Worksheet 7

To accompany Chapter 3.4 Transfer Functions

Colophon

This worksheet can be downloaded as a PDF_file. We will step through this worksheet in class. An annotatable copy of the notes for this presentation will be distributed before the second class meeting as Worksheet 7 in

the Week 3: Classroom Activities section of the Canvas site. I will also distribute a copy to your personal Worksheets section of the OneNote Class Notebook so that you can add your own notes using OneNote. You are expected to have at least watched the video presentation of Chapter 3.4 of the notes before coming to class. If you

After class, the lecture recording and the annotated version of the worksheets will be made available through Canvas.

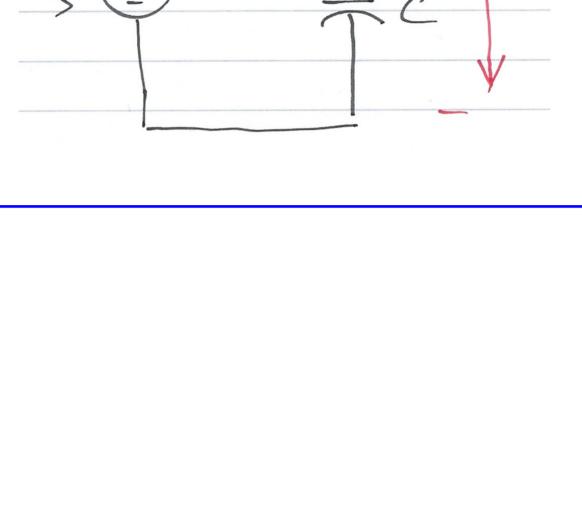
Transfer Functions

clear all

cd ../matlab

- A Couple of Examples
- Circuit Analysis Using MATLAB LTI Transfer Function Block
- imatlab_export_fig('print-svg') % Static svg figures. format compact

Transfer Functions for Circuits Example 6



Answer for Example 6

Worked solution for Example 6

Pencast: <u>ex6.pdf</u> - open in Adobe Acrobat Reader.

 $G(s) = \frac{V_{\text{out}}(s)}{V_s(s)} = \frac{R_L + sL + 1/sC}{R_g + R_L + sL + 1/sC}.$

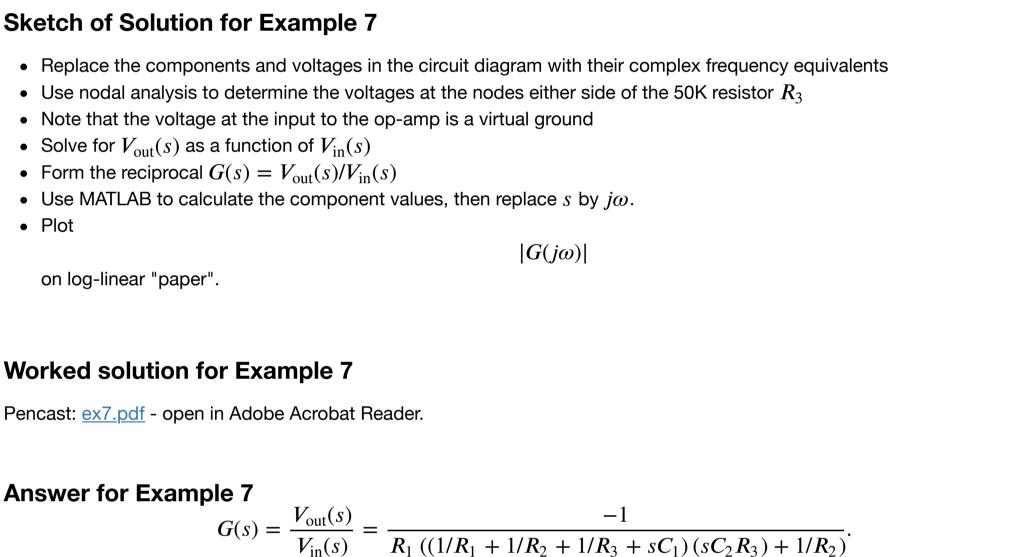
 $|G(j\omega)| = \frac{|V_{\text{out}}(j\omega)|}{|V_{\text{in}}(j\omega)|}$

10nF

ullet Use the *Voltage Divider Rule* to determine $V_{
m out}(s)$ as a function of $V_s(s)$

• Form G(s) by writing down the ratio $V_{\rm out}(s)/V_s(s)$

versus radian frequency ω rad/s.



In []: $R1 = 200*10^3$; $R2 = 40*10^3;$

Simplify coefficients of s in denominator

In []: den = R1*((1/R1+ 1/R2 + 1/R3 + s*C1)*(s*R3*C2) + 1/R2);

 $G(j\omega) = \frac{-1}{a\omega^2 - jb\omega + 5}$

Result is: 100*s*((7555786372591433*s)/302231454903657293676544 + 1/20000) + 5

Using Transfer Functions in Simulink for System Simulation

The Matlab solution: example8.m

From a previous analysis the transfer function is:

Define the circuit as a transfer function

In []: $G = tf([-1],[1 \ 3 \ 1])$

In []: step(G)

Simples!

