

Basic definitions

What is the difference between *Image processing* and *Computer Vision*?

There are many views – answer depends on who you ask

- Ans 1: None
- Ans 2: IP deals with 2D and CV with 3D-2D relationship
- Ans 3: IP's focus is on manipulating an image while CV's focus is on understanding given images
 - interpret, recognise, decide etc
- Ans 4: CV = **Artificial Intelligence married to IP!**

Syllabus

- Spatial domain proc. - Point and neighbourhood processing, histogram processing
- Image transforms – Fourier, Wavelets
- Colour image processing
- Morphological processing
- Image representation – Pyramids, Scale-space, Multi-resolution
- Image segmentation
- Feature detection and representation – corners, edges, blobs, SIFT, SURF

Common types of images

- Binary



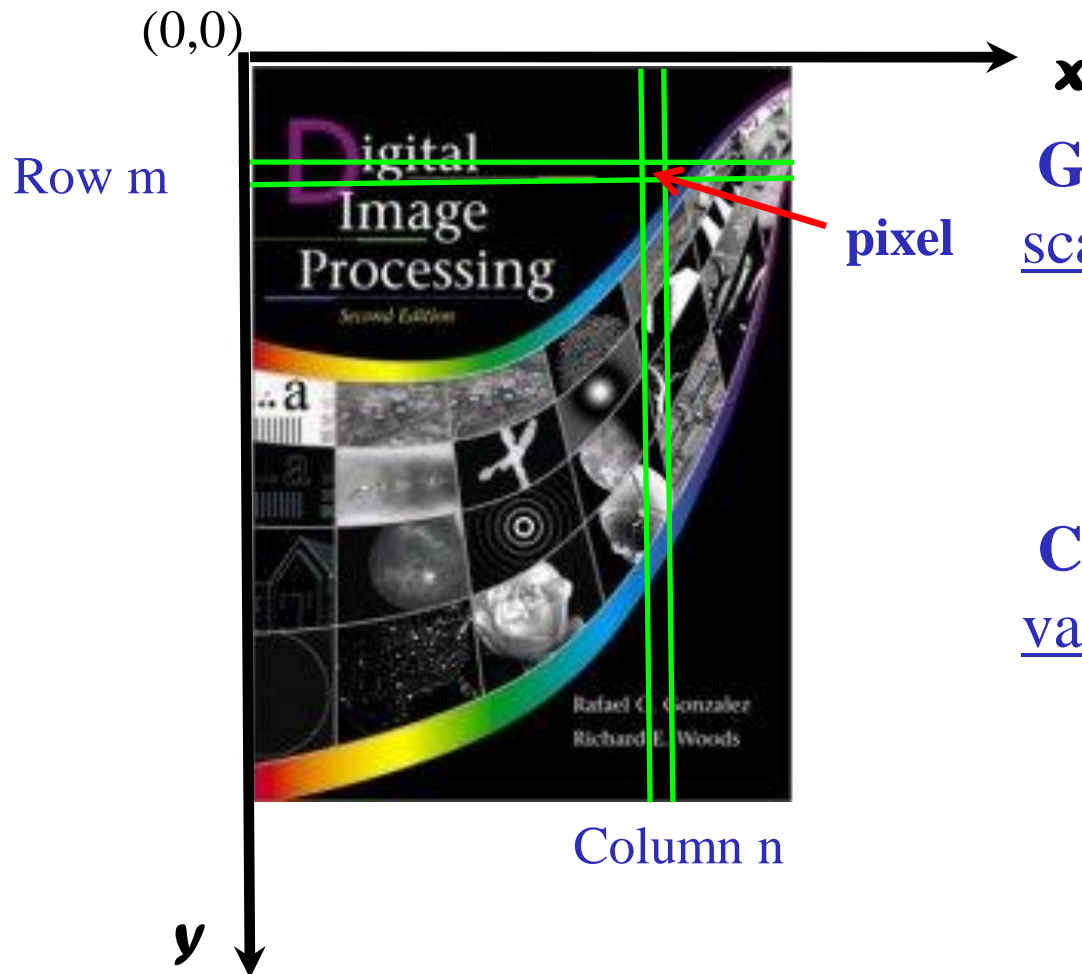
- Grey scale



- Colour



Digital Images – basic element



Greyscale image: Image is a scalar valued function

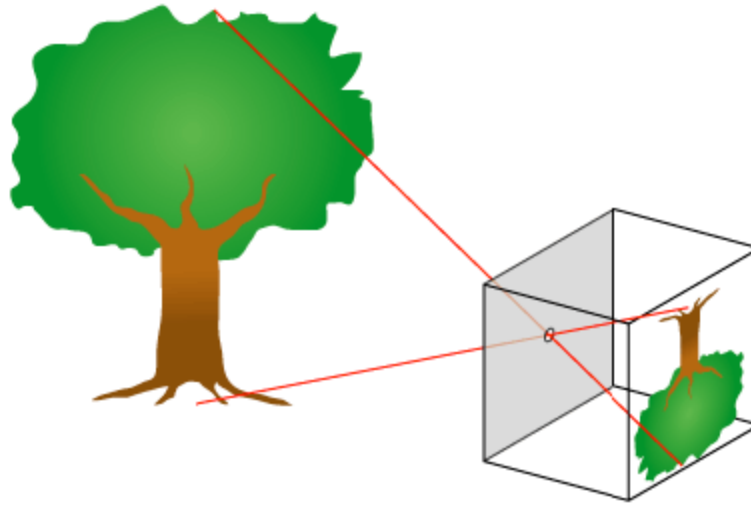
- Pixel value $\in [0, 255]$ for 8-bit image

Colour image: Image is a vector valued function

- vector has 3 elements to represent the colour
- each element is usually allocated 8 bits

