

C++ METAPROGRAMMING

A PARADIGM SHIFT

Louis Dionne, C++Now 2015

QUADRANTS OF COMPUTATION IN C++

RUNTIME COMPUTATIONS (CLASSIC)

RUNTIME SEQUENCES

```
std::vector<int> ints{1, 2, 3, 4};
```

RUNTIME FUNCTIONS

```
std::string f(int i) {
    return std::to_string(i * i);
}

std::string nine = f(3);
```

RUNTIME ALGORITHMS

```
std::vector<std::string> strings;
std::transform(ints.begin(), ints.end(),
              std::back_inserter(strings), f);
```

`constexpr` COMPUTATIONS

constexpr SEQUENCES

```
constexpr std::array<int, 4> ints{1, 2, 3, 4};
```

constexpr FUNCTIONS

```
constexpr int factorial(int n) {
    return n == 0 ? 1 : n * factorial(n - 1);
}

constexpr int six = factorial(3);
```

constexpr ALGORITHMS

```
template <typename T, std::size_t N, typename F>
constexpr std::array<std::result_of_t<F(T)>, N>
transform(std::array<T, N> array, F f) {
    // ...
}

constexpr std::array<int, 4> ints{1, 2, 3, 4};
constexpr std::array<int, 4> facts = transform(ints, factorial);
```

HETEROGENEOUS COMPUTATIONS (FUSION)

HETEROGENEOUS SEQUENCES

```
fusion::vector<int, std::string, float> seq{1, "abc", 3.4f};
```

HETEROGENEOUS FUNCTIONS

```
struct to_string {
    template <typename T>
    std::string operator()(T t) const {
        std::stringstream ss;
        ss << t;
        return ss.str();
    }
};

std::string three = to_string{}(3);
std::string pi = to_string{}(3.14159);
```

HETEROGENEOUS ALGORITHMS

```
fusion::vector<int, std::string, float> seq{1, "abc", 3.4f};  
fusion::vector<std::string, std::string, std::string> strings =  
    fusion::transform(seq, to_string{});
```

TYPE-LEVEL COMPUTATIONS (MPL)

TYPE-LEVEL SEQUENCES

```
using seq = mpl::vector<int, char, float, void>;
```

TYPE-LEVEL FUNCTIONS

```
template <typename T>
struct add_const_pointer {
    using type = T const*;
};

using result = add_const_pointer<int>::type;
```

TYPE-LEVEL ALGORITHMS

```
using seq = mpl::vector<int, char, float, void>;
using pointers = mpl::transform<seq,
                           mpl::quote1<add_const_pointer>>::type;
```

NOTE

```
fusion::vector != mpl::vector
```

CONSIDER

```
mpl::vector<int, void, char>{} // ok  
  
// error: field has incomplete type void  
fusion::vector<int, void, char>{}
```

CLAIM

TYPE-LEVEL \subset HETEROGENEOUS

WHY BOTHER?

C++14 IS A SERIOUS GAME CHANGER

→ WE CAN DO BETTER NOW

SEE FOR YOURSELF

CHECKING FOR A MEMBER: THEN

```
template <typename T, typename = decltype(&T::xxx)>
static std::true_type has_xxx_impl(int);

template <typename T>
static std::false_type has_xxx_impl(...);

template <typename T>
struct has_xxx
    : decltype(has_xxx_impl<T>(int{}))
{ };

struct Foo { int xxx; };
static_assert(has_xxx<Foo>::value, "");
```

CHECKING FOR A MEMBER: SOON

```
template <typename T, typename = void>
struct has_xxx
    : std::false_type
{ };

template <typename T>
struct has_xxx<T, std::void_t<decltype(&T::xxx)>>
    : std::true_type
{ };

struct Foo { int xxx; };
static_assert(has_xxx<Foo>::value, "");
```

CHECKING FOR A MEMBER: WHAT IT SHOULD BE

```
auto has_xxx = is_valid([](auto t) -> decltype(t.xxx) {});  
  
struct Foo { int xxx; };  
Foo foo{1};  
  
static_assert(has_xxx(foo), "");  
static_assert(!has_xxx("abcdef"), "");
```

