Lab 5: Fourier Series

Preamble

Associated Class Notes

This lab supports the materials covered in Chapter 4 Fourier Series of the course notes. You may wish to refer to worksheet 9 and worksheet 10 for additional examples to try.

This document is available in HTML format for online viewing and PDF for printing.

Other formats

Simulink_Modeling_(5th_Edition). The Simulink model used in Lab Exercise 16 was developed by Third Year EEE Student Fahad Algahtani as part of his Level 3

Project in 2013-2014.

To explore Fourier series and the use of the Symbolic Toolkit to compute the Fourier coefficients and to demonstrate the simulation and analysis of Fourier series in Simulink.

Aims

Assessment criteria

Up to 2 marks can be claimed if you complete Exercise 9, 1 mark for Exercise 10 and an addition 2 marks for Exercise 11.

Detailed marking criteria for this and the other labs and the project are given in the linked Assessment Criteria [Google sheet].

Setup

OneDrive\workspace

lab04 lab05

class, from Georgia Tech's Educational Matlab GUIs page.

MATLAB Command Name: fseriesdemo Download: FourierSeriesDemo (Version 1.44) Requirements: Matlab 6 or greater Tested on: Windows, Linux Last update: 30-Mar-2016 Right-click on the Blue Button labelled **FourierSeriesDemo** and save to your lab05 folder. If MATLAB issues a message about the need to change the working directory or add a folder to the MATLAB path. Accept the

and plot the Fourier series for the *triangular* waveform.

Lab Exercise 9: Computation of the coefficients of the Trig. Fourier Series In this lab exercise we will review the Fourier series for a square wave with odd and even symmetry before going on to compute

TrigFourierSeries.m

FourierSeries.m

trig_fseries.m

Part 1

 C_k .

Copy the script trig fseries.m and save it as a MATLAB Live Script ex9 2.mlx. Change the copy so that it computes

Download and open the Simulink model fourier_example.slx. Examine the settings for the sine terms and compare the amplitudes and frequencies of the settings with the results of running trig_fseries.m. Run the simulation and view the

Part 4

Change the settings so that the Simulink model uses the coefficients from the square-wave even-symmetry result. Simulate and capture the time and spectrum plots. Save your model as ex10 1.slx. *Hint*: Be careful to evaluate which set of coefficients are present in the Fourier series. Are they a_k or b_k ? What do you need to

We will also explore and confirm the stated results of even-, odd- and half-wave symmetries. Before you Start

In this lab exercise we will review the Fourier series for a square wave with odd and even symmetry before going on to compute

and plot the Fourier series for the triangular waveform.

Parseval's Theorem in the notes). In MATLAB this would be:

Exercise 10: Simulating Wave Analysis

change in the sine wave generators to get the right results?

Download the attached file: exp_fseries.m

Part 8 The Simulink model plots the *Power Spectrum* of the simulated reconstructed signal. To plot the power spectrum of a

of f(t) that you used in Exercise 9.

Part 7

a. Plot the Power Spectrum of the signal from exponential Fourier series coefficients computed in **Part 7**. Compare the computed power spectrum with the simulated power spectrum. Note: expect some differences! b. Estimate the power in the first N-harmonics of the signal using:

stem(k,C(k)*conj(C(k)))

Prms = sqrt(sum(C.*conj(C)))

MATLAB: P = sum(C.*conj(C))c. Estimate the RMS power in the signal

 $P = \sum_{k=-N}^{N} |C_k|^2$

 $P_{\rm RMS} = \sqrt{\sum_{k=-N}^{N} |C_k|^2}$

Note

Deadline

Claim

ex11.mlx.

What to hand in

Live Script ex9.mlx).

4. As evidence of completion of Lab Exercise 11, you should upload ex11 1.mlx and ex11 2.mlx (can be sections in one Live Script ex11.mlx).

- The deadline for claims and submission is 4:00 pm, 24th March 2021
- this could be changed, for example when computing FS for even signals, the limits could be adjusted to [-T/2, T/2]. In MATLAB we can achieve this by adding extra arguments to the function definition.

Part 9

Examine the code for the FourierSeries function that is defined in FourierSeries.m. Adapt the function definition so that the user can define the range of the Fourier Series integral. If you succeed, use the modified function to compute the Fourier series of the triangular wave form by exploiting half-wave symmetry. Save the script that does this as ex11 3.