$I[m,n]$ of size $M \times N$ has M rows and N columns and hence MN pixels

Image Acquisition

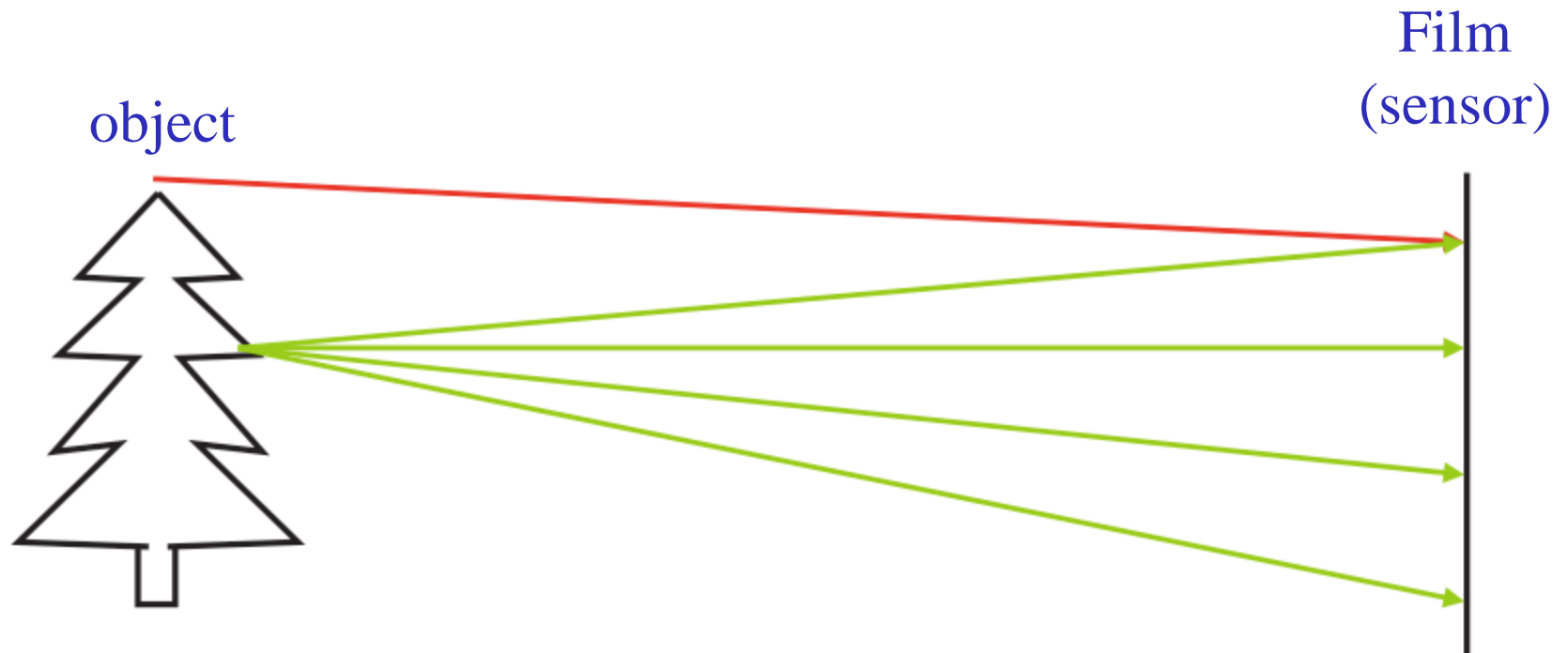


a) Image properties depend on:

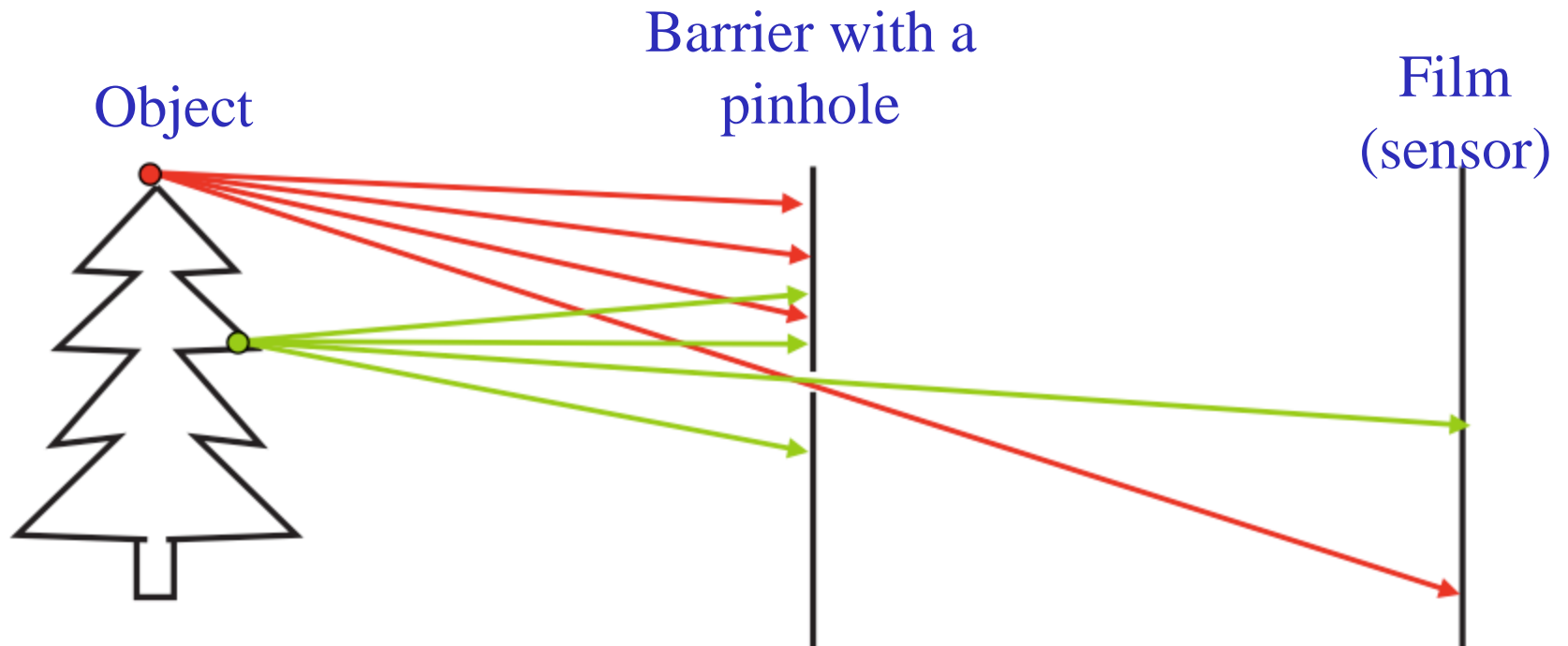
- Camera distance, viewpoint, motion
- Camera intrinsic parameters (e.g., lens aberration)
- Number of cameras
- Ambient illumination

