

# Lock-free by Example

(one very complicated example)

Tony Van Eerd  
C++Now, 2015

# Guide to Threaded Coding

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Use Locks

# Guide to Threaded Coding

1. Forget what you learned in Kindergarten  
*(ie stop Sharing)*
  2. Use Locks
  3. Measure
  4. Measure
  5. Change your Algorithm
  6. GOTO 1
- ∞. Lock-free

***Lock-free coding is the last thing you want to do.***

# Guide to Threaded Coding

1. Forget what you learned in Kindergarten  
*(ie stop Sharing)*

2. Use Locks
3. Measure
4. Measure
5. Change your Algorithm
6. GOTO 1

∞. **Lock-free**

∞+1. **Measure. Measure.**

***Lock-free coding is the last thing you want to do.***

# Guide to Threaded Coding

Don't Share  
Use Locks

# NOTE:

CAS = compare\_exchange (\_weak or \_strong)



# NOTE:

CAS = compare\_exchange

Not my coding style/structure

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CAS = compare\_exchange

Not my coding style/structure

Remember to lower the audience's expectations:

# NOTE:

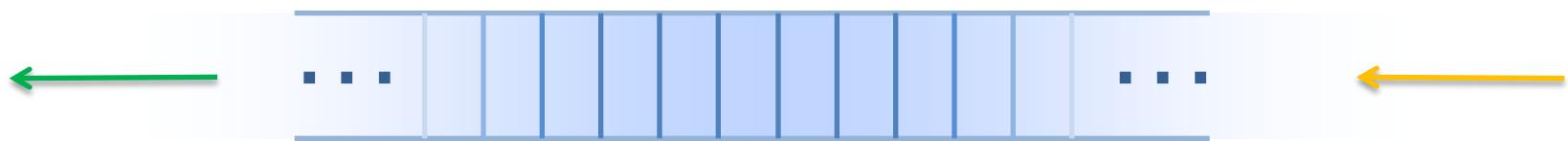
CAS = compare\_exchange

Not my coding style/structure

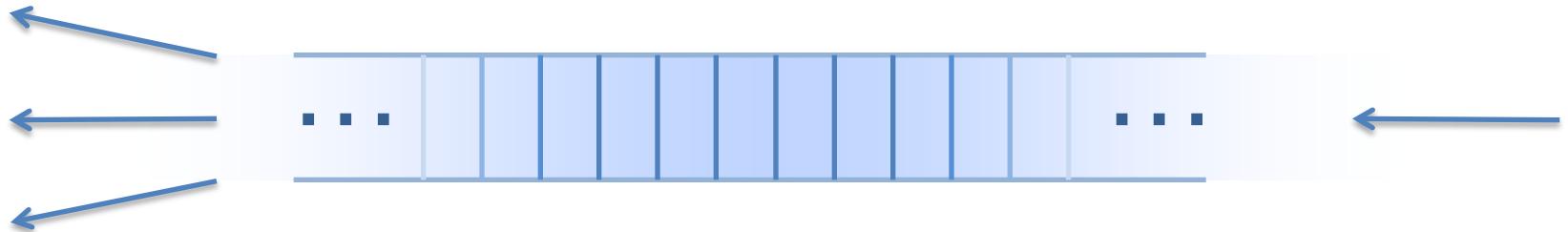
Remember to lower the audience's expectations:

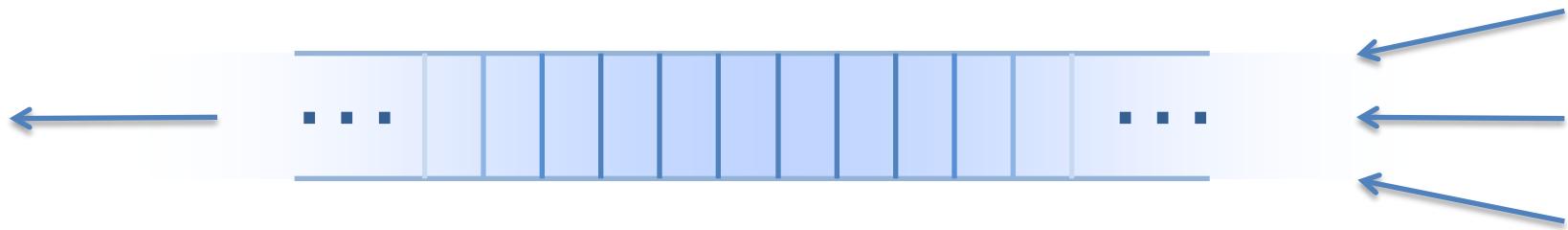
I'm not an expert.

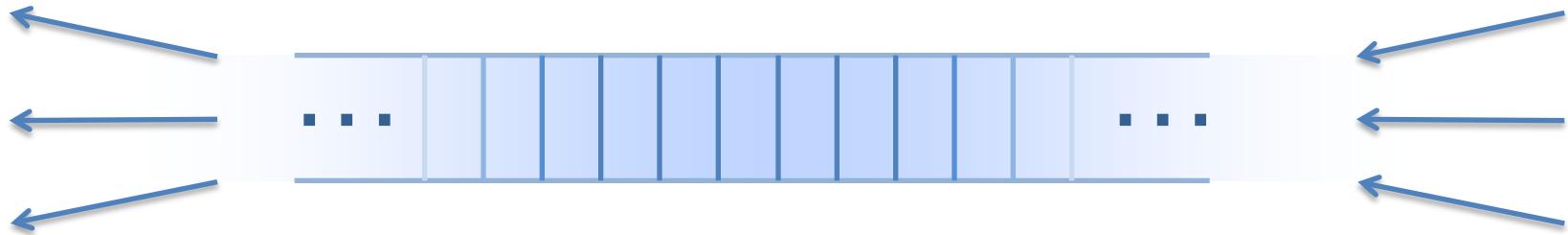




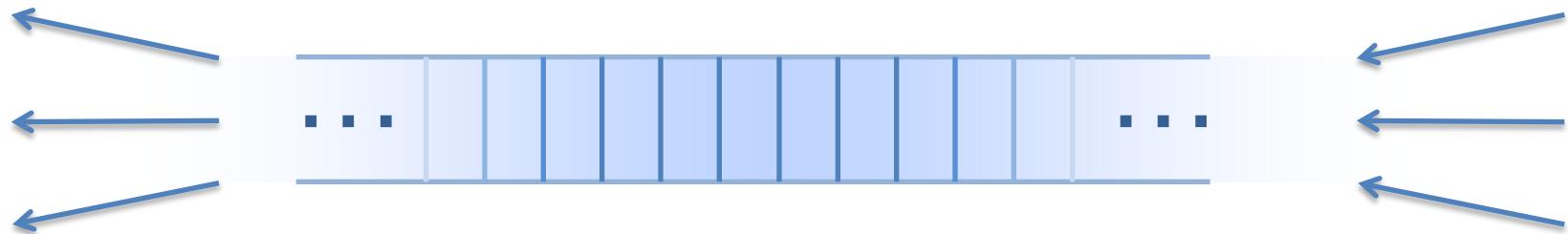




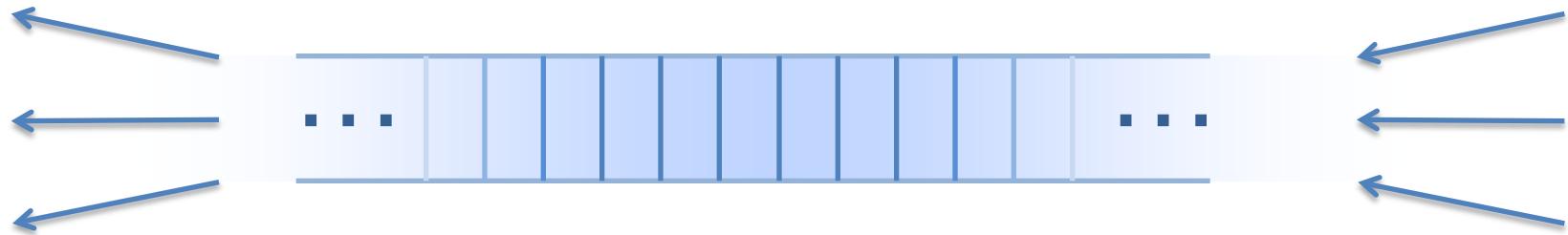




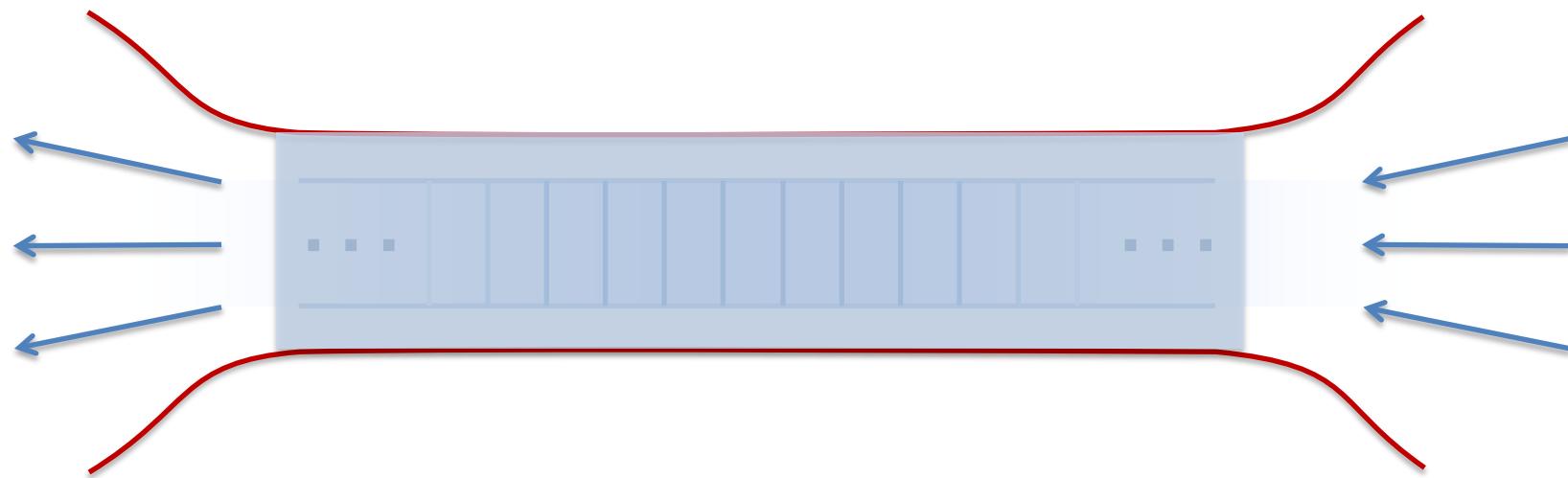
# Multi-Producer Multi-Consumer Queue



# MPMC Queue

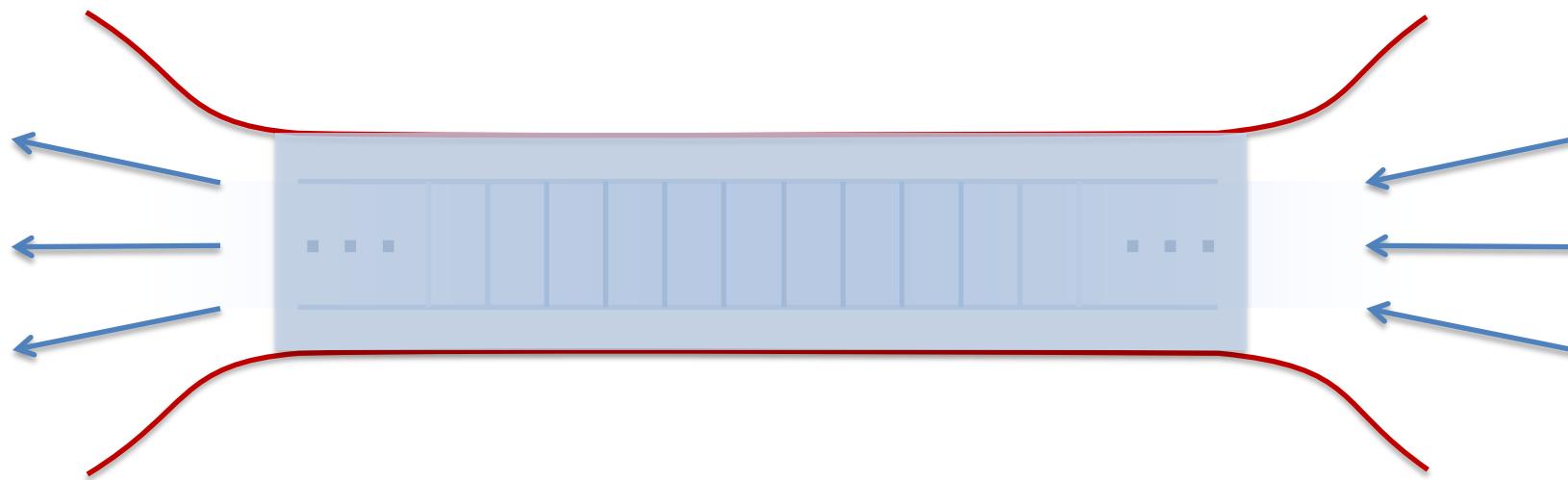


# MPMC Queue

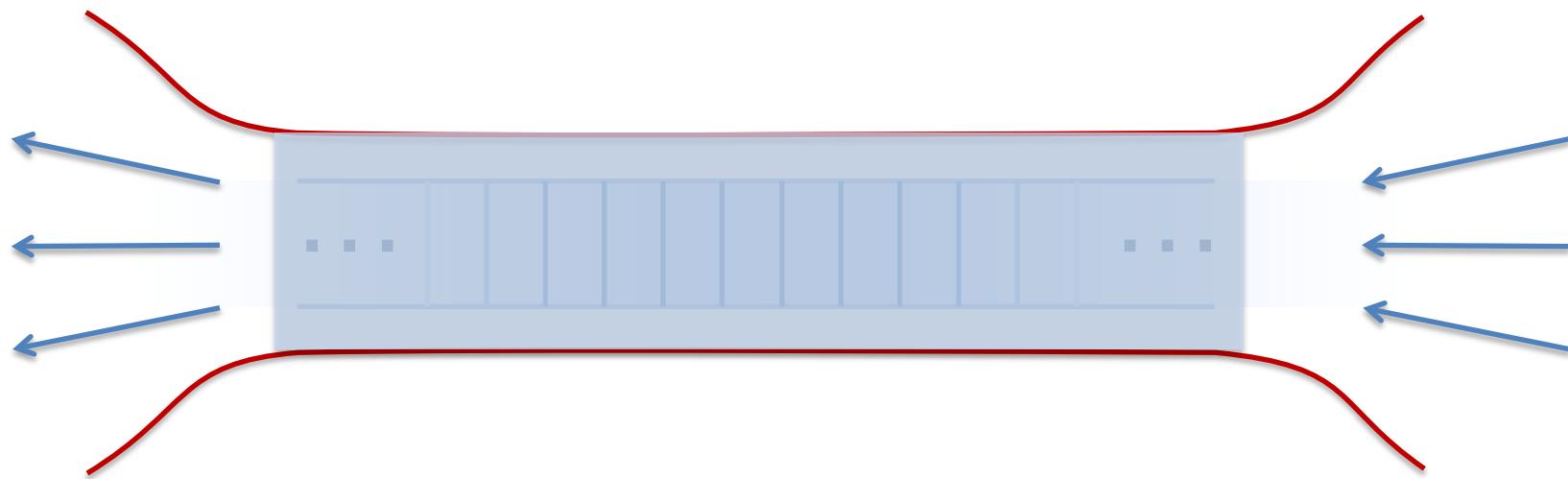


# MPMC Queue

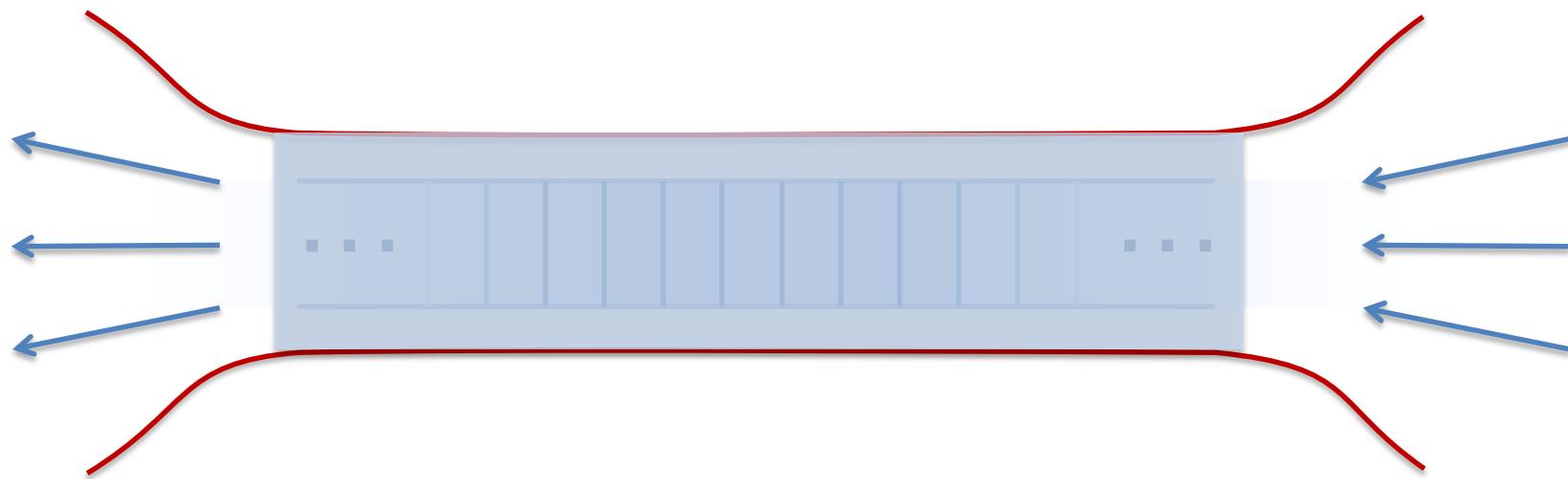
SPSC  
SPMC  
MPSC  
MPMC

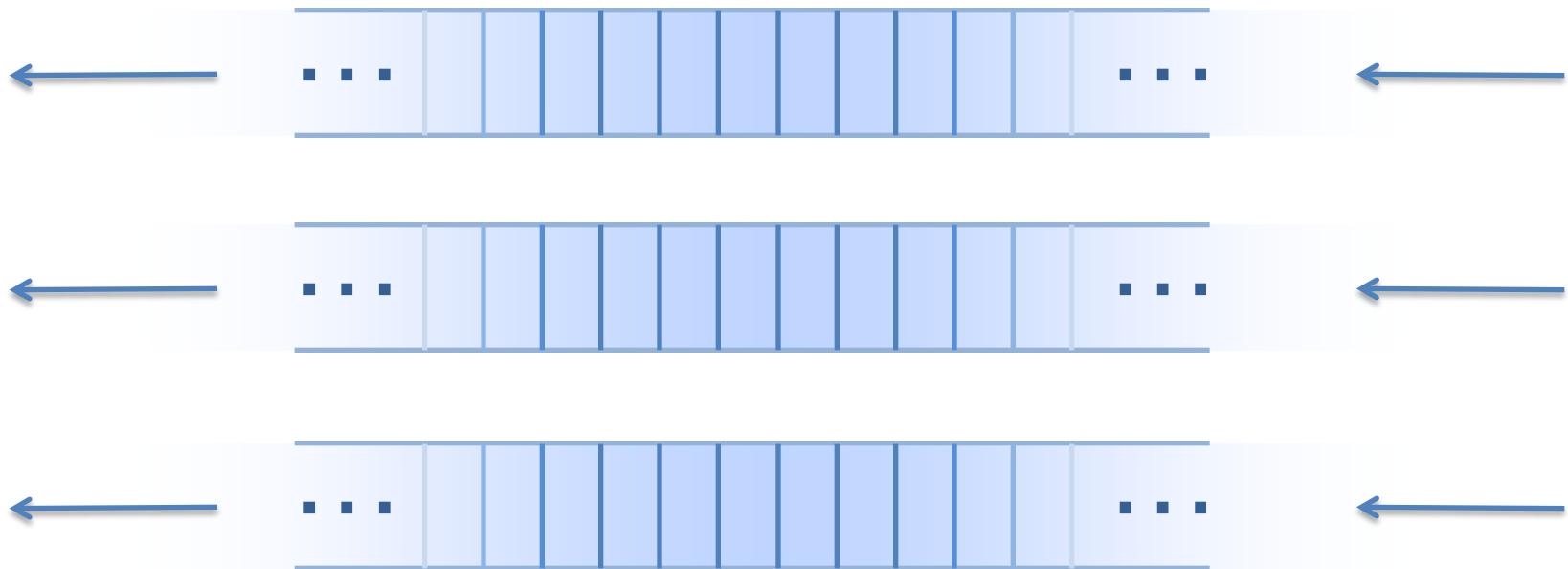


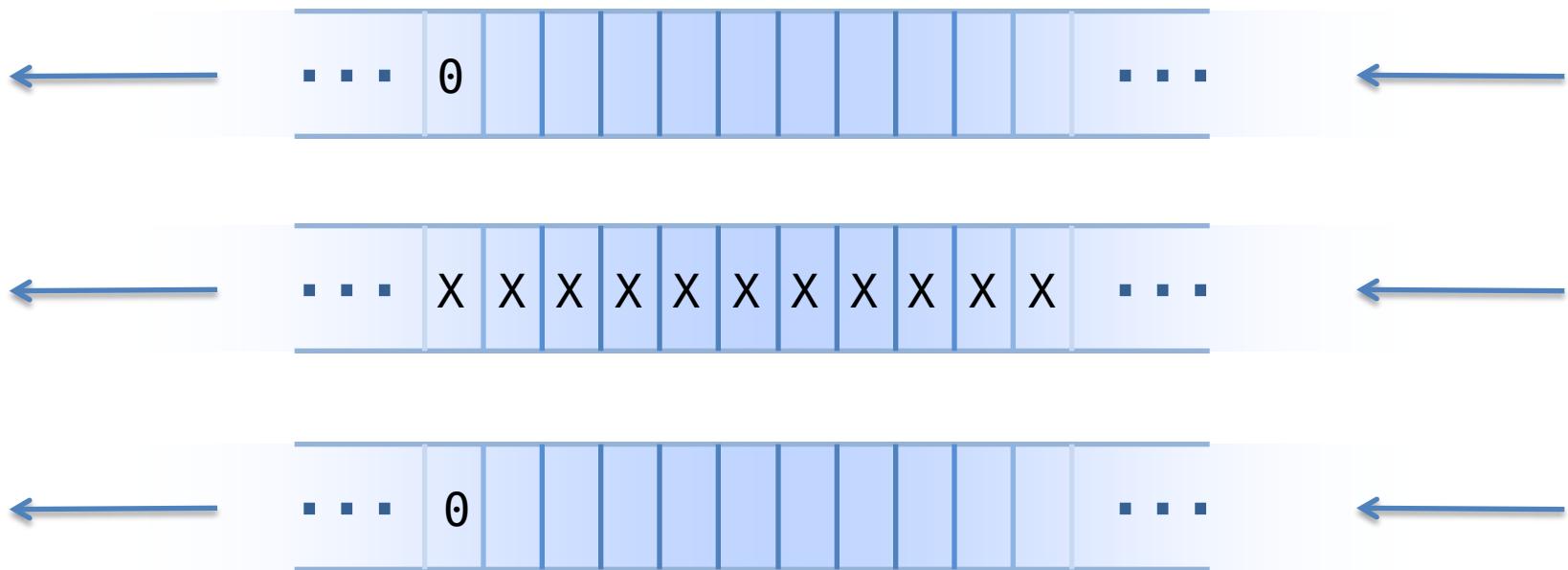
# MPMC Queue



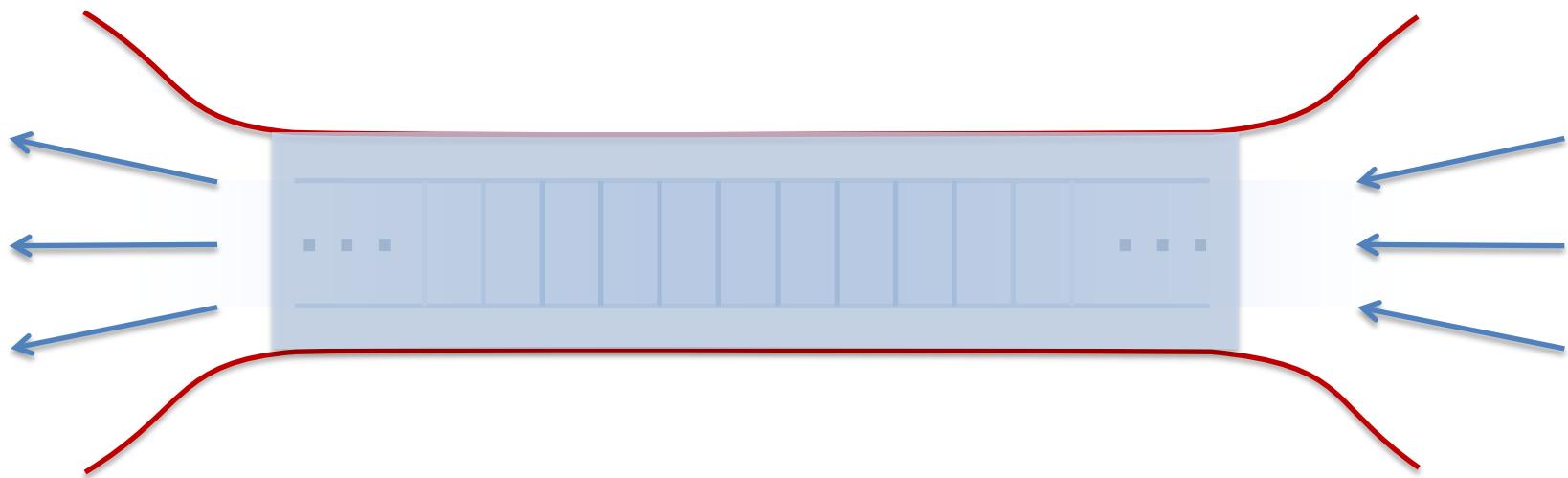
# Bottleneck

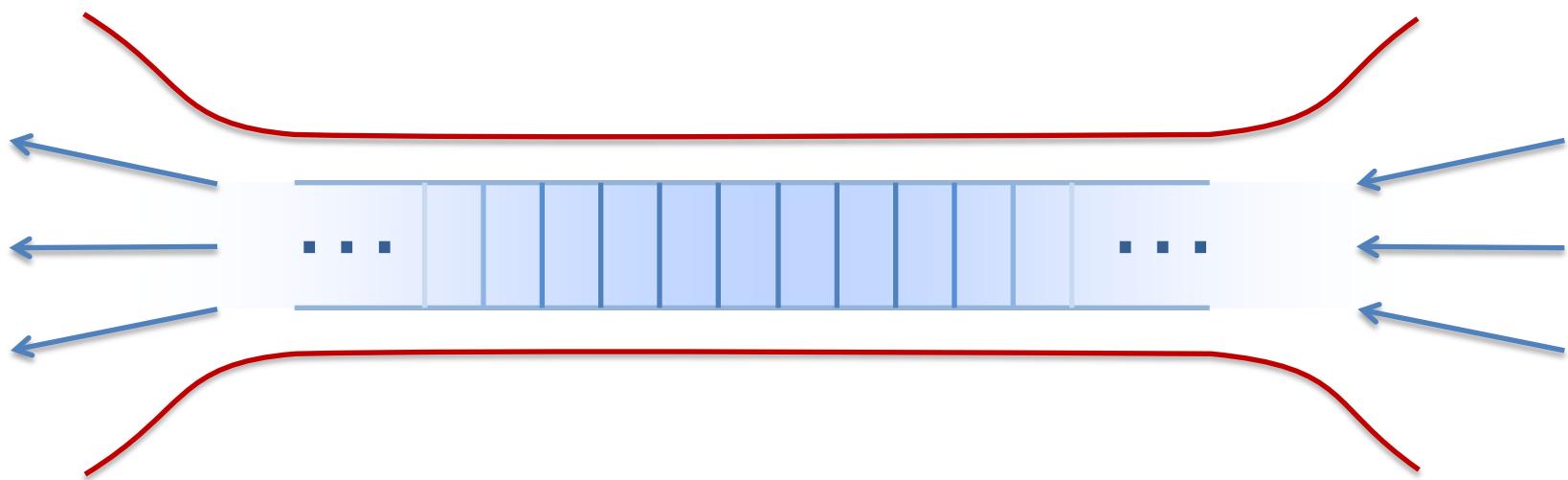


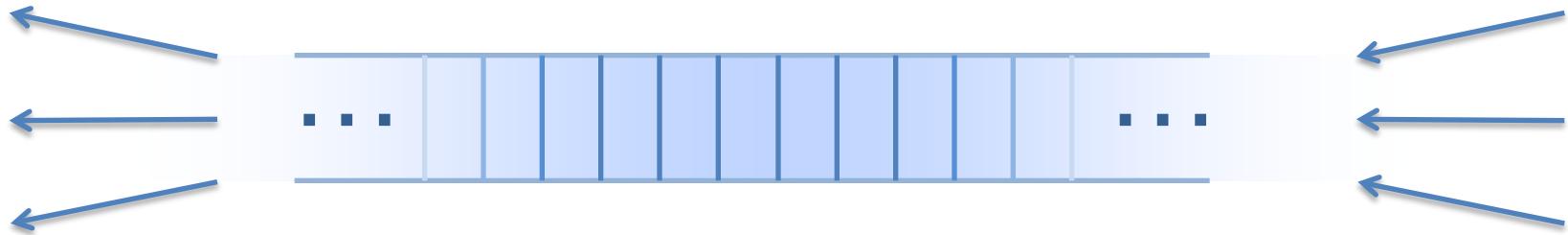


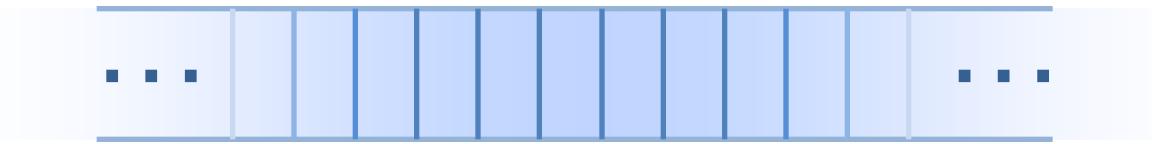


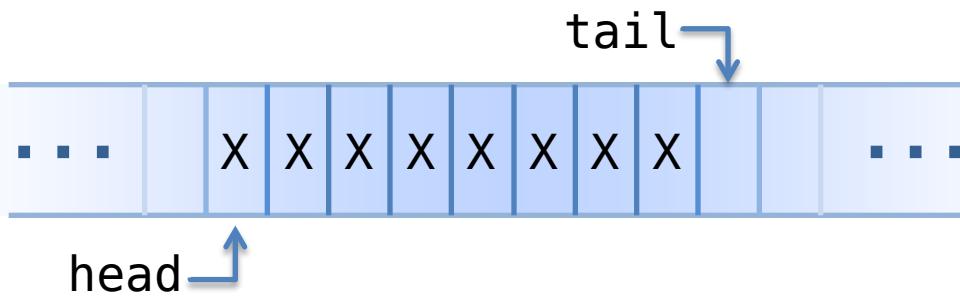






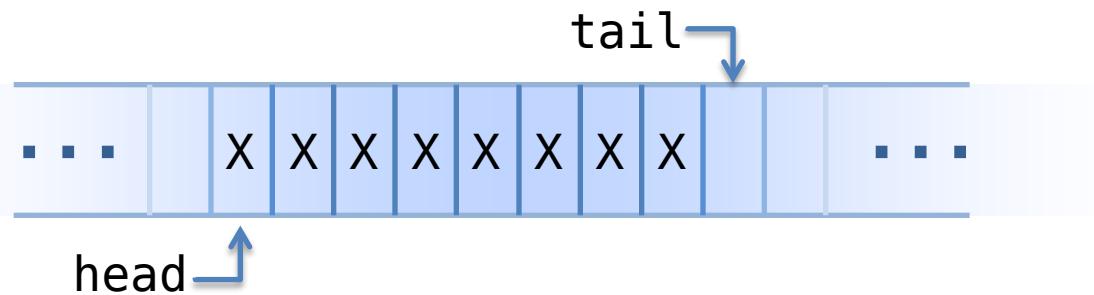






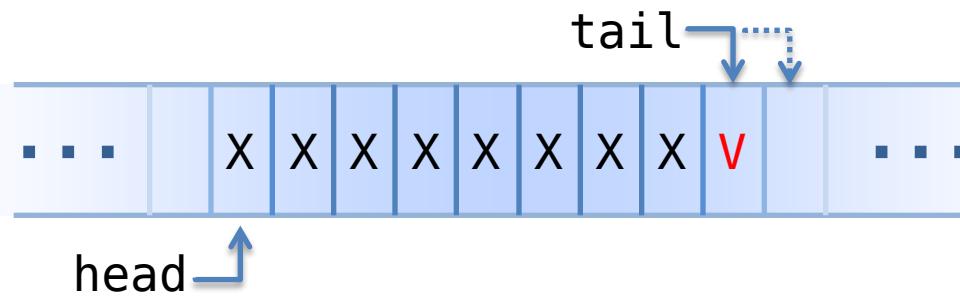


```
class Queue
{
    int buffer[some_size];
    size_t head;
    size_t tail;
};
```



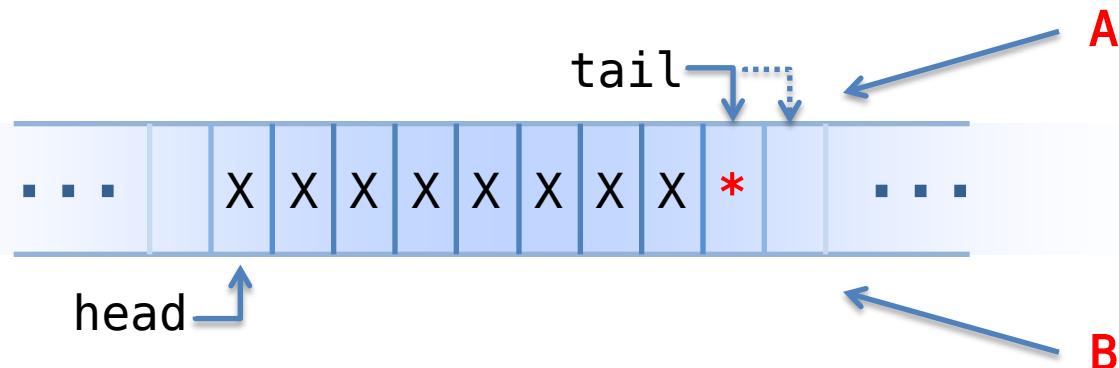


```
void push(int val)
{
    buffer[tail++] = val;
}
```





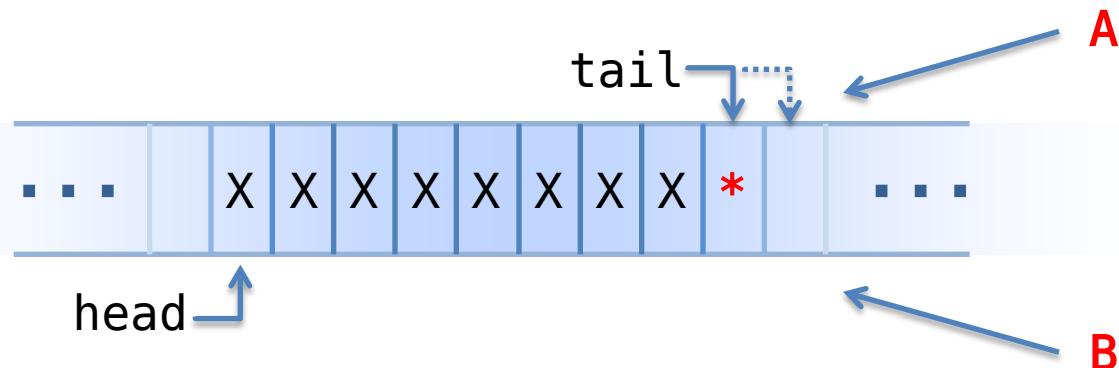
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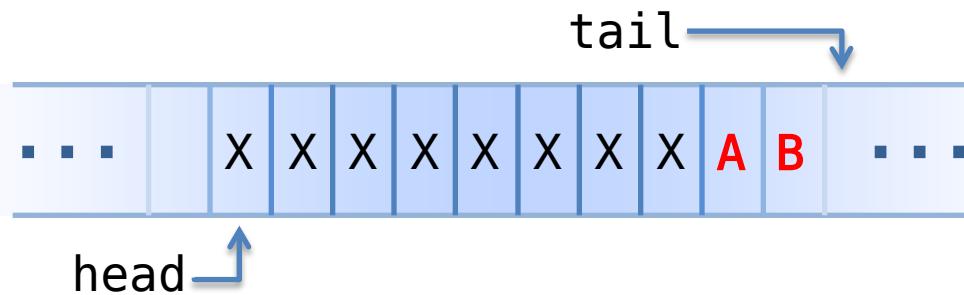


```
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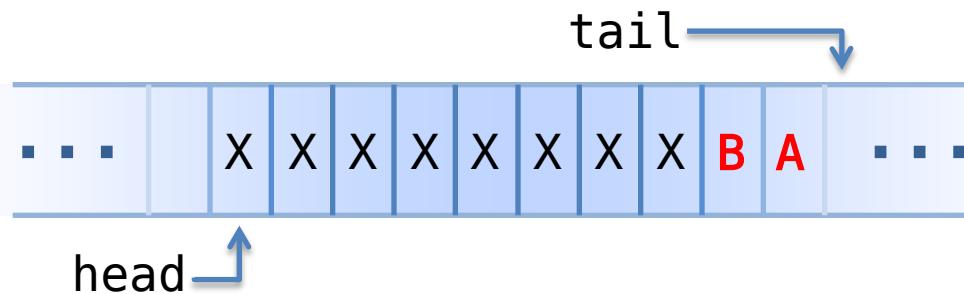
Possible Outcomes?



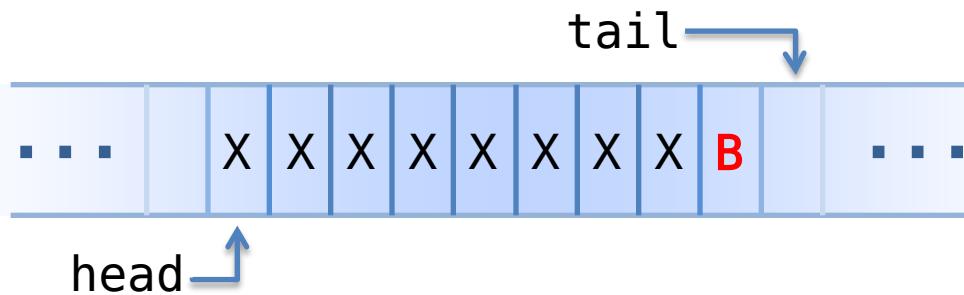
```
void push(int val)
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```



