less than or equal to the growth rate of  $g$ .  
Said differently, it means  $f$  is eventually always smaller than or within a constant multiple of  $g$ .

$$f = \Omega(g) \iff "f \geq g"$$

..." $f$  is 'big omega' of  $g$ " means the growth rate of  $f$  is greater than or equal to the growth rate of  $g$ .  
Said differently, it means  $f$  is eventually always larger than or within a constant multiple of  $g$ .

$$f = \Theta(g) \iff "f \approx g"$$

..." $f$  is 'big theta' of  $g$ " means  $f$  is in "big oh" *and* "big omega" of  $g$ , which means  $f$  and  $g$  have the same growth rate. Said differently, it means  $f$  is eventually always within a constant multiple of  $g$ .

$$f = o(g) \iff "f < g"$$

..." $f$  is 'little oh' of  $g$ " means the growth rate of  $f$  is strictly less than the growth rate of  $g$ .  
Said differently, it means  $f$  is eventually always smaller than  $g$ , even considering constant multiples.

$$f = \omega(g) \iff "f > g"$$

..." $f$  is 'little omega' of  $g$ " means the growth rate of  $f$  is strictly greater than the growth rate of  $g$ .  
Said differently, it means  $f$  is eventually always larger than  $g$ , even considering constant multiples.

There's no "little theta" notation that combines "little oh" *and* "little omega" because  $f$  cannot be both less than *and* greater than  $g$ . In other words, "little theta" of anything would be the empty set.

Don't fuss the format. All the variants below are used interchangeably for all 5 symbols:

$$f = O(g), f \in O(g), f(x) = O(g(x)), f \text{ is } O(g), f \text{ is in } O(g)$$