INTROSPECTION: THEN

```
namespace keys {
    struct name;
    struct age;
}

BOOST_FUSION_DEFINE_ASSOC_STRUCT(
    /* global scope */, Person,
    (std::string, name, keys::name)
    (int, age, keys::age)
)

int main() {
    Person john{"John", 30};
    std::string name = at_key<keys::name>(john);
    int age = at_key<keys::age>(john);
}
```

INTROSPECTION: NOW

```
struct Person {
    BOOST_HANA_DEFINE_STRUCT(Person,
        (std::string, name),
        (int, age)
    );
};

int main() {
    Person john{"John", 30};
    std::string name = at_key(john, BOOST_HANA_STRING("name"));
    int age = at_key(john, BOOST_HANA_STRING("age"));
}
```

GENERATING JSON: THEN

```
// sorry, not going to implement this
```

GENERATING JSON: NOW

```
struct Person {  
    BOOST_HANA_DEFINE_STRUCT(Person,  
        (std::string, name),  
        (int, age)  
    );  
};  
  
Person joe{"Joe", 30};  
std::cout << to_json(make_tuple(1, 'c', joe));
```

Output:

```
[1, "c", {"name": "Joe", "age": 30}]
```

HANDLE BASE TYPES

```
std::string quote(std::string s) { return "\"" + s + "\""; }

template <typename T>
auto to_json(T const& x) -> decltype(std::to_string(x)) {
    return std::to_string(x);
}

std::string to_json(char c) { return quote({c}); }
std::string to_json(std::string s) { return quote(s); }
```

HANDLE Sequences

```
template <typename Xs>
    std::enable_if_t<std::models<Sequence, Xs>(),
std::string> to_json(Xs const& xs) {
    auto json = transform(xs, [](auto const& x) {
        return to_json(x);
    });

    return "[" + join(std::move(json), ", ") + "]";
}
```

HANDLE Structs

```
template <typename T>
std::enable_if_t<models<Struct, T>(),  
std::string> to_json(T const& x) {  
    auto json = transform(keys(x), [&](auto name) {  
        auto const& member = at_key(x, name);  
        return quote(to<char const*>(name)) + " : " + to_json(member);  
    });  
  
    return "{" + join(std::move(json), ", ") + "}";  
}
```

STILL NOT CONVINCED?

HERE'S MORE

ERROR MESSAGES: THEN

```
using xs = mpl::reverse<mpl::int_<1>>::type;
```

```
boost/mpl/clear.hpp:29:7: error:  
  implicit instantiation of undefined template  
  'boost::mpl::clear_impl<mpl_::integral_c_tag>::apply<mpl_::int_<1> >'  
    : clear_impl< typename sequence_tag<Sequence>::type >  
      ^
```

