

When  $t = 1$  we want:

$$A_0 \cdot e^{-\frac{d}{2} \cdot t} \leq \epsilon$$

Which is equal to:

$$A_0 \cdot e^{-\frac{d}{2}} \leq \epsilon$$

Divide by  $A_0$  (positive number):

$$e^{-\frac{d}{2}} \leq \frac{\epsilon}{A_0}$$

Take the log:

$$-\frac{d}{2} \leq \log \frac{\epsilon}{A_0}$$

Multiply by -2:

$$d \geq -2 \cdot \log \frac{\epsilon}{A_0}$$

Therefore our dampen factor must be at least  $-2 \cdot \log \frac{\epsilon}{A_0}$ . However if we plug that into the exponential decay function  $N_0 \cdot e^{-\lambda \cdot t}$  we get:

$$A_0 \cdot e^{-2 \cdot \log(\frac{\epsilon}{A_0}) \cdot -\frac{1}{2} \cdot t}$$

Which simplifies to:

$$A_0 \cdot e^{\log(\frac{\epsilon}{A_0}) \cdot t}$$

Put  $t$  into the log-function:

$$A_0 \cdot e^{\log((\frac{\epsilon}{A_0})^t)}$$

$e$  to the power of some log is always the same as the value itself:

$$A_0 \cdot (\frac{\epsilon}{A_0})^t$$

And that is what is used in the code!