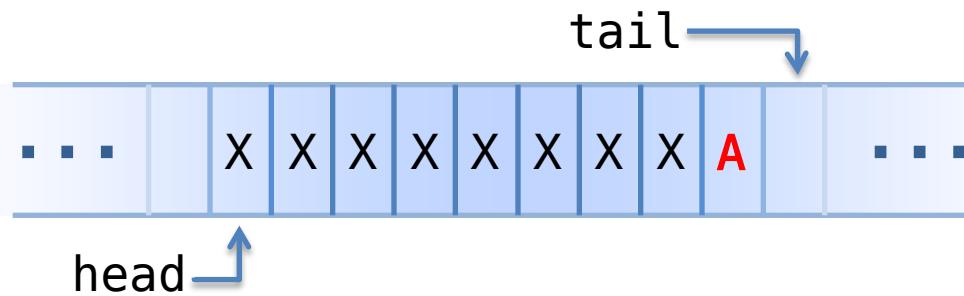
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void push(int val)
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```



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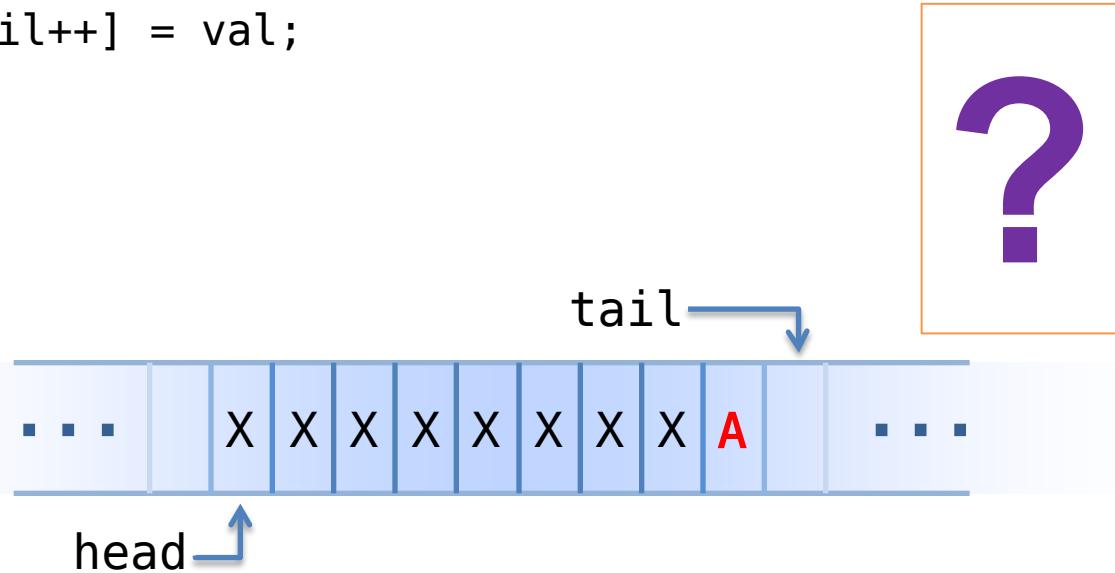


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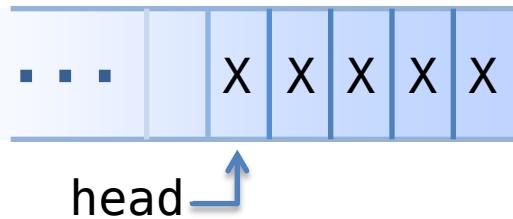


```
void push(int val)
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    buffer[tail++] = val;
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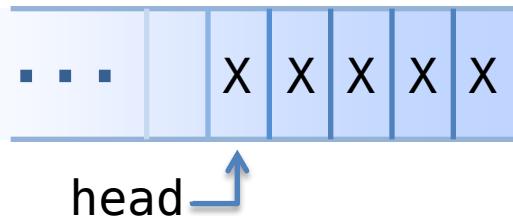


```
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    buffer[tail++] = val;
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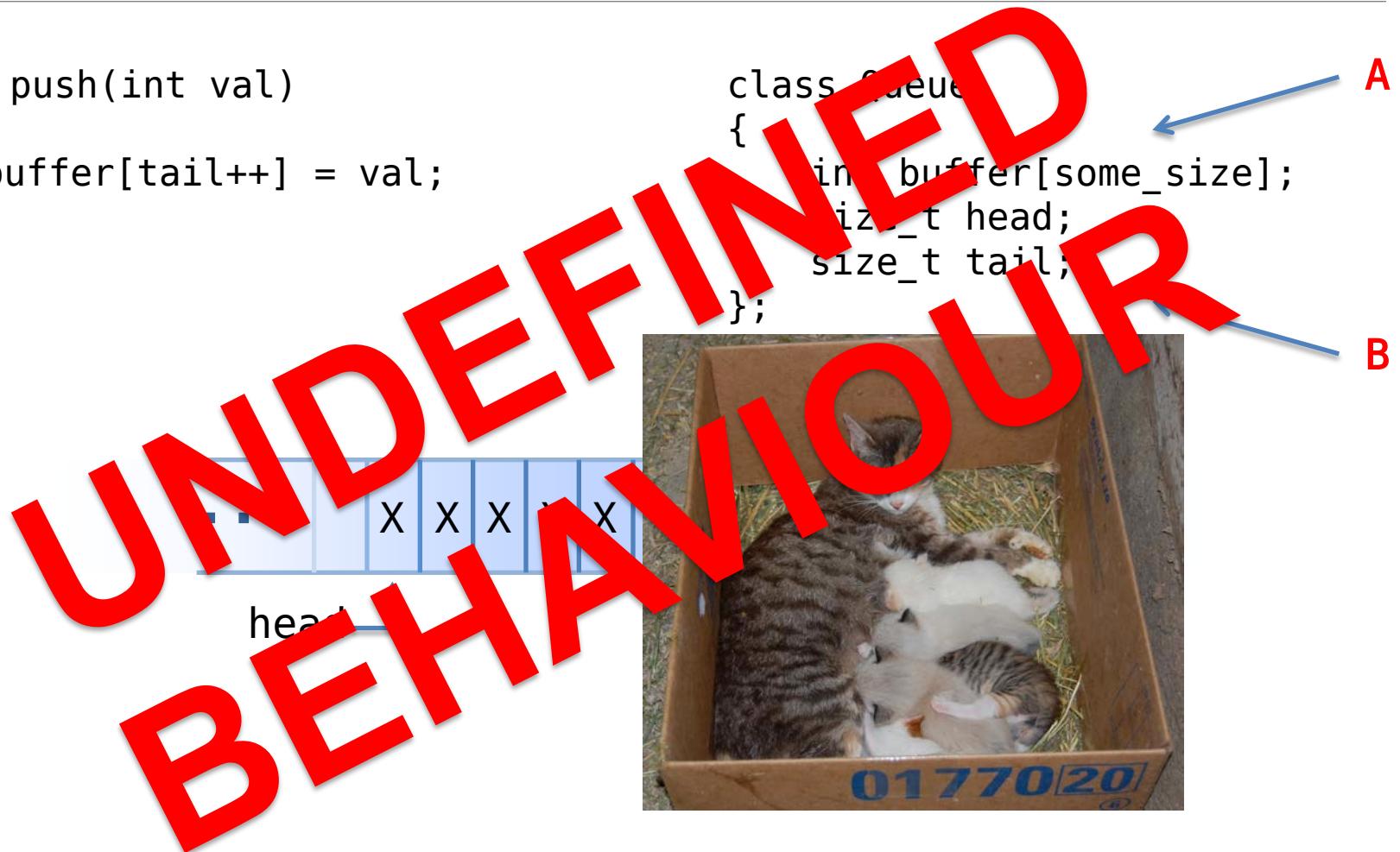
```
class Queue
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```

A  
B



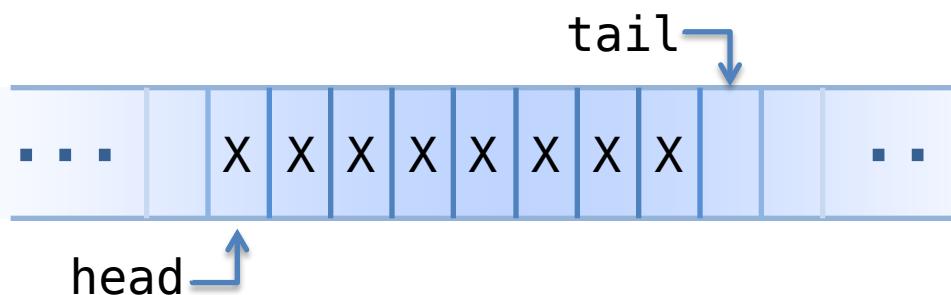
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A

B

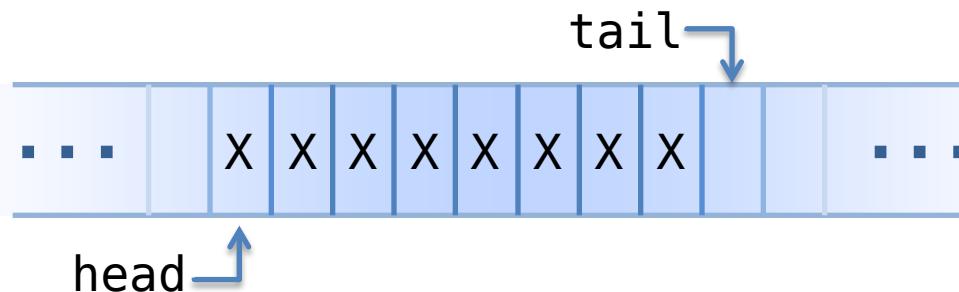


```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    atomic<int> buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

A

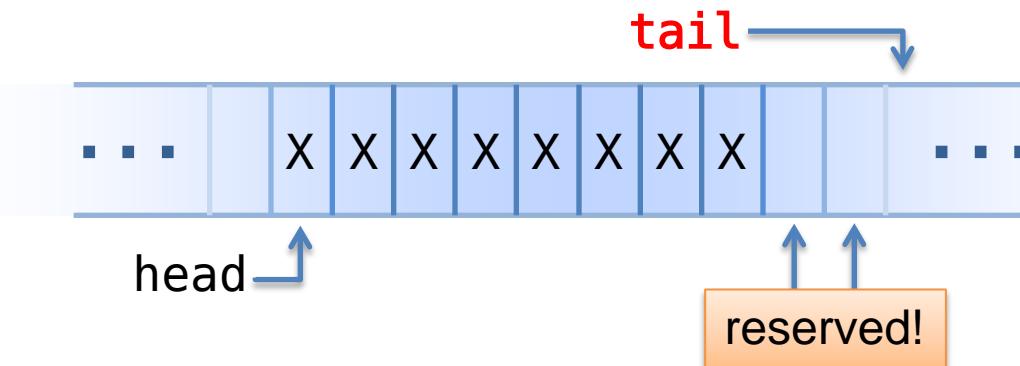
B





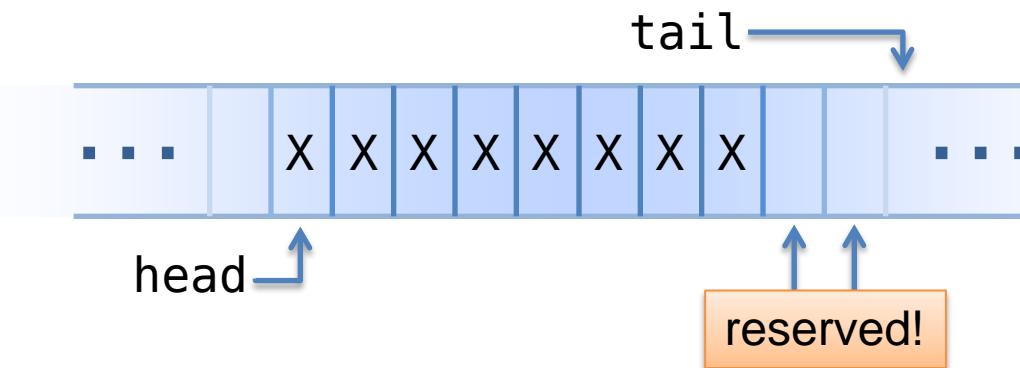
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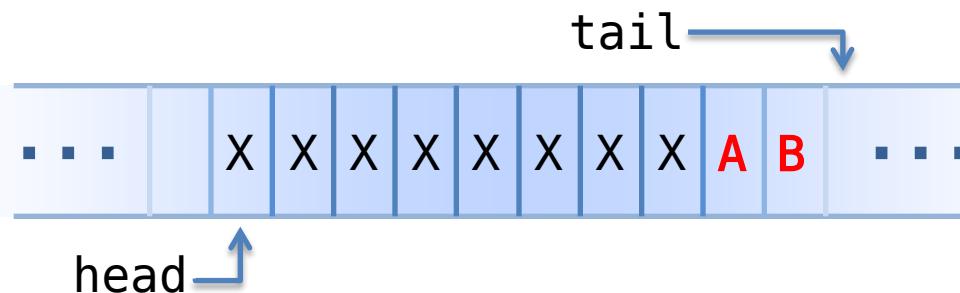
A

B



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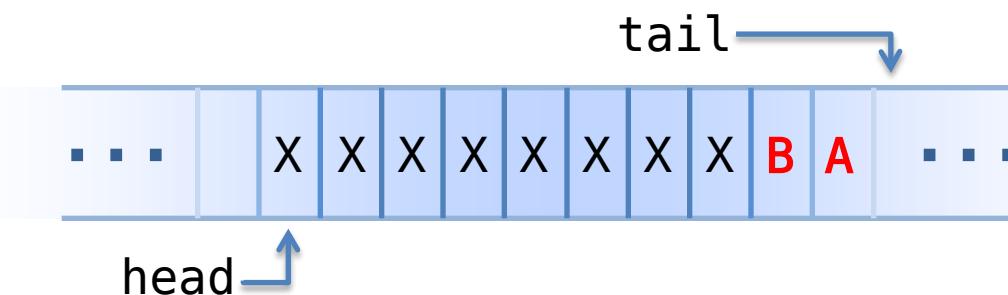


A

B

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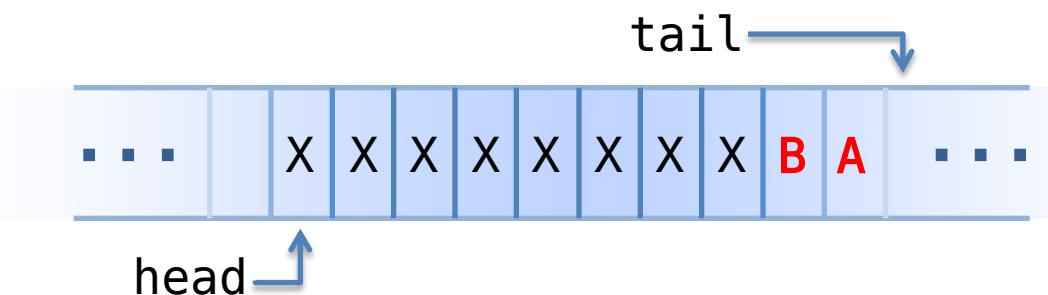
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B



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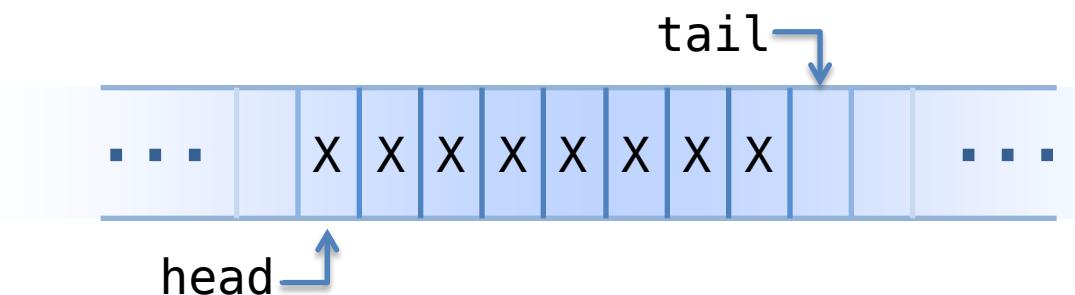


A  
B



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void push(int val)
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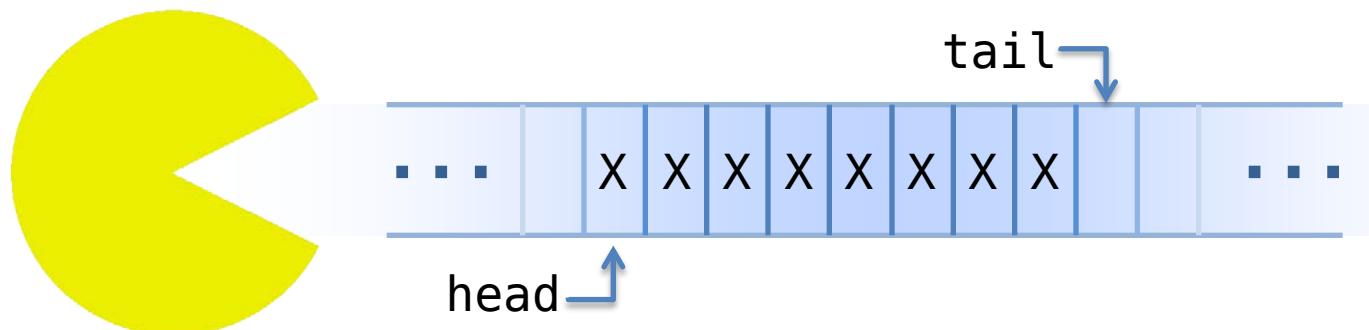
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```



A  
B

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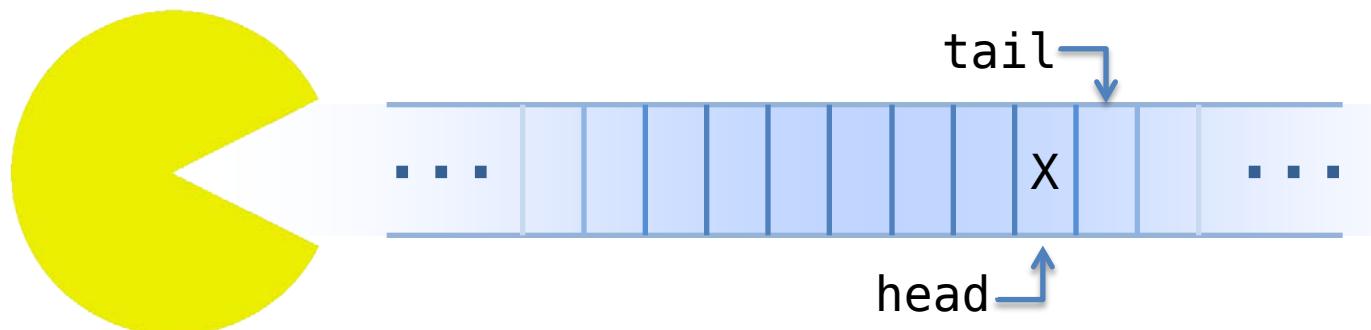


A  
B



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void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
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    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



A  
B



```
void push(int val)
{
    buffer[tail++] = val;
}
```

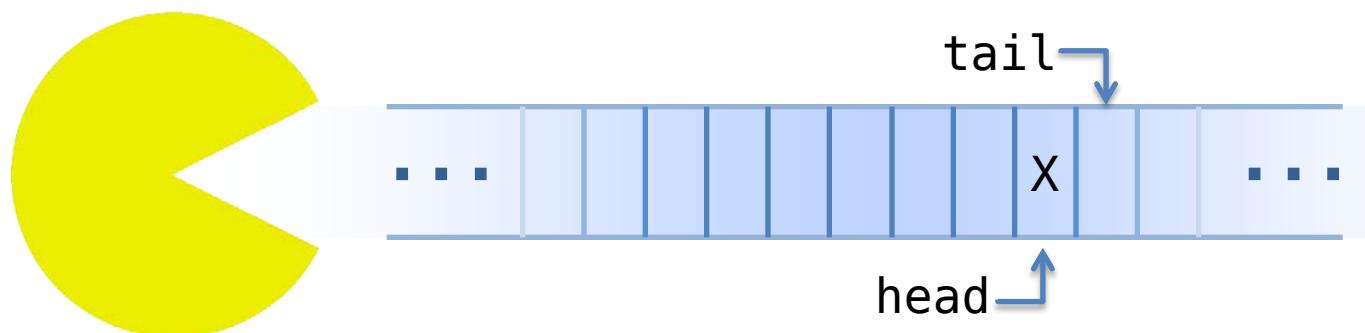
class Queue

{

```
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
```

};

X...  
A  
B





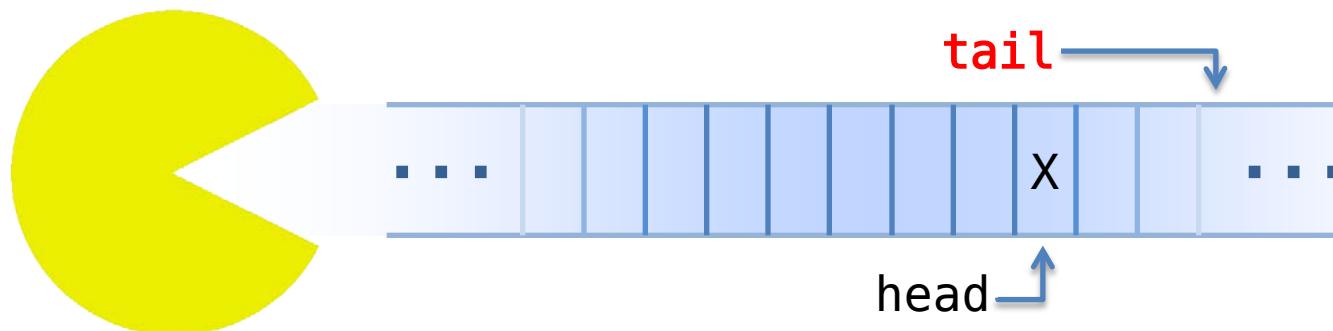
```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
```

```
{
```

```
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
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```

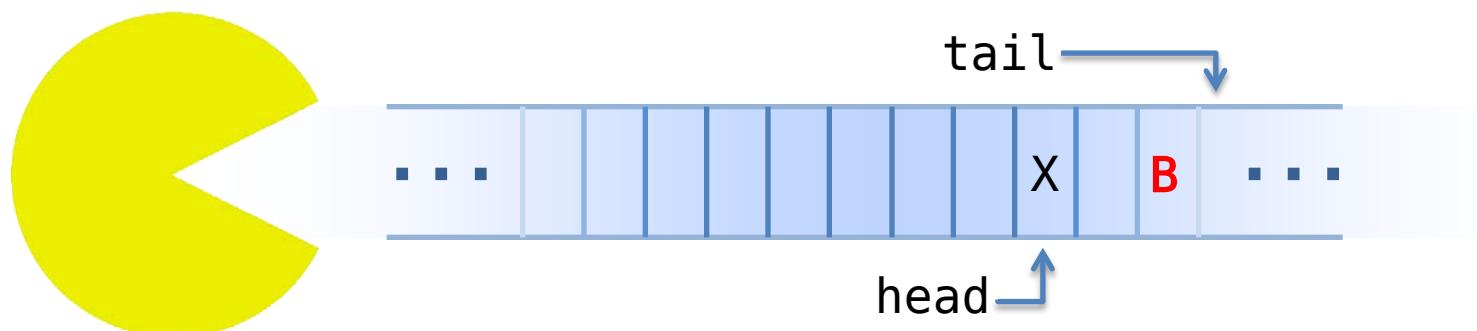
X...  
A  
B





```
void push(int val)
{
    buffer[tail++] = val;
}
```

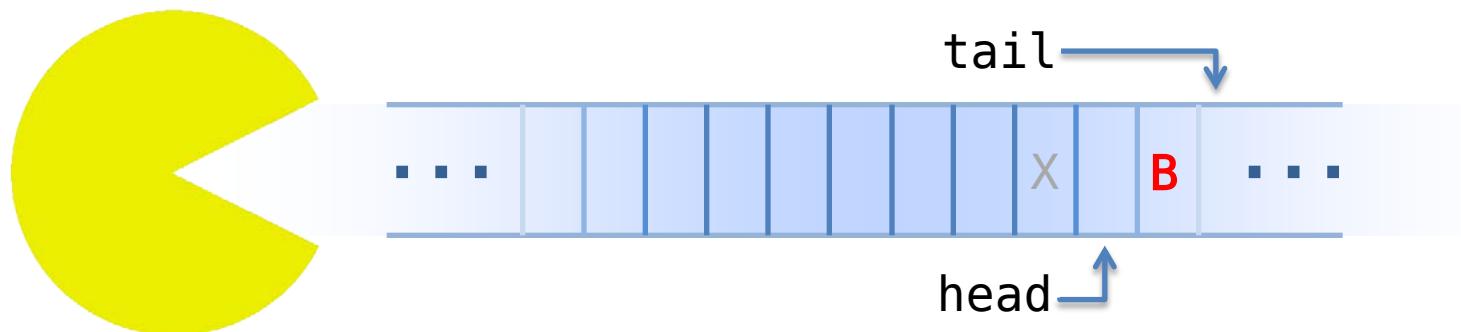
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class Queue
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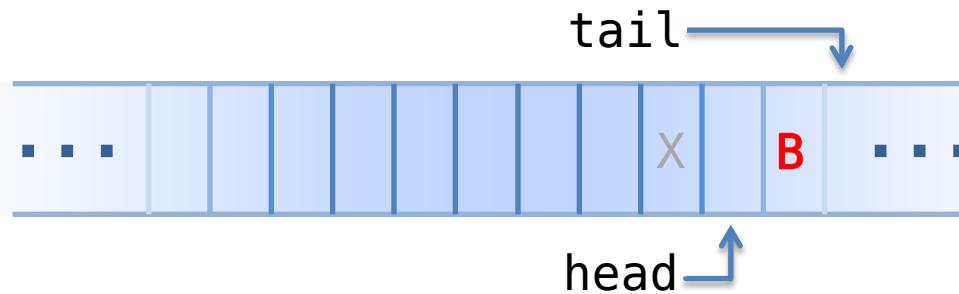
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};
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```
void push(int val)
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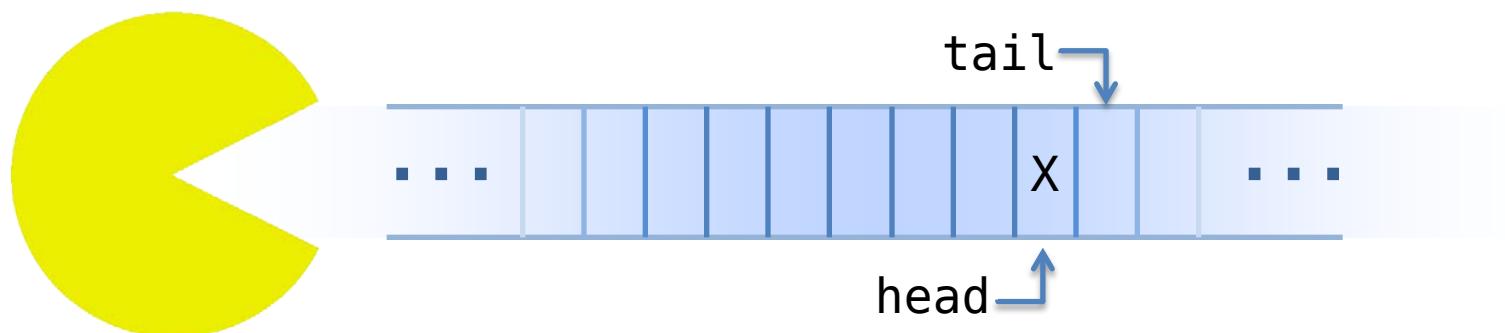




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X...

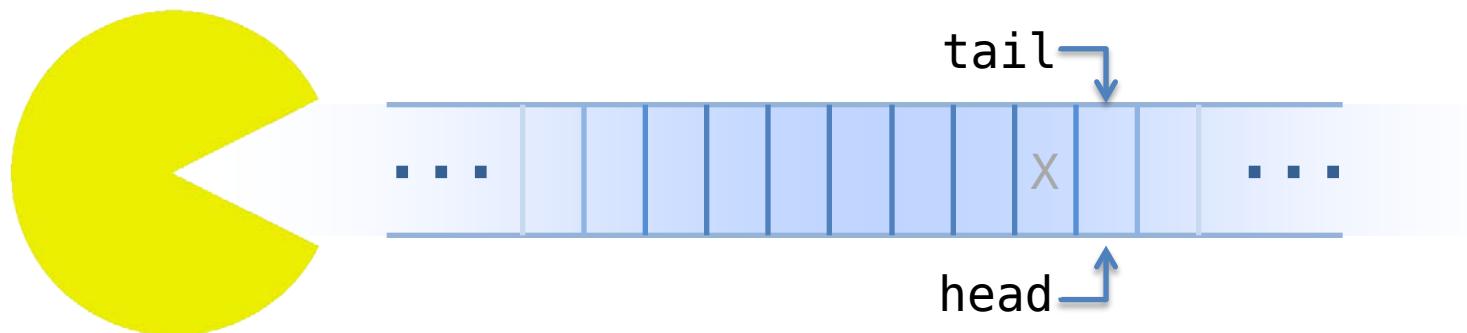




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X...

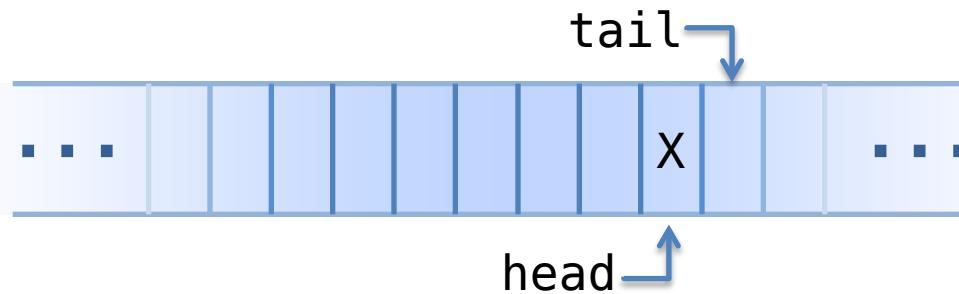
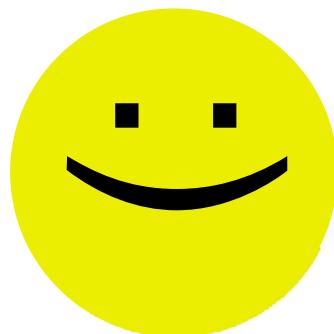




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{
    buffer[tail++] = val;
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```
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```

X...

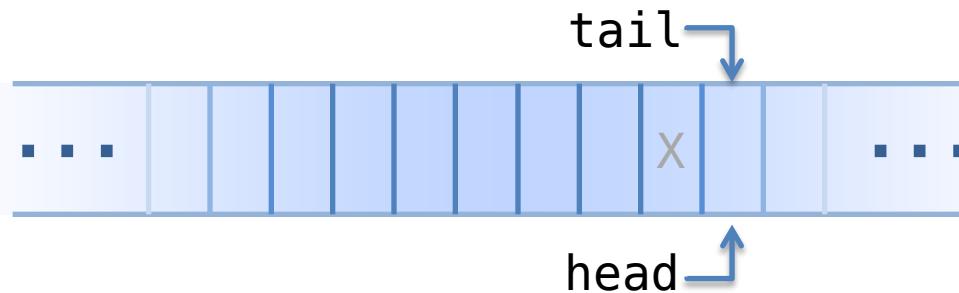




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```
class Queue
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};
```

X...

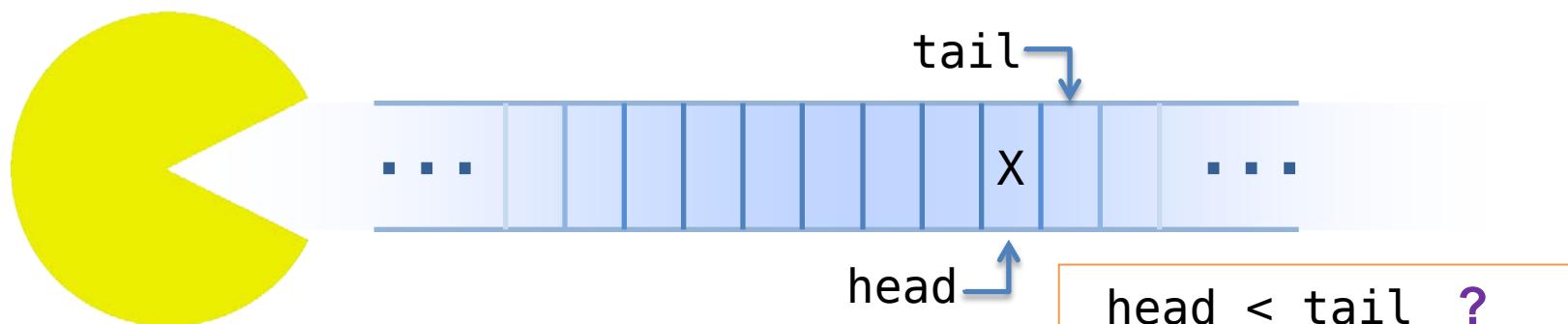




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X...

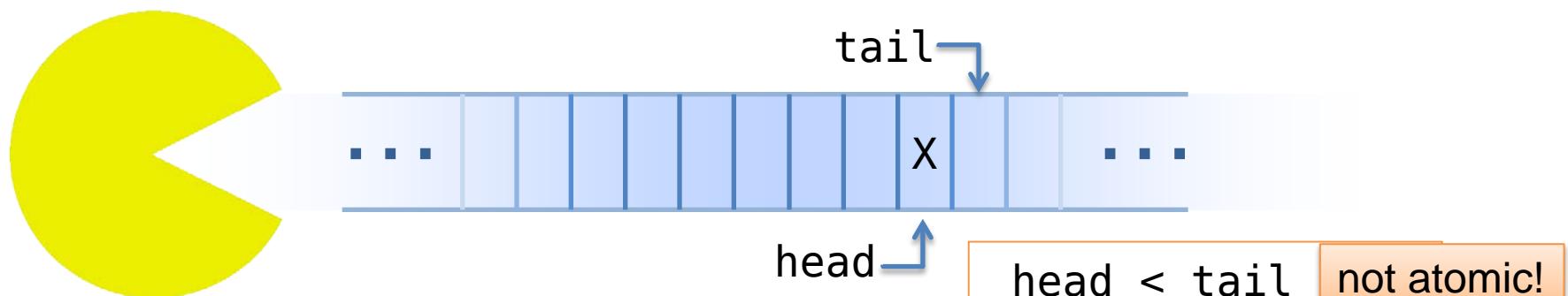




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X...