A problem with the scripts as provided is that the limits on the integrals are set in the range [0,T]. It would be convenient if

If you made the suggested change to FourierSeries, provide compatible changes to your copy of TrigFourierSeries. Test it on a square wave with even symmetry (Lab 9 Part 2). Save the resulting calling script as

Acknowledgements These examples have been adapted from Chapter 7 of Stephen Karris, Signals and Systems: With MATLAB Computing and

This will be a self-assessed exercise.

If you haven't already, create a suitable folder structure on your file-store for your labs. I suggest

FourierSeries

choice given. Spend some time playing with the settings and observing the results. We will use this as a check of results of the labs to follow.

Lab Exercises

and store them in your lab05 folder.

Hints: shift the waveform $\pi/2$ radians to the left by letting $f(t) = f(t + T_0/4)$. This *advances* the waveform by $T_0/4$ s. In calculating the final plot, subtract $T_0/4$ from τ . Part 3

FourierSeries function, defined in FourierSeries.m, to calculate the trigonometric Fourier series for the square wave

with odd-symmetry. In other words, it reconstructs the a_k and b_k Coefficients from the exponential Fourier series coefficients

reconstructed signal and the spectrum.

Change the settings so that the Simulink model uses the coefficients from the triangular wave result. Simulate and capture the time and spectrum plots. Save your model as ex10 2.slx. Lab Exercise 11: Computation of the coefficients of Exponential Fourier Series

Open the script exp fseries.m as a Live Script, run it and examine the results. Note that the script calls the FourierSeries function defined in TrigFourierSeries.m to calculate the exponential Fourier series for the square wave with odd-symmetry.

Copy the script exp_fseries.m and save it as ex11_1. Change the copy so that it computes and plots the exponential

exponential Fourier series we need to produce a stem plot. Each stem in the power spectrum is computed using $C_k C_k^*$ (see

Fourier series for the square-wave waveform with even symmetry (Section 7.4.1 in the textbook). *Hint*: Use the same definition

MATLAB:

C1 = Ck(1); % first harmonic Charm = Ck(2:length(Ck)); % remaining harmonics THD = 100 * sqrt(sum(Charm.*conj(Charm)))/sqrt(C1*conj(C1))

1. Complete the labwork self-assessment claim form and declaration. 2. As evidence of completion of Lab Exercise 9, you should upload ex9 1.mlx and ex9 2.mlx (can be sections in one

3. As evidence of completion of Lab Exercise 10, you should upload the Simulink models ex10 1.slx and ex10 2.slx.

Optional Additional Tasks: Review and Change the Code.

 $ex9_3$.

Preparation

We will also explore and confirm the stated results of even-, odd- and half-wave symmetries. **Download work files** Download the attached files:

Open the script trig_fseries.m as a MATLAB Live Script. Run the script and read through the results. Note that the script calls the TrigFourierSeries function, defined in the file TrigFourierSeries.m, which in turn calls the

Part 2 Save the m-file trig_fseries.m as a MATLAB Live Script ex9_1.mlx. Change the script so that it computes and plots the trig. Fourier series for the square-wave waveform with even symmetry (Section 7.4.1 in the textbook).

and plots the trig. Fourier series for the Triangular waveform (Section 7.4.3 in the textbook). Note Parts 2 and 3 can be added to trig_fseries and the whole submitted as a single Live Script file ex9.mlx providing that you use section headings to separate the parts and edit/add to the textual commentary to match the exercise descriptions.

Part 5

Part 6

d. Estimate the **Total Harmonic Distortion** in the signal THD% = $100 \frac{\sqrt{\sum_{k=2}^{N} |C_k|^2}}{\sqrt{|C_1|^2}}$ MATLAB:

As for Exercise 9, parts 7 and 8 can be added to exp_fseries and the whole submitted as a single Live Script file

Up to 2 marks can be claimed if you complete Exercise 9, 1 mark for Exercise 10 and an addition 2 marks Exercise 11. **Submission** You should submit the following to the Lab 05: Fourier series Assignment on Canvas.

Part 10 Examine the code that is defined in TrigFourierSeries. Note that it calls FourierSeries then computes ak and bk from the Ck coefficients. Why did I do that do you think?

Compute the FS of the half-wave rectified cosine function. Save the resulting calling script as ex11 4.

signals-and-systems-lab lab01 lab02 lab03

Use folder OneDrive\workspace\signals-and-systems-lab\lab05 for this lab. Before we start today's lab you will need to download and install the **Fourier series demo app**, that was demonstrated in

To install, visit the page and scroll down to find the Fourier Series Demo app (see image below) FourierSeriesDemo is a GUI that shows Fourier Series synthesis for different number

of Fourier coefficients. Different signals can be selected: square wave, sawtooth, triangle and rectified sinusoids.

Before you start