Worksheet 7

To accompany Chapter 3.4 Transfer Functions ¶

Colophon

This worksheet can be downloaded as a PDF file. We will step through this worksheet in class.

An annotatable copy of the notes for this presentation will be distributed before the second class meeting as Worksheet 7 in the Week 3: Classroom Activities section of the Canvas site. I will also distribute a copy to your personal Worksheets section of the OneNote Class Notebook so that you can add your own notes using OneNote.

You are expected to have at least watched the video presentation of Chapter 3.4 of the notes before coming to class. If you haven't watch it afterwards!

Second Hour's Agenda

After class, the lecture recording and the annotated version of the worksheets will be made available through Canvas.

• Transfer Functions

- A Couple of Examples
- Circuit Analysis Using MATLAB LTI Transfer Function Block
- Circuit Simulation Using Simulink Transfer Function Block
- In []: % Matlab setup clear all

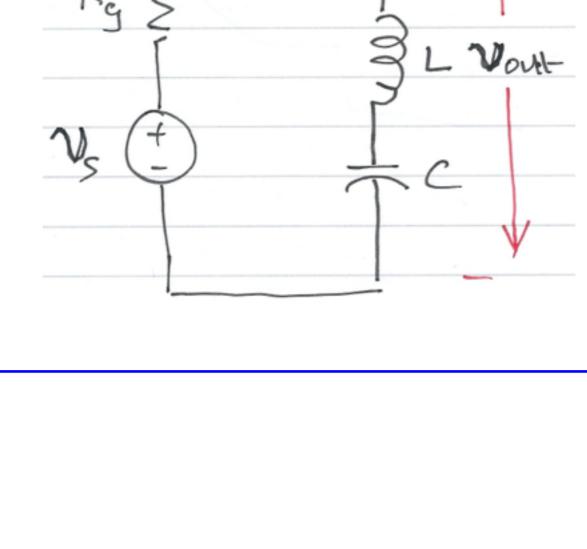
Transfer Functions for Circuits

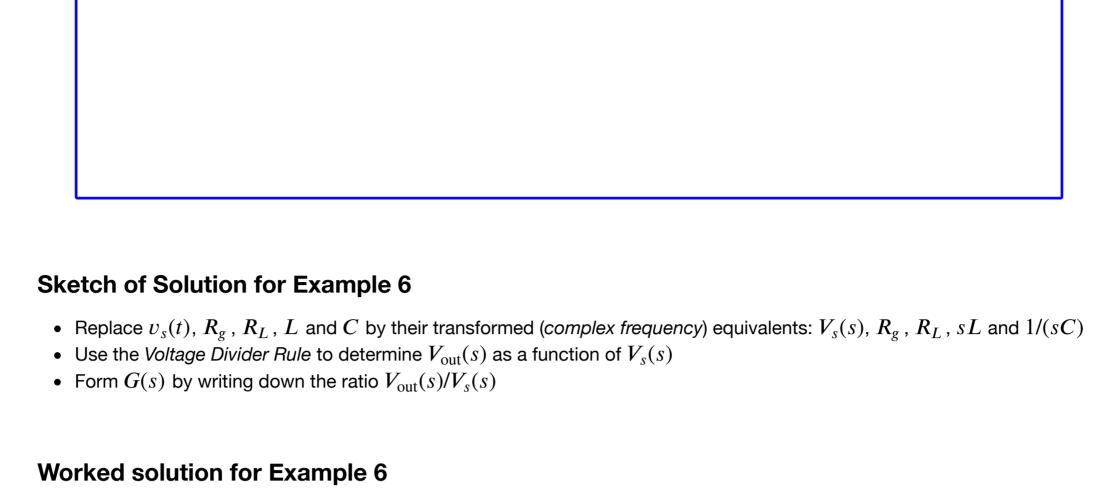
format compact

the applied (voltage) source v_s , and R_L represents the resistance of the load that consists of R_L , L and C .

Example 6

Derive an expression for the transfer function G(s) for the circuit below. In this circuit R_g represents the internal resistance of





Answer for Example 6

Pencast: ex6.pdf - open in Adobe Acrobat Reader.

Compute the transfer function for the op-amp circuit shown below in terms of the circuit constants R_1 , R_2 , R_3 , C_1 and C_2 .

 $|G(j\omega)| = \frac{|V_{\text{out}}(j\omega)|}{|V_{\text{in}}(j\omega)|}$

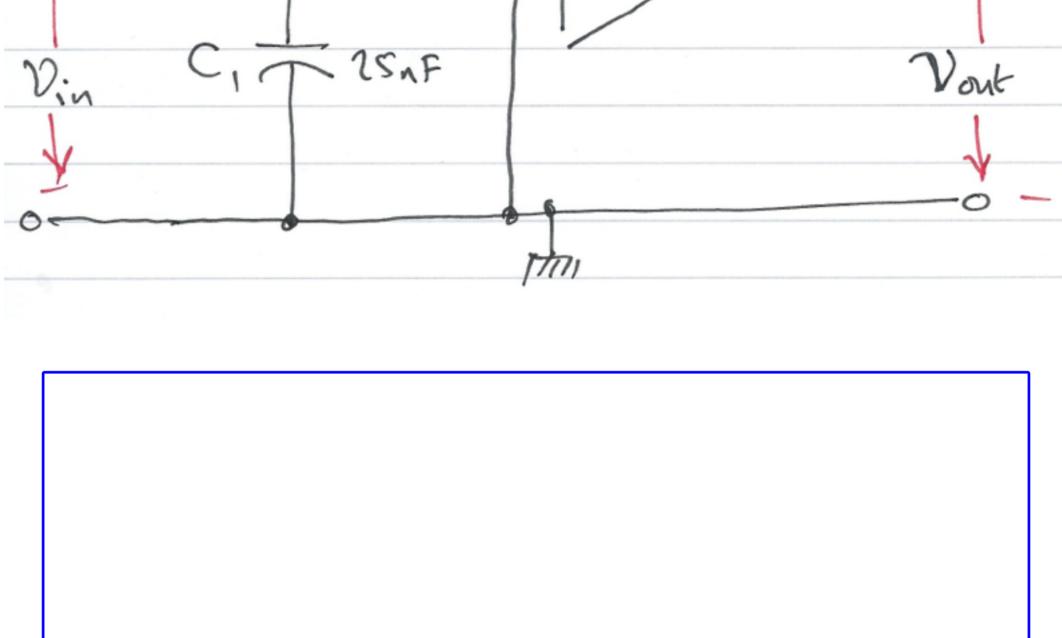
Then replace the complex variable s with $j\omega$, and the circuit constants with their numerical values and plot the magnitude