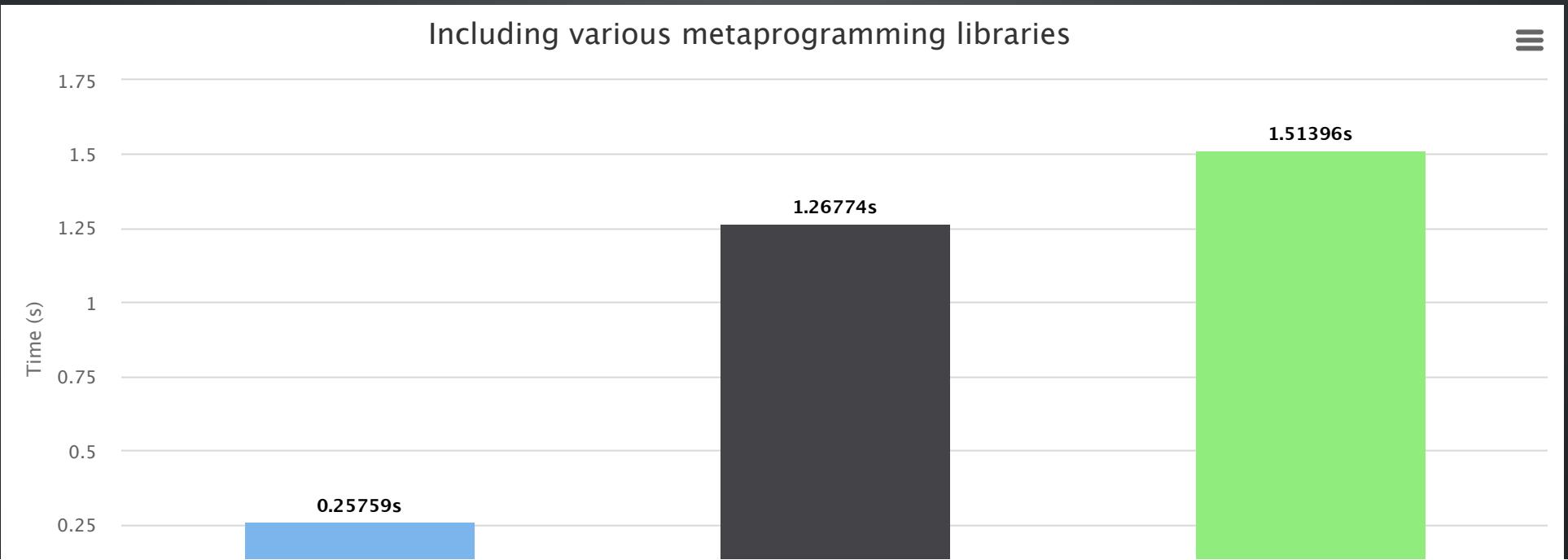
ERROR MESSAGES: NOW

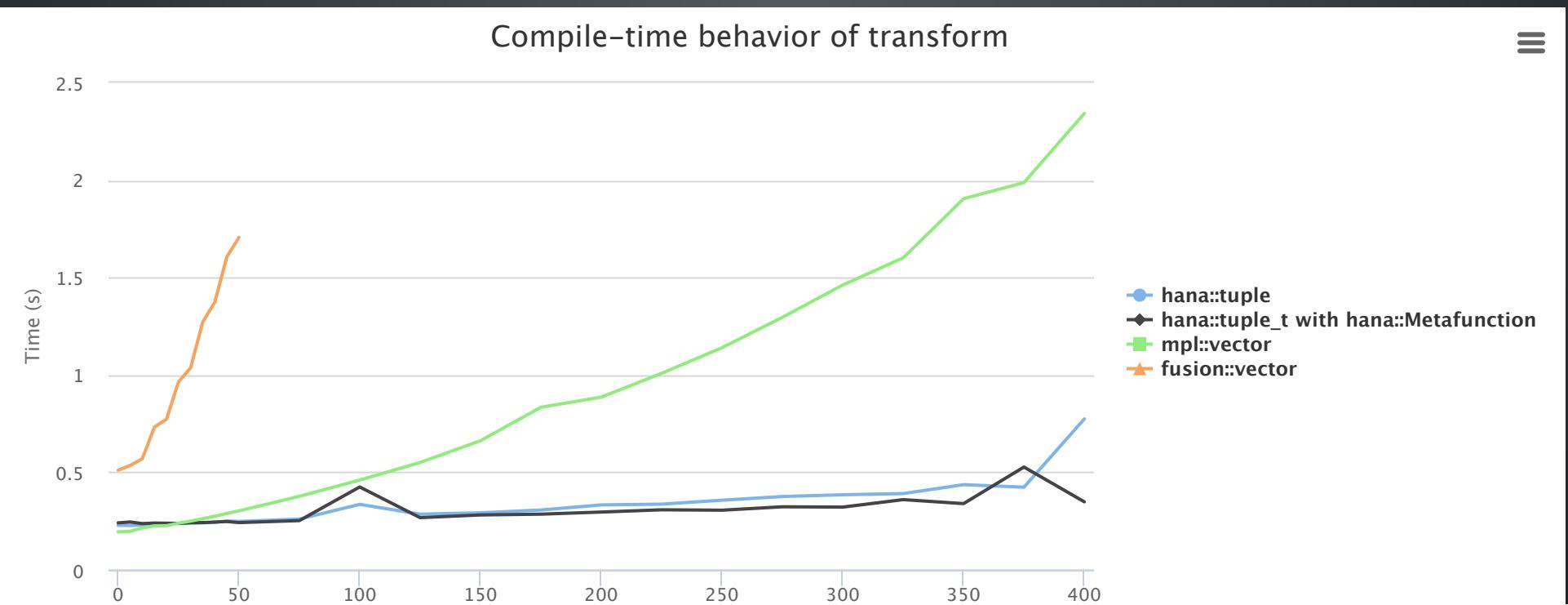
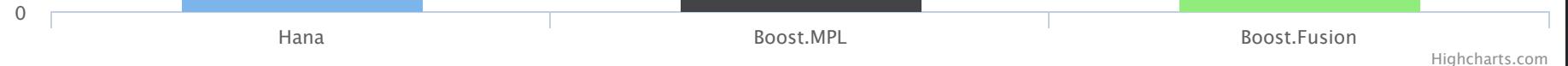
```
auto xs = hana::reverse(1);
```

```
boost/hana/fwd/sequence.hpp:602:13: error:  
  static_assert failed "hana::reverse(xs) requires xs to be a Sequence"  
  static_assert(_models<Sequence, typename datatype<Xs>::type>{},  
  ^                                ~~~~~~  
error_messages.cpp:19:24:  
  in instantiation of function template specialization  
  'boost::hana::_reverse::operator()<int>' requested here  
auto xs = hana::reverse(1);  
  ^
```