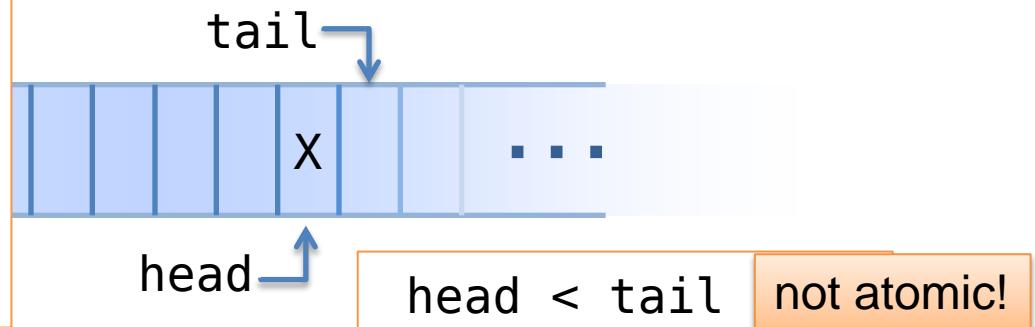


```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
if (atomic_less(head, tail))
{
    read_head();
};
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...

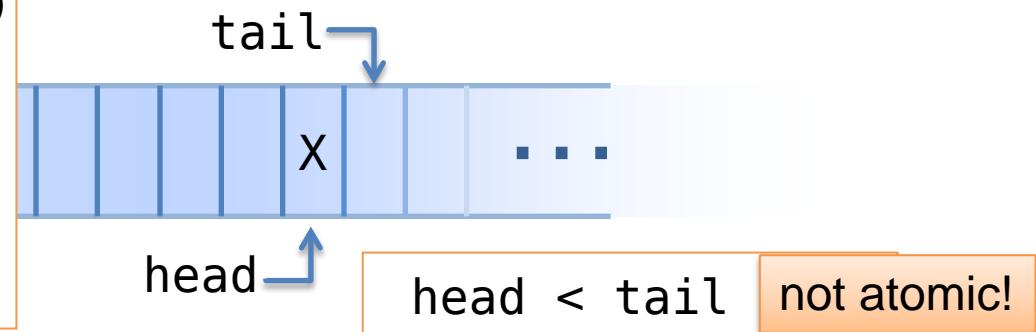




```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
if (atomic_less(head, tail))
{ THEN
    read_head();
};
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
if (atomic_less(head, tail))
{ THEN
    read_head();
}
};
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

tail

head

head < tail      not atomic!

```
void pu  
{  
buf  
}
```

```
if (atom  
{ THEN  
rea  
};
```

# THEN

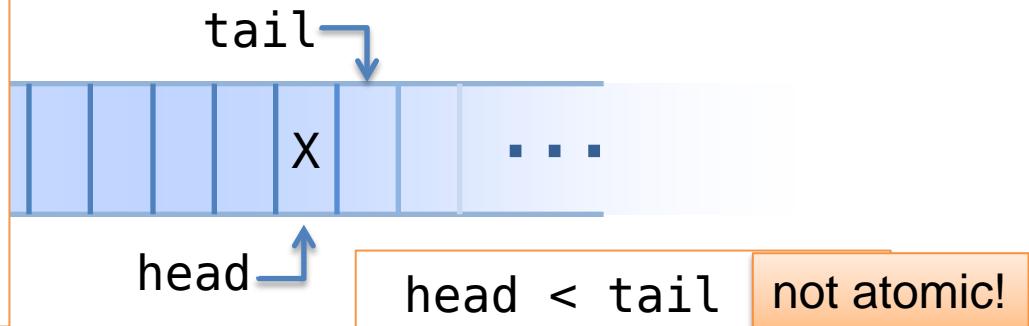
is a 4-letter word

atomic!

```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
if (atomic_less(head, tail))
{ THEN
    read_head();
};
```

```
class Queue
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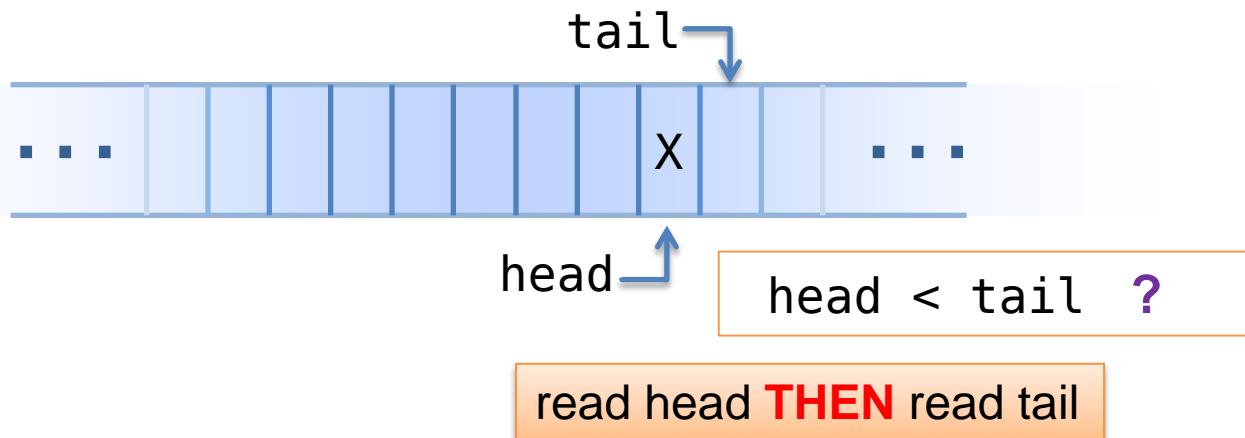




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X...

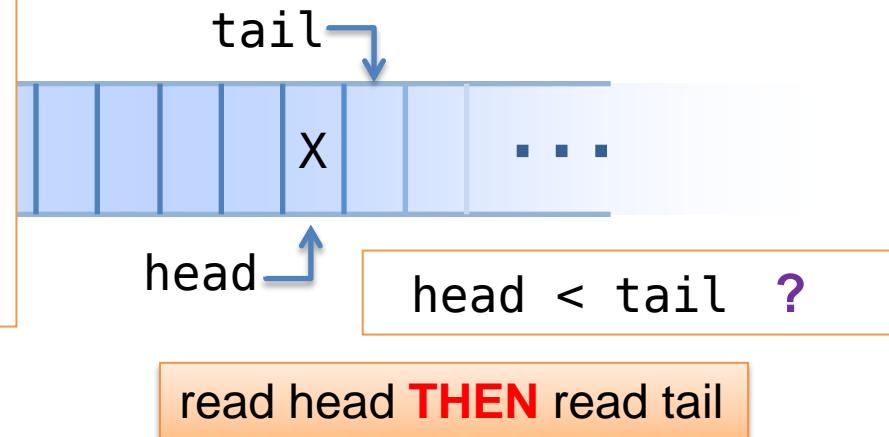




```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
statement1;
THEN
statement2;
THEN
statement3;
...
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



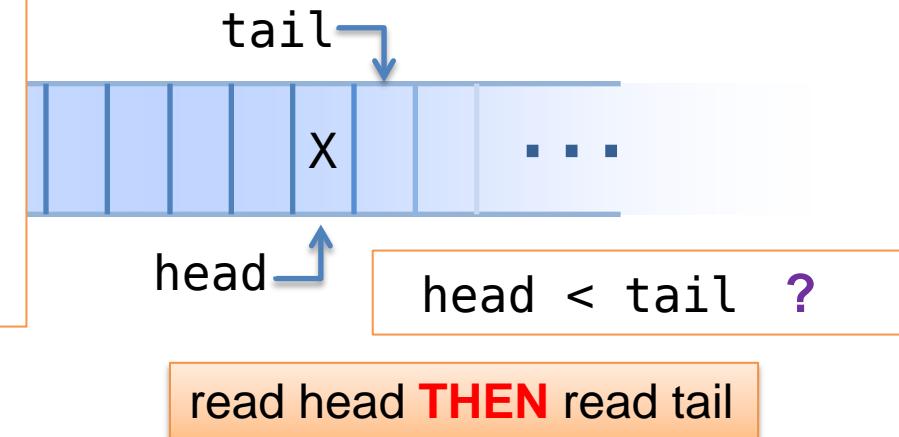


```
void push(int val)
{
    buffer[tail++] = val;
}
```

statement1;  
THEN  
statement2;  
THEN  
statement3;  
...

Local vs Shared

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



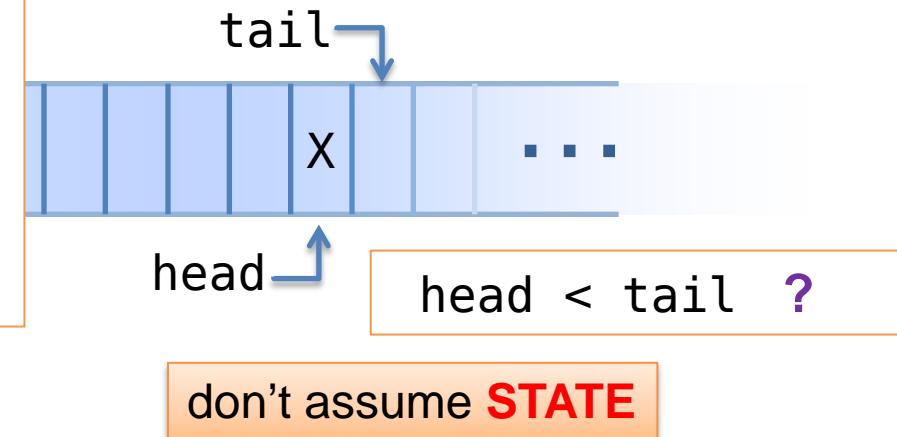


```
void push(int val)
{
    buffer[tail++] = val;
}
```

statement1;  
THEN  
statement2;  
THEN  
statement3;  
...

Local vs Shared

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

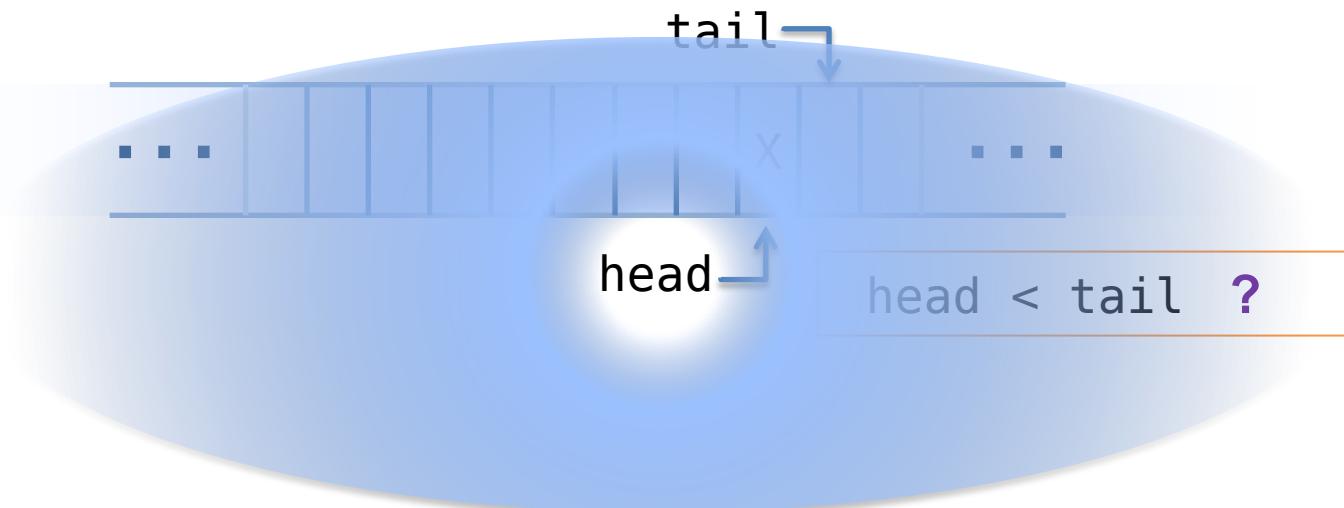




```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

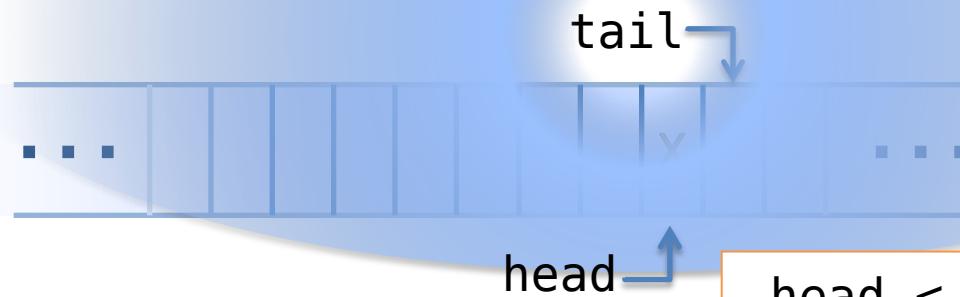
X...





```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
}
```



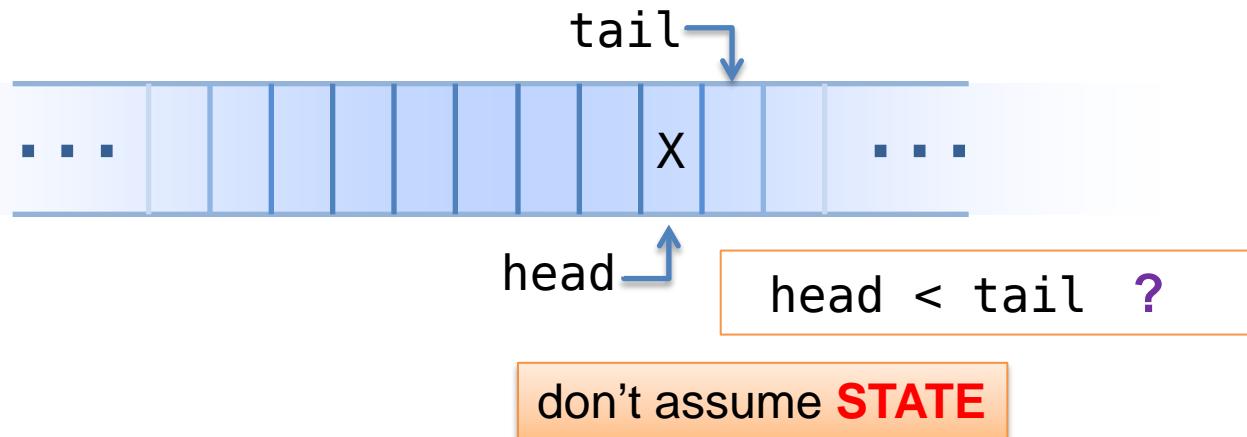
head < tail ?





```
void push(int val)
{
    buffer[tail++] = val;
}
```

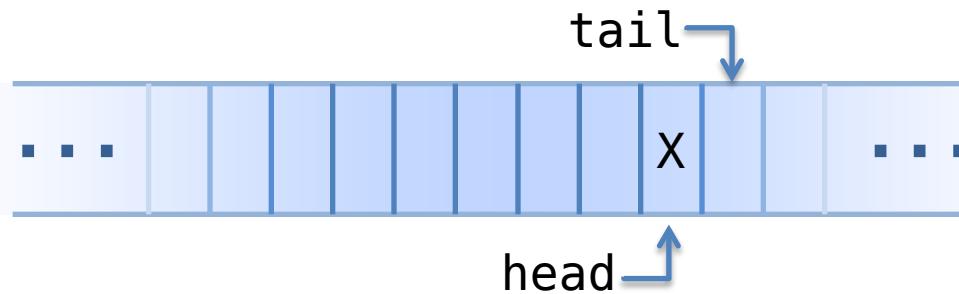
```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```





```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



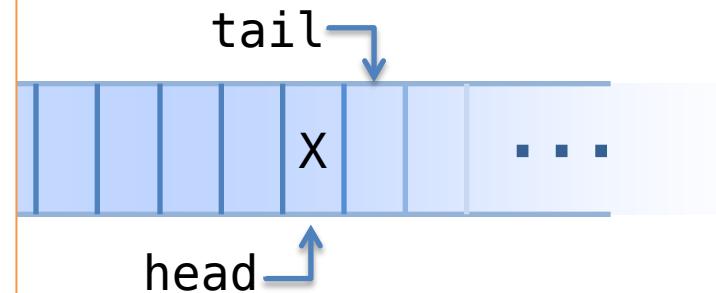
every **STATE** is a good **STATE**



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
statement1;
THEN
statement2;
THEN
statement3;
...
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



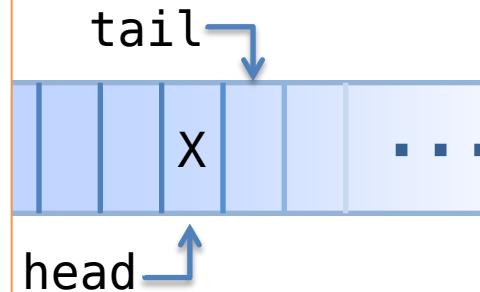
every **STATE** is a good **STATE**



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
if (some_state) {
    // some_state is still true(?)
    then_do_stuff();
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



X...

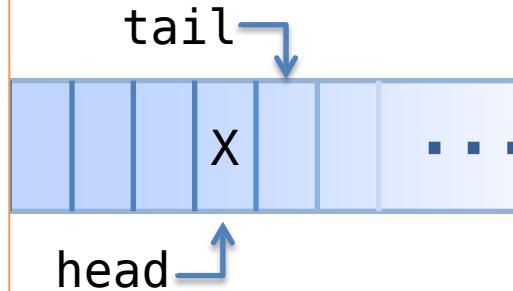
every **STATE** is a good **STATE**



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
void member_function {
    break_invariants;
    do_stuff;
    restore_invariants;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



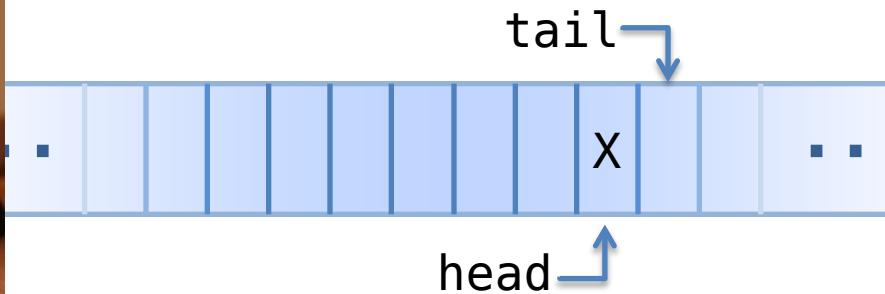
no “temporary suspension” of invariants



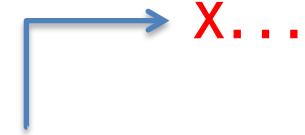
```
void push(int val)
{
    buffer[tail++] = val;
}
```



```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



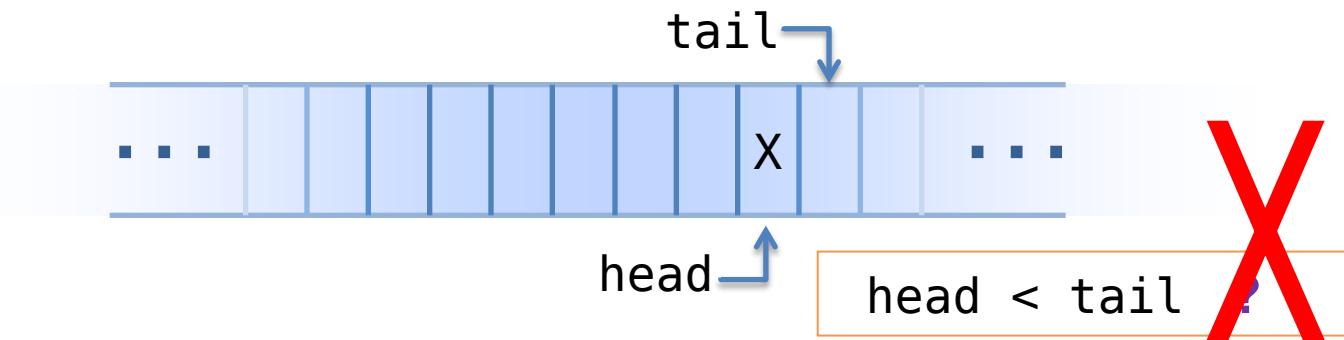
no “temporary suspension” of invariants





```
void push(int val)
{
    buffer[tail++] = val;
}
```

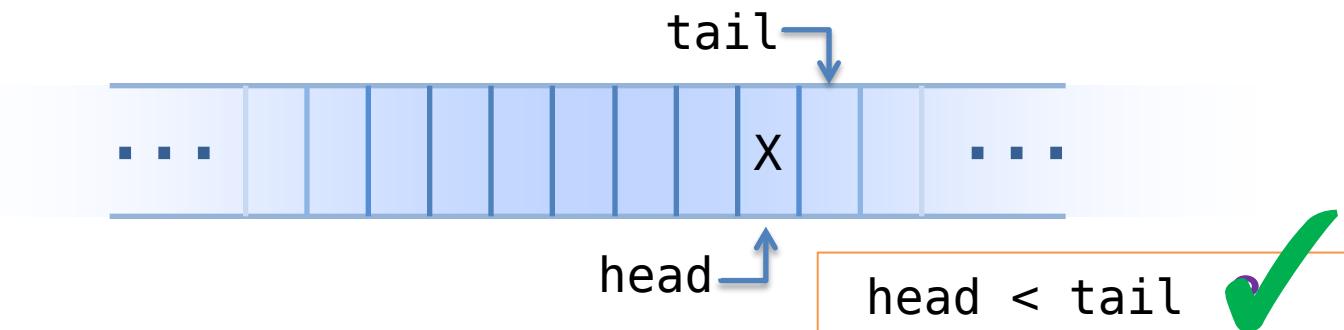
```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```





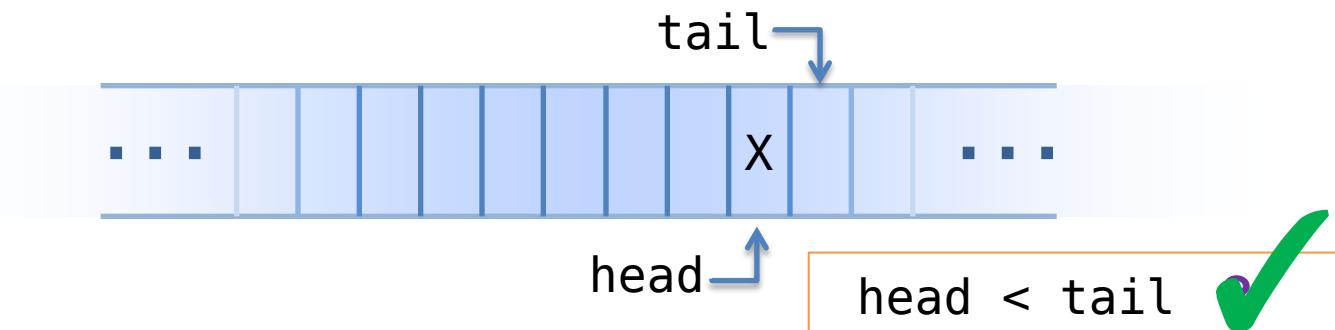
```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



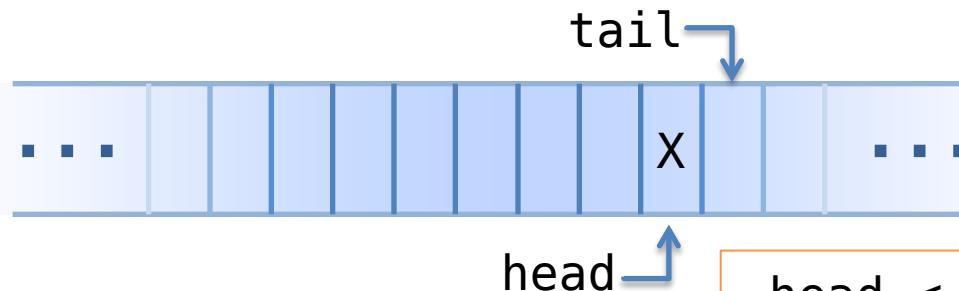
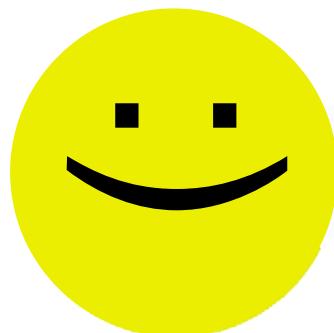
*ensure tail is always increasing*



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...



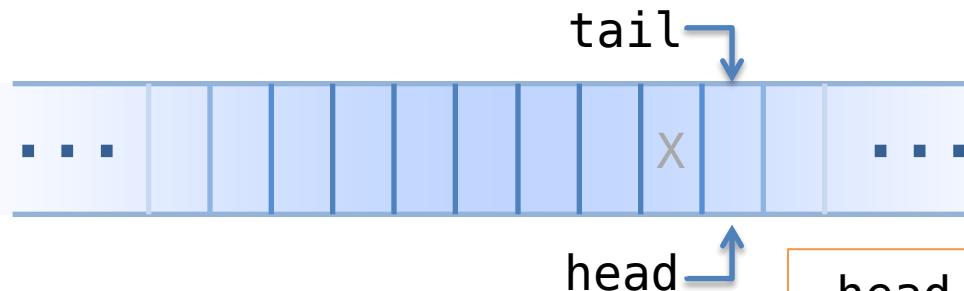
head < tail ?



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...



head

tail

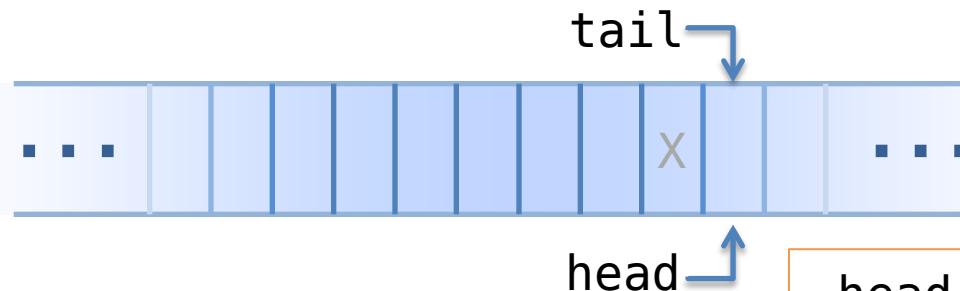
head < tail ?



```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

X...



head

tail

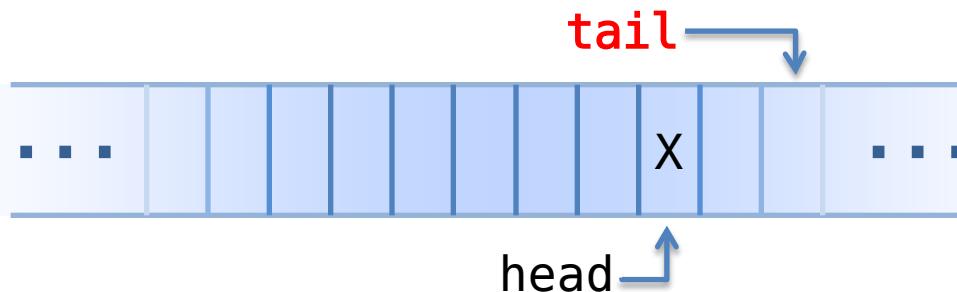
head < tail ?



```
void push(int val)
{
    buffer[tail++] = val;
}
```

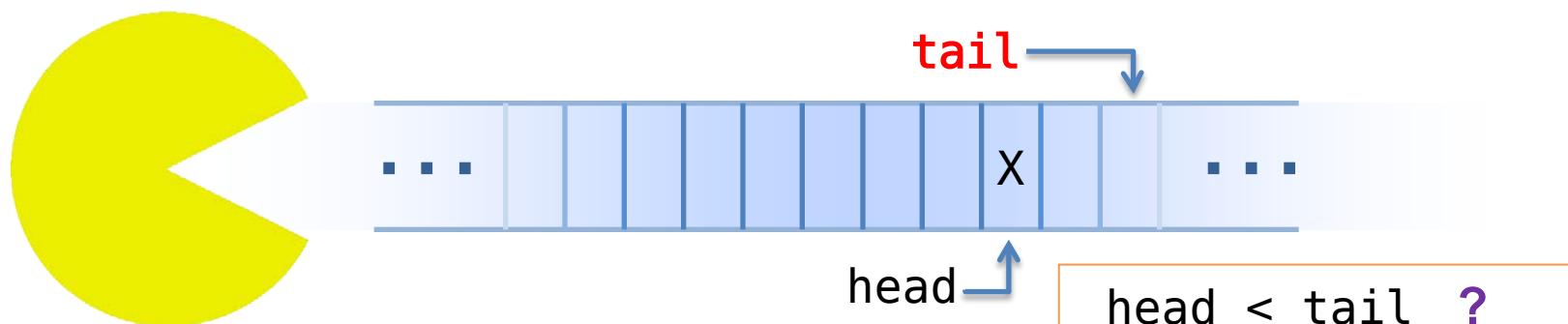
```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```

A



```
void push(int val)
{
    buffer[tail++] = val;
}
```

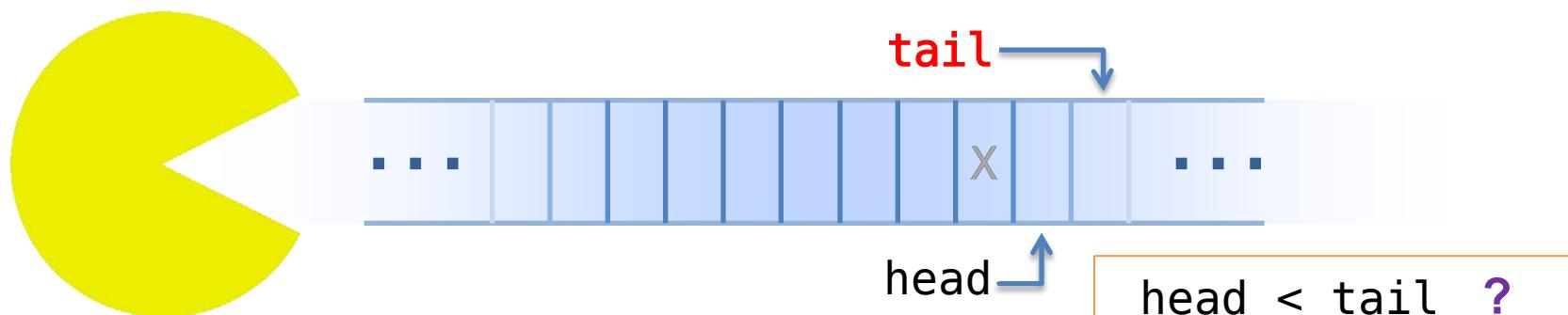
```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```





```
void push(int val)
{
    buffer[tail++] = val;
}
```

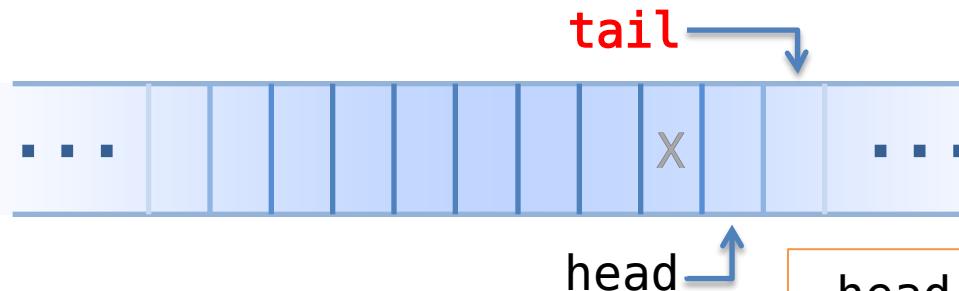
```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```





```
void push(int val)
{
    buffer[tail++] = val;
}
```

```
class Queue
{
    int buffer[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
};
```



head

tail

head < tail ?

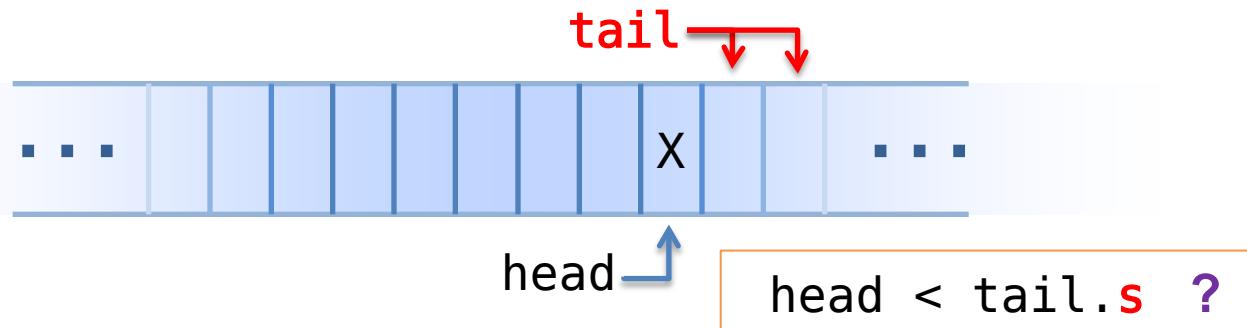
A

X...



```
void push(int val)
{
    ...
}
```

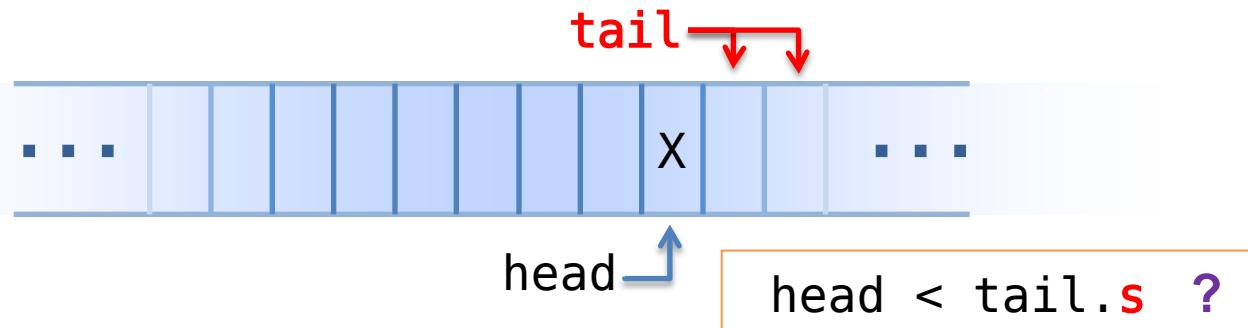
```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```





```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

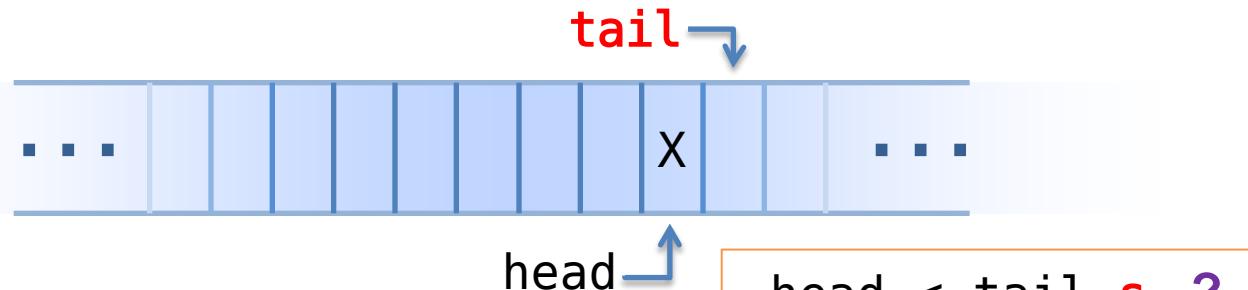
```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```





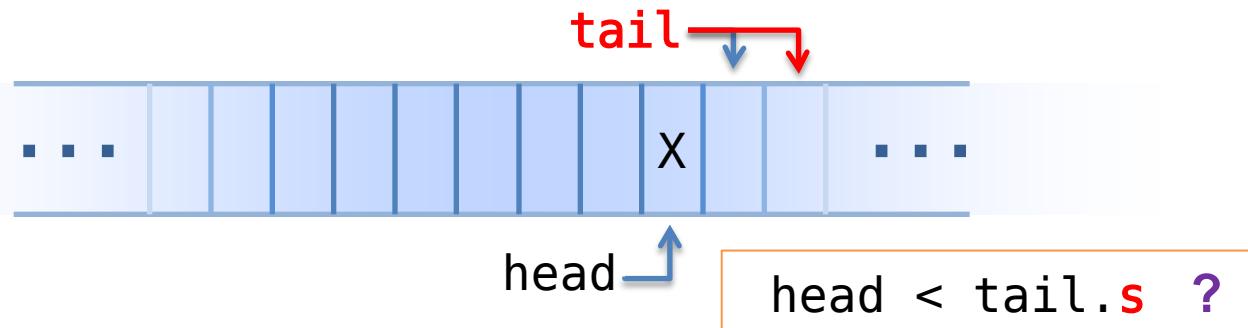
```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```



```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```

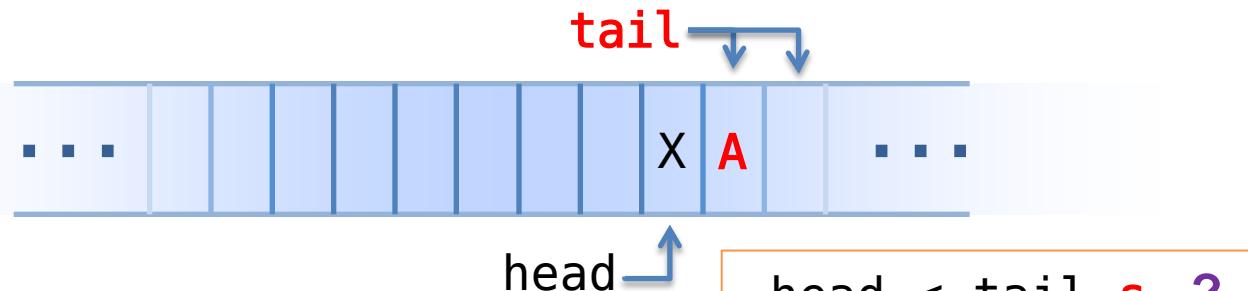




```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

A →

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```

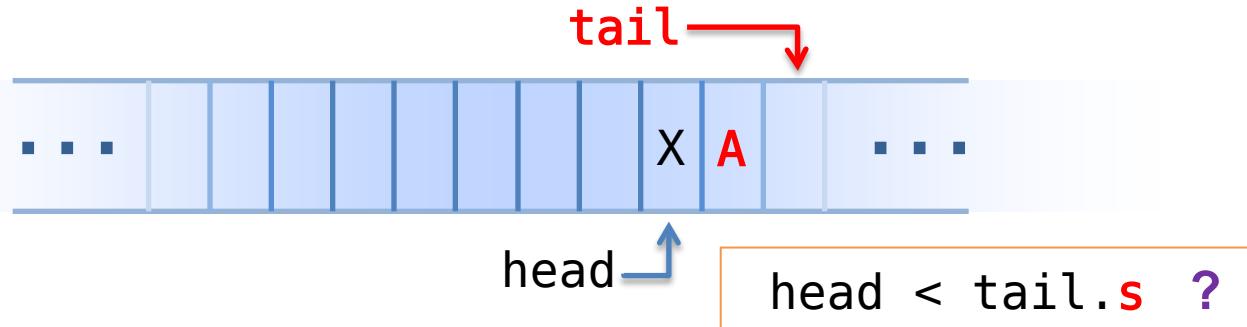




```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

A →

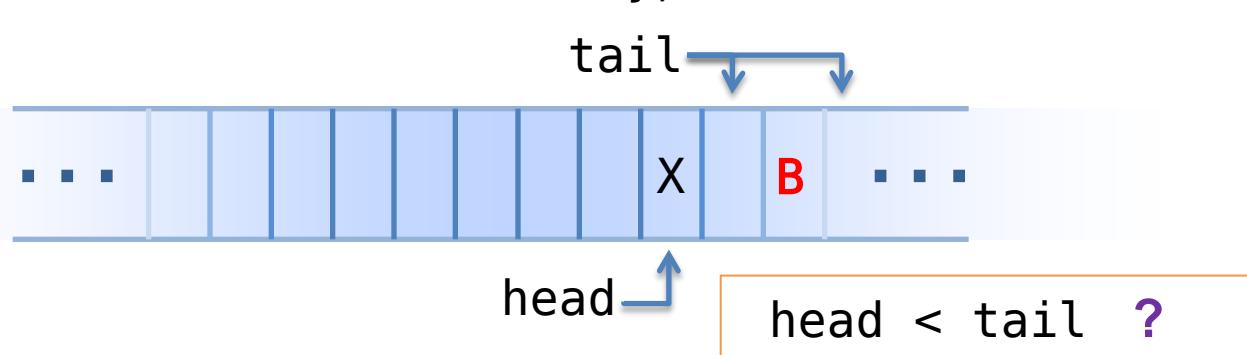
```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```





```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```





```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};

tail → →
-----  
... X B ...  
↑ head
```

head < tail ?



```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    tail.s++;
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};

tail → ↓ ↓
-----  
... X B ...  
head ↑
```

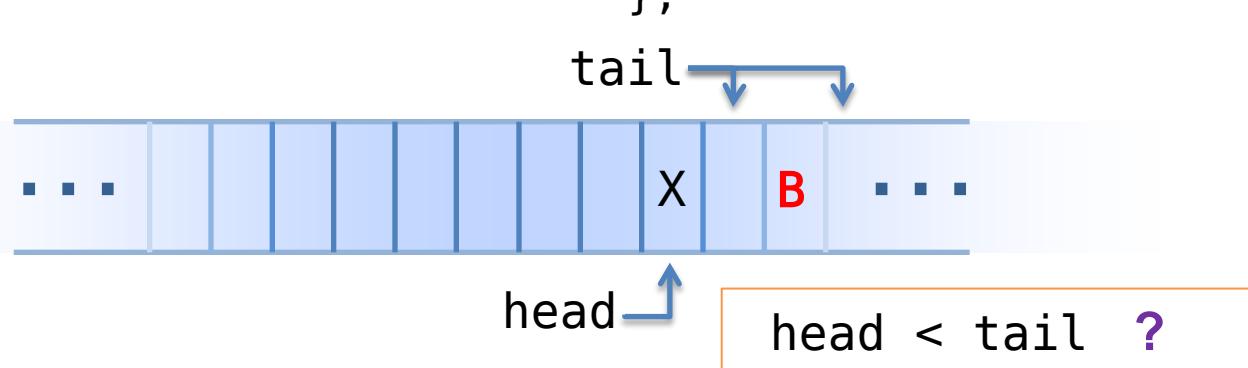
head < tail ?

The diagram illustrates a queue implementation using a buffer array and two atomic counters, head and tail. The buffer is represented as a horizontal array of blue cells. The head pointer is at the start of the array, indicated by an upward arrow. The tail pointer is at the end of the array, indicated by a downward arrow. The buffer contains elements X and B, with ellipses indicating more elements. A red double-headed arrow between the tail pointer and the buffer array indicates that the tail is currently pointing to the element after B. A question box asks if head is less than tail.



