

## Using Laplace Transforms for Circuit Analysis

The preparatory reading for this section is <u>Chapter 4</u> [<u>Kar12</u>] which presents examples of the applications of the Laplace transform for electrical solving circuit problems.

#### Colophon

An annotatable worksheet for this presentation is available as **Worksheet 6**.

- The source code for this page is <a href="laplace-transform/3/circuit\_analysis.ipynb">laplace\_transform/3/circuit\_analysis.ipynb</a>.
- You can view the notes for this presentation as a webpage (HTML).
- This page is downloadable as a PDF file.

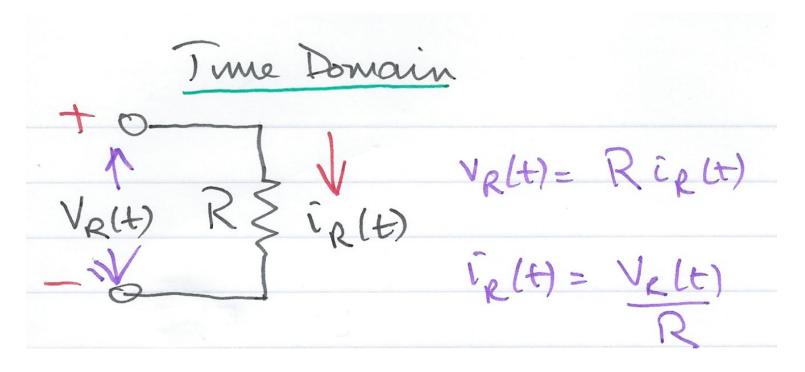
### Agenda

We look at applications of the Laplace Transform for

- Circuit transformation from Time to Complex Frequency
- Complex impedance
- Complex admittance

# Circuit Transformation from Time to Complex Frequency

Time Domain Model of a Resistive Network



Complex Frequency Domain Model of a Resistive Circuit

#### Colophon

<u>Agenda</u>

Print to PDF

<u>Circuit Transformation from Time to</u> <u>Complex Frequency</u>

<u>Time Domain Model of a Resistive</u> <u>Network</u>

Complex Frequency Domain Model of a Resistive Circuit

<u>Time Domain Model of an Inductive</u> <u>Network</u>

Complex Frequency Domain Model of an Inductive Network

<u>Time Domain Model of a Capacitive</u> <u>Network</u>

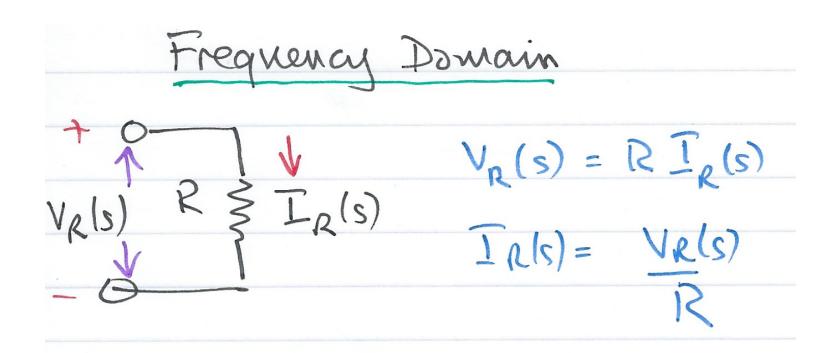
<u>Complex Frequency Domain of a</u> <u>Capacitive Network</u>

<u>Examples</u>

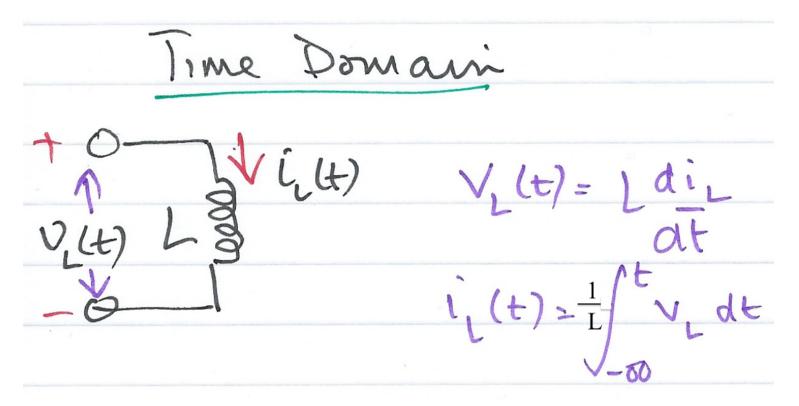
Complex Impedance Z(s)

Complex Admittance Y(s)