COMPILE-TIMES: THEN AND NOW

Including various metaprogramming libraries





WE MUST RETHINK METAPROGRAMMING

BUT HOW?
HERE'S MY TAKE

WHAT IS AN integral_constant?

```
template<class T, T v>
struct integral_constant {
    static constexpr T value = v;
    typedef T value_type;
    typedef integral_constant type;
    constexpr operator value_type() const noexcept { return value; }
    constexpr value_type operator()() const noexcept { return value; }
};
```

A TYPE-LEVEL ENCODING OF A `constexpr` VALUE

```
using one = integral_constant<int, 1>;
```

A `constexpr`-PRESERVING OBJECT

```
template <typename T>
void f(T t) { static_assert(t == 1, ""); }

constexpr int one = 1;
f(one);
// error: t is not constexpr in the body of f

f(integral_constant<int, one>{});
// ok: implicit conversion to int is constexpr
```

WE CAN DO constexpr ARITHMETIC

```
constexpr int two = ((3 * 2) + 4) / 5;
```

integral_constant VERSION

```
template <typename X, typename Y>
struct plus {
    using type = integral_constant<
        decltype(X::value + Y::value),
        X::value + Y::value
    >;
};

using three = plus<integral_constant<int, 1>,
                    integral_constant<int, 2>>::type;
```

BUT WHAT IF?

```
template <typename V, V v, typename U, U u>
constexpr auto
operator+(integral_constant<V, v>, integral_constant<U, u>)
{ return integral_constant<decltype(v + u), v + u>{}; }

template <typename V, V v, typename U, U u>
constexpr auto
operator==(integral_constant<V, v>, integral_constant<U, u>)
{ return integral_constant<bool, v == u>{}; }

// ...
```

TADAM!

```
static_assert(decltype(
    integral_constant<int, 1>{} + integral_constant<int, 4>{}
        ==
    integral_constant<int, 5>{})
)::value, "");
```

(OR SIMPLY)

```
static_assert(integral_constant<int, 1>{} + integral_constant<int, 4>{}  
             ==  
             integral_constant<int, 5>{}  
, "");
```

PASS ME THE SUGAR, PLEASE

```
template <int i>
constexpr integral_constant<int, i> int_{};

static_assert(int_{<1>} + int_{<4>} == int_{<5>}, "");
```

MORE SUGAR

```
template <char ...c>
constexpr auto operator"" _c() {
    // parse the characters and return an integral_constant
}

static_assert(1_c + 4_c == 5_c, "");
```

EUCLIDEAN DISTANCE

$\text{distance}((x_1, y_1), (x_2, y_2)) := \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$

COMPILE-TIME ARITHMETIC: THEN

```
template <typename P1, typename P2>
struct distance {
    using xs = typename minus<typename P1::x,
                           typename P2::x>::type;
    using ys = typename minus<typename P1::y,
                           typename P2::y>::type;
    using type = typename sqrt<
        typename plus<
            typename multiplies<xs, xs>::type,
            typename multiplies<ys, ys>::type
        >::type
    >::type;
};

static_assert(equal_to<
    distance<point<int_<3>, int_<5>>, point<int_<7>, int_<2>>>::type,
    int_<5>
>::value, "");
```