Simulink model

See example 8.slx

step response is then:

MATLAB Solution

input output function

Example

In []: $Gs = -1./(a*w.^2 - j.*b.*w + denG(3));$

xlabel('Radian frequency w (rad/s')

title('Magnitude Vout/Vin vs. Radian Frequency')

 $G(s) = \frac{V_{\text{out}}}{V_{\text{in}}} = \frac{-1}{R_1 \left[(1/R_1 + 1/R_2 + 1/R_3 + sC_1)(sR_3C_2) + 1/R_2 \right]}$ so substituting the component values we get: $G(s) = \frac{V_{\text{out}}}{V_{\text{in}}} = \frac{-1}{s^2 + 3s + 1}$

Recast Example 7 as a MATLAB problem using the LTI Transfer Function block.

In []: open example_8

We can find the step response by letting $v_{\rm in}(t)=u_0(t)$ so that $V_{\rm in}(s)=1/s$ then $V_{\rm out}(s)=\frac{-1}{s^2+3s+1}.\frac{1}{s}$ We can solve this by partial fraction expansion and inverse Laplace transform as is done in the text book with the help of Matlab's residue function. Here, however we'll use the LTI block that was introduced in the lecture.

Result Scope

Help

Sample based

T=10.000

• Solution 7 [solution7.m] • Example 8 [example8.m]

haven't watch it afterwards! **Agenda**

• Circuit Simulation Using Simulink Transfer Function Block In []: % Matlab setup

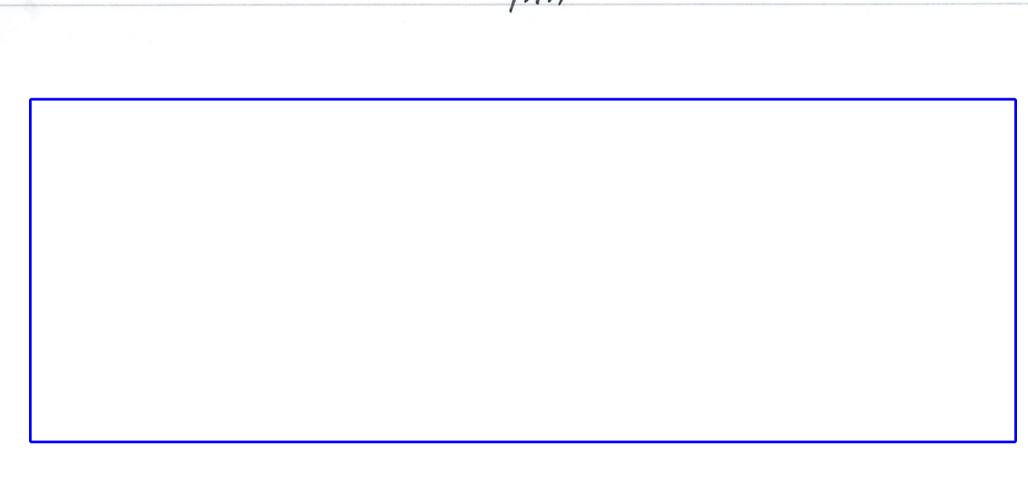
Transfer Functions for Circuits

Example 6

Derive an expression for the transfer function
$$G(s)$$
 for the circuit below. In this circuit R_g represents the internal resistance of the applied (voltage) source v_s , and R_L represents the resistance of the load that consists of R_L , L and C .

Sketch of Solution for Example 6 • Replace $v_s(t)$, R_g , R_L , L and C by their transformed (complex frequency) equivalents: $V_s(s)$, R_g , R_L , SL and 1/(SC)

Example 7 Compute the transfer function for the op-amp circuit shown below in terms of the circuit constants R_1 , R_2 , R_3 , C_1 and C_2 . Then replace the complex variable s with $j\omega$, and the circuit constants with their numerical values and plot the magnitude



In []: syms s;

The Matlab Bit

Week 3: Solution 7

 $R3 = 50*10^3;$

simplify(den)

In []: w = 1:10:10000;

In []: semilogx(w, abs(Gs))

grid

ylabel('|Vout/Vin|')

 $C1 = 25*10^{(-9)};$ $C2 = 10*10^{(-9)};$

See attached script: <u>solution7.m</u>.

For simplicity use parameters $R_1=R_2=R_3=1~\Omega$, and $C_1=C_2=1~\mathrm{F}$. Calculate the step response using the LTI functions. Verify the result with Simulink.

that it is not specific nor restricted to circuit analysis. It can, however be used in modelling and simulation studies.

The Simulink transfer function (Transfer Fcn) block shown above implements a transfer function representing a general

 $G(s) = \frac{N(s)}{D(s)}$

num(s) den(s)

Simulation

- ⊕ +

View

accompanying MATLAB folder.

Ready Let's go a bit further by finding the frequency response:

bode(G)

cd ../matlab

open solution7

In []:

Matlab Solutions For convenience, single script MATLAB solutions to the examples are provided and can be downloaded from the • Simulink model [example 8.slx]