```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ...
    }
}
```

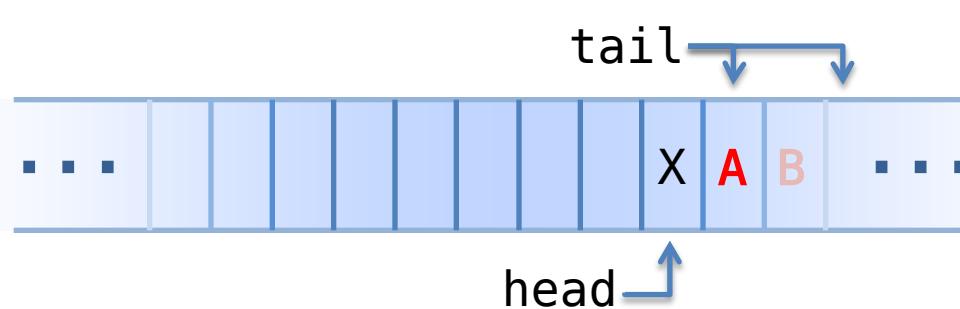
```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```





```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ...
    }
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```

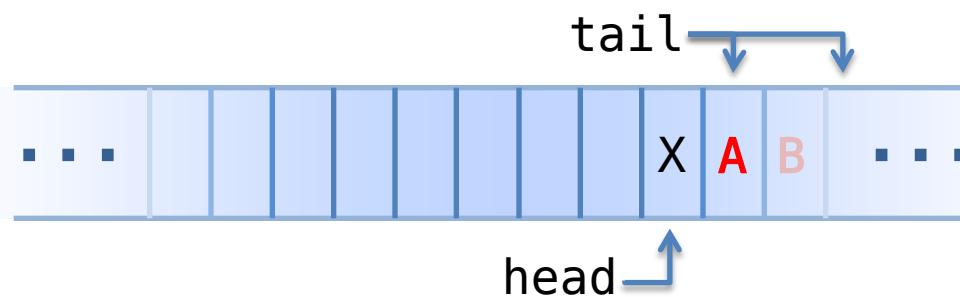




```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ...
    }
}
```

THEN

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```

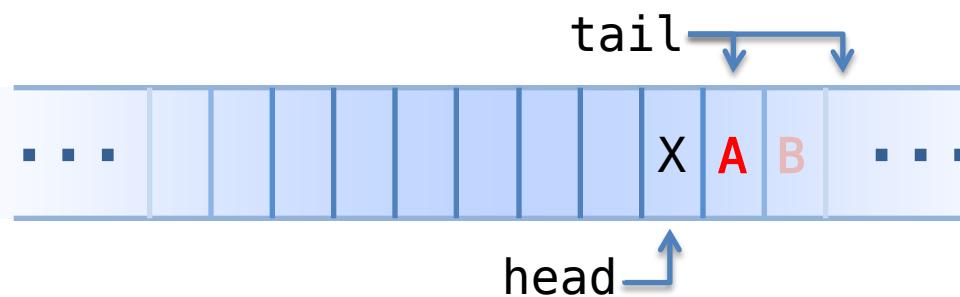




```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ...
    }
}
```

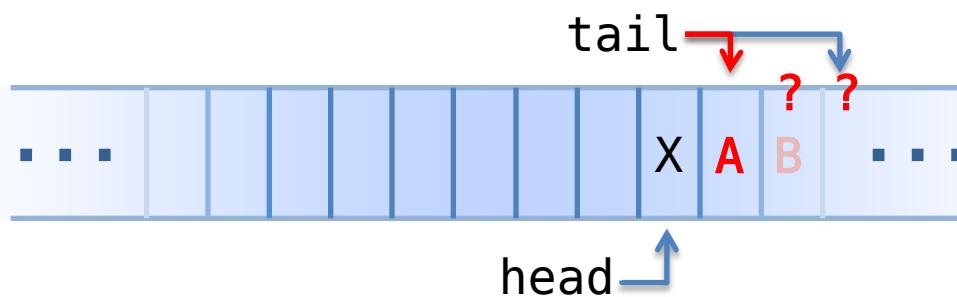
THEN

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```



```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ????
    }
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```



```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ????
    }
}
```

```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```

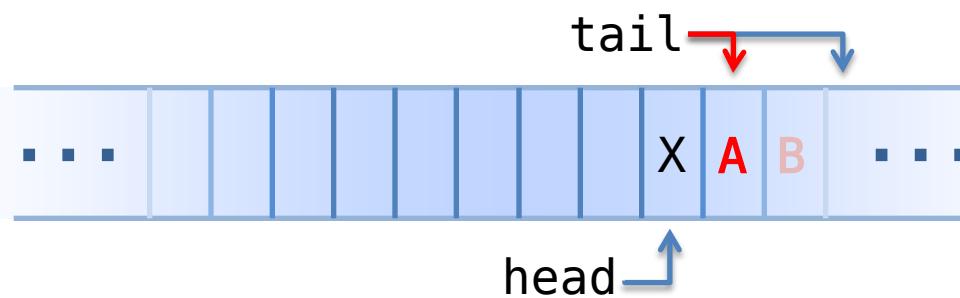
Compromise...

Queue of int -> Queue of int != 0



```
void push(int val)
{
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    if(tmp == tail.s) {
        tail.s = ????
    }
}
```

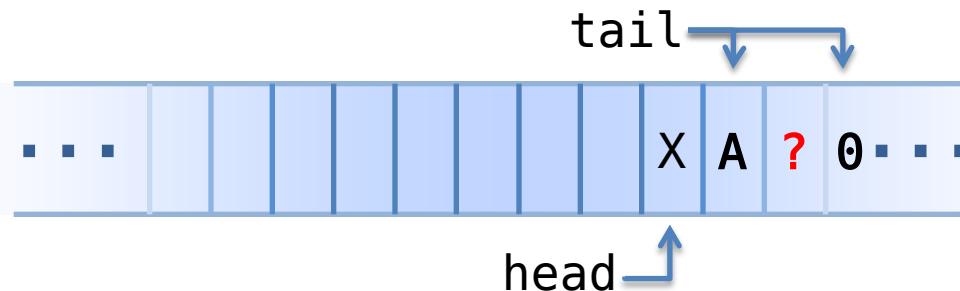
```
class Queue {
    int buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            tail.s++;  
        while (buffer[tail.s]);  
    }  
}
```

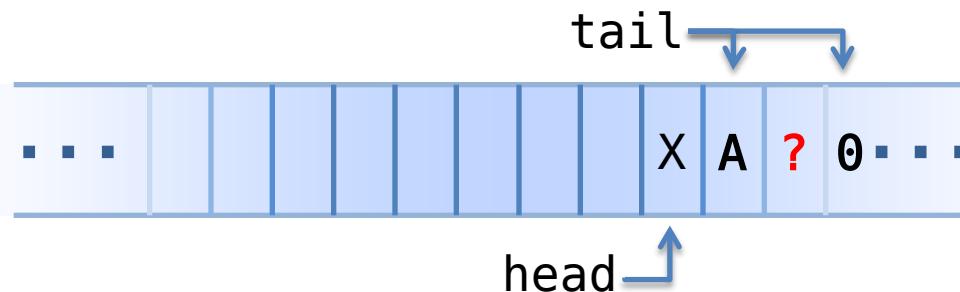
```
class Queue {  
    int buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            tail.s++;  
        A————→ while (buffer[tail.s]);  
    }  
}
```

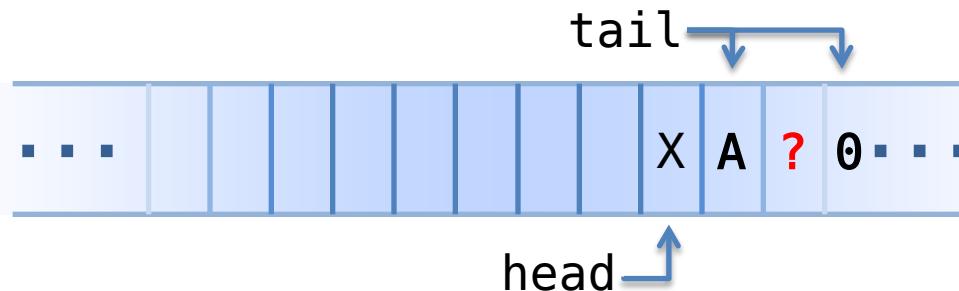
```
class Queue {  
    int buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            tail.s++;  
        while (buffer[tail.s]);  
    }  
}
```

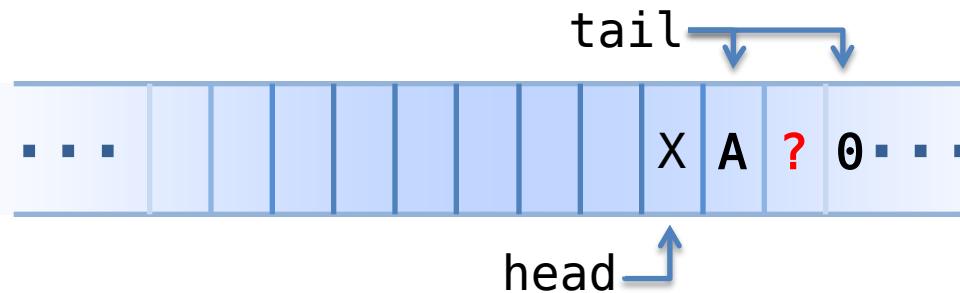
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) { THEN  
        do  
            tail.s++;  
        while (buffer[tail.s]);  
    }  
}
```

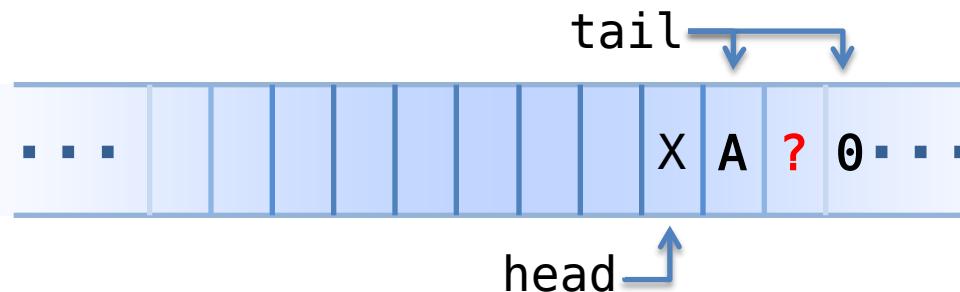
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            tail.s++;  
        while (buffer[tail.s]);  
    }  
}
```

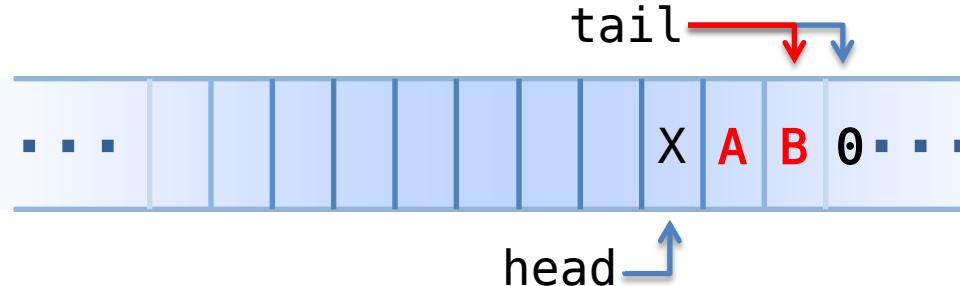
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    B→ if(tmp == tail.s) {  
        do  
            A→ tail.s++;  
        while (buffer[tail.s]);  
    }  
}
```

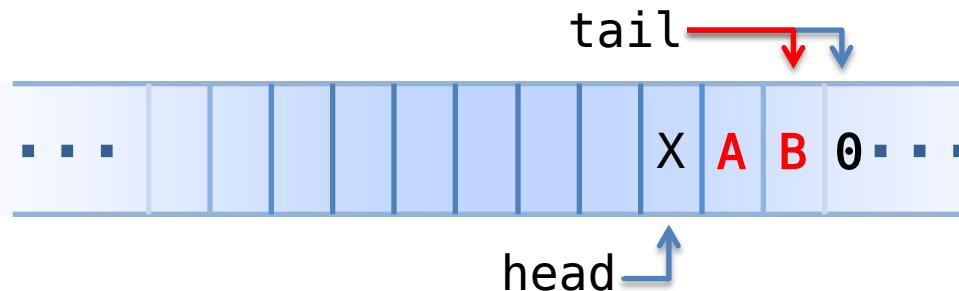
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        B-----  
        do  
        A-----  
            tail.s++;  
        while (buffer[tail.s]);  
    }  
}
```

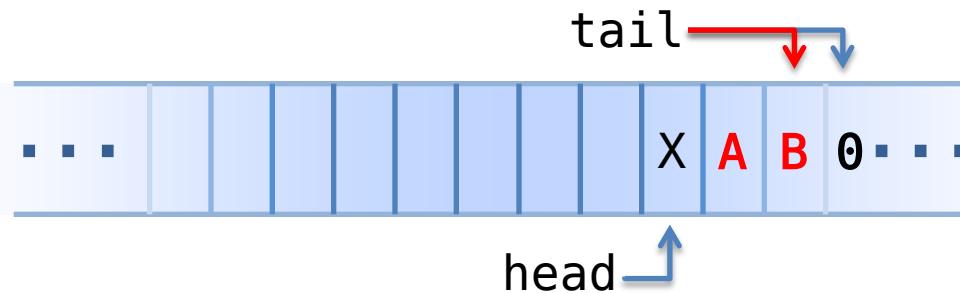
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            CAS(tail.s,tmp,tmp+1);  
        while (buffer[++tmp]);  
    }  
}
```

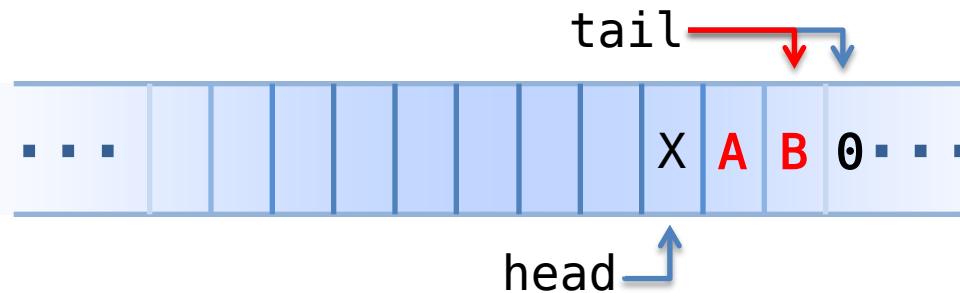
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    if(tmp == tail.s) {  
        do  
            CAS(tail.s,tmp,tmp+1);  
        while (buffer[++tmp]);  
    }  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```

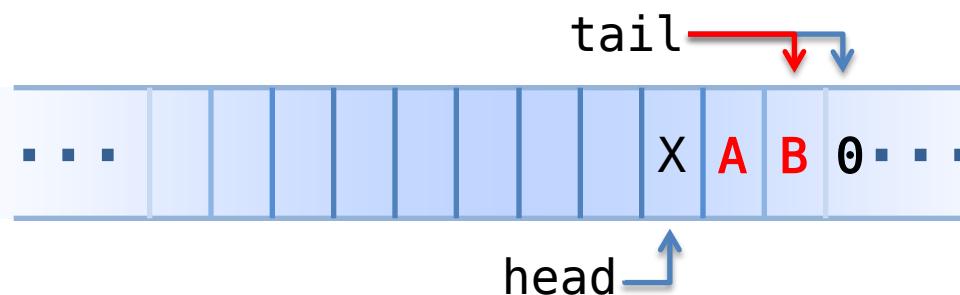




```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s,tmp,tmp+1);  
    while (buffer[++tmp]);  
}
```

B  
A →

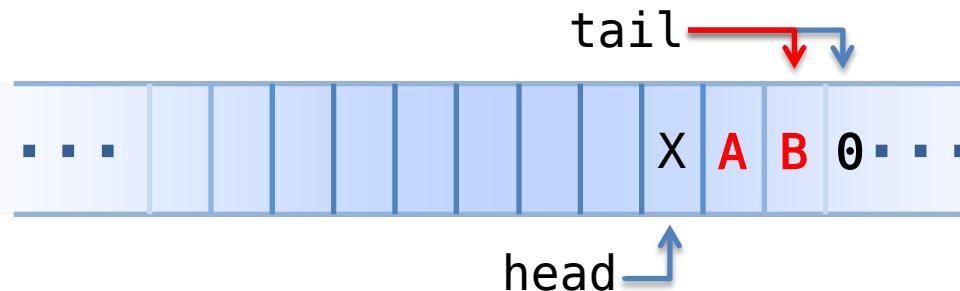
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    do  
        r = CAS(tail.s, tmp, tmp+1);  
    while (r && buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```

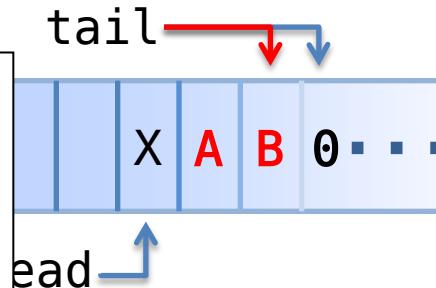




```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    do  
        r = CAS(tail.s, tmp, tmp+1);  
    while (r && buffer[++tmp]);  
}
```

```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

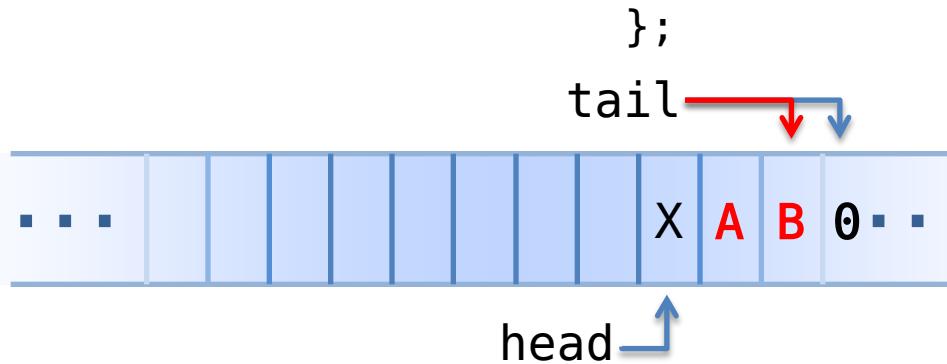
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e; } tail;  
};
```

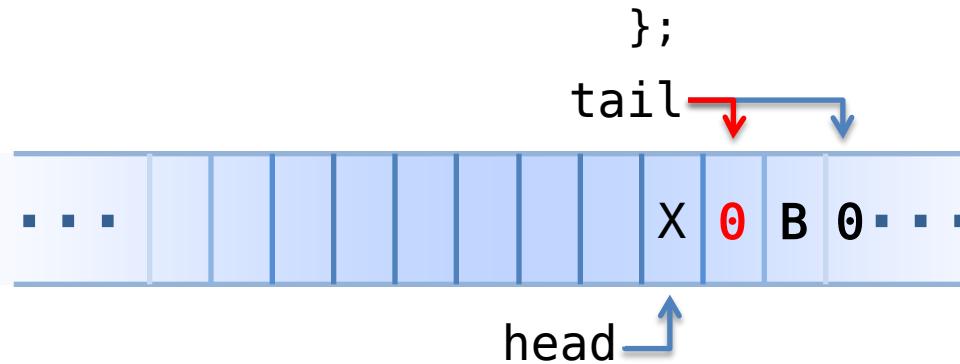




```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

A →  
**PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```

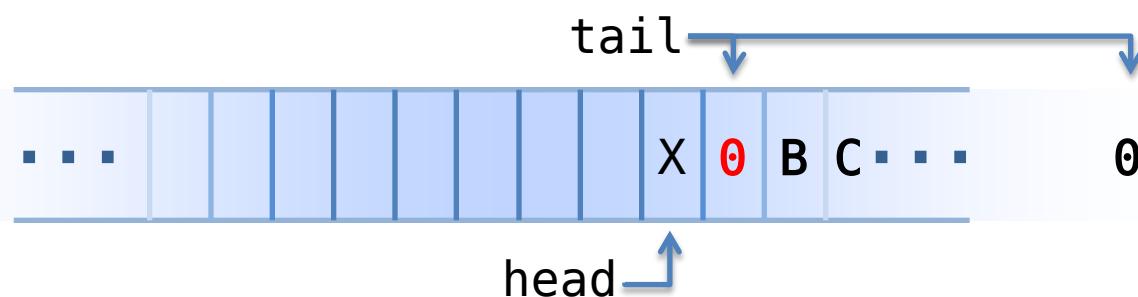


?



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    PAUSE  
    do  
        CAS(tail.s,tmp,tmp+1);  
    while (buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```

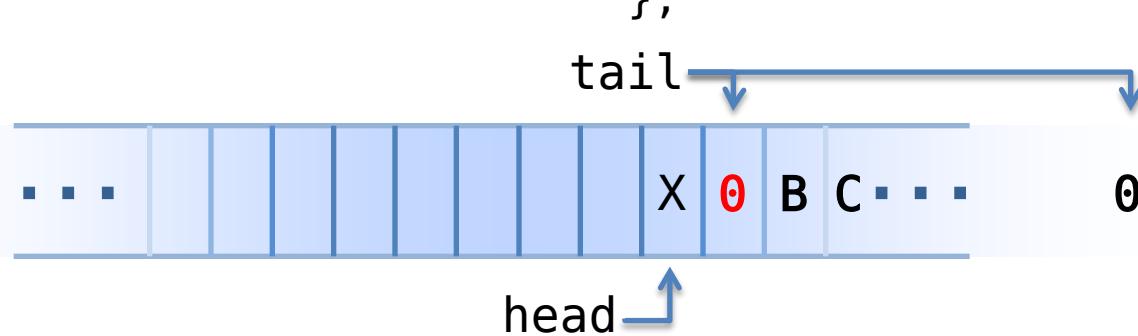




```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s,tmp,tmp+1);  
    while (buffer[++tmp]);  
}
```

A →  
**PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```



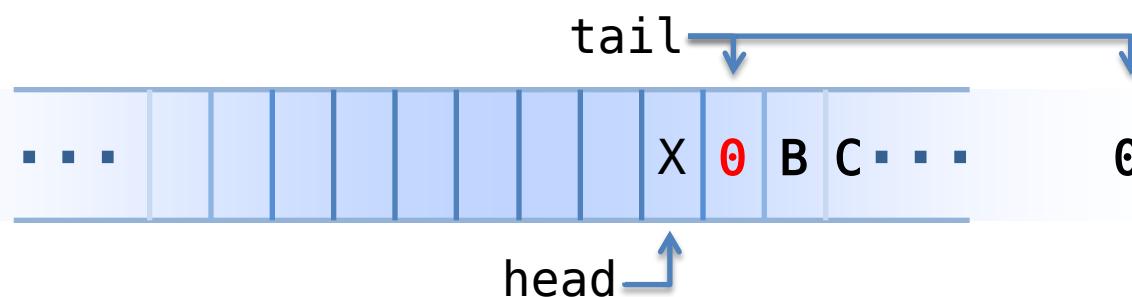
OK ?



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

A →  
**PAUSE**

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```



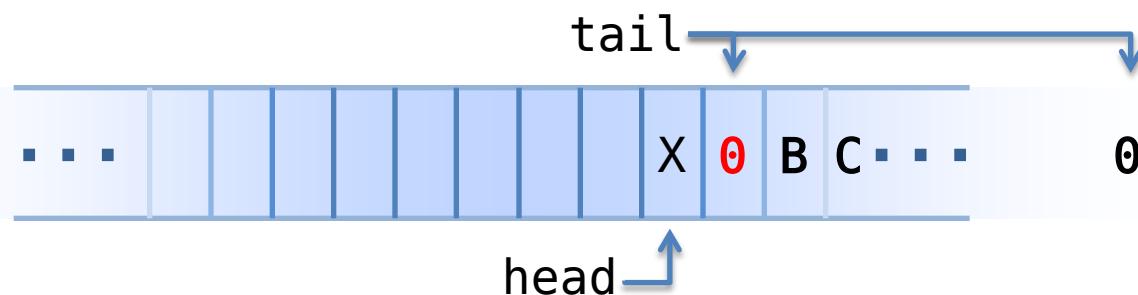
lock-free ?



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    PAUSE  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

```
int pop() {  
    if/while(!(head < tail.s))  
        return/wait;  
    ...  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
};
```

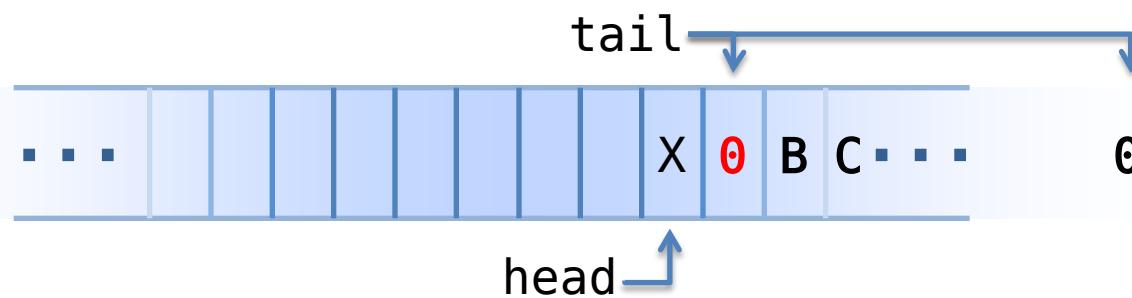


lock-free ?

```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    PAUSE  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

```
int pop() {  
    if/while(!(head < tail.s))  
        return/wait;  
    ...  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e; } tail;  
};
```

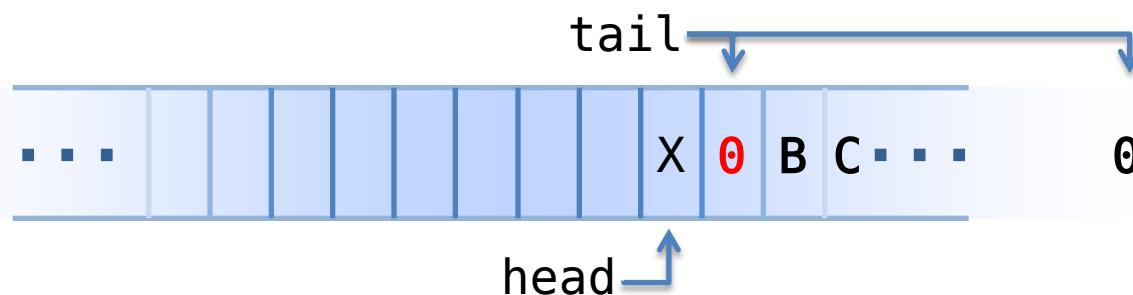


“block-free” ?



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    PAUSE  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e; } tail;  
};
```



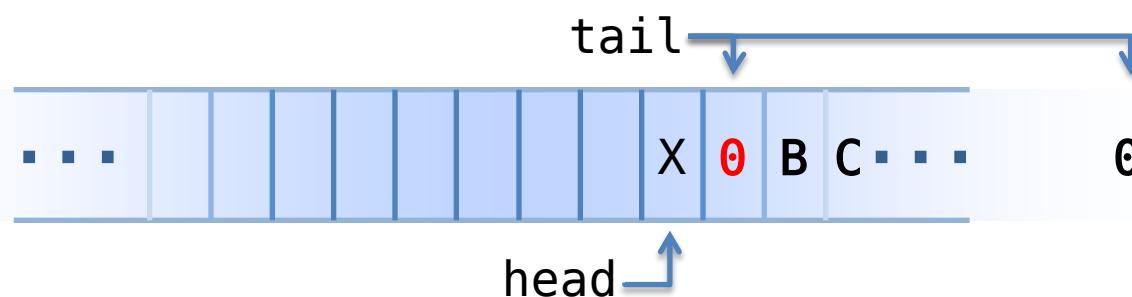
```
int pop() {  
    if/while(  
        return ...  
    }
```

An algorithm is ***lock-free*** if at all times at least one thread is guaranteed to be **making progress**.



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    PAUSE  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e; } tail;  
};
```



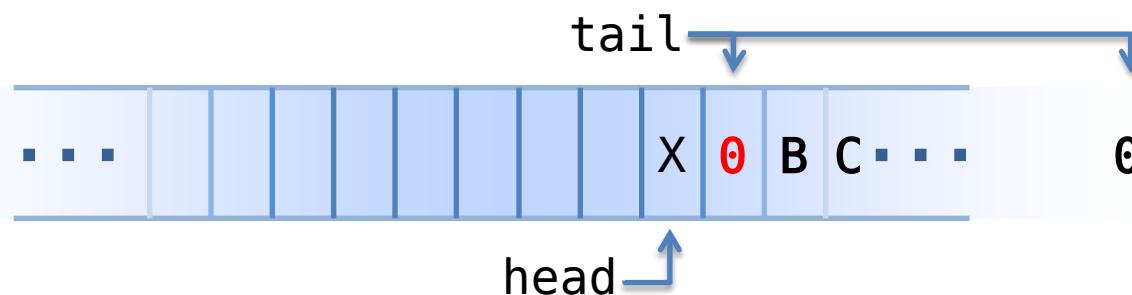
```
int pop() {  
    if/  
    ...  
}
```

If I suspended a certain thread at the worst time, for a long time or forever,  
do bad things happen?  
Yes -> not lockfree.

```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    PAUSE  
    do  
        CAS(tail.s, tmp, tmp+1);  
    while (buffer[++tmp]);  
}
```

```
int pop() {  
    if/while(!(head < tail.s))  
        return/wait;  
    ...  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e; } tail;  
};
```



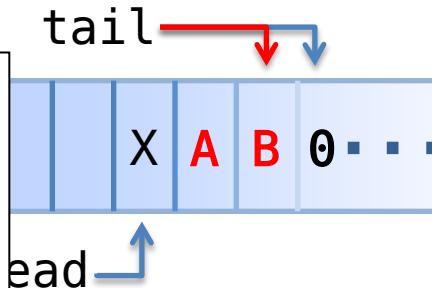
!= lock-free



```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    do  
        r = CAS(tail.s,tmp,tmp+1);  
    while (r && buffer[++tmp]);  
}
```

```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s,tmp,tmp+1);  
    while (buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```



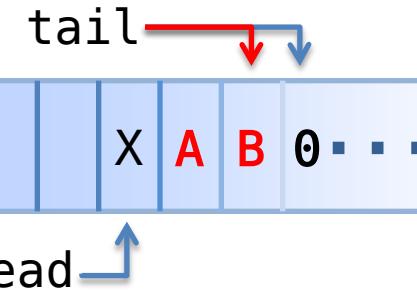


```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    do  
        r = CAS(tail.s,tmp,tmp+1);  
    while (r && buffer[++tmp]);  
}
```

A →  
**PAUSE**

```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s,tmp,tmp+1);  
    while (buffer[++tmp]);  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    do  
        r = CAS(tail.s,tmp,tmp+1);  
    while (r && buffer[++tmp]);  
}
```

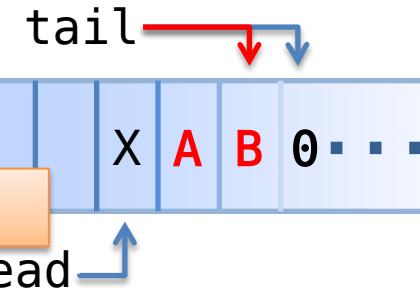
A →  
**PAUSE**

**!= lock-free**

```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    do  
        CAS(tail.s,tmp,tmp+1);  
    while (buffer[++tmp]);  
}
```

**~= lock-free**

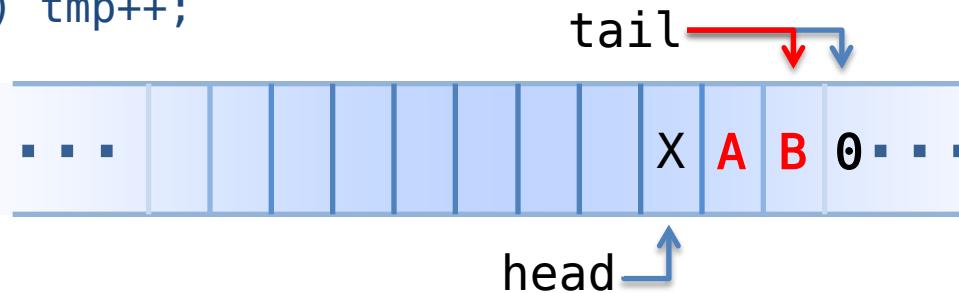
```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct {  
        atomic<size_t> s;  
        atomic<size_t> e;  
    } tail;  
};
```





```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    tmp = tail.s;  
    while (buffer[tmp]) {  
        r = tail.s.CAS(tmp, tmp+1);      };  
        if (r) tmp++;  
    }  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e; } tail;
```



```

void push(int val) {
    size_t tmp = tail.e++;
    buffer[tmp] = val;
    bool r;
    tmp = tail.s;
    while (buffer[tmp]) {
        r = tail.s.CAS(tmp, tmp+1);      };
        if (r) tmp++;
    }
}

```

```

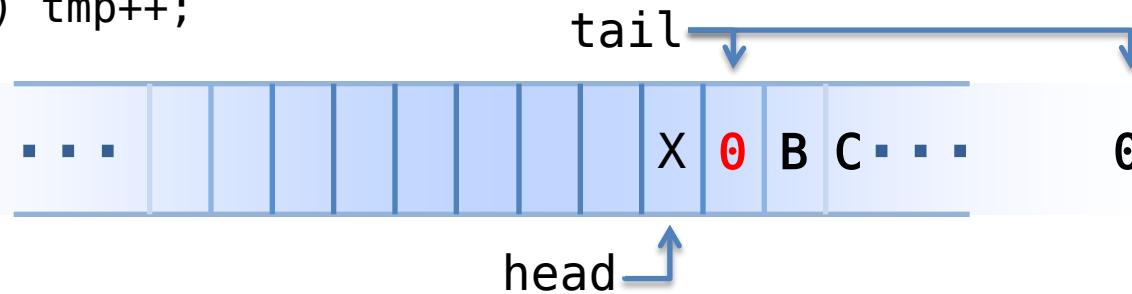
int pop() {
    if/while(!(head < tail.s))
        return/wait;
    ...
}

```

```

class Queue {
    atomic<int> buffer[SZ];
    atomic<size_t> head;
    struct { atomic<size_t> s;
              atomic<size_t> e;
            } tail;
}

```



**!= lock-free**

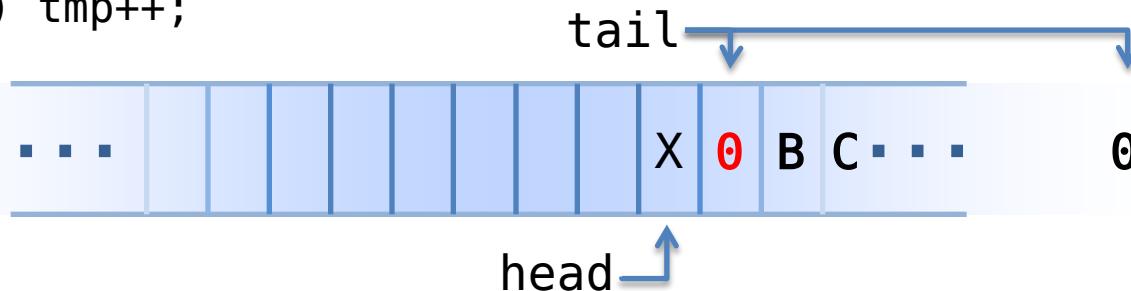






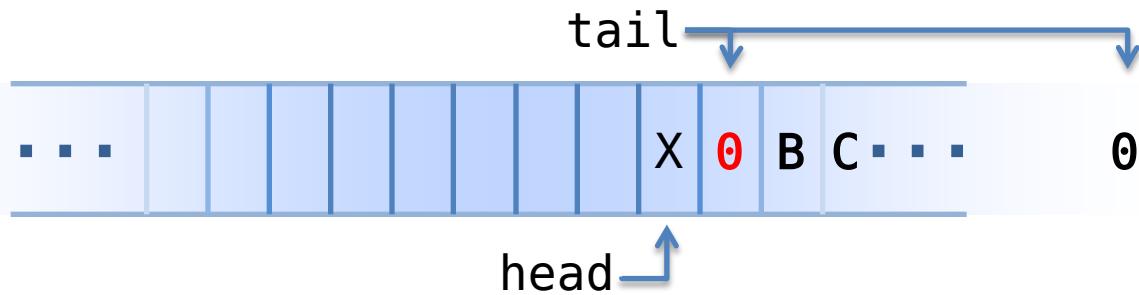
```
void push(int val) {  
    size_t tmp = tail.e++;  
    buffer[tmp] = val;  
    bool r;  
    tmp = tail.s;  
    while (buffer[tmp]) {  
        r = tail.s.CAS(tmp, tmp+1);  
        if (r) tmp++;  
    }  
}
```

```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e; } tail;
```

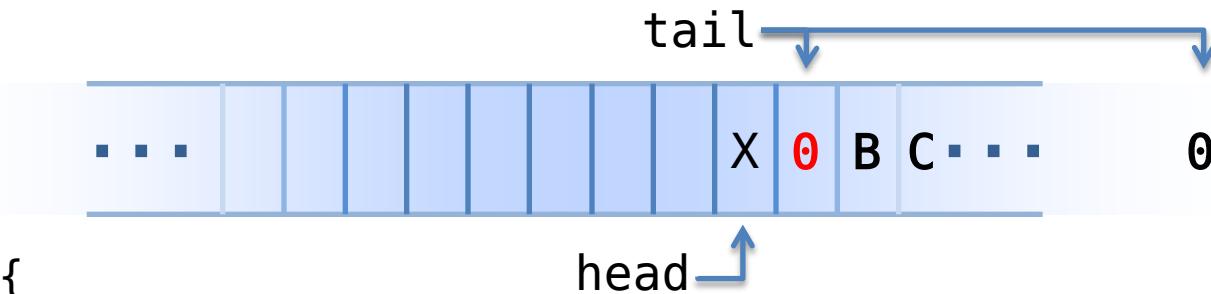


