# **Lab 5: Fourier Series**

## **Preamble**

### **Associated Class Notes**

This lab supports the materials covered in Chapter 4 Fourier Series of the course notes. You may wish to refer to worksheet 9 and worksheet 10 for additional examples to try.

### This document is available in HTML format for online viewing and PDF for printing.

Other formats

### These examples have been adapted from Chapter 7 of Stephen Karris, Signals and Systems: With MATLAB Computing and

**Acknowledgements** 

<u>Simulink Modeling (5th Edition)</u>. The Simulink model used in Lab Exercise 16 was developed by Third Year EEE Student Fahad Alqahtani as part of his Level 3

Project in 2013-2014.

### To explore Fourier series and the use of the Symbolic Toolkit to compute the Fourier coefficients and to demonstrate the

**Aims** 

simulation and analysis of Fourier series in Simulink.

lab01

Setup

### If you haven't already, create a suitable folder structure on your file-store for your labs.

# I suggest

Before you start

OneDrive\workspace

lab03 lab04 lab05

To install, visit the page and scroll down to find the Fourier Series Demo app (see image below)

Requirements: Matlab 6 or greater Tested on: Windows, Linux

(Version 1.44)

## Lab Exercises

# **Download work files**

Lab Exercise 9: Computation of the coefficients of the Trig. Fourier Series

Download the attached files:

and store them in your lab05 folder.

Part 1

the trig. Fourier series for the square-wave waveform with even symmetry (Section 7.4.1 in the textbook). *Hints*: shift the waveform  $\pi/2$  radians to the left by letting  $f(t) = f(t + T_0/4)$ . This *advances* the waveform by  $T_0/4$  s. In calculating the final plot, subtract  $T_0/4$  from  $\tau$ .

Save the m-file trig\_fseries.m as a MATLAB Live Script ex9\_1.mlx. Change the script so that it computes and plots

# Note

Part 2

Download and open the Simulink model fourier\_example.slx. Examine the settings for the sine terms and compare the amplitudes and frequencies of the settings with the results of running trig\_fseries.m. Run the simulation and view the reconstructed signal and the spectrum.

change in the sine wave generators to get the right results? Part 5

## Lab Exercise 11: Computation of the coefficients of Exponential Fourier Series In this lab exercise we will review the Fourier series for a square wave with odd and even symmetry before going on to compute

and plot the Fourier series for the triangular waveform.

**Parseval's Theorem** in the notes). In MATLAB this would be:

stem(k,C(k)\*conj(C(k)))

P = sum(C.\*conj(C))

Prms = sqrt(sum(C.\*conj(C)))

d. Estimate the **Total Harmonic Distortion** in the signal

**Exercise 10: Simulating Wave Analysis** 

Download the attached file: exp\_fseries.m

of f(t) that you used in Exercise 9. Part 8

FourierSeries function, defined in FourierSeries.m, to calculate the trigonometric Fourier series for the square wave with odd-symmetry. In other words, it reconstructs the  $a_k$  and  $b_k$  Coefficients from the exponential Fourier series coefficients  $C_k$ .

### Parts 2 and 3 can be added to trig\_fseries and the whole submitted as a single Live Script file ex9.mlx providing that you use section headings to separate the parts and edit/add to the textual commentary to match the exercise descriptions.

Part 4

Change the settings so that the Simulink model uses the coefficients from the triangular wave result. Simulate and capture the time and spectrum plots. Save your model as ex10 2.slx.

# Part 6 Open the script exp fseries.m as a Live Script, run it and examine the results. Note that the script calls the

Part 7

**Before you Start** 

The Simulink model plots the *Power Spectrum* of the simulated reconstructed signal. To plot the power spectrum of a

exponential Fourier series we need to produce a stem plot. Each stem in the power spectrum is computed using  $C_k C_k^*$  (see

a. Plot the Power Spectrum of the signal from exponential Fourier series coefficients computed in **Part 7**. Compare the

MATLAB:

c. Estimate the RMS power in the signal  $P_{\rm RMS} = \sqrt{\sum_{k=-N}^{N} |C_k|^2}$ MATLAB:

THD% =  $100 \frac{\sqrt{\sum_{k=2}^{N} |C_k|^2}}{\sqrt{|C_1|^2}}$ 

**Note** ex11.mlx.

Claim

**Deadline** 

MATLAB:

Up to 2 marks can be claimed if you complete Exercise 9, 1 mark for Exercise 10 and an addition 2 marks Exercise 11.