COMPILE-TIME ARITHMETIC: NOW

```
template <typename P1, typename P2>
constexpr auto distance(P1 p1, P2 p2) {
    auto xs = p1.x - p2.x;
    auto ys = p1.y - p2.y;
    return sqrt(xs*xs + ys*ys);
}

static_assert(distance(point(3_c, 5_c), point(7_c, 2_c)) == 5_c, "");
```

BUT RUNTIME ARITHMETIC WORKS TOO

```
auto p1 = point(3, 5); // dynamic values now
auto p2 = point(7, 2); //
assert(distance(p1, p2) == 5); // same function works!
```

PRETTY COOL? WAIT!

```
template <typename T, T n>
struct integral_constant {
    // ...

    template <typename F>
    void times(F f) const {
        f(); f(); ... f(); // n times
    }
};
```

LOOP UNROLLING: THEN

```
__attribute__((noinline)) void f() { }

int main() {
    #pragma PLZ UNROLL
    for (int i = 0; i != 10; ++i)
        f();
}
```

LOOP UNROLLING: NOW

```
__attribute__((noinline)) void f() { }

int main() {
    int_<10>.times(f);
}
```

SCEPTICAL?

```
_main:  
    ; snip  
    push    rbp  
    mov     rbp, rsp  
    call    __Z1fv  
    xor    eax, eax  
    pop    rbp  
    ret
```

SO FAR SO GOOD

WHAT IF?

```
template <typename ...T>
struct tuple {
    // ...

    template <typename N>
    constexpr decltype(auto) operator[](N const&) {
        return std::get<N::value>(*this);
    }
};
```

ACCESSING AN ELEMENT OF A TUPLE: THEN

```
tuple<int, char, float> values = {1, 'x', 3.4f};  
char x = std::get<1>(values);
```

ACCESSING AN ELEMENT OF A TUPLE: NOW

```
tuple<int, char, float> values = {1, 'x', 3.4f};  
char x = values[1_c];
```

WHY STOP HERE?

- `std::ratio`
- `std::integer_sequence`

WHAT ARE TYPES?

AREN'T THEY VALUES AFTER ALL?

```
using result = add_pointer<int>::type;
```

LET'S TREAT THEM AS SUCH!

```
class Type {  
    // ...  
};  
  
Type t{...};
```

WHAT ARE METAFUNCTIONS?

AREN'T THEY FUNCTIONS AFTER ALL?

```
template <typename T>
struct add_pointer {
    using type = T*;
};
```

LET'S TREAT THEM AS SUCH!

```
Type add_pointer(Type);
bool is_pointer(Type);
bool operator==(Type t, Type u);
// ...

Type t{...};
Type p = add_pointer(t);
assert(is_pointer(p));
```

COOL IDEA, BUT USELESS FOR METAPROGRAMMING

EASY FIX: USE TEMPLATES

```
template <typename T>
class Type { /* nothing */ };

Type<int> t{};
```

EASY FIX: USE TEMPLATES

```
template <typename T>
constexpr Type<T*> add_pointer(Type<T> const&)
{ return {}; }

template <typename T>
constexpr std::false_type is_pointer(Type<T> const&)
{ return {}; }

template <typename T>
constexpr std::true_type is_pointer(Type<T*> const&)
{ return {}; }
```

TADAM!

```
Type<int> t{};  
auto p = add_pointer(t);  
static_assert(is_pointer(p), "");
```

SUGAR

```
template <typename T>
constexpr Type<T> type{};  
  
auto t = type<int>;
auto p = add_pointer(t);
static_assert(is_pointer(p), "");
```

BUT WHAT DOES THAT BUY US?

TYPES ARE NOW FIRST CLASS CITIZENS!

```
auto xs = make_tuple(type<int>, type<char>, type<void>);  
auto c = xs[1_c];  
  
// sugar:  
auto ys = tuple_t<int, char, void>;
```

FULL LANGUAGE CAN BE USED

Before

```
using ts = vector<int, char&, void*>;
using us = copy_if<ts, or_<std::is_pointer<_1>,
                    std::is_reference<_1>>>::type;
```

After

```
auto ts = make_tuple(type<int>, type<char&>, type<void*>);  
auto us = filter(ts, [](auto t) {  
    return or_(is_pointer(t), is_reference(t));  
});
```