```
int pop() {  
    while  
    ;  
    ...  
}
```

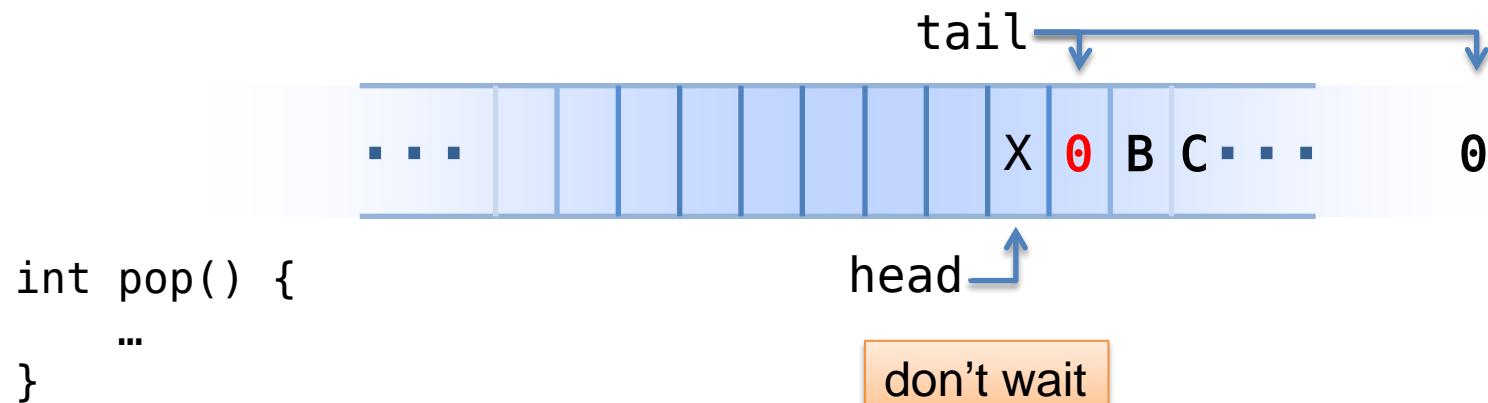
An algorithm is ***lock-free*** if at all times at least one thread is guaranteed to be **making progress**.

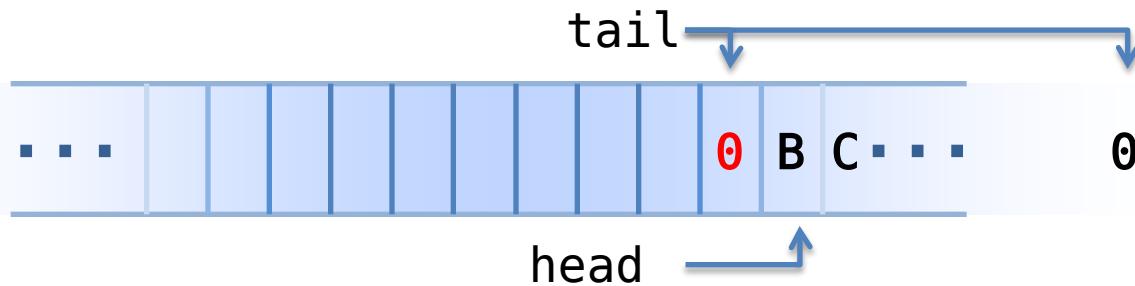


```
int pop() {  
    while (!(head < tail.s))  
        ;  
    ...  
}
```

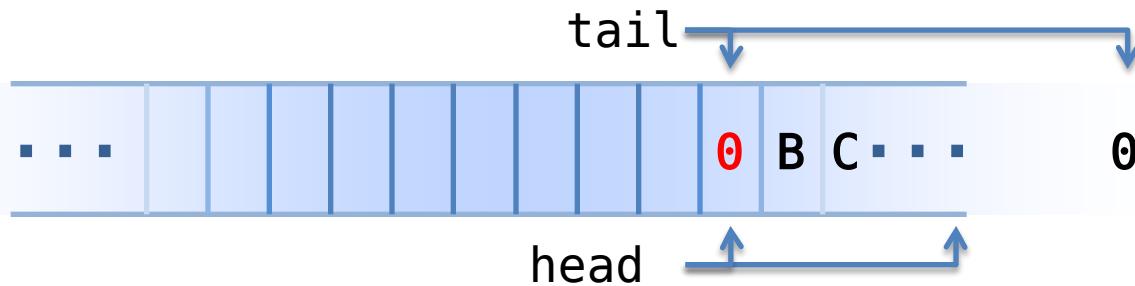


don't want to wait

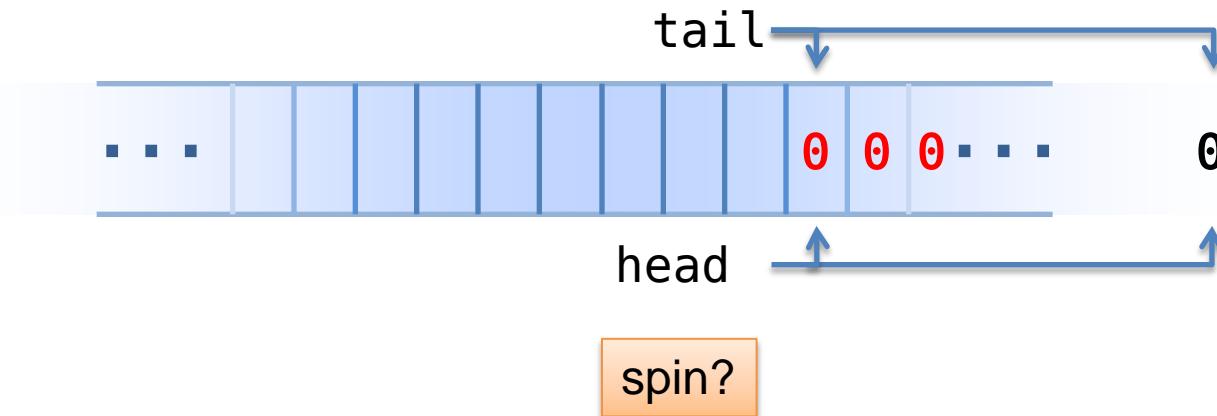


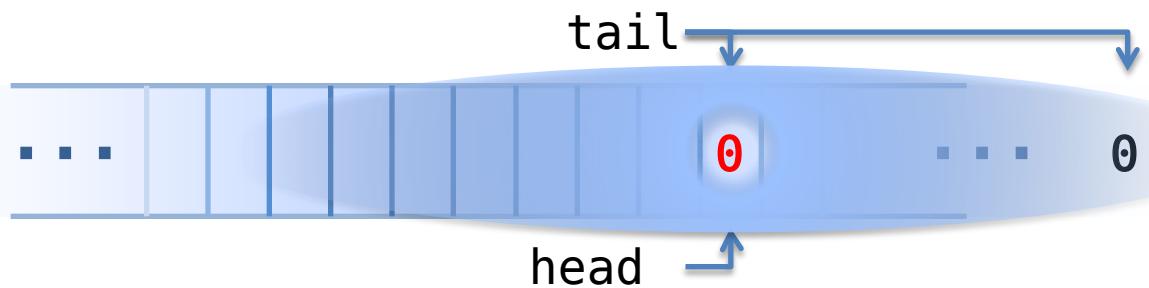


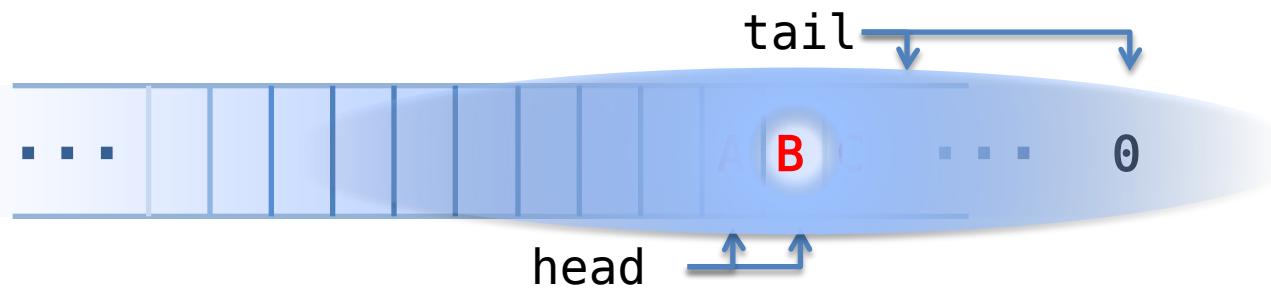
don't wait! (?)



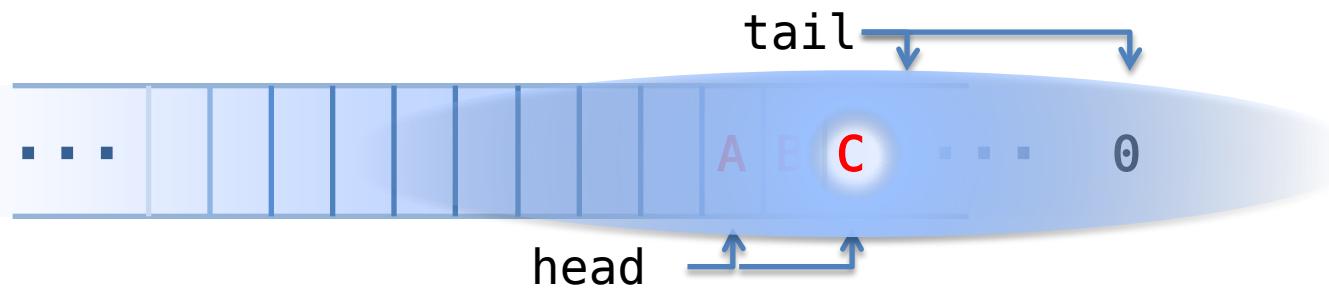
come back later (when?)



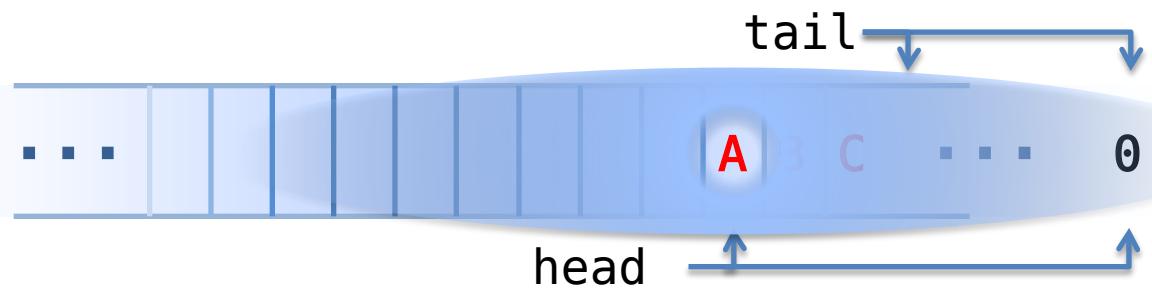




pop: B

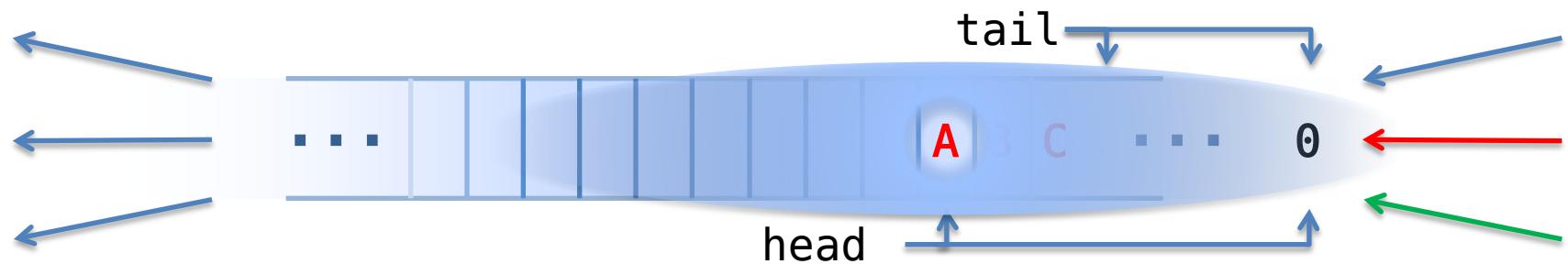


pop: B C



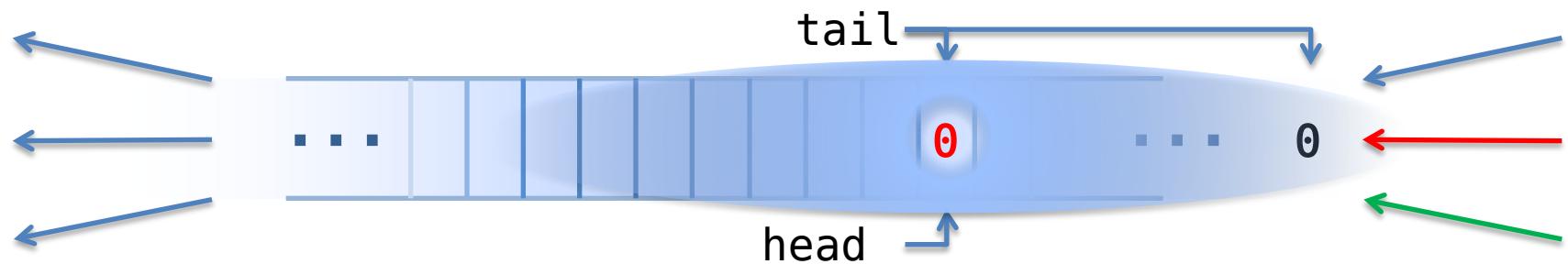
pop: B C A

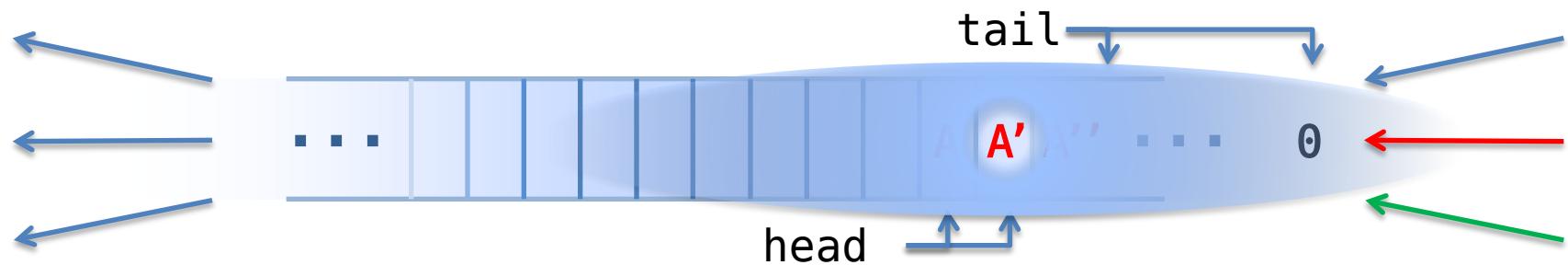
pop order ?



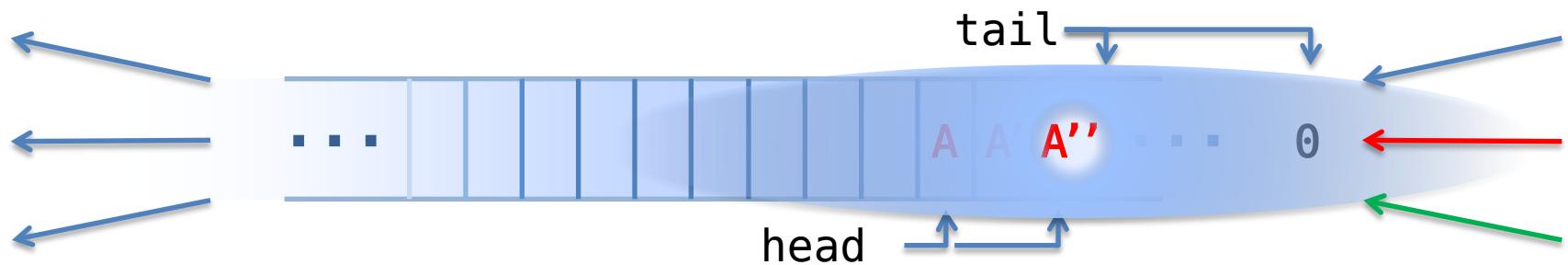
pop: B C A

pop order ?

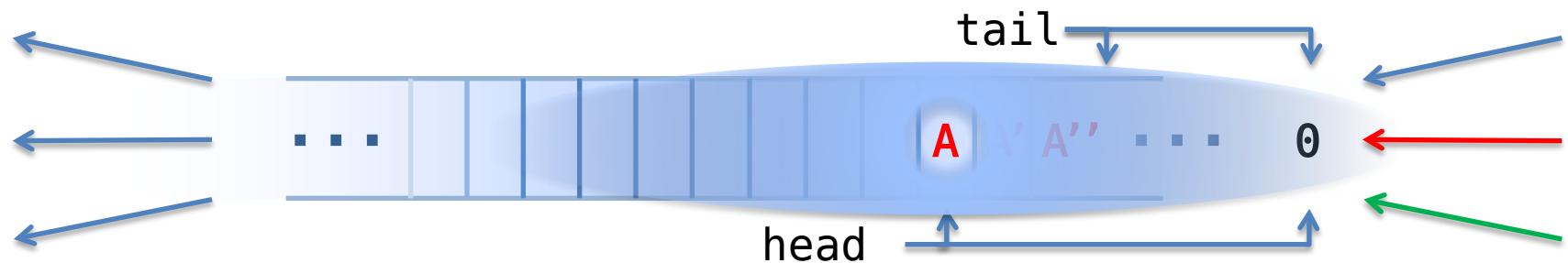




pop:  $A'$

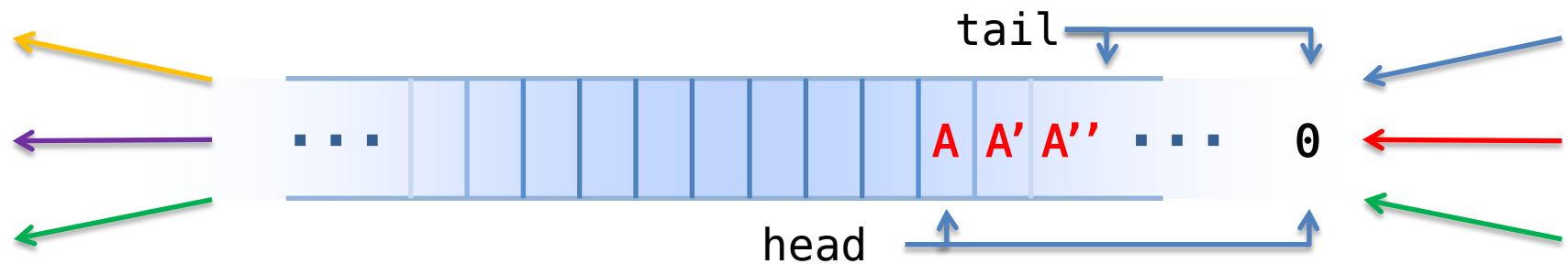


pop: **A' A''**



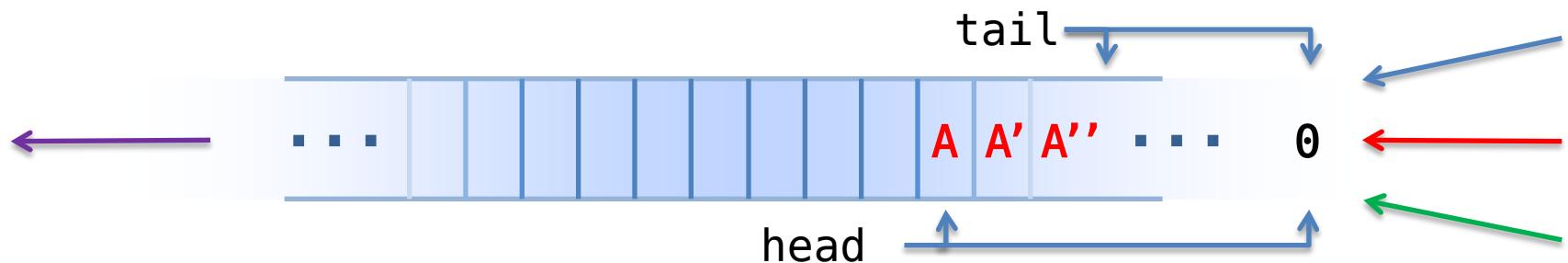
pop: **A' A'' A**

pop order ?



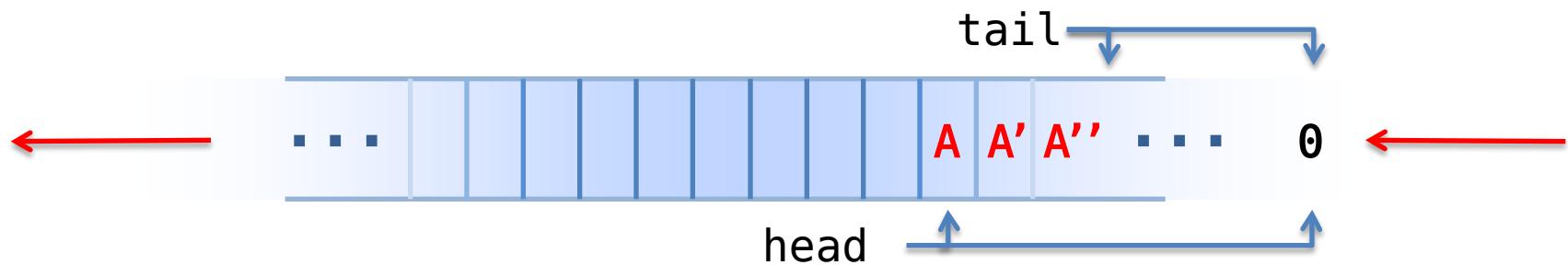
pop: **A' A'' A**

pop order ?



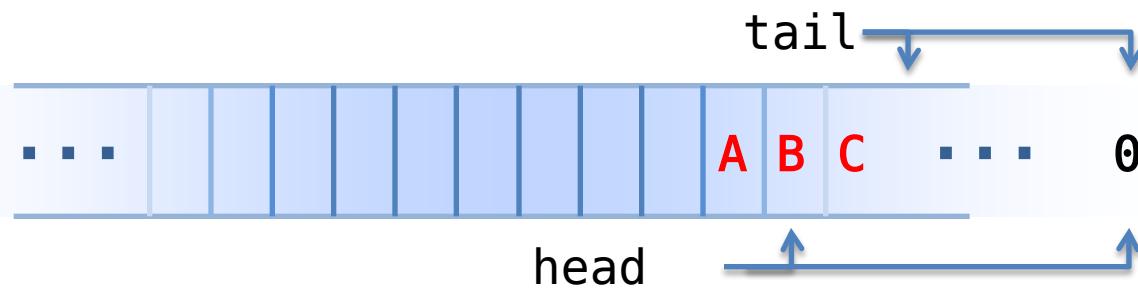
pop: A' A'' A

pop order ?



pop: **A' A'' A**

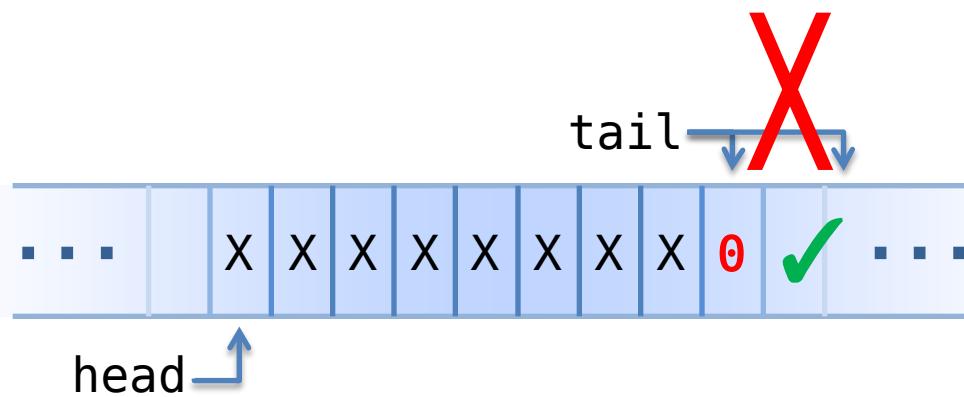
pop order ?

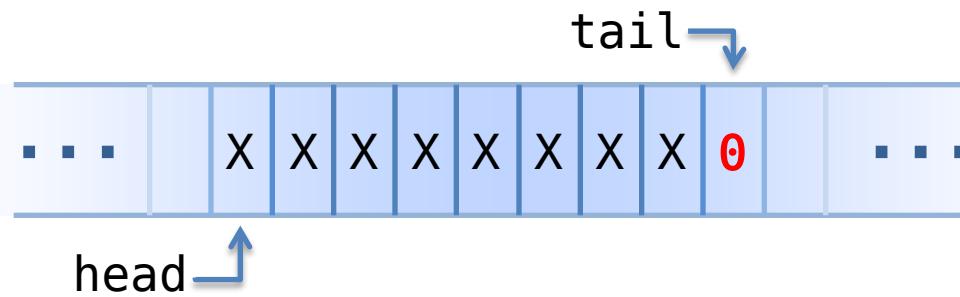


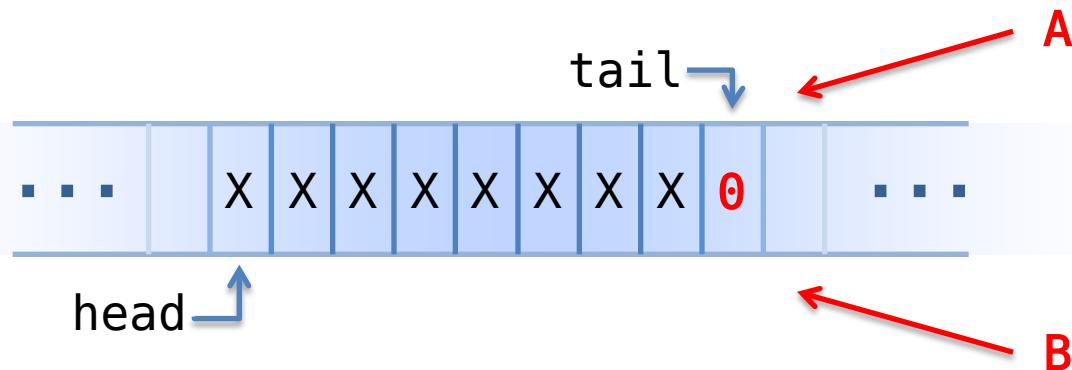
pop: B C A ... B?

did I read B already ?



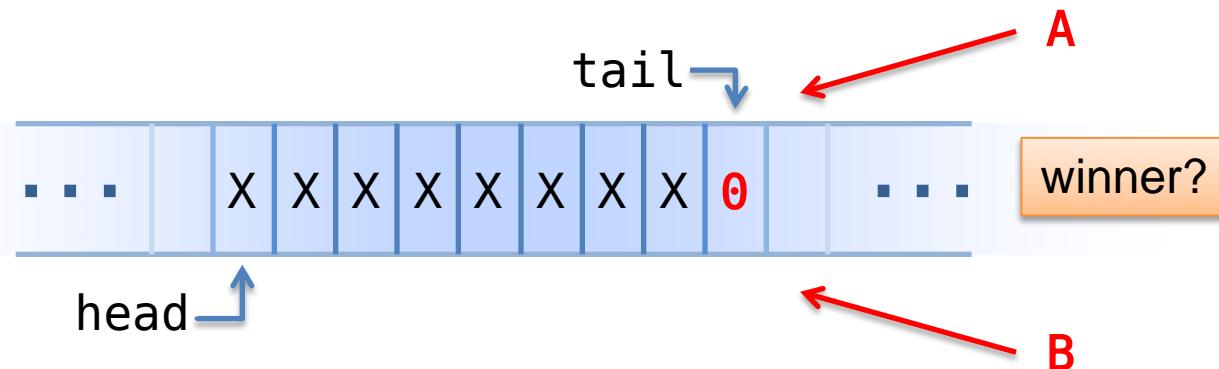






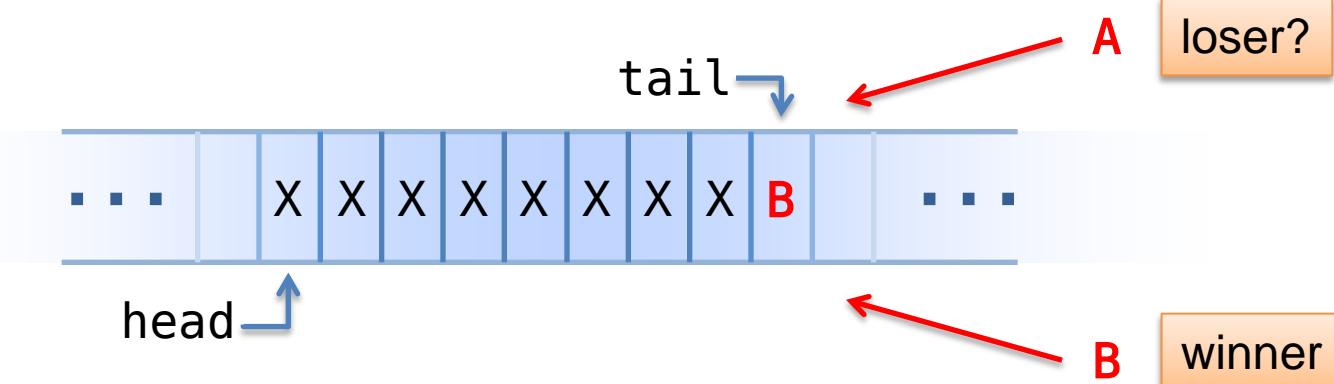


CAS(buffer[tail], 0, val)



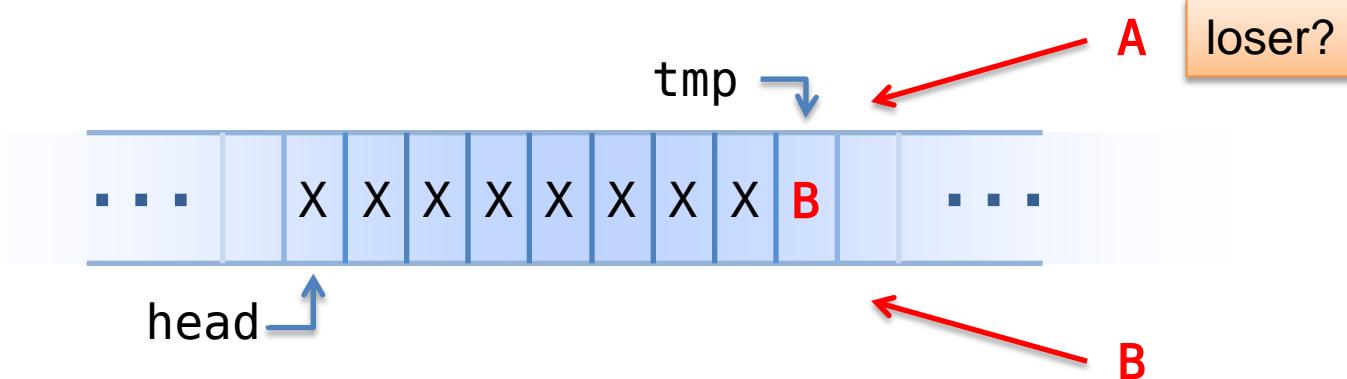


CAS(buffer[tail], 0, val)





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

**wait** for tail?

tmp ↴

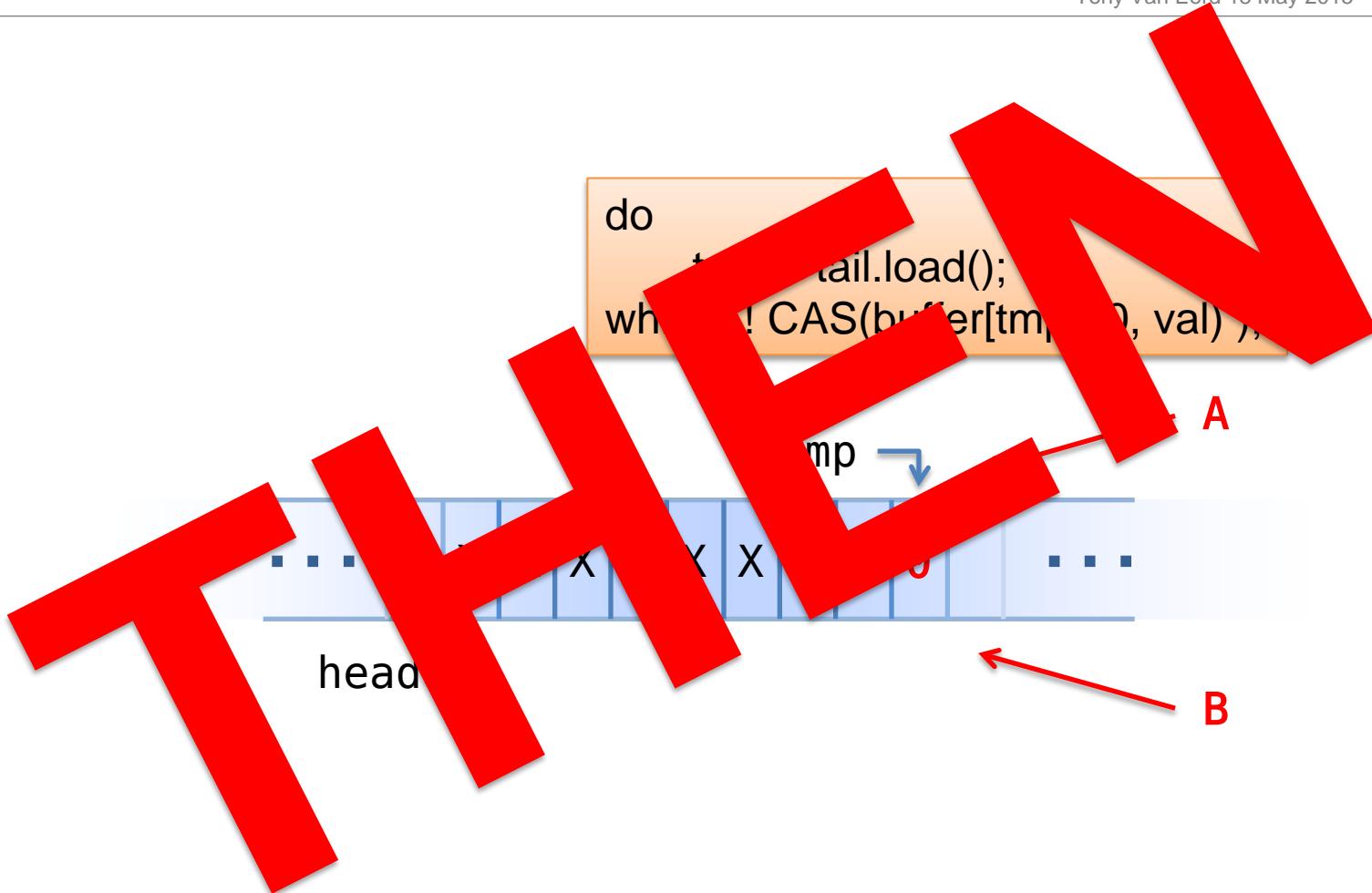
A

loser?



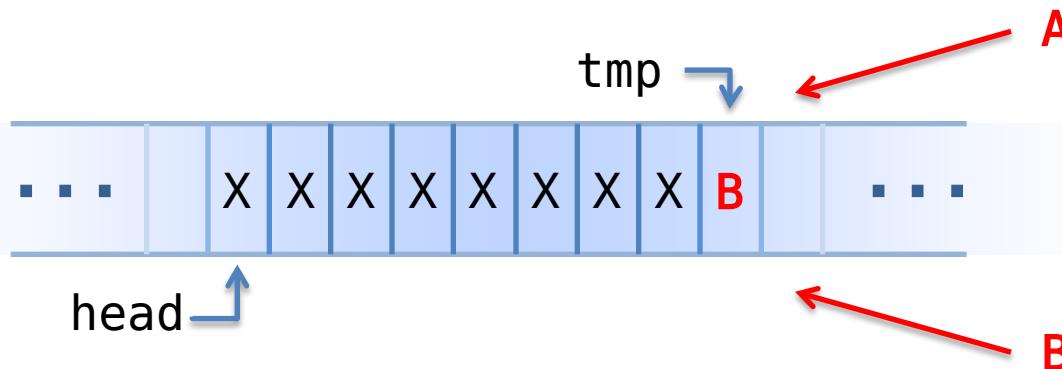
head ↗

↗ B



