# CSCI-UA.0480-003 Parallel Computing Lab Assignment 1

In this lab you will implement a method for solving a group of linear equations using MPI.

# What will your program do?

Given a set of n equations with n unknowns  $(x_1 \text{ to } x_n)$ , your program will calculate the values of  $x_1$  to  $x_n$  within an error margin of e%.

The format of the file is:

- line1: #unknowns
- line2: absolute relative error
- Initial values for each unknown
- line 3 till end: the coefficients for each equation. Each equation on a line. On the same line and after all the coefficients you will find the constant of the corresponding equation.

For example, if we want to solve a system of 3 linear equations, you can have a file like this one:

5136

3728

3696

The above file corresponds to the following set of equation:

 $5X_{1+} X_2 + 3X_3 = 6$ 

 $3X_{1} + 7X_{2} + 2X_{3} = 8$ 

 $3X_{1+}6X_{2}+9X_{3}=6$ 

The third line in the file tells us that the initial values for  $X_1$  is 2, for  $X_2$  is 3, and for  $X_3$  is 4. Those values may not be the solution, or are very far from the solution that must be within 1% of the real values (as given by the 0.01 in line 2).

## How will your program do that?

You will use Gaussian-Seidel method. OK, I think you don't know it, do you? Let me be nice and tell you about it.

We start with a set of n equations and n unknowns, like this:

$$a_{11}x_1 + a_{12}x_2 + a_{13}x_3 + \dots + a_{1n}x_n = b_1$$

$$a_{21}x_1 + a_{22}x_2 + a_{23}x_3 + \dots + a_{2n}x_n = b_2$$

$$\vdots$$

$$a_{n1}x_1 + a_{n2}x_2 + a_{n3}x_3 + \dots + a_{nn}x_n = b_n$$

You are given all  $a_{ij}$  and  $b_1$  to  $b_n$ . You need to calculate all Xs. Here are the steps:

1. Rewrite each equation such has the left-hand-side is one of the unknowns.

Rewriting each equation

Note: The Cs above refer to the constants, which are the  $b_1$  to  $b_n$ .

In general:

$$c_{i} - \sum_{\substack{j=1\\j \neq i}}^{n} a_{ij} x_{j}$$

$$x_{i} = \frac{1,2,...,n}{a_{ii}}$$

2. Remember that you were also given some initial values for the Xs in the input file. The absolute relative error is:

$$\left| \in_a \right|_i = \left| \frac{x_i^{new} - x_i^{old}}{x_i^{new}} \right| \times 100$$

Therefore, our goal is to reduce absolute relative error for each unknown to make it less or equal to relative error given in the input file (2nd line). Note: You need to multiply the error given in the file by 100 to match it with the above equation, or to not multiply the above equation by 100.

- 3. Substitute the initial values in the equation of  $X_1$  to get new value for  $X_1$ . Use that new value as well as the other initial values for  $X_2$  to  $X_n$  to get new value for  $X_2$ . Then use the new values for  $X_1$  and  $X_2$  and the rest of the initial values to get  $X_3$ , and so on.
- 4. Now we have a new set of Xs.
- 5. Calculate the absolute relative errors for each X.

- 6. If all errors are equal or less the given number (2nd line in the file) then you are done.
- 7. Otherwise go back to step 3 with the set of new Xs as  $X_{old}$ .

## What is the input to your program?

The input to your program is a text file named xxxx.eq where xxxx can be any name. We already discussed the file format.

### What is the output of your program?

Your program must output to stdout (the screen) the value of each unknown. The output must look like:

2

3

4

Where 2 correspond to the value of  $X_1$ , 3 corresponds to  $X_2$ , and 4 corresponds to  $X_3$ , ... . In the last line of the output show the number of iterations as: total number of iterations: 5

## What do I do after I finish my program?

We have provided you with a reference program *gsref* so you can check the correctness of your code. We will test your submission against this reference.

After you finish the parallel version of your program, compile it with:

```
mpicc -o gs gs.c
```

Where gs.c is your code. We provide a skeleton file to help you start.

After you compile your program and check its correctness do the following:

- Measure the time of your program (using *time* command) for 1, 2, 4, 8, 16, 32, and 64 processes. You may need to measure the time few times (~ 5) for each and take the average. Do the following with small.txt, medium.txt, and large.txt.
- Draw a graph where the x-axis is the number of processes and the y-axis is the time. There must be 3 curves on the same graph.
- What are your conclusions?
- Draw another graph that shows the speedup (again 3 curves are expected).
- What are your conclusions?
- Include the two graphs and your conclusions in a single pdf file that has your name and titled *lab1 submission*

#### What to submit?

Add the source code as well as the pdf file that contains your graphs and conclusions to a zip file named: lastname.firstname.zip

Where lastname is your last name, and firstname is your first name.

#### How to submit?

email the above zip file to our grader (not me, not the mailing list!) with subject line: lab1 submission

#### How will we grade this?

- We will test your code with 3 groups of linear equations of different number of variables. The grading will be as follows for each group:
  - o Correctness: 5
  - O Scalability (we will run your code with increasing number of processes depending on the number of equations): 10
  - This makes a total of 45 points.
- Your graphs and conclusions: 10 points
- Style (i.e. comments, spaces, ...): 5 points.

This makes a total of 60 points: (3\*15) + 10 + 5

#### **Penalties**

- If you do not follow the above protocol for submission and file name --> -1
- If your code does not compile, we will look at your source code; and out of the 45 points dedicated to the coding you may not get more than 30 (depending on how close your code is to a correct version).
- You may lose points also if your conclusions are like "As we can see from the graphs, x increasing with y". We need your explanation of what the graphs show, not your description of what we already see!