ONLY ONE LIBRARY IS REQUIRED

Before

```
// types (MPL)
using ts = mpl::vector<int, char&, void*>;
using us = mpl::copy_if<ts, mpl::or_<std::is_pointer<_1>,
                           std::is_reference<_1>>>::type;

// values (Fusion)
auto vs = fusion::make_vector(1, 'c', nullptr, 3.5);
auto ws = fusion::filter_if<std::is_integral<mpl::_1>>(vs);
```

After

```
// types
auto ts = tuple_t<int, char&, void*>;
auto us = filter(ts, [](auto t) {
    return or_(is_pointer(t), is_reference(t));
});

// values
auto vs = make_tuple(1, 'c', nullptr, 3.5);
auto ws = filter(vs, [](auto t) {
    return is_integral(t);
});
```

UNIFIED SYNTAX MEANS MORE REUSE

(AMPHIBIOUS EDSL USING BOOST.PROTO)

```
auto expr = (_1 - _2) / _2;  
  
// compile-time computations  
static_assert(decltype(evaluate(expr, 6_c, 2_c))::value == 2, "");  
  
// runtime computations  
int i = 6, j = 2;  
assert(evaluate(expr, i, j) == 2);
```

UNIFIED SYNTAX MEANS MORE CONSISTENCY

Before

```
auto map = make_map<char, int, long, float, double, void>(
    "char", "int", "long", "float", "double", "void"
);

std::string i = at_key<int>(map);
assert(i == "int");
```

After

```
auto map = make_map(
    make_pair(type<char>, "char"),
    make_pair(type<int>, "int"),
    make_pair(type<long>, "long"),
    make_pair(type<float>, "float"),
    make_pair(type<double>, "double"))
);

std::string i = map[type<int>];
assert(i == "int");
```

SO WE CAN REPRESENT TYPES AS VALUES

BUT HOW CAN WE GET BACK THE TYPES?

```
auto t = add_pointer(type<int>); // could be a complex type computation
using T = the-type-represented-by-t;
// do something useful with T here...
```

EASY FIX: USE NESTED ALIAS

```
template <typename T>
struct Type {
    using type = T;
};
```

AND THEN decltype

```
auto t = add_pointer(type<int>);  
using T = decltype(t)::type;  
static_assert(std::is_same<T, int*>{}, "");  
// do something useful with T here...
```

3 STEP PROCESS

1. Wrap types into `type<...>`
2. Perform computations
3. Unwrap with `decltype(. . .):::type`

ISN'T THAT CUMBERSOME?

NOT REALLY

ONLY DONE AT SOME THIN BOUNDARIES

```
auto t = type<T>;
auto result = huge_type_computation(t);
using Result = decltype(result)::type;
```

NOT ALWAYS REQUIRED

```
auto t = type<T>;
auto result = type_computation(t);
static_assert(result == type<Something>, "");
```

EVEN THEN, IT'S NOT THAT BAD

FINDING SMALLEST TYPE: THEN

```
template <typename ...T>
struct smallest
: deref<
  typename min_element<
    vector<T...>, less<sizeof_<_1>, sizeof_<_2>>
  >::type
>
{ };

template <typename ...T>
using smallest_t = typename smallest<T...>::type;

static_assert(std::is_same<
  smallest_t<char, long, long double>, char
>::value, "");
```

FINDING SMALLEST TYPE: NOW

```
template <typename ...T>
auto smallest = minimum(tuple_t<T...>, [ ](auto t, auto u) {
    return sizeof_(t) < sizeof_(u);
});

template <typename ...T>
using smallest_t = typename decltype(smallest<T...>)::type;

static_assert(std::is_same<
    smallest_t<char, long, long double>, char
>::value, "");
```

**SO TYPES ARE OBJECTS
WHAT SHOULD BE THEIR INTERFACE?**

IT'S PRECISELY <type_traits>!

```
add_pointer    -> std::add_pointer
add_const      -> std::add_const
add_volatile   -> std::add_volatile
// ...

is_pointer     -> std::is_pointer
is_const       -> std::is_const
is_volatile    -> std::is_volatile
// ...

operator==    -> std::is_same
// ...
```

THERE'S A GENERIC LIFTING PROCESS

LET'S RECONSIDER:

```
template <typename T>
Type<T*> add_pointer(Type<T>) { return {}; }
```