```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

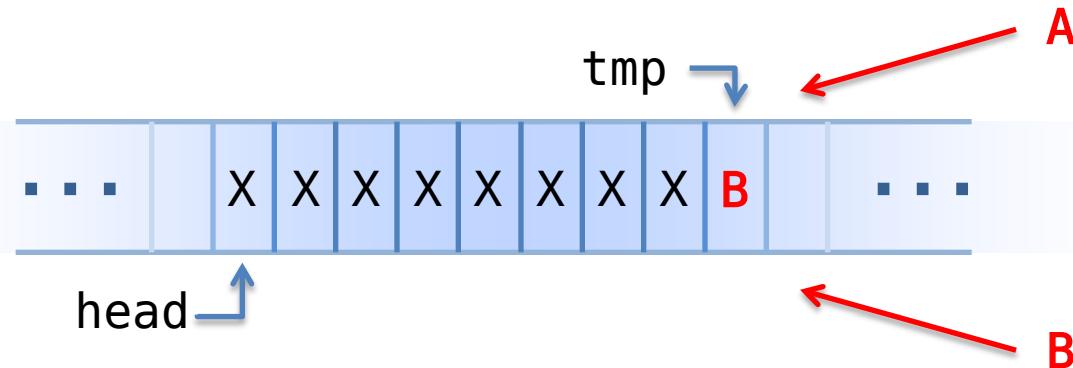
if CAS fails  
**THEN** try again





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

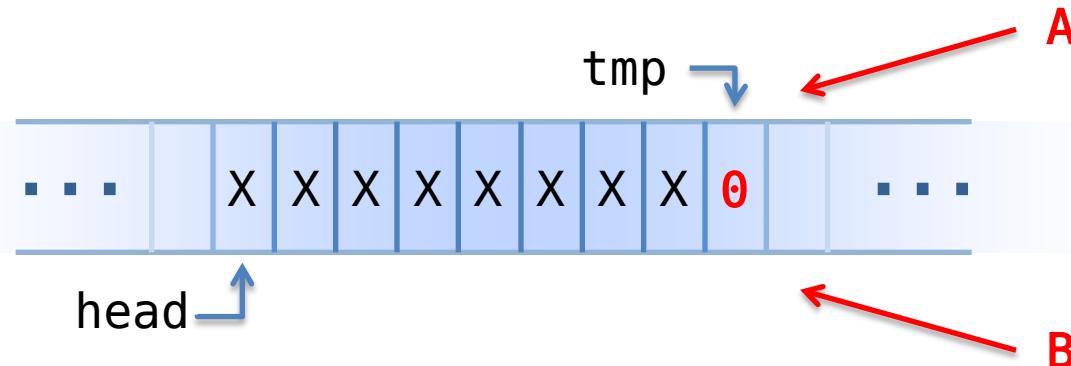
read tail  
**THEN** read buffer





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

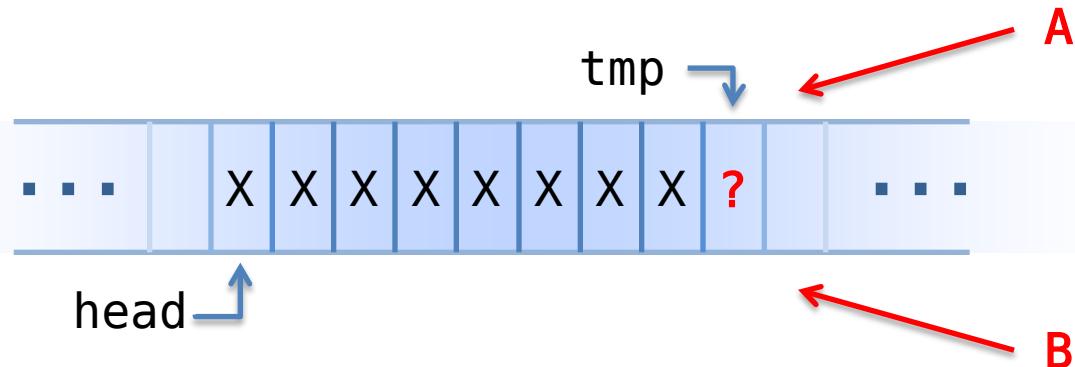
read tail  
**THEN** read buffer





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

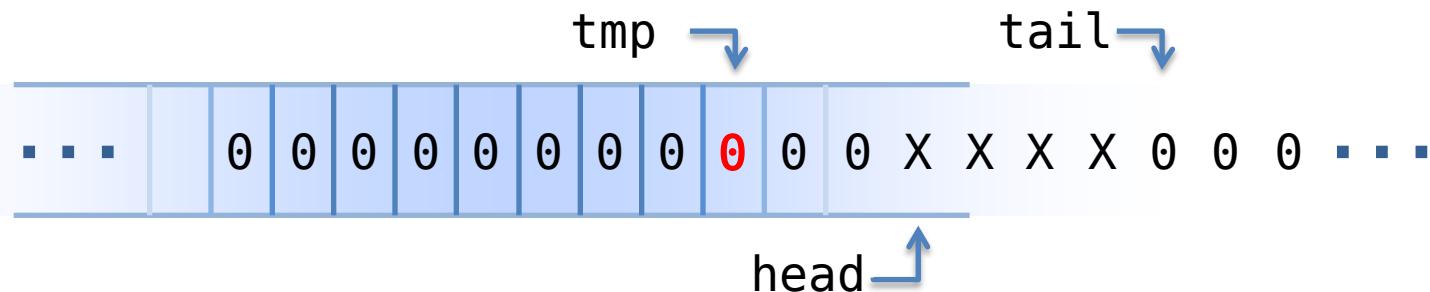
read tail  
**THEN** read buffer





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

read tail  
**THEN** read buffer





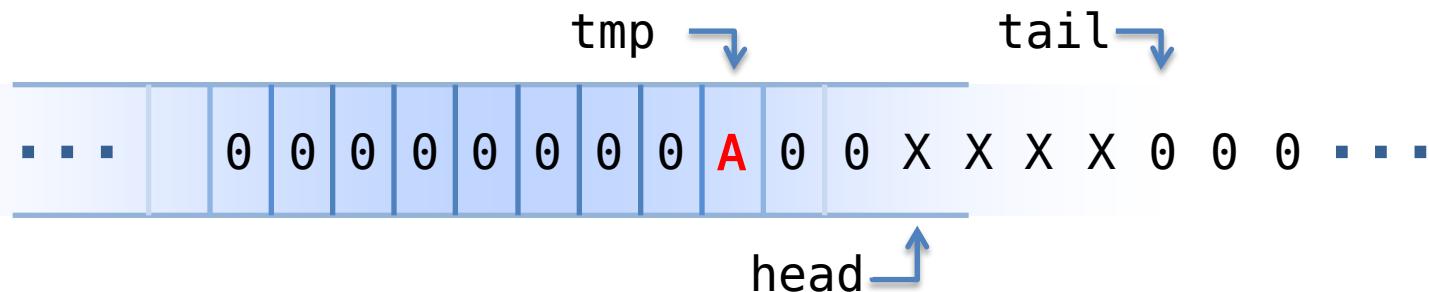
do

    tmp = tail.load();

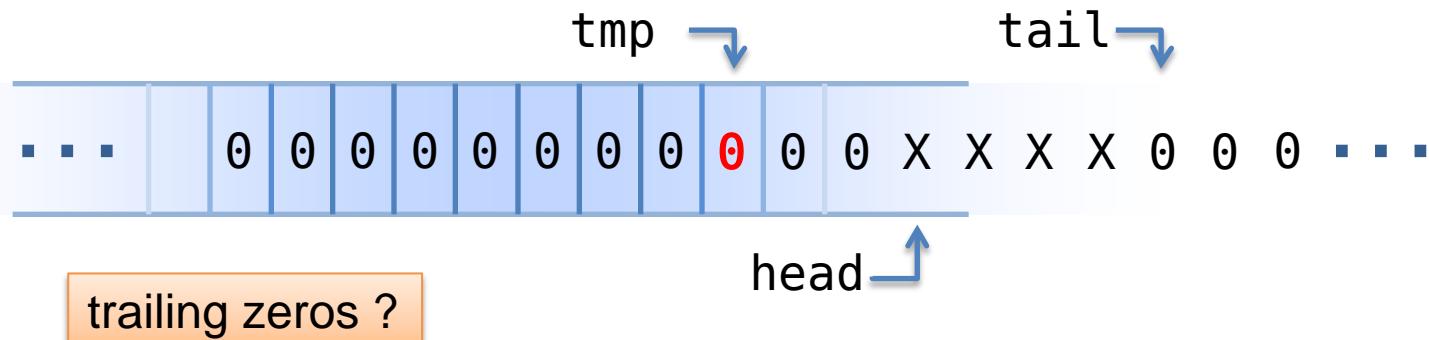
    while ( ! CAS(buffer[tmp], 0, val) );

read tail

THEN read buffer

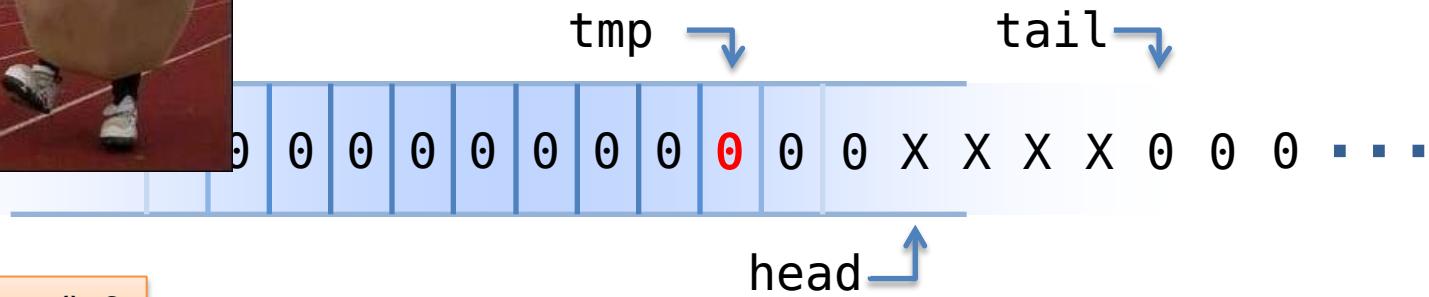


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```





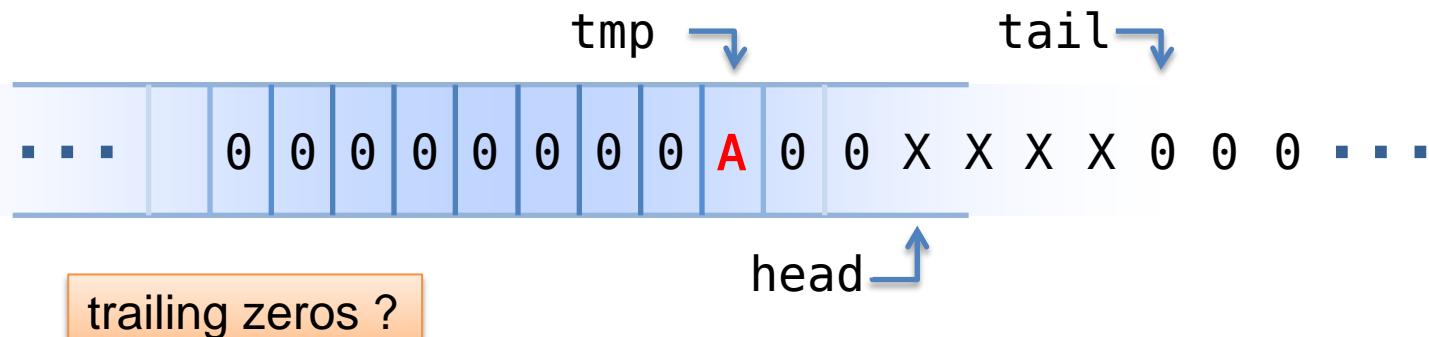
```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```



pop() ?



```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

## Compromise...

↓  
0 0 0 ...

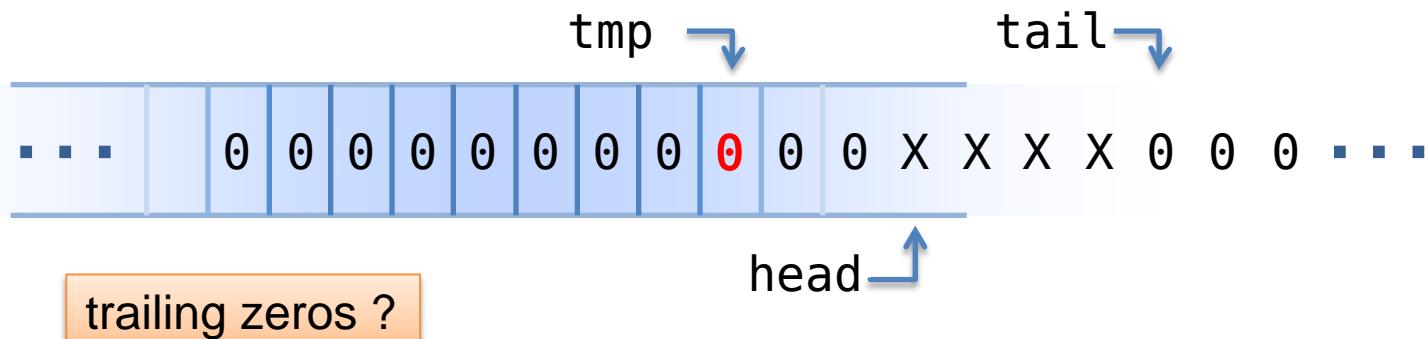
### Queue of int

-> Queue of int != 0

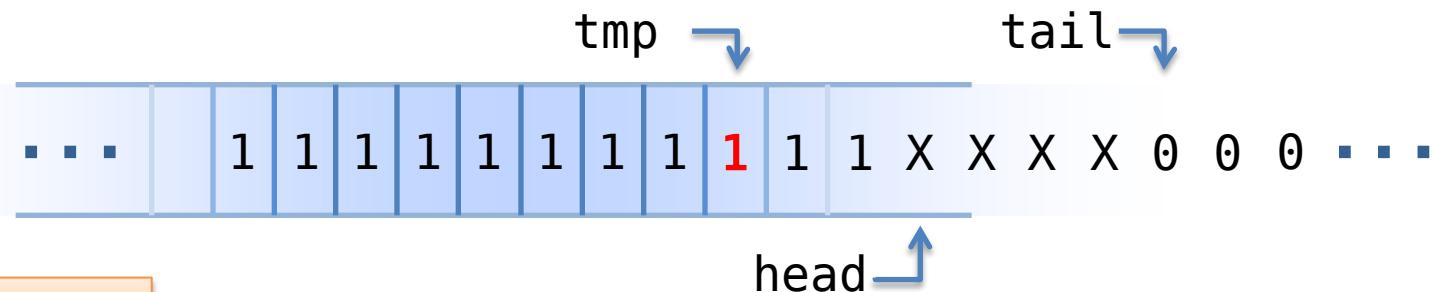
-> Queue of int != 0 or 1



```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```



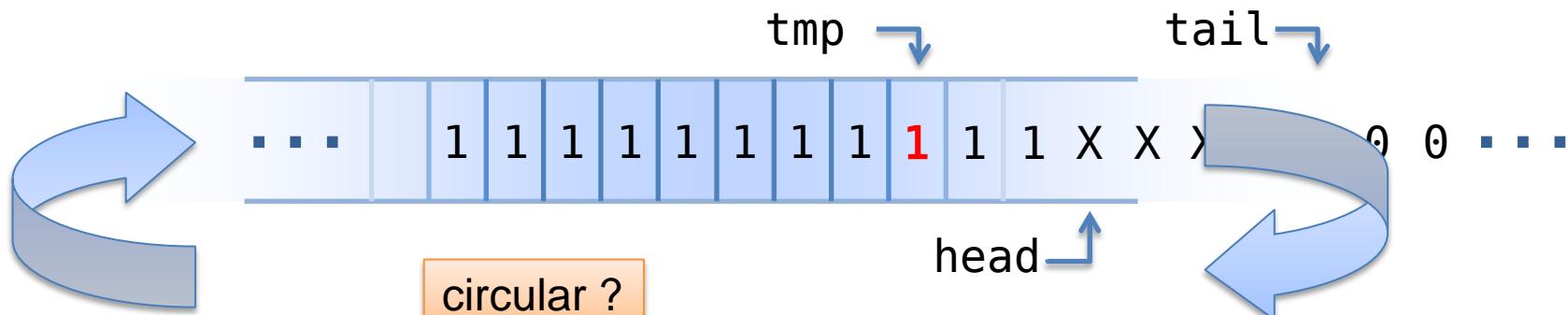
```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```



pop() ?



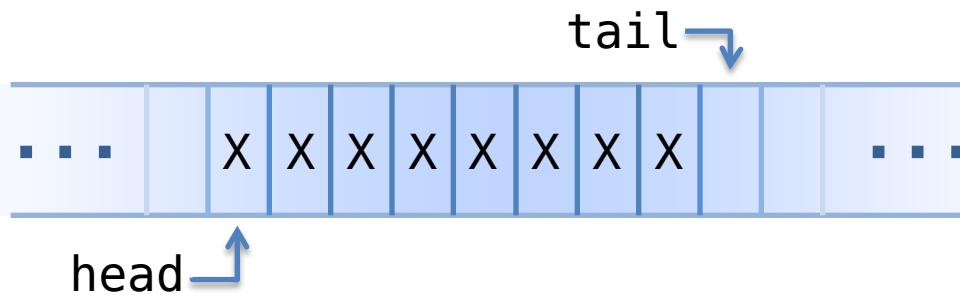
```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```





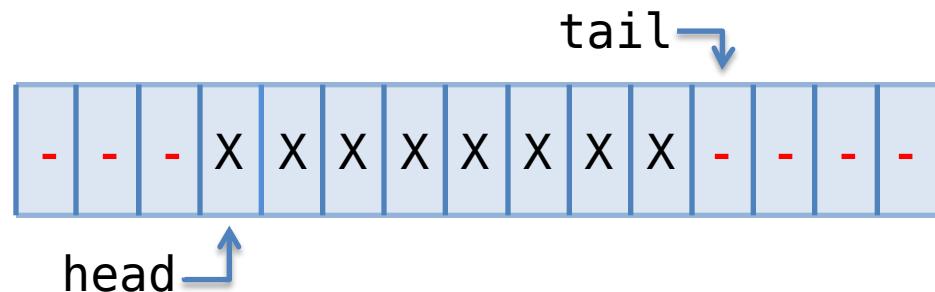


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```



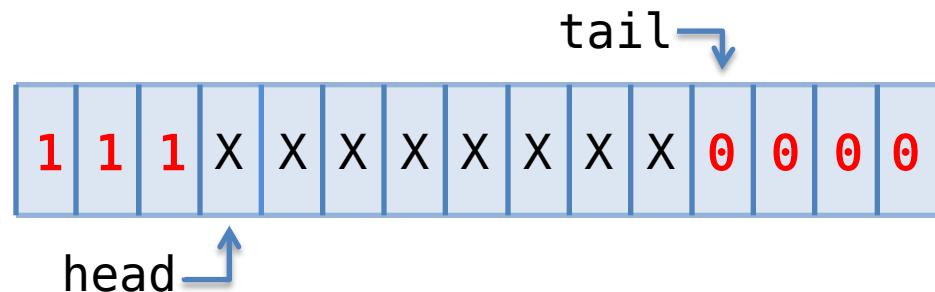


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

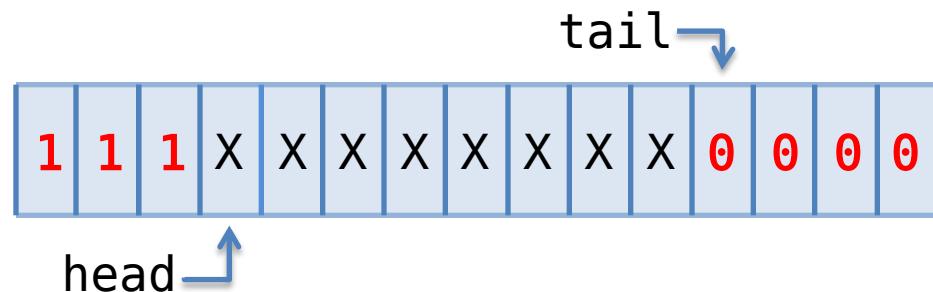




1	1	1	X	X	X	X	X	X	X	0	0	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---

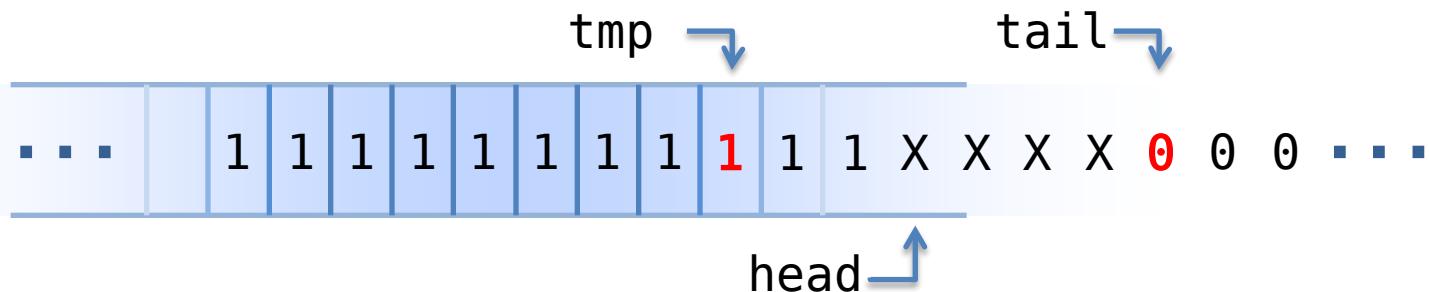


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

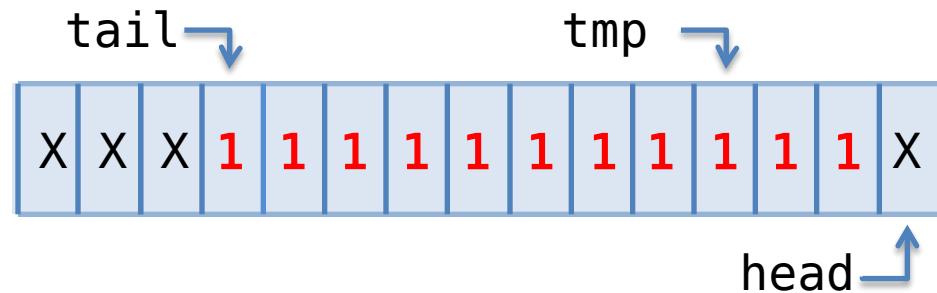




```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

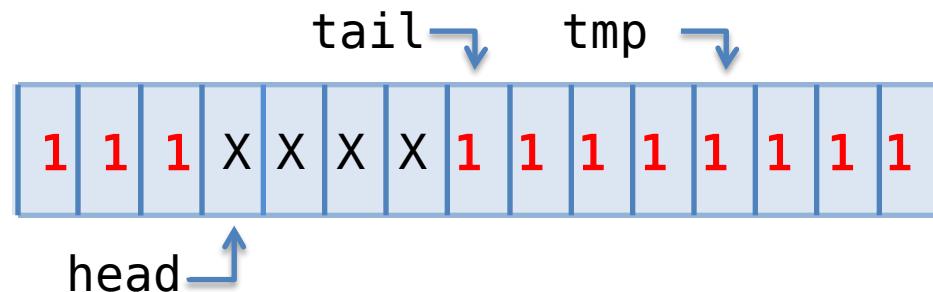


```
do
    tmp = tail.load();
while ( ! CAS(buffer[tmp], 0, val) );
```





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

# Compromise...



```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

## Compromise...

**Queue of int**

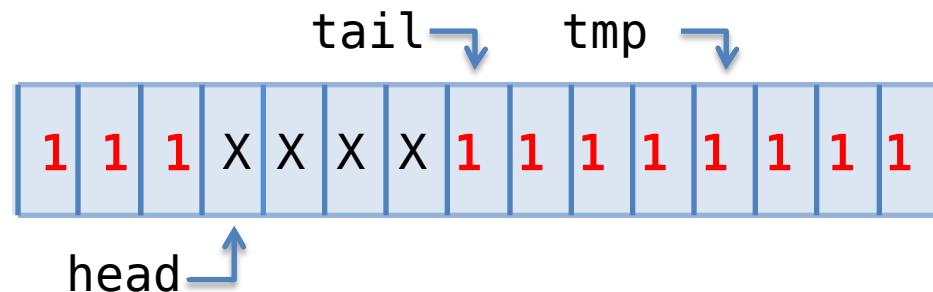
**-> Queue of int != 0**

**-> Queue of int != 0 or 1**

**-> Queue of int < 0**

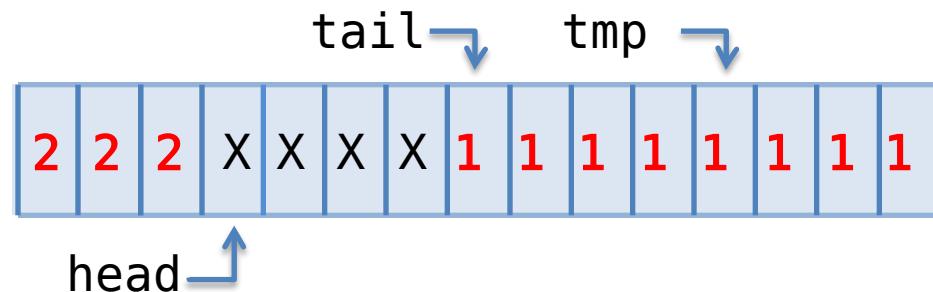


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```



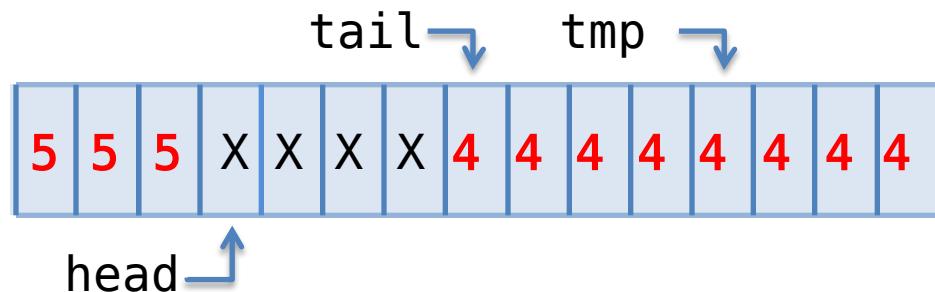


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```



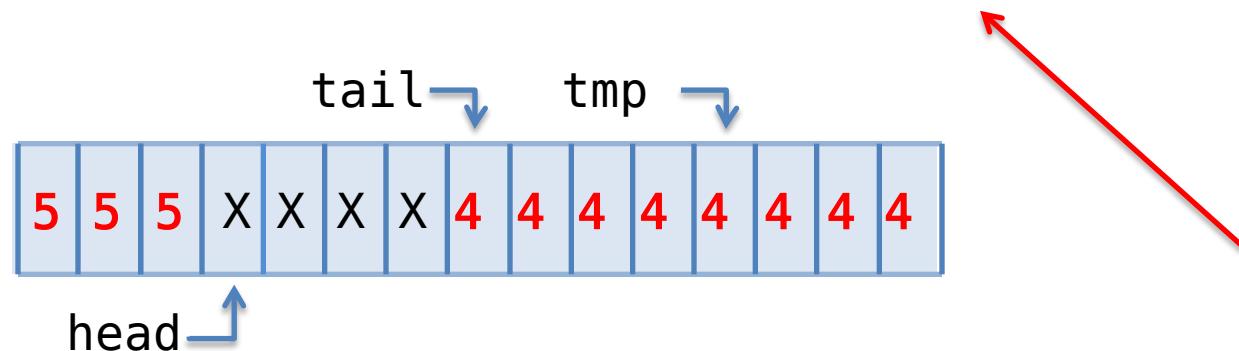


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```



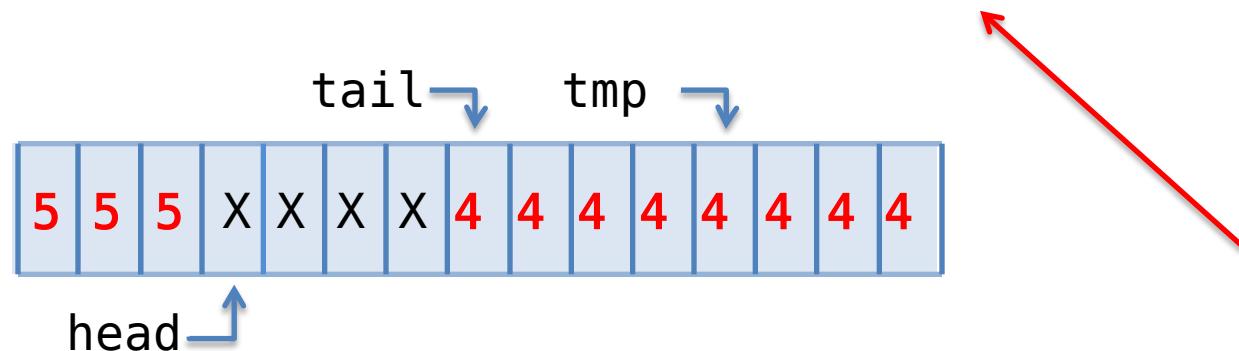


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

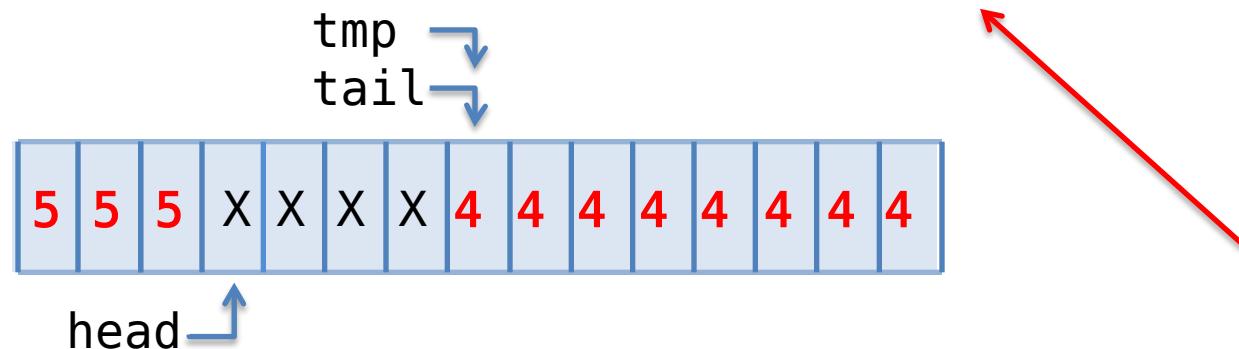




```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 0, val) );
```

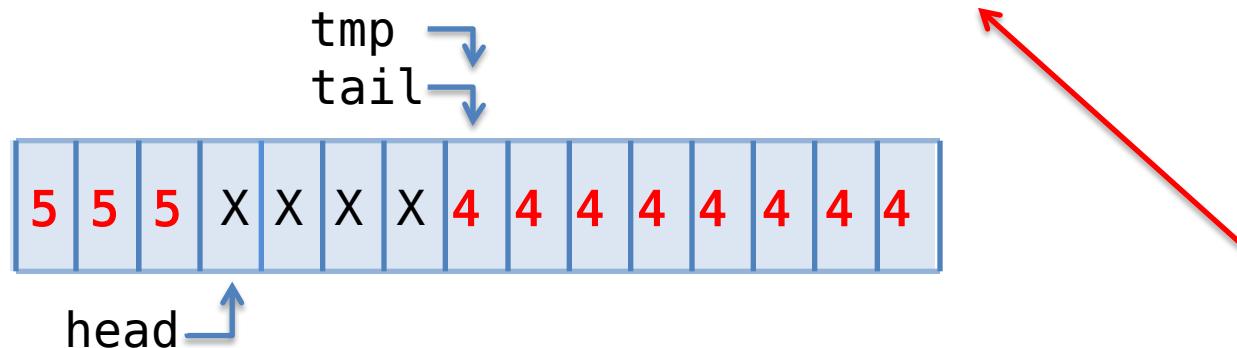


```
do
    tmp = tail.load();
while ( ! CAS(buffer[tmp], 0, val) );
```



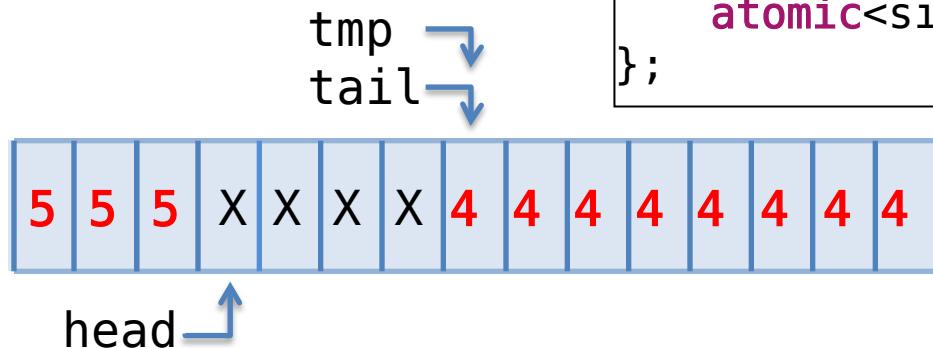


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 4, val) );
```





```
class Queue {  
    atomic<int> buffer[SZ];  
    atomic<size_t> head;  
    struct { atomic<size_t> s;  
             atomic<size_t> e;  
         } tail;  
    atomic<size_t> generation;  
};
```



# MOAR

tmp  
tail

```
class Queue {
    atomic<int> buff[SIZE];
    atomic<size_t> head;
    atomic<size_t> tail;
    atomic<size_t> generation;
};
```

# STATE

The diagram illustrates the state of a queue. At the bottom, a horizontal bar is divided into 16 blue segments. The first segment contains the value '5'. The second segment contains '4'. The third segment contains 'X'. The fourth segment contains '4'. The fifth through eighth segments contain '4'. The ninth through twelfth segments are empty. The thirteenth through sixteenth segments are also empty. A blue arrow labeled 'head' points to the boundary between the first and second segments. A blue arrow labeled 'tail' points to the boundary between the third and fourth segments.

# MOAR

do

tmp  
tail

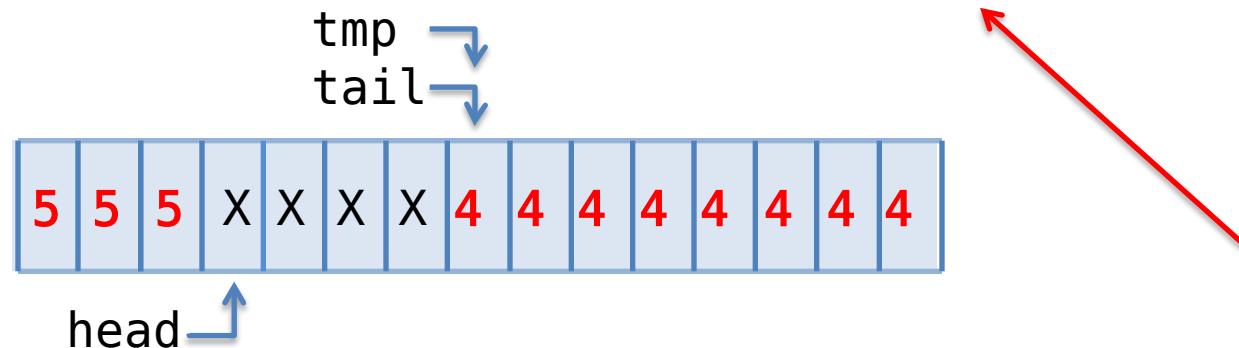
```
class Queue {
    atomic<int> buf[SZ];
    atomic<size_t> head;
    atomic<size_t> tail;
    atomic<size_t> generation;
};
```

# THEN

The diagram shows a horizontal array of 16 blue squares representing memory cells. The first cell contains the value '5'. The next two cells contain 'X'. The fourth cell contains '4' and is labeled 'head'. The fifth cell contains '4'. The last cell contains '4'. Blue arrows point from the labels 'tmp' and 'tail' to the second and third cells respectively.