 $G(s) = \frac{V_{\text{out}}(s)}{V_s(s)} = \frac{R_L + sL + 1/sC}{R_g + R_L + sL + 1/sC}.$

versus radian frequency ω rad/s.

Example 7

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$G(s) = \frac{V_{\text{out}}(s)}{V_{\text{in}}(s)} = \frac{-1}{R_1 \left((1/R_1 + 1/R_2 + 1/R_3 + sC_1)(sC_2R_3) + 1/R_2 \right)}.$

Worked solution for Example 7

Pencast: <u>ex7.pdf</u> - open in Adobe Acrobat Reader.

Sketch of Solution for Example 7

• Solve for $V_{\mathrm{out}}(s)$ as a function of $V_{\mathrm{in}}(s)$

on log-linear "paper".

Answer for Example 7

See attached script: <u>solution7.m</u>.

The Matlab Bit

In []: syms s;

In []: $R1 = 200*10^3$;

In []: format long

In []: a = denG(1);

In []: w = 1:10:10000;

b = denG(2);

In []: semilogx(w, abs(Gs))

In []: $Gs = -1./(a*w.^2 - j.*b.*w + denG(3));$

a nicely formatted document.

input output function

Calculate the step response using the LTI functions.

From a previous analysis the transfer function is:

so substituting the component values we get:

Verify the result with Simulink.

Matlab's residue function.

In []: $G = tf([-1],[1 \ 3 \ 1])$

Simples!

Simulink model

See <u>example 8.slx</u>

open example 8

In []:

In []:

Define the circuit as a transfer function

MATLAB Solution

The Matlab solution: example8.m

 $R2 = 40*10^3;$ $R3 = 50*10^3;$

simplify(den)

 $C1 = 25*10^{(-9)}$; $C2 = 10*10^{(-9)}$;

Plot

• Form the reciprocal $G(s) = V_{\rm out}(s)/V_{\rm in}(s)$

Week 3: Solution 7

• Replace the components and voltages in the circuit diagram with their complex frequency equivalents

 $|G(j\omega)|$

• Use nodal analysis to determine the voltages at the nodes either side of the 50K resistor R_3

• Note that the voltage at the input to the op-amp is a virtual ground

• Use MATLAB to calculate the component values, then replace s by $j\omega$.

Result is: 100*s*((7555786372591433*s)/302231454903657293676544 + 1/20000) + 5 Simplify coefficients of s in denominator

denG = sym2poly(ans)

In []: den = R1*((1/R1+ 1/R2 + 1/R3 + s*C1)*(s*R3*C2) + 1/R2);

In []: numG = -1;Plot For convenience, define coefficients *a* and *b*:

 $G(j\omega) = \frac{-1}{a\omega^2 - jb\omega + 5}$

Please use the file tf_matlab.m to explore the Transfer Function features provide by Matlab. Use the publish option to generate

The Simulink transfer function (Transfer Fcn) block shown above implements a transfer function representing a general

 $G(s) = \frac{V_{\text{out}}}{V_{\text{in}}} = \frac{-1}{R_1 \left[(1/R_1 + 1/R_2 + 1/R_3 + sC_1)(sR_3C_2) + 1/R_2 \right]}$

 $G(s) = \frac{V_{\text{out}}}{V_{\text{in}}} = \frac{-1}{s^2 + 3s + 1}$

 $V_{\text{out}}(s) = \frac{-1}{s^2 + 3s + 1} \cdot \frac{1}{s}$

We can solve this by partial fraction expansion and inverse Laplace transform as is done in the text book with the help of

xlabel('Radian frequency w (rad/s') ylabel('|Vout/Vin|') title('Magnitude Vout/Vin vs. Radian Frequency') grid

Using Transfer Functions in Matlab for System Analysis

Using Transfer Functions in Simulink for System Simulation

 $G(s) = \frac{N(s)}{D(s)}$ that it is not specific nor restricted to circuit analysis. It can, however be used in modelling and simulation studies. **Example** Recast Example 7 as a MATLAB problem using the LTI Transfer Function block. For simplicity use parameters $R_1=R_2=R_3=1~\Omega$, and $C_1=C_2=1~\mathrm{F}$.

step response is then: step(G)

Here, however we'll use the LTI block that was introduced in the lecture.

We can find the step response by letting $v_{\rm in}(t)=u_0(t)$ so that $V_{\rm in}(s)=1/s$ then

Result Scope View Tools Simulation Help

num(s) den(s)



• Simulink model [example8.slx] cd ../matlab

• Example 8 [example8.m]

Matlab Solutions accompanying MATLAB folder.

• Solution 7 [solution7.m]

open solution7

In []: |

In []:

ls

0.5

Ready Let's go a bit further by finding the frequency response: bode(G)

For convenience, single script MATLAB solutions to the examples are provided and can be downloaded from the

T=10.000

Sample based