THIS COULD ALSO BE WRITTEN AS

```
template <typename T>
auto add_pointer(Type<T>) {
    return type<typename std::add_pointer<T>::type>;
}
```

THERE'S A PATTERN

```
template <template <typename ...> class F>
struct Metafunction {
    template <typename ...T>
    auto operator()(Type<T> ...) const {
        return type<
            typename F<T...>::type
        >;
    }
};

Metafunction<std::add_pointer> add_pointer{};

auto i = type<int>;
auto i_ptr = add_pointer(i);
static_assert(is_pointer(i_ptr), "");
```

SUGAR, AGAIN

```
template <template <typename ...> class F>
constexpr Metafunction<F> metafunction{};  
  
auto add_pointer = metafunction<std::add_pointer>;
auto remove_reference = metafunction<std::remove_reference>;
auto add_const = metafunction<std::add_const>;
// ...
```

CASE STUDY: SWITCH FOR boost::any

```
boost::any a = 3;
std::string result = switch<std::string>(a)(
    case<int>([](int i) { return std::to_string(i); })
, case<double>([](double d) { return std::to_string(d); })
, empty([] { return "empty"; })
, default_([] { return "default"; })
);
assert(result == "3");
```

DISCLAIMER:
NOT AS GOOD AS SEBASTIAN'S

FIRST

```
template <typename T>
auto case_ = [](auto f) {
    return std::make_pair(hana::type<T>, f);
};

struct _default;
auto default_ = case_<_default>;
auto empty = case_<void>;
```

THE BEAST

```
template <typename Result = void, typename Any>
auto switch_(Any& a) {
    return [&a](auto ...cases_) -> Result {
        auto cases = hana::make_tuple(cases_...);

        auto default_ = hana::find_if(cases, [](auto const& c) {
            return c.first == hana::type<_default>;
        });
        static_assert(!hana::is_nothing(default_),
                     "switch is missing a default_ case");

        auto rest = hana::filter(cases, [](auto const& c) {
            return c.first != hana::type<_default>;
        });

        return hana::unpack(rest, [&](auto& ...rest) {
            return impl<Result>(a, a.type(), default_->second, rest...);
        });
    };
}
```

PROCESSING CASES

```
template <typename Result, typename Any, typename Default,
          typename Case, typename ...Rest>
Result impl)
{
    using T = typename decltype(case_.first)::type;
    if (t == typeid(T)) {
        return hana::if_(hana::type<T> == hana::type<void>,
                        [](auto& case_, auto& a) {
                            return case_.second();
                        },
                        [](auto& case_, auto& a) {
                            return case_.second(*boost::unsafe_any_cast<T>(&a));
                        }
                    )(case_, a);
    }
    else
        return impl<Result>(a, t, default_, rest...);
}
```

BASE CASE

```
template <typename Result, typename Any, typename Default>
Result impl
```

ABOUT 70 LOC

AND YOUR COWORKERS COULD UNDERSTAND
(MOSTLY)

MY PROPOSAL: HANA

- Heterogeneous + type level computations
- 75+ algorithms
- 8 heterogeneous containers
- Improved compile-times

WORKING ON C++14 COMPILERS

- Clang >= 3.5
- GCC 5 (almost)

AVAILABLE IN YOUR NEXT BOOST RELEASE!

(HOPEFULLY)

FORMAL REVIEW: JUNE 10 - JUNE 24

EMBRACE THE FUTURE

EMBRACE HANA

THANK YOU

<http://ldionne.com>

<http://github.com/ldionne>

BONUS

SORTING AT COMPILE-TIME: THEN

```
template <typename Sequence, typename Pred>
struct sort_impl;

template <typename Sequence, typename Pred>
struct sort
: eval_if<empty<Sequence>,
  identity<Sequence>,
  sort_impl<Sequence, Pred>
>
{ };
```

SORTING AT COMPILE-TIME: THEN

```
template <typename Sequence, typename Pred>
struct sort_impl {
    using pivot = typename begin<Sequence>::type;
    using parts = typename partition<
        iterator_range<typename next<pivot>::type,
                        typename end<Sequence>::type>
    , apply2<typename lambda<Pred>::type, _1,
              typename deref<pivot>::type>
    , back_inserter<vector<>>
    , back_inserter<vector<>>
    >::type;

    using part1 = typename push_back<
        typename sort<typename parts::first, Pred>::type,
        typename deref<pivot>::type
    >::type;

    using part2 = typename sort<typename parts::second, Pred>::type;

    using type = typename insert_range<
        part1, typename end<part1>::type, part2
    >::type;
};
```