**Submission** You should submit the following to the Lab 05: Fourier series Assignment on Canvas.

1. Complete the labwork self-assessment claim form and declaration. 2. As evidence of completion of Lab Exercise 9, you should upload ex9 1.mlx and ex9 2.mlx (can be sections in one

The deadline for claims and submission is 4:00 pm, 24th March 2021

from the Ck coefficients. Why did I do that do you think?

this could be changed, for example when computing FS for even signals, the limits could be adjusted to [-T/2, T/2]. In MATLAB we can achieve this by adding extra arguments to the function definition.

Part 9 Examine the code for the FourierSeries function that is defined in FourierSeries.m. Adapt the function definition so

that the user can define the range of the Fourier Series integral. If you succeed, use the modified function to compute the Fourier series of the triangular wave form by exploiting half-wave symmetry. Save the script that does this as ex11 3.

A problem with the scripts as provided is that the limits on the integrals are set in the range [0,T]. It would be convenient if

4. As evidence of completion of Lab Exercise 11, you should upload ex11 1.mlx and ex11 2.mlx (can be sections in

If you made the suggested change to FourierSeries, provide compatible changes to your copy of TrigFourierSeries. Test it on a square wave with even symmetry (Lab 9 Part 2). Save the resulting calling script as

 $ex9_3$ .

**Assessment criteria** This will be a self-assessed exercise.

Up to 2 marks can be claimed if you complete Exercise 9, 1 mark for Exercise 10 and an addition 2 marks for Exercise 11. Detailed marking criteria for this and the other labs and the project are given in the linked Assessment Criteria [Google sheet].

signals-and-systems-lab

**FourierSeries** 

lab02

FourierSeriesDemo is a GUI that shows Fourier Series synthesis for different number of Fourier coefficients. Different signals can be selected: square wave, sawtooth, triangle and rectified sinusoids.

Download:

MATLAB Command Name: fseriesdemo

FourierSeriesDemo

Last update: 30-Mar-2016 Right-click on the Blue Button labelled FourierSeriesDemo and save to your lab05 folder. Open and run fseriesdemo/fseriesdemo.m. If MATLAB issues a message about the need to change the working directory or add a folder to the MATLAB path. Accept the choice given. Spend some time playing with the settings and observing the results. We will use this as a check of results of the labs to follow.

#### In this lab exercise we will review the Fourier series for a square wave with odd and even symmetry before going on to compute and plot the Fourier series for the *triangular* waveform. We will also explore and confirm the stated results of even-, odd- and half-wave symmetries.

 TrigFourierSeries.m FourierSeries.m trig\_fseries.m

Open the script trig fseries.m as a MATLAB Live Script. Run the script and read through the results. Note that the script calls the TrigFourierSeries function, defined in the file TrigFourierSeries.m, which in turn calls the

Part 3 Copy the script trig fseries.m and save it as a MATLAB Live Script ex9 2.mlx. Change the copy so that it computes and plots the trig. Fourier series for the Triangular waveform (Section 7.4.3 in the textbook).

and capture the time and spectrum plots. Save your model as ex10 1.slx. *Hint*: Be careful to evaluate which set of coefficients are present in the Fourier series. Are they  $a_k$  or  $b_k$ ? What do you need to

Change the settings so that the Simulink model uses the coefficients from the square-wave even-symmetry result. Simulate

# We will also explore and confirm the stated results of even-, odd- and half-wave symmetries.

FourierSeries function defined in TrigFourierSeries.m to calculate the exponential Fourier series for the square wave with odd-symmetry.

Copy the script exp fseries.m and save it as ex11 1. Change the copy so that it computes and plots the exponential

Fourier series for the square-wave waveform with even symmetry (Section 7.4.1 in the textbook). *Hint*: Use the same definition

computed power spectrum with the simulated power spectrum. *Note*: expect some differences! b. Estimate the power in the first N-harmonics of the signal using:  $P = \sum_{k=-N}^{N} |C_k|^2$ 

C1 = Ck(1); % first harmonic Charm = Ck(2:length(Ck)); % remaining harmonics THD = 100 \* sqrt(sum(Charm.\*conj(Charm)))/sqrt(C1\*conj(C1)) As for Exercise 9, parts 7 and 8 can be added to exp\_fseries and the whole submitted as a single Live Script file

### Live Script ex9.mlx). 3. As evidence of completion of Lab Exercise 10, you should upload the Simulink models ex10 1.slx and ex10 2.slx.

one Live Script ex11.mlx).

What to hand in

Optional Additional Tasks: Review and Change the Code.

Part 10 Examine the code that is defined in TrigFourierSeries. Note that it calls FourierSeries then computes ak and bk

Compute the FS of the half-wave rectified cosine function. Save the resulting calling script as ex11 4.

Use folder OneDrive\workspace\signals-and-systems-lab\lab05 for this lab. **Preparation** Before we start today's lab you will need to download and install the Fourier series demo app, that was demonstrated in class, from Georgia Tech's Educational Matlab GUIs page.