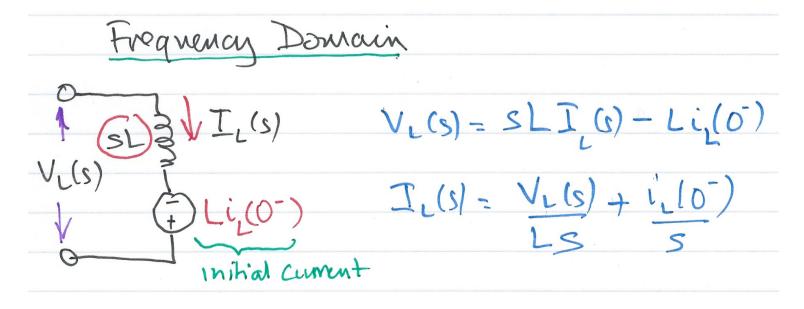
Reference



Time Domain Model of an Inductive Network



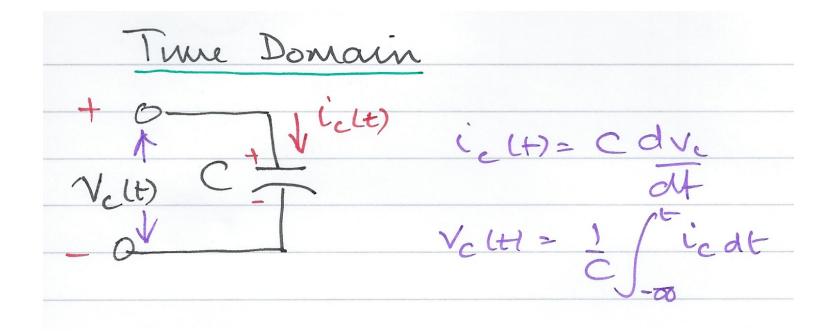
Complex Frequency Domain Model of an Inductive Network



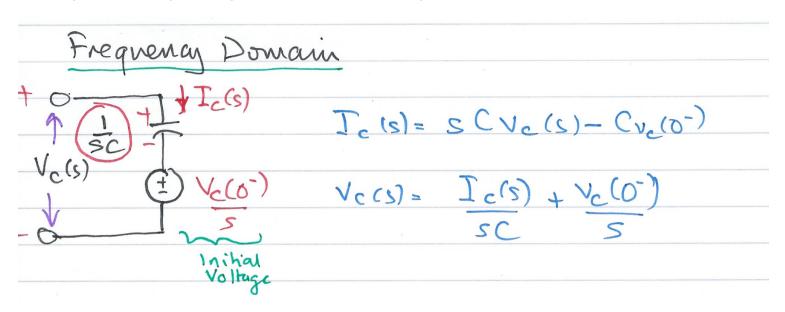
Time Domain Model of a Capacitive Network







### Complex Frequency Domain of a Capacitive Network

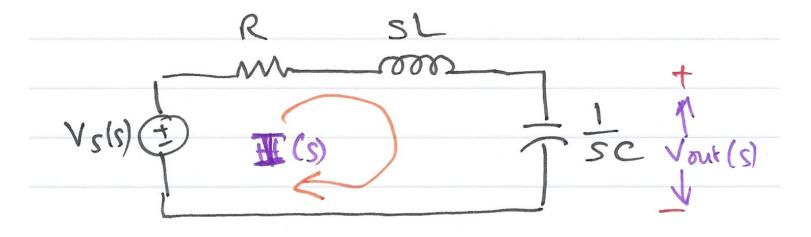


#### Examples

We will work through these in class. See worksheet 6.

# Complex Impedance Z(s)

Consider the s-domain RLC series circuit, where the initial conditions are assumed to be zero.



For this circuit, the sum

$$R + sL + \frac{1}{sC}$$

represents that total opposition to current flow. Then,

$$I(s) = \frac{V_s(s)}{R + sL + 1/(sC)}$$

and defining the ratio  $V_s(s)/I(s)$  as Z(s), we obtain

$$Z(s) = \frac{V_s(s)}{I(s)} = R + sL + \frac{1}{sC}$$

$$I(s) = \frac{V_s(s)}{Z(s)}$$

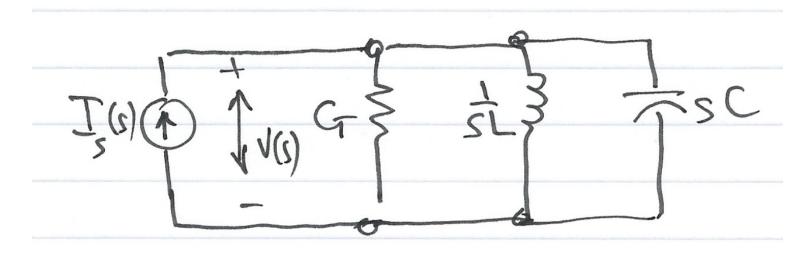
where

$$Z(s) = R + sL + \frac{1}{sC}.$$

Since  $s = \sigma + j\omega$  is a complex number, Z(s) is also complex and is known as the *complex input impedance* of this RLC series circuit.

# Complex Admittance Y(s)

Consider the s-domain GLC parallel circuit shown below where the initial conditions are zero.



For this circuit

$$GV(s) + \frac{1}{sL}V(s) + sCV(s) = I_s(s)$$

$$\left(G + \frac{1}{sL} + sC\right)V(s) = I_s(s)$$

Defining the ratio  $I_s(s)/V(s)$  as Y(s) we obtain

$$Y(s) = \frac{I_s(s)}{V(s)} = G + \frac{1}{sL} + sC = \frac{1}{Z(s)}$$

The s-domain voltage V(s) can be found from

$$V(s) = \frac{I_s(s)}{Y(s)}$$

where

$$Y(s) = G + \frac{1}{sL} + sC.$$

Y(s) is complex and is known as the *complex input admittance* of this GLC parallel circuit.

#### Reference

See Bibliography.

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