b) Visual properties of the 3D world captured

Working of a camera

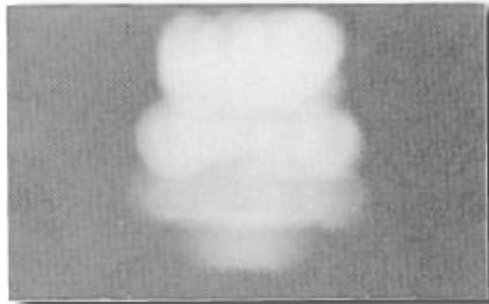


Difficult to interpret the image when the film is directly in front of an object



- The barrier blocks off most of the rays
- This reduces blurring
- Aperture = Opening of the pinhole

pinhole too big:
bright and blurred



2 mm



7 mm

pinhole right size:
dark and crisp



0.6 mm



0.5 mm

pinhole too small:
dark and diffraction blur

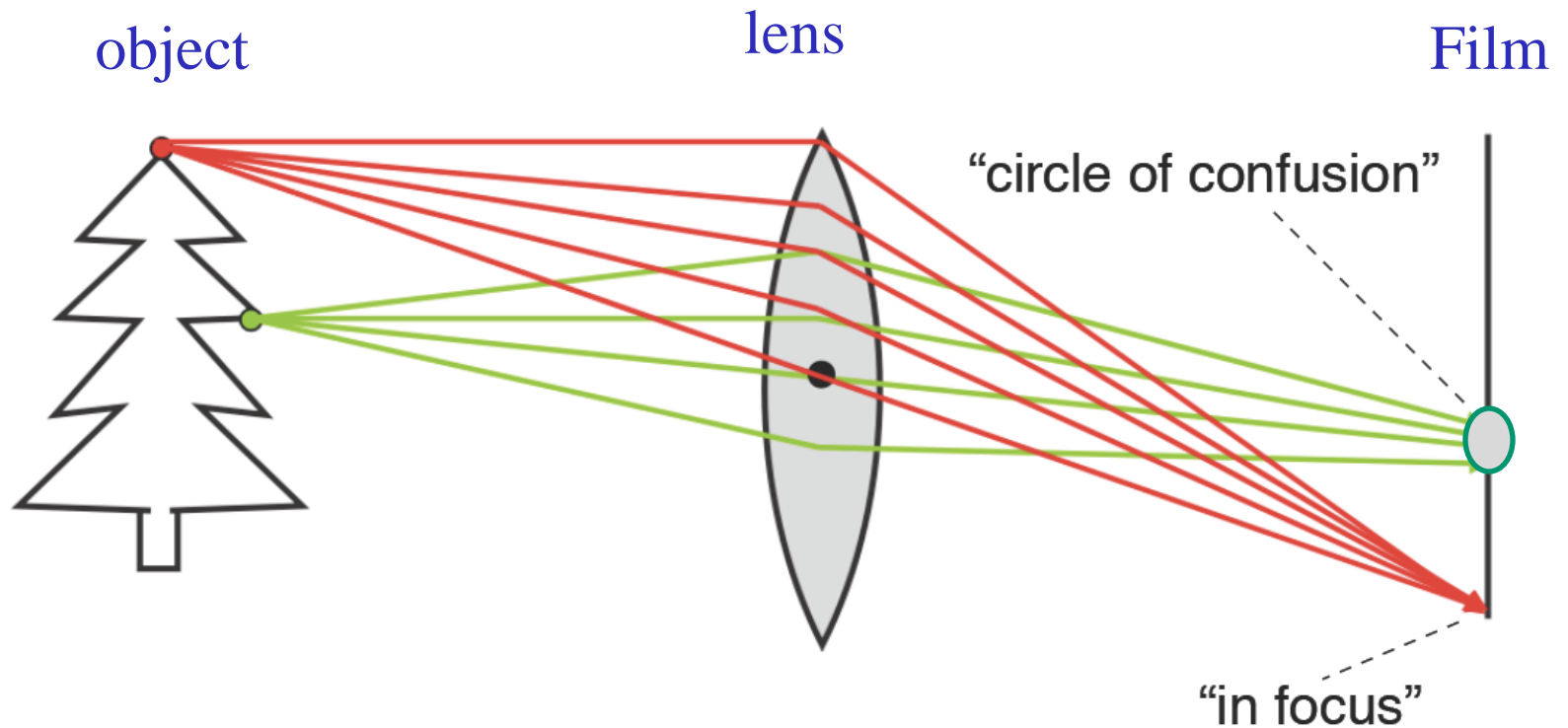


0.15 mm

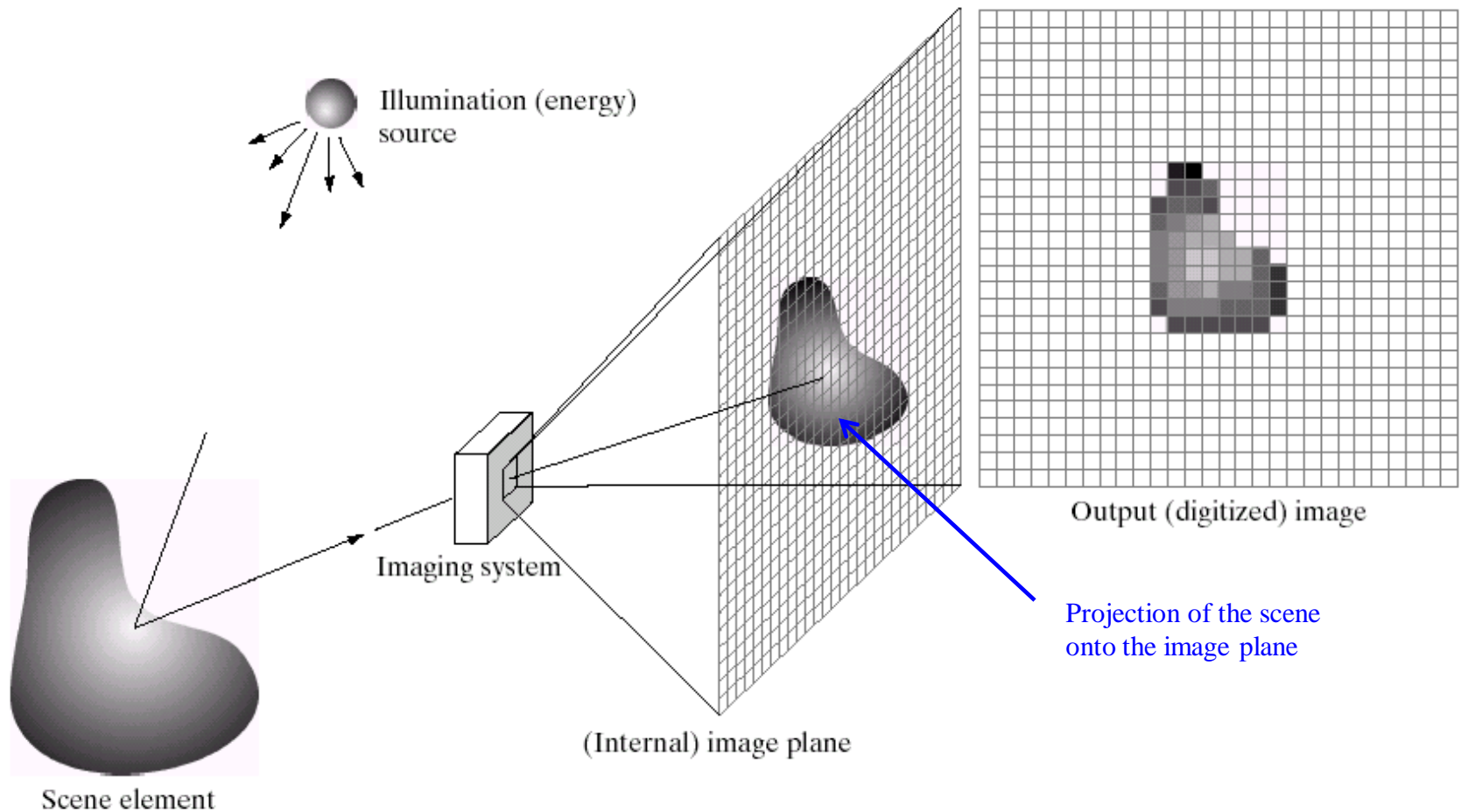


0.05 mm

Adding lens ..



The lens focuses light onto the film



$$f(x, y) = i(x, y)r(x, y)$$

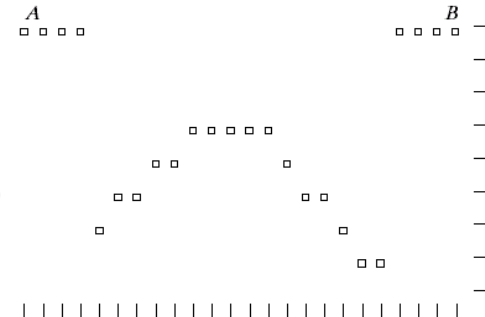
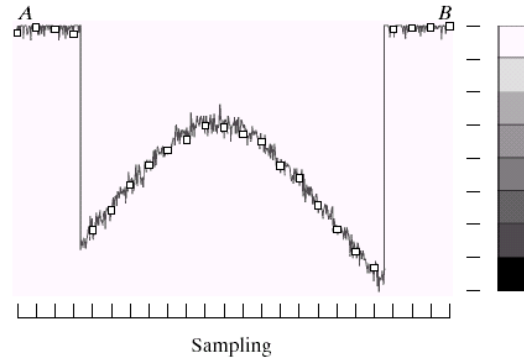
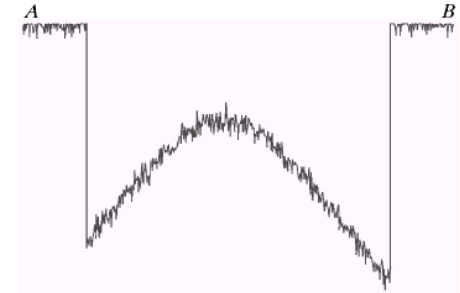
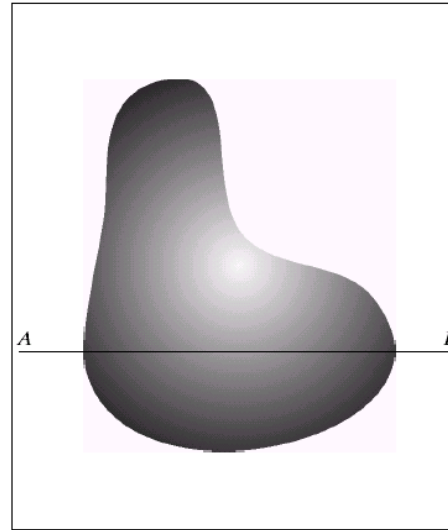
$$0 < i(x, y) < \infty; 0 < r(x, y) < 1$$