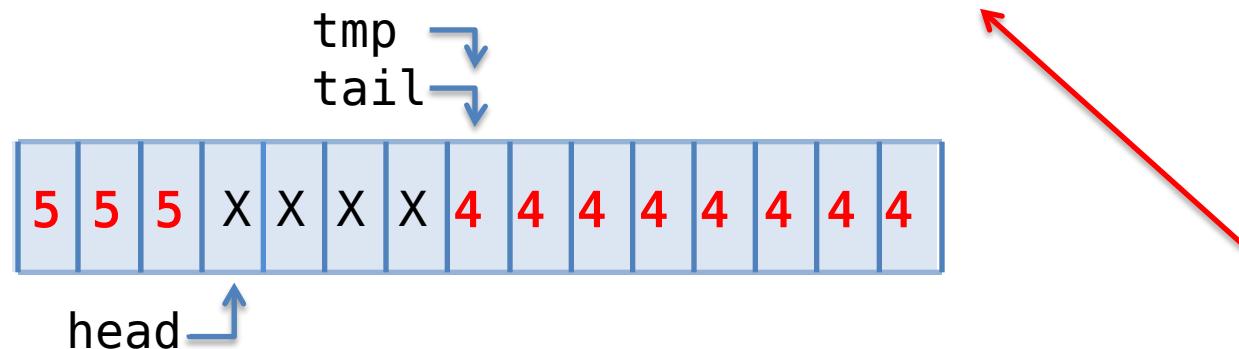


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], 4, val) );
```





```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```



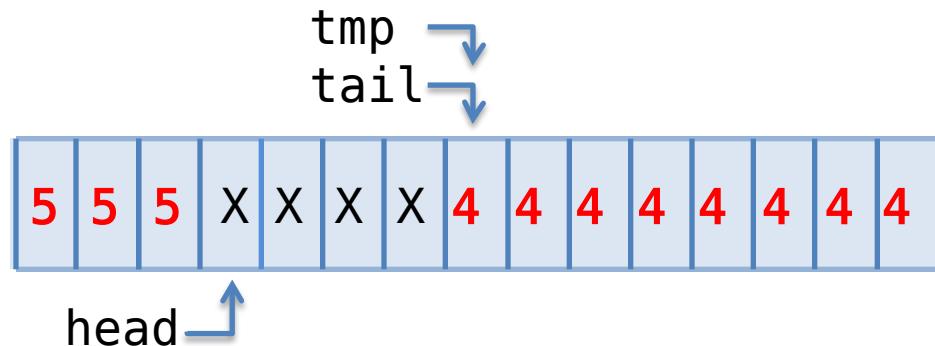
```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```

tmp 

Compromise...

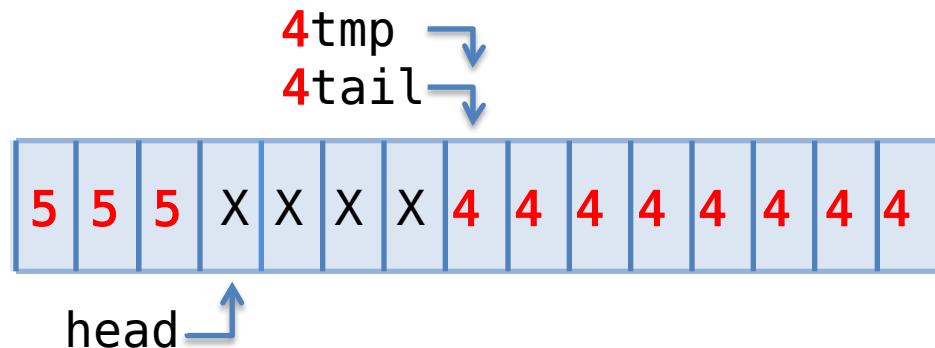


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```





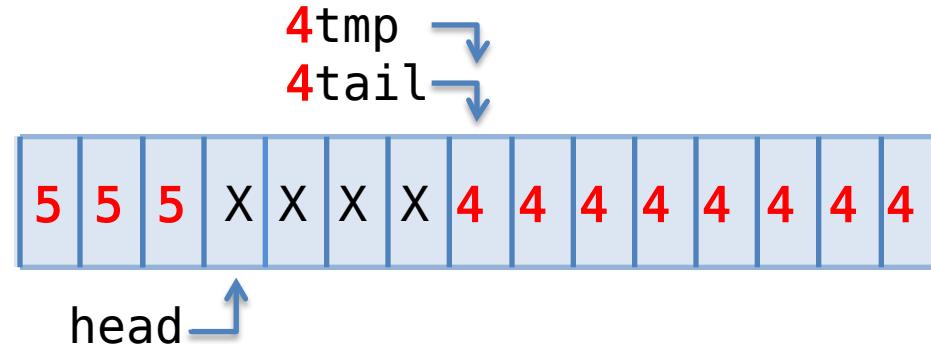
```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```





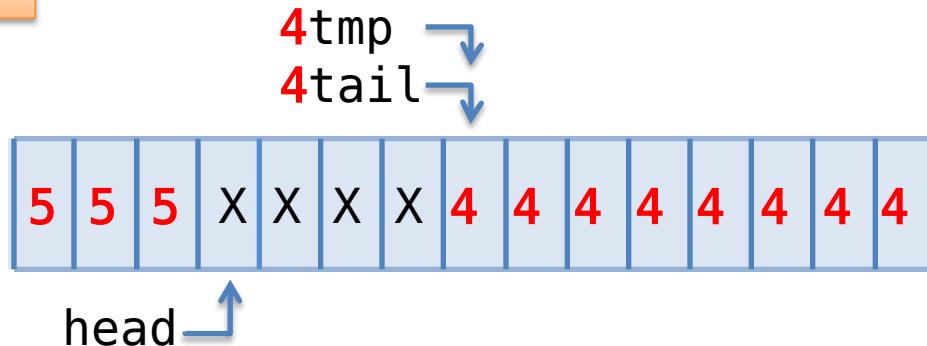
```
class index {  
    size_t value; // gen | idx  
    size_t generation();  
    operator size_t();  
    index& operator++();  
    //etc  
};
```

```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```

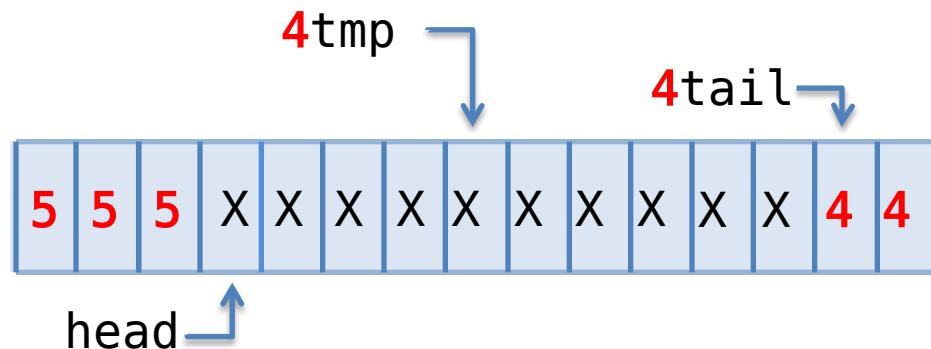


snapshot

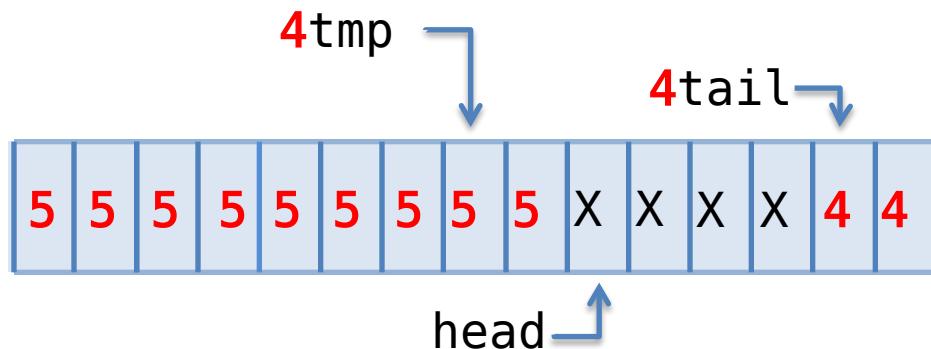
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );



```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```



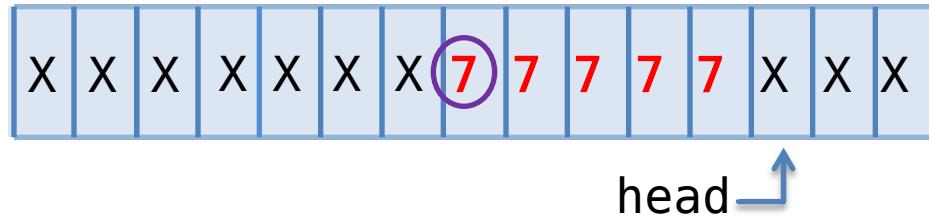
```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```





do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );

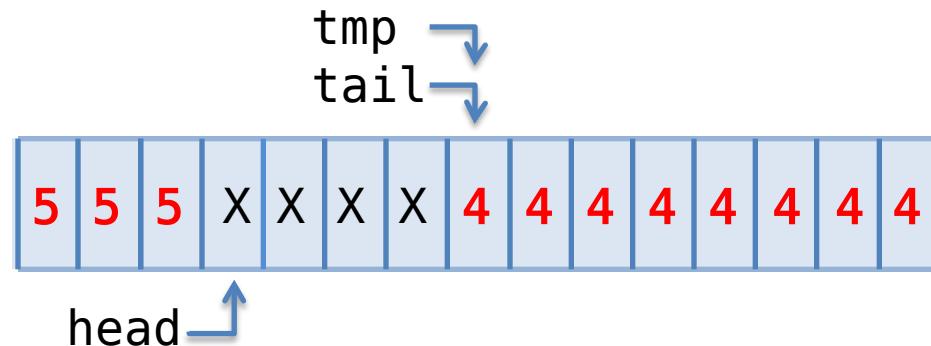
4 tmp  
7 tail



All states are valid states for all lines of code (\*)

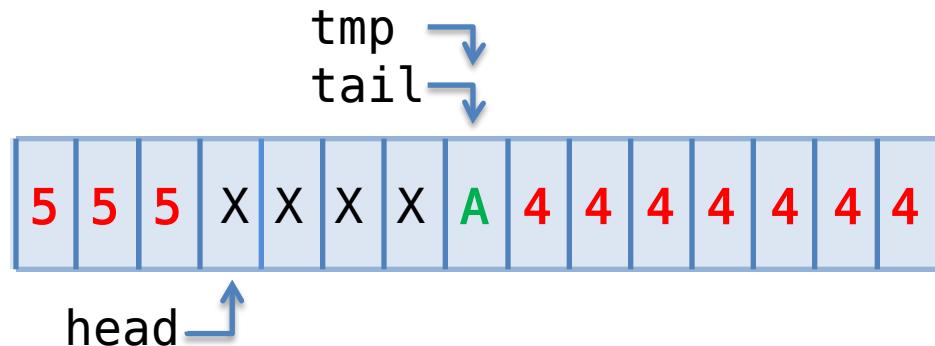


```
do
    tmp = tail.load();
while ( ! CAS(buffer[tmp], gen(tmp), val) );
```



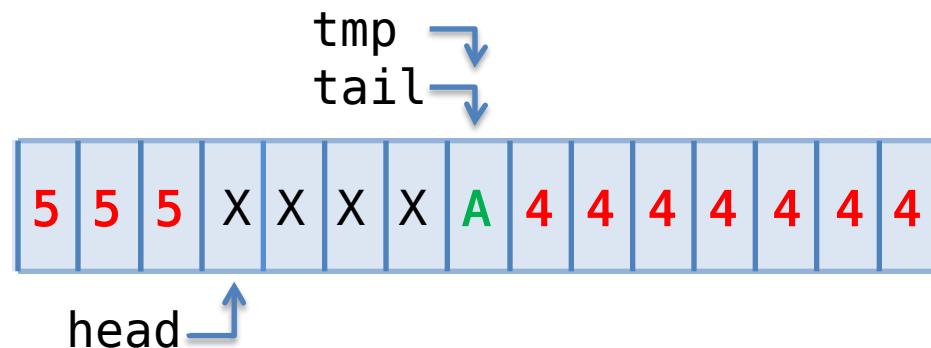


```
do  
    tmp = tail.load();  
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
```



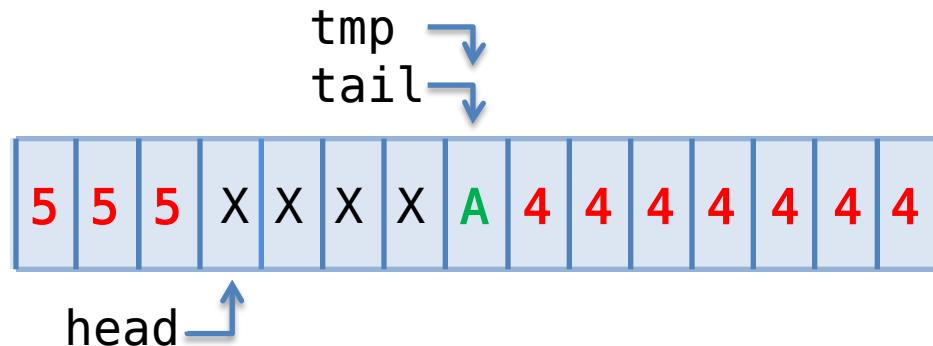


```
do
    tmp = tail.load();
while ( ! CAS(buffer[tmp], gen(tmp), val) );
tail++; //???
```





```
do
    tmp = tail.load();
    while ( ! CAS(buffer[tmp], gen(tmp), val) );
tail++; //???
```





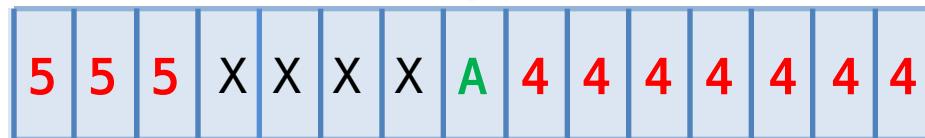
spinlock ?

do

    tmp = tail.load();

    while ( ! **CAS**(buffer[tmp], gen(tmp), val) );  
        tail++; //???

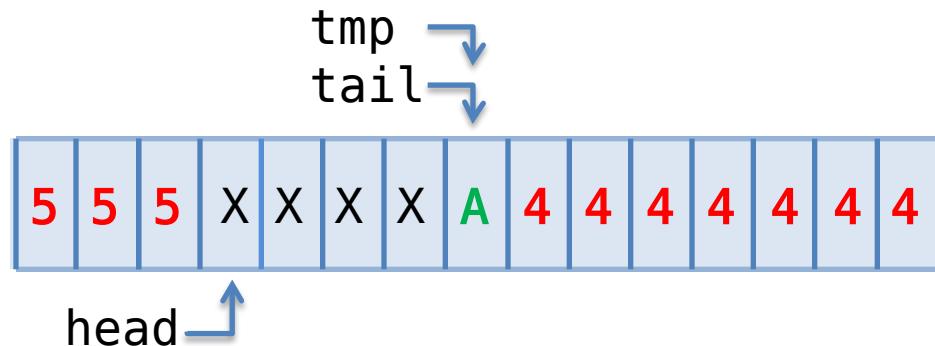
tmp  
tail



head



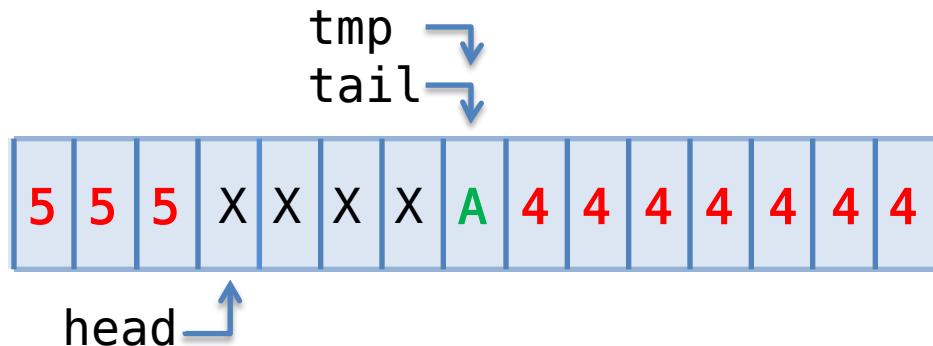
```
do {  
    tmp = tail.load();  
    while (buffer[tmp] != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
tail++; // yes!
```





```
do {  
    tmp = tail.load();  
    while (buffer[tmp] != gen(tmp))  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
tail++; // yes!
```

same





```
do {  
    tmp = tail.load();  
    while (buffer[tmp] != gen(tmp))  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
tail++; // yes!
```

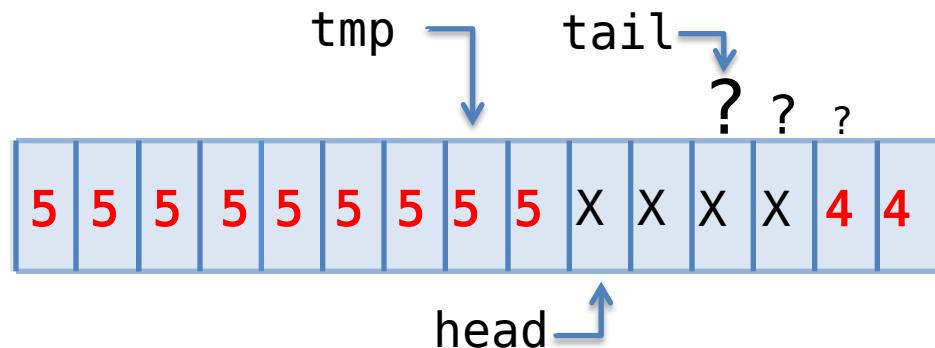
same

tmp ↗ tail ↘

Sorry Herb...

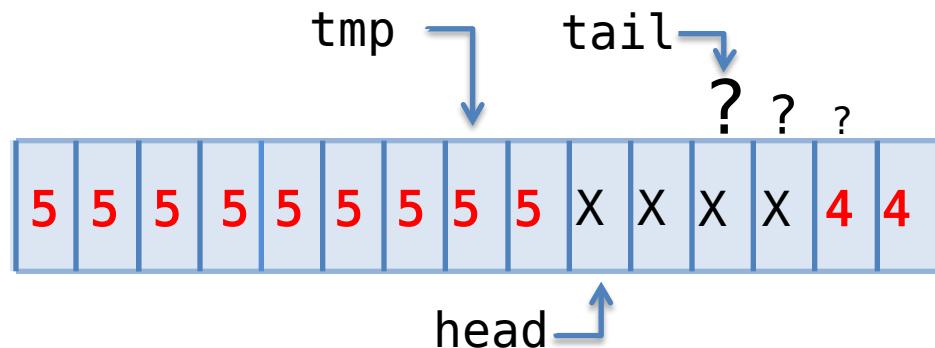


```
do {  
    tmp = tail.load(memory_order_relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
tail++; // yes!
```



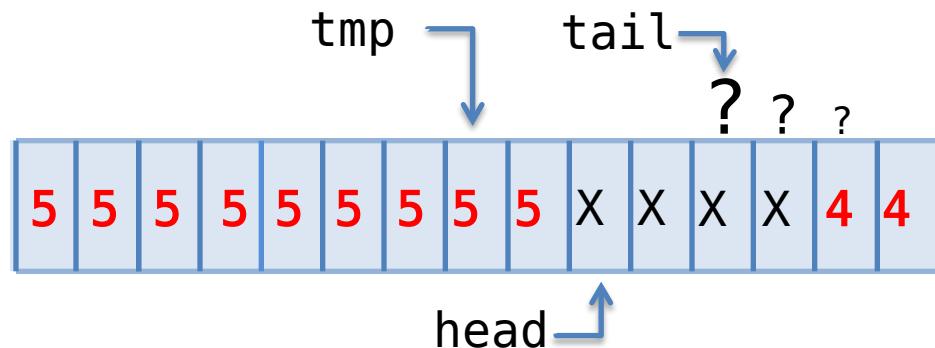


```
do {  
    tmp = tail.load(memory_order_relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
tail = tmp + 1;
```





```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```





do {

tmp = **oldtail** = tail.load(relaxed);

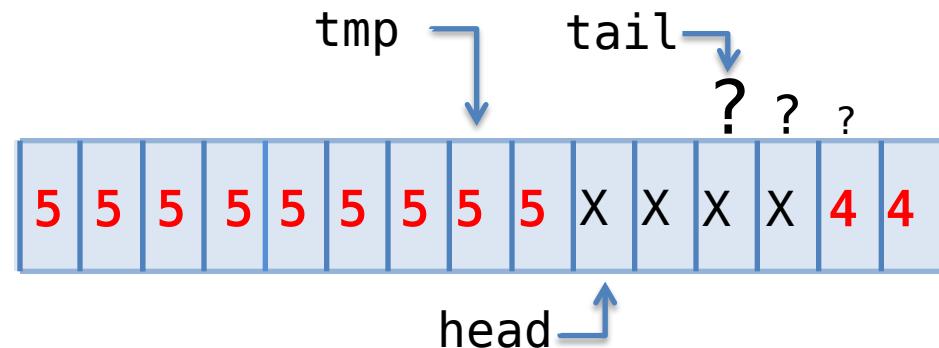
while (buffer[tmp].load(relaxed) != gen(tmp))

tmp++;

} while ( ! CAS(buffer[tmp], gen(tmp), val) );

**CAS(tail, oldtail, tmp+1);**

ABA?

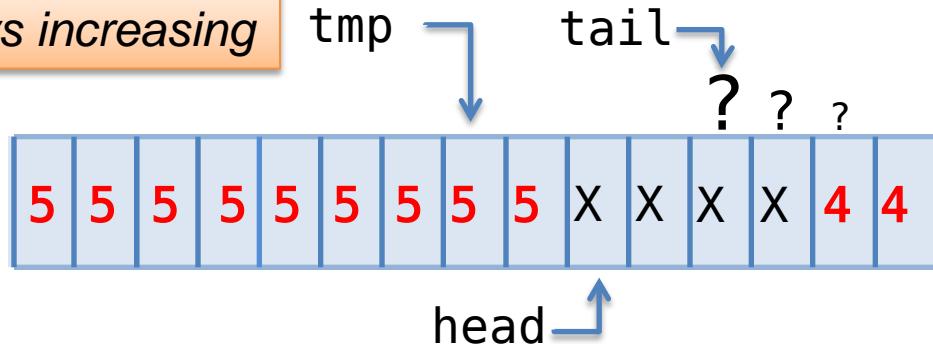




ABA?

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

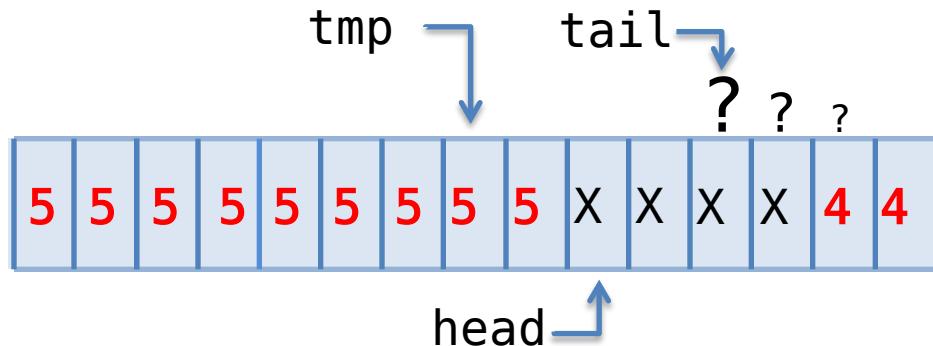
*ensure tail is always increasing*





```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

Is tail up to date “now”? →





```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

Is tail up to date “now”? →

tmp = tail ↓

? ? ?

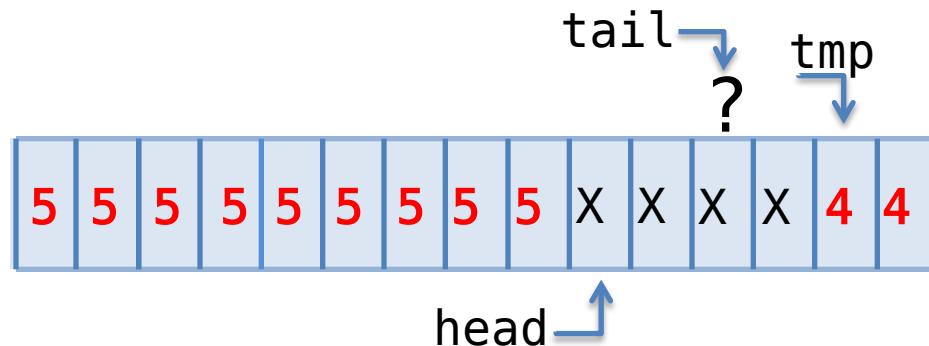


head ↑



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

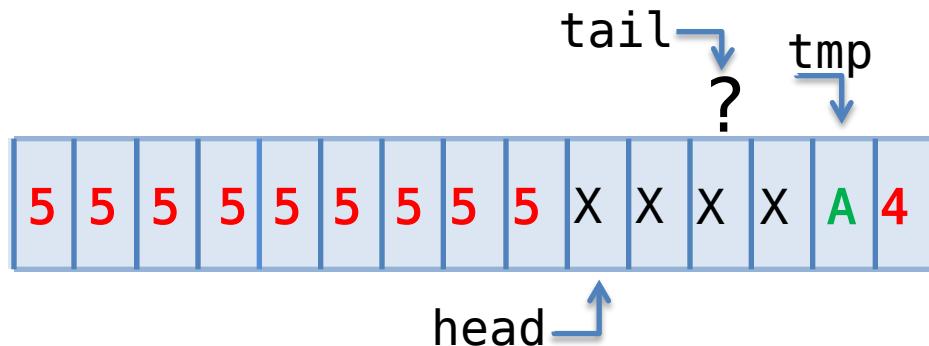
Is tail up to date “now”? →





```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

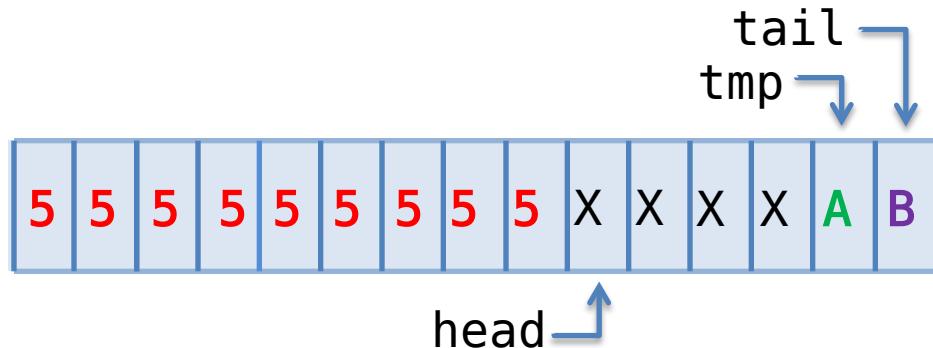
Is tail up to date “now”?





```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

Is tail up to date “now”? →



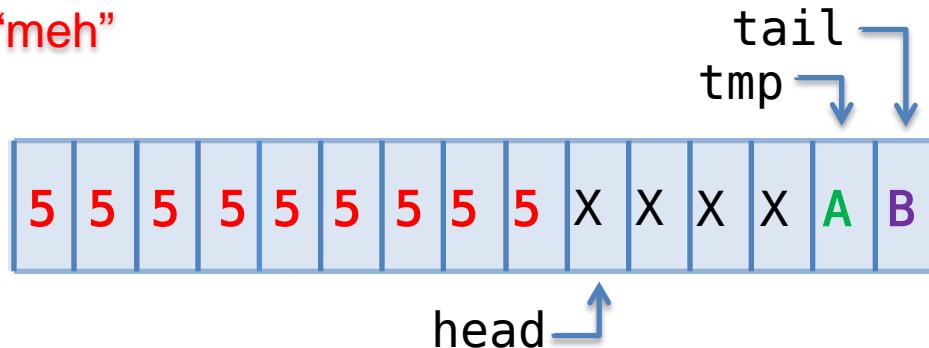


```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

Is tail up to date “now”?



“meh”

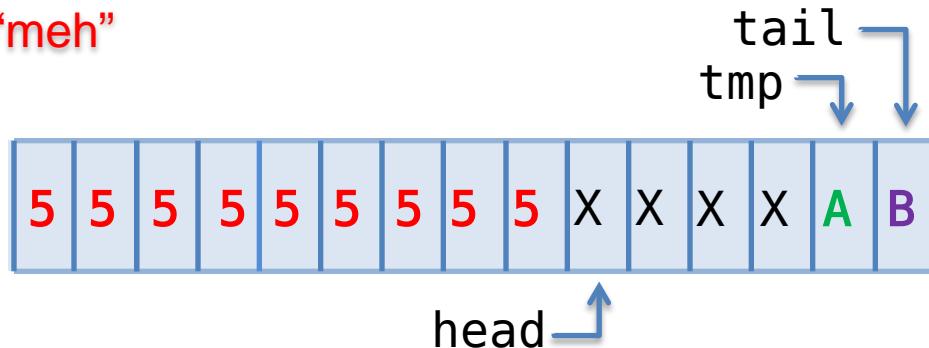




```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1, relaxed);
```

Is tail up to date “now”? →

“meh”



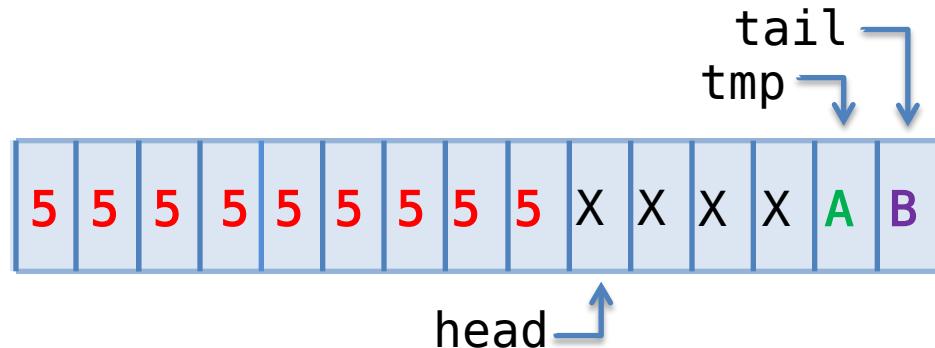


push(val)



do {

```
tmp = oldtail = tail.load(relaxed);
while (buffer[tmp].load(relaxed) != gen(tmp))
    tmp++;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



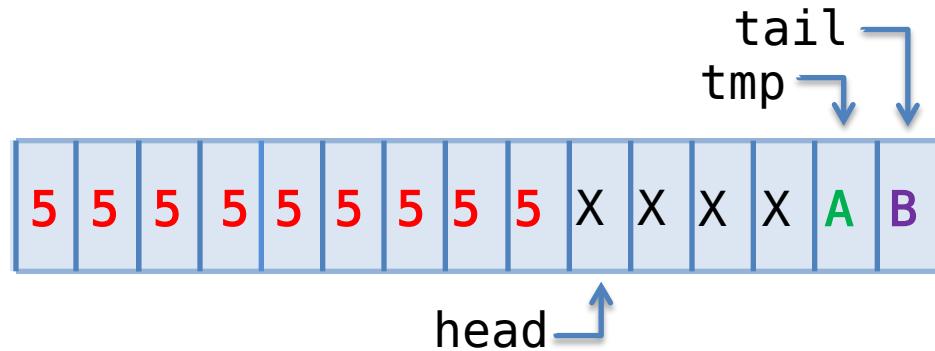


push(val)



do {

```
tmp = oldtail = tail.load(relaxed);
while (buffer[tmp].load(relaxed) != gen(tmp))
    tmp++;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



push(val)



do {

```
tmp = oldtail = tail.load(relaxed);
while (buffer[tmp].load(relaxed) != gen(tmp))
    tmp++;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?

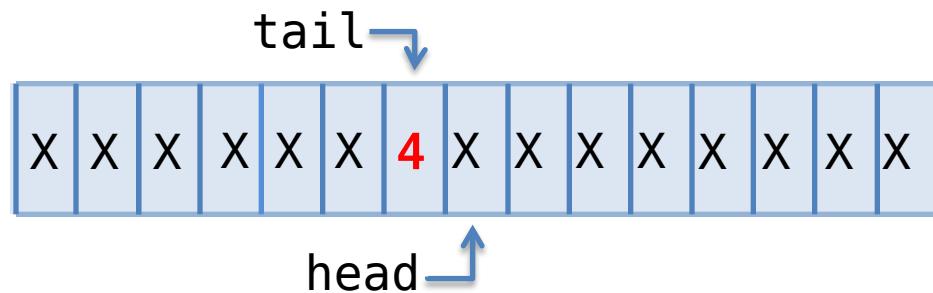


push(val)



do {

```
tmp = oldtail = tail.load(relaxed);
while (buffer[tmp].load(relaxed) != gen(tmp))
    tmp++;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?

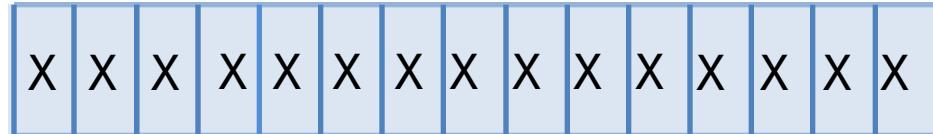


push(val)



do {

```
tmp = oldtail = tail.load(relaxed);
while (buffer[tmp].load(relaxed) != gen(tmp))
    tmp++;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?

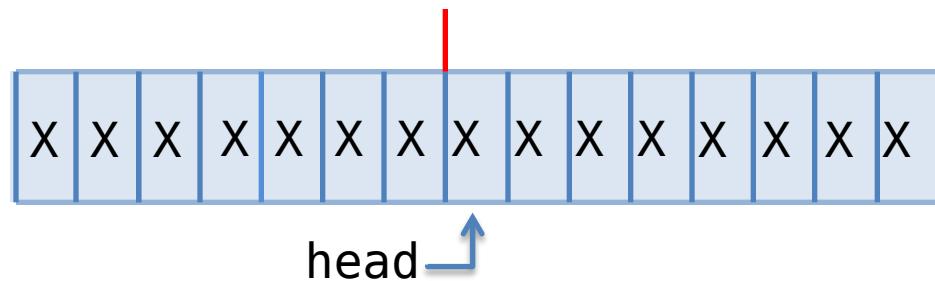


push(val)



do {

```
tmp = oldtail = tail.load(relaxed);
while (buffer[tmp].load(relaxed) != gen(tmp))
    tmp++;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



push(val)



do {

```
tmp = oldtail = tail.load(relaxed);
while (buffer[tmp].load(relaxed) != gen(tmp))
    tmp++;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

tail

? ? | ? ?



All states are valid states for all lines of code?

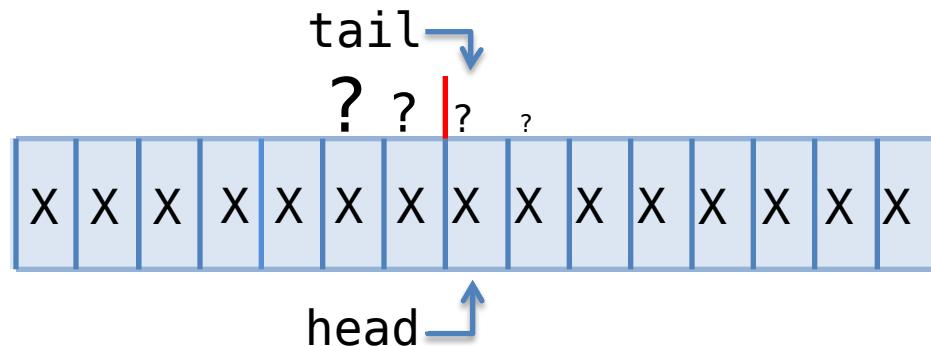


push(val)



do {

```
tmp = oldtail = tail.load(relaxed);
while (buffer[tmp].load(relaxed) != gen(tmp))
    tmp++;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



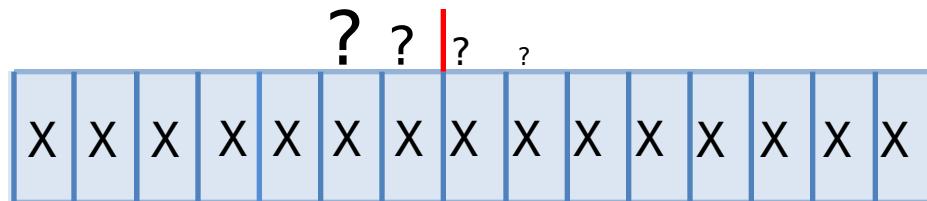
push(val)



do {

```
tmp = oldtail = tail.load(relaxed);
while (buffer[tmp].load(relaxed) != gen(tmp))
    tmp++;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

tail



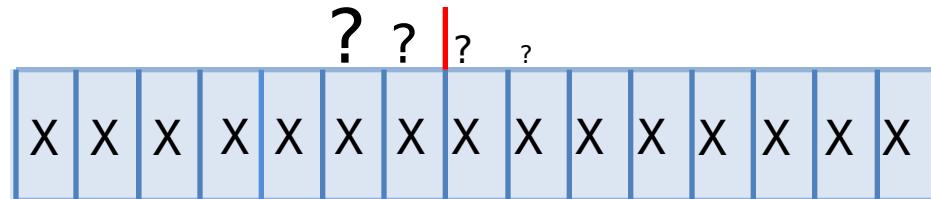
All states are valid states for all lines of code?



(worse?) spinlock ?

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
    CAS(tail, oldtail, tmp+1);
```

tail



All states are valid states for all lines of code?

(worse?) spinlock ?

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
    CAS(tail, oldtail, tmp+1);
```

tail

Compromise...

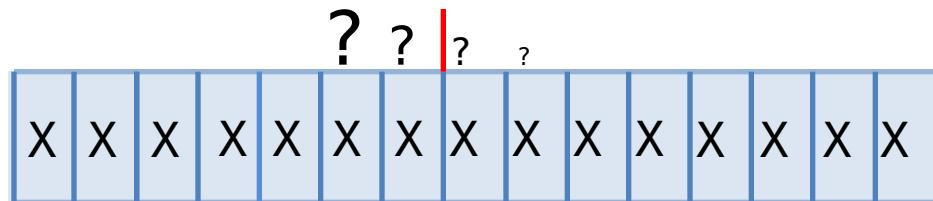
All states are valid states for all lines of code?



(worse?) spinlock ?  
overflow ?

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp].load(relaxed) != gen(tmp))  
        tmp++;  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

tail

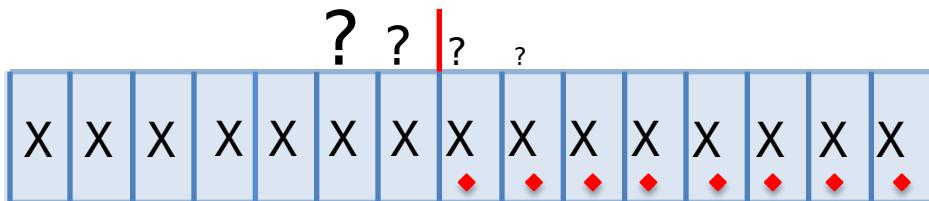


All states are valid states for all lines of code?



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    g = gen(tmp);  
    while ((b = buffer[tmp]) != g && odd(g)==odd(b))  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val | odd(gen)) );  
    CAS(tail, oldtail, tmp+1);
```

4tail



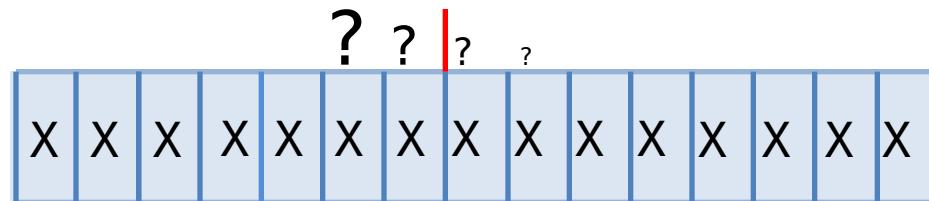
All states are valid states for all lines of code?



spinlock on full ?

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
    CAS(tail, oldtail, tmp+1);
```

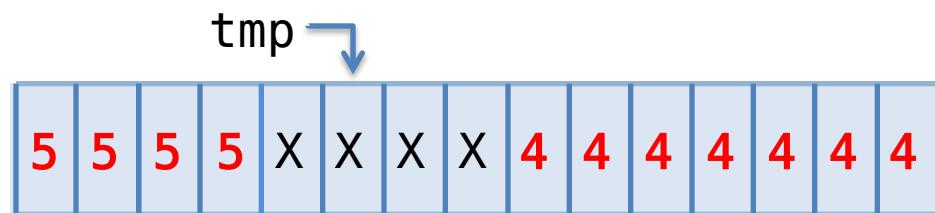
4tail



All states are valid states for all lines of code?



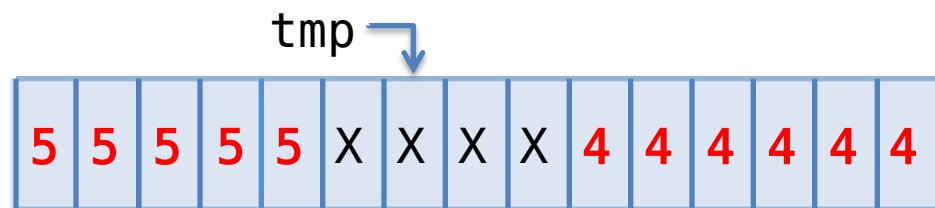
```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



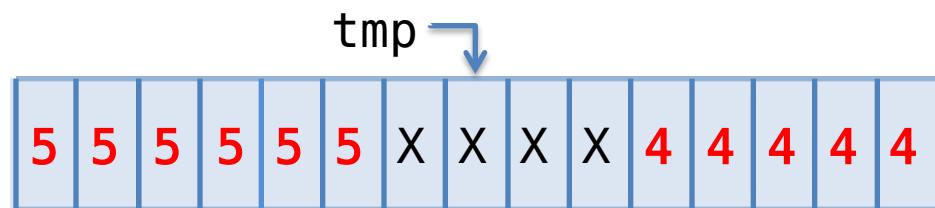
```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



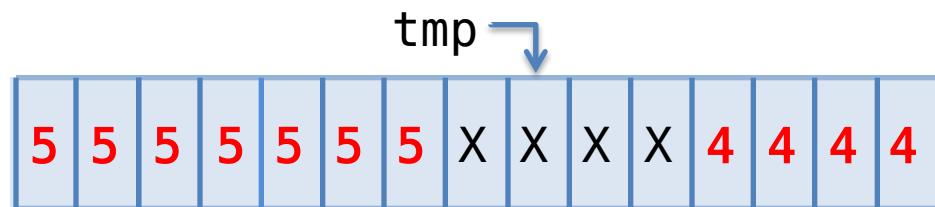
```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



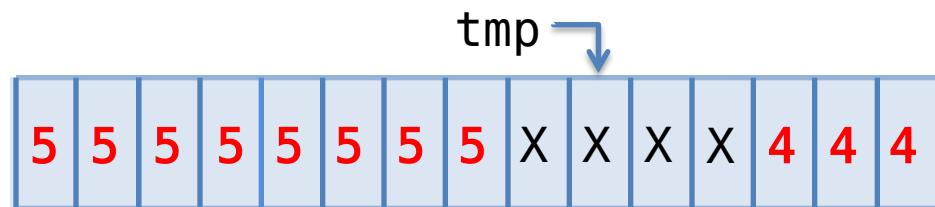
```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?



```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```

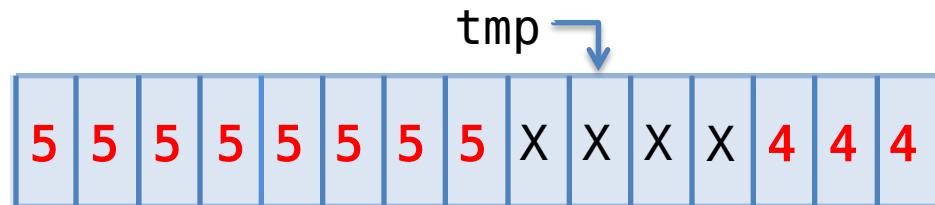


All states are valid states for all lines of code?



spinlock **NOT** full ?

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    while (buffer[tmp] != gen(tmp) && tmp - oldtail < size)  
        tmp++;  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
    CAS(tail, oldtail, tmp+1);
```

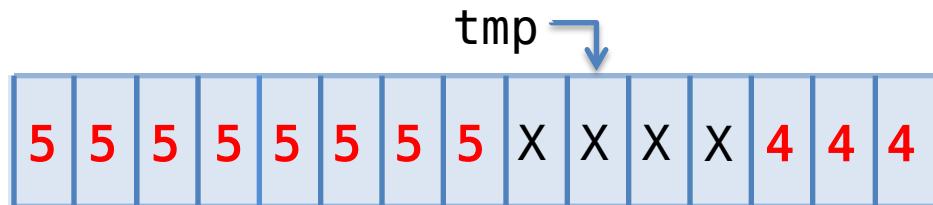


All states are valid states for all lines of code?