SORTING AT COMPILE-TIME: NOW

```
template <typename Xs, typename Pred>
auto sort(Xs xs, Pred pred) {
    return eval_if(length(xs) < size_t<2>,
        lazy(xs),
        lazy([](auto xs) {
            auto pivot = head(xs);
            auto parts = partition(tail(xs), partial(pred, pivot));
            return concat(
                append(sort(second(parts), pred), pivot),
                sort(first(parts), pivot)
            );
        })(xs)
    );
}
```

CASE STUDY: INDEXED SORTING

```
auto types = tuple_t<int[3], int[2], int[1]>;
auto indexed = indexed_sort(types, [](auto t, auto u) {
    return sizeof_(t) < sizeof_(u);
});

auto sorted = first(indexed);
auto indices = second(indexed);

static_assert(sorted == tuple_t<int[1], int[2], int[3]>, "");
static_assert(indices == tuple_c<std::size_t, 2, 1, 0>, "");
```

THE BEAST

```
auto indexed_sort = [](auto list, auto predicate) {
    auto indices = to<Tuple>(range(0_c, size(list)));
    auto indexed_list = zip.with(make_pair, list, indices);
    auto sorted = sort(indexed_list, [&](auto const& x, auto const& y) {
        return predicate(first(x), first(y));
    });
    return make_pair(transform(sorted, first), transform(sorted, second));
};
```

WITH FUSION/MPL ...

```
template <typename Types, typename Predicate = quote2<less>>
struct indexed_sort {
    using indexed_types = typename copy<
        zip_view<vector<Types, range_c<long, 0l, size<Types>::value>>>,
        back_inserter<vector<>>>
    >::type;

    using sorted = typename sort<
        indexed_types,
        apply2<typename lambda<Predicate>::type, front<_1>, front<_2>>
    >::type;

    using type = pair<
        typename transform<sorted, front<_1>>::type,
        typename transform<sorted, back<_1>>::type
    >;
};
```

FAKING THE INITIAL SEQUENCE: NOW

```
using Sequence = decltype(unpack(sorted, template_<_tuple>))::type;
auto index_map = second(indexed_sort(indices, less));

Sequence s;
int (&a)[3] = s[index_map[0_c]];
int (&b)[2] = s[index_map[1_c]];
int (&c)[1] = s[index_map[2_c]];
```

FAKING THE INITIAL SEQUENCE: THEN

```
using Sequence = fusion::result_of::as_vector<Sorted>::type;
using IndexMap = indexed_sort<Indices>::type::second;

Sequence s;
int (&a)[3] = fusion::at_c<at_c<IndexMap, 0>::type::value>(s);
int (&b)[2] = fusion::at_c<at_c<IndexMap, 1>::type::value>(s);
int (&c)[1] = fusion::at_c<at_c<IndexMap, 2>::type::value>(s);
```

std::common_type: N3843

```
template <typename T, typename U>
using builtin_common_t = std::decay_t<decltype(
    true ? std::declval<T>() : std::declval<U>()
)>;
```

```
template <typename, typename ...>
struct ct { };
```

```
template <typename T>
struct ct<void, T> : std::decay<T> { };
```

```
template <typename T, typename U, typename ...V>
struct ct<void_t<builtin_common_t<T, U>>, T, U, V...>
    : ct<void, builtin_common_t<T, U>, V...>
{ };
```

```
template <typename ...T>
struct common_type : ct<void, T...> { };
```

std::common_type::Now

```
template <typename ...>
auto common_type_impl = nothing;

template <typename T1, typename ...Tn>
auto common_type_impl<T1, Tn...> = monadic_fold<Maybe>(
    tuple_t<Tn...>, type<std::decay_t<T1>>,
    sfinae([](auto t, auto u) -> decltype(
        traits::decay(true ? traits::declval(t) : traits::declval(u)))
    ) { return {}; })
);

template <typename ...T>
struct common_type : decltype(common_type_impl<T...>) { };
```