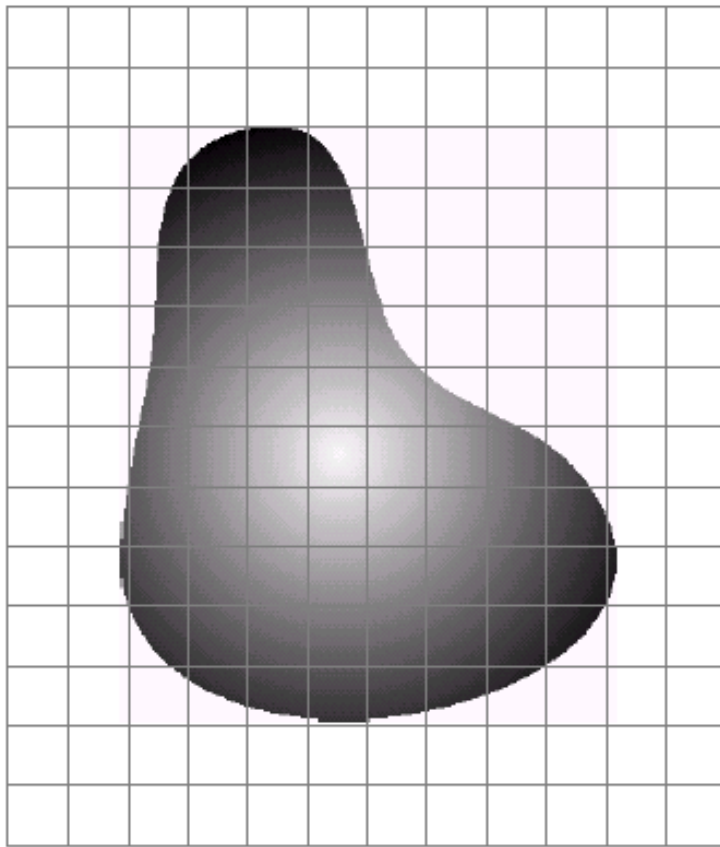
i : incident illumination

r : illumination reflected by the objects

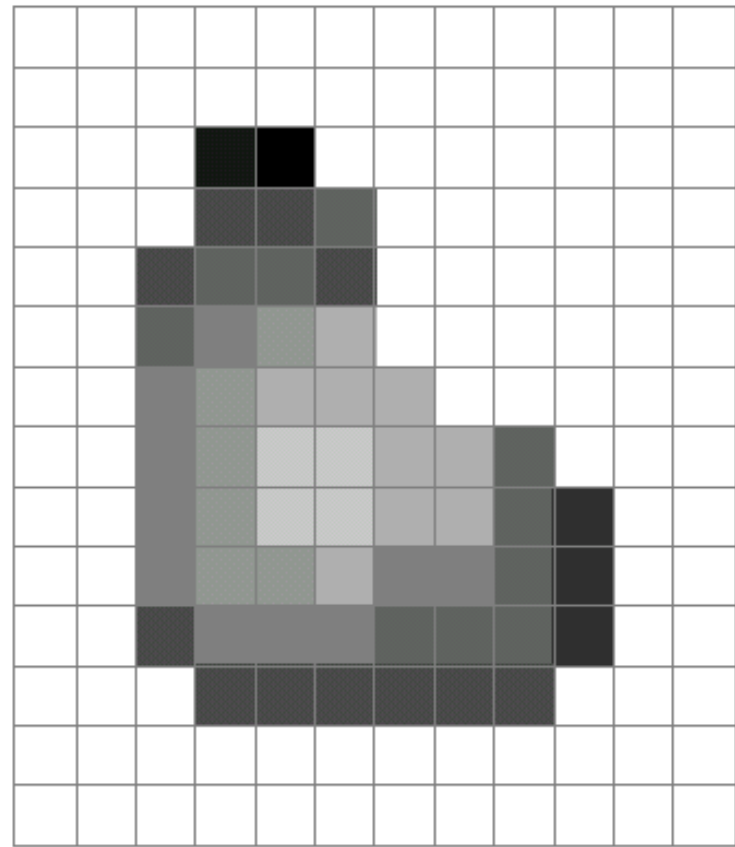
Sampling and Quantization

- $f(x,y)$ is a continuous image w.r.to
 - the spatial variables x, y
 - amplitude f
- Digital conversion needs
 - **Sampling**: discretising the spatial variables
 - **Quantisation**: discretising the (intensity) amplitude





Continuous image projected on image grid



Result of sampling and quantization

The quality of a digital image primarily depends on

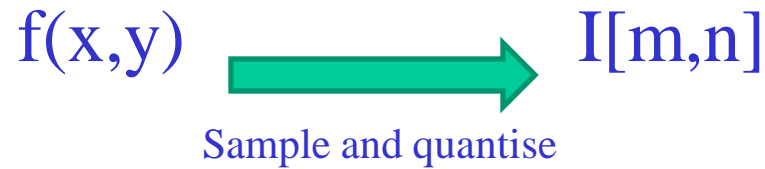
1. The number of samples used for the spatial variables
2. The number of discrete gray levels used in quantization
3. Image content

What does HD format focus on? 1, 2 or both?

Digital Image Repn. - alternatives

- As a vector $I(x)$
 - Using row or column ordering of a matrix
 - Used for computational efficiency
- Positional indexing
 - Each pixel has a single index address

Image resolution



- **Spatial resolution:** $(x,y) \rightarrow [m,n]$
 - Discretising the (spatial) domain of the function by choosing a **sampling rate**
 - Size of the image $M \times N$ = mega/giga pixels
- **Pixel or radiometric:** $f \rightarrow I$
 - Discretising the range of the function by selecting the **quantisation levels**
 - Bit-depth of the image b bits/pixel

Insufficient image resolution -effects

$$f(x,y) \rightarrow I[m,n]$$

- Too few quantisation levels for I (bits)
 - *False contouring*
- Undersampling the space (x,y)
 - *Ring*ing around edges due to *aliasing*
 - *Blockiness/checkerboard effect* with physical size of the pixel becoming larger

What is the ideal resolution?

- Depends on scene being imaged

In general:

Globally, slow variations are visually important

Locally, fast variations are visually important

1024 X 1024



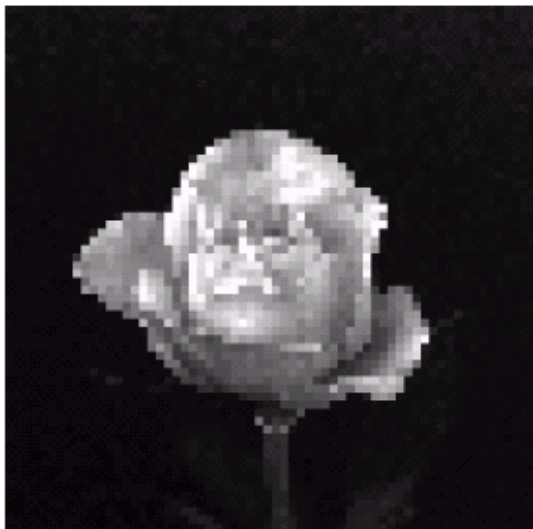
512 X 512



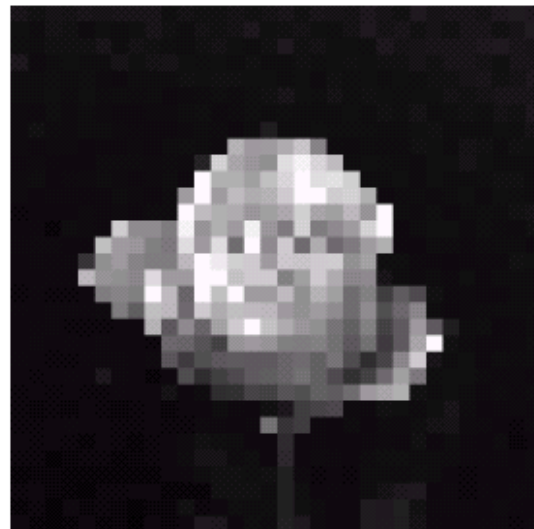
256 X 256



128 X 128



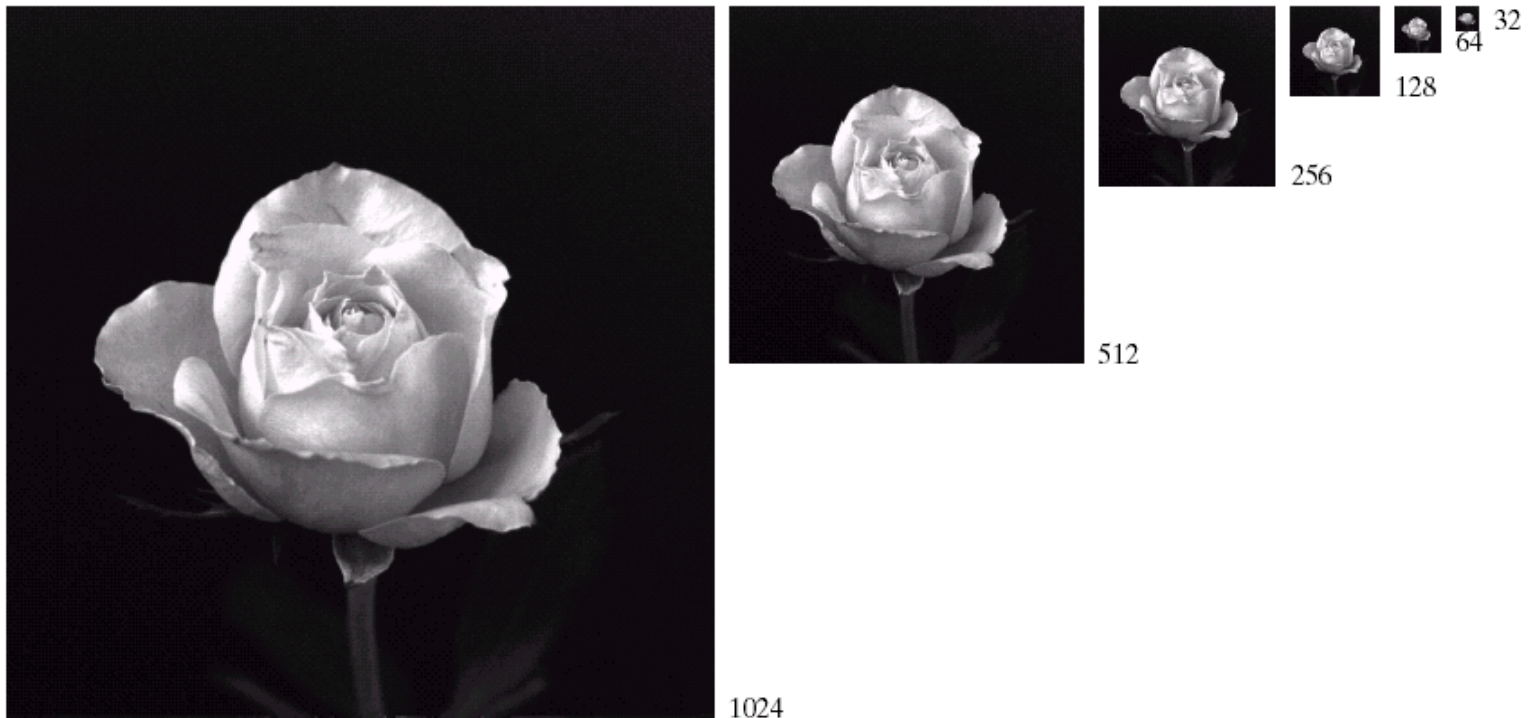
64 X 64



32 X 32

Spatial and Gray-level resolution

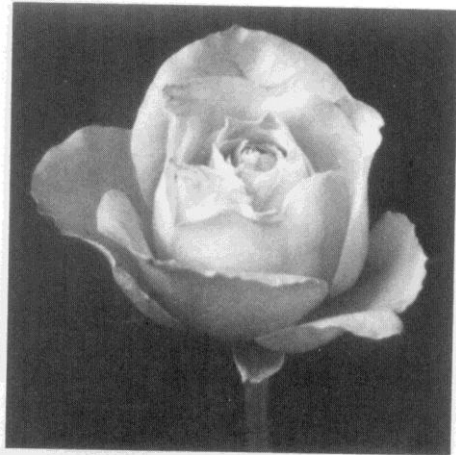
- Resolution
 - Spatial: the smallest discernible detail in an image (*sampling*)
 - Gray-level: the smallest discernible change in gray



Effect of reducing spatial resolution (fix number of gray-levels- 256)

Bit/radiometric resolution – effect of pixel depth

8 bits



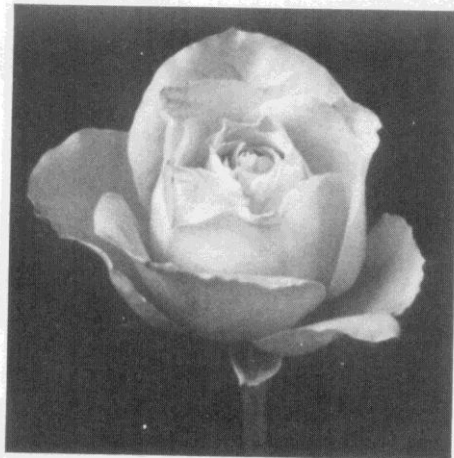
(a)