“fullish” →

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

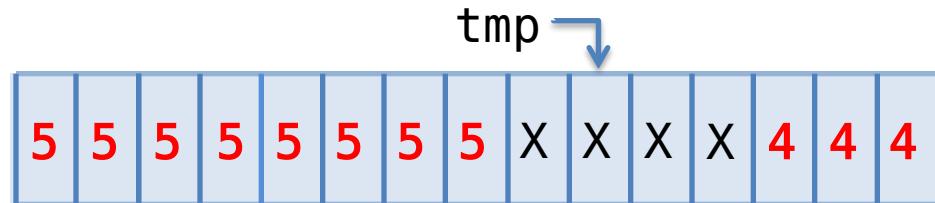


All states are valid states for all lines of code?



```
if (some_state)
{
    // still some_state???
    ...
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

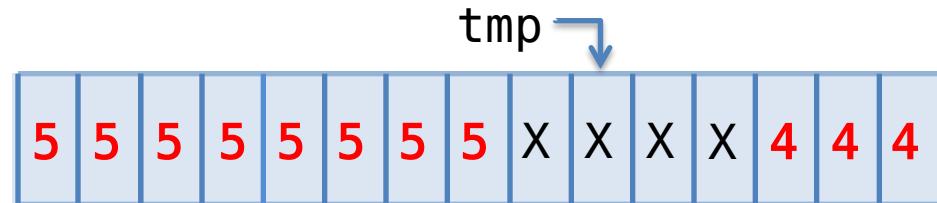


All states are valid states for all lines of code?



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

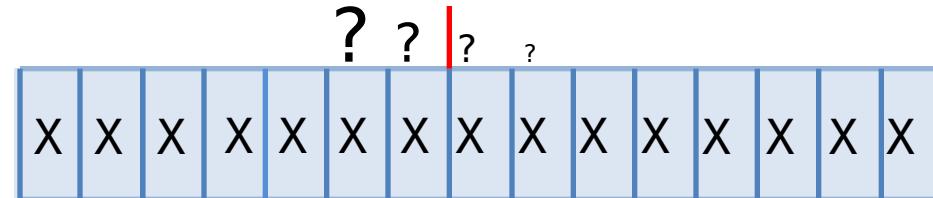
```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?

```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

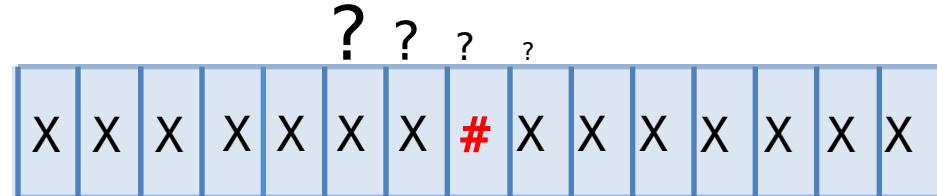


All states are valid states for all lines of code?



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

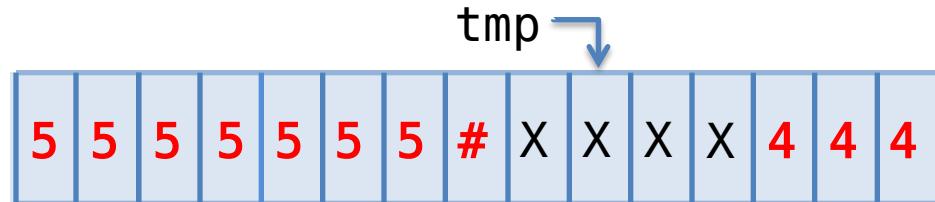


All states are valid states for all lines of code?



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

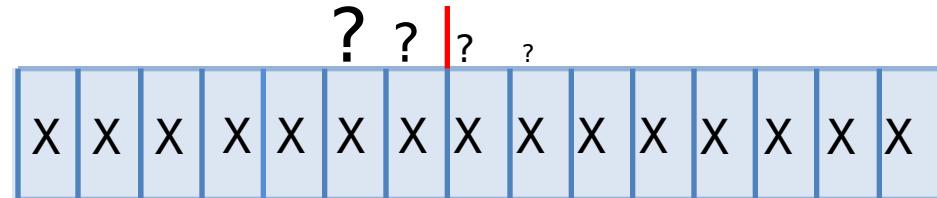
```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?

```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

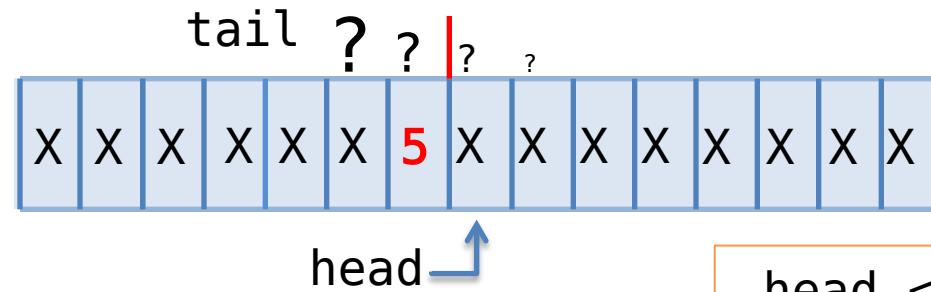


All states are valid states for all lines of code?



```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

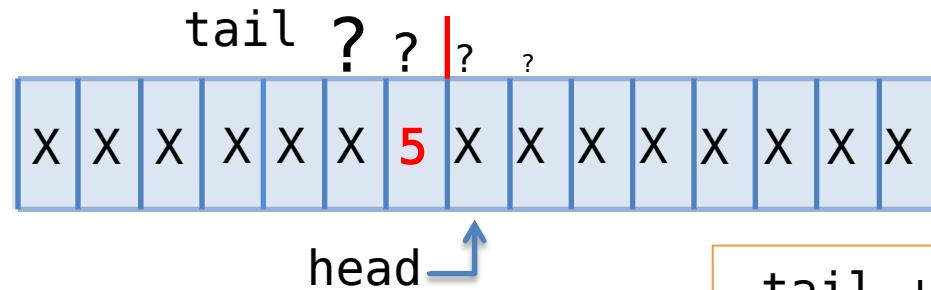


All states are valid states for all lines of code?

head < tail ?

```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

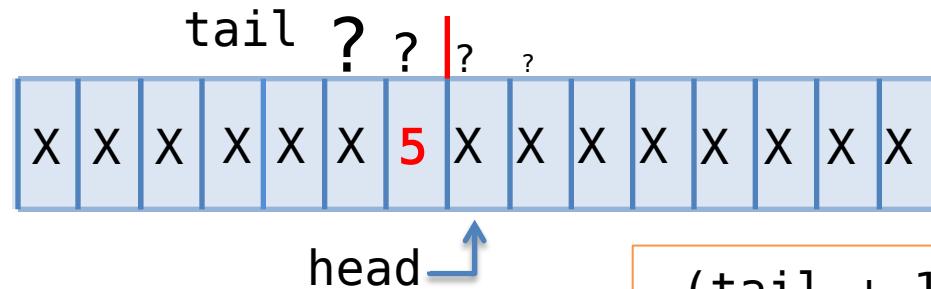


tail + 1 != head?

All states are valid states for all lines of code?

```
if (full)
{
    // still full???
    // or now empty?
    ...
}
```

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

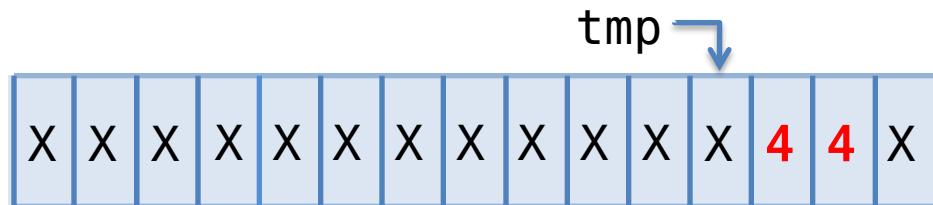


All states are valid states for all lines of code?

$(tail + 1)\%SZ \neq head\%SZ$  ?

“fullish” →

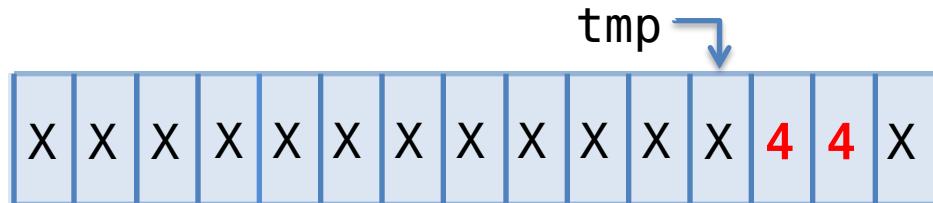
```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) ...???;
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?

“fullish” →

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) wait_for_space();
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

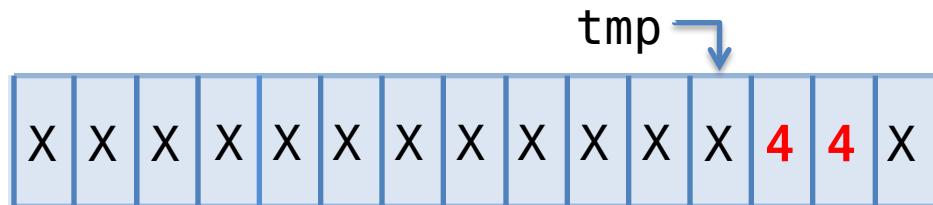


All states are valid states for all lines of code?



“fullish” →

```
do {
    tmp = oldtail = tail.load(relaxed);
    tmp = find_tail(tmp, &oldtail);
    if (tmp == FULL) { wait_for_space(); continue; }
} while ( ! CAS(buffer[tmp], gen(tmp), val) );
CAS(tail, oldtail, tmp+1);
```

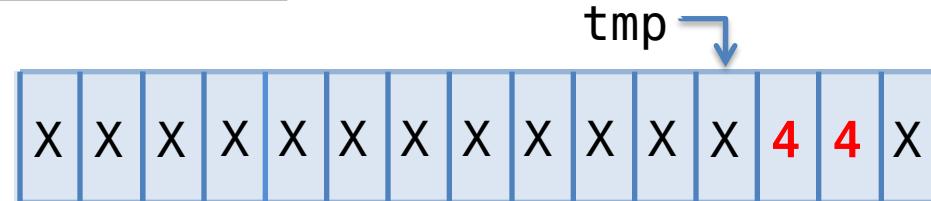


All states are valid states for all lines of code?



```
wait_for_space()  
{  
    unique_lock lock(mutex);  
  
    while (still_fullish())  
        cond_full.wait(lock);  
}
```

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    tmp = find_tail(tmp, &oldtail);  
    if (tmp == FULL) { wait_for_space(); continue; }  
} while ( ! CAS(buffer[tmp], gen(tmp), va) );  
CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?

# Lock-free by Example

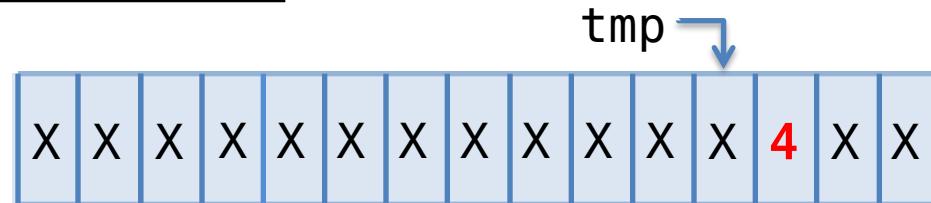
(one very complicated example)

Tony Van Eerd  
C++Now, 2015



```
{  
    unique_lock lock(mutex);  
  
    while (still_fullish())  
        cond_full.wait(lock);  
}
```

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    tmp = find_tail(tmp, &oldtail);  
    if (tmp == FULL) { wait_for_space(); continue; }  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
    CAS(tail, oldtail, tmp+1);
```

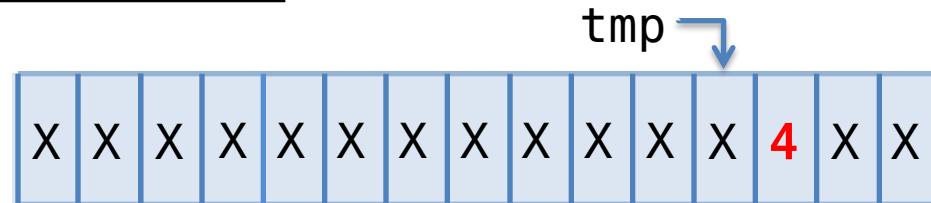


All states are valid states for all lines of code?



```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```

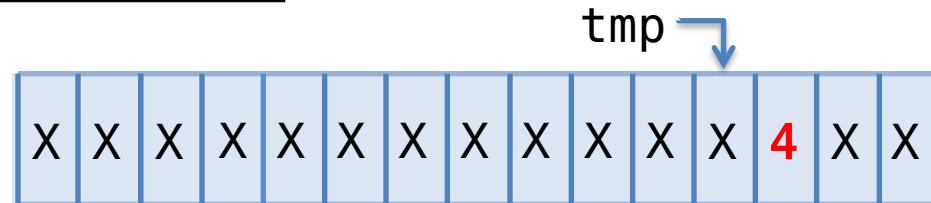
```
do {  
    tmp = oldtail = tail.load(relaxed);  
    tmp = find_tail(tmp, &oldtail);  
    if (tmp == FULL) { wait_for_space(); continue; }  
    } while ( ! CAS(buffer[tmp], gen(tmp), val) );  
    CAS(tail, oldtail, tmp+1);
```



All states are valid states for all lines of code?

```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```

```
do {  
    tmp = oldtail = tail.load(relaxed);  
    tmp = find_tail(tmp, &oldtail);  
    if(tmp == FULL) wait_for_space(&tmp,&oldtail);  
} while ( ! CAS(buffer[tmp], gen(tmp), val) );  
CAS(tail, oldtail, tmp+1);
```



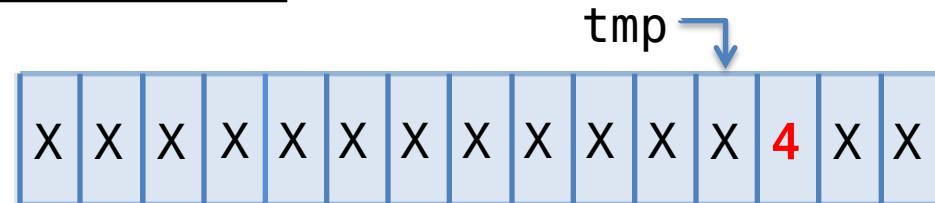
All states are valid states for all lines of code?



```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



who calls **notify()** “queue not full“ ?



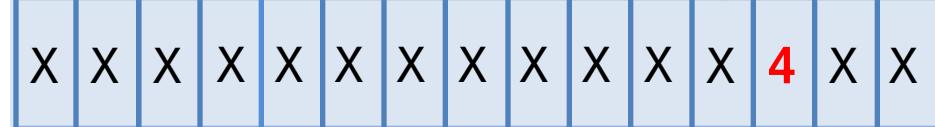


```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



who calls **notify()** “queue not full“ ?

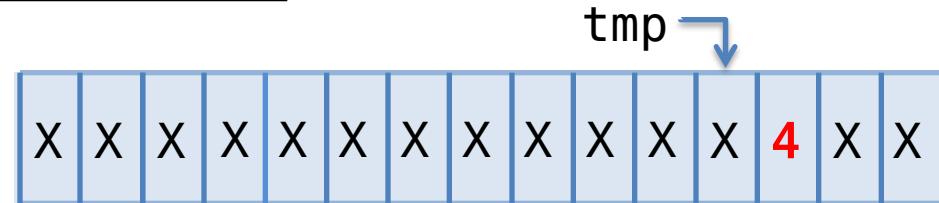
tmp ↴



```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



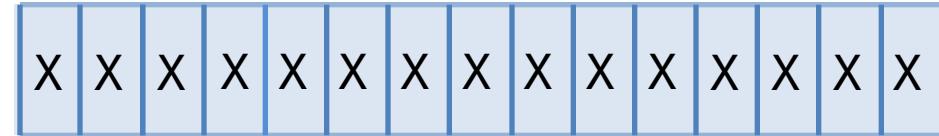
```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
int pop() {  
    ...  
    unique_lock lock(mutex);  
    cond_full.notify();  
}
```



```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
int pop() {  
    ...  
    unique_lock lock(mutex);  
    cond_full.notify();  
}
```



```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
int pop() {  
    ...  
    unique_lock lock(mutex);  
    cond_full.notify();  
}
```

# Lock-free by Example

(one very complicated example)

Tony Van Eerd  
C++Now, 2015



```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
int pop() {  
    ...  
    unique_lock lock(mutex);  
    cond_full.notify();  
}
```





```
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```



```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
int pop() {  
    ...  
    unique_lock lock(mutex);  
    cond_full.notify();  
}
```



```
waiting = true;  
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```

I'm  
waiting!



```
int pop() {  
    ...  
    cond_full.notify();  
}
```



```
int pop() {  
    ...  
    unique_lock lock(mutex);  
    cond_full.notify();  
}
```



```
waiting = true;  
{  
    unique_lock lock(mutex);  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```

I'm  
waiting!

```
int pop() {  
    ...  
    unique_lock<mutex> lock(mutex);  
    cond_full.notify();  
}
```

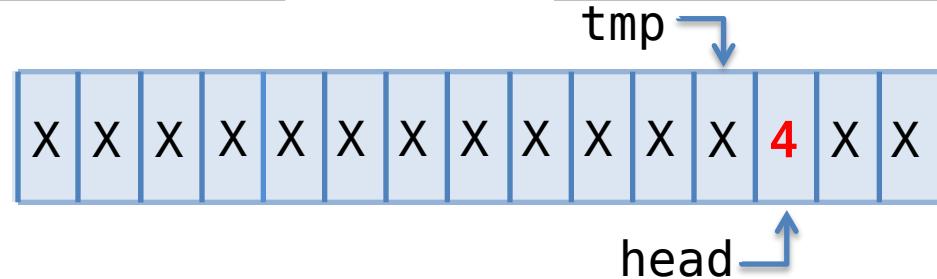




```
waiting = true;  
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}
```

I'm  
waiting!

```
int pop() {  
    ...  
    if (waiting) {  
        unique_lock lock(mutex);  
        cond_full.notify();  
    }  
}
```

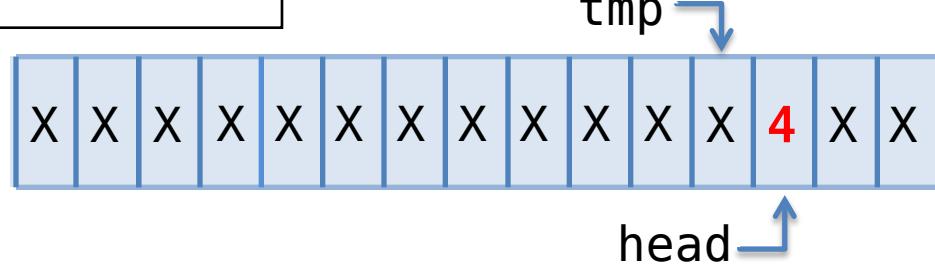




```
waiting = true;  
{  
    unique_lock lock(mutex);  
  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
}  
waiting = false;
```

I'm  
waiting!

```
int pop() {  
    ...  
    if (waiting) {  
        unique_lock lock(mutex);  
        cond_full.notify();  
    }  
}
```

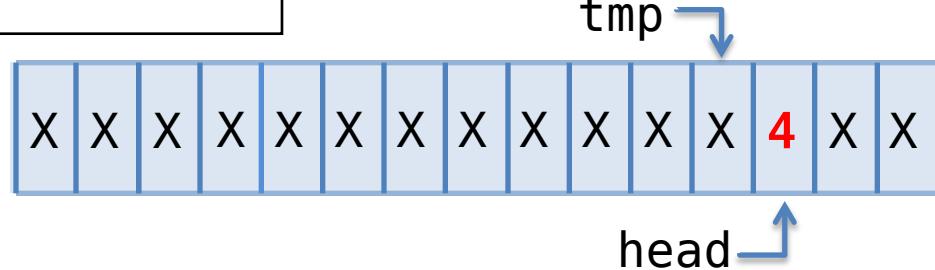




```
waiting++;
{
    unique_lock lock(mutex);
    while ( ! ...find_tail... )
        cond_full.wait(lock);
}
waiting--;
```

I'm  
waiting!

```
int pop() {
    ...
    if (waiting) {
        unique_lock lock(mutex);
        cond_full.notify();
    }
}
```

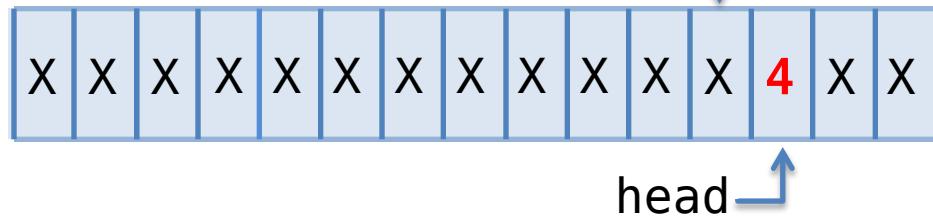




```
waiting++;
{
    unique_lock lock(mutex);
    while ( ! ...find_tail... )
        cond_full.wait(lock);
}
waiting--;
```

I'm  
waiting!

```
int pop() {
    ...
    if (waiting) {
        unique_lock lock(mutex);
        cond_full.notify();
    }
}
```

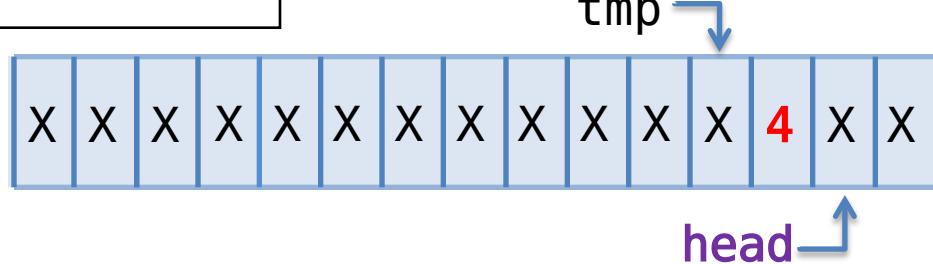




```
waiting++;
{
    unique_lock lock(mutex);
    while ( ! ...find_tail... )
        cond_full.wait(lock);
}
waiting--;
```

I'm  
waiting!

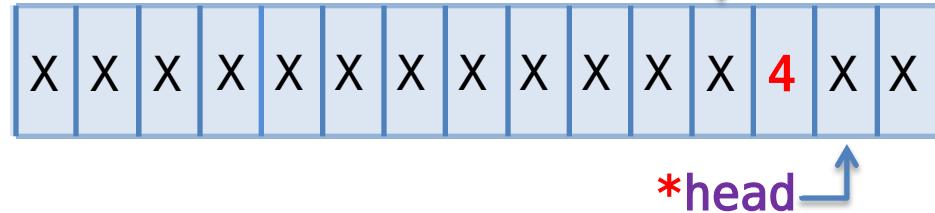
```
int pop() {
    ...CAS(head, oldhead, tmp+1);
    if (waiting) {
        unique_lock lock(mutex);
        cond_full.notify();
    }
}
```





```
{  
    unique_lock lock(mutex);  
    if (waiting++ == 0)  
        head.set_waitbit();  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
    if (--waiting == 0)  
        head.clear_waitbit();  
}
```

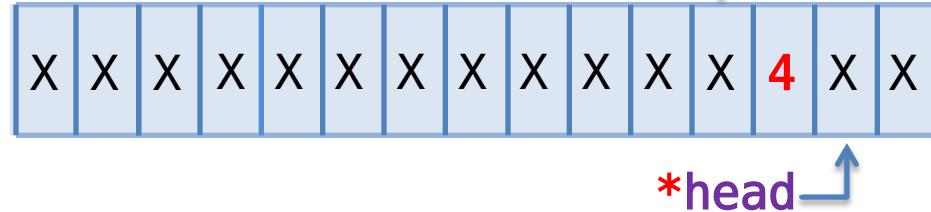
```
int pop() {  
    ...CAS(head, oldhead, tmp+1);  
    if (oldhead.waitbit()) {  
        unique_lock lock(mutex);  
        cond_full.notify();  
    }  
}
```





```
{  
    unique_lock lock(mutex);  
    if (waiting++ == 0)  
        head.set_waitbit();  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
    if (--waiting == 0)  
        head.clear_waitbit();  
}
```

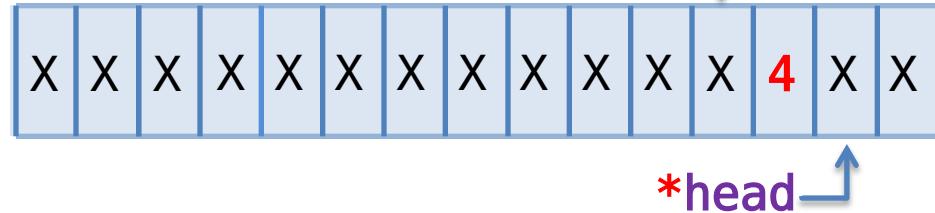
```
int pop() {  
    ...CAS(head, oldhead, tmp+1);  
    if (oldhead.waitbit()) {  
        unique_lock lock(mutex);  
        cond_full.notify();  
    }  
}
```





```
{  
    unique_lock lock(mutex);  
    if (waiting++ == 0)  
        head.set_waitbit();  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
    if (--waiting == 0)  
        head.clear_waitbit();  
}
```

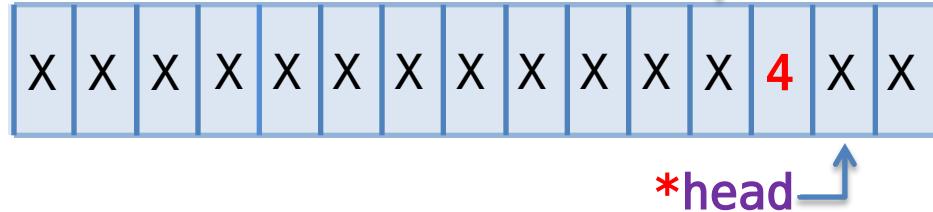
```
int pop() {  
    ...CAS(head, oldhead, tmp+1);  
    if (oldhead.waitbit()) {  
        unique_lock lock(mutex);  
        cond_full.notify();  
    }  
}
```





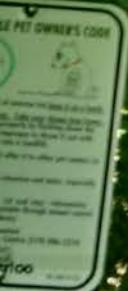
```
{  
    unique_lock lock(mutex);  
    if (waiting++ == 0)  
        head.set_waitbit();  
    while ( ! ...find_tail... )  
        cond_full.wait(lock);  
    if (--waiting == 0)  
        head.clear_waitbit();  
}
```

```
int pop() {  
    ...CAS(head, oldhead, tmp+1);  
    if (oldhead.waitbit()) {  
        unique_lock lock(mutex);  
        cond_full.notify();  
    }  
}
```



NOTE: **waiting** is NOT atomic





100





# Looking Back

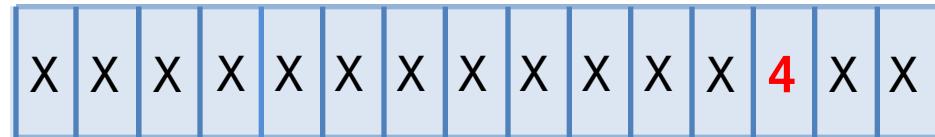


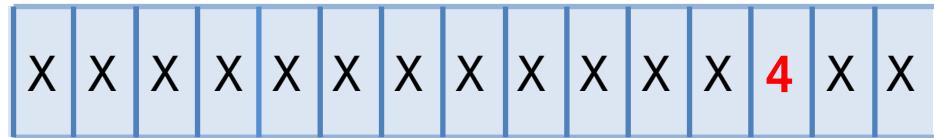
# Looking Back

push()



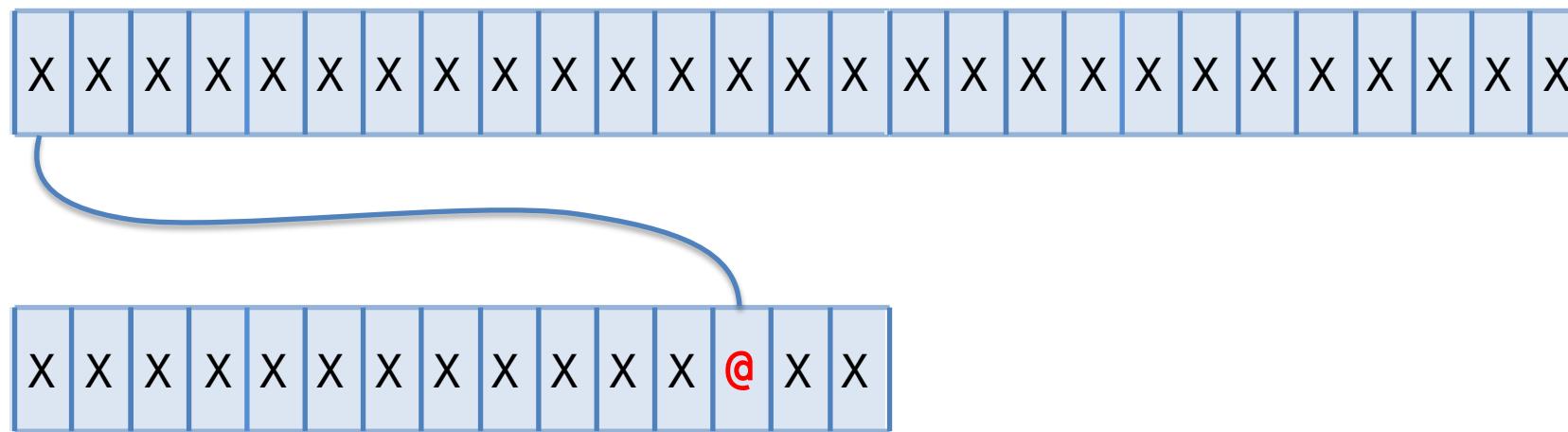
# Looking Ahead

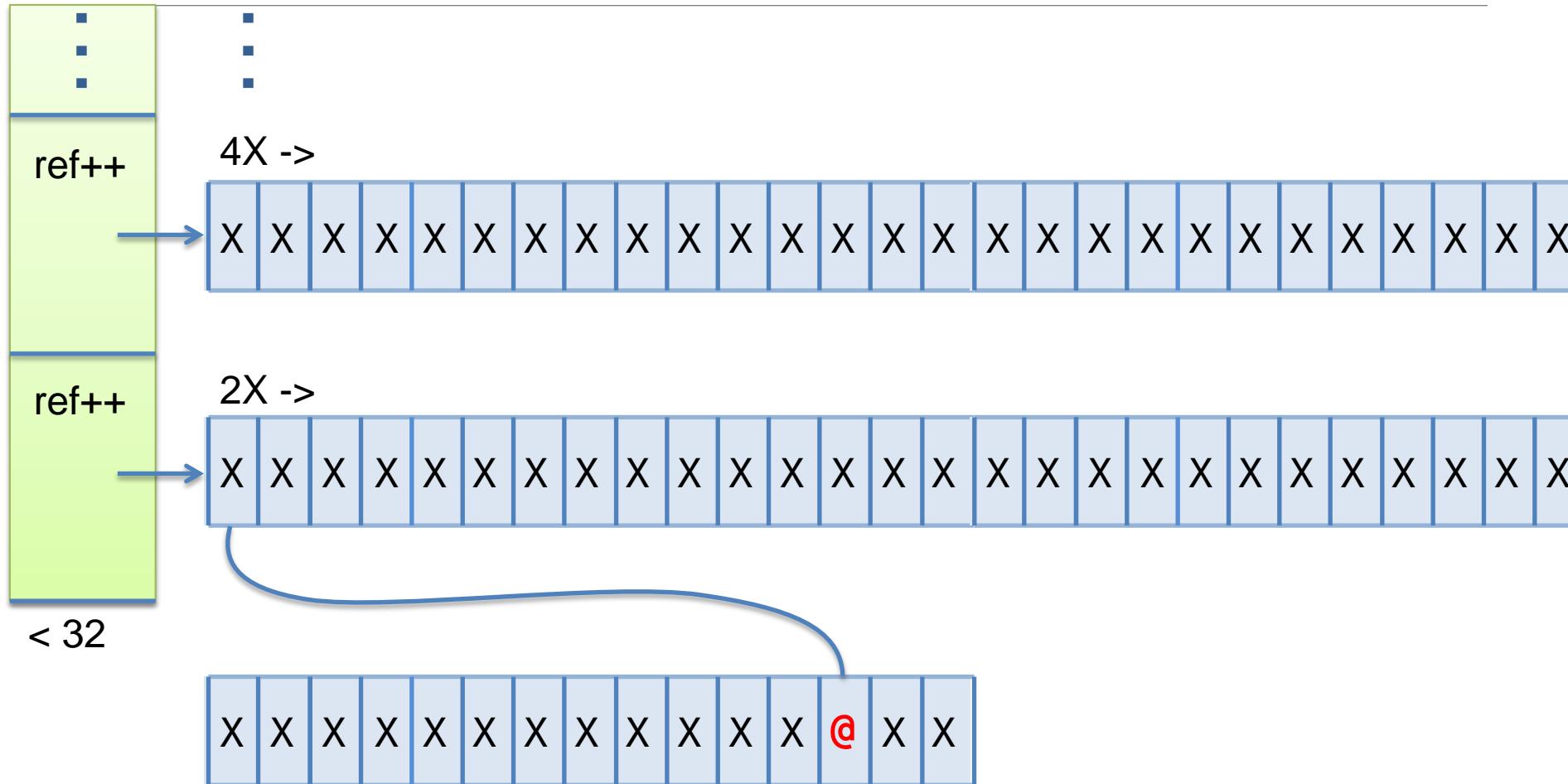






2X ->



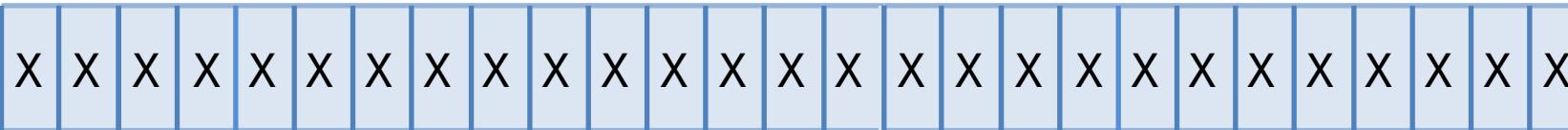




- ▪ ▪ + Structures, not just ints!

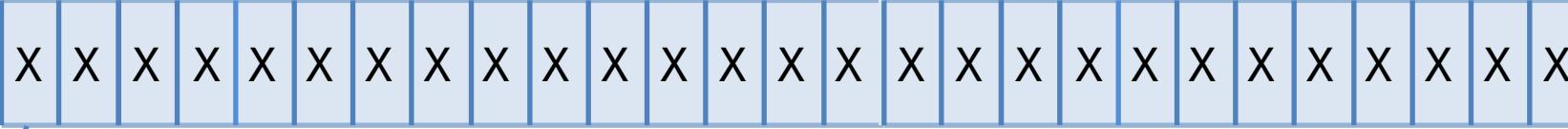
ref++

4X ->

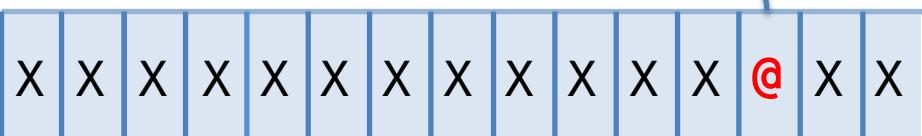


ref++

2X ->



< 32













# “The Problem with Threads”

<http://ptolemy.eecs.berkeley.edu/>

<http://ptolemy.eecs.berkeley.edu/publications/papers/06/problemwithThreads/>

“A part of the Ptolemy Project experiment was to see whether **effective software engineering practices** could be developed for an academic research setting. We developed a process that included a code maturity rating system (with four levels, red, yellow, green, and blue), **design reviews, code reviews, nightly builds, regression tests, and automated code coverage metrics**. The portion of the kernel that ensured a consistent view of the program structure was written in early 2000, design reviewed to yellow, and code reviewed to green. The **reviewers included concurrency experts**, not just inexperienced graduate students (Christopher Hylands (now Brooks), Bart Kienhuis, John Reekie, and myself were all reviewers). We wrote **regression tests that achieved 100 percent code coverage**. The nightly build and regression tests ran on a two processor SMP machine, which exhibited different thread behavior than the development machines, which all had a single processor. The Ptolemy II **system** itself began to be **widely used**, and every use of the system exercised this code. **No problems were observed until the code deadlocked on April 26, 2004, four years later.**”



**All states are valid states for all lines of code!**