



$$\{\theta_k\}, \{T_{model}^{camera_j}\} =$$

$$\underset{\{\theta_k\}, \{T_{model}^{camera_j}\}}{\text{argmin}} \sum_i^m \sum_j^n \|P(T_{model}^{camera_j} \cdot M_{ij} \{\theta_k\}) - m_j\|_2^2$$

$$\sum_i^m \sum_j^n \|r_{ij}\|_2^2 = \| [r_{00} \dots r_{0m} \ r_{10} \dots r_{1m}]^T \|_2^2$$

$$a^\wedge = \begin{bmatrix} 0 & -a_3 & a_2 \\ a_3 & 0 & -a_1 \\ -a_2 & a_1 & 0 \end{bmatrix}$$

$$\begin{aligned} \exp(\phi^\wedge) &= \exp(\theta n^\wedge) = \sum_{n=0}^{\infty} \frac{1}{n!} (\theta n^\wedge)^n \\ &= \cos\theta I + (1 - \cos\theta) n n^T + \sin\theta n^\wedge \end{aligned}$$

$$\mathcal{S} = \begin{bmatrix} \rho \\ \phi \end{bmatrix} \in \mathbb{R}^6 \rightarrow SE(3)$$

$$\mathcal{S}^\wedge = \begin{bmatrix} \phi^\wedge & \rho \\ 0^T & 0 \end{bmatrix} \quad T = \begin{bmatrix} R & t \\ 0^T & 1 \end{bmatrix}$$

$$t = J\rho \quad J = \frac{\sin\theta}{\theta} I + \left(1 - \frac{\sin\theta}{\theta}\right) a a^T + \frac{1 - \cos\theta}{\theta} a^\wedge$$

$$u = f_x \frac{x'}{z'} + c_x$$

$$v = f_y \frac{y'}{z'} + c_y$$

$$\frac{\partial e}{\partial \delta \delta} = \lim_{\delta \delta \rightarrow 0} \frac{e(\delta \delta \oplus \delta) - e(\delta)}{\delta \delta} = \frac{\partial e}{\partial p'} \frac{\partial p'}{\partial \delta \delta}$$

$$\frac{\partial e}{\partial p'} = \begin{bmatrix} \frac{f_x}{z'} & 0 & -\frac{f_x x'}{z'^2} \\ 0 & \frac{f_y}{z'} & -\frac{f_y y'}{z'^2} \end{bmatrix}$$

$$\frac{\partial(TP)}{\partial \delta \delta} = \lim_{\delta \delta \rightarrow 0} \frac{\exp(\delta \delta^\wedge) \exp(\delta^\wedge) P - \exp(\delta^\wedge) P}{\delta \delta}$$

$$= \lim_{\delta \delta \rightarrow 0} \frac{(I + \delta \delta^\wedge) \exp(\delta^\wedge) P - \exp(\delta^\wedge) P}{\delta \delta}$$

$$= \lim_{\delta \delta \rightarrow 0} \frac{\delta \delta^\wedge \exp(\delta^\wedge) P}{\delta \delta}$$

$$= \lim_{\delta \delta \rightarrow 0} \frac{\begin{bmatrix} \delta \phi^\wedge & \delta p \\ 0^\top & 0 \end{bmatrix} \begin{bmatrix} R p + t \\ 1 \end{bmatrix}}{\delta \delta}$$

$$= \lim_{\delta \delta \rightarrow 0} \frac{\begin{bmatrix} \delta \phi^\wedge (R p + t) + \delta p \\ 0^\top \end{bmatrix}}{[\delta p, \delta \phi]^\top}$$

$$= \begin{bmatrix} I & -(R p + t)^\wedge \\ 0^\top & 0^\top \end{bmatrix}$$