3 bits



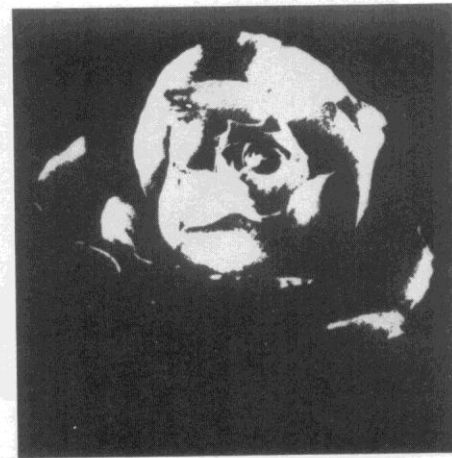
(f)

6 bits



(c)

1 bit



(e)

Effect of varying the number of gray level in a digital image

256 levels



128 levels



16 levels



8 levels



64 levels

32 levels

4 levels

2 levels

Digital Image Storage

- **Image:** $M \times N \times \text{bits/pixel}$
 - Ex. For grey scale, medium resolution images
 $M = 256 = N$ and $8 \text{ bits/pixel} = 1 \text{ byte}$
Storage requirement (raw image) $\sim 65 \text{ Kbytes}$
 - Ex. For color images = $MN \times 3$ colour planes
 $M = N = 256$ and $\text{bits/pixel} = 3 \text{ bytes}$
(1 byte each for R,G and B)
Storage requirement $\sim 196 \text{ Kbytes}$
- **Video:** $MN \text{ bytes/frame} \times \text{frame rate} \times \text{time}$
 - Ex. For a 10 minute video
 $65\text{Kb/frame} \times 20 \text{ frames/sec} \times 10 \times 60 \text{ sec} = 780 \text{ Mb}$

Pixel Neighbourhoods

A neighbourhood is a region adjacent to a given pixel
- set of pixels that share an edge or corner

➤ 4-neighbours (square)

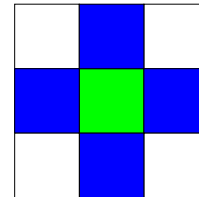
- 2 horiz. plus 2 vertical

➤ 8-neighbours (square)

- 4 diag. plus 4 neighbours

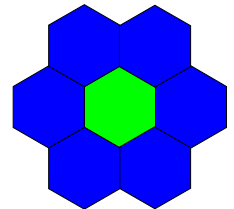
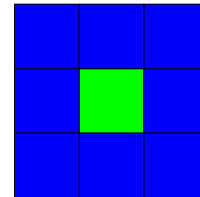
➤ 6-neighbours

- Used in hexagonal
tessellations



4-neighbours
D-neighbours

8-neighbours



6-neighbours

Neighbours

Given a pixel **p** at [m,n], its neighbours are:

- 4-Neighbours of **p**: $N_4(p) = \{2 \text{ vert. and } 2 \text{ horiz. pixels}\}$
 - Pixels at [m-1,n], [m+1,n], [m,n-1], [m,n+1]
- D-Neighbours of **p**: $N_D(p) = \{4 \text{ diagonal pixels}\}$
 - Pixels at [m+1,n+1], [m+1,n-1], [m-1,n+1], [m-1,n-1]
- 8-Neighbours of **p**: $N_8(\mathbf{p}) = N_D(\mathbf{p}) \cup N_4(\mathbf{p})$

Distance Measures

Given pixels p and q at (x_p, y_p) and (x_q, y_q)

- Euclidean distance L_2 norm (*‘as the crow flies’*)

$$[(x_p - x_q)^2 + (y_p - y_q)^2]^{1/2}$$

- City block distance L_1 norm

$$|(x_p - x_q)| + |(y_p - y_q)|$$

- Chebychev or chessboard distance L_∞ norm

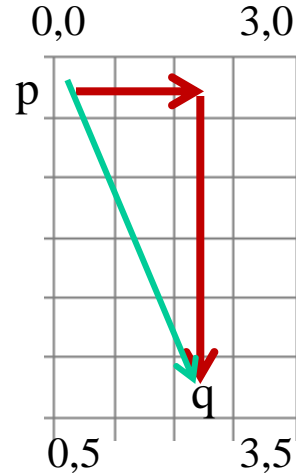
$$\max \{ |(x_p - x_q)|, |(y_p - y_q)| \}$$

Example

Euclidean distance:

City block distance:

Chess board distance:



What is the locus of
equidistant points in each of
these cases?

Connectivity

Connectivity is a measure of the **adjacency** between pixels of similar values

Pixels **p** is 4 or 8-connected to **q** if they have similar values AND $\mathbf{q} \in N_{4 \text{ or } 8}(\mathbf{p})$

Mixed connectivity

$\mathbf{q} \in N_4(\mathbf{p})$ OR

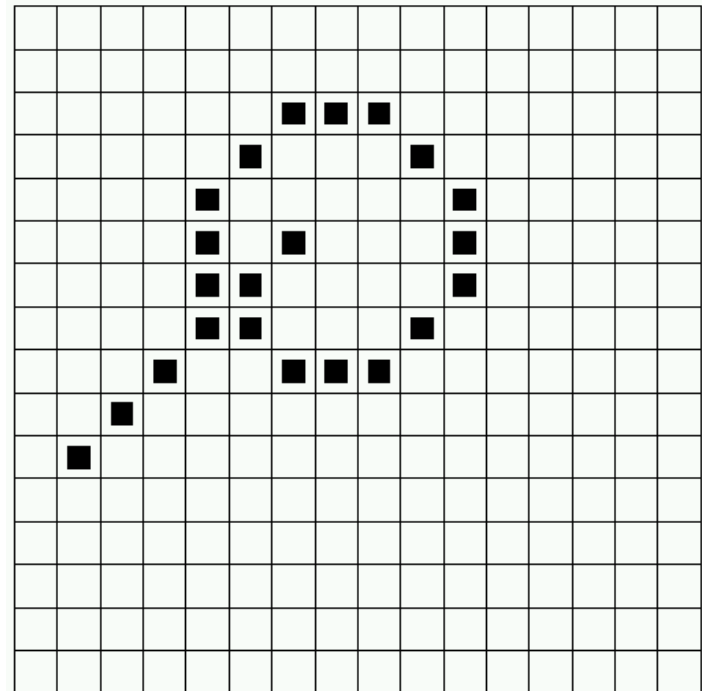
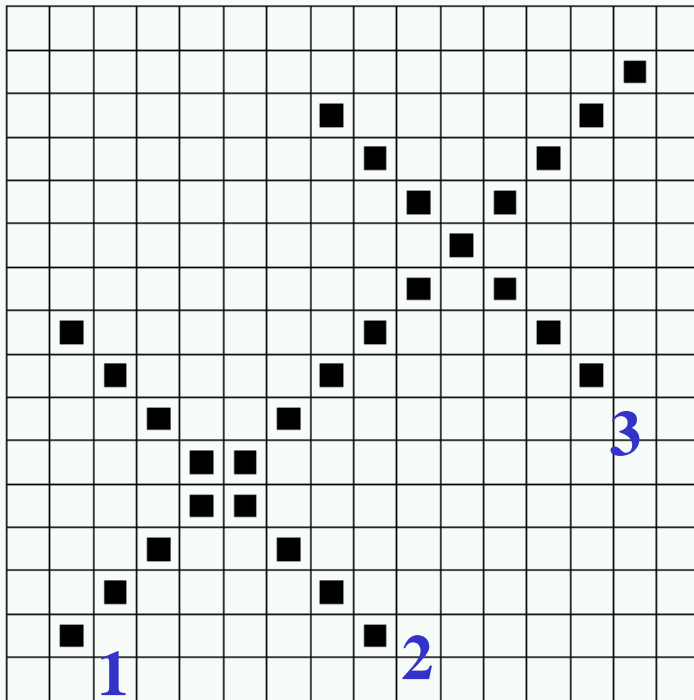
$\mathbf{q} \in N_D(\mathbf{p})$ AND $N_4(\mathbf{p}) \cap N_4(\mathbf{q}) = \Phi$

no loops can be present as is possible with N_8 .

Regions

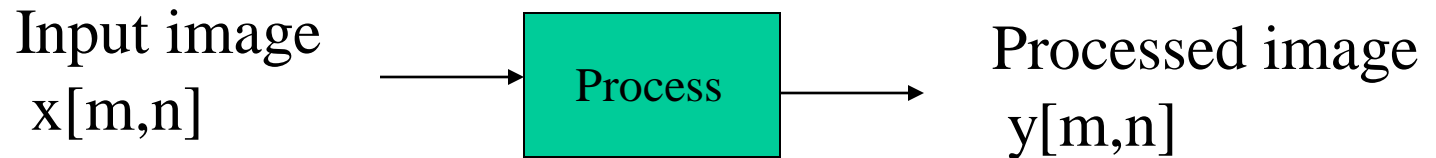
- A region is a contiguous set
 - neighbouring pixels should “touch” each other
- Square grid poses problems to defining regions
- Hexagonal grid does not pose problems

Examples



Processing an Image

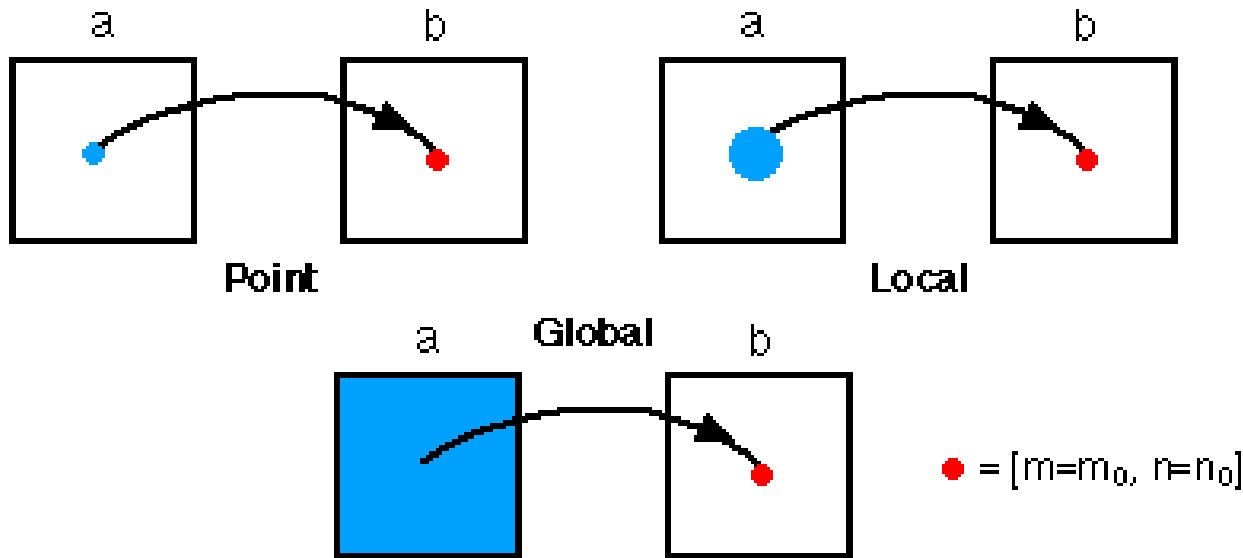
Spatial domain processing



Transform (frequency) domain processing



Spatial domain processing



a: input image
b: processed image

$$\begin{aligned}b[m_0, n_0] &= f(a[m_0, n_0]) \\b[m_0, n_0] &= f(a[N(m_0, n_0)]) \\b[m_0, n_0] &= f(a[m, n])\end{aligned}$$

Techniques for spatial domain processing

- Local or Point Operations
 - Each pixel's value is changed according to its original value
- Neighbourhood operations
 - Each pixel's value is changed according to the values of its neighbouring pixels
 - Linear or nonlinear
- Global operations
 - Each pixel's value is changed according to some global property of the entire input image
- **Challenges:** pixel addressing load, computational load, memory requirements

Type of manipulations on $I[m,n]$

On the **dependent variable** (I)

- Arithmetic (**last class**)
 - $\{+, -, *, /\}$
- Logical (binary IP)
 - $\{\text{AND, OR, NOT}\}$
- Set (binary morphological proc.)
- Statistical
 - $\{\text{Mean, variance, median, mode etc}\}$
- Convolution, correlation
 - linear vs circular convolution
 - Window/mask based computation

On the **independent variables** (m,n)

- Geometric
 - Affine transformation
- Up/down sampling
 - zoom, pan